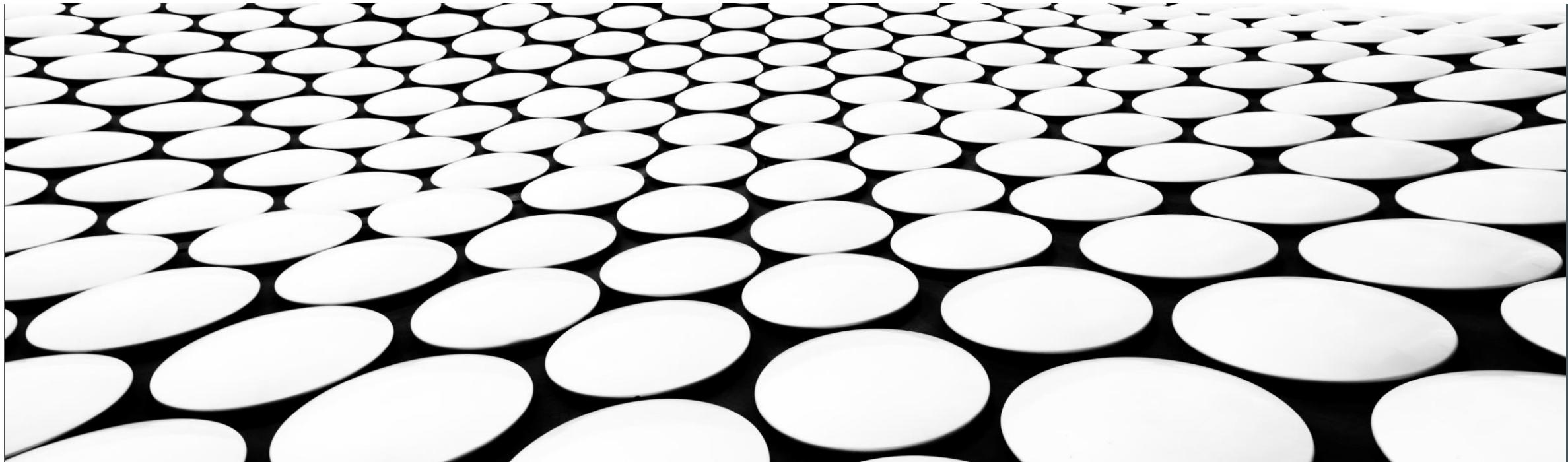

INFO-H-502 – VIRTUAL REALITY

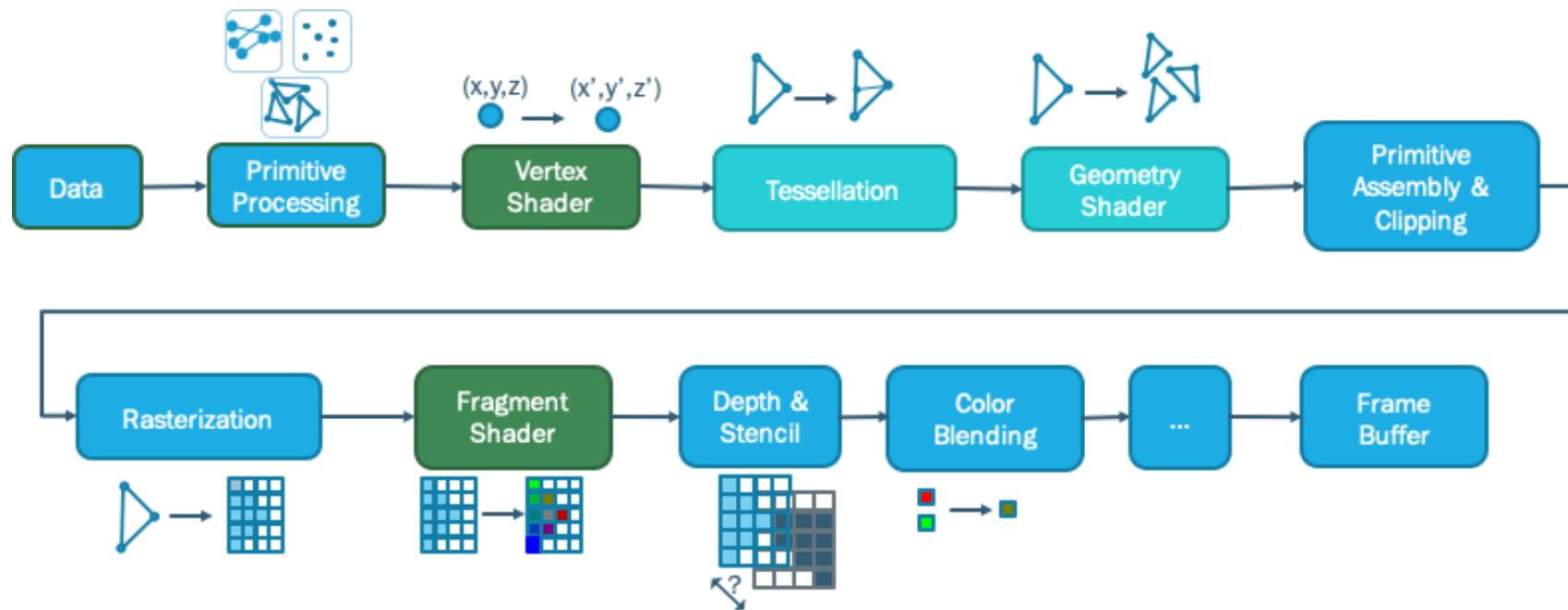
EXERCISES 03

ELINE SOETENS – LAURIE VAN BOGAERT

GAUTHIER LAFRUIT – DANIELE BONATTO

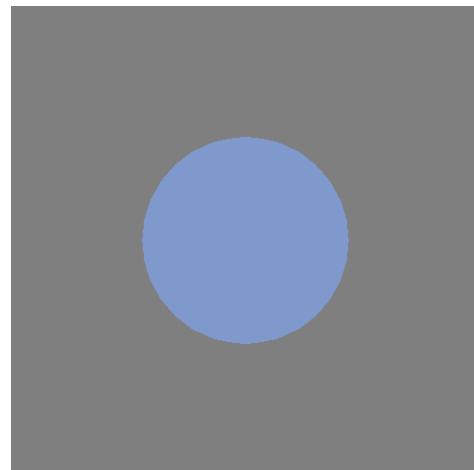


LAST TIME

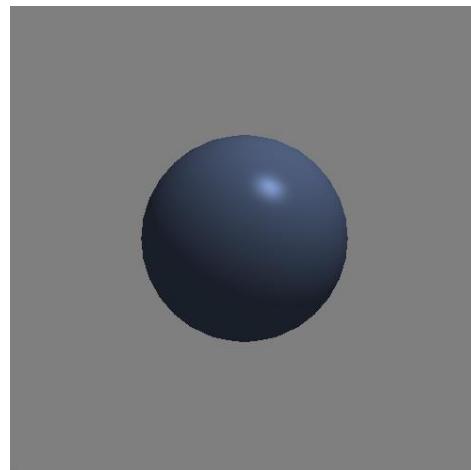


The whole pipeline

THIS TIME

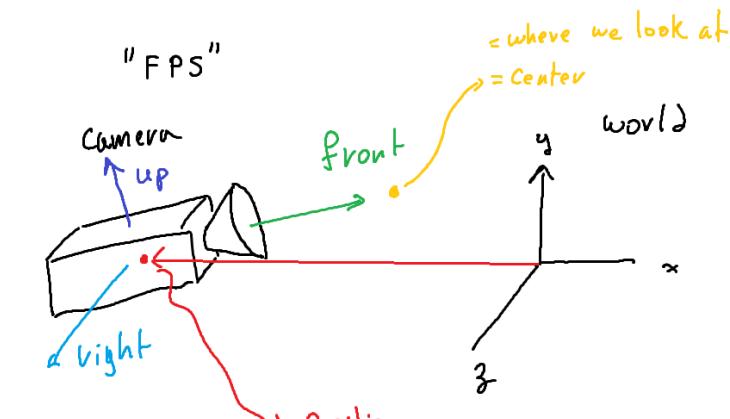


VS

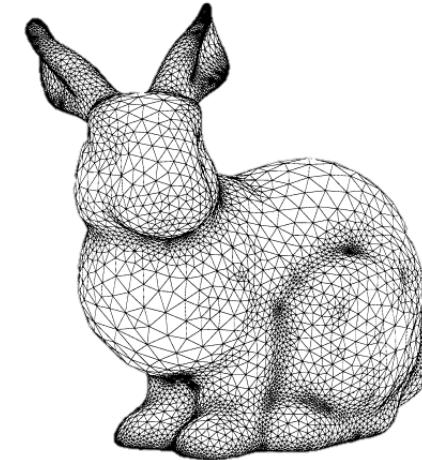


No lights

Lights



Camera



Loading a model

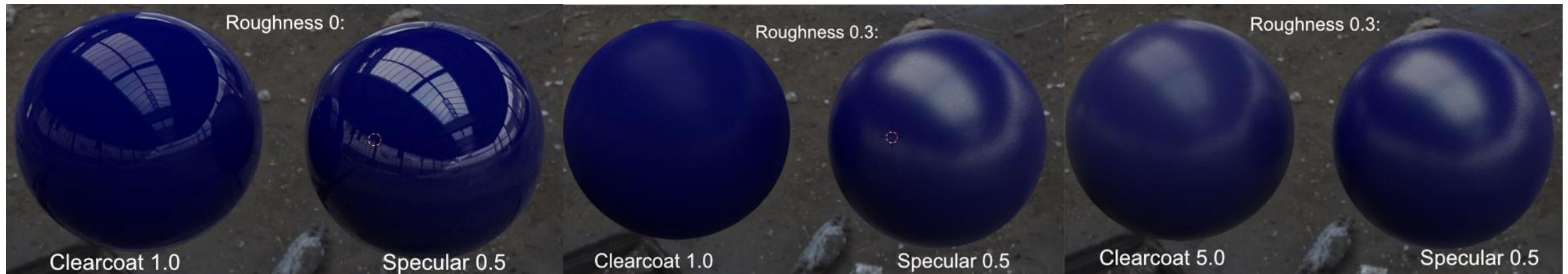
```
MeshVersionFormatted 1
Dimension 3
Vertices
5433
-0.0260146 0.112578 0.0363871 0
-0.0321783 0.174119 -0.00263321 0
-0.080718 0.152855 0.0302446 0
-0.0231294 0.112186 0.0386436 0
0.0164928 0.122293 0.0314234 0
-0.0248365 0.156574 -0.00377469 0
0.0452628 0.0863563 0.0200367 0
-0.071339 0.155715 0.00712639 0
-0.0100758 0.125949 0.0297379 0
-0.0720133 0.154518 0.0303984 0
```

THEORY VS EXERCISES

- In the theoretical lectures: Raytracing
- Here: what is light and how we can draw nice things without raytracing (less computation)
 - Feel free to skip the theoretical slides and jump to how to implement! (Slide ~17)
 - Theory in here only to help comprehension

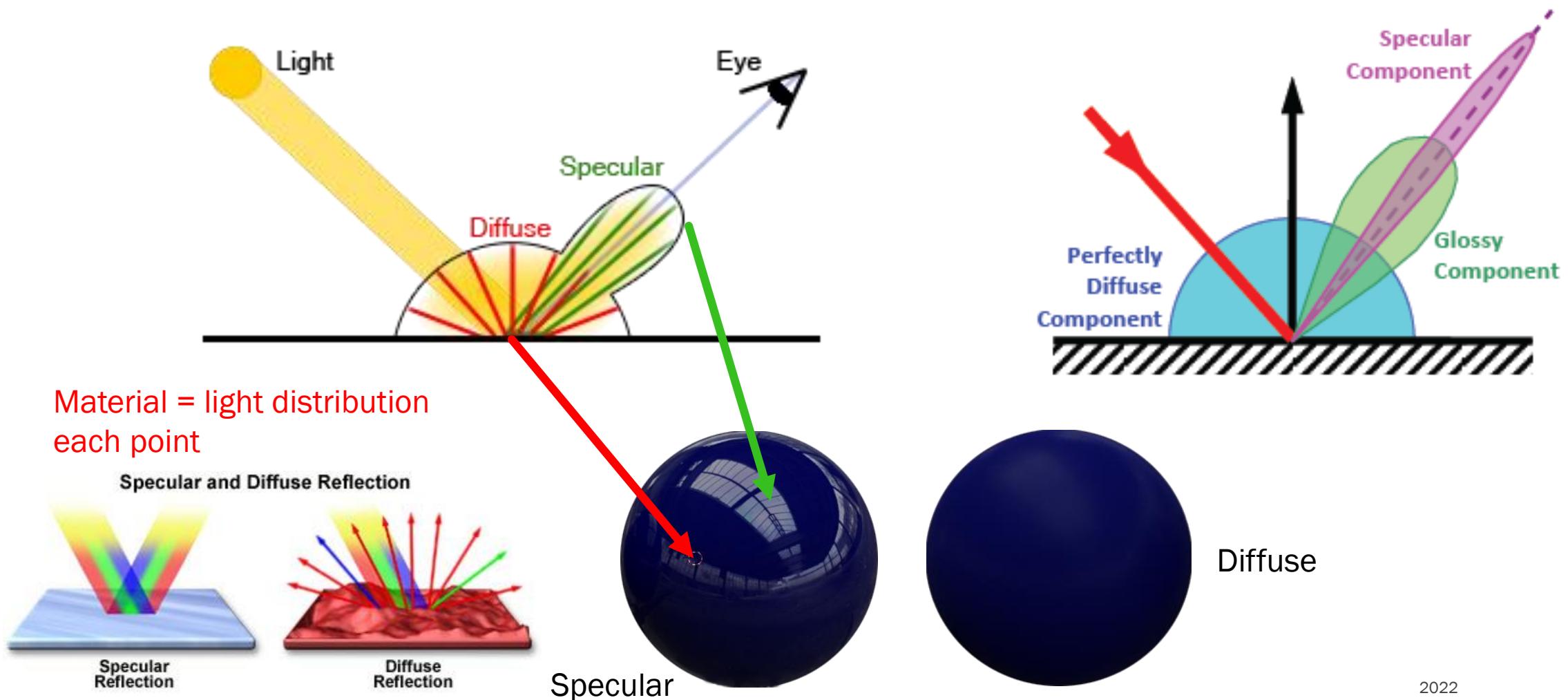
LIGHT – BIDIRECTIONAL REFLECTANCE DISTRIBUTION FUNCTION (BRDF)

