

# A Generic Construction of Dynamic Single Sign-on with Strong Security

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**Abstract.** Single Sign-On (SSO) is a core component in a federated identity management (FIM). Dynamic Single Sign-on (DSSO) is a more flexible SSO where users can change their service requirements dynamically. However, the security in the current SSO and DSSO systems remain questionable. As an example, personal credentials could be illegally used to allow illegal users to access the services. It is indeed a challenging task to achieve strong security in SSO and DSSO. In this paper, we propose a generic construction of DSSO with strong security. We propose the formal definitions and security models for SSO and DSSO, which enable one to achieve the security of SSO and DSSO with the underlying (standard) security assumptions. We also provide a formal security proof on our generic DSSO scheme.

**Keywords:** Single Sign-on, Authentication, Security.

## 1 Introduction

With an increasing use of personalized/protected services, users need to maintain more and more usernames and the corresponding passwords in order to access the entitled services. This imposes a burden on users. Single Sign-on (SSO) provides a good remedy to this problem, as it allows a single password to be used to access multiple services. A traditional SSO system comprises three entities: an identity provider (IdP), a group of users (Us) and a group of service providers (SPs). The IdP manages the user's personally identifiable information (PII), authenticates network users and issues credentials to them. SPs provide services to users once they are authenticated by the IdP. SSO is a system where a user authenticates himself to the IdP and can access the designated SPs without the need for further authentication [24]. SSO can shift the great administrative burden of the numerous users profiles from SPs to the IdP. Hence, SSO plays a core role in the federated identity management (FIM) where the exchange of the user's identity-related information can be optimized [5].

Unfortunately, current SSO systems have some obvious flaws. For instance, they are fragile to resist single point of failure [16,22,23]. The main reason for this

is that the IdP must always be online, otherwise users cannot be granted services from SPs. They are not well protected from illegally using a personal credential, where a credential could be used for an illegitimate user to gain the services which should not be accessed by him. These systems are subject to impersonation attacks. When a password is compromised, the attacker can impersonate the user and log in using the compromised account. This is mainly due to the missing of individual participation principle provided in the thirteenth principle of Organization for Economic CO-Operation and Development (OECD) [20] and the missing of the user control and consent principle for the laws of identity [6]. All these flaws stem from the lack of active/dynamic control over the process by the user, after the user has entered the correct password. In the following, we review some existing SSO systems. Although those systems provide elegant solutions to SSO, they suffer from various attacks.

Released 1999, Microsoft .NET Passport is one of the most widely deployed SSO systems, where a passport server acts as the IdP [22]. It uses cookies to store and convey user's PII. When a user access to an SP, the SP redirects the user to the passport server for authentication. After authentication, the passport server creates three cookies: ticket cookie, profile cookie and visited sits cookie. The ticket cookie contains the unique identifier and a timestamp. The profile cookie consists of the user's profile information. The visited sits cookie contains the lists sites the user has accessed. All cookies created by the passport server are encrypted with the triple DES encryption algorithm under the shared key between the passport server and all SPs. The passport server sends these cookies to the user. The user redirects them to the SP. The SP decrypts the cookies and obtains the user's authentication information. .Net Passport incurs some attacks, such as single point of failure, key management failure, misuse of cookies, etc. [16,22,23].

In September 2001, the Liberty Alliance Project was launched [17]. This project was aimed to create an open, federated, SSO solution for the digital economy via any device connected to the Internet. The Liberty project does not use cookies to transfer information between IdPs and SPs. Instead, it transfers information through HTTP redirects and URL encodings. In Liberty Alliance, an SSO Service (SSOS) provides users an Identity Web Services Framework (ID-WSF)-based means to obtain Liberty authentication assertions enabling them to interact with SPs [18]. In this system, the user only shows his credentials to the SP, without proving the ownership of them. Therefore, it is unable to prevent credential transfer, namely the user can share his credentials with other illegal users.

Proposed in 2005, OpenID is an open, decentralized standard for authenticating users. In OpenId, users are allowed to access to different services with the same digital identity where the SPs trust the IdP. OpenID solves the problem without relying on any centralized IdP to confirm digital identity. There are more than one IdP in OpenID system, users can get their OpenID from any IdP in the system. OpenID can be used as an effective mean for cross company authentication as well as for SSO. OpenID has two major modes of operation: Dumb

mode and Smart mode [21,28]. In the Dumb mode, the SP needs to compare the authentication assertion received from the user with the initial one stored in the IdP to prevent the malicious attackers. While in the Smart mode, the IdP encrypts the authentication assertion under the shared key between the SP and the IdP. Therefore, in both modes, the IdP must always be online to enable users authentication.

In 2003, Pahalidis and Mitchell presented a taxonomy of SSO system [24]. They divided SSO systems into four categories: local pseudo-SSO systems, proxy-based pseudo-SSO systems, local true SSO systems and proxy-based true SSO systems. They designed two SSO systems based on trusted platforms and GSM/UMTS, respectively [25,26]. In order to resolve the single point of failure, two distributed SSO systems Cornell SSO (CorSSO) and Threshold Passport (ThresPassport) were proposed by Josephson and Chen in 2004 and 2005, respectively [7,15]. In these systems, the authentication key is split into  $n$  different shares, and each share is sent to an authentication server. Only authenticated by at least  $t$  authentication servers, can the user get services from an SP. Recently, user-centric federated identity management systems have been proposed to protect user's PII [30,27]. In 2009, based on a private credential mechanism, Suriadi and Foo proposed a user-centric federated SSO system (UFed SSO), in which the user can minimize the release of his PII [31]. Although, every system mentioned above has its merits, they did not provide a security proof.

In 2006, Bhargav-Spantzel and Camenisch [30] proposed a taxonomy and raised some open issues on user centric federated identity management systems. They classified the existing systems into two predominant variants: credential-focused systems and relation-focused systems. In credential-focused systems, the IdPs must be offline and issue long-term credentials. While in relationship-focused systems, users need to maintain the relationship with the online IdPs that create short-term credentials for them during transactions. They defined an universal user centric FIM which should have long-term as well as short-term credentials, online and offline IdP. However, this scheme has not been investigated thoroughly.

### *Our Contribution*

In this paper, we propose a novel dynamic SSO scheme, which resists against all the previously described attacks. We formalize the definitions and the security models for SSO and DSSO. It is the first time that the formal definitions and security models for SSO and DSSO are formally defined. We give a generic construction of DSSO systems based on three building blocks: (1) CCA-secure broadcast encryption, (2) strongly existentially unforgeable signature, and (3) zero knowledge proof. We provide a formal security proof for our generic construction.

### *Paper Organization*

The rest of this paper is organized as follows. In Section 2, we propose the formal definitions and security models for SSO and DSSO. We review the three building blocks which are used to construct DSSO in Section 3. In Section 4, a generic

construction for DSSO is described. In Section 5, we reduce the security of our construction to the underlying assumptions. Section 6 concludes this paper.

## 2 Formal Definitions and Security Models

In this section, we provide a formal definition and a security model for SSO and DSSO.

