

# TP frottements 2

## Mesures

La distance est notée “d”.

Les dimensions des billes sont notées au dessus.

```
In[50]:= di = Quantity[Around[8.5,0.1],"Centimeters"];  
d = UnitConvert[di, "Meters"]  
  
bille1diam = Quantity[1,"Millimeters"];  
bille2diam = Quantity[1.5,"Millimeters"];  
bille3diam = Quantity[2,"Millimeters"];  
  
b1r = N[UnitConvert[bille1diam/2, "Meters"]]  
b2r = N[UnitConvert[bille2diam/2, "Meters"]]  
b3r = N[UnitConvert[bille3diam/2, "Meters"]]  
  
t1l = Quantity[Around[{4.07,4.15,4.11,4.05,4.18},0.005], "Seconds"]  
t2l = Quantity[Around[{1.63,1.83,1.74,1.88,1.77},0.005], "Seconds"]  
t3l = Quantity[Around[{1.15,1.14,1.17,1.18,1.14},0.005], "Seconds"]
```

Out[51]=  $(0.0850 \pm 0.0010) \text{ m}$

Out[55]=  $0.0005 \text{ m}$

Out[56]=  $0.00075 \text{ m}$

Out[57]=  $0.001 \text{ m}$

Out[58]=  $\{ (4.070 \pm 0.005) \text{ s}, (4.150 \pm 0.005) \text{ s}, (4.110 \pm 0.005) \text{ s}, (4.050 \pm 0.005) \text{ s}, (4.180 \pm 0.005) \text{ s} \}$

Out[59]=  $\{ (1.630 \pm 0.005) \text{ s}, (1.830 \pm 0.005) \text{ s}, (1.740 \pm 0.005) \text{ s}, (1.880 \pm 0.005) \text{ s}, (1.770 \pm 0.005) \text{ s} \}$

Out[60]=  $\{ (1.150 \pm 0.005) \text{ s}, (1.140 \pm 0.005) \text{ s}, (1.170 \pm 0.005) \text{ s}, (1.180 \pm 0.005) \text{ s}, (1.140 \pm 0.005) \text{ s} \}$

## Calculs 1

La moyenne des temps a été prise afin de calculer la vitesse.

```
In[61]:= t1 = Mean[t11]
         t2 = Mean[t21]
         t3 = Mean[t31]
```

```
Out[61]= (4.1120 ± 0.0022) s
```

```
Out[62]= (1.7700 ± 0.0022) s
```

```
Out[63]= (1.1560 ± 0.0022) s
```

```
In[64]:= v1 = d/t1
         v2 = d/t2
         v3 = d/t3
```

```
Out[64]= (0.02067 ± 0.00024) m/s
```

```
Out[65]= (0.0480 ± 0.0006) m/s
```

```
Out[66]= (0.0735 ± 0.0009) m/s
```

## Calculs 2

Le travail de formules pour les forces :

```
In[67]:= volsp =  $\frac{4}{3} \pi * R^3$ ;
         m =  $\rho_{acier} * volsp$ ;

         fp = m * g;
         fa =  $\rho_{glyc} * volsp * g$ ;
         ff =  $6 * \pi * R * \eta * vlim$ ;
```

```
Factor[Solve[Expand[ff + fa == fp],  $\eta$ ]]
```

```
[factorise [résous [développe
```

```
Out[72]= { {  $\eta \rightarrow \frac{2 g R^2 (\rho_{acier} - \rho_{glyc})}{9 vlim}$  } }
```

## Calculs 3

Application numérique pour calculer  $\eta$  :

```

In[73]:= gc = Quantity[9.81,"Meters"/"Seconds"^2];
ρacierc = Quantity[7850,"Kilograms"/"Meters"^3];
ρglycc = Quantity[1260,"Kilograms"/"Meters"^3];

R1 = b1r;
vlim1 = v1;
η1i =  $\frac{2 \text{ gc } R1^2 (\rho\text{acierc} - \rho\text{glycc})}{9 \text{ vlim1}}$ ;
η1 = UnitConvert[η1i, "Millipascals"*"Seconds"]

R2 = b2r;
vlim2 = v2;
η2i =  $\frac{2 \text{ gc } R2^2 (\rho\text{acierc} - \rho\text{glycc})}{9 \text{ vlim2}}$ ;
η2 = UnitConvert[η2i, "Millipascals"*"Seconds"]

R3 = b3r;
vlim3 = v3;
η3i =  $\frac{2 \text{ gc } R3^2 (\rho\text{acierc} - \rho\text{glycc})}{9 \text{ vlim3}}$ ;
η3 = UnitConvert[η3i, "Millipascals"*"Seconds"]

