

Quasi-Resonant Clocking: Continuous Voltage-Frequency Scalable Resonant Clocking System for Dynamic Voltage-Frequency Scaling Systems

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Abstract—This paper describes quasi-resonant-clocking (QRC), a continuous voltage-frequency scalable resonant clocking architecture capable of dynamic voltage and frequency scaling (DVFS). The use of runtime control by QRC is central to ensuring robust, efficient operation across variations in process, voltage, and temperature. QRC exhibits instantaneous wide-range duty-cycle control, required for a broader class of clocking applications involving large capacitive loads. Two QRC variants, QRC_{foot} and QRC_{pass}, are presented with test-chip measurements under DVFS operation in 65-nm CMOS. The QRC test-chip demonstrates a maximum energy reduction of 47% at 132 MHz. Across both implementations, energy measurements based on runtime DVFS in 0.7–1.2 V range indicate energy reduction in the 32%–47% range.

Index Terms—Dynamic voltage and frequency scaling (DVFS), low power, process-voltage-temperature (PVT) tolerant, resonant clocking, runtime delay-locked-loop (DLL)-based control, system clocking, tunable duty-cycle, voltage-frequency-scalability.

I. INTRODUCTION

POWER dissipation continues to play a central role in impacting computing performance, mobility, and cost over a broad range of digital systems, from high-performance microprocessors [1]–[3] to ultra-low-power systems employing aggressive pipelining [4]. Fine-grained clock gating has significantly reduced clock power [3], [5], but the large global clock distribution driving these clock-gates accounts for a sizable fraction of total system power [6], [7]. Enabling clock power reduction, therefore, remains critical to the efficient implementation of digital systems.

Resonant clocking has been proposed as an efficient approach to global clock distribution [8]–[19]. Fig. 1 illustrates the central idea behind resonant-clocking—introducing inductance (L) into the clock network, and enabling efficient LC resonance between the clock load (C_{load}) at frequencies close to the natural (or resonant) frequency, $f_0 = 1/(2\pi LC^{1/2})$.

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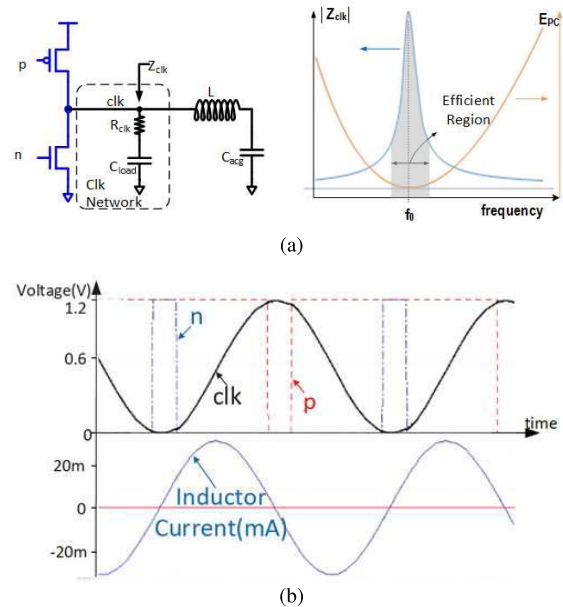


Fig. 1. Traditional resonant clocking. (a) Simplified resonant clock schematic with lumped global clock drivers and load. Driving the resulting tank circuit yields efficiency around the natural frequency f_0 . C_{acg} is a large dc-current blocking capacitor. (b) Schematic simulation waveform of traditional resonant clocking using a pulse driver [9], [13], [15] to generate sinusoidal waveforms.

In contrast with conventional CV^2 per-cycle energy dissipation, the energy delivered by the supply to a resonant clock system each cycle needs to only compensate for the I^2R losses in the LC tank. High quality-factor (Q) designs, achieved through reduced R_L and R_{clk} sustain clock oscillations with a significantly lower energy dissipation per cycle(E_{PC}): $E_{PC} = \pi/4QC_{load}V_{dd}^2$ [15].

Recent implementations have overcome several outstanding processor integration challenges. Two such important challenges are the design of inductors in-line with power trunks [6], [7], [14], [20]–[22], and addressing system- Q degradation due to power grid eddy-current flow [6]. The result of these efforts has been processor designs with significant clock power reduction, positively impacting power-constrained performance and battery-life.

Meanwhile, the increased significance of dynamic voltage and frequency scaling (DVFS) [23], and a trend toward its

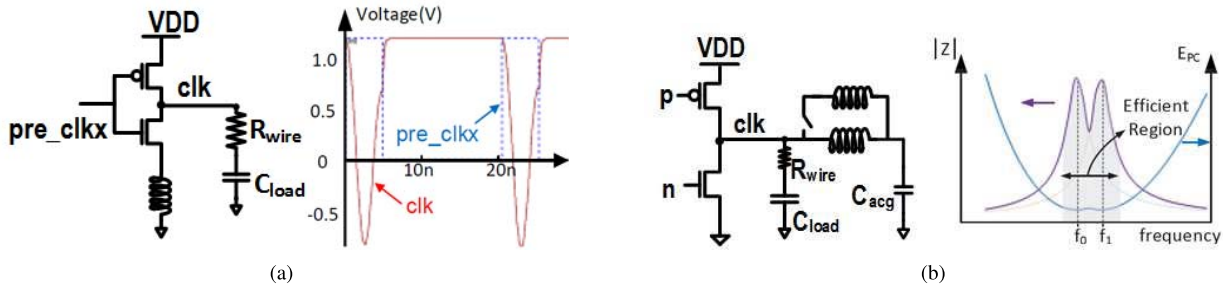


Fig. 2. (a) Intermittent resonance enables continuous frequency control of a clock “blip” for sub-threshold applications. (b) Tuned-inductor-based resonant clocking extends the range of efficient resonance through programmable inductance of the LC tank.

increasingly aggressive use across a broader voltage-frequency range dilutes resonant clocking efficiency benefits. Resonant clock efficiencies, attractive at clock frequencies close to f_0 (Fig. 1), quickly diminish along with Z_{tank} outside a small frequency range away from f_0 . Although power-constrained performance benefits remain, the broader energy-efficiency advantages of the technique are diminished as systems spend a smaller portion of time within this narrow frequency range.

Recent works have attempted to address this challenge using techniques suitable for their specific applications [7], [24]. However, these techniques face challenges of limited frequency-tunability [7], limited duty cycle control [24], or clock clock waveforms that transitions to $-V_{\text{dd}}$, limiting scalability [24].

In this paper, we elaborate upon quasi-resonant-clocking (QRC) [25], a DVFS-compliant technique that achieves continuous voltage and frequency scalability. The proposed approach produces rail-to-rail clock waveforms with near-arbitrary duty-cycle control. With the exception of [24] (itself restricted to sub-threshold designs) the proposed approach is the only architecture capable of achieving *uniform* energy efficiency continuously across the 0 to f_0 frequency range. A key enabler of efficient, process-voltage-temperature (PVT) robust operation, and DVFS support is *autonomous* timing control of QRC related circuits which can track slewing supply-voltages during DVFS events, and temperature variations. The proposed technology is capable of a frequency range of 0– f_0 , and sub-threshold to nominal- V_{dd} operation. We present circuits and architectures for two different variants of QRC, notably QRC_{pass} and QRC_{foot} which offer different capabilities and efficiencies. We also present an analysis of QRC energy and its dependence on key QRC parameters. This model is used to determine optimal design parameters, and examine the fundamental tradeoff between efficiency and rise/fall times exhibited by all resonant-clock systems. The two proposed QRC variants are validated through test-chip demonstrations of a DVFS system consisting of an eight-way multiply-accumulate (MAC) array in 65-nm CMOS. Last, we present test-chip measurements obtained from each of these two implementations.

