

Q1

CoqIDE

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hw9.v

```

Lemma ex1: forall A, ~~A -> ~A.
Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.

```

1 goal
A : Prop
~ ~ ~ A -> ~ A (1/

Messages Errors Jobs

Ready, proving ex1 Line: 3 Char: 7 Offset: 46 0 / 0

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hw9.v

```

Lemma ex1: forall A, ~~A -> ~A.
Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.

```

1 goal
A : Prop
H : ~ ~ ~ A
~ A (1/

Messages Errors Jobs

Ready, proving ex1 Line: 4 Char: 7 Offset: 53 0 / 0

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hw9.v

```

Lemma ex1: forall A, ~~A -> ~A.
Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.

```

1 goal
A : Prop
H : ~ ~ ~ A
H0 : A

(1/
False

Messages Errors Jobs

Ready, proving ex1 Line: 5 Char: 7 Offset: 60 0 / 0

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hw9.v

```

Lemma ex1: forall A, ~~A -> ~A.
Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.

```

1 goal
A : Prop
H0 : A

(1/
~ ~ A

Messages Errors Jobs

Ready, proving ex1 Line: 6 Char: 12 Offset: 72 0 / 0

CoqIDE

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hw9.v

```

Lemma ex1: forall A, ~~A -> ~A.
Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.

```

1 goal
A : Prop
H0 : A
H : ~ A
False (1/

Messages Errors Jobs

Ready, proving ex1 Line: 7 Char: 7 Offset: 79 0 / 0

CoqIDE

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hw9.v

```

Lemma ex1: forall A, ~~A -> ~A.
Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.

```

1 goal
A : Prop
H0 : A
A (1/

Messages Errors Jobs

Ready, proving ex1 Line: 8 Char: 12 Offset: 91 0 / 0

CoqIDE

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hw9.v

```

Lemma ex1: forall A, ~~~A -> ~A.
Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
    
```

No more goals.

Messages Errors Jobs

Ready, proving ex1
 Line: 9 Char: 10 Offset: 101
 0 / 0

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hw9.v

```

Lemma ex1: forall A, ~~~A -> ~A.
Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
    
```

Messages Errors Jobs

Ready
 Line: 10 Char: 5 Offset: 106
 0 / 0

Q2

CoqIDE

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hw9.v

```

Lemma ex1: forall A, ~~A -> ~A.
Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A \/ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.

```

1 goal

```

forall A B : Prop,
A \/ B -> ~ [~ A /\ ~ B]

```

Messages Errors Jobs

Ready, proving ex2 Line: 12 Char: 46 Offset: 153 0 / 0

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hw9.v

```

Proof.
intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A \/ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.

```

1 goal

```

forall A B : Prop,
A \/ B -> ~ [~ A /\ ~ B]

```

Messages Errors Jobs

Ready, proving ex2 Line: 13 Char: 7 Offset: 160 0 / 0

CoqIDE

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hw9.v

```

intro.
intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A \ / B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.

```

```

1 goal
A : Prop

forall B : Prop,
A \ / B -> ~ (~ A /\ ~ B)

```

Messages Errors Jobs

Ready, proving ex2 Line: 14 Char: 7 Offset: 167 0 / 0

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hw9.v

```

intro.
intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A \ / B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.

```

```

1 goal
A, B : Prop

A \ / B -> ~ (~ A /\ ~ B)

```

Messages Errors Jobs

Ready, proving ex2 Line: 15 Char: 7 Offset: 174 0 / 0

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hw9.v

```

intro.
destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

```

```

1 goal
A, B : Prop
H : A /\ B
~ ( ~ A /\ ~ B )

```

Messages Errors Jobs

Ready, proving ex2 Line: 16 Char: 7 Offset: 181 0 / 0

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hw9.v

```

destruct H.
intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

```

```

1 goal
A, B : Prop
H : A /\ B
H0 : ~ A /\ ~ B
False

```

Messages Errors Jobs

Ready, proving ex2 Line: 17 Char: 7 Offset: 188 0 / 0

CoqIDE

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hw9.v

```

intro.
destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A \/ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),

```

1 goal
A, B : Prop
H : A \/ B
H0 : ~ A
H1 : ~ B

False

Messages Errors Jobs

Ready, proving ex2 Line: 18 Char: 13 Offset: 201 0 / 0

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hw9.v

```

destruct H.
apply H0.
Qed.

Lemma ex2: forall A B, A \/ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.

```

2 goals
A, B : Prop
H : A
H0 : ~ A
H1 : ~ B

False

False

Messages Errors Jobs

Ready, proving ex2 Line: 19 Char: 12 Offset: 213 0 / 0

CoqIDE

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hw9.v

```

apply H0.
Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.