- This is how materials are modelled

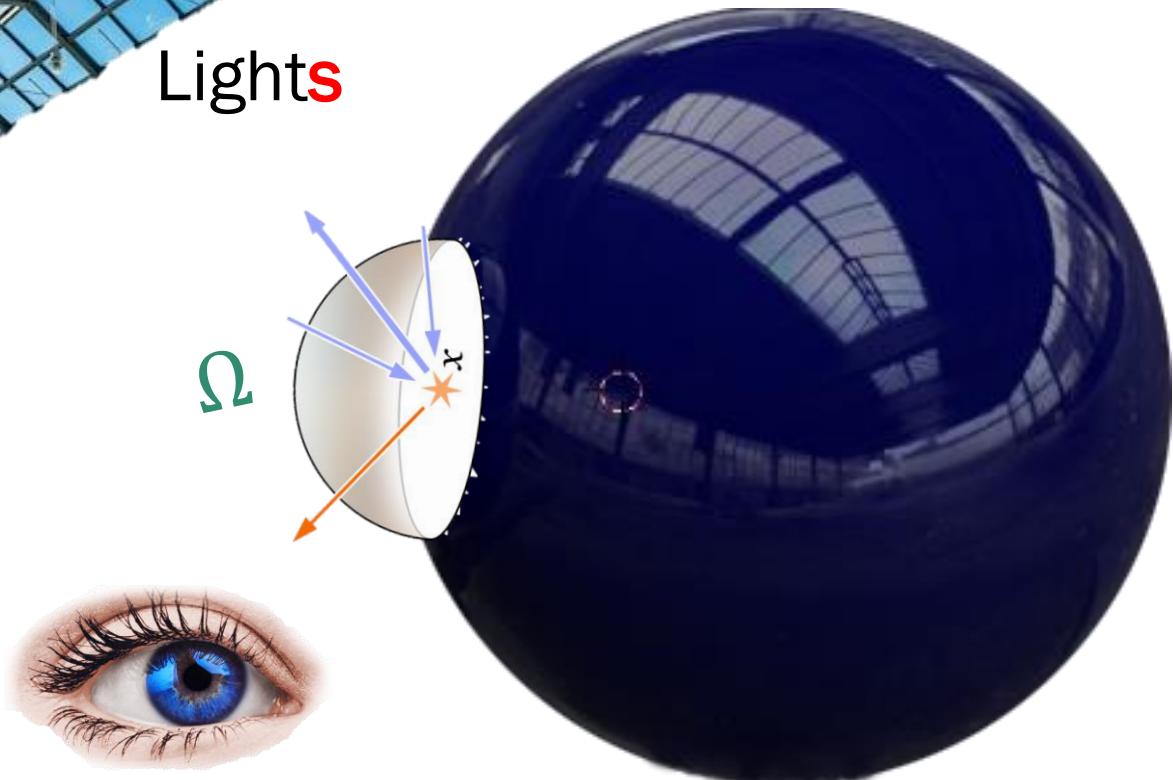


Mix of diffuse and specular lights

LIGHT – BIDIRECTIONAL REFLECTANCE DISTRIBUTION FUNCTION (BRDF)



LIGHT – BIDIRECTIONAL REFLECTANCE DISTRIBUTION FUNCTION (BRDF)

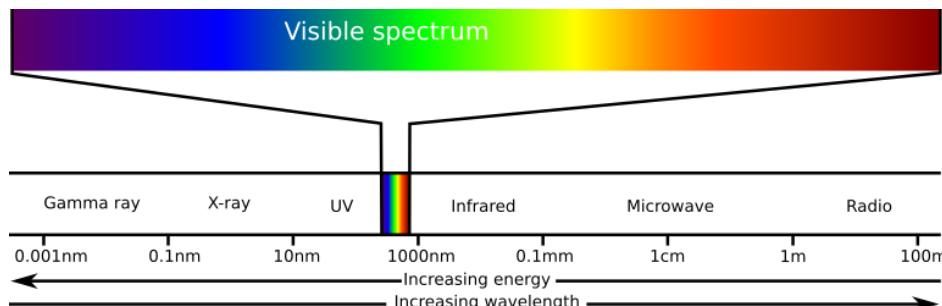


Compute it at each point

BUT: light comes from everywhere

LIGHT – THE RENDERING EQUATION

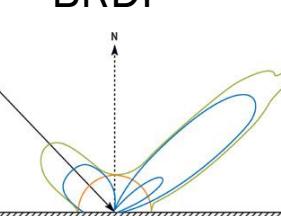
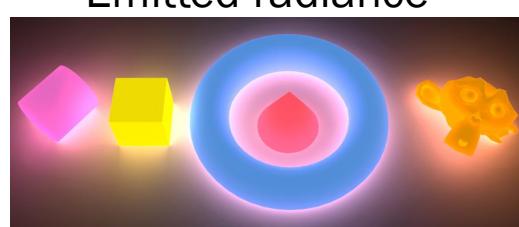
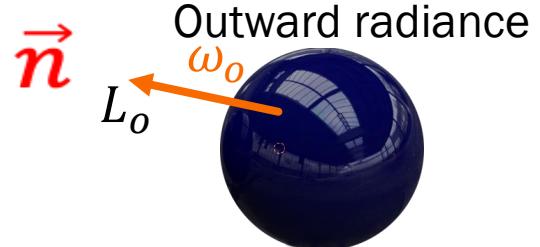
λ = wavelength



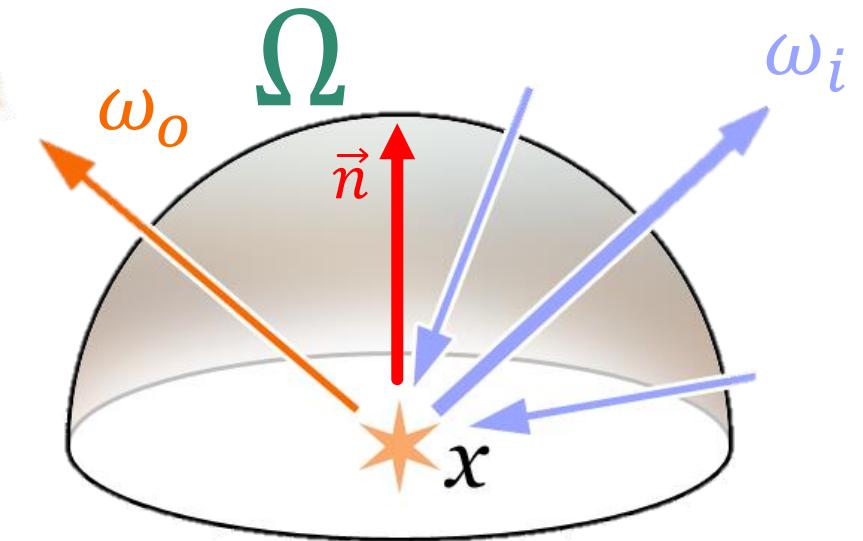
t = time

How is it computed?

- $$L_o(\vec{x}, \omega_o, \lambda, t) = L_e(\vec{x}, \omega_o, \lambda, t) + \int_{\Omega} f_r(\vec{x}, \omega_i, \omega_o, \lambda, t) L_i(\vec{x}, \omega_i, \lambda, t) (\omega_i \cdot \vec{n}) d\omega_i$$



Add all the lights



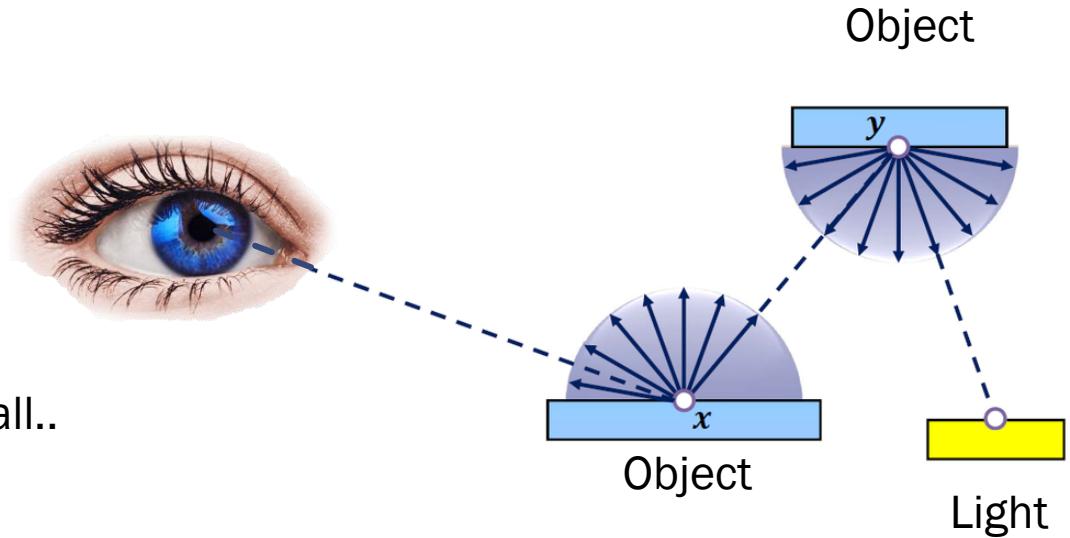
BRDF
Inward radiance
= $L_o(\vec{x}', \omega_i, \lambda, t)$
Raytracing
Recursion here

$\cos \theta$ weight

LIGHT – THE RENDERING EQUATION

- $$L_o(\vec{x}, \omega_o, \lambda, t) = L_e(\vec{x}, \omega_o, \lambda, t) + \int_{\Omega} f_r(\vec{x}, \omega_i, \omega_o, \lambda, t) L_i(\vec{x}, \omega_i, \lambda, t) (\omega_i \cdot \vec{n}) d\omega_i$$

This is a recursive call..



BUT... how can we code this..
...without raytracing...

RENDERING EQUATION – SIMPLIFICATIONS – CONSTANCE IN TIME

Outward radiance

Emitted radiance

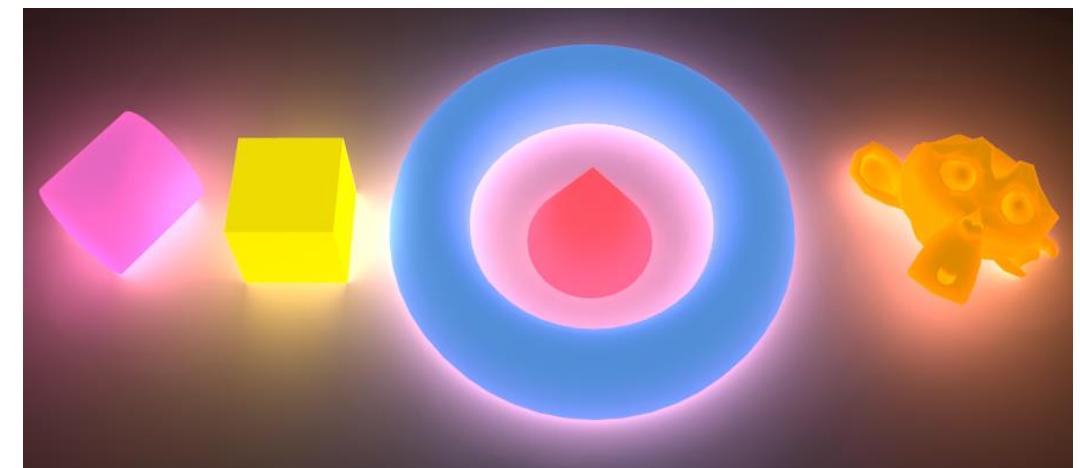
BRDF

Inward radiance

- $L_o(\vec{x}, \omega_o, \lambda, t) = L_e(\vec{x}, \omega_o, \lambda, t) + \int_{\Omega} f_r(\vec{x}, \omega_i, \omega_o, \lambda, t) L_i(\vec{x}, \omega_i, \lambda, t) (\omega_i \cdot \vec{n}) d\omega_i$
- $L_o(\vec{x}, \omega_o, \lambda, t) = L_e(\vec{x}, \omega_o, \lambda, t) + \int_{\Omega} f_r(\vec{x}, \omega_i, \omega_o, \lambda, t) L_i(\vec{x}, \omega_i, \lambda, t) (\omega_i \cdot \vec{n}) d\omega_i$
- $L_o(\vec{x}, \omega_o) = L_e(\vec{x}, \omega_o) + \int_{\Omega} f_r(\vec{x}, \omega_i, \omega_o) L_i(\vec{x}, \omega_i) (\omega_i \cdot \vec{n}) d\omega_i$

SIMPLIFYING THE EMITTED LIGHT

- $L_o(\vec{x}, \omega_o) = L_e(\vec{x}, \omega_o) + \int_{\Omega} f_r(\vec{x}, \omega_i, \omega_o) L_i(\vec{x}, \omega_i) (\omega_i \cdot \vec{n}) d\omega_i$
- The emitted light can be set as a constant color for the object
- $L_e(\vec{x}, \omega_o) = E$
- $L_o(\vec{x}, \omega_o) = E + \int_{\Omega} f_r(\vec{x}, \omega_i, \omega_o) L_i(\vec{x}, \omega_i) (\omega_i \cdot \vec{n}) d\omega_i$

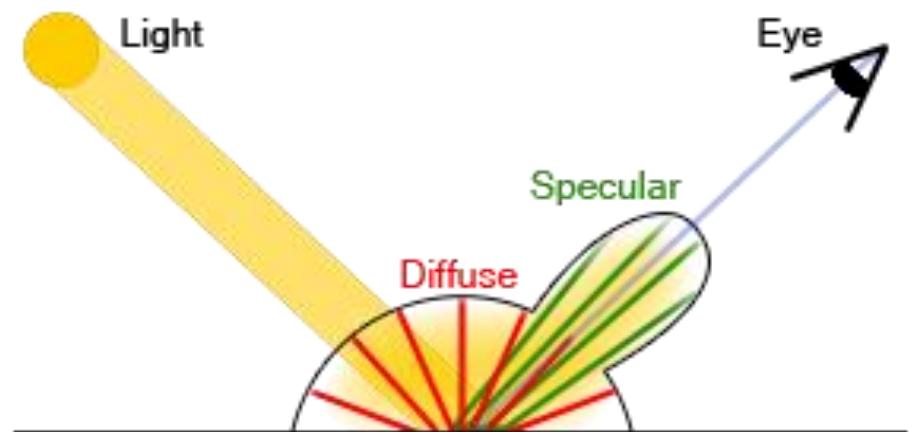


SIMPLIFYING THE BRDF

Let's focus on the light i

- $L_o(\vec{x}, \omega_o) = E + \int_{\Omega} f_r(\vec{x}, \omega_i, \omega_o) L_i(\vec{x}, \omega_i) (\omega_i \cdot \vec{n}) d\omega_i$
- The BRDF can be decomposed in specular and diffuse parts
- $f_r(\vec{x}, \omega_i, \omega_o) = \text{diffuse} + \text{specular} (= \text{diff} + \text{spec})$
- $L_o(\vec{x}, \omega_o) = E + \int_{\Omega} (\text{diff} + \text{spec}) L_i(\vec{x}, \omega_i) (\omega_i \cdot \vec{n}) d\omega_i$