```

Out[79]=  $(173.7 \pm 2.0) \text{ s mPa}$

Out[83]=  $(168.3 \pm 2.0) \text{ s mPa}$

Out[87]=  $(195.4 \pm 2.3) \text{ s mPa}$

Vu que  $\eta$  est une constante pour un liquide à une température donnée, on prend la moyenne pour la suite :

```

In[88]:= ηf = Mean[{η1,η2,η3}]
inηre = UnitConvert[ηf[[1]]["Uncertainty"]/ηf[[1]]["Value"],"Percent"]

```

Out[88]=  $(179.1 \pm 1.2) \text{ s mPa}$

Out[89]= 0.685675%

## Modèle 1

Calcul de formule pour le modèle.

```

In[90]:= volspm =  $\frac{4}{3} \pi * rm^3$ ;
mm =  $\rho_{acierm} * volspm$ ;

fpm = mm * gm;
fam =  $\rho_{glycm} * volspm * gm$ ;
ffm =  $6 * \pi * rm * \eta m * vm$ ;

Solve[Expand[atot mm == fpm - fam - ffm], atot]
|résous |développe
Out[95]=  $\left\{ \left\{ atot \rightarrow \frac{-9 vm \eta m + 2 gm rm^2 \rho_{acierm} - 2 gm rm^2 \rho_{glycm}}{2 rm^2 \rho_{acierm}} \right\} \right\}$ 

```

## Modèle 2

In[2092]=

```

gmp = 9.81;
ρaciermp = 7850;
ρglycmp = 1260;
ηmp = UnitConvert[ηf,"Pascals"*"Seconds"][[1]]["Value"];

rmp = 0.0015;
vop = 0;

const1 = 2 gmp rmp² ρaciermp - 2 gmp rmp² ρglycmp;
const2 = 2 rmp² ρaciermp;

Afun[v_] :=  $\left( \frac{-9 v \eta_{mp} + \text{const1}}{\text{const2}} \right)$ ;
Calcfun[v_,t_] := vop + t*Afun[v];

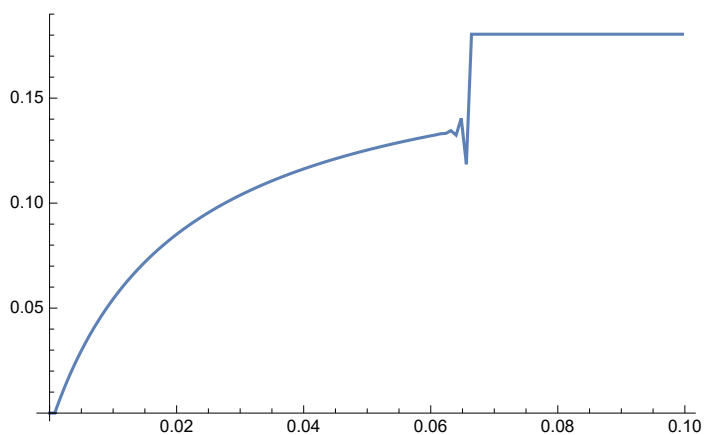
Solve[Afun[vlimtest] == 0,vlimtest]

vlimfun = 0.18044580728859538;
vlist = {vop};
tlist = {0};
Δtfun = 0.00081;
tfun = 0;
vfun = vop;
isfinish = False;
Do[{vfun = Calcfun[vfun, tfun], tfun = tfun + Δtfun, If[vfun ≤ vlimfun && isfinish == False, AppendTo[vlist, vfun], AppendTo[tlist, tfun]}];
ListLinePlot[Transpose[{tlist,vlist}]]

```

Out[2102]= {{vlimtest → 0.180446}}

Out[2111]=



## Modèle 3

Ne marche pas encore !!!

In[2130]:=

```

Afunm[v_] :=  $\left( \frac{-9 v \eta_{mp} + \text{const1}}{\text{const2}} \right);$ 
Calcfunm[v_, t_, i_] := i + t * Afunm[v];

Manipulate[
  {tlistm={0}, vlistm={vom}, isfinishm = False, vfunm=vom, tfunm=0,
  Do[
    {vfun = Calcfun[vfunm, tfunm, vom], tfunm = tfunm+0.1/tmax, If[vfunm ≤ vlimfun && isfinishm
    ListLinePlot[Transpose[{tlistm, vlistm}]]},
    {vom, 0, 1, 0.1}, {tmax, 0, 10000, 100}]

```

Out[2132]=