The remainder of this paper is organized as follows. In Section II, we review related work in the area of frequency-scalable resonant clocking. In Section III, we provide an overview of the QRC architecture and the salient aspects of its

operation. Circuit and architecture descriptions for each variant of the QRC implementation are discussed in Sections IV and V. An analysis of QRC, including the examination of energy-optimal design parameters is presented in Section VI. Test-chip architecture, evaluations and measurements of both variants, QRC_{foot} and QRC_{pass} , are presented in Section VII.

II. RELATED WORK

Several prior works in the literature have focused on addressing the limited frequency range of resonant clocking. These approaches range from disabling resonant clocking at frequencies outside a narrow range [6], to alternative resonant clocking implementations which extend resonant operation outside its narrow operating range.

A technique originally proposed and demonstrated in [26], [27] for I/O pad and display drivers, and re-implemented more recently in [28] involves using switched capacitor banks to transition a clock load through a sequence of intermediate voltage levels. Although slightly less efficient than inductor-based techniques, the switched-capacitor-based technique offers notable advantages: 1) simpler logic control; 2) ease of integration; and 3) natural voltage scalability. However, though effective for its originally intended application of driving adiabatic logic or LCD drivers [26], [27], this approach is not well suited to system clocking—employing the technique efficiently results in clock waveform “shelving” [27] (the clock voltage levels off at intermediate voltages during) that impacts efficiency and race-immunity among timing elements. In more severe situations, non-monotonic clock waveforms near mid-rail voltages [28] can result in runt clock pulses.

More recently, intermittent resonant clocking, a novel technique achieving uniform efficiency resonant clocking from 0– f_0 has been proposed [24]. Illustrated in Fig. 2(a), the technique presents a novel topology to deliver an RLC oscillation enabled clock “blip” from V_{dd} to $-V_{\text{dd}}$. The pMOS can hold clk at V_{dd} for an arbitrary duration before commencing the next “blip.” Frequency scaling is achieved by varying the duration of time that the clk net remains at V_{dd} . The proposed architecture, developed for sub-threshold operation, does not scale to higher voltages by construction. Non-compliant CMOS voltages—the clock waveform transitions below 0 V to a body-drain diode-drop voltage of approximately 700 mV—prevent operation at nominal voltages. Furthermore, operation at

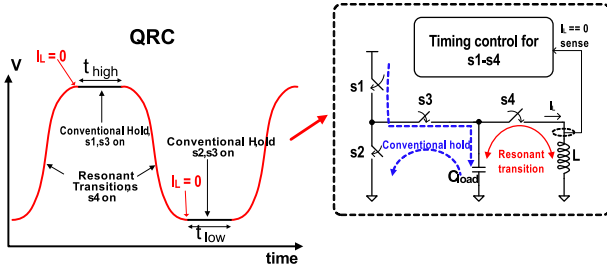


Fig. 3. Quasi-resonant clocking: key rationale.

higher voltages also results in the dissipative turn-on of the nMOS diode turn-on as clock transitions below -700 mV, shunting the RLC system. Finally, the inability to control duty cycle limits the approach to use in flip-flop-based system clocking applications..

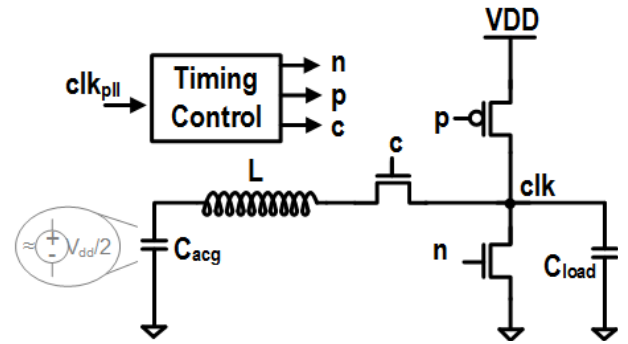
Bandwidth extension through additional programmable inductors to modulate total inductance [Fig. 2(b)] and shift f_0 has been demonstrated [7], and recently implemented in a production processor [22]. The proposed approach caters to its target application, but does not provide continuous voltage-frequency scalability across a broad range. It is, therefore, not well suited to applications seeking a truly broad resonant-clock operating frequency range. Furthermore, the placement of additional inductors in an already physically and electrically constrained environment places additional inductor design challenges and complexity, and relies on technology to deliver inductors of sufficient quality-factor.

III. QRC OVERVIEW

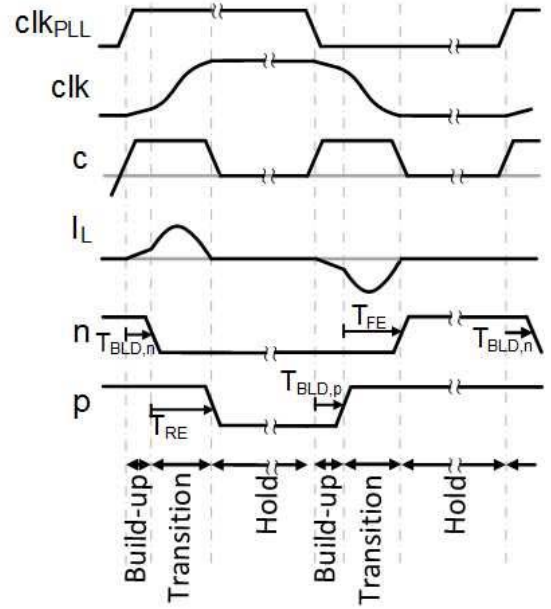
QRC achieves continuous frequency scalability by effectively interleaving conventional and resonant modes of clock operation. Fig. 3 illustrates the rationale behind the QRC architecture. The time instant when the clock voltage is at its maximum or minimum is ideal for disconnecting the inductor from the clock domain (discussed further in this section). Disconnecting the inductor safely and efficiently enables the clock to be held to the supply and ground rail for an arbitrary duration of time (τ_{high} and τ_{low} , respectively), readily achieving frequency and duty-cycle control.

A simplified circuit diagram for the proposed QRC clocking scheme is shown in Fig. 4(a). Conduction switch M_c conditionally disconnects the inductor from the clock network at the end of each resonant transition, twice every cycle. C_{acg} blocks dc inductor current flow and is large enough to act as an ac ground connection.

Fig. 4(b) shows a simplified QRC timing diagram, identifying signal transitions for n , p , and c , controlled precisely through the *Timing Control* module. Consider the steady-state operation of the QRC system. The voltage across C_{acg} ($C_{\text{acg}} \approx 30 \cdot C_{\text{load}}$) remains steady at $V_{\text{dd}}/2$ (for a 50% duty-cycle clock). At the start of the clock cycle, $V(\text{clk}_{\text{PLL}}) = 0$, $V(\text{clk}) = 0$. As clk_{PLL} transitions to V_{dd} , c is asserted and connects the inductor to the resonant system, effecting an RL current build-up in the inductor. $T_{\text{BLD},n}$ and $T_{\text{BLD},p}$ correspond to the inductor-current build-up times before the rising and



(a)



(b)

Fig. 4. QRC architecture relies on precise timing of n , p , and c signals provided by the timing control module to achieve interleaved conventional and hold operation. (a) QRC: simplified schematic. (b) QRC: simplified timing diagram.

falling transitions of the resonant clock, respectively. Use of $T_{\text{BLD},p}$ and $T_{\text{BLD},n}$ are motivated by two factors.

- 1) A longer build-up provides a sharper slew for the output clocks, essential for reliable digital systems.
- 2) Suitably tuned build-up durations provide improved efficiency [6], [15]. The optimal build-up duration varies depending on a number of factors including the resistance in the build-up and resonant paths and the load capacitance.