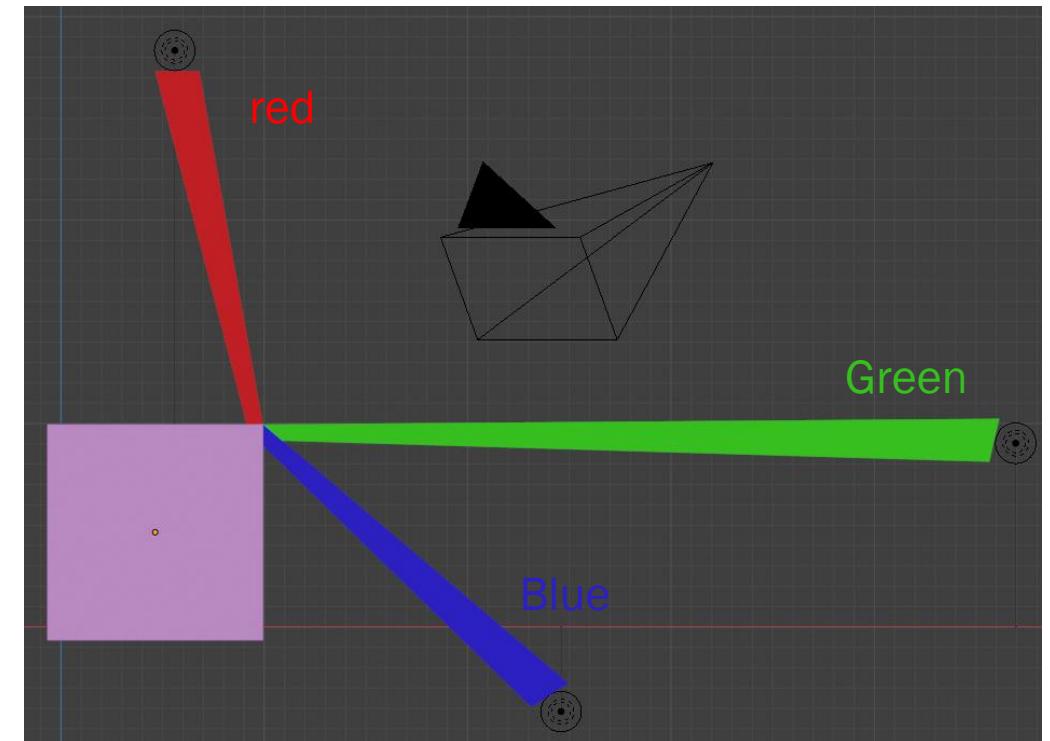
No more dependence in ω_o for the diffuse light



SIMPLIFYING THE INWARD RADIANCE

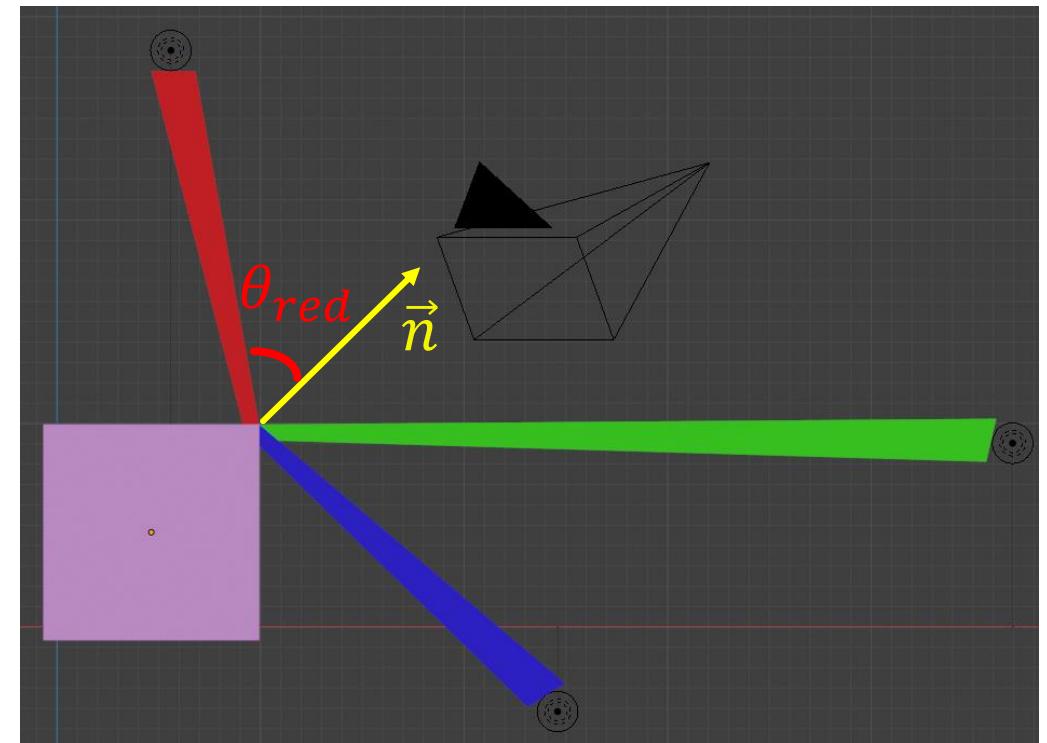
- $L_o(\vec{x}) = E + \int_{\Omega} (diff + spec) L_i(\vec{x}, \omega_i) (\omega_i \cdot \vec{n}) d\omega_i$
- Radiance coming from reflection of other objects is considered negligible
- The inward radiance can be set as a constant color (per light)
- $L_i(\vec{x}, \omega_i) = L_i$
- $L_o(\vec{x}) = E + \int_{\Omega} (diff + spec). L_i (\omega_i \cdot \vec{n}) d\omega_i$

Let's focus on the light i



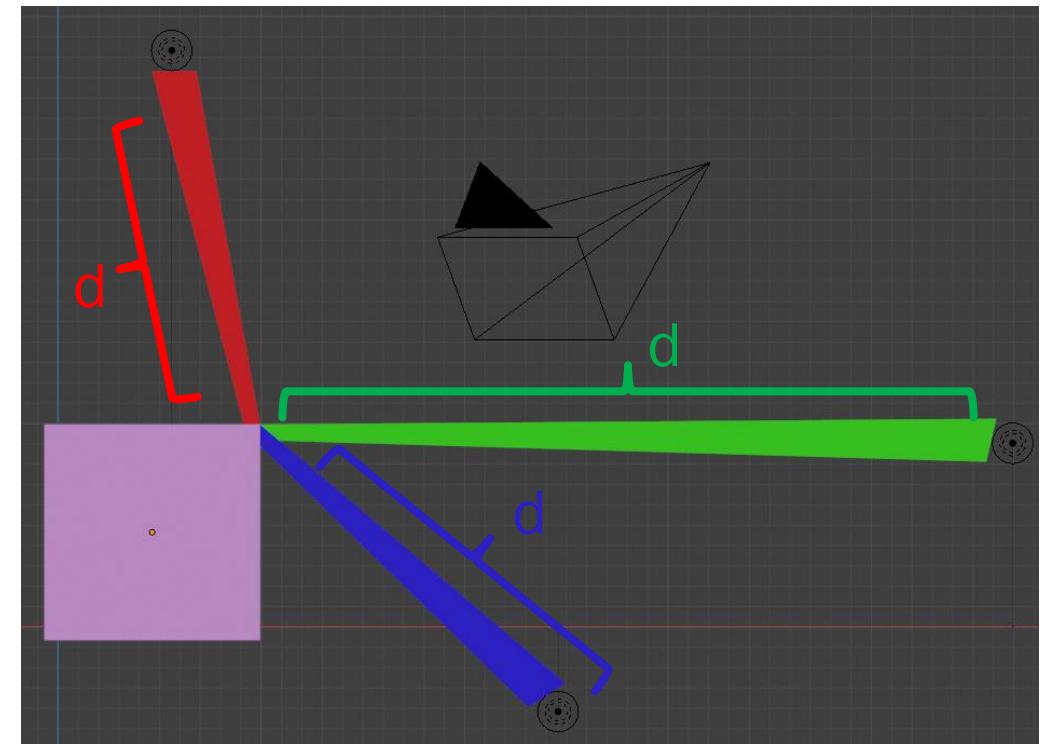
SIMPLIFYING – NOTE: THE CONTRIBUTION OF EACH LIGHT

- $L_o(\vec{x}) = E + \int_{\Omega} (diff + spec).L_i (\omega_i \cdot \vec{n}) d\omega_i$
- Those lights are still attenuated with the cosine (or removed)
- $(\omega_i \cdot \vec{n}) = \cos \theta_i$
- $L_o(\vec{x}) = E + \int_{\Omega} (diff + spec).L_i \cos \theta_i d\omega_i$



SIMPLIFYING – NOTE: ATTENUATION WITH DISTANCE

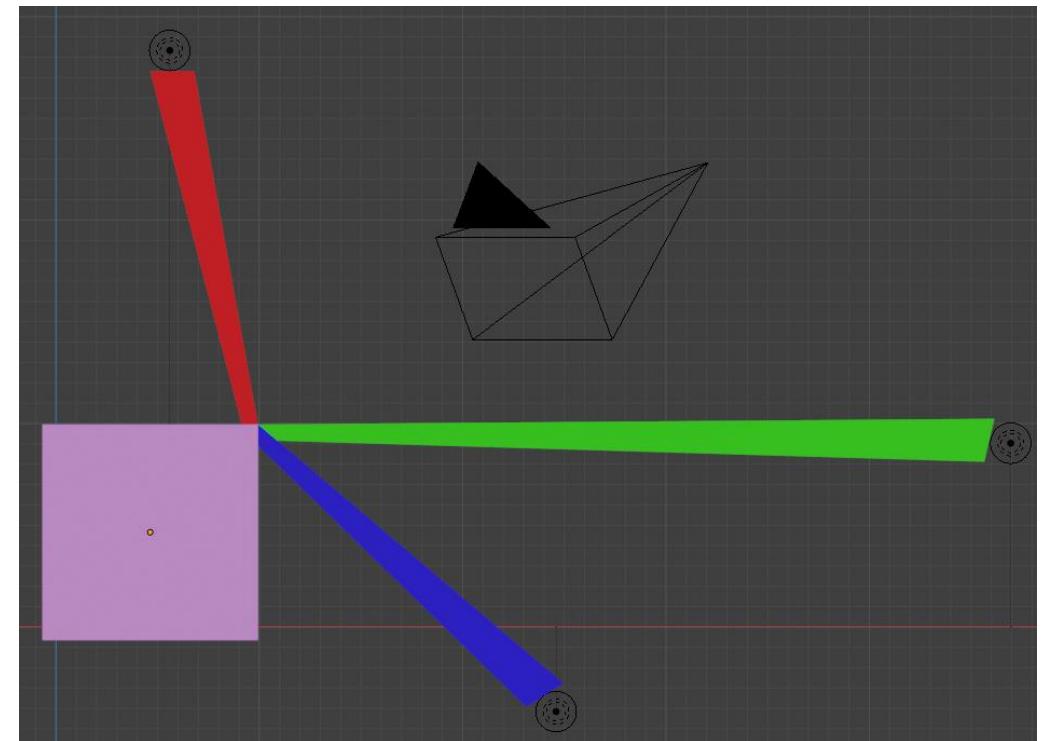
- $L_o(\vec{x}) = E + \int_{\Omega} (diff + spec).L_i \cos \theta_i d\omega_i$
- All contributing lights are not at the same distance to the object
- $L_i \rightarrow L_i \cdot att_i$ (multiply by attenuation factor)
- $L_o(\vec{x}) = E + \int_{\Omega} (diff + spec).L_i \cdot att_i \cdot \cos \theta_i d\omega_i$



SIMPLIFYING THE INTEGRAL

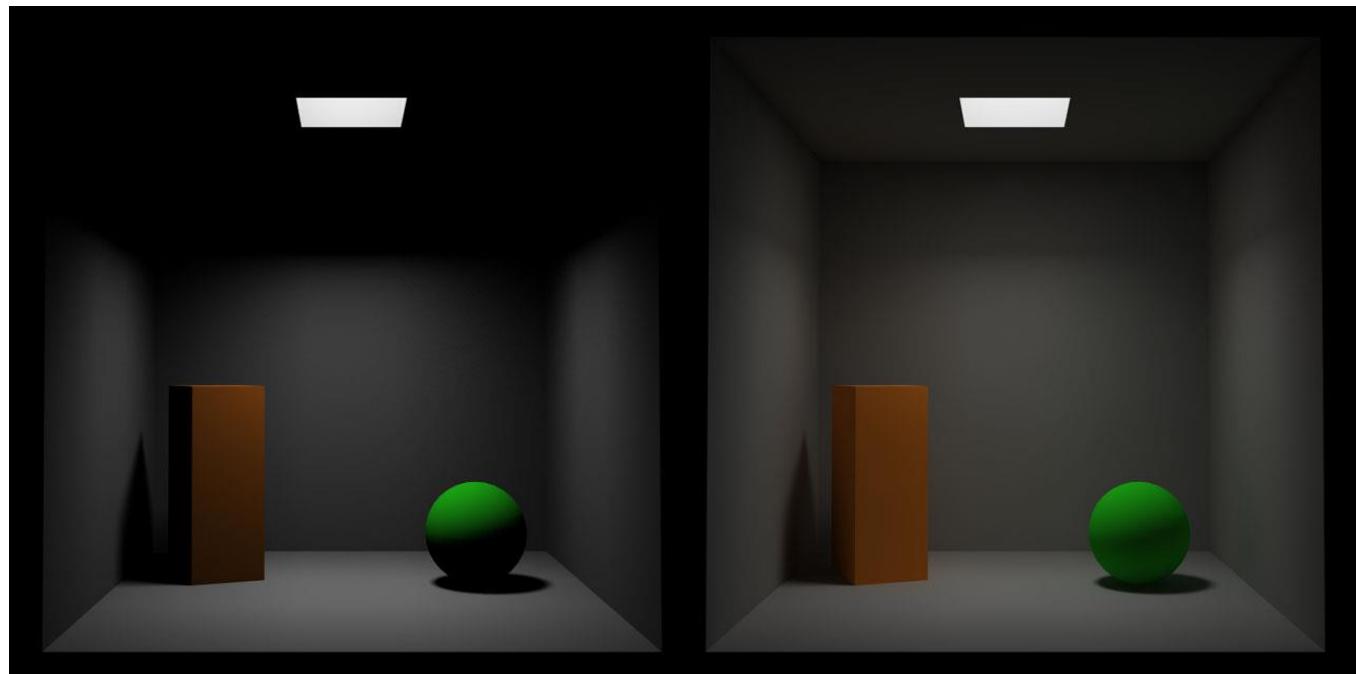
Only 3 lights here!