```

2 goals
A, B : Prop
H : A
H1 : ~ B

A

False

Messages Errors Jobs

Ready, proving ex2 Line: 20 Char: 13 Offset: 226 0 / 0

CoqIDE

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hw9.v

```

Qed.

Lemma ex2: forall A B, A /\ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.

```

1 goal
A, B : Prop
H : B
H0 : ~ A
H1 : ~ B

False

Messages Errors Jobs

Ready, proving ex2 Line: 21 Char: 9 Offset: 235 0 / 0

CoqIDE

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hw9.v

```

Lemma ex2: forall A B, A /\ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.

```

```

1 goal
A, B : Prop
H : B
H0 : ~ A

```

Messages

Errors

Jobs

Ready, proving ex2
 Line: 22 Char: 13 Offset: 248
 0 / 0

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hw9.v

```

Lemma ex2: forall A B, A /\ B -> ~(~A /\ ~B).
Proof.
intro.
intro.
intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.

```

```

No more goals.

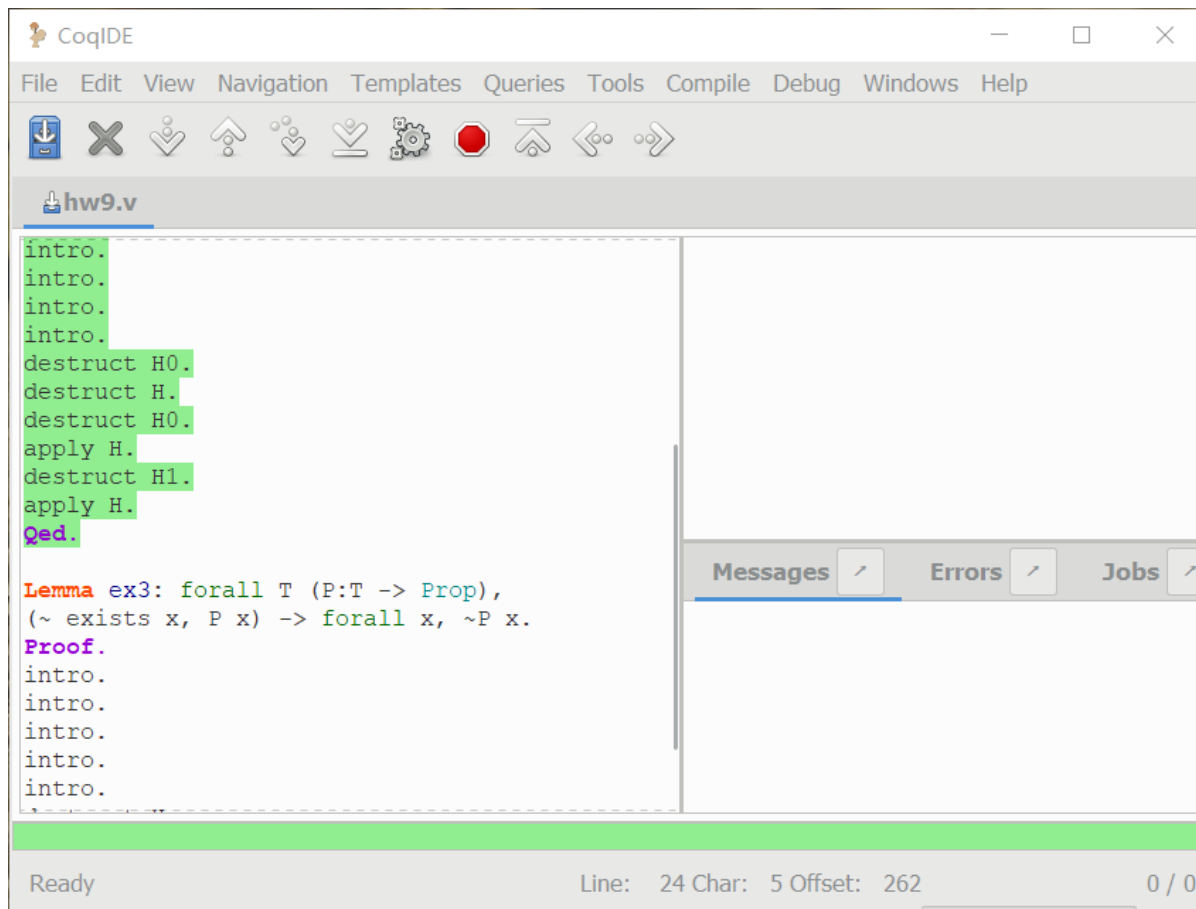
```

Messages

Errors

Jobs

Ready, proving ex2
 Line: 23 Char: 9 Offset: 257
 0 / 0



Q3

CoqIDE

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hw9.v

```

intro.
intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.