### 2.1 Single Sign-on

In SSO systems, a user needs to authenticate himself to the IdP once for access to multiple SPs without the need to re-authentication. In order to protect the PII of the user, an ideal SSO system should satisfy the basic requirement that only the intended SPs can check the user's PII. Now we formalise the definition of SSO as follows:

**Definition 1.** *A Single Sign-on system consists of five algorithms: system setup algorithm  $\text{Setup}(\cdot)$ , enrollment algorithm  $\text{Enrol}(\cdot)$ , credential generation algorithm  $\text{CreGen}(\cdot)$ , credential verification algorithm  $\text{CreVer}(\cdot)$ , and proof of knowledge algorithm  $\text{PK}(\cdot)$ .*

- $\text{Setup}(\lambda)$ : Taking as input a security parameter  $\lambda \in \mathbb{N}$ , it returns public parameters  $PP$  and a public-secret key pair  $(K_{IP}, K_{IS}) \leftarrow \mathcal{G}(1^\lambda)$  for the IdP.
- $\text{Enrol}(PP, RI)$ : Taking as input public parameters  $PP$ ,  $SP_i$ 's registration information  $RI_{SP_i}$  or  $U$ 's registration information  $RI_U$ , it returns  $(ID_{SP_i}, K_{SP_i})$  to  $SP_i$ , and  $(ID_U, A_U)$  to  $U$ , where  $ID_{SP_i}$  and  $ID_U$  are the identifiers of  $SP_i$  and  $U$  in the circle of trust (CoT)<sup>1</sup>,  $K_{SP_i}$  is  $SP_i$ 's verification key and  $A_U$  is  $U$ 's access right which is a set consisting of the identifiers of the service providers that the user has selected.  $U$  generates his public-secret key pair  $(K_{UP}, K_{US}) \leftarrow \mathcal{G}(1^\lambda)$ .
- $\text{CreGen}(K_{IS}, M_U, ID_U, T_U, K_{UP}, PP)$ : Taking as input the IdP's secret key  $K_{IS}$ , an authentication assertion  $M_U$ , user's identifier  $ID_U$ , user's public key  $K_{UP}$ , a timestamp  $T_U$  and public parameters  $PP$ , it returns a credential  $Cre_U$ .
- $\text{CreVer}(K_{SP_i}, Cre_U, M_U, ID_U, K_{UP}, T_U, K_{IP}, PP)$ : Taking as input the service provider  $SP_i$ 's verification key  $K_{SP_i}$ , the user's credential  $Cre_U$ , the authentication assertion  $M_U$ , the user's identifier  $ID_U$ , user's public key  $K_{UP}$ , IdP's public key  $K_{IP}$ , the timestamp  $T_U$  and public parameters  $PP$ , it returns *True* if and only if the service provider  $ID_{SP_i} \in A_U$  and the credential  $Cre_U$  is created by the IdP. Otherwise it returns *False*.
- $\text{PK}((K_{US}, K_{UP}), \gamma)$ : Taking as input the user's public-secret key pair  $(K_{UP}, K_{US})$  and a random number  $\gamma$ , it returns a number  $s$  such that  $\text{Accept} \leftarrow \text{PKVer}(s, K_{UP}, \gamma)$  if and only if  $K_{US}$  is the user's secret key corresponding to the public key  $K_{UP}$ , where  $\text{PKVer}(\cdot)$  is the verification algorithm in the proof of knowledge. Otherwise it returns *Reject*.

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<sup>1</sup> A circle of trust consists of the identity provider and service providers, where each service provider trusts the identity provider.

## 2.2 The Security of Single Sign-on

In SSO systems, three types of attacks should be considered: collusion credential forging attacks, collusion impersonation attacks and coalition credential forging attacks. In the collusion credential forging attacks, malicious users can collaboratively forge a credential for the target user. They can impersonate the target one to get services from the service providers whose identifiers are listed in the forged credential. In the collusion impersonation attacks, we assume that the malicious service providers have checked the credentials of a user and therefore obtained the corresponding proof information on the user. Hence, malicious service providers can collaboratively mimic the owner of the credentials. In the coalition credential forging attacks, malicious users and service providers can collaboratively forge a credential for the target user, in which the identifiers of the malicious service providers are not included.

In order to formalise our notions of security for SSO systems, we define a series of games between two Turing machines: Challenger and Adversary  $\mathcal{A}$ .

**Game 1: Collusion Credential Forging Attacks.**

**Init.** Let  $\mathcal{A}$  be all malicious users.  $\mathcal{A}$  begins by outputting the target user  $U^*$  for whom it wants to forge a credential.

**Setup.** The challenger runs  $\text{Setup}(\lambda)$  to generate the public parameter  $PP$  and the public-private key pair  $(K_{IP}, K_{IS})$ . It sends  $\mathcal{A}$  the public parameter  $PP$  and the public key  $K_{IP}$ .

**Enrollment queries.**  $\mathcal{A}$  can adaptively issue enrollment queries  $\{RI_{U_1}, RI_{U_2}, \dots, RI_{U_{qe}}\}$ , where  $RI_{U_i} \neq RI_{U^*}$ ,  $qe \leq (|\mathbb{U}| - 1)$ ,  $\mathbb{U}$  is the set consists of all users in the CoT. The challenger returns  $\{(ID_{U_1}, A_{U_1}), (ID_{U_2}, A_{U_2}), \dots, (ID_{U_{qe}}, A_{U_{qe}})\}$ .

**Credential generation queries.**  $\mathcal{A}$  can adaptively issue credential generation queries  $\{(ID_{U_1}, K_{UP_1}), (ID_{U_2}, K_{UP_2}), \dots, (ID_{U_{qc_1}}, K_{UP_{qc_1}})\}$ , where  $(ID_{U_i}, K_{UP_i}) \neq (ID_{U^*}, K_{UP^*})$ . The challenger returns  $\{Cre_{U_1}, Cre_{U_2}, \dots, Cre_{U_{qc_1}}\}$ .

**Credential verification queries.**  $\mathcal{A}$  can adaptively issue credential verification queries  $\{(ID_{U_1}, K_{UP_1}, Cre_{U_1}), (ID_{U_2}, K_{UP_2}, Cre_{U_2}), \dots, (ID_{U_{qc_2}}, K_{UP_{qc_2}}, Cre_{U_{qc_2}})\}$ . Upon receiving a query, the challenger returns *True* or *False*.

**Output.**  $\mathcal{A}$  outputs a credential  $Cre_{U^*}^*$  for  $U^*$ .  $\mathcal{A}$  wins the game if

1.  $True \leftarrow \text{CreVer}(K_{SP_i}, Cre_{U^*}^*, ID_{U^*}^*, K_{UP^*}^*, T_{U^*}^*, K_{IP}, PP)$  and
2.  $(ID_{U^*}^*, Cre_{U^*}^*) \notin \{(ID_{U_1}, Cre_{U_1}), (ID_{U_2}, Cre_{U_2}), \dots, (ID_{U_{qc_1}}, Cre_{U_{qc_1}})\}$ .