- $L_o(\vec{x}) = E + \int_{\Omega} (diff + spec).L_i . att_i . \cos \theta_i d\omega_i$
- We have only a finite number (N) of lights in a scene!
- $\iiint \rightarrow \sum_N$
- $L_o(\vec{x}) = E + \sum_N (diff + spec).L_i . att_i . \cos \theta_i$



SIMPLIFYING – NOTE: TOO DARK?

- $L_o(\vec{x}) = E + \sum_N (diff + spec) \cdot L_i \cdot att_i \cdot \cos \theta_i$
- Too many simplifications, scene too dark...
- Add some « ambient » light: A
- $L_o(\vec{x}) = A + E + \sum_N (diff + spec) \cdot L_i \cdot att_i \cdot \cos \theta_i$
- Represent the light reflected from other objects

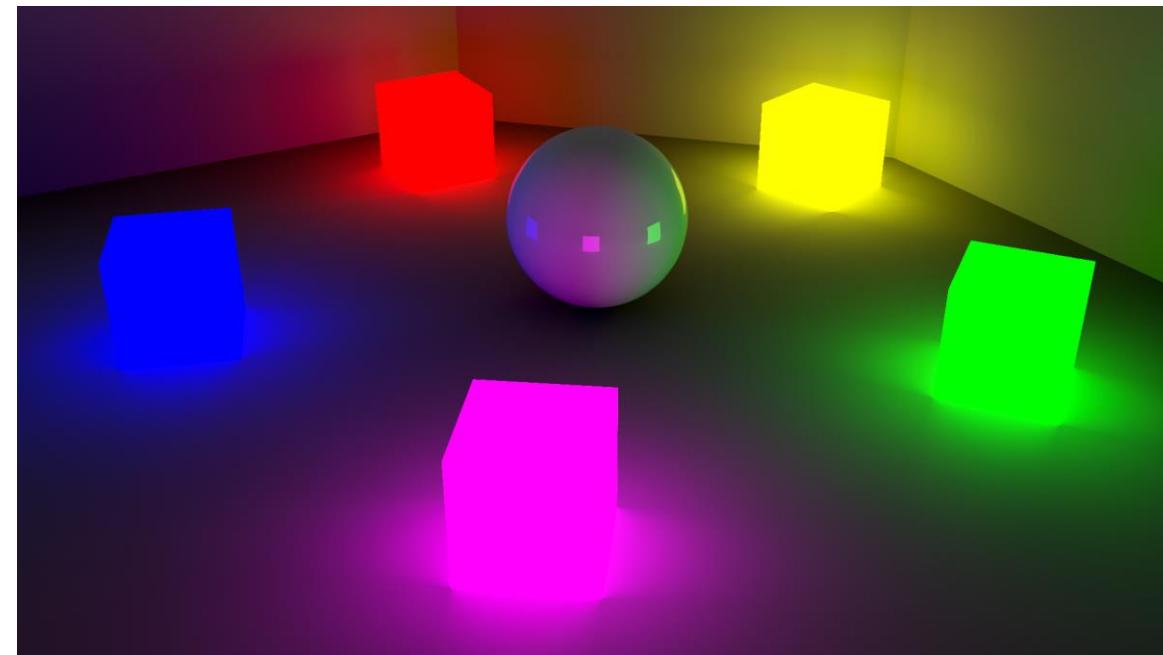


RENDERING EQUATION FOR OPENGL (~BLINN-PHONG MODEL)

- $L_o(\vec{x}) = A + E + \sum_N (diff + spec) \cdot L_i \cdot att_i \cdot \cos \theta_i$

$$(\omega_i \cdot \vec{n})$$

$$\equiv$$



$L_o(\vec{x})$ = Output light color at vertex x

A = Ambient light to compensate

E = Emitted light from the object

Diff = Diffuse factor of the vertex (to be computed)

Spec = Specular factor of the vertex (to be computed)

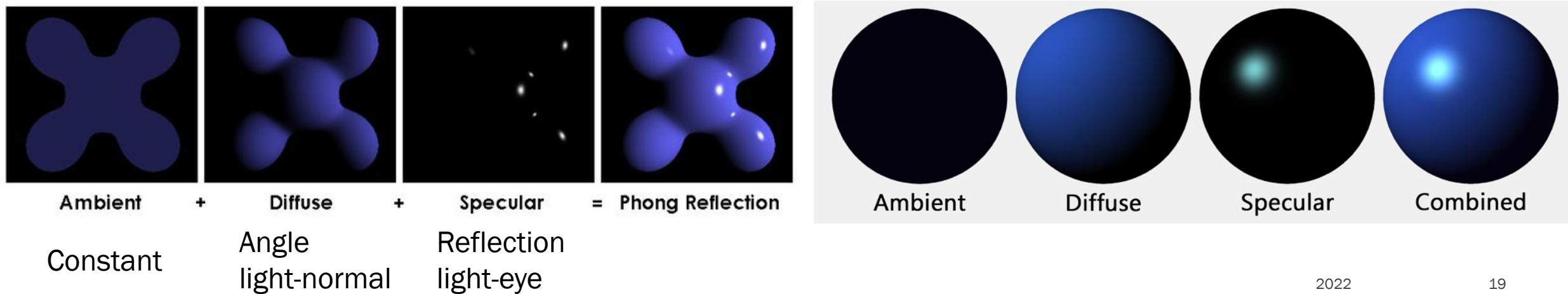
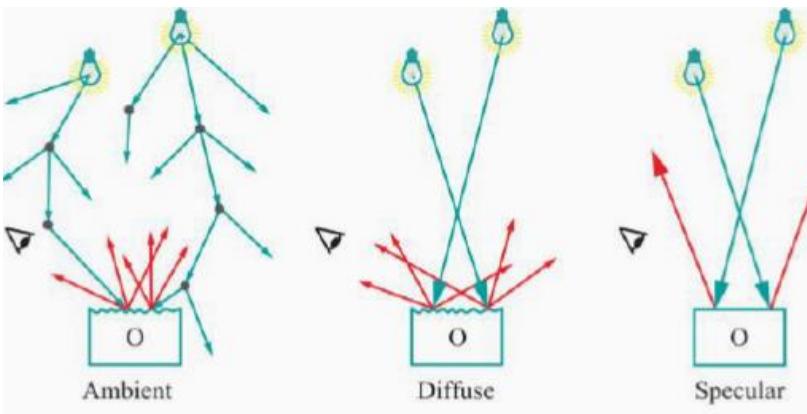
L_i = Constant color for each light i

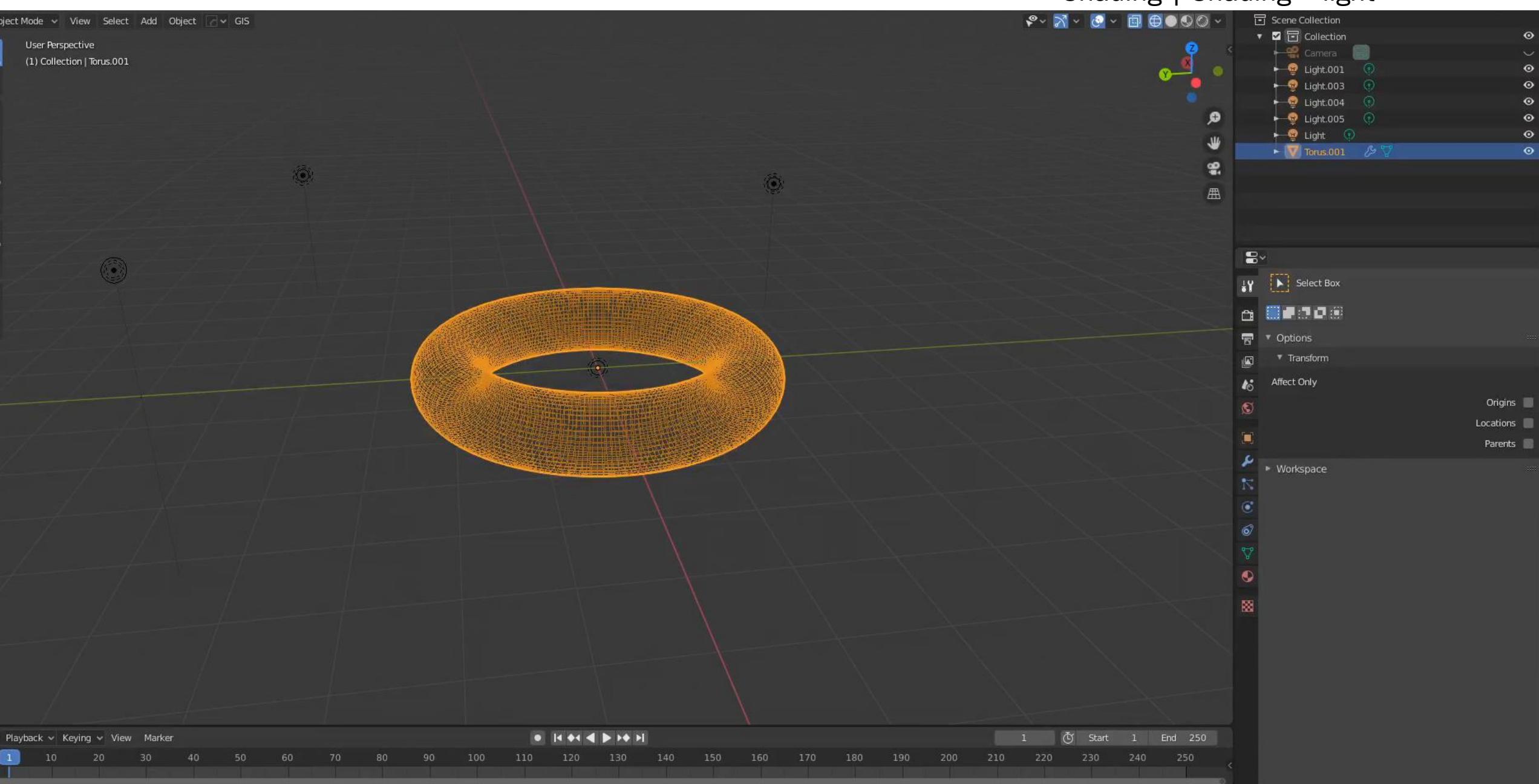
att_i = Attenuation factor for the light i

θ_i = Angle between the light position and the vertex normal

You can skip all previous slides for the exercises!

RENDERING EQUATION - COMPONENTS





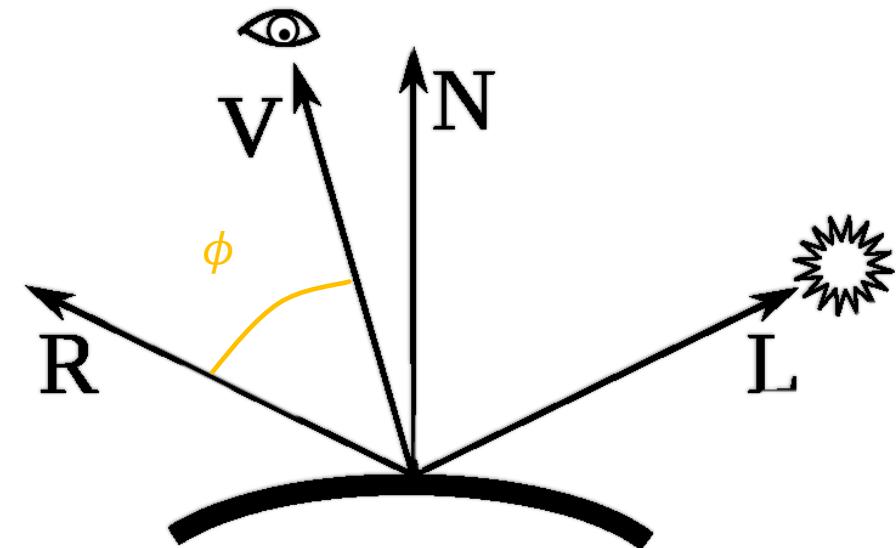
DIFFUSE LIGHT

The diagram shows a yellow sun icon at the bottom left emitting a yellow arrow pointing towards a black vertical line representing a surface. The surface has a grey textured base and a black top edge. From the black edge, several red arrows point upwards and outwards, labeled "incident light". At the top right of the surface, there is a blue arrow pointing upwards, labeled "specular reflection". Several other red arrows point upwards from the surface, labeled "diffuse reflection". The angle between the incident light and the normal vector is indicated by a blue line segment connecting the incident light ray to the surface, with the text "($\omega_i \cdot \vec{n}$) = cos θ = angle between the light and the normal" below it. A blue curved arrow at the top left is labeled "Angular dependence".

- $L_o(\vec{x}) = A + E + \sum_N (diff + spec) \cdot L_i \cdot att_i \cdot (\omega_i \cdot \vec{n})$
- $L_o(\vec{x}) = A + E + \sum_N (diff \cdot (\omega_i \cdot \vec{n}) + spec \cdot (\omega_i \cdot \vec{n})) \cdot L_i \cdot att$
- Depends on the light position and the normal at a point
 - $diff = 1$ (Empirically!)
 - $(\omega_i \cdot \vec{n}) = \cos \theta = \text{angle between the light and the normal}$
- Need to discard negative values as they do not make sense
 - $\max(\omega_i \cdot \vec{n}, 0)$

SPECULAR LIGHT (BLINN-PHONG MODEL)

- $L_o(\vec{x}) = A + E + \sum_N ((\omega_i \cdot \vec{n}) + \text{spec.}(\omega_i \cdot \vec{n})).L_i.att_i$
- $L_o(\vec{x}) = A + E + \sum_N ((\omega_i \cdot \vec{n}) + \text{spec.}(\omega_i \cdot \vec{n})).L_i.att_i$
- Depends on the light vector (L) and the View vector (V) (the camera)
 - Compute the reflection vector (R) from L
 - $R = 2(N \cdot L)N - L$
 - $\cos \phi = R \cdot V$
- $\text{spec} = \cos^\gamma \phi$
- **REMARK:** this is a WRONG MODEL! The $(\omega_i \cdot \vec{n})$ factor disappeared! (But nice results), spec should be divided by it!



! dot products !