After duration $T_{\text{BLD},n}$, n transitions to 0, turning off the hitherto conducting M_n , starting the LC transition of clk from 0 to V_{dd} . After a delay (T_{RE}) determined by the natural frequency of the LC network, clk reaches its peak voltage. A comparator detects this peak, prompting the timing module to de-assert c and disconnect the inductor from the network precisely when inductor current $I_L = 0$ with help from a timing-control module. Concurrently, p transitions to 0, turning on M_p , and driving clk to V_{dd} rail. At the end of

The clock cycle time, T_{clk} can be written as: $T_{\text{clk}} = T_{\text{BLD},p} + T_{\text{RE}} + T_{\tau_{\text{high}}} + T_{\text{BLD},n} + T_{\text{FE}} + T_{\tau_{\text{low}}}$. Frequency and duty cycle programmability is achieved by varying $T_{\tau_{\text{high}}}$ and $T_{\tau_{\text{low}}}$ independently in QRC [29]. T_{RE} and T_{FE} are determined by the natural frequency of the LC system: $T_{\text{RE}} + T_{\text{FE}} = 1/f_0 = 2\pi LC^{1/2}$. Consequently, the maximum operating frequency using QRC is therefore limited by f_0 , corresponding to ordinary resonant operation.

DVFS events require charging C_{acg} to $V_{\text{dd}}/2$. However, at prevalent levels of capacitance ($\approx 30 \cdot C_{\text{load}}$), the charge-discharge durations amount to a few clock cycles, and do not pose an overhead for DVFS. In addition, any settling time resulting from the voltage transition has a minor temporary impact on clock slew and efficiency.

To provide PVT-robust, efficient clocking compatible with runtime voltage and frequency transitions, QRC faces two important challenges—timing control, and the efficiency of the M_c switch. Turning M_c off while $I_L \neq 0$ results in wasteful dissipation and voltage ringing that exceeds the supply rail, degrading both efficiency and reliability. Furthermore, precise timing must be maintained across variation in PVT, and across the DVFS-enabled V_{dd} range. An all-digital runtime control system relying on a sense-amplifier and dual-edge triggered delay-locked-loop (DLL) provides the necessary current detection.

The second challenge of ensuring robust and efficient operation arises from the quiescent $V_{dd}/2$ voltage across C_{acg} , motivating design of a gate driver to meet the resulting gate-overdrive needs of M_c . These challenges manifest separately in QRC_{foot} and QRC_{pass} and are therefore addressed individually through different gate-driver circuits.

In this section, we discuss the architecture and circuits that constitute the QRC_{foot} 65 nm test-chip implementation. In particular, we describe two key enabling sub-systems. A DLL-enabled *Timing Control* module and the footer-driver circuit.

Fig. 5 illustrates the QRC_{foot} architecture [25]. M_c is connected as a footer device between the bottom-plate of C_{acg} and ground. A footer arrangement provides full gate overdrive ($V_{\text{gs}} = V_{\text{dd}}$). The *Timing-control* module uses a comparator sampling the source-drain terminals of M_c , and clocked by c to provide feedback to the *Timing Control* module to ensure carefully timed assertions and de-assertions of p , n , and c_{pre} . Although M_c enjoys full gate-overdrive when $c = V_{\text{dd}}$, a driver circuit is required enforcing device cutoff when $V(\text{clk})$ is in conventional mode, as discussed further in Section IV-B.

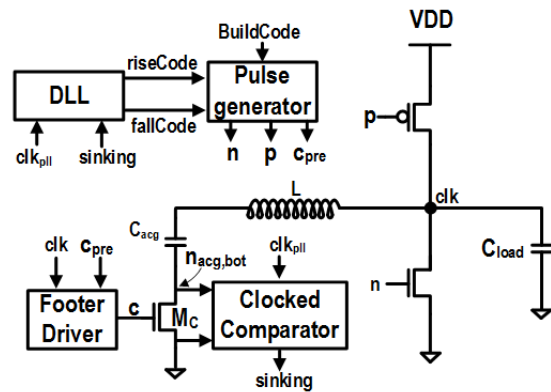


Fig. 5. QRC_{foot} simplified schematic. Use of M_c as a footer requires a footer-driver to prevent current backflow. A clocked comparator provides all-digital zero- I_L detection.

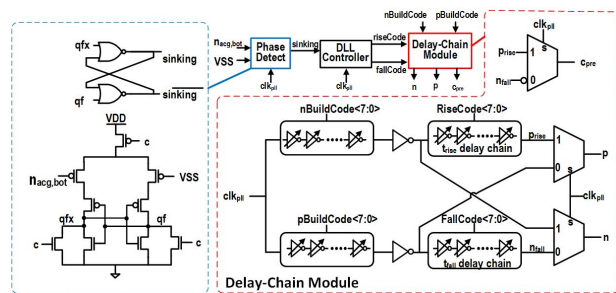


Fig. 6. Timing control module (shown for QRC_{foot} , Fig. 5) employs a “dual-DLL” architecture, controlling two delay chains with a single front-end phase-detector, precisely timing signals n , p , and c . MUXes provide glitchless, context-dependent delay.

A. Timing Control Module

The *Timing Control* module orchestrates the assertion/de-assertion of n , p , and c to enable robust, efficient operation under slewing V_{dd} and f_{clk} conditions expected in DVFS. Timing requirements for n , p , and c are stringent to ensure the inductor is disconnected from the clock domain when $I_L = 0$ at the end of each resonant transition to avoid wasteful, reliability-degrading under-damped voltage oscillations. The assertion and de-assertion delays of n and p are determined by frequency of the output clock (f_{clk} , f_0 , $T_{\text{BLD},n}$, $T_{\text{BLD},p}$) (Fig. 5). Finally c switches twice every cycle, and is asserted for durations T_{RF} and T_{FF} of each resonant transition of clk.

Fig. 6 summarizes the implementation of the *Timing Module*. A DLL implementation aligns two events—the de-assertion of c (the gate-driver output, which disconnects the inductor from the network), and the advent of zero current flow in the inductor. The need to align these events twice every cycle (one for each clock edge) when transitioning from resonant to conventional mode motivates a “dual-DLL” architecture, with a shared front-end phase-detector and two delay-chains to achieve the desired timing control for each transition. Independent delay chains provide separate control of current buildup durations ($T_{BLD,n}$, $T_{BLD,p}$) and clock transition times (T_{RE} , T_{FE}) (Fig. 5) for rise and fall clock edges to support non 50% duty-cycles.

A p-type strong-ARM latch, triggered on the de-asserting (for an nMOS M_c) edge of c , performs

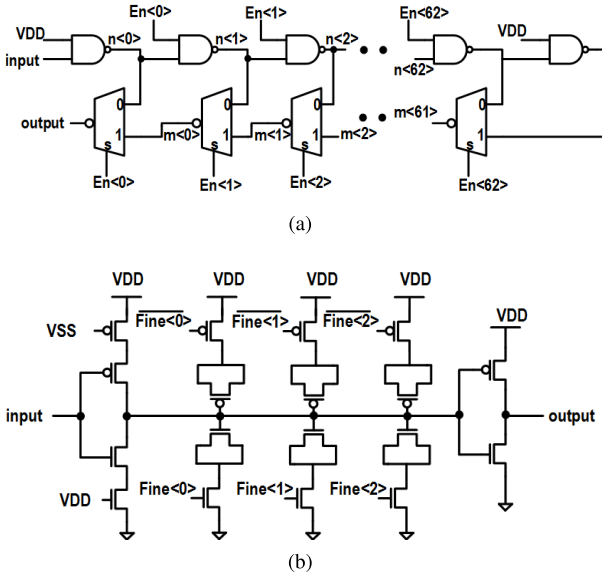


Fig. 7. Delay chain design ensures the range and precision required at across the entire V_{dd} range. (a) Coarse delay chain. (b) Fine delay chain.

phase-detection, determining current flow direction through M_c by sampling the relative polarity of its source and drain terminals twice every cycle. Thus, the phase-detector determines whether c is de-asserted too early or late relative to the $I_L = 0$ event based on the direction of current flow (with C_{acg} either *sourcing* or *sinking* current). This phase-detector output provides the required early/late signals to the dual-DLL. The DLL controller updates the rise and fall delay chains, with the *rise_delay* (*fall_delay*) chain updated based on the comparator sample when the clk voltage is V_{dd} (0). Delay-code update-driven glitches are avoided by updating delays when delay-chain outputs are not observed—Updates to the *rise_delay* (*fall_delay*) chain occur when clk is 0 (V_{dd}). Glitch-less, context-dependent delay for n , p , and c is provided by using selection MUXes.