**Definition 2.** A Single Sign-on system is  $(t, qe, qc_1, qc_2, \epsilon)$ -secure against collusion credential forging attacks if no  $t$ -time adversary, who makes at most  $qe$  enrollment queries,  $qc_1$  credential generation queries and  $qc_2$  credential verification queries, has advantage at least  $\epsilon$  in Game 1.

**Game 2. Collusion Impersonate Attacks.**

**Init.** Let  $\mathcal{A}$  be all malicious service providers in the CoT.  $\mathcal{A}$  begins by outputting a user  $U^*$  whom it wants to impersonate.

**Setup.** The challenger runs  $\text{Setup}(\lambda)$  to obtain the public parameters  $PP$  and the public-secret key pair  $(K_{IP}, K_{IS})$ . It sends  $\mathcal{A}$  the public parameter  $PP$  and the public key  $K_{IP}$ .

**Proof of Knowledge queries.**  $\mathcal{A}$  can adaptively issues proof of knowledge queries  $\{(K_{UP_1}, \gamma_1), (K_{UP_2}, \gamma_2), \dots, (K_{UP_{qp}}, \gamma_{qp})\}$ , where  $K_{UP_i} \neq K_{UP}^*$ . The challenger returns  $\{s_1, s_2, \dots, s_{qp}\}$ .

**Challenge.** The challenger sends a challenge  $(K_{UP}^*, \gamma^*)$  to  $\mathcal{A}$ .

**Output.**  $\mathcal{A}$  outputs  $s^*$ .  $\mathcal{A}$  wins the game if

1.  $\text{Accept} \leftarrow \text{PKVer}(s^*, K_{UP}^*, \gamma^*)$  and
2.  $K_{UP}^* \notin \{K_{UP_1}, K_{UP_2}, \dots, K_{UP_{qp}}\}$ .

**Definition 3.** A Single Sign-on system is  $(t, qp, \epsilon)$ -secure against collusion impersonation attacks if no  $t$ -time adversary, who makes at most  $qp$  proof of knowledge queries, has advantage at least  $\epsilon$  in Game 2.

**Game 3: Coalition Credential Forging Attacks.**

**Init.** Let  $\mathcal{A}$  be the coalition, which consists of all malicious users and service providers.  $\mathcal{A}$  begins by outputting a user  $U^*$  that it wants to impersonate and a service provider  $SP^*$  that it wants to attack.

**Setup.** The challenger runs  $\text{Setup}(\lambda)$  to generate the public parameters  $PP$  and the public-secret key pair  $(K_{IP}, K_{IS})$ . It sends  $\mathcal{A}$  the public parameter  $PP$  and the public key  $K_{IP}$ .

**Enrollment queries.**  $\mathcal{A}$  can adaptively issue enrollment queries  $\{RI_{U_1}, RI_{U_2}, \dots, RI_{U_{qe_1}}\}$  and  $\{RI_{SP_1}, RI_{SP_2}, \dots, RI_{SP_{qe_2}}\}$ , where  $RI_{U_i} \neq RI_U^*$ ,  $RI_{SP_i} \neq RI_{SP}^*$ ,  $qe_1 \leq (|\mathbb{U}| - 1)$ ,  $qe_2 \leq (|\mathbb{SP}| - 1)$ ,  $\mathbb{SP}$  is the set consists of all service providers in the CoT, and  $qe_1 + qe_2 = qe$ . The challenger returns  $\{(ID_{U_1}, A_{U_1}), (ID_{U_2}, A_{U_2}), \dots, (ID_{U_{qe_1}}, A_{U_{qe_1}})\}$  and  $\{(ID_{SP_1}, K_{SP_1}), (ID_{SP_2}, K_{SP_2}), \dots, (ID_{SP_{qe_2}}, K_{SP_{qe_2}})\}$ .

**Credential generation queries.**  $\mathcal{A}$  can adaptively issue credential generation queries  $\{(ID_{U_1}, K_{UP_1}), (ID_{U_2}, K_{UP_2}), \dots, (ID_{U_{qc_1}}, K_{UP_{qc_1}})\}$ , where  $(ID_{U_i}, K_{UP_i}) \neq (ID_U^*, K_{UP}^*)$ . The challenger returns  $\{Cre_{U_1}, Cre_{U_2}, \dots, Cre_{U_{qc_1}}\}$ .

**Credential verification queries.**  $\mathcal{A}$  can adaptively issue credential verification queries  $\{(ID_{U_1}, K_{UP_1}, Cre_{U_1}), (ID_{U_2}, K_{UP_2}, Cre_{U_2}), \dots, (ID_{U_{qc_2}}, K_{UP_{qc_2}}, Cre_{U_{qc_2}})\}$ . The challenger returns *True* or *False*.

**Output.**  $\mathcal{A}$  outputs a credential  $Cre_U^*$ .  $\mathcal{A}$  wins the game if

1.  $\text{True} \leftarrow \text{CreVer}(K_{SP}^*, Cre_U^*, M_U^*, ID_U^*, K_{UP}^*, T_U^*, K_{IP}, PP)$ .

2.  $(ID_U^*, Cre_U^*) \notin \{(ID_{U_1}, Cre_{U_1}), (ID_{U_2}, Cre_{U_2}), \dots, (ID_{U_{qc_1}}, Cre_{U_{qc_1}})\}$ .
3.  $ID_{SP}^* \in A_U^*$  and  $ID_{SP} \notin A_U^*$  if  $SP \in \mathcal{A}$ .

**Definition 4.** A Single Sign-on system is  $(t, qe, qc_1, qc_2, \epsilon)$ -secure against coalition credential forging attacks if no  $t$ -time adversary, who makes at most  $qe$  enrollment queries,  $qc_1$  credential generation queries, and  $qc_2$  credential verification queries, has advantage at least  $\epsilon$  in the Game 3.

### 2.3 Dynamic Single Sign-on

DSSO is an SSO system in which the user can change his choice dynamically. We formalise the definition of DSSO as follows:

**Definition 5.** A dynamic single sign-on system (DSSO) consists of seven algorithms:  $\text{Setup}(\cdot)$ ,  $\text{Enrol}(\cdot)$ ,  $\text{CreGen}(\cdot)$ ,  $\text{CreVer}(\cdot)$ ,  $\text{PK}(\cdot)$ , an addition algorithm  $A(\cdot)$  and a deletion algorithm  $D(\cdot)$ . Where  $\text{Setup}(\cdot)$ ,  $\text{Enrol}(\cdot)$ ,  $\text{CreGen}(\cdot)$ ,  $\text{CreVer}(\cdot)$  and  $\text{PK}(\cdot)$  are the same as in definition 1.

- $A(ID_{SP})$  : Taking as input the service provider  $SP$ 's identifier  $ID_{SP}$ , it returns  $A_U \leftarrow A_U \cup \{ID_{SP}\}$ .
- $D(ID_{SP})$  : Taking as input the service provider  $SP$ 's identifier  $ID_{SP}$ , it returns  $A_U \leftarrow A_U \setminus \{ID_{SP}\}$ .

