# Term Paper

For Research Directions

University of Nebraska at Omaha

by

Chad Crowe

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Supervisor

Dr. Hall

#### 0.1 Abstract

Existing machine learning models performs well on single data types. Yet, there is little research on machine learning with multiple data types. From the existing research on multiple data types, these treat each data type and their features as independent. This paper proposed that each data type is not independent, i.e. when modeling a single phenomenon with multiple data types, correlations exist between the data type features. This paper proposes that some model information is only captured by combining features from each data type. In light of existing research that acknowledges how combining data types into a model only learn single-data type features, this paper proposes a methodology for improving model performance with multiple data types. Specifically, this paper proposes using boosting with combined Convolutional Neural Networks (CNNs) to generate weak DNN models to improve performance when used in ensemble with existing single-data type models.

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#### **Problem**

There is a growing problem within many IT fields. IT is experiencing a massive growth in data. This data is large, diverse, and differently structured. The massive amount of diverse and unstructured data provides a problem in both processing and understanding this data. This data is complicated and might contain more than plain text data. The data very well could contain text and images. The ability to understand and process this data can be important to researcher's within this growing field. While there exist tools that can process text data, or which process image data, there are a lack of effective methods for analyzing text and image data. The field finds itself fast growing and with a multitude of data without a good way to extract useable knowledge from that data.

## Overview of the Topic

The existing methodology for analyzing multi-data type datasets is to analyze each data type separately. Current practice has seen a massive amount of success analyzing individual data types. It is assumed that analyzing each data type separately will perform well enough for the vast majority of use cases. While the assumption is true, there are many cases where increased model performance can improve knowledge on important datasets. Also, multi-data type datasets are fairly new. It is likely too early for practitioners and researchers to conclude that single-data type analysis is sufficient for most use-cases. The field of machine learning research is constantly improving, and this paper makes strides to add to the growing field's knowledge.

Existing research on multi-data type datasets have almost exclusively used autoencoders because of their ability to represent complex data. Yet, these models have problems. They tend to learn single data type features and, in the end, perform worse than their single-data type model counterparts. The lack of performance by autoencoders on multi-data type features provides opportunity for improving modeling

multi-data type features.

Within this area are many types of datasets. There are datasets with many types of data, yet, images and text data are very common types of data in datasets. This paper applies the tools and knowledge of applied machine learning to datasets containing both text and image data. Yet, before speaking about solving this problem, it is worth talking about general principles when modeling any dataset.

Most deep learning models consist of nodes and layers. The node and layer architecture provide flexible methods for learning and memorizing new data. Extra layers provide opportunity for models to continue extracting data. The combination of nodes and layers allow for different machine learning architectures. Recent research has expanded upon nodes and layers to create more advanced architectures. Some of these architectures have been labeled as deep, denoting the many layers they contain. Other advances connect nodes in new ways, like connecting nodes to previous layers as with Recurrent Neural Networks (RNNs). Each architecture and configuration have different benefits and learns data differently. Some of these architectures will be more deeply covered in subsequent sections.

It is worth a quicker dive into the basic mechanics of machine learning models. Machine learning models take inputs. These inputs are transformed by models into outputs. There are many manipulations on the data while it passes through the models. The outputs depend on the type of machine learning. Two common tasks within machine learning are classification and regression. Classification models tend to output a probability for each classification through the final layer. How the input is manipulated depends on the type of machine learning model. One common type of

machine learning model is an Artificial Neural Network (ANNs), which apply simple functions to the inputs, such as a signoid, Relu, or tanh function. The model is generally composed of a few layers, where each node is connected to each node in its subsequent layer. The network's input weights, for each layer are adjusted based on the model's error. The Convolutional Neural Network (CNNs) is similar. The CNN is also composed of nodes. Half of the CNN learning is the same as ANNs, i.e. nodes connect to one another and go through a simple learning function like Relu. The difference with CNNs is how the layers are connected. Instead of connecting all layers together, CNNs split the data up into regional chunks, e.g. the upper right array of data. The region of datas are connected. One intersting behavior from the CNN is that region sizes are halved and joined. In this way, regional behavior is captured and joined together in the output. Another major type of machine learning model is a current Neural Network (RNNs). RNNs are very similar to ANNs, except their layers are connected differently. The RNNs layers do not always connect to the next layer, i.e. the layer's output may serve as input to a previous/the same layer. This provides a cycle of input output information within the neural network. This allows each layer to have some input from future layers, which creates a sense of network memory, where previous data serves as input to the network's current behavior.

Machine learning models are often applied in particular ways. For example, CNNs are often applied to images because they learn regional data well. NN are often applied to text data because they are simple and can memorize the word distributions for languages. RNNs are often applied to videos because they can remember data from past inputs. As will be covered more below, each of these simple models is

regularly applied to single data types. Applying these models to multiple data types will be covered in the related work and later sections.

There are many major threads under development in the arena of applied machine learning. These pertain to machine learning with each type of data. Examples of popular data types are images and text. These data types are popular because they are commonly available. Such data are available in public repositories of data or through application APIs, such as text and image data that is available from utilizing the Twitter API. Each data type has multiple facets. More interestingly, certain machine learning algorithms perform better and differently for particular data types. Neural Networks (NNs) perform very well on simple text learning tasks, yet struggle to learn image data. Convolutional Neural Networks (CNNs) may underperform with text-analysis, but have excelled at image-analysis. Analysis with sequences tends to use Long-Term Short Memory nodes (LSTMs) because the model incorporates sequence memory.

While there are many techniques for analyzing different types of data, society and academia has seen an increase in the amount of available data. Moreover, not all data is the same. There are many types of text data. A researcher can analyze text data from Twitter, which looks different than text data from a research paper, which also looks different from text data translated from audio data. The different data types and variations within data types are a challenge for researchers. The creation of theories about Twitter text data represents advances in our knowledge of social media. Creating models that are better at understanding text data that is created from audible speech can further research's understanding of text sentence structure.

These examples only illustrate that there are many ways to approach each data type, and each data type provides many ways to explore and understand its data.

