

Topics

Representation and Deep Learning

► Limitations of MLPs

Deep Image Classification (part 1)

- Input layers
- Convolutional layers
- ReLU activations



In the previous lecture we covered MLPs

- Can represent any decision boundary
- Efficient gradient computation via backpropagation

Sounds like MLPs solve our cat vs. dog classification problem

- lacktriangle Just make H large enough / use several hidden layers
- What do you think?



Turns out it's not that simple

We've been processing whole images, D=3072

- $ightharpoonup \dim(\theta)$ increases quickly with H (≈ 1.5 m at H = 500)
- As well as the number of hidden layers (network depth)

Such complex MLPs are hard to train

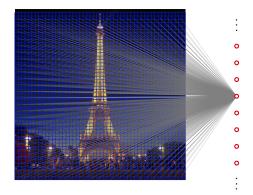
Gradient Descent likely gets us nowhere

Generalization performance would likely be lackluster anyways

Next lecture



 $\dim(\boldsymbol{\theta})$ increases quickly with D and H



Recall that pixel values make bad features

- ▶ Better use MLP in traditional image classification pipeline
- \blacktriangleright CIFAR-10 test accuracy with HoG features is $\approx 60\%$

Low-level features are again the limiting factor

- ▶ Recall that we want task-specific high-level features
- But we can't design such feature extractors



MLPs for Image Classification Representation Learning

We cannot design reliable high-level feature extractors

- ▶ But maybe we can learn them
- ► This task is called Representation Learning

In a way MLPs do this already

- ▶ Hidden layer learns to extract H features from x
- Output layer classifies these features



MLPs for Image Classification Representation Learning

But we already know this does not work for images

- ► MLP has to learn good features in single step
- Using rather simple transformations

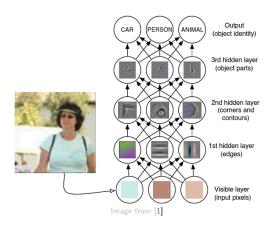
Making the MLP deeper by adding hidden layers should help

- Gain ability to learn features in hierarchical way
- Later features build upon earlier (simpler) ones
- ► This is the idea behind Deep Learning (DL)



Deep (Representation) Learning

Deep Learning is Representation Learning with DNNs



Deep (Representation) Learning

However the limitations of MLPs persist

- $ightharpoonup \dim(\theta)$ increases quickly with depth
- Complex MLPs are hard to train

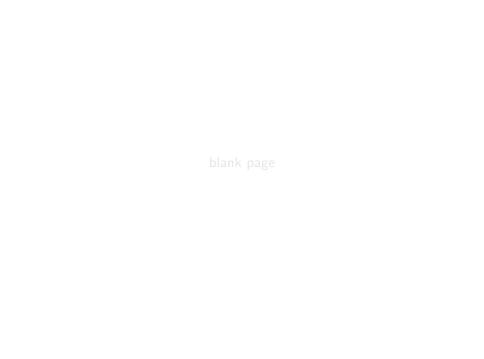
Also MLPs have (again) no understanding of images

- Reason we had to convert images to vectors x
- Losing spatial information in the process

In order for DL to work we need a better NN architecture

► One optimized for image (grid/tensor) data





Deep Image Classification Input Layer

Should make use of spatial structure of images

▶ Not sensible to flatten images to vectors

Retain structure by arranging input neurons accordingly

- ▶ If input images have size $W_0 \times H_0$ and C_0 channels
- ▶ Input neurons form $W_0 \times H_0 \times C_0$ grid
- ▶ W_0 is width, H_0 is height, C_0 is depth of layer 0

Deep Image Classification Input Layer



Input Image



Input Layer

Feature Extraction

Spatially close pixels are highly correlated, others are not

► Nearby pixels correspond to same object (or part)

A good image feature extraction layer must account for this

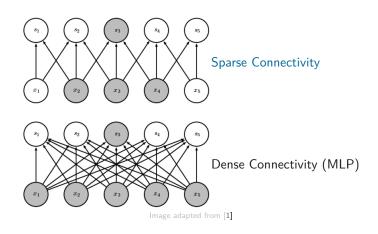
Compute features from spatially close pixels

We can achieve this by

- lacktriangle Arranging hidden layer neurons in $W_l imes H_l$ grid
- ightharpoonup Connecting only spatially close neurons (similar W, H)
- ► Neurons are thus sparsely connected (fewer parameters)



Feature Extraction



Feature Extraction

 W_l and H_l depend on input width and height

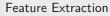
- ▶ Usually $W_l = W_{l-1}$ and $H_l = H_{l-1}$ to preserve resolution
- ▶ With padding in border regions (replication)

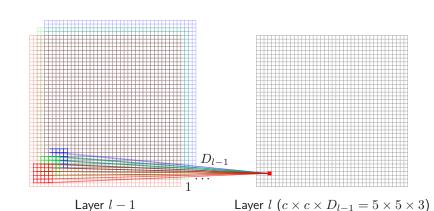
Connectivity c along W and H dimensions

▶ Configurable but usually c = 3, that is 3×3

Connectivity along depth dimension is usually D_{l-1}

Want to make use of all local information





Feature Extraction

Extraction should work the same anywhere in input

- ► We generally don't know where objects will appear
- Due to varying object location and viewpoint