### 2.4 The Security of Dynamic Single Sign-on

In multiple parties communication and dynamic schemes, because the participants can join or leave frequently, two special attacks should be addressed, namely forward security and backward security. In DSSO, users can be added to or revoked from a service dynamically; therefore a secure DSSO system can resist these attacks. By forward security, we mean that the  $SP$  can not validate the credentials, which were issued before he is added to the user's access right  $A_U$ . By backward security, we mean that the service providers can not validate the credentials, which are issued after he has been removed from the the user's access right  $A_U$ . We formalise these two attacks by the following games.

**Game 4: Forward Security.**

**Setup.** Let  $\mathcal{A}$  be malicious service providers. The challenger runs  $\text{Setup}(\lambda)$  to generate the public parameters  $PP$  and the public-secret key pair  $(K_{IP}, K_{IS})$ . It sends  $\mathcal{A}$  the public parameter  $PP$  and the public key  $K_{IP}$ .

**Credential verification queries.**  $\mathcal{A}$  can adaptively issue credential verification queries  $\{(ID_{U_1}, K_{UP_1}, Cre_{U_1}), (ID_{U_2}, K_{UP_2}, Cre_{U_2}), \dots, (ID_{U_{qc}}, K_{UP_{qc}}, Cre_{U_{qc}})\}$ , which were issued after  $\mathcal{A}$  has been joined to  $A_U$ . The challenger returns *True* or *False*.

**Challenge.** The challenger sends to  $\mathcal{A}$  an old credential  $Cre_U^O$ , which was issued before he is joined to  $A_U$ .

**Output.**  $\mathcal{A}$  outputs *True* or *False*.  $\mathcal{A}$  wins the game if his answer on  $Cre_U^O$  is correct.

**Definition 6.** A *Dynamic Single Sign-on system* is  $(t, qc, \epsilon)$ -forward secure if no  $t$ -time adversary, who makes at most  $qc$  credential verification queries, has advantage at least  $\epsilon$  in the Game 4.

**Game 5: Backward Security.**

**Setup.** Let  $\mathcal{A}$  be malicious service providers. The challenger runs  $\text{Setup}(\lambda)$  to generate the public parameters  $PP$  and the public-secret key pair  $(K_{IP}, K_{IS})$ . It sends  $\mathcal{A}$  the public parameter  $PP$  and the public key  $K_{IP}$ .

**Credential verification queries.**  $\mathcal{A}$  can adaptively issue credential verification queries  $\{(ID_{U_1}, K_{UP_1}, Cre_{U_1}), (ID_{U_2}, K_{UP_2}, Cre_{U_2}), \dots, (ID_{U_{qc}}, K_{UP_{qc}}, Cre_{U_{qc}})\}$ , which were issued before  $\mathcal{A}$  is deleted from  $A_U$ . The challenger returns *True* or *False*.

**Challenge.** The challenger sends  $\mathcal{A}$  a new credential  $Cre_U^N$  which was issued after he has been deleted from  $A_U$ .

**Output.**  $\mathcal{A}$  outputs *True* or *False*.  $\mathcal{A}$  wins the game if his answer on  $Cre_U^N$  is correct.

**Definition 7.** A *Dynamic Single Sign-on system* is  $(t, qc, \epsilon)$ -backward secure if no  $t$ -time adversary, who makes at most  $qc$  credential verification queries, has advantage at least  $\epsilon$  in the Game 5.

### 3 Building Blocks

In this section, we provide three building blocks, which are used to construct DSSO systems.

#### 3.1 Broadcast Encryption System

The notion of broadcast encryption was proposed by Fiat and Naor in 1993 [10]. A broadcast encryption system consists of three randomized algorithms:

- **Setup**( $n, \lambda$ ): Taking as input the number of receivers  $n$  and security parameter  $\lambda$ , it outputs  $n$  secret keys  $K_{R1}, K_{R2}, \dots, K_{Rn}$  and public parameters  $PP_B$ .
- **Encrypt**( $S, PP_B$ ): Taking as input a subset  $S \subseteq \{ID_1, ID_2, \dots, ID_n\}$  and public parameters  $PP_B$ , it outputs a pair  $(Hdr, K)$ , where  $Hdr$  is called the header and  $K \in \mathcal{K}$  is a message encryption key.  $(S, Hdr)$  is often called the full header.
- **Decrypt**( $Hdr, K_{Ri}, PP_B$ ): Taking as input the header  $Hdr$ , the secret key  $K_{Ri}$  for the receiver  $ID_i \in S$  and the public parameter  $PP_B$ , it outputs the message encryption key  $K \in \mathcal{K}$ .



### 3.2 Chosen Ciphertext Security of Broadcast Encryption System

The chosen ciphertext security of broadcast encryption system is defined using the following game between a challenger and an adversary  $\mathcal{A}$  [1,9].

**Init.** The adversary  $\mathcal{A}$  outputs a receivers set  $S^* \subseteq \{ID_1, ID_2, \dots, ID_n\}$  which he wants to attack.

**Setup.** The challenger runs  $\text{Setup}(n, \lambda)$  to generate secret keys  $K_{R1}, K_{R2}, \dots, K_{Rn}$  and public parameters  $PP_B$ . It sends  $\mathcal{A}$  all secret key  $K_{Ri}$  for  $ID_i \notin S^*$ .

**Query phase 1.**  $\mathcal{A}$  issues decryption queries  $q_1, q_2, \dots, q_t$ , where  $q_i = (Hdr, ID_i)$ ,  $ID_i \in S^*$ . The challenger responds with  $\text{Decrypt}(Hdr, K_{Ri}, PP_B)$ .

**Challenge.** The challenger runs algorithm  $\text{Encrypt}(S^*, PP_B)$  to obtain  $(Hdr^*, K)$ , where  $K \in \mathcal{K}$ . The challenger chooses a random  $b \in \{0, 1\}$ . It sets  $K_b = K$  and chooses a random  $K_{1-b} \in \mathcal{K}$ . It sends  $(Hdr^*, K_0, K_1)$  to  $\mathcal{A}$ .

**Query phase 2.**  $\mathcal{A}$  can adaptively issue decryption queries  $q_{t+1}, q_{t+2}, \dots, q_d$ , where  $q_j = (Hdr, ID_j)$ ,  $ID_j \in S^*$ . The only constraint is that  $Hdr \neq Hdr^*$ . The challenger returns  $\text{Decrypt}(Hdr, K_{Ri}, PP_B)$ .

**Guess.**  $\mathcal{A}$  outputs its guess  $b' \in \{0, 1\}$  for  $b$ .  $\mathcal{A}$  wins the game if  $b = b'$ .

**Definition 8.** A broadcast encryption system is  $(t, n, q_d, \epsilon)$  CCA-secure if no  $t$ -time adversary  $\mathcal{A}$ , who makes at most  $q_d$  decryption queries, has advantage at least  $\epsilon$  in the above game.