When providing new machine learning insights, whether it be theories or achitectures, those theories need to be validated. It is very common for papers to cite benchmark models on publically available data as a reference point for model performance. There are many such benchmarks within the field of applied machine learning. Many of these benchmarks are the performance of well-tuned machine learning algorithms on a given set of data. Though this paper will not create a model and apply it to a benchmark, it will cite potential benchmarks for new papers or models implementing the theories presented.

## Paper Overview

The paper focuses on a methodology for training a combined model. This methodology is a natural conclusion based on the related work. The paper begins in the next section with the related work. The related work will begin describing current practice when modeling single data types. The related work will discuss why single data types tend to be treated independently. The main thrust of this reason is that particular architectures tend to perform better at modeling each data type. In light of data-type specific architectures, the related work can explain the lack of research and success at modeling multiple-type datasets.

The paper will then begin explaining existing work on mutli-type datasets. Most of this work concerns generative models, and so provide no methodology for classification or regression with multi-type datasets. Yet, these related work provide an important lesson. The works delineate that when training a generative model with multiple data types, that the models tend to only learn single data type features. Such single data type learning occurs because the features are stronger. Also, in

cases where the output type is of one type, the feedback encourages learning features whose type matches the output.

With this knowledge, it is worth exploring ways to train multi-type models, while preventing single-data type learning. The next section of the related work will discuss LSTMs because of their use with multiple data types and their ability to learn data transformations. Since LSTMs have been considered as a way to translate between data types, they are worth mentioning here. Other methods for training models on multiple data types will also be considered, such as Convolutional Neural Networks (CNNs) with videos and methods to translate images and videos into text.

Having finished the related work, the paper will reiterate the problem. Given a problem that needs solving, the research will propose a general solution and discuss an overview of possible implications for stakeholders, i.e. the field and the general public. The next section will discuss existing theories that gave rise to the ideas in this paper. Finally, the paper will describe its methodology. The last section of the methodology will describe how the research will be evaluated both qualitatively and quantitatively.

## Related Work

#### 4.0.0.1 Single Data Type Architectures

One paper my Simonyan and Zisserman explore very deep CNNs on large-scale image recognition. The authors found that the trick to having deep CNNs is to have small filters. The authors had 3x3 CNN filters with 16-19 layers and their model are two of the best performing convnets publically available. The authors performed no fine-tuning and fed their model fixed-size 224x224 RGB images. The only preprocessing done is subtracting the mean RGB value computed on the training set from each pixel so that the pixel intensity values tend to fall in a semi-normal distribution around zero. Surpisingly, the stride is kept at one, which is common in practice but requires more time for training. Spatial pooling ocurs five times, which follow the conv layers, though sometimes the model has multiple conv layers before the data is pooled. Maxpooling is performed on a small 2x2 window with a stride of 2, which likely saves a lot of model training time. The authors used a ReLU on all layers and none of the layers

contain Local Response Normalization (LRN), as such normalization only leads to great memory consumption and computation time. The benefit to the many small filters is that the number of weights in the convnet is not greater than that of a shallow net with larger convnet layers. The model utilized a mini-batch of 256 with momentum set to 0.9, which is a common pattern in many of these papers. The model did include L2 normalization with the multiplier set to 5\*10-4. A dropout of 0.5 was used, which seems very large compared with most papers, which probably use 0.3. The learning rate is initially set to 0.1 and decreased by a factor of 10 when the validation set accuracy stopped improving. A common theme in the related work is a large learning rate to initialize weights, which then dramatically decrease for small performance increases. The authors obtains fixed-size 224x224 convnet images by randomly cropping and rescaling training images. The crops also underwent random horizontal flipping and random RGB color shifts. The authors emphasized that using a large set of crops can lead to an improved accuracy. The training time took 2-3 weeks and training with 1000 classes on 1.3M images, and tested on 100k images, and validated on 50k images.

Ji Lee performs sequential short-text classification with ANNs. The author's point is that text classifications often occur by only considering a text, not necessarily its preceding or subsequent texts. The paper proposes that using information preceding short texts may improve classification accuracy. Their model initially generates vector representations for short-texts using either the RNN or CNN architectures. The authors utilized early stopping after 10 epochs and performed hyperparameter training. Their model serves as a benchmark for ANN performance to sequential

short-text classification.

Shen et. al explores attention mechanisms for machine learning. The subject of attention mechanisms is not well known within machine learning. It has recently attracted a large amount of attention, due it its performance and speed of computation. Since attention mechanisms are more lightweight, they train faster. The mechanism, as will be explained, still relies on nodes, and therefore has much of the flexibility of neural networks. Shen et. al delve into a type of attention mechanisms, a recurrent attention and bi-way attention mechanisms denoted as a Directional Self-Attention Network (DiSAN). The paper shows that its DiSAN model outperforms complicated RNN models in prediction accuracy and time efficiency on existing benchmarks. The paper is relevant because it presents another, quite new machine learning mechanism that has shown promise for applied machine learning.

The attention mechanism takes advantage of a hidden neural network layer. The hidden layer works on the input sequence and predicts the importance of their weights. This creates a mechanism where neural network inputs are scrutinized by a separate neural network. The separate neural network determines the importance of the weights, and give credence to those weights, so that the model primarily uses the most important inputs. The result is a categorical distribution for the input sequence, and the neural network nodes have memory of which input sequences are important or more relevant. One disadvantage of these networks is that temporal order of input information is lost. The paper's DiSAN model helps fix this by providing sequential memory for the attention networks. The paper demonstrates that their attention mechanism models perform particularly well at alignment scores between two sources,

i.e. does well at providing a similarity score between two sources or texts.

There are a few jewels in the Shen et. al paper, like how an additive function for attention often outperforms multiplicative attention, and is also more memory efficient. Their models make us of cross-entropy as an optimization objective and include L2 regularization. The minimization optimizer is Adadelta with mini-batch of size 64. The initial learning rate is quite large, i.e. 0.5, which is decreased over epochs. The weight matrices for networks use GloVe and are pre-trained with out of vocabularty words, which initially were randomely initialized from a uniform distribution. The model uses a dropout of 0.25 and 0.2. The dropout is also varied throughout the learning process. The final model uses fewer parameters than either RNN or CNN networks by margins of 3%. The model is applied to the Standford Sentiment Treebank and performs better than the best existing model by 0.52%. The model is also applied to Sentences Involving Compositional Knowledge (SICK) and with a similar performance. Of important note is the model's bi-directional ability to track different features in forward progressing layers than a backward focused layer, one picking up word families and the latter focusing on word carousel.