By starting resonant clock transitions a fixed delay ($T_{BLD,n}$ and $T_{BLD,p}$) after clk_{PLL} , QRC is transparent to duty-cycle changes made at its input, on clk_{PLL} . This feature is beneficial for optimizing phase-paths in some digital designs. Furthermore, any changes in input clock duty-cycle are instantaneously referred to the output, a key benefit in IVR applications involving runtime modulation of clock duty-cycle.

Programmable delay is achieved through a telescopic delay chain [30] for coarse resolution, combined with a programmable load inverter chain for fine delay control (Fig. 7). A thermometer code controls the coarse telescopic delay chain [30], and MOS-based capacitors offer programmable load in the fine delay chain. The delay chain was designed to provide sufficient resolution at $V_{dd} = 0.7$ V, and range at $V_{dd} = 1.2$ V for robust, efficient QRC operation.

Fig. 8 summarizes the operation of the DLL controller. Upon cold-start, the system first safely determines PVT-dependent delay-code settings. Reliability degradation due to initially mistimed c signals upon start-up are managed by first locking with only a fraction of the M_c device,

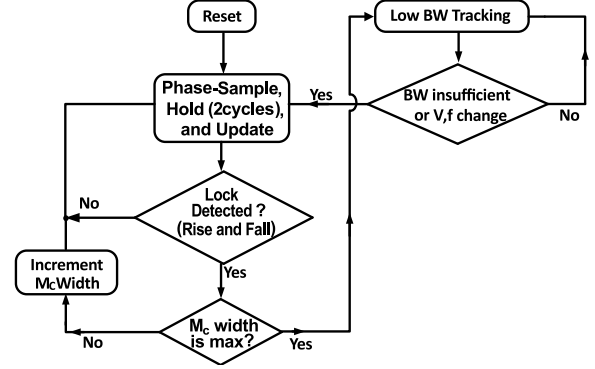


Fig. 8. DLL lock acquisition procedure, avoiding reliability challenges before DLL-lock, and finally transitioning to a low-bandwidth mode sufficient to track temperature variation.

limiting I_L , and throttling any under-damped voltage oscillations. After achieving DLL lock for both edges (rising and falling), the controller increases M_c width and returns to locking mode, making any necessary delay adjustments to re-lock. This interleaved lock and M_c -width update is repeated until the target M_c width is reached. Once locked, the DLL transitions into a low-power mode, with a sampling rate (kilohertz range) required tracking temperature changes on the die, rendering DLL controller power negligible.

B. Footer Driver Circuit

The QRC_{foot} implementation employs a footer for efficient operation through full gate overdrive. However, when $V(clk) = 0$, the $V_{dd}/2$ voltage across the C_{acg} results in the footer drain voltage reaching $-V_{dd}/2$ (Fig. 9). Using traditional drivers to set the gate voltage c to 0 V is therefore insufficient, and results in current back-flow from the ground terminal which discharges C_{acg} . A footer driver is therefore designed to drive c to achieve full gate overdrive when on, and ensure cut-off when non-conducting. When the network is in resonant mode with $V(c_{pre}) = V_{dd}$, the driver drives c to V_{dd} , allowing M_c to conduct in the linear mode regardless of clock polarity. When clk is held at V_{dd} in conventional mode with $V(c_{pre}) = 0$, the drain voltage of M_c ($n_{acg,bot}$) transitions to $V_{dd}/2$, and the driver drives c to 0 V. However, when $V(clk) = 0$ in conventional mode, the drain of M_c transitions to $-V_{dd}/2$, requiring that the driver set c to $-V_{dd}/2$ to ensure M_c is in cut-off.

We implemented a footer driver [Fig. 9(b)] to efficiently enable this functionality. The pull-up network consisting of M_0 and M_1 sets c to V_{dd} during build-up and resonant transition. In conventional mode, disabling M_c when $V(clk_{PLL}) = V_{dd}$ similarly involves a conventional pull-down through conducting devices M_2 and M_3 . M_4 and M_5 are in cutoff and do not interfere in the action of the pull-down network. When $V(clk_{PLL}) = 0$ in conventional mode, $n_{acg,bot}$, the erstwhile drain of M_c is $-V_{dd}/2$, M_5 conducts to ensure that c is connected to n , ensuring $V_{gs} = 0$. M_4 is employed to connect the gate terminal of M_3 to n , thereby avoiding current back-flow in the pull-down stack. Thick oxide devices are required for M_4 and M_5 to withstand higher oxide stress when

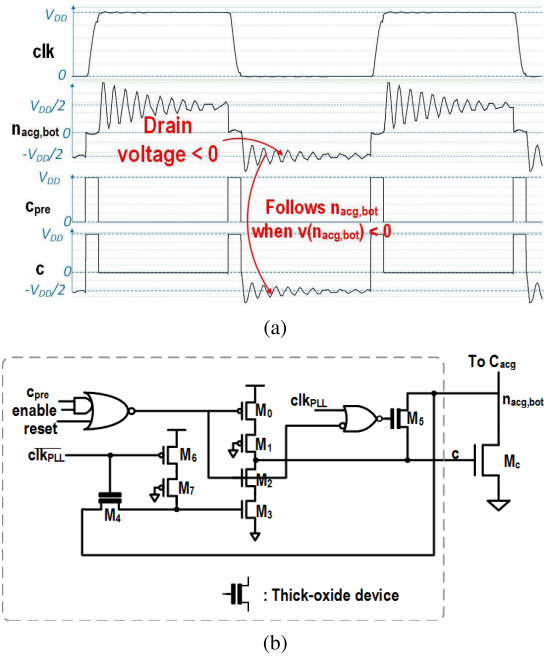


Fig. 9. (a) $n_{acg.bot}$ node (see Fig. 5) transitions below 0 V, settling towards $-V_{DD}/2$. Holding c to 0 V is insufficient to ensure cutoff of M_c . The footer driver ties the gate of M_c to $n_{acg.bot}$, ensuring cutoff. (b) Footer driver schematic. The driver ties the gate of M_c to $n_{acg.bot}$ through M_5 . M_4 is fed-back to the pull-down stack to avoid current backflow through $M_2 - M_3$.

conducting. The higher V_{th} of these devices is offset by the increased gate overdrive of $3/2V_{DD} - V_{th}$ during conduction. M_1 and M_7 are protection devices employed to prevent oxide stress related degradation in M_0 and M_6 , respectively.

V. QRC_{pass} Design

In this section, we discuss circuits and architectures that constitute the QRC_{pass} design. The QRC_{pass} topology enables a single inductor to be shared between multiple clock load domains for a Single Inductor multiple output capability. This feature is promising for a variety of applications including driving multi-phase bridges of an integrated buck converter. Similar to QRC_{foot}, QRC_{pass} relies on the same *Timing Control* module for precise signal timing. In this section, we focus on modules that are distinct from the QRC_{foot} implementation, namely, the sense-amplifier and the gate-overdrive circuits.

QRC_{pass} employs a gate-booted nMOS pass-gate (M_c) to serve as the conduction switch (Fig. 10), resulting in a set of current-sensing and gate-overdrive challenges distinct from those in QRC_{foot}. Unlike QRC_{foot}, where the sense-amplifier measures M_c source-drain polarity around a 0 V common mode, QRC_{pass} requires polarity sensing with a common-mode of V_{DD} and 0 V after the rising and falling edges of clk , respectively. In addition, the $V_{DD}/2$ voltage across C_{acg} results in reduced gate overdrive for M_c .