### 3.3 Signature Scheme

Digital signature scheme was proposed by Diffie and Hellman [8]. A signature scheme consists of four algorithms:

- **Setup**( $\gamma$ ): Taking as input the security parameter  $\gamma$ , it outputs the public parameters  $PP_S$ .
- **KeyGen**( $\gamma, PP_S$ ): Taking as input the security parameter  $\gamma$  and the public parameters  $PP_S$ , it outputs a public-secret key pair  $(K_S, K_P)$ .
- **Sign**( $K_S, m, PP_S$ ): Taking as input the secret key  $K_S$ , a message  $m$  and the public parameters  $PP_S$ , it outputs a publicly verifiable signature  $\sigma$ .
- **Ver**( $m, \sigma, K_P, PP_S$ ): Taking as input the message  $m$ , the signature  $\sigma$ , the public key  $K_P$  and the public parameters  $PP_S$ , it outputs *True* if the signature is correct. Otherwise it outputs *False*.

### 3.4 Strong Unforgeability of Signature

A digital signature system is said to be secure if it is existentially unforgeable under a chosen-message attack [2,13]. The strong unforgeability of signature is defined using the following game between a challenger and an adversary  $\mathcal{A}$ .

**Setup.** The challenger runs  $\text{Setup}(\gamma)$  and  $\text{KeyGen}(\gamma, PP_S)$  to generate the public parameters  $PP_S$  and a public-secret key pair  $(K_P, K_S)$ . It sends public parameters  $PP_S$  and public key  $K_P$  to  $\mathcal{A}$ .

**Signature queries.**  $\mathcal{A}$  can adaptively issue up to  $qs$  signature queries  $\{m_1, m_2, \dots, m_{qs}\}$ . To each query  $m_i$ , the challenger runs algorithm  $\text{Sign}(K_S, m_i, PP_S)$  to produce the corresponding signature  $\sigma_i$ . The challenger responds with message-signature pairs  $\{(m_1, \sigma_1), (m_2, \sigma_2), \dots, (m_{qs}, \sigma_{qs})\}$ .

**Output.**  $\mathcal{A}$  outputs a message-signature pair  $(m^*, \sigma^*)$ .  $\mathcal{A}$  wins the game if

1.  $\text{True} \leftarrow \text{Ver}(m^*, \sigma^*, K_P, PP_S)$  and
2.  $(m^*, \sigma^*) \notin \{(m_1, \sigma_1), (m_2, \sigma_2), \dots, (m_{qs}, \sigma_{qs})\}$ .

**Definition 9.** A signature is  $(t, qs, \epsilon)$ -strongly existentially unforgeable under adaptive chosen-message attacks if no  $t$ -time adversary, who makes at most  $qs$  signature queries, has advantage at least  $\epsilon$  in the above game.

### 3.5 Zero Knowledge Proof

Zero knowledge proof (ZKP) was introduced by Goldwasser, Micali and Rackoff in 1985 [14]. It is an interactive protocol by which a prover  $P$  (Peggy) can convince a verifier  $V$  (Victor) that he knows a secret without revealing any information about it to  $V$ . The formal definition of zero knowledge proof is as follows:

**Definition 10.** Let  $(P, V)$  be a pair of Turing machines and  $V$  is polynomially bounded.  $P$  and  $V$  share the same input and can interact with each other. Let  $L$  be a language. We say that a pair  $(P, V)$  is zero knowledge proof system, if  $P$  and  $V$  satisfy the following properties:

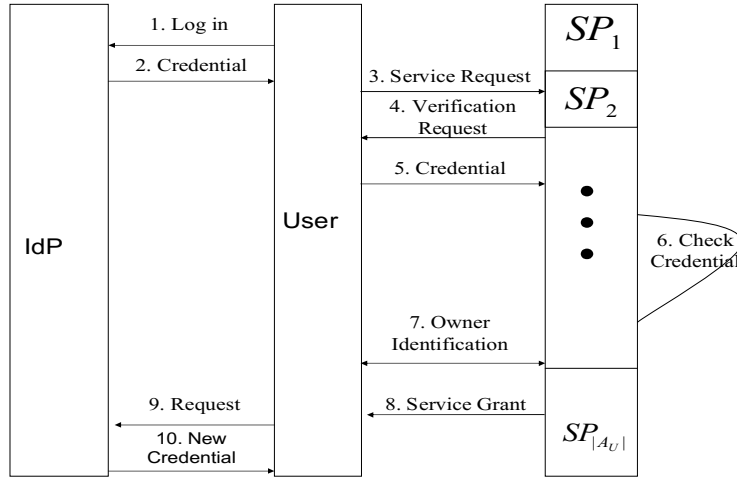
- **Completeness:** For any input  $x \in L$  to  $(P, V)$ ,  $\Pr[s \leftarrow (P, V)(x), V(x, s) = 1] \geq 1 - \frac{1}{n^k}$ , for each  $k$  and sufficiently large  $n$  which denotes the length of the input.
- **Soundness:** For any  $x \notin L$ , and any prover  $P'$ ,  $\Pr[s \leftarrow (P', V)(x), V(x, s) = 1] < \frac{1}{n^k}$ .
- **Zero-knowledge:** For any  $x \in L$ , and any verifier  $V'$ , there exists a simulator  $S$  such that two distribution  $S_{V'}(x)$  and  $\text{View}_{V'}(x)$  are computationally indistinguishable.

Any language in  $\mathcal{NP}$  has an interactive zero knowledge proof system [11,12]. Let  $(P, V)$  be an interactive zero knowledge proof system. By  $(P, V)(x)$  we denote that the prover  $P$  executes an interactive zero knowledge proof protocol with the verifier  $V$  to prove that he knows the secret corresponding to  $x$ .

## 4 Generic Construction for Dynamic Single Sign-on

Our generic construction for DSSO consists of three building blocks: a CCA-secure broadcast encryption scheme  $\text{BroEnc}(\cdot)$ , a strongly unforgeable signature

scheme  $\text{Sign}(\cdot)$  and a zero knowledge proof scheme  $(P,V)(\cdot)$ . In our construction, users can change their choices dynamically, while other participants (users and SPs) in the system do not need to change their credentials. When the user logs in, the IdP creates a credential for him. The user can then use this credential to access all designated SPs, instead of sending different credentials to different SPs. For each logging request, the IdP creates a new credential for the user. At this point of time, a user can also be revoked due to expiry of his membership, for instance. Our construction can prevent illegal credential sharing, which is defined as all-or-nothing non-transferability. By all-or-nothing non-transferability, we mean that all the credentials of a user are shared, once he shares one of them with others [30,3,4,19]. Figure 1 provides the architecture of our construction.