Ji et al. presents another method for recognizing human action with CNNs. The topic is particularly interesting because it represents a model that translates between very different data types. The approach is simple and uses a CNN to predict actions at the frame level. Another CNN then takes inputs from contiguous frames via their location. The end-result is a 3D CNN that combines each 2D frame and uses time as the third dimension. The hope is that the CNN models will capture temporal information from the adjacent frames. This seems like a very good method

to represent the data with very little bias. The model outperformed 2D CNNs, which seems sensible since the 3D model contains the 2D model plus more information.

Wenpeng et al perform a comparative study between CNN and RNN for Natural Langauge Processing (NLP). This is an interseting subject, since RNNs and CNNs differently model sentences. RNNs capture units in sequence and CNNs are good at extracting positional invariant features. Both CNNs and RNNS are also the primary types of DNNs. The paper covers multiple NLP tasks with each type of network, specifically CNNs, Gated Recurrent Units (GRUs), and LSTMs. It is wroth mentioning that the networks in the study did not obtain great performance on existing benchmarks, which may limit the value of the study's insights. The NLP tasks are sentiment/relation classification, textual entailment, answer selection, questionrelation matching, and part-of-speech tagging. The authors found that both CNNs and RNNS provide complementary information on text classification tasks. The authors also found that changing hidden layer sizes and batch sizes resulted in large performance fluctuations. A related work in the study found that RNNs compute a weighted sum of n-grams while CNNs extract the most important n-grams and only consider their resulting activation.

There were a few papers on deep learning with video data. One interesting paper performed deep learning by using CNNs on mulitple frames. This paper was by Hossein Mobahi. The paper performs large-scale object recognition. Videos are composed of multiple frames, which provides a number of frames which contain the same objects. These similar frames can each be processed by a CNN to provide additional information and possibly better accuracy in object recognition. The paper learns the

objects, based on the frame-to-frame video motion by performing classification on each frame. The authors see learning from multiple frames more related to evolution, as humans experience learning through the world, which is constantly moving and changing. The paper made use of 72x72 sized images of 100 images, where each object was shot 100 times at angles that each differed by 5 degrees.

#### 4.0.0.2 RNNs

Building on the topic of LSTMs within video representations, since many of these interact with both image and motion data. Srivastava et al. created an unsupervised model for learning on video data with LSTMs with the ultimate goal of action recognition. They cite one challenge as tracking multiple objects moving in a background. The paper said that LSTM was useful at extracting and extrapolating motion beyond what the video observed, though that metric seems difficult to measure in terms of goodness or performance. The authors also took the approach of skip-gram models of trying to predict in-between frames to train their model. The final model predicted up to 13 frames in the future and took 20 hours to converge on only 300 hours of data. The resulting predictions and reconstructions were blurry. The blurriness was fixed by adding more LSTM units to remember image data. They faced the issue of LSTM and their gradients vanishing. Despite this, they had 74.3% accuracy on recognizing actions from video data, which seems respectible. The authors found that the model often loss the ability to keep precise object features in future frames, though it could recreate long-term object motion.

Alex Graves at Toronto persents a paper on predicting future handwriting using LSTMs. The resulting system was able to generate highly realistic cursive handwriting in a wide variety of styles. The topic is interesting because it is an example of using a different machine learning architecture to translate data from video to another format, i.e. predicted handwriting sequences. The topic of translating data to a type of prediction is interesting for the term paper's topic. Existing work has used LSTMs to generate future sequences in domains like music. RNNs are nice because they are fuzzy in the sense that they do not use exact templates from the training data to make predictions but use internal representations to interpolate from the training data to a result. This RNN reconstitution of training data is an interesting way to transform data from one type to another. It might be interesting to use RNNs as a translator from one data format to another, then use that representation to train another machine learning model. The paper builds on this principle and finds that a better data type translation occurs when the LSTMs are given longer memories. The model uses skip connections to all input layers, which does not connect top RNN layers to bottom RNN layers, assuming that these connections are likely unrelated and unhelpful to the final model. The paper also constrained its gradients to a smaller range to prevent large derivatives in the backpropagation. The authors also found that retraining with iteratively increased regularization results in faster training than random weights with regularization. This makes sense, since the initial weights are likely better than random weights. Their network only took four epochs to converge. It is good to know that LSTMs can converge so quickly.

Building on learning data type representations, Cho et al. builds upon phrase

representations using RNN encode-decoders with the purpose of language modeling. The authors use two RNNs as an encoder-decoder pair. There is definitely an emerging trend in the related work where RNNs are used to create internal data representations for encoding data to another data type. The model translates from English to French and learns the translation probability of an English phrase corresponding to a French phrase. The model can conversly be used to score a given pair of input and output sequences. The authors also acknowledged that simply training statistical models do not necessarily lead to the optimal performance.

Wojciech Zaremba explores RNN regularization. Dropout is the most successful technique for regularizing neural networks, but they do not work well with RNNS and Long Short-Term Memory units (LSTMs). Dropout works by randomly dropping outputs on a certain percentage of nodes. Dropout is used as a form of regularization to make networks more generic and stable on new inputs. Being able to apply regularization to RNNs or LSTMs could make video deep learning much more performant. Due to lack of regularization effectiveness in RNNs, RNNs tend to quickly overfit on large networks. The author's trick is to apply the dropout operator only to the non-recurrent connections. The final model uses minibatch of size 20 with 650 units per layer of the LSTM.