A. Sense-Amplifier Latch

Fig. 11 shows the proposed sense amplifier (sense-amp) implemented for QRC_{pass}. In order to sample twice every cycle, with common mode voltages of 0 and V_{DD} , respectively,

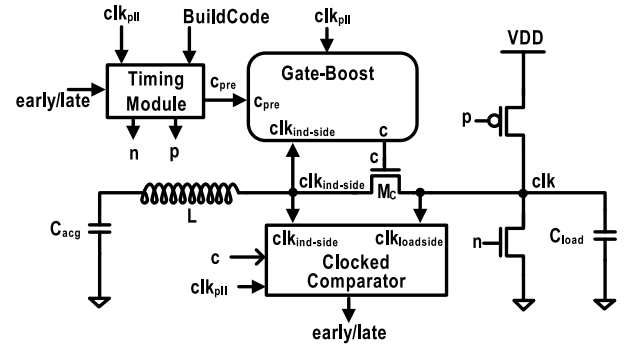


Fig. 10. QRC_{pass} simplified schematic. M_c is employed as a nMOS pass-gate. Gate-overdrive is employed to ensure a uniform 1.2-V gate overdrive throughout conduction.

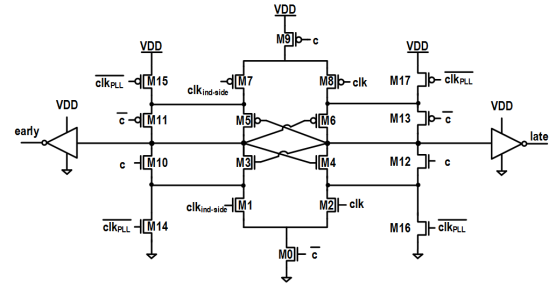


Fig. 11. QRC_{pass} clocked comparator schematic. The comparator operates with alternating input common mode voltages of 0 V and V_{DD} , twice every cycle.

the proposed sense-amplifier exhibits alternating operation of pull-down and pull-up sense-amplifier sections. When $clk_{PLL} = 1$, the sense-amplifier amplifies the differential current drive in M_1 and M_2 (enabled by footer device M_0) to determine current flow direction in M_c . Devices $M_3 - M_6$ provide the positive feedback to resolve the differential current drive, $M_{10} - M_{13}$ serve to pre-charge sense-amplifier nodes during both clock transitions. Finally M_{15}, M_{17} (M_{14}, M_{16}) provide the necessary power (ground) connection to the sense-amplifier when $clk = 1$ ($clk = 0$). Devices $M_1 - M_8$ are up-sized, and employ non-minimum channel length devices to mitigate random mismatch between differential devices.

B. Gate Boosting

Placing M_c between the inductor and clk allows multiple domains to share a single inductor, but results in degraded gate overdrive. A standard 2X voltage doubler [31]–[33] applied to M_c provides the necessary gate overdrive but is not feasible due to the $2V_{DD}$ gate-source voltage that will result as clk approaches 0. We propose a gate boosting topology suited to the QRC_{pass} implementation [Fig. 12(a)] that relies on bootstrapping the gate of M_c with the transition of $clk_{ind-side}$. The resulting system provides full gate overdrive ($V_{DD} - V_{th}$) for M_c throughout the resonant clk transition between the supply rails. The proposed circuit ensures that c the gate signal provided to M_c is 0 V when $c_{pre} = 0$. When $c_{pre} = 1$, the boosting circuit delivers a voltage of $1.2 V + V_S$ (where V_S is the source voltage of M_c), consistently ensuring full gate-overdrive for M_c .

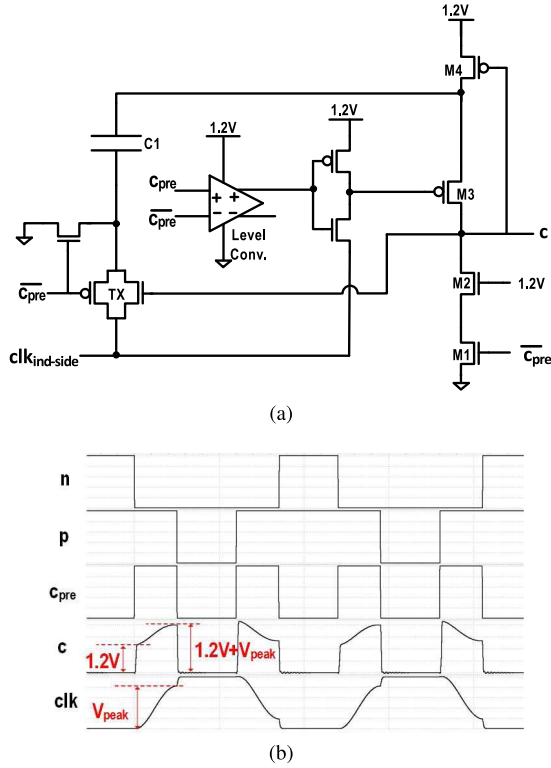


Fig. 12. (a) Schematic circuit for pass-gate boosting. The proposed topology provides a constant 1.2-V V_{gs} to M_c while using only logic devices while maintaining reliability. (b) Pass-gate boosting simulation waveforms.

Fig. 12(b) illustrates the operation of the proposed circuit. In conventional mode ($c_{pre} = 0$), series devices M_1 and M_2 (a gate-oxide protection device) drive c to 0 V, ensuring cutoff. The boosting capacitor (C_1) pre-charges to 1.2 V. In resonant mode, as $c_{pre} = 1$, turning M_c , TX conducts ($c_{pre} = 1$) connecting the bottom-plate of C to n_{Lside} . M_3 conducts, driving out to $V(n_{Lside}) + 1.2$ V. This gate overdrive is maintained during the entire resonant transition, both rising and falling. Notably, while maintaining a 1.2-V gate-source and gate-drain voltage during operation, the gate voltage safely transitions up to 2.4 V (When $V_{dd} = 1.2$ V) while M_c conducts. The gate-oxide of M_c is protected by the conducting channel while conducting.

An off-chip 1.2-V supply voltage was used to aid test and characterization of the proposed circuit. An integrated implementation of the supply using charge-pumps is relatively straightforward due to the low-current draw of the 1.2-V supply. Alternatively, the 1.2-V supply can be replaced with V_{dd} , resulting in a voltage doubler gate-oxide stress compliant design at the cost of reduced efficiency at low voltages.

In QRC_{pass}, turning off of the pass gate causes an underdamped RLC oscillation at node n_{sw} as the drain capacitance of the pass-gate transitions from either V_{dd} or 0 to $V_{dd}/2$ [Fig. 13(b)]. This underdamped oscillation is unavoidable, but does not affect the reliability of devices in the QRC system.

VI. ANALYSIS

A. Energy Dissipation Analysis

In this section, we present simulations and analytical models for QRC energy dissipation consisting of switching and

conduction loss components. Simulations are used to examine aspects of QRC design that are either onerous or impossible to demonstrate through measurement of the test-chip. Given the similarity of the analysis between QRC_{pass} and QRC_{foot}, we restrict our focus on the QRC_{pass} implementation for brevity. We use the simplified schematic in Fig. 13(a) to analyze the energetics of QRC.

The energy-per-cycle (EPC) dissipation of a resonant clocking system modeled as an equivalent R , L , and C system can be approximated as [15]

$$EPC_{res} = \frac{\pi}{4Q} C V_{dd}^2 \quad (1)$$

where Q is the system quality factor.