**Fig. 1.** DSSO Architecture

1. **System Set-up.** Runs the  $\text{Setup}(\lambda)$  to generate the public parameters  $PP$ , which includes all public parameters in the three underlying building blocks, and a public-secret key pair  $(K_{IP}, K_{IS}) \leftarrow \mathcal{G}(1^\lambda)$  for the IdP, where  $\lambda$  is the security parameter.
2. **Enrollment.**
  - (a) **Service providers enrollment.**  $SP_i$  submits his necessary registration information  $RI_{SP_i}$  to the IdP. The IdP issues an identifier  $ID_{SP_i}$  for  $SP_i$ , sends a verification key  $K_{SP_i}$  to him, which is regarded as the receiver key in the broadcast encryption scheme, and stores  $(SP_i, ID_{SP_i}, K_{SP_i})$  for him.
  - (b) **User enrollment.**  $U$  sends his necessary registration information  $RI_U$  to the IdP. The IdP issues an identifier  $ID_U$  for him. The user generates his public-secret key pair  $(K_{UP}, K_{US}) \leftarrow \mathcal{G}(1^\lambda)$  and sends the public key  $K_{UP}$  to the IdP. The IdP decides the user's access right  $A_U$ , which is a set that consists of the identifiers of the service providers that the user can access, and stores  $(ID_U, K_{UP}, A_U)$  for the user. Note that  $A_U$  will be regarded as the receiver set  $S$  in broadcast encryption.

### 3. Single Sign-on.

- (a) **Log in.**  $U$  uses his username and corresponding password to log in the system.
- (b) **Credential generation.** The IdP runs  $\text{BroEnc}(|A_U|)$  to generate the broadcast encryption key  $K$  which can only be computed by the service providers whose identifiers are listed in  $A_U$ , and encapsulates it in  $(A_U, Hdr)$ . IdP generates a signature  $\delta_U = \text{Sign}(K_{IS}, M_U, ID_U, K_{UP}, T_U)$ , where  $K_{IS}$  is the secret key of IdP,  $M_U$  is an authentication assertion,  $ID_U$  is the user's identifier,  $K_{UP}$  is the user's public key and  $T_U$  is a timestamp. Then, IdP encrypts the signature  $\delta_U$  under  $K$ . The credential for the user is

$$Cre_U = (A_U, Hdr, D), \text{ where } D = E_K(\delta_U, M_U, ID_U, K_{UP}, T_U).$$

- (c) **Service request.**  $U$  sends a service request to the service provider  $SP_i$  ( $ID_{SP_i} \in A_U$ ).
- (d) **Verification request.**  $SP_i$  asks  $U$  to show his credential to him.
- (e) **Credential verification.**  $U$  sends  $Cre_U$  to  $SP_i$ .  $SP_i$  computes the broadcast encryption key  $K$  from  $(A_U, Hdr)$  using his verification key  $K_{SP_i}$ , decrypts  $D = E_K(\delta_U, M_U, ID_U, K_{UP}, T_U)$  and verifies the signature  $\delta_U$ . If  $\delta_U$  is a valid signature on  $(M_U, ID_U, K_{UP}, T_U)$ ,  $SP_i$  executes the next step. Otherwise  $SP_i$  aborts.
- (f) **Owner identification.**  $U$  executes zero knowledge proof protocol  $(U, SP_i)$  ( $K_{UP}$ ) with  $SP_i$  to prove that he knows the secret key  $K_{US}$  corresponding the public key  $K_{UP}$  included in  $Cre_U$ .
- (g) **Service grant.** If the zero knowledge proof is successful,  $SP_i$  grants the services to the user. Otherwise,  $SP_i$  rejects the services.

If the user wants to access to other  $SP$ s whose identifiers are listed in  $A_U$ , he can send  $Cre_U$  to them directly, without having to request the IdP to issue a new credential for him, namely step (a) and (b) can be omitted.

### 4. Dynamic Change.

If the user needs to change his access right, when he logs in, he must submit a request to the IdP. After checking it, the IdP creates a new credential for the user, according to his current status.

- (a) **Request.**  $U$  must submit a request for changing  $A_U$  to the IdP. After checking the request, the IdP does the following two changes on  $A_U$ .
- (b) **Add.** The IdP adds a service provider  $SP_j$  to the user's access right  $A_U$  by setting  $A_U \leftarrow A_U \cup \{ID_{SP_j}\}$ , and updates the broadcast encryption key  $K$ .
- (c) **Delete.** The IdP deletes a service provider  $SP_j$  from  $A_U$  by setting  $A_U \leftarrow A_U \setminus \{ID_{SP_j}\}$ , and updates the broadcast encryption key  $K$ .
- (d) **New credential generation.** The IdP uses the updated broadcast encryption key  $K$  to generate a new credential for  $U$ .

## 5 Security Analysis

In this section, we prove that our construction for DSSO is secure against collusion credential forging attacks, collusion impersonate attacks and coalition credential forging attacks, and provides forward security and backward security.

**Theorem 1.** *Our generic construction for DSSO is  $(t, qe, qc_1, qc_2, \epsilon)$ -secure against collusion credential forging attacks if the broadcast encryption scheme is  $(t, n, qc_1, \epsilon_1)$  CCA-secure and the signature scheme is  $(t, qc_2, \epsilon, (1 - \epsilon_1)^{qc_2})$ -strongly existentially unforgeable.*

**Proof.** Suppose there exists  $t$ -time malicious users  $\mathcal{A}$  that  $(t, qe, qc_1, qc_2, \epsilon)$  breaks the collusion credential unforgeability of our generic construction for DSSO. We will show that there exists an algorithm  $\mathcal{B}$  who can  $(t, qc_2, \epsilon, (1 - \epsilon_1)^{qc_2})$  breaks the strongly existential unforgeability of the underlying signature scheme.

**Init.** Algorithm  $\mathcal{B}$  runs  $\mathcal{A}$  and receives a user  $U^*$  for whom  $\mathcal{A}$  wants to forge a credential.

**Setup.**  $\mathcal{B}$  sends the public parameters  $PP$  and the IdP's public key  $K_{IP}$  to  $\mathcal{A}$ .

**Enrollment queries.**  $\mathcal{A}$  can adaptively issues at most  $qe$  enrollment queries  $\{RI_{U_1}, RI_{U_2}, \dots, RI_{U_{qe}}\}$ , where  $RI_{U_i} \neq RI_{U^*}$ ,  $qe \leq (|\mathbb{U}| - 1)$ .  $\mathcal{B}$  returns  $\{(ID_{U_1}, A_{U_1}), (ID_{U_2}, A_{U_2}), \dots, (ID_{U_{qe}}, A_{U_{qe}})\}$ .

**Credential generation queries.**  $\mathcal{A}$  can adaptively issue credential generation queries  $\{(ID_{U_1}, K_{UP_1}), (ID_{U_2}, K_{UP_2}), \dots, (ID_{U_{qc_1}}, K_{UP_{qc_1}})\}$ , where  $(ID_{U_i}, K_{UP_i}) \neq (ID_{U^*}, K_{UP^*})$ .  $\mathcal{B}$  redirects these queries to the challenger. The challenger returns  $\{Cre_{U_1}, Cre_{U_2}, \dots, Cre_{U_{qc_1}}\}$ , where  $Cre_{U_i} = (A_{U_i}, Hdr_i, D_i)$ ,  $D_i = E_{K_i}(\delta_i, M_{U_i}, ID_{U_i}, K_{UP_i}, T_{U_i})$  and  $\delta_i = \text{Sign}(K_{IS}, M_{U_i}, ID_{U_i}, K_{UP_i}, T_{U_i})$ .