#### 4.0.0.3 Architectures Will Multiple Data Types

Karen et al. proposes a unique use of combining CNNs for action recognition in videos. The goal is to capture complementary information from still frames and their motion. The recognition of human actions in video is well researched. This

paper builds upon existing works by creating a new architecture for analyzing human actions by combining an image-based model and a movement-based model, e.g. one model tracks the still images and the other tracks the gradient of movement in those images. In this way, the paper presents a technique to combine two different data types into a single CNN model. The overall idea is the motion and still-frame data types are very different. Also, actions often contain motion. The action motion can aid to the identification of the action. The CNNs are separately trained and later combined via their softmax scores. The paper does some interesting calculations for the motion in order to account for a moving camera by subtracting movement that exists across the entire frame. The CNNs do max-pooling with a 3x3 window and a stride of 2, which seemed practically too large. The images were 224x224 and randomely cropped, horizontally flipped, and underwent RGB jittering. The authors found that such fine-tuning only gave marginal improvements over the training set. The paper also saw that large dropout over-regularises learning and leads to a worse overall accuracy.

Translating images to videos is a popular topic. It is particularly interesting because it performs translation from one data type to another. Donahue et al presents a model transcribing video to text descriptions. The paper proposes an architecture known as Long-term Recurrent Convolutional Networks (LRCNs). The goal of the architecture is to levarage CNN recognition strengths and to have an RNN remember time-varying inputs and outputs. One of the largest difficulties with the model is deciding how much time-varying information to remember, which were not deterministic in this model due to their issue of the vanishing gradient in their RNN model.

The authors see their model as an improvement on video activity datasets with complex time dynamics and improve existing benchamrks by 4%. The LRCN predicts the video class at each time step and average the predictions for a final classification. The model extracts from 16 frame clips and uses a stride of 8 frames from each video. The model is trained on TACoS, a dataset for video/sentence pairs.

Graves from Google researched speech recognition with RNNs. The paper presents a system to transcribe audio data to text. The paper is novel because it performs transcription without a phonetic representation. The model uses a bidirectional LSTM RNN architecture. Current practice working from audio to text data comprises speaker normalization and vocal tract length normalization. The normalized voice is then fed into a model. The extra step of normalization of voices makes the model bad at dealing with outlier voices, such as the elderly. By having the model directly transcript the audio data, the model can overcome the difficulties of odd voice tracts. There are papers by Graves that perform raw speech with RNNs and Restricted Boltzman Machines (RBMs), but the model is expensive and tends to be worse than conventional processing. A previous work did speech recognition with this architecture (Eybern et al., 2009), but it used a shallow architecture and did not deliver compelling results. An advantage of this research is its use of bidirectional RNNs to capture the whole utterances and their context. This is possibly useful in the core research proposed by the term paper as a method for analyzing the entire context of speech data.

### Area within IT

The area of interest within IT is applied machine learning on multi-data type datasets. Applied machine learning is a popular field within IT and operates on many datasets. One type of dataset within the field is multi-data type datasets. These are datasets whose input data have multiple types, e.g. a dataset that contains both image and text data. An example of such a dataset might be X-Ray data and a list of patient symptoms. The mix of multiple data types makes the problem more complex. Also, these datasets are important, but have received less attention by researchers, partly due to their complexity. There are opportunities for new methods and theories for analyzing multi-data type datasets. This makes the area within IT an interesting field for new research.

## Topic

#### 6.0.1 What is known about this topic?

Little has been invested creating benchmarks on multi-data type datasets. Rather, researchers have moved straight to using auto-encoders because of their ability to handle complex data.

While the use of auto-encoders and Restricted Boltzmann Machines (RBMs) have justification, these are limited in their application. Auto-encoders and RBMs are generative models and are not used for classification or regression problems. This leaves a gap for analyzing multi-data type datasets for the purpose of regression and classification.

There is existing research on multi-data type datasets. As previously mentioned, these analyze each data type separately. The benefit of this existing research is that benchmarks exist for performance and training time. This provides a reference point for the model methodology proposed by this paper to be compared against.

#### 6.0.2 What needs to be known?

Research in multi-data types have assumed that LSTMs and autoencoders work well at processing combined inputs. Yet, this has not been shown to be true. Rather, research by Ngiam et al. found that RBMs tended to not learn combined representations because the single data type signals were strong enough to control the network weights (YEAR). Even when LSTMs have been used with multi-data type datasets, they have only been used to translate from one data type to another. Moreover, LSTM performance on multi-data type datasets was largely a factor of increased memory (Ji Lee, YEAR). This leaves a gap for a methodology that analyzes multi-data type datasets.

A large research gap is detecting that joint data type features exist. Research has no methods for detecting if correlated features exist between two data types. The knowledge that correlated features exist give incentive to data users to exploit these correlations to create better machine learning models. This paper sees the ability to detect correlated features within multi-data type datasets as a significant knowledge gap that could aid analysis future researchers and help train many datasets.

Another gap is an architecture for processing multi-type datasets. In light of most research analyzing each data type separately, there has been less research trying to combine data types. The reason for this problem is that each data type performance is very different on CNNs vs NNs. Yet, if research could propose an architecture for combining the data, beyond an auto-encoder or RBM, that architecture could prove useful discovering new features on these multi-type datasets.

#### 6.0.3 What would you like to know?

It would be worthwhile to apply the methodology set forth in future sections to existin multi-data type benchmarks like Flickr 8k and 30k. Such an analysis would shed light on the feasibility of the methodology. Part of the methodology uses boosting. It would be interesting to see the use of boosting with Deep Neural Networks (DNNs). Boosting is not commonly applied to DNNs since there really is not a concept of a weak model with NN. NN, contrasted with weak models like decision trees, can learn massive featuresets with controlled overfitting. This makes single DNNs good models. It will be interesting to see if the proposed concept of a NN weak model for boosting shows performance gains on existing benchmarks. It will also be interesting if the proposed combined architecture yields any weak models, which might imply that the architecture identified either weak single-type or joint data type features.

#### 6.0.4 Why is it important?

Data with multiple data types is becoming more common. The new data provides a new challenge for researchers for analyzing the data. One important challenge is drawing data from each data type, e.g. feature correlations between data types. These joint data type features are a new source of knowledge for data scientists and researchers. New knowledge has the potential for better performing models and improvement in current practice.