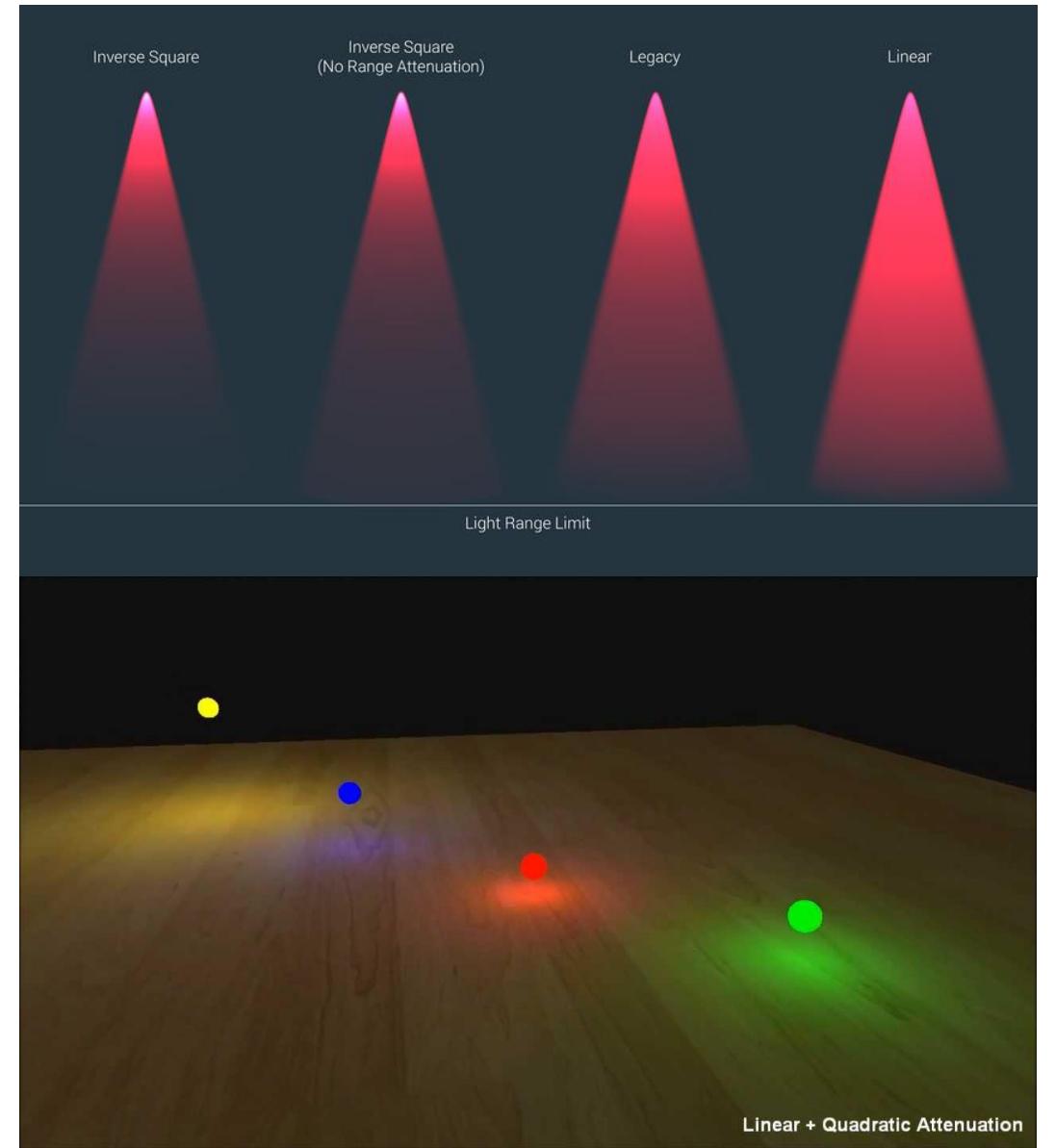
! Normal vectors !

More on the wrong model here:

<https://computergraphics.stackexchange.com/questions/7590/phong-and-the-rendering-equation-whats-with-the-cosine>

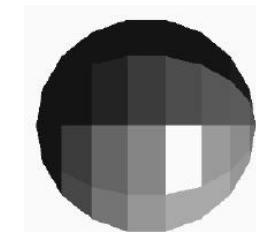
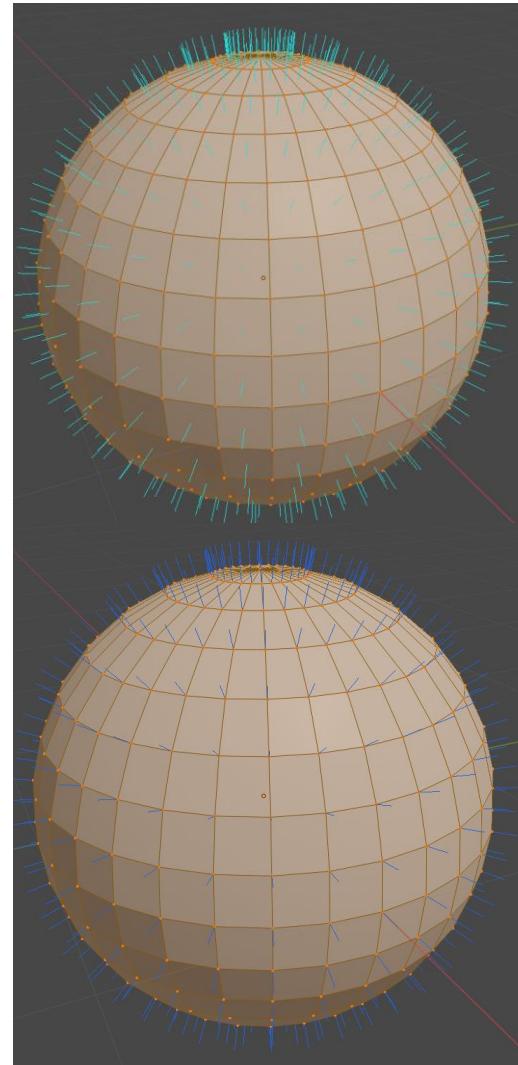
ATTENUATION WITH THE DISTANCE

- $L_o(\vec{x}) = A + E + \sum_N ((\omega_i \cdot \vec{n}) + spec).L_i.att_i$
- $att_i = \frac{1}{k_c^i + k_l^i d^i + k_q^i (d^i)^2}$
 - k_c = Constant attenuation
 - k_l = Linear attenuation
 - k_q = Quadratic attenuation
 - d = Distance between the light source and the fragment

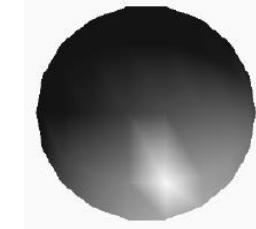


WHERE IS THE RENDERING EQUATION COMPUTED?

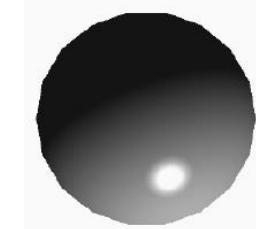
- Flat Shading
 - Every triangle in the scene has one normal
- Gouraud shading
 - Each vertex of each triangle has a normal
 - The **light is computed per vertex** (vertex shader)
 - The **light is interpolated** in the fragment shader
- Phong shading
 - Each vertex of each triangle has a normal
 - The **normals are interpolated** between the vertex and fragment shaders
 - The **light is computed for every fragment** using the normal



Flat

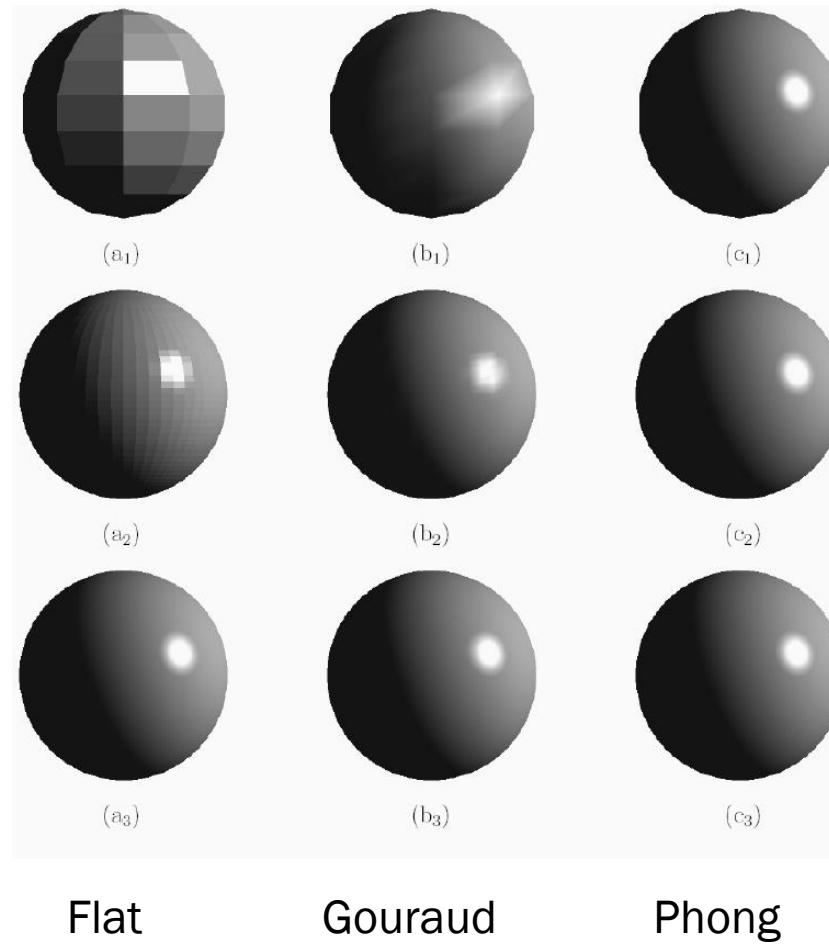


Gouraud



Phong

SHADING AND TRIANGLE COUNT



Less triangles

More triangles

IS THIS IMAGE ACHIEVABLE WITH OPENGL

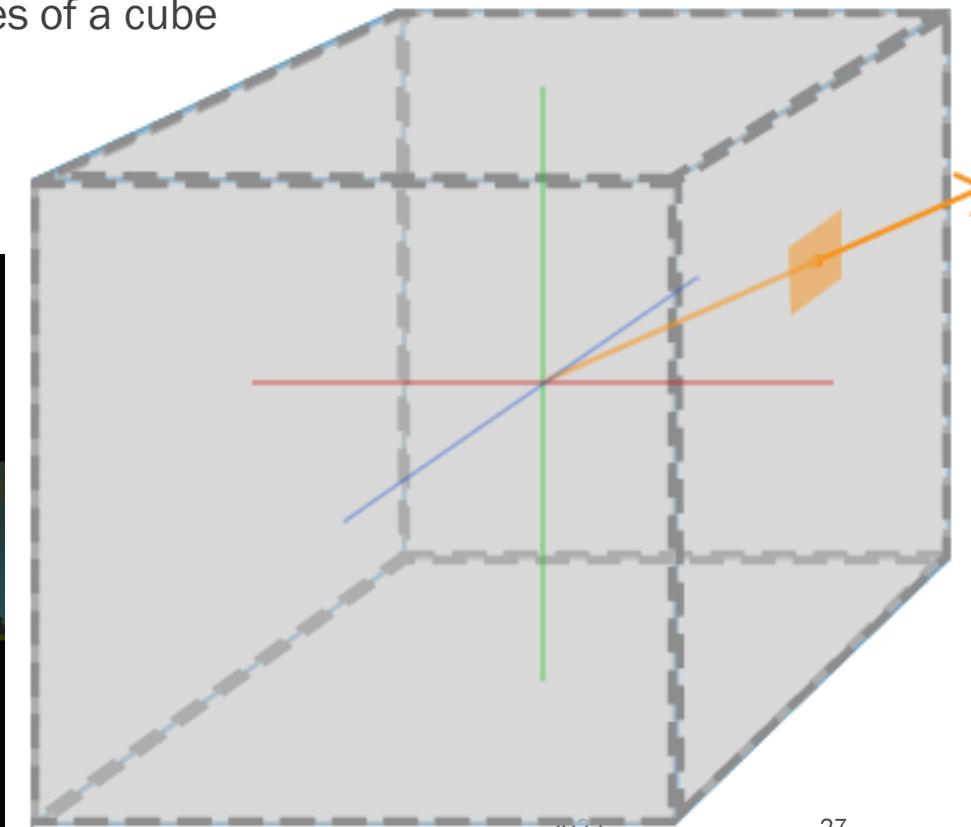
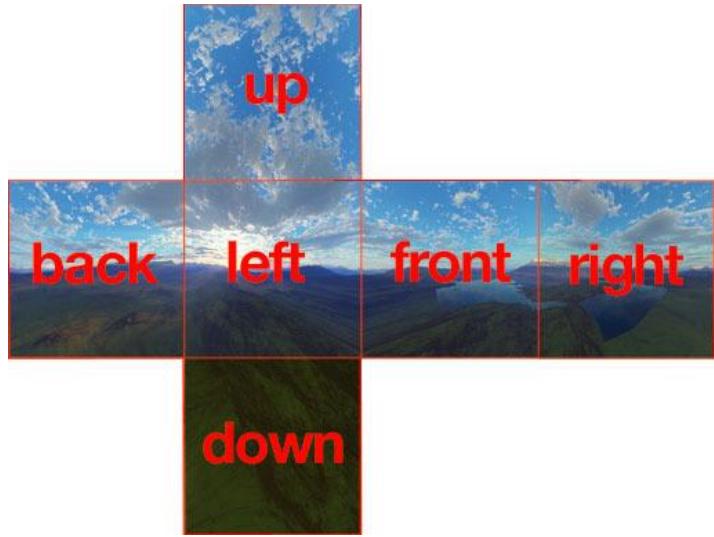


No! Because we don't have raytracing

Yes! Using a cube map

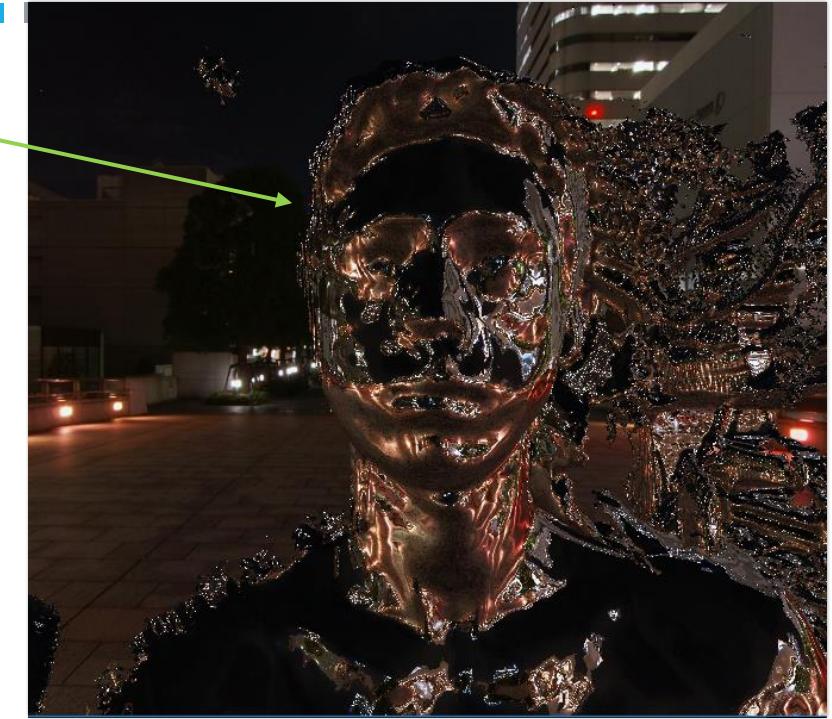
CUBEMAPS

- Cubemap: A texture containing 6 individual 2D textures forming the sides of a cube
- Shaders let you « sample » the cube map using a 3D vector