**Credential verification queries.**  $\mathcal{A}$  can adaptively issue credential verification queries  $\{(ID_{U_1}, K_{UP_1}, Cre_{U_1}), (ID_{U_2}, K_{UP_2}, Cre_{U_2}), \dots, (ID_{U_{qc_2}}, K_{UP_{qc_2}}, Cre_{U_{qc_2}})\}$ .  $\mathcal{B}$  redirects these queries to the challenger. The challenger returns *True* or *False*.

**Output.**  $\mathcal{A}$  outputs a credential  $Cre_U^* = (A_U^*, Hdr^*, D^*)$ , where  $(ID_U^*, Cre_U^*) \notin \{(ID_{U_1}, Cre_{U_1}), (ID_{U_2}, Cre_{U_2}), \dots, (ID_{U_{qc_1}}, Cre_{U_{qc_1}})\}$

$\mathcal{B}$  sends  $Cre_U^*$  to  $SP_l$  ( $ID_{SP_l} \in A_U^*$ ).  $SP_l$  returns the corresponding plaintext  $(M_U^*, ID_U^*, K_{UP}^*, T_U^*)$  or  $\perp$  for meaningless ciphertext.

1. If  $\perp$  is responded, namely  $D^*$  is not the corresponding ciphertext of  $(M_U^*, ID_U^*, K_{UP}^*, T_U^*)$  under the encryption key  $K^*$  encapsulated in  $Hdr^*$ ,  $\mathcal{B}$  aborts. The simulation fails.
2. If the corresponding plaintext  $(M_U^*, ID_U^*, K_{UP}^*, T_U^*)$  is responded, namely  $\mathcal{A}$  can get the broadcast encryption key  $K^*$  from  $Hdr^*$ ,  $\mathcal{B}$  will abort.  $\mathcal{B}$  can use  $\mathcal{A}$  to break the broadcast encryption scheme. Due to the broadcast encryption is  $(t, n, qc_1, \epsilon_1)$  CCA-secure, the probability that  $(M_U^*, ID_U^*, K_{UP}^*, T_U^*)$  is received is at most  $\epsilon_1$ .

3. If  $\mathcal{B}$  does not abort, he can obtain a valid signature  $\delta^*$  on  $(M_U^*, ID_U^*, K_{UP}^*, T^*)$  at the same advantage  $\epsilon$ .

Now we compute the probability that  $\mathcal{B}$  does not abort. If the broadcast encryption scheme is  $(t, n, qc_1, \epsilon_1)$  CCA-secure, then  $\mathcal{B}$  can abort at most  $\epsilon_1$ . Therefore, the probability that  $\mathcal{B}$  does not abort during the  $qc_2$  credential verification queries is at least  $(1 - \epsilon_1)^{qc_2}$ . Thus, the advantage that  $\mathcal{B}$  can break the strongly existential unforgeability of the underlying signature scheme is at least  $\epsilon \cdot (1 - \epsilon_1)^{qc_2}$  which contradicts the assumption that the underlying signature is  $(t, qc_2, \epsilon \cdot (1 - \epsilon_1)^{qc_2})$ -strongly existentially unforgeable.

**Theorem 2.** *Our generic construction for DSSO is secure against collusion impersonation attacks if the zero knowledge proofs scheme is secure.*

**Proof.** Let  $\mathcal{A}$  be malicious service providers to whom  $U$  has showed credentials and proved the ownership of these credentials. If  $\mathcal{A}$  can impersonate  $U$ , we will show that there exists an algorithm  $\mathcal{B}$  (knowledge extractor) can break the security of the underlying zero knowledge scheme.

If  $\mathcal{A}$  can impersonate  $U$  to prove that he is the owner of the credentials which  $U$  has showed to him, he must execute the ZKP protocol with some service providers to prove that he knows the secret key  $K_{US}$  corresponding to the public key  $K_{UP}$ . If  $\mathcal{A}$  can do this,  $\mathcal{B}$  (knowledge extractor) can use the rewinding techniques to obtain the user's secret key  $K_{US}$  from two different challenges sent to  $U$  and  $\mathcal{A}$ . So,  $\mathcal{B}$  can use  $\mathcal{A}$  to break the security of the underlying zero knowledge proofs scheme.

Note that, in our generic construction, the user can not share his credentials with others. Because, if he wants to share one credential with others, he must reveal his secret key  $K_{US}$  to them and all credentials of the user will be shared with others. This is the so-called all-or-nothing non-transferability property mentioned at section 4.

**Theorem 3.** *Our generic construction for DSSO is  $(t, qc, qc_1, qc_2, \epsilon)$ -secure against coalition credential forging attacks if the broadcast encryption scheme is  $(t, n, qc_1, \epsilon_1)$  CCA-secure, the signature scheme is  $(t, qc_2, \epsilon \cdot (1 - \epsilon_1)^{qc_2})$ -strongly existentially unforgeable.*

**Proof.** Suppose there exists  $t$ -time coalition  $\mathcal{A}$  that  $(t, qc, qc_1, qc_2, \epsilon)$  can forge a credential for the target user, in which the identifiers of the malicious service providers are not included. We will show that there exists an algorithm  $\mathcal{B}$  who can  $(t, qc_2, \epsilon \cdot (1 - \epsilon_1)^{qc_2})$ -break the strongly existential unforgeability of the underlying signature scheme.

**Init.** Algorithm  $\mathcal{B}$  runs  $\mathcal{A}$  and receives a target user  $U^*$  for whom  $\mathcal{A}$  wants to forge a credential and a target service provider  $SP^*$  that  $\mathcal{A}$  wants to attack.

**Setup.**  $\mathcal{B}$  sends the public parameters  $PP$  and IdP's public key  $K_{IP}$  to  $\mathcal{A}$ .

**Enrollment queries.**  $\mathcal{A}$  can adaptively issue enrollment queries  $\{RI_{U_1}, RI_{U_2}, \dots, RI_{U_{qe_1}}\}$ , where  $RI_{U_i} \neq RI_U^*$ ,  $qe_1 \leq (|U| - 1)$ , and  $\{RI_{SP_1}, RI_{SP_2}, \dots, RI_{SP_{qe_2}}\}$ , where  $RI_{SP_i} \neq RI_{SP}^*$ ,  $qe_2 \leq (|SP| - 1)$ , and  $qe_1 + qe_2 = qe$ .  $\mathcal{B}$  redirects these queries to the challenger. The challenger returns  $\{(ID_{U_1}, A_{U_1}), (ID_{U_2}, A_{U_2}), \dots, (ID_{U_{qe_1}}, A_{U_{qe_1}})\}$  and  $\{(ID_{SP_1}, K_{SP_1}), (ID_{SP_2}, K_{SP_2}), \dots, (ID_{SP_{qe_2}}, K_{SP_{qe_2}})\}$  respectively.

