n [134	<pre>import pandas as pd import numpy as np import sympy as sp import math as m from sympy import collect, simplify, expand, fraction, latex, diff, cancel, nsimplify from IPython.display import display, Markdown, Math from scipy.integrate import odeint import matplotlib.pyplot as plt plt.rcParams['figure.figsize'] = [20, 10]</pre> class numden_coeff: definit(self, expr, symb):  all num_colf denum_r fraction(cypr)
	<pre>self.num, self.denum = fraction(expr) self.symb = symb self.common_factor = None self.lst_denum_coeff = self.build_lst(self.denum) self.lst_num_coeff = self.build_lst(self.num)  def build_lst(self, poly):     order = sp.Poly(poly, self.symb).degree()     lst = [expand(poly).coeff(self.symb**i) for i in range((order), 0, -1)]     lst.append(poly.subs(self.symb,0))     if (self.common_factor == None):         self.common_factor = lst[0]  lst = [simplify(lst[i]/self.common_factor) for i in range(order + 1)]     return lst</pre>
	<pre>def disp(self):     display(Markdown(r"Numerator coefficients (\beta)"), self.lst_num_coeff)     display(Markdown(r"Denominator coefficients (alpha)"), self.lst_denum_coeff)  Problem 1  a, b, p, e = sp.symbols("a b p e")</pre>
	zeta, omega, gamma_prime, gamma, theta1, theta2 = sp.symbols("zeta omega \\gamma^{\}\] gamma theta_1 theta_y, u, uc, ym = sp.symbols("y(t) u(t) u_{c}(t) y_m")    y_eq = sp.solve(sp.Eq(y*p**2, (-a*p*y + b*u)), y)[0]    u_eq = sp.solve(sp.Eq(u, (theta1*(y - uc) - theta2*p*y)), u)[0]    y_eq = sp.solve(sp.Eq(y, y_eq.subs(u, u_eq)), y)[0]    display(Math("y = "+latex(y_eq))) $y = -\frac{b\theta_1 u_c(t)}{ap + bp\theta_2 - b\theta_1 + p^2} $ the above equation is $y$ in which $-p\theta_2 y(t) - \theta_1 u_c(t) + \theta_1 y(t)$ has been subbed in for $u$
n [136	<pre>bm0, am1, am0 = sp.symbols("b_{m0} a_{m1} a_{m0}")  b_m0 = omega**2 a_m1 = 2*zeta*omega a_m0 = b_m0  # Bm = bm0 # Am = (p**2 + am1*p + bm0)  Bm = omega**2 Am = (p**2 + 2*zeta*omega*p + omega**2)</pre>
	$\begin{array}{l} {\rm Gm} = {\rm Bm/Am} \\ {\rm Gm} \\ {\rm display} \left( {\rm Math} \left( {\rm "G}_{\_} \{ {\rm m} \} \right. =  {\rm "+latex} \left( {\rm Gm} \right)  \right) \\ \\ G_m = \frac{\omega^2}{\omega^2 + 2\omega p\zeta + p^2} \\ {\rm Jext, the assumption \ that \ the \ plant \ } y \ {\rm will \ follow \ exactly \ the \ reference \ model \ } y_m \ {\rm is \ made \ to \ derive \ } \theta_1 \ {\rm and} \ \theta_2. \ {\rm This \ yeilds} \\ \\ {\rm num, \ den \ = \ fraction \ } (y_{\_} {\rm eq}) \\ \\ {\rm num\_m, \ den\_m \ = \ fraction \ } ({\rm Gm*uc}) \\ \\ \end{array}$
	theta_1 = sp.solve(sp.Eq(num, num_m), theta1)[0] theta_2 = sp.solve(sp.Eq(den.subs(theta1, theta_1), den_m), theta2)[0]      display(Math("\\theta_1 = \;"+latex(theta_1)))      display(Math("\\theta_2 = \;"+latex(theta_2))) $\theta_1 = -\frac{\omega^2}{b} $ $\theta_2 = \frac{-a + 2\omega\zeta}{b}$ Hent the somistivity of the error to $\theta_1$ and $\theta_2$ was derived. This will be used to derive equations for $\dot{\theta}_1$ and $\dot{\theta}_2$ . The somistivities $\frac{\partial e_1}{\partial \theta_2}$ and