Current practice contains many datasets with multiple types. Of particular note

are examples in the medical field. Search Kaggle alone gave provided many medical datasets with text and image data types, like: skin cancer datasets, Pulmonary Chest X-Ray abnormalities, Chest X-Ray Images for Pneumonia, DDSM Mammography, Blood Cell Images, CT Medical Images, Findings and Measuring Lungs in CT Data, MRI and Alzheimers, X-ray Bone Shadow Suppression, and many more. These represent a small sample of a large number of datasets with important information. Such examples and the feasibility of garnishing more quality data from these datasets is a good justification for further research. It is likely that new information that better connect text data like symptoms with images could discover breakthroughs in diagnosing patients. The potential benefits are far reaching but seem realistic if joint data type features can be extracted and added to current machine learning models.

#### 6.0.5 Why we should care?

Research into better understanding joint data type datasets is worthwhile because these datsets are common and affect many persons. The previous section listed many medical datasets containing text and image data. Such medical datasets are important for the general population, so any improvement in understanding or processing of this data has a larger impact on society. Improved models means improved results. Moreover, these bette results are drawn from relationships between each data type, and so may provide a larger understanding of behavior over the entire dataset, between data types. This larger and across data type understanding could improve how current practice makes use of medical images and symptom data together, rather

than separately. The general public should care about the research because it will provide new insights and methodologies for datasets which affect the general public. The research can improve researcher's ability to extract knowledge out of these datasets, which will lead to greater insights and betterment of the public.

## Open Problems/Questions in IT

# 7.0.1 What is the gap between what is known and what needs to be known?

Research has analyzed data with single data types with a great degree of accuracy. There are commonplace techniques for analyzing each data type. Moreover, these models are well-known and simple, such as CNNs for videos, NN for text, and RNNs for images. Given that simple models work well on simple data types, an interesting question is how well simple models process multiple data types. This is a valid question and lies more in the arena of what needs to be known.

There has been less research analyzing multiple data types. The research that has examined related data types focuses on the relationship between audio, movement, and images in videos. Of the research performing machine learning on multi-type datasets, these papers use autoencoders and LSTMs. Yet, the models have tended to only learn single type features, since single type features are more significant or

receive stronger negative feedback than joint data type features. This leaves a major gap in modeling joint data type datasets. There is a need for a methodology for both detecting and extracting joint data type features.

#### 7.0.2 What would you like to know?

There is a need to verify that joint features in multi-type datasets exist. The ability to detect these features can encourage researchers to make note that such features exist and should be included in their analysis. Finally, there is a needed methodology for including these features in machine learning models. Each of these gaps in current research knowledge and methodology is interesting and becoming more relevant with growing datasets. One challenge in this interest is verifying that the detected features are actually joint data type features, and not just better learning with single data types.

It would be interesting to apply a methodology for detecting joint data type features to existing datasets. These datasets could be surveyed and the existence of joint data type features could be recorded. Such a list of datasets also provides other researchers with benchmarks for testing new multi-data type features.

#### 7.0.3 Interesting Questions About the Research Gap

The previous section explained the gap in existing methodologies for analyzing joint data type features in a dataset. Based on the gap, an apropos question is if it is possible to detect joint data type features. A following question is how significant these features are. Considering that previous models ignored joint features and only learned single-type features, it makes sense that either the joint features are weaker or only occur in a limited set of the dataset. If indeed these features can be shown to exist, an interesting question is how they can be extracted from datasets. Both validating the existance of joint data type features and extracting those features are gaps and worthwhile questions. The next section will present research questions. Those research questions have the goal of exploring joint data type features, both their existence and extraction. The methodology for exploring answers to both of those questions involves a lot of existing machine learning theory. Those theories are boosting and weak models, which will be explored in future sections.

#### 7.1 Research Question

When applying boosting to individual data type models, by using weakly trained multi-type CNNs for the ensemble models, how does this affect the model's performance in classification/regression?

#### 7.1.1 Expounding on the Research Question

The idea for the research question hinges on the related work. The related work concluded that when training multi-data type models, that these models only learn single data type features. The implication is that joint data type features are less pronounced than single-data type features, or that because joint data type features may not match the type of the output that these features receive less negative feedback

and so undergo less training. From the reality that joint features are less pronounced, any modeling with joint features must consider single-data type features. When this knowledge is given the context of current practice, it seems unwise to ditch single-data type models entirely. Rather, models that detect joint features can be used in conjunction with single-data type features. Such combination of models is known as an ensemble method, where multiple models are considered for the final output, since multiple semi-independent models tend to give better predictions than any single model.

Building on the idea of an ensemble method that uses joint data type features, the research question strong hinges on the theory that joint data type features are more complicated and nuanced than single-data type features. The research question also acknowledges that current single-data type models are very good and have achieved good performance on existing benchmarks. It is likely that a joint model will not perform as well as either individual model, but instead aid the individual model's performance. The general theory of aiding existing model performance sounds a lot like existing boosting and bagging methods on structured data. These methods create weaker model, i.e. models that do not perform as well or only slightly better than random chance, and use those models to strengthen existing models. The strengthening is done by identifying weak points in the model, e.g. misclassifications or poor regression predictions. Boosting methods then build the weak models based on the poor performance of the main model. The result is a main model with multiple weaker models to that offset weaknesses in the main model. This is the general idea being proposed by the research question.

Now given that there is training data for the combined model, i.e. the data misclassified or poorly regressed by the main data on the training data, the only missing piece is the architecture for the combined model. It would be simple enough to concatenate text and image pixel intensities together as the combined model. Yet, this seems like a poor option. Existing research has shown that more abstract data types like images are poorly handled by NNs and better handled by CNNs. It seems reasonable for a base combined model to somehow include CNNs when including any image data. The main challenge is how to include image data with CNNs and text data.

As was explained in the related work, CNNs group features based on their location. CNN layers can either compress the data in half or compare features across groups. The ability for CNNs to behave like a normal NN by comparing values across groups is an advantage. If text data can be represented as one group, and image data as another group, then these can be compared in a NN fashion within a CNN.