Achieved by letting neurons compute the same operation

- For linear layers this means identical weights and bias
- ▶ So $n_h(\mathbf{X}_h) = \mathbf{A}_l \cdot \mathbf{X}_h + b_l$ with $\mathbf{X}_h, \mathbf{A}_l \in \mathbb{R}^{c \times c \times D_{l-1}}$

Feature Extraction

Neurons in layer l compute $n_h(\mathbf{X}_h) = \mathbf{A}_l \cdot \mathbf{X}_h + b_l$

- $ightharpoonup {f A}_l \cdot {f X}_h$ is a linear combination (like before)
- $ightharpoonup {f A}_l$ is identical for all neurons in layer

The overall transformation of the layer is thus

- ightharpoonup A convolution of the input with kernel \mathbf{A}_l
- ightharpoonup Followed by an additive bias b_l

Such layers are thus called convolutional (conv) layers

► Fundamental DL layer

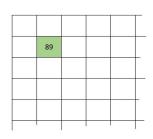


Feature Extraction

Recall how discrete convolutions work (here $D_{l-1} = 1$)

0	-1	0
-1	5	-1

Kernel Matrix



Output Matrix

Image Matrix

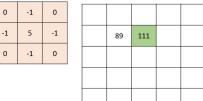
$$105 * \frac{0}{1} + 102 * \frac{-1}{1} + 100 * \frac{0}{1} + 103 * \frac{-1}{1} + 99 * \frac{5}{1} + 103 * \frac{-1}{1} + 101 * \frac{0}{1} + 98 * \frac{-1}{1} + 104 * \frac{0}{1} = 89$$

Image from machinelearninguru.com

Feature Extraction

Recall how discrete convolutions work (here $D_{l-1} = 1$)

Kernel Matrix -1



Output Matrix

Image Matrix

$$102 * 0 + 100 * -1 + 97 * 0$$

+99 * -1 + 103 * 5 + 101 * -1
+98 * 0 + 104 * -1 + 102 * 0 = 111

Image from machinelearninguru.com

Feature Extraction

Neurons thus "detect" features via $n_h(\mathbf{X}_h) = \mathbf{A}_l \cdot \mathbf{X}_h + b_l$

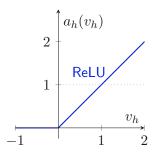
- lacktriangle Respond to local structures similar to ${f A}_l$
- lacksquare Similar to template matching with learned template ${f A}_l$

Conv layers are thus rather simple feature extractors

- Power comes from stacking such layers
- With activation functions (and other layers) in between

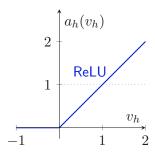
Standard activation function for conv layers is ReLU

- Stands for Rectified Linear Unit
- Speeds up optimization



CNNs often use ReLU everywhere

► Also after linear layers



Feature Extraction

One issue remains

- Every neuron performs same operation
- So layer can learn to extract only one feature

To overcome this problem we replicate the neurons \mathcal{D}_l times

- ▶ Resulting in a $W_l \times H_l \times D_l$ grid of neurons
- ▶ Arranged in D_l feature maps of size $W_l \times H_l$
- Only neurons in same feature map share parameters

Layer can thus learn D_l different features

▶ Hyperparameter, usually $D_l \in \{32, 64, 128, 256, 512\}$



Feature Extraction

Number of weights A_l depends only on c, D_{l-1} , D_l

- $ightharpoonup c = 3, \, D_{l-1} = 3, \, D_l = 32 \implies 864 \text{ weights}$
- ► $c = 3, D_{l-1} = 32, D_l = 64 \implies 18.5$ k weights

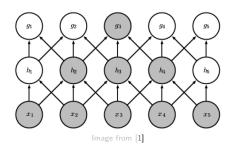
Way fewer parameters than with linear layers

- Can stack several conv layers
- ▶ Layer l learns to combine layer l-1 features to new ones
- ► This is exactly the hierarchical approach we desire

Feature Extraction

Neurons see small part of previous layer (sparse connectivity)

▶ But larger input region (receptive field) as depth increases



Feature Extraction

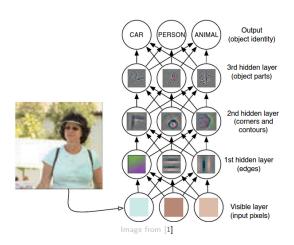
So in networks of conv layers

- ► Direct connections are sparse
- But receptive field can span most/all of image

Feature extraction approach is thus part-based

- Learn local features (e.g. presence of eye or nose)
- Learn global features (e.g. presence of face) from those

Feature Extraction



Feature Extraction

NNs that include conv layers are called CNNs

Convolutional Neural Networks

Other common layer types of such networks (next lecture)

- Pooling layers for dimensionality reduction
- Linear layers to obtain w (e.g. class scores)

Bibliography

[1] Ian Goodfellow, Yoshua Bengio, and Aaron Courville. *Deep Learning*. 2016.