	Next, the sensistivity of the error to $\theta_1$ and $\theta_2$ was derived. This will be used to derive equations for $\theta_1$ and $\theta_2$ . The sensitivities $\frac{\partial e}{\partial \theta_1}$ and the seen below
te	$\frac{\partial e}{\partial \theta_2} = \frac{b^2 p \theta_1 u_c(t)}{\left(-b\theta_1 + p^2 + p \left(a + b\theta_2\right)\right)^2}$ hese equations can be further simplified by deriving an equation for $u_c$ in terms of $y_m$ . This way, the sensistivitives can be expressed in erms of $y_m$ , a variable in which we have an equation. The equation for $u_c$ and the new equations for $\frac{\partial e}{\partial \theta_1}$ and $\frac{\partial e}{\partial \theta_2}$ in terms of $y_m$ can be even below $ u_c = \text{sp.solve}(\text{sp.Eq}(\text{ym}, \text{Gm*uc}), \text{uc})[0] $ $ \text{del}_e = \text{thetal\_subd} = \text{del}_e = \text{thetal.subs}([(\text{uc}, \text{u\_c}), (\text{thetal}, \text{theta\_1}), (\text{theta2}, \text{theta\_2})]) $
	$ \begin{aligned} & \text{del\_e\_theta2\_subd} = \text{del\_e\_theta2.subs}([(\text{uc}, \text{u\_c}), (\text{theta1}, \text{ theta\_1}), (\text{theta2}, \text{ theta\_2})]) \\ & \text{display}(\text{Math}("\text{u\_c} = \;"+\text{latex}(\text{u\_c}))) \\ & \text{display}(\text{Math}(") \setminus \text{frac}(\)) \\ & \text{display}(\text{Math}("\setminus \text{frac}(\))) \\ & \text{display}(\text{Math}("\setminus \text{frac}(\))) \\ & u_c = \frac{y_m \left(\omega^2 + 2\omega p \zeta + p^2\right)}{\omega^2} \\ & \frac{\partial e}{\partial \theta_1} = -\frac{bpy_m \left(2\omega \zeta + p\right)}{\omega^2 \left(\omega^2 + 2\omega p \zeta + p^2\right)} \\ & \frac{\partial e}{\partial \theta_1} = -\frac{bpy_m \left(2\omega \zeta + p\right)}{\omega^2 \left(\omega^2 + 2\omega p \zeta + p^2\right)} \\ & \frac{\partial e}{\partial \theta_1} = -\frac{bpy_m \left(2\omega \zeta + p\right)}{\omega^2 \left(\omega^2 + 2\omega p \zeta + p^2\right)} \end{aligned} $
[140	$\frac{\partial e}{\partial \theta_2} = -\frac{bpy_m}{\omega^2 + 2\omega p\zeta + p^2}$ Hext, equations for $th\dot{e}ta_1$ and $th\dot{e}ta_2$ were derived using the equation $\dot{\theta} = -\gamma' e \frac{\partial e}{\partial \theta}$ , the results of which can be seen below $\frac{\partial e}{\partial \theta_1} = -\frac{\partial e}{\partial \theta_1} = -\frac{\partial e}{\partial \theta_2} = -\frac{\partial e}{\partial \theta_1} = -\frac{\partial e}{\partial \theta_2} = -\frac{\partial e}{\partial \theta_2$