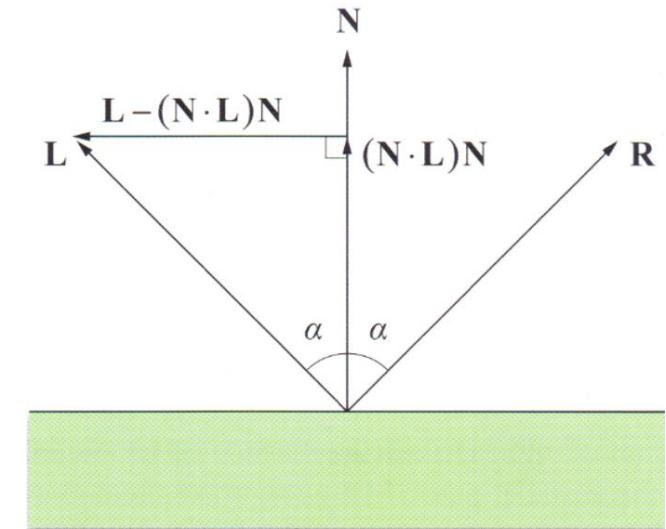


REFLECTION

This is what you should obtain



- Possible because we **sample** our **cubemap**
- $R = 2(L \cdot N)N - L$
- R is the vector used to sample the cubemap

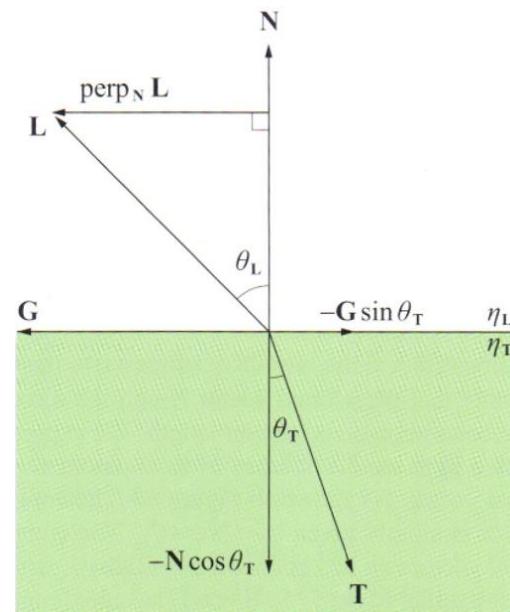


REFRACTION

This is what you should obtain



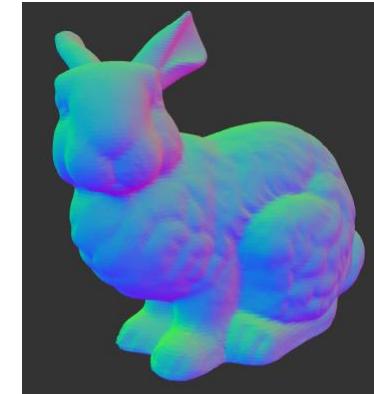
- Refraction also possible because we sample a cubemap
- $T = \left(\frac{\eta_L}{\eta_T} N \cdot L - \sqrt{1 - \frac{\eta_L^2}{\eta_T^2} [1 - (N \cdot L)^2]} \right) N - \frac{\eta_L}{\eta_T} L$
- Vector used to sample the cubemap



Some η_T :	
Air	1.00
Water	1.33
Ice	1.309
Glass	1.52
Diamond	2.42

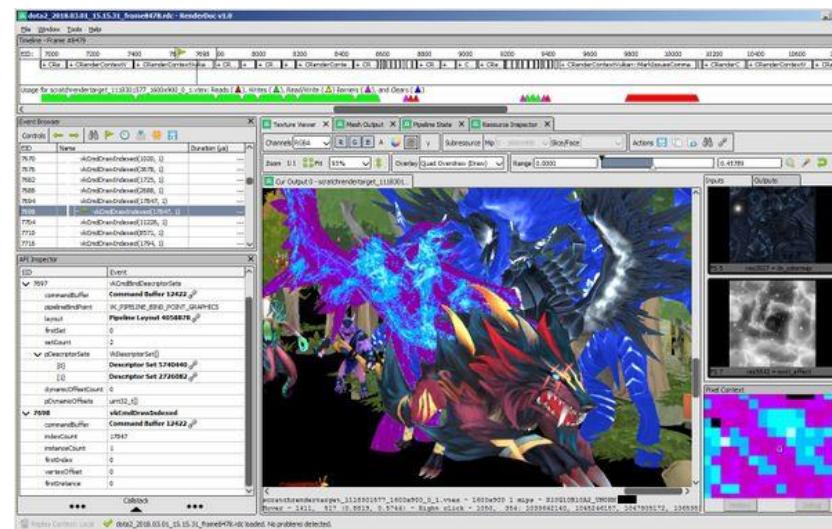
DEBUGGING

- To debug your codes: Output any **vector** you want to check as the **color**!
 - Transformations required between vector spaces, eg: $[-1,1]^3 \mapsto [0,1]^3$
 - If object is black -> the vector contains only zeros

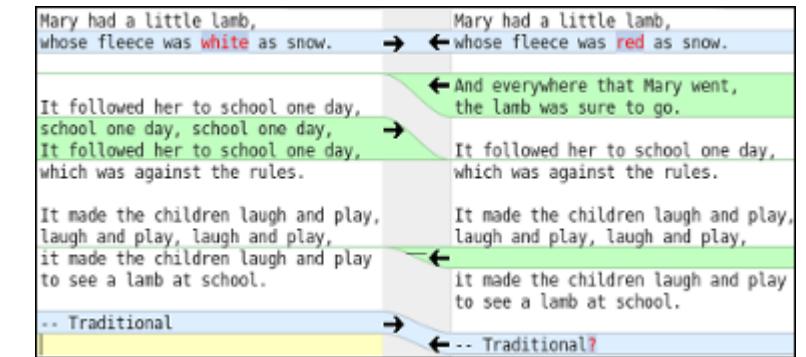


Normals as color

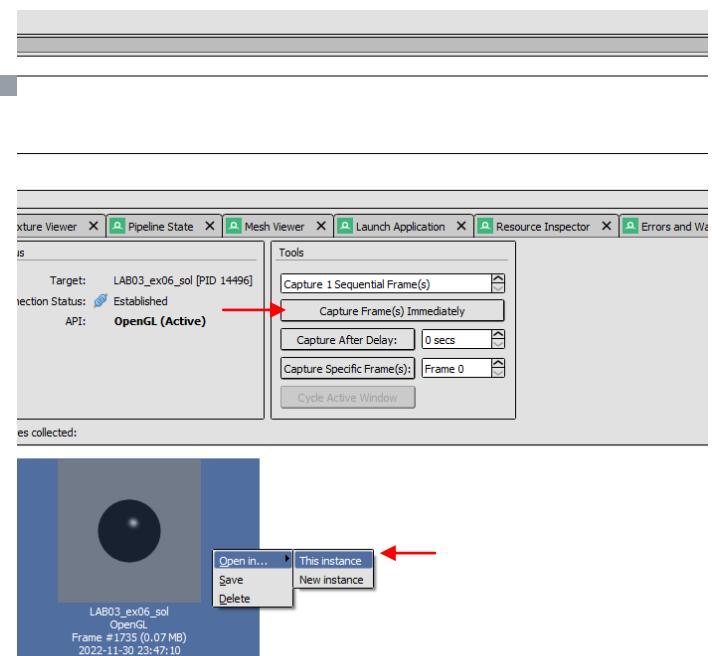
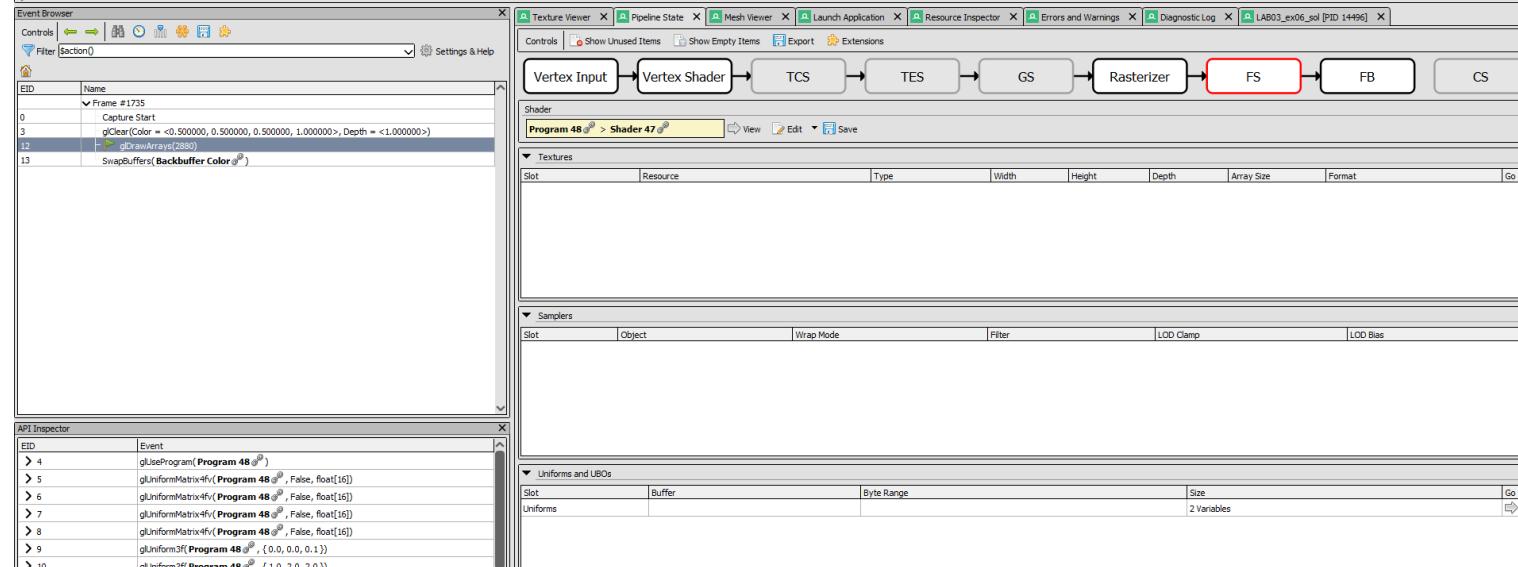
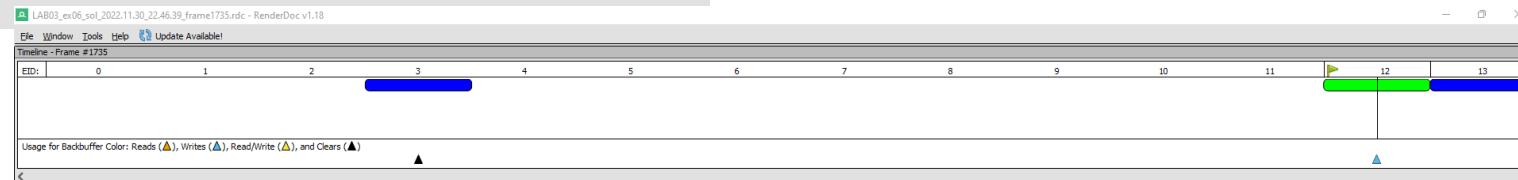
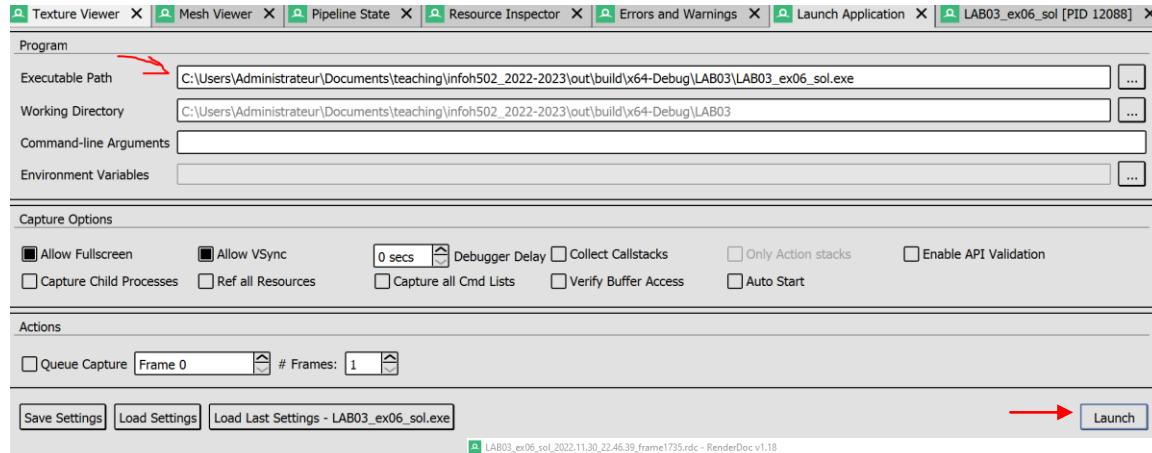
- Use MELD to compare the solutions/your code/exercise code/web code
 - <https://meldmerge.org/>



- (C++) Use RenderDoc !
 - Nice youtube tutorials



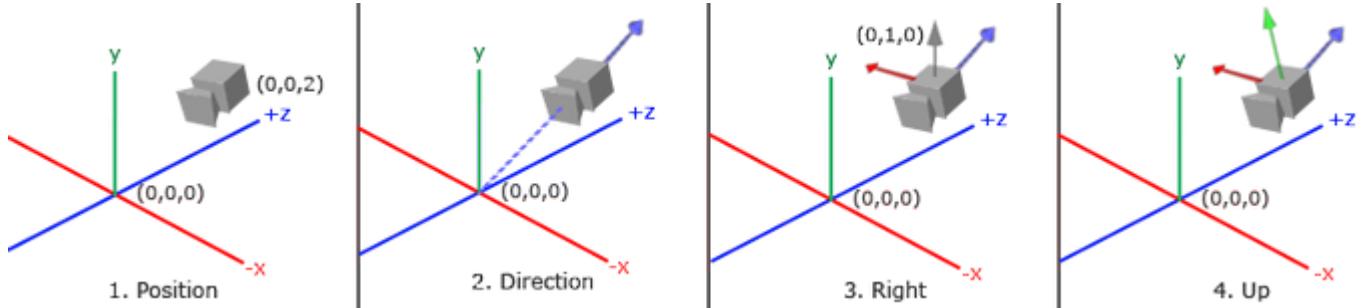
RENDERDOC (LINUX AND WINDOWS ONLY)