Part of the proposed methodology of this paper is to use a CNN for the boosting model. This CNN will combine image and text data in a very particular way. The CNN will be twice as wide as the image. The left side will contain the image, the right side will contain the text with surrounding whitespace. By creating two squares in the CNN, when layers are halved in size, text and image data are technically kept separate within the CNN. Each layer that compares data between groups will capture relationships between the text and image. This allows for the CNN to evolve text and image data, while developing separate and combined features. The strength of this architecture is that it allows image data to undergo convolutions while interacting

with the text data. A weakness of the model is that text data is trained on a CNN.

Yet, as the related work showed, CNNs are able to obtain decent performance with text data.

The interesting part of this research is how it considers single-data type features. These features are normally a problem when identifying joint data type features. Yet, when only test data is used where single-data type features perform poorly, i.e. where misclassifications or poorly predicted regressions occur, this leaves an opportunity for training joint type features. Boosting has shown great performance at improving structured data models. It seems like there is opportunity for boosting to be used with NNs. Traditionally boosting has been done with decision trees. Yet, NN and different from structured data. A weaker NN can be trained on a small amount of data. By providing both data types to the NN, it is more likely that the NN will learn from these features. Boosting is also nice because it only considers models that improve performance. The final group of boosted CNN models can be given equal weight in the ensemble of each individual model.

### 7.1.2 Open Research Problems in IT

### 7.1.2.1 1. Detecting Joint Data Type Features

There are many datasets that contain multiple data types. Yet, there is no litmus test for identifying that correlated features exist between data types. The creation of a method for identifying the existence of joint data type features would aid researcher's when deciding how to approach and learn on the dataset. The creation of a method

to detect these between dataset features is an open question this paper can begin to address.

# 7.1.2.2 2. Methodology for Regression and Classification with Multiple Data Types

Auto-encoders can be used to create generative models. These work by learning ways to represent the data. In this way, they can be used to transform data. The related work covered a few examples of using auto-encoders to transform one data type into another. Yet, these encoders are only generative, not exact. The models learn general patterns. This makes autoencoders useful to learning general patterns from input to output, but not useful for the more common classification or regression problems. This creates a gap for ways to perform classification and regression on multi-data datasets. This gap exists because these datasets are complicated, joint data type features have weaker feedback signals (Ngiam et al., YEAR), and there is no common methodology for even detecting the existence of these features within a dataset.

## 7.2 Purpose Statement

### 7.2.1 Central Intent for the Study

The topic of combining models of different data types offers a lot of promise. If researcher's can find better ways to model complex data, i.e. data that contains multiple data types, then researcher's and practitioners will have better tools for analyzing real-world data. Most data in the world is complex, interconnected, and

can be represented in many ways. For example, medical diagnosing patients makes use of visual data, e.g. X-Rays and a set of symptons, which can be represented as text data. Having ways to combine the analysis of text and image data can produce models that make better predictions on these datasets.

The central intent for the research is creating a methodology to improve the analysis of multi-data type datasets. The research question poses both a methodology and architecture for analyzing this data. The intent of the research question is to improve current model performance on these datasets, while showing that joint data type features exist.

### 7.2.2 Contributing to a Body of Knowledge within IT

One of the researchers in this paper works within advertising. Most of the datasets in this field comprise multiple data types. Examples are posts, which can contain images, video, text, and other metadata. While this is the general field of interest, the proposed research question is very generic and should apply to many contexts. The body of knowledge within IT is multi-faceted. One facet is the analysis of multi-type datasets. Another facet is the use of boosting techniques for DNNs. A third facet is the combined CNN architecture proposed for processing text and image data. The use of boosting in DNNs and a proposed architecture for new datasets can contribute to current research within applied machine learning.

#### 7.2.3 Is there an area of practice you would like to improve?

In searching for dataset on multi-data type models that are comprised on image and text data on Kaggle, most of the datasets were within medicine. Examples include X-Rays, CT Scans, MRIs, as well as a set of symptoms or relevant data about the scan or patient. Processing medical images is a well studied field within machine learning. This paper hopes to improve the field of medical image processing by providing researcher's with a methodology for combining current medical imaging practice with other complicated text or numerical data.

The paper's main contributer is a software engineer at LinkedIn on their advertisement reporting team. The LinkedIn advertising team is responsible for the real-time reporting of advertising events that occur on LinkedIn. Anytime an advertisement is seen or interacted with, our team collects those events and reports them to advertisers. A benefit of being on this team is being involved in the process of creating new advertising platforms and analyzing the performance of advertising campaigns. The involvement with advertising gives the authors particular interest at analyzing advertiser content. The advertising team deal with many types of advertising data, like user reactions, images, and comments. This provides interest in these advertising metrics, whose inputs are diverse types of data, e.g. text, image, and video data.

# Chapter 8

# Theory

Theory speaks to which accepted theories the topic relies on. One such assumption is that having more knowledge about a dataset will create machine learning models which perform better on the same data. The goal of extracting knowledge from a dataset for a machine learning model is often known as feature extraction. Practitioners who perform better feature extraction create models that perform better. This feature extraction consists of extracting information from the model. Another aspect is the quality of those features, i.e. do the features predict data behavior. The proposition of this paper is more knowledge, i.e. features can be extracted when considering text and image datasets together, rather than each separately. These joint features provide new knowledge, therefore new features, which should result in knowledge gained and a potentially better performing final machine learning model.

Another theory is that data types are not always mutually exclusive in their features, i.e. that correlations can exist between features in different data types.

This theory has been shown to be true in videos by decomposing data into visual and

audio data. Yet, this theory has less support between text and image datasets. This research provides opportunity to affirm or prove false for datasets consisting of text and image data.

Machine learning in the past decade has made random forest and boosting algorithms more popular. These algorithms operate on the assumptions that adding tweaks to models via weaker models can improve model weak points. Random forests are an ensemble of decision trees, and boosting methods tend to use random forests to improve weak points in model performance. The decision trees are a good choice for improving model weak points because they are quick to train and work well on small datasets. It is assumed that the combined model training on a small dataset will converge quickly and operate similarly. Moreover, ensemble and boosting methods operate on a general theory that tweaking models at weak points can significantly improve model performance. Building on this theory, new methods that can improve model weakpoints can largely improve model performance.

