

Insertion Sort in C

What is Insertion Sort?

- A simple sorting algorithm
- Works like sorting playing cards in your hand
- Builds the final sorted array **one item at a time**



Algorithm Idea

1. Start from the **second element**
2. Compare with elements before it
3. Shift larger elements to the right
4. Insert the element into the correct position
5. Repeat until array is sorted



C Implementation

```
#include <stdio.h>

void insertionSort(int arr[], int n) {
    for (int i = 1; i < n; i++) {
        int key = arr[i];
        int j = i - 1;

        while (j >= 0 && arr[j] > key) {
            arr[j + 1] = arr[j];
            j--;
        }
        arr[j + 1] = key;
    }
}
```



What is Binary Search?

- Efficient algorithm for finding an element in a **sorted array**
- Works by repeatedly dividing the search interval in half
- Compare target with the middle element:
 - If equal → found
 - If smaller → search left half
 - If larger → search right half



Algorithm Idea

1. Start with `low = 0`, `high = n-1`
2. Compute `mid = (low + high) / 2`
3. Compare `arr[mid]` with `key`
 - If `arr[mid] == key` → return `mid`
 - If `arr[mid] > key` → search left half
 - Else → search right half
4. Repeat until `low > high`



Recursive Implementation (C)

```
int binarySearchRec(int arr[], int low, int high, int key) {  
    if (low > high) return -1;  
  
    int mid = (low + high) / 2;  
  
    if (arr[mid] == key)  
        return mid;  
    else if (arr[mid] > key)  
        return binarySearchRec(arr, low, mid - 1, key);  
    else  
        return binarySearchRec(arr, mid + 1, high, key);  
}
```



Example Dry Run

Array: {1, 3, 5, 7, 9, 11, 13}

Search for 7

low=0, high=6 \rightarrow mid=3 \rightarrow arr[3]=7 \rightarrow found at index 3

Search for 6

low=0, high=6 \rightarrow mid=3 \rightarrow arr[3]=7 (too big)

low=0, high=2 \rightarrow mid=1 \rightarrow arr[1]=3 (too small)

low=2, high=2 \rightarrow mid=2 \rightarrow arr[2]=5 (too small)

low=3, high=2 \rightarrow stop \rightarrow not found



What is the Fibonacci Sequence?

- Each number is the sum of the two preceding numbers
- Defined as:
 - $F(0) = 0$
 - $F(1) = 1$
 - $F(n) = F(n-1) + F(n-2)$, for $n \geq 2$

Example sequence:

0, 1, 1, 2, 3, 5, 8, 13, ...



Recursive Definition in C

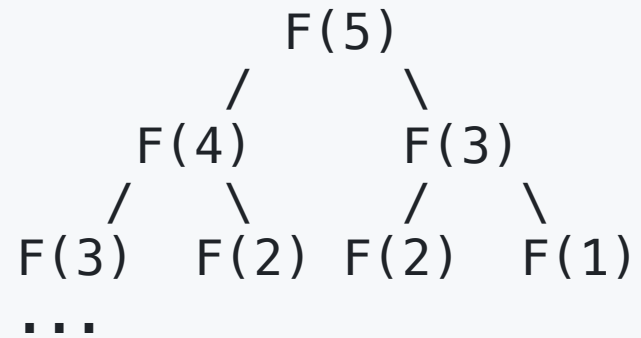
```
int fibonacci(int n) {  
    if (n == 0) return 0; // base case  
    if (n == 1) return 1; // base case  
    return fibonacci(n-1) + fibonacci(n-2); // recursion  
}
```

Example Trace: F(5)

```
fibonacci(5)
= fibonacci(4) + fibonacci(3)
= (fibonacci(3) + fibonacci(2)) + (fibonacci(2) + fibonacci(1))
= ...
= 5
```



Tree of calls (partial):



Towers of Hanoi

- You have **3 pegs**: Source (A), Auxiliary (B), Destination (C)
- **n disks** of different sizes are stacked on Source peg
- Goal: Move all disks to Destination peg
- Rules:
 - i. Only one disk moved at a time
 - ii. A disk can only be placed on an empty peg or on a larger disk
 - iii. Disks must maintain order

Recursive Idea

To move n disks from $A \rightarrow C$ using B :

1. Move $n-1$ disks from $A \rightarrow B$ (using C)
2. Move the largest disk from $A \rightarrow C$
3. Move $n-1$ disks from $B \rightarrow C$ (using A)



Example for 3 Disks

1. Move 2 disks from A \rightarrow B
2. Move disk 3 from A \rightarrow C
3. Move 2 disks from B \rightarrow C

Moves:

A \rightarrow C

A \rightarrow B

C \rightarrow B

A \rightarrow C

B \rightarrow A

B \rightarrow C



C Implementation

```
#include <stdio.h>

void hanoi(int n, char from, char to, char aux) {
    if (n == 1) {
        printf("Move disk 1 from %c to %c\n", from, to);
        return;
    }
    hanoi(n - 1, from, aux, to);
    printf("Move disk %d from %c to %c\n", n, from, to);
    hanoi(n - 1, aux, to, from);
}

int main() {
    int n = 3;
    hanoi(n, 'A', 'C', 'B');
    return 0;
}
```



What is Merge Sort?

- A **Divide and Conquer** sorting algorithm
- Steps:
 - i. Divide array into two halves
 - ii. Recursively sort both halves
 - iii. Merge the two sorted halves
- **Always $O(n \log n)$ time complexity**



Algorithm Outline

1. If array has 0 or 1 elements → already sorted
2. Otherwise:
 - Divide array into left and right halves
 - Recursively sort each half
 - Merge two sorted halves into one sorted array

Merge Function

```
void merge(int arr[], int l, int m, int r) {  
    int n1 = m - l + 1;  
    int n2 = r - m;  
  
    int L[n1], R[n2];  
  
    for (int i = 0; i < n1; i++) L[i] = arr[l + i];  
    for (int j = 0; j < n2; j++) R[j] = arr[m + 1 + j];  
  
    int i = 0, j = 0, k = l;  
    while (i < n1 && j < n2) {  
        if (L[i] <= R[j]) arr[k++] = L[i++];  
        else arr[k++] = R[j++];  
    }  
    while (i < n1) arr[k++] = L[i++];  
    while (j < n2) arr[k++] = R[j++];  
}
```



Merge Sort Function

```
void mergeSort(int arr[], int l, int r) {  
    if (l < r) {  
        int m = l + (r - l) / 2;  
  
        // Recursively sort left and right halves  
        mergeSort(arr, l, m);  
        mergeSort(arr, m + 1, r);  
  
        // Merge sorted halves  
        merge(arr, l, m, r);  
    }  
}
```



Example Dry Run

Array = {12, 11, 13, 5, 6, 7}

Divide \rightarrow {12, 11, 13} and {5, 6, 7}

Recursively sort:

{12, 11, 13} \rightarrow {11, 12, 13}

{5, 6, 7} \rightarrow {5, 6, 7}

Merge:

{11, 12, 13} and {5, 6, 7} \rightarrow {5, 6, 7, 11, 12, 13}



Visualization of Recursive Calls

```
mergeSort([12,11,13,5,6,7])  
  → mergeSort([12,11,13])  
    → mergeSort([12,11])  
      → mergeSort([12]) & mergeSort([11])  
        → merge([12], [11]) → [11,12]  
      → mergeSort([13]) → [13]  
        → merge([11,12], [13]) → [11,12,13]  
  → mergeSort([5,6,7]) → [5,6,7]  
  → merge([11,12,13], [5,6,7]) → [5,6,7,11,12,13]
```