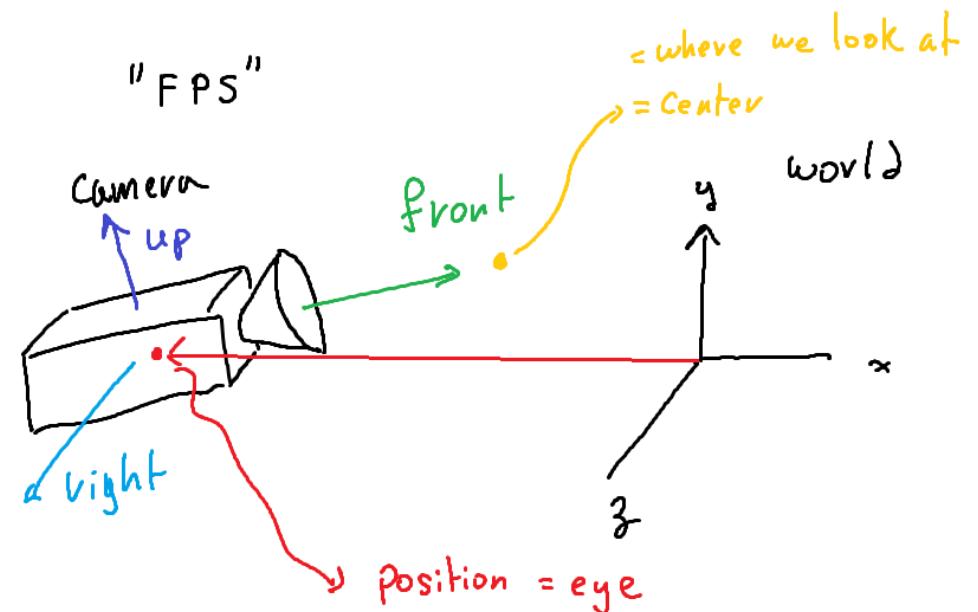
DOWNLOADING LAB 3 FROM GITLAB (WITHOUT CLONING)

- Download the LAB03 folder/ git pull the repository
- Put it at the same place that the LAB01 & LAB02 folders
- Change the CMakeList file directly:
 - In the top-most CMakeList.txt -> Put COMPILE_LAB03 to ON
 - Regenerate Cmake cache
- OR Change the configuration cache file :
 - Microsoft Visual Studio : right click on CMakeList.txt (on top) -> edit cmake setting -> COMPILE_LAB03 to ON
 - VSCode : Ctrl/Cmd + shift + p -> edit cmake cache (ui) -> COMPILE_LAB03 to ON

EXERCISE 01



- Read exercise 01 code to understand how the camera works
 - camera.js
 - What is the difference between the View/Projection matrices AND the provided camera ?



The provided code follows those conventions

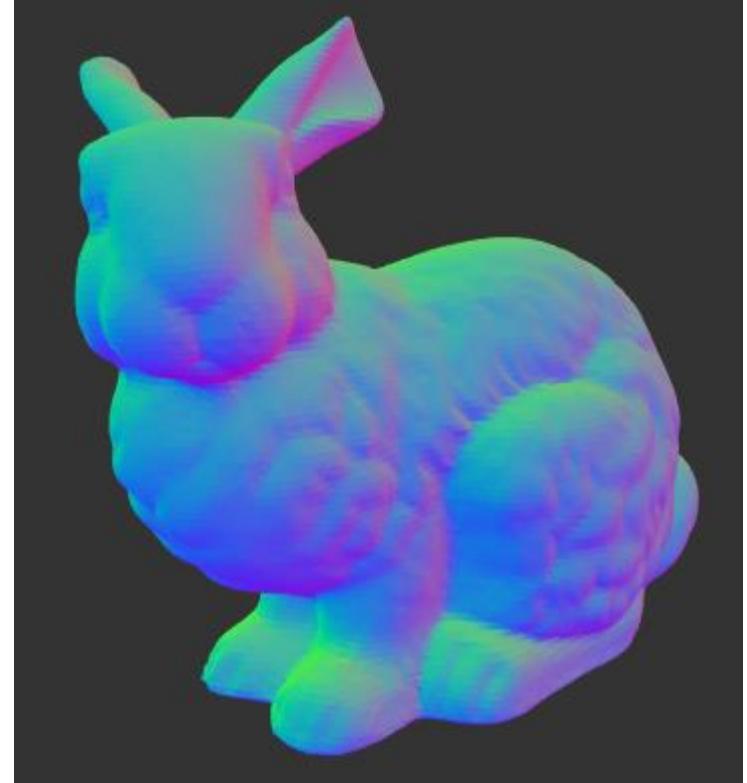
EXERCISE 02

- What does a Wavefront .obj file contain?
- Explain (at least to yourself)
 - v = ?
 - vt = ?
 - vn = ?
 - f = ?

```
# Blender v2.81 (sub 16) OBJ File: ''
# www.blender.org
o Cube
v 1.000000 1.000000 -1.000000
v 1.000000 -1.000000 -1.000000
v 1.000000 1.000000 1.000000
v 1.000000 -1.000000 1.000000
v -1.000000 1.000000 -1.000000
v -1.000000 -1.000000 -1.000000
v -1.000000 1.000000 1.000000
v -1.000000 -1.000000 1.000000
vt 0.625000 0.500000
vt 0.875000 0.500000
vt 0.875000 0.750000
vt 0.625000 0.750000
vt 0.375000 0.750000
vt 0.625000 1.000000
vt 0.375000 1.000000
vt 0.375000 0.000000
vt 0.625000 0.000000
vt 0.625000 0.250000
vt 0.375000 0.250000
vt 0.125000 0.500000
vt 0.375000 0.500000
vt 0.125000 0.750000
vn 0.0000 1.0000 0.0000
vn 0.0000 0.0000 1.0000
vn -1.0000 0.0000 0.0000
vn 0.0000 -1.0000 0.0000
vn 1.0000 0.0000 0.0000
vn 0.0000 0.0000 -1.0000
s off
f 1/1/1 5/2/1 7/3/1 3/4/1
f 4/5/2 3/4/2 7/6/2 8/7/2
f 8/8/3 7/9/3 5/10/3 6/11/3
f 6/12/4 2/13/4 4/5/4 8/14/4
f 2/13/5 1/1/5 3/4/5 4/5/5
f 6/11/6 5/10/6 1/1/6 2/13/6
```

EXERCISE 02

- Make an object reader and load an object you create in Blender
 - You will need to read the content of the file
 - Then stock the relevant information in a way you can use with OpenGL
 - Go to the annex to see how to export your blender project as a .obj file with the associated texture

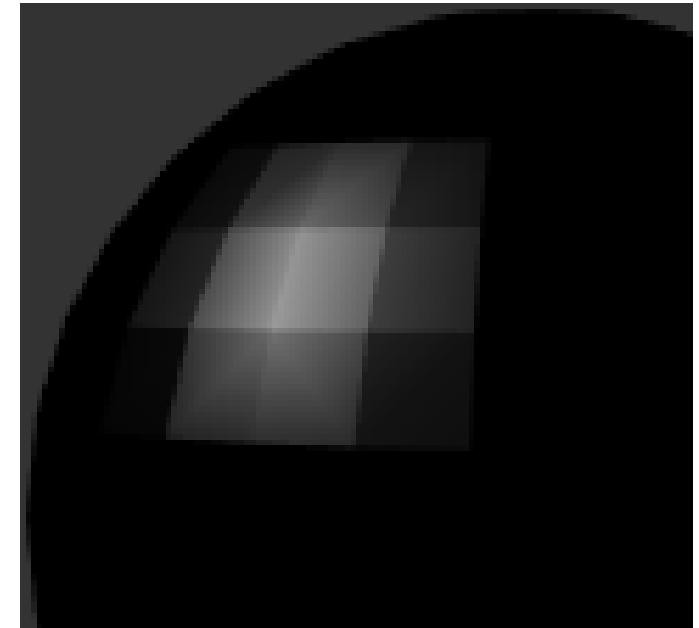


INTERLUDE – A NOTE ON OBJECT FILE

- A lot of format exist
 - .obj : fairly easy to read, only contains the vertices
 - .mtl : materials file used with .obj, describe light reflecting properties of materials → pretty old but still works well
 - Collada (.dae) : more comprehensive, contains vertices, material properties, and even shader ! Usefull for more advanced object/effect (animation ...)
 - gltf/gltb: A standard for 3D scenes and models, supported by many software (if you want to read it by hand :
<https://www.willusher.io/graphics/2023/05/16/0-to-gltf-first-mesh> or there is also header only library for it
<https://github.com/syoyo/tinygltf>)
- Complex model available online can use other format
- Existing library to load different file formats (assimp, ...), you can use them BUT :
 - You should understand the format you use i.e. what are the data in the file (vertices, texture coordinate, material properties ?) and how are they used in the opengl pipeline

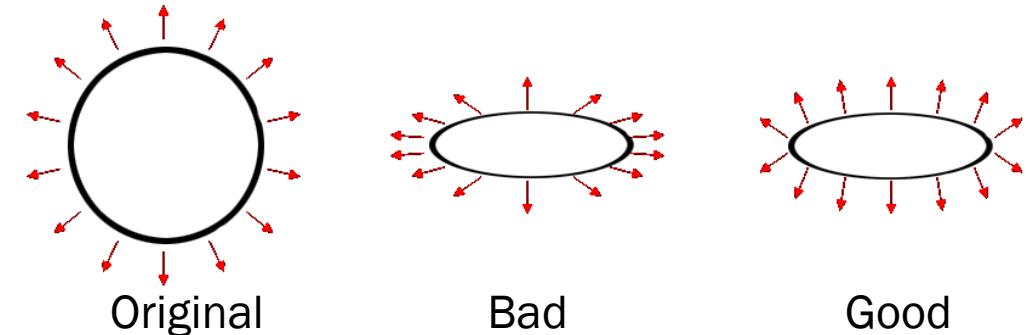
EXERCISE 03

- Implement Gouraud **diffuse** light on a sphere
 - You need to make the sphere and export it from Blender
 - Don't forget to put the light somewhere in your scene (it's a vec3 sent to the shader)
 - Don't forget that normals are NOT vectors but are unitary vectors:
 - They transform in space differently! (M, V, P)
 - See next slide ;)



NORMALS TRANSFORMATION BETWEEN THE MODEL AND WORLD COORDINATES

- A normal \mathbf{n} is a unitary vector
- Any transformation applied on it should preserve $\text{norm}(\mathbf{n}) == 1.0$
- We cannot do $\text{Model} * \mathbf{n}$ as this would result in non-normalized normal
- How does a normal transform?
 - Translation should NOT affect the normal
 - Rotation is applied to normal as with the position
 - Uniform scaling of position does NOT affect the direction of the normal
 - Non-uniform scaling affects the direction of the normal
- How to take all of this into consideration?
 - As usual, linear algebra to the rescue!

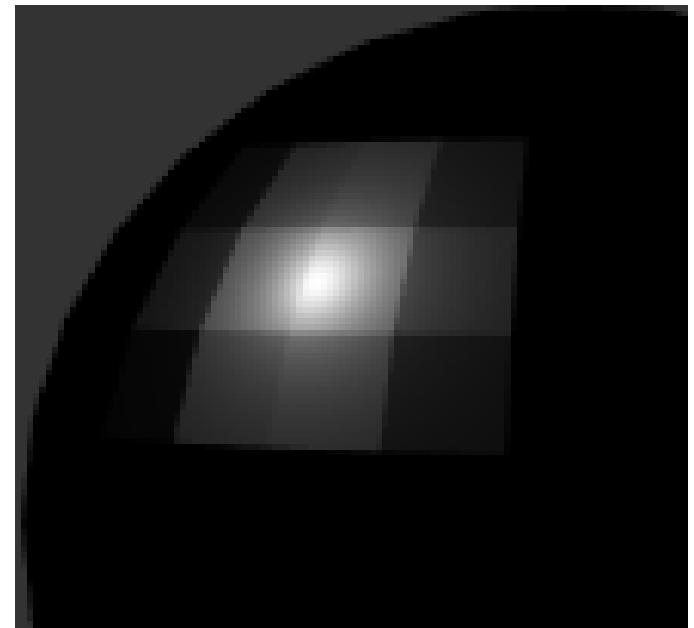


NORMALS TRANSFORMATION BETWEEN THE MODEL AND WORLD COORDINATES - PROOF

- Let $n \in \mathbb{R}^3$ be a normal at a point $p \in \mathbb{R}^3$ and $M \in \mathbb{R}^{3 \times 3}$ a transformation matrix
- We are looking how n transforms when we transform p .
- Let $W \in \mathbb{R}^{3 \times 3}$ be an unknown transform for n corresponding to $Mp \in \mathbb{R}^3$
 - We have $n \mapsto Wn$ and $p \mapsto Mp$
- Every point define a tangent plane and perpendicularity between p and n must be preserved (ie: $n^T p = 0$)
- By using the transformations we have $n^T p = 0 \Leftrightarrow (Wn)^T (Mp) = 0$
- By using the transpose, we want: $n^T W^T M p = 0$
- One solution is $W^T M = I \Leftrightarrow W^T = M^{-1} \Leftrightarrow W = M^{-T}$
- We found what we were looking for! The transformation of the normal vector using the model matrix!

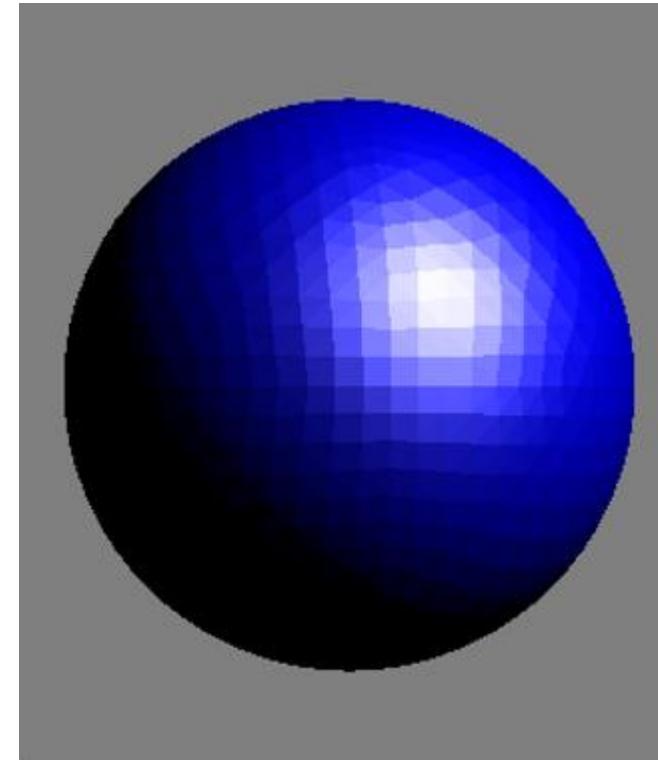
EXERCISE 04

- Implement Phong **diffuse** light on a sphere
- Compare with the previous exercise!
(the light must be placed carefully to see the difference)
- What is the difference between `sphere_coarse.obj` and `sphere_smooth.obj` ?
- Compare Gouraud and Phong: rough idea of how many computations are needed?