### 8.0.1 Philosophical Assumptions

### 8.0.2 Social Reality

Multimodel research accepts that data types can be combined and encoded into new representations of that data. These models can represent both data types and aid to knowledge gleamed from the dataset. The overarching theory behind the multi-model research proposes that when multiple data types describe a phenomenon, that those data types are related. The theory is that some of the data from each data type is

correlated, since the data is extracted from the same event. It is as if each data type is a vector of information. When each data types' vector is combined it creates a final data point, a master data point of sorts, which describes the phenomenon. By combining each data type a machine learning model can better predict the master data point, or the phenomenon as a whole. For example, social media advertisement contains an image and a description. The user's reaction to an advertisement is likely a factor of not only the image or the description, but a factor of both the image and its description. The theory poses that when data naturally occur together, each type of data contains correlations with the other type of data.

The research question also assumes that new machine learning architectures can better learn when designed to take advantage of correlations that may exist between the different data types. These different architectures can either add data to existing models or improve upon existing models that usually only operate on one type of data. By considering how each data type might interact, and how the model can learn from this interaction, the model may be able to better learn and represent the data and its features.

#### 8.0.3 What we understand to be true

Some of the required theories are generally accepted. It is known when multiple data types exist, machine learning models can learn by including both data types in its models. This can be seen in ensemble models. It is also well accepted that model performance can be improved by weaker models, which are trained via boosting.

Current theories have also shown that different data types can be analyzed with the same architecture. For example, a CNN can perform image analysis and NLP tasks. Yet, CNNs will perform worse and differently on NNs than on CNNs. Also, a NN can process text and image data, but NN poorly draw out image features. Existing studies have also transcribed one data type to another, such as sentence descriptions of images.

# Chapter 9

# Methodology

### 9.1 Means of Investigation

Benchmark datasets already exist for multi-data type datasets. Many of these datasets and performance metrics are on Kaggle and mentioned in the related work. The benchmarks are useful because they provide the data for the experiment. The benchmarks are also reference points for model performance and training time. Moreover, there are many types of benchmarks containing text and image data. This allows for the methodology to be tested for regression and classification performance. This simplifies testing the methodology for multi-type datasets.

There are more nuanced aspects of the research question. One such nuance is the assertion that the model will perform boosting on the dataset. Boosting is a common machine learning technique and creates weak models that perform slightly better than random chance. One means of investigation will use existing boosting libraries to create an ensemble of boost models from the CNN architecture. The investigation will be if the boosting library is able to generate weak models from the CNNs, implying that it is possible to create weak models from NNs.

Building on the combined model, another means of investigation will be the performance of the final ensemble of models. These models will contain a trained NN text-based model, CNN image-based model, and the ensemble of combined CNN models. One means of investigation will be the classification accuracy/regression performance of averaging ball three models on a dataset.

#### 9.1.0.1 Qualitative/Inductive

The combined CNN model helps generate new insights and research questions due to its ability to visualize the activations at each layer. A benefit of CNNs is the ability to visually depict features in each layer. It is common for object classification to see the many layers of CNN and the activation in each layer. One layer might find eyes, ears, tails, and other image features. One benefit of using a combined CNN is that each layer's activations can be visualized and may provide insight and future research questions into what is occurring within a combined CNN.

Boosting is a very popular idea that has yet to be applied to DNNs. The performance of a boosting algorithm to DNNs has the potential to generate many related research questions. For one, is it possible to create a weak model with boosting out of CNNs. Secondly, how long does it take to generate a weak CNN? A more interesting question is how many weak CNNs a boosting approach will create. Futhermore, the performance of the ensemble of CNNs will be interesting, as well as how the ensemble of individual models and the CNN are combined.

The architecture of the CNN has the potential to generate more research. The architecture seems like an intuitive way to combine text and image data. It also opens up a general approach to combining image and text data. Related research could explore the best configuration for dense and pooling layers with multi-data type architectures, since it is the dense layers that combine image and text data. There is also the potential to create multi-type models with LSTMs and NN, then to compare their performance in boosting with the CNN. The research direction has a lot of potential outcomes and may generate a lot of related research.

#### 9.1.0.2 Quantitative/Deductive

The deductive approach for this paper tests the theory that joint features exist. The paper proposes a methodology that emphasizes and provides a environment that should foster the detection of joint data type features. The deductive hypothesis is that joint features exist, and this hypothesis is tested in the proposed methodology. The ability for boosting methods to create weak models would affirm that joint data type features likely exist, as single-data type features would have been detected by either single-data type models. The very reason that boosting is not used for DNNs is because single type models are capable of analyzing, memorizing, and performing with huge feature sets, which is the weakpoint random forests have that boosting helps mitigate.

Another hypothesis is that a combined CNN is capable of detecting joint data type features. This is closely connected to the previous hypothesis. The ability to create weak models from boosting affirms this hypothesis, while an inability to generate weak models from boosting implies either that CNNs are unable to capture joint data type features, or that those features do not exist. The ability to improve existing single data type models with a combined model is a third hypothesis tested by the research methodology. If the final ensemble model, comprised of boosted CNNs, a text-based NN and image-based CNN outperforms current best-benchmarks, then the research has demonstrated that utilizing combined models can improve model performance.

#### 9.1.1 Means of Evidence

#### 9.1.1.1 Data Collection

The paper has mentioned existing multi-data type benchmarks like Flickr 8k, 30k. There are existing benchmarks for these datasets. Other datasets also exist on Kaggle that include notebooks that will provide trained models and their performance. With the provided tools, implementing the research will only require downloading the datasets and benchmark models, which are publically available. The availability of data and research's open sourcing tools and data make this step in the research process much easier. Outside of downloading the datasets and models, there is no other necessary data collection for the implementing the research methodology.

#### 9.1.1.2 Data Analysis

After data and model collection, the researcher will have the necessary data and singletype models to begin the analysis. Many of existing models are Keras or TensorFlow models, and so can be imported into existing projects. These models are often pretrained, or include a script to run which trains the models in a few hours. From there, the third CNN architecture can be created. As mentioned earlier, the combined CNN model has dimensions image-height x 2 \* image-width. The left-side of the CNN takes an image as input, and the right side takes the word vector padded with whitespace. The following layers in the CNN have dense and pooling layers. This CNN model can be passed to standard boosting libraries and provided as config during Keras training. The boosting library will generate weak models. The user can ensemble each individual model with the combined model. This final model needs to testing, as each individual models are already trained and the weak models have been created. The performance can be evaluated on the validation dataset. The performance of the ensemble models can be reported on the benchmark data and recorded, as well as the number of weak models created by the boosting library. The layers of the weak CNN models can also be visualized and included in the final results. Each of these outputs will guide discussion on model performance, the ability to generate weak DNNs, and the ability to extract joint features from a combined model.