	$\dot{\theta}_2 = \frac{\gamma' bepy_m}{\omega^2 + 2\omega p \zeta + p^2}$ etting $\gamma = \gamma' b$ gives $\frac{1}{\omega^2 + 2\omega p \zeta + p^2}$ theta1_dot_subd = theta1_dot*gamma/(gamma_prime*b) theta2_dot_subd = theta2_dot*gamma/(gamma_prime*b) $\frac{1}{\omega^2 + 2\omega p \zeta + p^2}$ display(Math("\\dot{\\theta}_1 = \;"+latex(theta1_dot_subd))) display(Math("\\dot{\\theta}_2 = \;"+latex(theta2_dot_subd)))
	$ \dot{\theta}_1 = \frac{e \gamma p y_m \left(2 \omega \zeta + p\right)}{\omega^2 \left(\omega^2 + 2 \omega p \zeta + p^2\right)}  $ $ \dot{\theta}_2 = \frac{e \gamma p y_m}{\omega^2 + 2 \omega p \zeta + p^2}  $ $ \text{hese equations were develloped into ODEs in which the ODE solver could digest}  $ $ \text{obj\_theta1\_dot} = \text{numden\_coeff(theta1\_dot\_subd/ym, p)}  $ $ \text{obj\_theta2\_dot} = \text{numden\_coeff(theta2\_dot\_subd/ym, p)}  $ $ \text{atheta1} = \text{obj theta1 dot.lst denum coeff[::-1]}  $
	$ \begin{aligned} &\text{btheta1} = \text{obj\_theta1\_dot.lst\_num\_coeff[::-1]} \\ &\text{atheta2} = \text{obj\_theta2\_dot.lst\_num\_coeff[::-1]} \\ &\text{btheta2} = \text{obj\_theta2\_dot.lst\_num\_coeff[::-1]} \\ &\text{display(Math("\alpha\dot{\theta}_1 = ;"+latex(atheta1))} \\ &\text{display(Math("\alpha\dot{\theta}_1 = ;"+latex(btheta1))} \\ &\text{display(Math("\alpha\dot{\theta}_2 = ;"+latex(atheta2)))} \\ &\text{display(Math("\alpha\dot{\theta}_2 = ;"+latex(btheta2)))} \\ &\alpha\dot{\theta}_1 = \left[\omega^2,  2\omega\zeta,  1\right] \end{aligned} $
[143	$\begin{split} \beta\dot{\theta}_1 &= \left[0, \frac{2e\gamma\zeta}{\omega}, \frac{e\gamma}{\omega^2}\right] \\ \alpha\dot{\theta}_2 &= \left[\omega^2, 2\omega\zeta, 1\right] \\ \beta\dot{\theta}_2 &= \left[0,  e\gamma\right] \\ \\ \text{gamma\_val} &= 7.5 \\ \text{omega\_val} &= 1.5 \\ \text{zeta\_val} &= 0.6 \\ \\ \text{ym\_d, ym\_dd} &= \text{sp.symbols("} \\ \text{dot{y}\_{m}} \\ \text{thetald, thetaldd} &= \text{sp.symbols("} \\ \text{dot{heta}\_{1}} \\ \text{dot{heta}\_{1}} \\ \end{split}$
	theta2d, theta2dd = sp.symbols("\\dot{\\theta}_{2}\) \\dot{\\theta}_{2}\")  theta1_ddd = -atheta1[0]*theta1d - atheta1[1]*theta1dd + btheta1[1]*ym_d + btheta1[2]*ym_dd  theta2_ddd = -atheta2[0]*theta2d - atheta2[1]*theta2dd + btheta2[1]*ym_d  theta1_ddd_subd = theta1_ddd.subs([(gamma, gamma_val), (omega, omega_val), (zeta, zeta_val)])  theta2_ddd_subd = theta2_ddd.subs([(gamma, gamma_val), (omega, omega_val), (zeta, zeta_val)])  theta1_ddd_func = sp.lambdify([theta1d, theta1dd, ym_d, ym_dd, e], theta1_ddd_subd)  theta2_ddd_func = sp.lambdify([theta2d, theta2dd, ym_d, e], theta2_ddd_subd)  display(Math("\\dddot{\\theta}_1 = \;"+latex(theta1_ddd)+"\;=\;"+latex(theta1_ddd_subd)))  display(Math("\\dddot{\\theta}_1 = \;"+latex(theta2_ddd)+"\;=\;"+latex(theta2_ddd_subd)))
<b>F</b>	$ \ddot{\theta}_{1} = -2\ddot{\theta}_{1}\omega\zeta + \frac{\ddot{y}_{m}e\gamma}{\omega^{2}} - \dot{\theta}_{1}\omega^{2} + \frac{2\dot{y}_{m}e\gamma\zeta}{\omega} = -1.8\ddot{\theta}_{1} + 3.3333333333333333333333333333333333$
