## CPS 491 - Capstone II

Source: <a href="https://github.com/cps491sp21-team13/cps491sp21-main-repo.git">https://github.com/cps491sp21-team13/cps491sp21-main-repo.git</a>

University of Dayton

Department of Computer Science

CPS 491 - Capstone II, Semester Year

Instructor: Dr. Phu Phung

### Capstone II Project

# Compressible Learning Agents for Autonomous Cyber-Physical Systems

### **Team members**

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### **Company Mentor**

Matthew Clark, Principal Scientist

Galois

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## **Project Management Information**

Management board (private access): https://trello.com/b/kVF2rdUV/cps-491-team-13

Source code repository (private access): <a href="https://github.com/cps491sp21-">https://github.com/cps491sp21-</a>

team13/cps491sp21-main-repo

Project homepage (public): <a href="https://cps491sp21-team13.github.io/">https://cps491sp21-team13.github.io/</a>

#### **Revision History**

Description	Version	Date
Details of Taylor and convolutional approximations	0.1	16/02/2021
Details data-driven SINDy approach/change-of-basis strategy for building neural networks	0.2	16/03/2021

### **Overview**

The goal of this project is to explore and document the correlation between the configuration of deep neural networks and the analytical mathematical functions that they model. A long term goal, possibly not explored in this project specifically, is to develop methods for *decomposing* an arbitrary deep neural network into smaller networks with intuitive behavior, and *simplifying* the network into the minimum network needed to model the desired mathematical function.

## **Project Context and Scope**

This project is a contribution to research into the development of machine learning models that learn intuitively.

### **High-level Requirements**

By the end of the semester, we hope to have reasonably comprehensive documentation of the different ways simple neural networks can approximate simple functions. The process of compiling this documentation should involve careful inspection of trained neural networks guided by mathematics.

## **Implementation**

Most work on this project is being done in a Jupyter notebook using markdown for mathematics and Tensorflow for implementing neural networks.

For now, I am focused on fitting functions to pretrained neural networks using SINDy, a regression based technique. Here is a code snippit that illustrates how we can fit discover a function of the form  $r\sin(x + \phi) + b$ . For more details, see the notebook itself.

```
# Construct some sample data
f = lambda x: 0.5*tf.sin(x + 0.79) + 0.2
xdata = tf.random.uniform([100], minval=0.0, maxval=math.pi * 2.0)
ydata = f(xdata) + tf.random.normal([100], stddev=0.05)
# A function for converting from cartesian to polar coordinates
\# (x,y) -> (r,theta)
def cart2polar(x, y):
  r = math.sqrt(x**2.0 + y**2.0)
  theta = math.acos(x/r) if y >= 0.0 else 2*math.pi - math.acos(x/r)
  return [r,theta]
# Fit regression against a basis of functions \{\sin(x), \cos(x)\}
# to get w0, w1, b
X = np.column_stack([tf.sin(xdata), tf.cos(xdata)])
reg = sklearn.linear_model.LinearRegression()
reg.fit(X, ydata)
w0, w1 = reg.coef_
b = reg.intercept_
```

```
# Output model equation in two different forms
print(f"Model: {w0:.2f}sin(x) + {w1:.2f}cos(x) + {b:.2f}")
r, theta = cart2polar(w0, w1)
print(f"Model: {r:.2f}sin(x + {theta:.2f}) + {b:.2f}")
print(f"Model R^2 value: {reg.score(X, ydata):.2f}")
```

### **Software Process Management**

### **Scrum process**

#### Sprint 0

Duration: 20/01/2021-27/01/2021

#### Completed Tasks:

1. Studied fuzzy inference systems from material provided from Galois

2. Studied automatic differentiation.

#### **Sprint Retrospection:**

Good	Could have been better	How to improve?
learned a lot of preliminary information	documentation of progress	take more notes on what I read about/discover

#### Sprint 1

Duration: 27/01/2021-03/02/2021

#### Completed Tasks:

- 1. Learned tensor manipulation and learning models in Tensorflow
- 2. Experimented with small neural networks in a Jupyter notebook

#### **Sprint Retrospection:**

Good	Could have been better	How to improve?
good pace aquiring new knowlege and documenting what I have learned	could have started experimenting with small networks sooner	reach out to ask questions sooner

#### Sprint 2

Duration: 03/02/2021-09/02/2021

#### **Completed Tasks:**

- 1. Learned about convolution from Linear Systems.
- 2. Detailed a technique for constructing neural networks that approximate arbitrary functions inspired by convolution.
- 3. Detailed a technique for approximating arbitrary polynomials with neural networks based on Taylor-series expansion.

#### **Sprint Retrospection:**

Good	Could have been better	How to improve?
documentation was thorough and clear	direction of work could have been more focused toward project goal	more formal communication about the precise goal of the project

#### Sprint 3

Duration: 28/02/2021-09/02/2021

#### Completed Tasks:

1. Explored Taylor series approximations and detailed a method of building a neural network using a Taylor series approximation

2. Explored Fourier series approximations

#### **Sprint Retrospection:**

Good	Could have been better	How to improve?
Documentation was clear	Better communication with company sponsor regarding the direction of the project	smaller, more frequent communication

#### Sprint 4

Duration: 01/03/2021-16/03/2021

#### Completed Tasks:

1. Learned about spline-theory as it relates to deep learning.

2. Learned about SINDy approach to fitting functions to data.

#### **Sprint Retrospection:**

Good	Could have been better	How to improve?
Learning was done quickly and efficiently	Could have implemented ideas more instead of just detailing them in math	organize notebook and code

## **Acknowledgments**

I would like to thank Mr. Matthew Clark, Principal Scientist at Galois, for mentoring this project.