```

```

1 goal

forall (T : Type) (P : T -> Prop),
~ (exists x : T, P x) ->
forall x : T, ~ P x

```

Messages Errors Jobs

Ready, proving ex3
 Line: 27 Char: 37 Offset: 335
 0 / 0

CoqIDE

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hw9.v

```

intro.
destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.

```

```

1 goal

forall (T : Type) (P : T -> Prop),
~ (exists x : T, P x) ->
forall x : T, ~ P x

```

Messages Errors Jobs

Ready, proving ex3
 Line: 28 Char: 7 Offset: 342
 0 / 0

CoqIDE

File Edit View Navigation Templates Queries Tools Compile Debug Windows Help

hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
  (~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.
```

```

1 goal
T : Type

forall P : T -> Prop,
~ (exists x : T, P x) ->
forall x : T, ~ P x
```

Messages

Errors

Jobs

Ready, proving ex3
 Line: 29 Char: 7 Offset: 349
 0 / 0

CoqIDE

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hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
  (~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.
```

```

1 goal
T : Type
P : T -> Prop

~ (exists x : T, P x) ->
forall x : T, ~ P x
```

Messages

Errors

Jobs

Ready, proving ex3
 Line: 30 Char: 7 Offset: 356
 0 / 0

CoqIDE

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hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.

```

```

1 goal
T : Type
P : T -> Prop
H : ~ (exists x : T, P x)

forall x : T, ~ P x

```

Messages Errors Jobs

Ready, proving ex3 Line: 31 Char: 7 Offset: 363 0 / 0

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hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.

```

```

1 goal
T : Type
P : T -> Prop
H : ~ (exists x : T, P x)
x : T

~ P x

```

Messages Errors Jobs

Ready, proving ex3 Line: 32 Char: 7 Offset: 370 0 / 0

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hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.

```

```

1 goal
T : Type
P : T -> Prop
H : ~ (exists x : T, P x)
x : T

~ P x

```

Messages Errors Jobs

Ready, proving ex3 Line: 32 Char: 7 Offset: 370 0 / 0

CoqIDE

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hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.

```

```

1 goal
T : Type
P : T -> Prop
H : ~ (exists x : T, P x)
x : T
H0 : P x

False

```

Messages Errors Jobs

Ready, proving ex3 Line: 33 Char: 7 Offset: 377 0 / 0

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hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.

```

1 goal
T : Type
P : T -> Prop
x : T
H0 : P x

exists x0 : T, P x0

Messages Errors Jobs

Ready, proving ex3 Line: 34 Char: 12 Offset: 389 0 / 0

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hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.

```

1 goal
T : Type
P : T -> Prop
x : T
H0 : P x

P x

Messages Errors Jobs

Saved Line: 35 Char: 10 Offset: 399 0 / 0

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hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.

```

No more goals.

Messages

Errors

Jobs

Ready, proving ex3
 Line: 36 Char: 10 Offset: 409
 0 / 0

CoqIDE

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hw9.v

```

destruct H0.
destruct H.
destruct H0.
apply H.
destruct H1.
apply H.
Qed.

Lemma ex3: forall T (P:T -> Prop),
(~ exists x, P x) -> forall x, ~P x.
Proof.
intro.
intro.
intro.
intro.
intro.
destruct H.
exists x.
apply H0.
Qed.

```

Messages

Errors

Jobs

Ready
 Line: 37 Char: 5 Offset: 414
 0 / 0

Appendix-source code

Q1

```
Lemma ex1: forall A, ~~~A → ~A.  
Proof.  
  intro.  
  intro.  
  intro.  
  destruct H.  
  intro.  
  destruct H.  
  apply H0.  
Qed.
```

Q2

```
Lemma ex2: forall A B, A ∨ B → ~(~A ∧ ~B).  
Proof.  
  intro.  
  intro.  
  intro.  
  intro.  
  destruct H0.  
  destruct H.  
  destruct H0.  
  apply H.  
  destruct H1.  
  apply H.  
Qed.
```

Q3

```
Lemma ex3: forall T (P:T → Prop),  
  (~ exists x, P x) → forall x, ~P x.  
Proof.  
  intro.  
  intro.  
  intro.  
  intro.  
  intro.
```

```
destruct H.  
exists x.  
apply H0.  
Qed.
```