	<pre>y, y_dot = y0[2], y0[3] theta1, theta1_dot, theta1_dotdot = y0[4], y0[5], y0[6] theta2, theta2_dot, theta2_dotdot = y0[7], y0[8], y0[9] u = y0[10] u_c_ode = m.sin(m.pi*t/15) &gt;= 0  ym_dotdot = -2*omega*zeta*ym_dot - omega**2*ym + omega**2*u_c_ode y_dotdot = -(a + b*theta2)*y_dot + b*theta1*(y - u_c_ode) e = y_dot - ym_dot  theta1_dotdotdot = theta1_ddd_func(theta1_dot, theta1_dotdot, ym_dot, ym_dotdot, e) theta2_dotdotdot = theta2_ddd_func(theta2_dot, theta2_dotdot, ym_dot, e)  u = theta1*(y - u_c_ode) - theta2*y_dot</pre>
[145	<pre>return [ym_dot, ym_dotdot,</pre>
	<pre>gamma_val = 5 omega_val = 1.5 zeta_val = 0.6 a_val = 3 b_val = 1  # calculation of input signal t = [i for i in sample_range] u_c = np.ones(sample_depth) u_c[np.where([m.sin(t[i]*m.pi*T_val/15)&lt;=0 for i in sample_range])] = 0  y0 = [0]*11  ode_res = odeint(ode_solver, y0, t, args=(a_val, b_val, omega_val)</pre>
	<pre>omega_val,</pre>
	Error  0.0  -0.4
	-0.6 -0.8 -0.8 -0.8 Control Signal u
	2
F m b	Part 2.2 (Normalized MIT) or the noramlized MIT rule, the equation for theta needed to be updated. The equations derived for $\dot{\theta}_i$ are the sensistivity equations multiplied by $\gamma e$ therfore, the same procedure for building hte $\dot{\theta}_i$ equations can be reused by simply divinding everything by $\gamma e$ at the eggining. These new equations will keep the same names as before in the code as to not make many updates to the existing code. the nly difference will be setting the actual $\dot{\theta}_i$ equal to $\frac{\gamma\psi\frac{\partial e}{\partial \theta}}{\alpha+\psi^2}$ . Additionally, the fact that $\psi=-\frac{\partial e}{\partial \theta}$ will have to be taken into account. obj_theta1_dot = numden_coeff(theta1_dot_subd/(ym*e*gamma), p) obj_theta2_dot = numden_coeff(theta2_dot_subd/(ym*e*gamma), p)
	atheta1 = obj_theta1_dot.lst_denum_coeff[::-1] btheta1 = obj_theta1_dot.lst_num_coeff[::-1]
Т	$\begin{array}{l} \partial\theta_1 & [e^{i\gamma}, das, e^{i\gamma}] \\ \beta\frac{\partial e}{\partial\theta_1} = \left[0, \frac{2\zeta}{\omega}, \frac{1}{\omega^2}\right] \\ \alpha\frac{\partial e}{\partial\theta_2} = \left[\omega^2,  2\omega\zeta,  1\right] \\ \beta\frac{\partial e}{\partial\theta_2} = \left[0,  1\right] \\ \text{the below equations are named $\theta_i$ simply becasue the code template derived above was reused to minimise the updates needed to the ode. These equations are actually for \frac{\partial e}{\partial\theta_i}$
[147	<pre>gamma_val = 7.5 omega_val = 1.5 zeta_val = 0.6  ym_d, ym_dd = sp.symbols("\\dot{y}_{m} \\ddot{y}_{m}") thetald, thetaldd = sp.symbols("\\dot{\\theta}_{1} \\ddot{\\theta}_{2}")  theta2d, theta2dd = sp.symbols("\\dot{\\theta}_{2} \\ddot{\\theta}_{2}")  theta1_ddd = atheta1[0]*theta1d + atheta1[1]*theta1dd + btheta1[1]*ym_d + btheta1[2]*ym_dd theta2_ddd = atheta2[0]*theta2d + atheta2[1]*theta2dd + btheta2[1]*ym_d  theta1_ddd_subd = theta1_ddd.subs([(gamma, gamma_val), (omega, omega_val), (zeta, zeta_val)])</pre>