# Chapter 10

# Conclusion

Current approaches to modeling multi-type datasets tend to treat each data type as independent. Yet, it is unlikely that each data type is independent. Rather, it is likely that correlations exist across data types. The trouble researchers face is detecting and extracting joint data type features. This paper proposes that boosting based techniques can be applied to multi-data type datasets to extract joint data type features. These methods seem promising based on the success boosting has exhibited on small datasets at model weak points. If such a method is performant, then it provides researchers a way to detect joint data type features. Moreover, the methodology is simple and can be implemented on existing benchmark datasets.

The research should generate answers and more paths for future research questions. Such paths include the performance of combined models alongside existing single-data type models, the ability to create weak models with DNNs, and architectures for multi-data type models. The outcomes of the research will aid the understanding of multi-data type datasets, what can be known, and how joint features

might be extracted. Hopefully the proposed research proves helpful to those furthering multi-data type models within the domain of machine learning.

# Bibliography

- Baudi, P. and Pichl, J. Sentence Pair Scoring: Towards Unified Framework. (C).
- Crowe, C. (2018). Initial Related Work. pages 1–4.
- Donahue, J., Hendricks, L. A., Guadarrama, S., Rohrbach, M., Venugopalan, S., Saenko, K., Darrell, T., Austin, U. T., Lowell, U., and Berkeley, U. C. Long-term Recurrent Convolutional Networks for Visual Recognition and Description.
- Enerative, F. O. R. G., Of, M. O., and Ideos, N. A. V. (2014). V (1) m: a b f g m n v. pages 1–15.
- Fan, Y., Lu, X., Li, D., and Liu, Y. (2016). Video-Based Emotion Recognition using CNN-RNN and C3D Hybrid Networks. (November).
- Ghosh, A. and Veale, T. (2016). Fracking Sarcasm using Neural Network. pages 161–169.
- Graves, A. Generating Sequences With Recurrent Neural Networks. pages 1–43.
- Graves, A. (2014). Towards End-to-End Speech Recognition with Recurrent Neural Networks. 32.
- Hurri, J. (2003). Simple-Cell-Like Receptive Fields Maximize Temporal. 691(3):663–691.
- Ji, S. and Yu, K. (2010). 3D Convolutional Neural Networks for Human Action Recognition.
- Karpathy, A., Toderici, G., Shetty, S., Leung, T., Sukthankar, R., and Fei-fei, L. (2015). Large-scale Video Classification with Convolutional Neural Networks Presenter: Esha Uboweja Problem Classification of videos in sports datasets. (June 2014).
- Lan, Z., Lin, M., Li, X., Hauptmann, A. G., and Raj, B. Beyond Gaussian Pyramid: Multi-skip Feature Stacking for Action Recognition.
- Le, Q. V., Zou, W. Y., Yeung, S. Y., and Ng, A. Y. Learning hierarchical invariant spatio-temporal features for action recognition with independent subspace analysis.

- Lee, J. Y. and Dernoncourt, F. (2016). Sequential Short-Text Classification with Recurrent and Convolutional Neural Networks.
- M, N. E. N. E. and Yuille, A. (2015). D c m r n n (-rnn). 1090(2014):1-17.
- Merri, B. V. and Fellow, C. S. (2014). Learning Phrase Representations using RNN Encoder Decoder for Statistical Machine Translation. pages 1724–1734.
- Michalski, V. and Memisevic, R. Modeling Deep Temporal Dependencies with Recurrent "Grammar Cells". pages 1–9.
- Mobahi, H., Weston, J., America, N. E. C. L., and Way, I. (1996). Deep Learning from Temporal Coherence in Video.
- Sainath, T. N., Vinyals, O., Senior, A., and York, N. No Title. pages 1–5.
- Simonyan, K. Two-Stream Convolutional Networks for Action Recognition in Videos. pages 1–9.
- Simonyan, K. and Zisserman, A. (2015). Very Deep Convolutional Networks for Large-Scale Image Recognition. *International Conference on Learning Representations (ICRL)*, pages 1–14.
- Soomro, K., Zamir, A. R., Shah, M., and Recognition, A. (2012). UCF101: A Dataset of 101 Human Actions Classes From Videos in The Wild. (November).
- Srivastava, N. (2014). Unsupervised Learning of Video Representations using LSTMs.
- Srivastava, N. (2015). Unsupervised Learning of Video Representations using LSTMs. 37.
- Susskind, J., Memisevic, R., Hinton, G., and Pollefeys, M. Modeling the joint density of two images under a variety of transformations.
- Sutskever, I. Sequence to Sequence Learning with Neural Networks. pages 1–9.
- Understanding, R. N. N. C.-f. L. DiSAN: Directional Self-Attention Network for RNN/CNN-Free Language Understanding.
- Vosoughi, S. and Roy, D. (2016). Tweet2Vec: Learning Tweet Embeddings Using. pages 16–19.
- Wang, J., Yang, Y., Mao, J., Huang, Z., Huang, C., and Xu, W. CNN-RNN: A Unified Framework for Multi-label Image Classification. pages 2285–2294.
- Wang, J., Yu, L.-c., Lai, K. R., and Zhang, X. (2016). Dimensional Sentiment Analysis Using a Regional CNN-LSTM Model. pages 225–230.
- Yin, W., Kann, K., and Yu, M. (2016). Comparative Study of CNN and RNN for Natural Language Processing.

Yin, W. and Sch, H. ABCNN: Attention-Based Convolutional Neural Network for Modeling Sentence Pairs.

Zaremba, W. and Com, V. G. (2013). arXiv : 1409 . 2329v3 [ cs . NE ] 3 Nov 2014.