To analyze QRC energy dissipation, we start by noting that a lossless LC resonant clock transition is sinusoidal, with magnitude $V_{dd}/2$ around a dc voltage level $V_{dd}/2$. The total capacitance $C_{total} = C_{load} + C_p$ stores a charge of $C_{total} V_{dd}/2$, corresponding to an energy storage of $1/2 \cdot C_{total} (V_{dd}/2)^2$. In practice, C_{load} charges to a lower value, V_{peak} [Fig. 13(b)], the difference accounting for the conduction losses in the system. V_{peak} , the voltage of clk at the end of its resonant transition, and E_{cond} , the per-cycle conduction loss can be determined using known values of Q

$$\begin{aligned} V_{peak} &= \frac{V_{dd}}{2} \left(1 + e^{\left(\frac{-\pi}{\sqrt{4Q^2 - 1}} \right)} \right) \\ E_{cond} &= (C_{load} + C_p) V_{dd} (V_{dd} - V_{peak}) \\ &= (C_{load} + C_p) V_{dd} \left[V_{dd} - \frac{V_{dd}}{2} \left(1 + e^{\left(\frac{-\pi}{\sqrt{4Q^2 - 1}} \right)} \right) \right]. \end{aligned} \quad (2)$$

An additional source of energy loss arises from conventional charge and discharge of parasitic capacitance, C_p on the inductor side of the switch. Twice every cycle, this capacitance transitions from $V_{dd}/2$ to the supply rails at the onset of the resonant transition and returns to the mid-rail voltage after the transition. The resulting energy dissipation, $E_{sw,parasitic}$ can be modeled as

$$E_{sw,parasitic} = 4 \cdot \frac{1}{2} C_p \frac{V_{dd}^2}{4} = \frac{1}{2} C_p V_{dd}^2. \quad (3)$$

Similarly, the system incurs switching losses in the driver twice, once for each transition

$$E_{sw,driver} = 2 \cdot \frac{1}{\eta_{boost}} \cdot C_{Mc} \cdot (V_{dd} + 1.2)^2 \quad (4)$$

where C_{Mc} is the capacitance of the M_c switch and η_{boost} is the efficiency of the gate boosting module. Adding (2)–(4) provides the expression for total losses per-cycle

$$\begin{aligned} E_{tot} &= (C_{load} + C_p) V_{dd} (V_{dd} - V_{peak}) + \frac{1}{2} C_p V_{dd}^2 \\ &\quad + \frac{2}{\eta_{boost}} \cdot C_{Mc} \cdot (V_{dd} + 1.2)^2. \end{aligned} \quad (5)$$

The tradeoff between switching and conduction losses is apparent in M_c width selection (Fig. 14). Increasing M_c width reduces resistance, and E_{cond} , at the expense of increased $E_{sw,driver}$. Including the resistive contribution of M_c in the $I^2 R$ losses in (2), and using the resulting V_{peak}

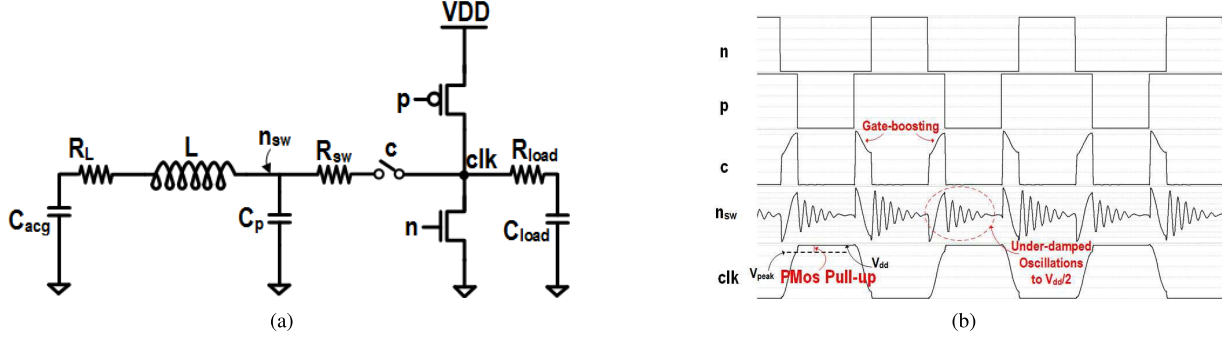


Fig. 13. (a) Equivalent circuit used for QRC_{pass} energy dissipation analysis. (b) QRC_{pass} simulation waveforms relevant to energy dissipation.

to obtain E_{tot} , the resulting analytical EPC results derived from (3)–(5) match well with simulation results (with parasitic capacitance).

Fig. 14 shows the existence of an optimal M_c width, trading off switching and conduction losses in (5). As seen from (2), increased resistance due to the clock distribution, the inductor, or reduced series switch width, degrades system Q, increasing conduction losses. On the other hand, larger switches increase switching losses. In our proposed implementation of QRC_{pass} and QRC_{foot} , the switch-width was designed to be tunable by having several banks of MOSFET in parallel. In post-silicon, a onetime calibration was run to fix the optimal switch width.

B. f_{max}

For QRC, clock frequency is modulated by inserting a hold-high/hold-low duration between the resonant transition and changing the duration of them. The maximum frequency is possible when $\tau_{\text{hold high}} = \tau_{\text{hold low}} = \tau_{\text{buildup}} = 0$, which corresponds to a sinusoidal clock waveform operating at its natural frequency, f_0 .

Increased f_0 delivers broader operating range but at the expense of reduced energy savings (1)

$$\begin{aligned} \text{EPC}_{\text{res}} &= \frac{\pi}{4Q} C V_{\text{dd}}^2 = \frac{\pi}{4} (2\pi f_0 RC) C V_{\text{dd}}^2 \\ &= \text{EPC}_{\text{conv}} \left(\frac{1}{2} \pi^2 f_0 RC \right). \end{aligned} \quad (6)$$

f_{max} can be calculated from the targeted energy savings

$$\begin{aligned} \text{Energy_efficiency, } \eta_{\text{res}} &= 1 - \frac{\text{EPC}_{\text{res}}}{\text{EPC}_{\text{conv}}} \\ f_0 &= \frac{2(1 - \eta_{\text{res}})}{\pi^2 RC}. \end{aligned} \quad (7)$$

From (7) it can be seen that increasing f_0 degrades efficiency. This trend imposes a tradeoff between energy-efficiency and maximum achievable frequency. In designs with extremely high clock loading (global clock distributions of microprocessors), multiple distributed inductors have been shown to be effective, with each inductor resonating with a portion of the total clock load (see [6], [7]).