[148	<pre>theta2_ddd_subd = theta2_ddd.subs([(gamma, gamma_val), (omega,omega_val), (zeta, zeta_val)]) theta1_ddd_func = sp.lambdify([theta1d, theta1dd, ym_d, ym_dd], theta1_ddd_subd) theta2_ddd_func = sp.lambdify([theta2d, theta2dd, ym_d], theta2_ddd_subd)  def ode_solver(y0, t, a, b, omega, zeta, gamma, alpha):  ym, ym_dot = y0[0], y0[1] y, y_dot = y0[2], y0[3] theta1, theta1_dot, theta1_dotdot = y0[4], y0[5], y0[6] theta2, theta2_dot, theta2_dotdot = y0[7], y0[8], y0[9] theta1_norm = y0[10] theta2_norm = y0[11]</pre>
	<pre>u = y0[12] u_c_ode = m.sin(m.pi*t/15) &gt;= 0  ym_dotdot = -2*omega*zeta*ym_dot - omega**2*ym + omega**2*u_c_ode y_dotdot = -(a + b*theta2_norm)*y_dot + b*theta1_norm*(y - u_c_ode) e = y_dot - ym_dot  theta1_dotdotdot = theta1_ddd_func(theta1_dot, theta1_dotdot, ym_dot, ym_dot) theta2_dotdotdot = theta2_ddd_func(theta2_dot, theta2_dotdot, ym_dot)  theta1_n = theta1*e*gamma/(alpha + (theta1)**2) theta2_n = theta2*e*gamma/(alpha + (theta2)**2)  u = theta1_norm*(y - u_c_ode) - theta2_norm*y_dot</pre>
[149	<pre>return [ym_dot, ym_dotdot,</pre>
	<pre>alpha_val = 1 gamma_val = 5 omega_val = 1.5 zeta_val = 0.6 a_val = 3 b_val = 1  # calculation of input signal t = [i for i in sample_range] u_c = np.ones(sample_depth) u_c[np.where([m.sin(t[i]*m.pi*T_val/15)&lt;=0 for i in sample_range])] = 0  y0 = [0]*13</pre>
	<pre>ode_res = odeint(ode_solver, y0, t, args=(a_val, b_val,</pre>
	plt.plot(t, ode_res[:,12]) plt.grid() plt.show()  Error  06  04  02
	-0.2 -0.4 -0.6
	Control Signal u
	15
F	Problem 2 Part 1 irst, an equation for $y$ was derived in terms of $u_c$ . This was done by subbing $u=\theta_1u_c-\theta_2y$ into $y=\frac{bu}{p}$ . This yeilds
1 [150	<pre>y, u, uc, ym, e = sp.symbols("y(t) u(t) u_{c}(t) y_m e") alpha, beta, gamma, b, theta1, theta2, p = sp.symbols("alpha beta gamma b theta_1 theta_2 p")  V1 = 0.5*e**2 V2 = 1/(b*gamma*2)*(alpha - b*theta2)**2 V3 = 1/(b*gamma*2)*(beta - b*theta1)**2 V = V1 + V2 + V3  y_eq = b*u/p u_eq = theta1*uc - theta2*y  y_eq = sp.solve(sp.Eq(y,y_eq.subs(u, u_eq)),y)[0] display(Math("y = "+latex(y_eq)))</pre>
N [151	$y=rac{b heta_1u_c(t)}{b heta_2+p}$ Next, an equation for $y_m$ was derived from $G_m$ . This giave $y_m=0$ beta $y_m=0$ and $y_m=0$ and $y_m=0$ beta $y_m=0$ and $y_m=0$ and $y_m=0$ beta beta $y_m=0$ beta $y_$
N	display (Math ("y_{m}) = "+latex (ym_eq))) $y_m = \frac{\beta u_c(t)}{\alpha + p}$ Much like in question 1, the true values in terms of process/model parameters were derived for $\theta_1$ and $\theta_2$ . This was done by equating the umerators and denominators of $y$ and $y_m$ . This gave $\begin{aligned} \text{num, den = fraction}(y_eq) \\ \text{num, den = fraction}(y_eq) \\ \text{num, den = fraction}(y_eq) \\ \text{theta}_1 = \text{sp.solve}(\text{sp.Eq}(\text{num, num}_m), \text{ theta}_1)[0] \end{aligned}$