**Credential generation queries.**  $\mathcal{A}$  can adaptively issue credential generation queries  $\{(ID_{U_1}, K_{UP_1}), (ID_{U_2}, K_{UP_2}), \dots, (ID_{U_{qc_1}}, K_{UP_{qc_1}})\}$ .  $\mathcal{B}$  redirects these queries to the challenger. The challenger returns  $\{Cre_{U_1}, Cre_{U_2}, \dots, Cre_{U_{qc_1}}\}$ , where  $Cre_{U_i} = (A_{U_i}, Hdr_i, D_i)$ ,  $D_i = E_K(\delta_i, MU_i, ID_{U_i}, K_{UP_i}, T_i)$  and  $\delta_i = \text{Sign}(K_{IS}, MU_i, ID_{U_i}, K_{UP_i}, T_i)$ .

**Credential verification queries.**  $\mathcal{A}$  can adaptively issue credential verification queries  $\{(ID_{U_1}, K_{UP_1}, Cre_{U_1}), (ID_{U_2}, K_{UP_2}, Cre_{U_2}), \dots, (ID_{U_{qc_2}}, K_{UP_{qc_2}}, Cre_{U_{qc_2}})\}$ .  $\mathcal{B}$  redirects these queries to the challenger. The challenger returns *True* or *False* by decrypting  $D_i$  and verifying  $\delta_i$ .

**Output.**  $\mathcal{A}$  outputs a credential  $Cre_U^* = (A_U^*, Hdr^*, D^*)$ , where  $(ID_U^*, Cre_U^*) \notin \{(ID_{U_1}, Cre_{U_1}), (ID_{U_2}, Cre_{U_2}), \dots, (ID_{U_{qc_1}}, Cre_{U_{qc_1}})\}$ ,  $ID_{SP}^* \in A_U^*$  and  $ID_{SP} \notin A_U^*$  if  $SP \in \mathcal{A}$ .

$\mathcal{B}$  sends  $Cre_U^*$  to  $SP^*$ .  $SP^*$  returns the corresponding plaintext  $(M_U^*, ID_U^*, K_{UP}^*, T^*)$  or  $\perp$  for meaningless ciphertext.

1. If  $\perp$  is responded, namely  $D^*$  is not the corresponding ciphertext of  $(\delta^*, M_U^*, ID_U^*, K_{UP}^*, T^*)$  under encryption key  $K^*$  encapsulated in  $Hdr^*$ ,  $\mathcal{B}$  aborts. The simulation fails.
2. If the corresponding plaintext  $(M_U^*, ID_U^*, K_{UP}^*, T_U^*)$  is responded, namely  $\mathcal{A}$  can compute the broadcast encryption key  $K^*$  from  $Hdr^*$ ,  $\mathcal{B}$  will abort.  $\mathcal{B}$  can use  $\mathcal{A}$  to break the broadcast encryption scheme. Due to the assumption that broadcast encryption is  $(t, n, qc_1, \epsilon_1)$ CCA-secure, the advantage that  $(M_U^*, ID_U^*, K_{UP}^*, T_U^*)$  is responded is at most  $\epsilon_1$ .
3. If  $\mathcal{B}$  does not abort, he can obtain a valid signature  $\delta^*$  on  $(M_U^*, ID_U^*, K_{UP}^*, T_U^*)$  at the same advantage  $\epsilon$ .

Now, we compute the probability that  $\mathcal{B}$  does not abort at the  $qc_2$  credential verification queries. Due to the broadcast encryption scheme is  $(t, n, qc_1, \epsilon_1)$ CCA-secure, the probability of  $\mathcal{B}$  aborts when he gets the corresponding ciphertext is at most  $\epsilon_1$  for each decryption query. Therefore the probability of  $\mathcal{B}$  does not abort at the  $qc_2$  decryption queries is at least  $(1 - \epsilon_1)^{qc_2}$ . So, the probability that  $\mathcal{B}$  can break the strongly existential unforgeability of the underlying signature scheme is at least  $\epsilon \cdot (1 - \epsilon_1)^{qc_2}$  which contradicts the assumption that the underlying signature scheme is  $(t, qc_2, \epsilon \cdot (1 - \epsilon_1)^{qc_2})$ -strongly existentially unforgeable.

**Theorem 4.** *Our generic construction for DSSO is  $(t, qc, \epsilon)$ -forward secure if the broadcast encryption scheme is  $(t, n, qc, \epsilon)$ CCA-secure.*

**Proof.** Suppose there exists a  $t$ -time malicious service provider  $\mathcal{A}$  that  $(t, qc, \epsilon)$  breaks the forward security of our generic construction for DSSO. We will show there exists an algorithm  $\mathcal{B}$  who can  $(t, n, qc, \epsilon)$  breaks the CCA security of the broadcast encryption scheme. By  $A_U^O$ , we denote the access right of  $U$  before  $\mathcal{A}$ 's identifier is listed in it.

**Setup.**  $\mathcal{B}$  sends public parameter  $PP$ , and the IdP's public key  $K_{IP}$  to  $\mathcal{A}$ .

**Credential verification queries.**  $\mathcal{A}$  can adaptively issue credential verification queries  $\{(ID_{U_1}, K_{UP_1}, Cre_{U_1}), (ID_{U_2}, K_{UP_2}, Cre_{U_2}), \dots, (ID_{U_{qc}}, K_{UP_{qc}}, Cre_{U_{qc}})\}$ , which are issued after his identifier has been added to  $A_U$ .  $\mathcal{B}$  redirects these queries to the challenger. The challenger returns *True* or *False*.

**Challenge.**  $\mathcal{B}$  sends  $\mathcal{A}$  an old credential  $Cre_U^O$ , where  $Cre_U^O = (A_U^O, Hdr_O, D_O)$ ,  $D_O = E_{K_O}(\delta_O, m_U, ID_U, K_{UP}, T_O)$  and  $ID_{\mathcal{A}} \notin A_U^O$ .

**Output.**  $\mathcal{A}$  outputs a correct verification result *True* or *False* on credential  $Cre_U^O$  at least  $\epsilon$ .

If it is,  $\mathcal{A}$  can decrypt  $D_O = E_{K_O}(\delta_O, m_U, ID_U, K_{UP}, T_O)$  at least  $\epsilon$ . Namely,  $\mathcal{A}$  is not a receiver in the broadcast encryption scheme, but can compute the broadcast encryption key  $K_O$  from  $Hdr_O$  at least  $\epsilon$ . So,  $\mathcal{B}$  can use  $\mathcal{A}$  to break the CCA security of the broadcast encryption scheme at least  $\epsilon$ .

**Theorem 5.** *Our generic construction for DSSO is  $(t, qc, \epsilon)$ -backward secure if the broadcast encryption scheme is  $(t, n, qc, \epsilon)$ CCA-secure.*

The proof is similar to that of theorem 4. We omit the proof due to the page constraint.

## 6 Conclusion

The current SSO systems suffer from various security issues such as illegally sharing credentials and difficulties in user revocation. In this paper, we formalised the definitions and security models for SSO and DSSO, and proposed a generic scheme of DSSO. Our generic scheme provides a sound solution to these problems. We also provided a formal security proof of our scheme.

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