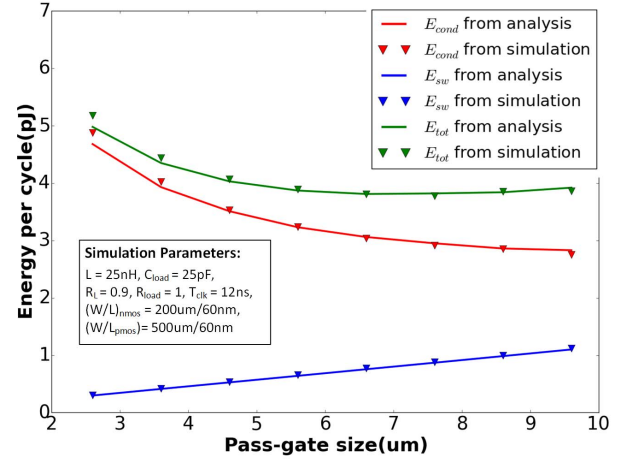


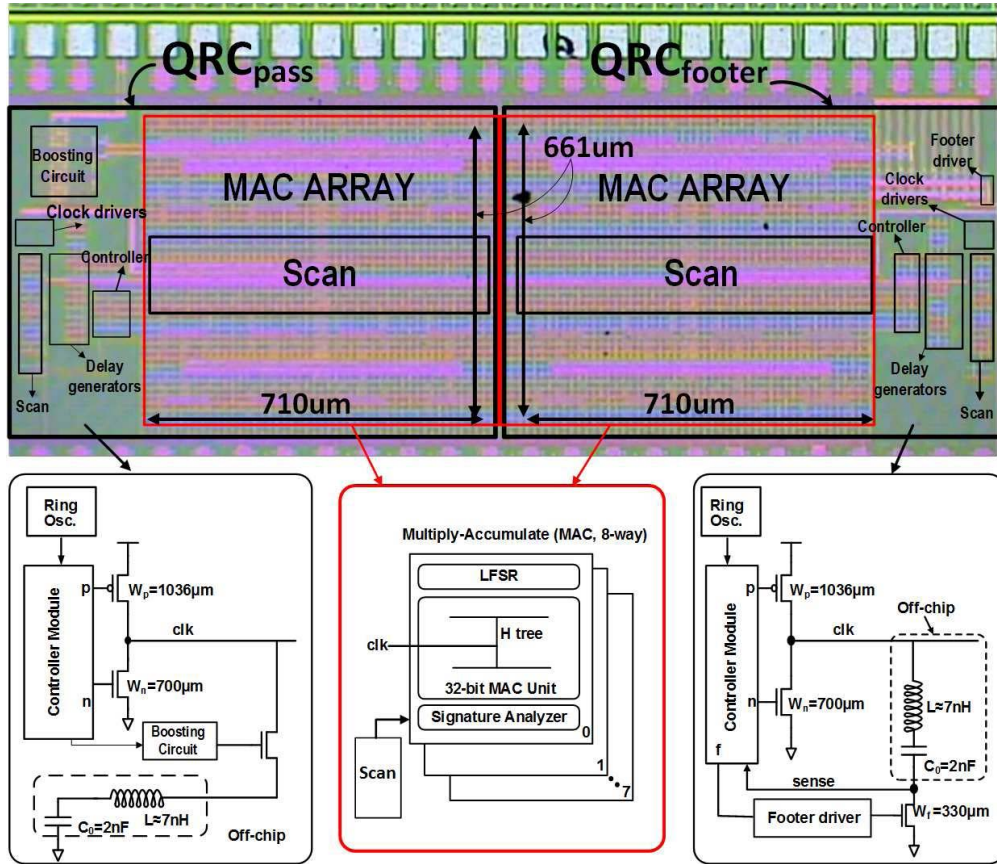
Fig. 14. Comparison of post-layout simulations of QRC with analytical results from (5).

VII. TEST-CHIP ARCHITECTURE AND MEASUREMENTS

In this section, we present the architecture and implementation of the QRC test-chip featuring the QRC_{foot} and QRC_{pass} variants, and their test-chip measurements.

A. Test-Chip Architecture

QRC_{foot} and QRC_{pass} are implemented separately as DVFS compliant clock distributions for an eight-way MAC array datapath in 65-nm CMOS (Fig. 15). Both datapaths employ build-in self test and scan-chains for functional and parametric test. The eight-way MAC was implemented using synthesis, auto-place and route (SAPR). The SAPR flow was augmented to produce a tapered H-Tree wire clock distribution driving a three-level H-Tree driving a clock mesh on metal layers M4 and M5. The clocked comparators, footer-driver, charge pump, delay circuits, and the clock drivers were custom developed. Resonant clocks typically exhibit relatively lower skew due to low network resistance [6], [7]. The inherent slew degradation in resonant clocks, however, causes significant PVT-induced skew in post-gater clock distributions, leading to potential setup and hold-time degradation. Of the several techniques available to mitigate this degradation [6], [7], [15], we adopt latch-based design [15] approach. C_{acg} is implemented as an off-chip electrolytic capacitor for both variants.

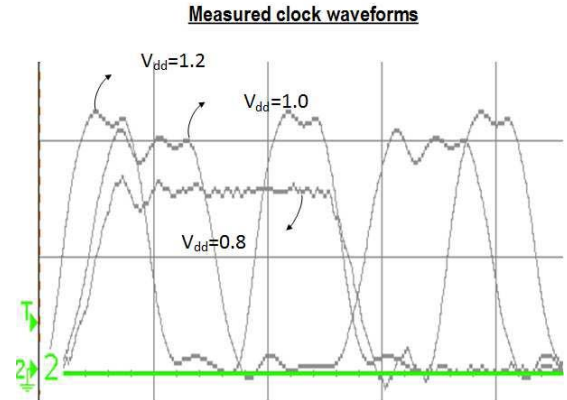
Fig. 15. Dieshot of the QRC_{pass} and QRC_{foot} test-chip.

This test-chip used an off-chip inductor in the implementation of QRC_{foot} and QRC_{pass} . While on-chip inductors can be used for QRC, the choice of off-chip inductors was driven by the desire to explore the impact of inductor selection for slewrates and efficiency tradeoffs, and be able to readily capture resulting QRC clock waveforms (Fig. 16). Notably, use of on-chip inductors does not significantly degrade system efficiency because M_c losses largely dominate system Q (≈ 1.3 for QRC_{pass} , ≈ 1.2 – 1.8 for QRC_{foot}). Robust system operation was ensured through the design of the resonant-clock latch-based design methodology [15]. Runtime voltage-frequency scaling was performed by using a ring-oscillator powered by the logic supply as a clock source. The energy measurements reported in this paper include the dissipation from all constituent QRC sub-systems. In QRC_{foot} and QRC_{pass} , the value of C_{acg} and L are 5 nF and 7 nH, respectively. The extracted value of capacitance, C_{load} is approximately 180 pF.

As mentioned in Section III, an energy-optimal selection of $T_{BLD,p}/T_{BLD,n}$ exists. In the QRC_{pass} and QRC_{foot} implementations, $T_{BLD,p}/T_{BLD,n}$ was implemented with tunable delay chains. After a one-time calibration, the optimum $T_{BLD,p}/T_{BLD,n}$ duration was found to be 80 ps at 1 V.

B. QRC_{foot} and QRC_{pass} Test-Chip Measurements

Fig. 17 shows the uniform energy dissipation per-cycle (EPC) for the QRC_{foot} across a range of operating

Fig. 16. Oscilloscope traces of the QRC clk waveforms across V_{dd} and operating frequency.

frequencies with V_{dd} fixed at 0.8 V. Conventional clocking dissipation was conservatively estimated by downsizing the programmable clock driver to allow EPC measurements at iso-clock slew. This comparison also ignores any electromigration challenges associated with conventionally driving the entire clock load through a central buffer, and ignores the clock power dissipation that would be incurred in distributed clock buffers. The resulting energy efficiency-achieved QRC_{foot} energy reduction compared to conventional clocking is also shown in Fig. 17. Measurements at 0.8 V indicate EPC

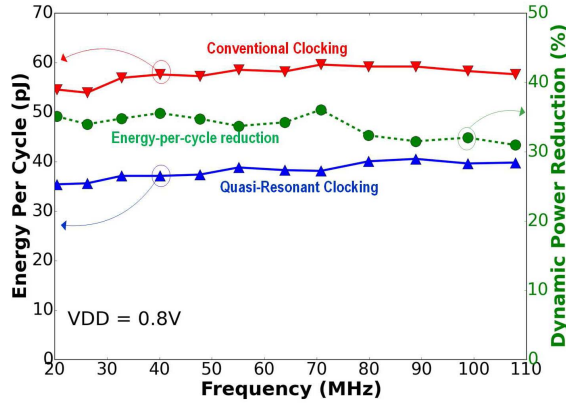


Fig. 17. EPC measurements of QRC_{foot} at $V_{\text{dd}} = 0.8 \text{ V}$ versus operating frequency.