А	theta_2 = sp.solve(sp.Eq(den, den_m), theta2)[0] $ \frac{display(Math(") \cdot (heta_1 = ; "+latex(theta_1)))}{display(Math(") \cdot (heta_2 = ; "+latex(theta_2)))} $ $ \theta_1 = \frac{\beta}{b} $ $ \theta_2 = \frac{\alpha}{b} $ is sensitivity equations was derived for $\dot{e}$ . This was done with the equation $\dot{e} = \dot{y} - \dot{y}_m$ . The resulting equation was further manipluated by adding and subtracting $\alpha y$ to have an error term $(e)$ in the equation
[153	<pre>y, u, uc, ym = sp.symbols("y(t) u(t) u_{c}(t) y_m") alpha, beta, b, theta1, theta2, p = sp.symbols("alpha beta b theta_1 theta_2 p")  y_dot = b*u_eq ym_dot = -alpha*ym + beta*uc e_dot = collect(expand(y_dot - ym_dot), y) e_dot_poly = sp.Poly(e_dot, [y,uc]) e_dot_poly_subd = e_dot_poly.as_expr().subs([(theta1, theta_1), (theta2, theta_2)])  e_dot_alt = uc*(b*theta1 - beta) - b*theta2*y - e + alpha*y e_dot_alt_poly = sp.Poly(e_dot_alt, [e, theta1, theta2])</pre>
	$ \begin{aligned} & \text{V\_subd} = \text{V.subs}([(e,0), (\text{theta1}, \text{theta\_1}), (\text{theta2}, \text{theta\_2})])} \\ & \text{display}(\text{Math}("\\text{\ensuremath{"}}\ \text{\ensuremath{"}}\ \ensuremath$
y S	ubing in $\theta_1$ and $\theta_2$ into $\dot{e}$ gives $\dot{e}=-\alpha y(t)+\alpha y_m$ . Therefore, if the error is to go to 0, and $\theta_1$ and $\theta_2$ converge to their true values, the must converge to $y_m$ ubing these results into the equation provided in the assingment document gives $T(e)=0.5e^2+\frac{(\alpha-b\theta_2)^2}{2b\gamma}+\frac{(-b\theta_1+\beta)^2}{2b\gamma}=0$ herefore, the first condition for the lyapunov function is satisfied (i.e. V = 0 at the equilibrium point) $ = \frac{1}{2} \left( $
	$ \begin{split} & \text{V\_dot} = \text{nsimplify}(\text{diff}(\text{V1, e})) * \text{eDot} + \text{ diff}(\text{V2,theta2}) * \text{theta2Dot} + \text{ diff}(\text{V3,theta1}) * \text{theta1Dot} \\ & \text{V\_dot\_subd} = \text{V\_dot\_subs}([(\text{eDot, e\_dot\_alt})]) \\ & \text{V\_dot\_subd\_alt} = \text{V\_dot\_subs}([(\text{eDot, e\_dot\_alt}), (\text{theta1, theta\_1}), (\text{theta2, theta\_2})]) \\ & \text{V\_dot\_subd\_poly} = \text{sp.Poly}(\text{V\_dot\_subd, [theta1Dot, theta2Dot, y, uc]}) \\ & \text{display}(\text{Math}("\\text{\dot}\{\text{V}\}(\text{e}) = \;"+\text{latex}(\text{V\_dot}))) \\ & \text{display}(\text{Math}("\\text{\dot}\{\text{V}\}(\text{e}) = \;"+\text{latex}(\text{V\_dot\_subd\_poly.as\_expr}()))) \\ & \\ & \dot{V}(e) = -\frac{\dot{\theta}_1(-b\theta_1 + \beta)}{\gamma} - \frac{\dot{\theta}_2(\alpha - b\theta_2)}{\gamma} + \dot{e}e \end{split} $
S V	$\dot{V}(e) = \frac{\dot{\theta}_1 \left(b\theta_1 - \beta\right)}{\gamma} + \frac{\dot{\theta}_2 \left(-\alpha + b\theta_2\right)}{\gamma} - e^2 + u_c(t) \left(be\theta_1 - \beta e\right) + y(t) \left(\alpha e - be\theta_2\right)$ $\text{ubbing the true values for } \theta_1 \text{ and } \theta_2 \text{ into } \dot{V}(e) \text{ gives}$ $\dot{V}(e) = -e^2$ $\text{Which means that } \dot{V}(e) \text{ is decreasing thus satisfying Lyanupov's second criteria.}$ $\text{Derivation of Control Parameters}$ $\text{lst\_coeffs} = \text{V\_dot\_subd\_poly.coeffs()} \\ \text{equ } 1 = \text{lst\_coeffs[0]*thetalDot} + \text{lst\_coeffs[3]*uc}$
$\frac{\dot{\theta}}{-}$	equ_1 = 1st_coeffs[0]*theta1Dot + 1st_coeffs[3]*uc equ_2 = 1st_coeffs[1]*theta2Dot + 1st_coeffs[2]*y    theta1_dot = sp.solve(sp.Eq(equ_1, 0), theta1Dot)[0]   theta2_dot = sp.solve(sp.Eq(equ_2, 0), theta2Dot)[0]    the equations for updating the control parameters can be obtained from $\frac{\partial}{\partial t} (b\theta_1 - \beta) + u_c(t)(be\theta_1 - \beta e) = 0$ $\frac{\partial}{\partial t} (b\theta_1 - \beta) + u_c(t)(be\theta_1 - \beta e) = 0$
<u>.</u> =	and $rac{\dot{ heta}_2\left(-lpha+b heta_2 ight)}{\gamma}+y(t)\left(lpha e-be heta_2 ight)=0$ $\Rightarrow \ \dot{ heta}_2=e\gamma y(t)$ For $\gamma=0.2$
[156	<pre>T = 0.01 sample_depth = int(100/T) # 1000 samples totalling 100 seconds (since sample time T is 0.1 secons) sample_range = range(sample_depth)  t = [i for i in sample_range] uc = np.ones(sample_depth) uc[np.where([m.sin(t[i]*m.pi*T/15)&lt;=0 for i in sample_range])] = 0  # actual parameters b = 2 beta = 1 alpha = 1</pre>
	<pre>gamma = 1 gamma = 0.2  y = [0] ym = [0] u = [0] e = 0  theta_1 = [0] theta_2 = [0]  for i in range(sample_depth):     theta_1.append(theta_1[i] - T*e*gamma*uc[i])     theta_2.append(theta_2[i] + T*e*gamma*y[i])  y.append(y[i] + T*b*(theta_1[-1]*uc[i] - theta_2[-1]*y[i]))</pre>
	<pre>y.append(y[i] + T*b*(theta_1[-1]*uc[i] - theta_2[-1]*y[i])) ym.append(ym[i] + T*(-alpha*ym[i] + beta*uc[i]))  e = y[i] - ym[i] y.pop(-1) theta_1.pop(-1) theta_2.pop(-1)  plt.title("y vs. u_c", fontsize=20) plt.plot(t,uc) plt.plot(t,y) plt.show()  plt.title("Theta_1 and Theta_2", fontsize=20) plt.plot(t, theta_1)</pre>
	14 - 12 - 10 - 08 - 06 - 06 - 06 - 0 - 0 - 0 - 0 - 0 - 0
	0.4 - 0.2 - 0.0 -
t[156]:	<pre><matplotlib.legend.legend 0x1beccc8f0d0="" at=""></matplotlib.legend.legend></pre>
t[156]:	<pre><matplotlib.legend.legend 0x1beccc8f0d0="" at=""></matplotlib.legend.legend></pre>
	<pre>Theta_1 and Theta_2</pre> The
	<pre>cmatplotlib.legend.Legend at 0xlbeccc8f0d0&gt;</pre> Theta_1 and Theta_2  0.3  0.1  0.0  0.0  0.0  0.0  0.0  0.0
F	For $\gamma=1$ The sample_depth = int.(100/T) \( \frac{1}{1000 \ samples totalling 100 \ seconds \( (since \ sample time T is 0.1 \ secons) \) sample_trange = range (sample_depth)  t = [i for i in sample_range] \( uc = np.ones (sample_depth) \)  uc [np.where([m.sin(t[i]*m.pi*T/15)<=0 for i in sample_range])] = 0  f actual parameters  b = 2  beta = 1 alpha = 1
F	Theta_l and Theta_2  Theta_l and Theta_l and Theta_2  Theta_l and Theta_l and Theta_2  Theta_l and Theta_l a