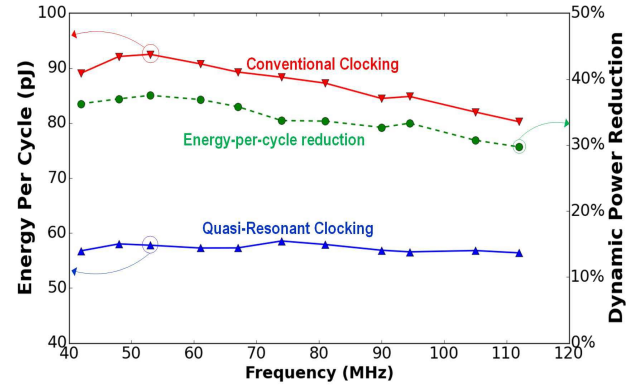


Fig. 20. EPC measurements of QRC_{pass} at $V_{\text{dd}} = 0.7 \text{ V}$ versus operating frequency.

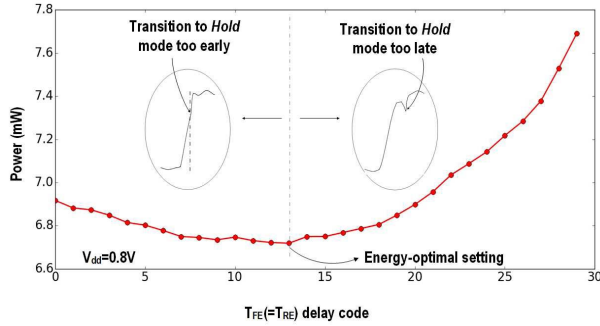


Fig. 18. EPC measurements of QRC_{foot} over a range of delay values for c . The autonomous timing control module was overridden to enable the delay code sweep.

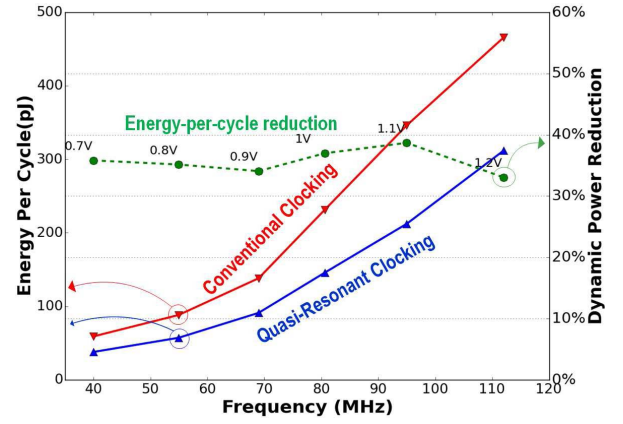


Fig. 21. EPC measurements of QRC_{pass} operating under a Dynamic Voltage-Frequency Scaling range of 0.7–1.2 V.

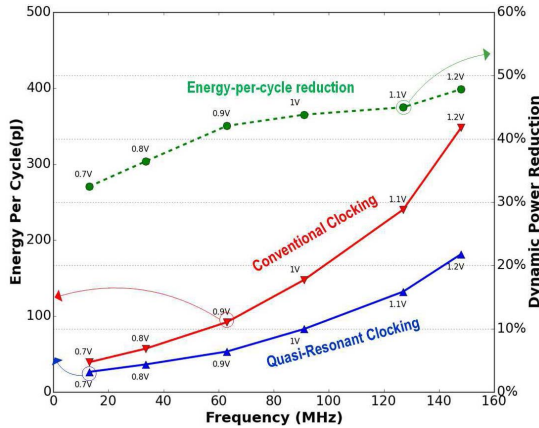


Fig. 19. EPC measurements of QRC_{foot} operating under a dynamic voltage-frequency scaling range of 0.7–1.2 V.

savings of 32%–39% compared to the traditional clocking. Since gate overdrive was not employed for M_c in QRC_{foot} , higher voltages yield improved energy efficiency due to the more significant reduction in conduction losses.

To demonstrate importance of precisely timed gate control of M_c , a manual override was used to sweep the delay codes for the t_{rise} and t_{fall} delay chains (Fig. 6) across a range of values and the resulting EPC reduction was measured.

Fig. 18 demonstrates the impact of M_c timing on energy-efficiency. Low delay codes result in premature de-assertion of M_c , while late delay codes result in late M_c disconnection, both resulting in excessive conduction losses.

The energy efficiency of QRC_{foot} under DVFS is shown in Fig. 19. The core supply voltage was swept from 1.2 to 0.7 V, and the on-chip core-supply powered ring oscillator provided the accompanying frequency scaling. QRC_{foot} achieves an energy reduction of 32%–47% (across 0.7–1.2 V). QRC does not fundamentally limit scaling V_{dd} to 0.7 V or set a lower bound on the operating frequency in any way, a fact verified through simulation. The test-chip lower bounds in frequency and voltage in this test chip were the result of a design oversight pertaining to the use of level converters.

Fig. 20 shows measured EPC versus frequency at $V_{\text{dd}} = 0.8 \text{ V}$. Fig. 21 shows EPC dissipation of QRC_{pass} across a V_{dd} range of 0.7–1.2 V. Also included for reference are the conventional EPC numbers at corresponding voltages. Compared to traditional resonant clocking, QRC_{pass} efficiency is relatively insensitive to frequency. Consistent with simulations, measured EPC values are lower than conventional clocking, but higher than QRC_{foot} . Increased QRC_{pass} EPC over QRC_{foot} is largely attributable to the additional switching losses in the boosting circuit. Notably, QRC_{pass} efficiency remains

	JSSC'13[6]	ISSCC'14[7]	ISSCC'13[20]	This work	
				QRC _{foot}	QRC _{pass}
Process Technology	32nm CMOS	22nm SOI	40nm CMOS	65nm CMOS	65nm CMOS
System Resonant frequency	3.3GHz	≈ 3.1GHz, 4GHz (two modes)	Always Resonant	Always Resonant	Always Resonant
Voltage-Frequency scalable resonance	No	No	No	Yes	Yes
Voltage Range	1.0V-1.2V	0.75-1.05V	0.37V*	0.7V-1.2V	0.7V-1.2V
Frequency Range	2.4-4GHz	2.5GHz - 5GHz	DC - 0.98MHz	DC - 152MHz	DC - 132MHz
Duty Cycle Control	Limited	Limited	No	Yes	Yes
Dynamic Power Reduction	15%-30%	25%-33%	36%	32%-47%*	34%-38%*
Inductor	On-Chip (1nH-3nH each)	On Chip (0.3nH-2.5nH each)	Off-chip 7μH	Off-chip ~7nH	Off-chip ~7nH
SIMO-capable	No	No	No	No	Yes

Fig. 22. Comparison of the proposed QRC architecture and test-chip measurements with related works.

approximately constant across voltage and frequency scaling, a trend enabled by gate-boosting M_c .

Fig. 22 compares key design metrics of both QRC variants with related works. Overall, QRC demonstrates scaling across a wide voltage–frequency range. Near-uniform efficiency is achieved over a broad range of frequencies. Another important capability of QRC is its ability to achieve a broad duty-cycle range and ability to service multiple clock domains using a single inductor.

VIII. CONCLUSION

We presented the QRC architecture and demonstrated the first-ever continuous voltage–frequency scalable resonant clocking system. Autonomous timing control of QRC circuits plays a central role in enabling robust, efficient QRC operation. We presented test-chip implementation of two variants of QRC, implemented in 65-nm CMOS. Energy-efficiency measurements from the test-chip validate ability to QRC to achieve uniform efficiency across frequency scaling. DVFS measurements in the 0.7–1.2 V range indicate EPC reduction of 32%–47%, and 34%–38% using QRC_{foot} and QRC_{pass}, respectively. Ability to achieve 0-cycle latency duty-cycle control offers a promising opportunity for QRC to be employed in a broader range of applications driving large capacitive loads beyond system clocking.

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