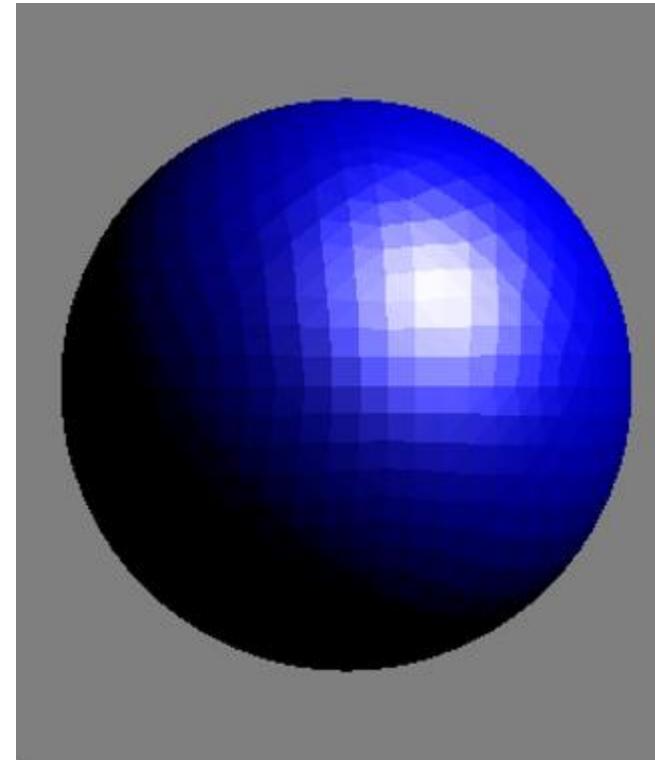
EXERCISE 05

- Implement Gouraud specular light
 - Which vectors do you need?
 - In which shader are those vectors computed?

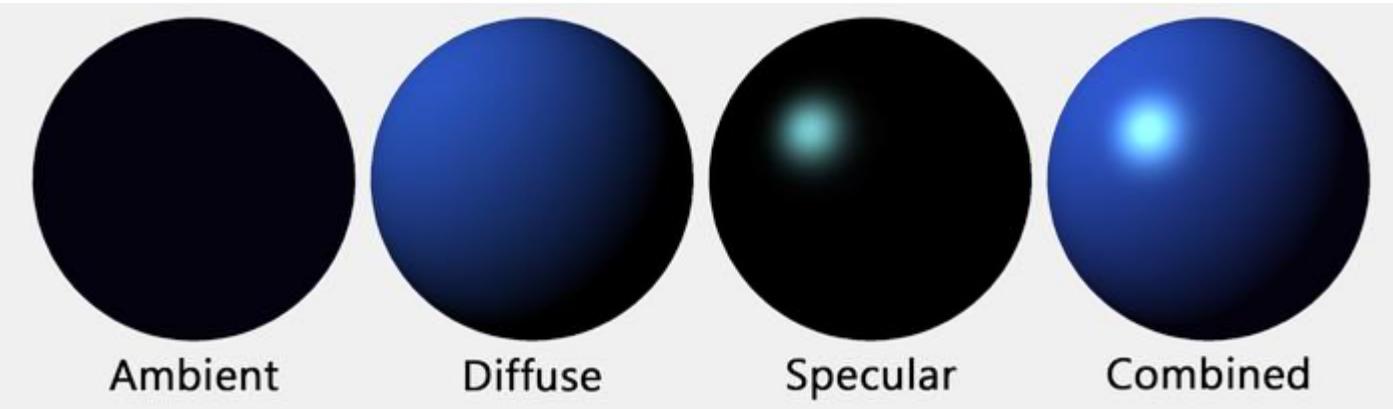


EXERCISE 06

- Implement Phong specular light
 - Which vectors do you need?
 - In which shader are those vectors computed?



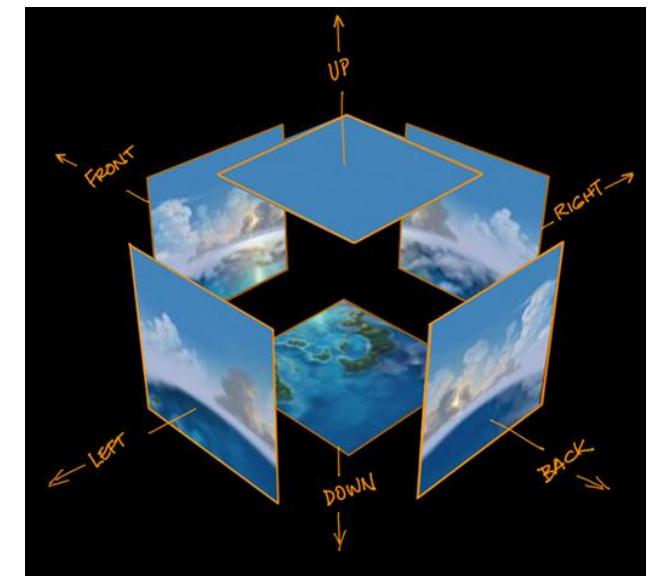
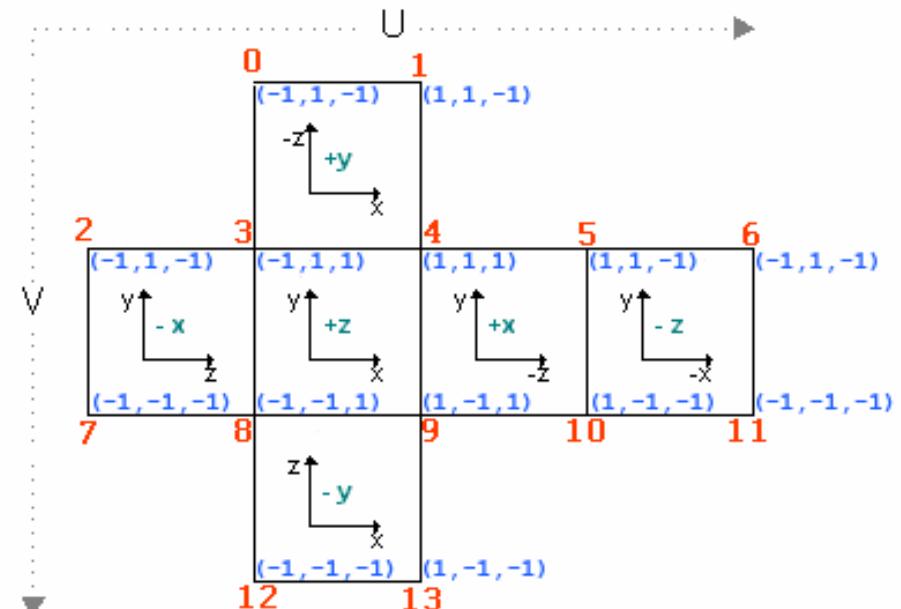
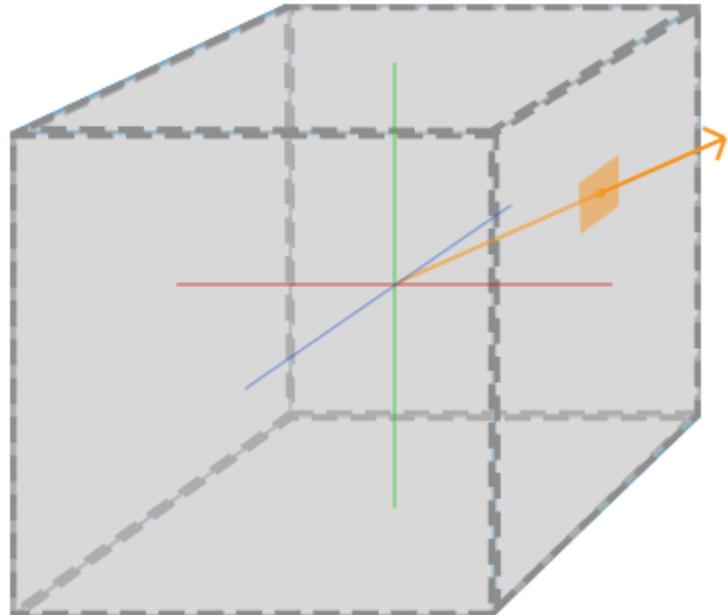
EXERCISE 07



- Implement the light equation on your object
 - Warning: In the solution only one light and a simplified light equation!
 - You can do way better!
- $L_o(\vec{x}) = A + E + \sum_N (diff + spec) \cdot L_i \cdot att_i \cdot \cos \theta$

EXERCISE 08

- Cubemap
 - Find cubemaps, eg: <http://www.humus.name/index.php?page=Textures>
 - 6 textures
 - Or use the one with the exercises LAB3/textures/cubemaps/yokohama3 (from the same website)
 - To sample the cube map use a samplerCube
- A good way to debug cubemaps is to make your own texture with a different color on each face!



EXERCISE 09

- Implement a reflective object



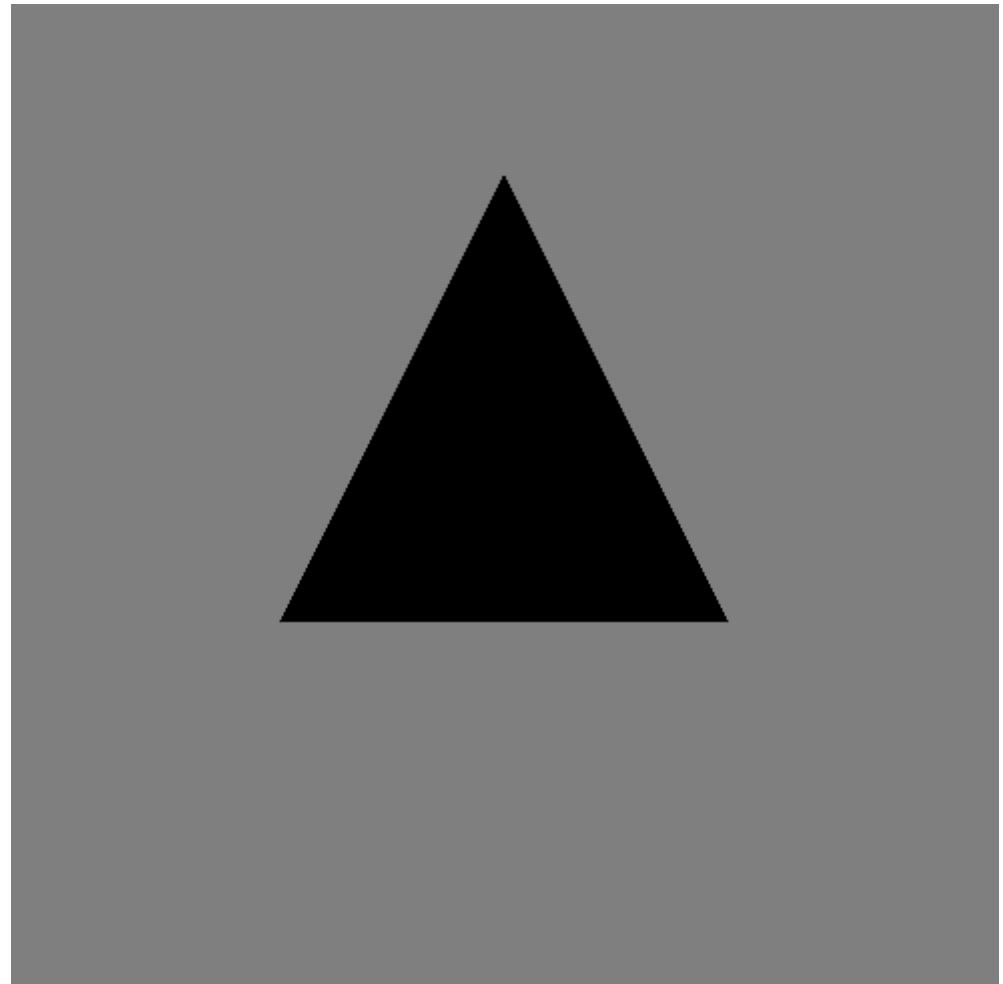
EXERCISE 10

- Implement a refractive object



EXERCISE 11

- Debug the code using Renderdoc (<https://renderdoc.org/>) to identify where is the bug. The goal is to make the texture appears on the triangle.
 - Hint: Appendix 0 may help you

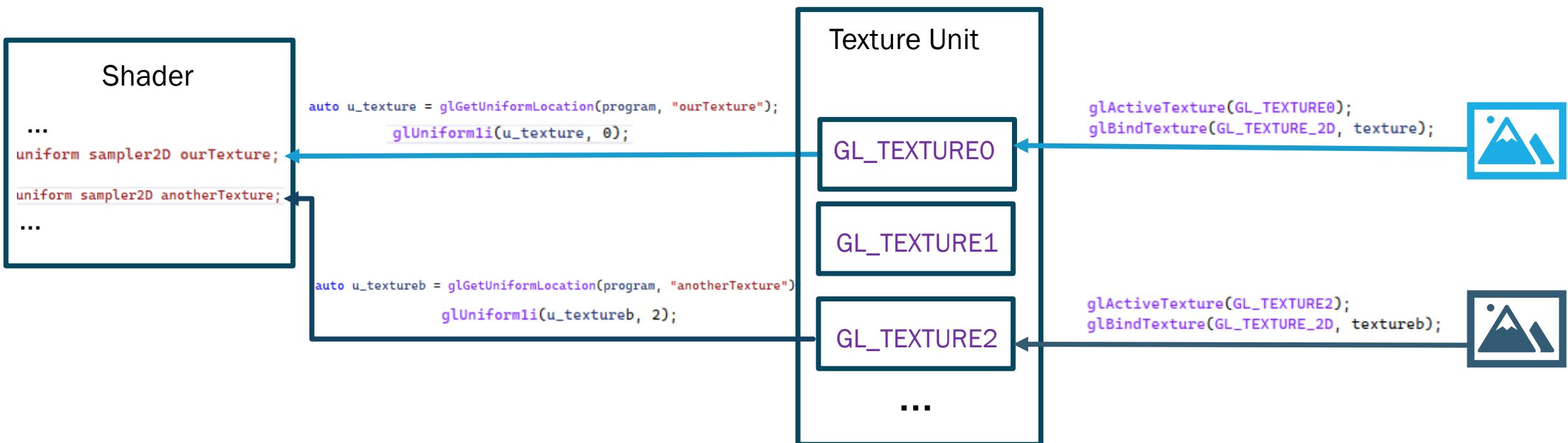


SUPPLEMENTARY EXERCISE FOR THE BRAVE: EQUIRECTANGULAR TO CUBEMAP

- You can find beautiful equirectangular cubemaps here: <https://hdrihaven.com/hdris/>
- But you need to write some code to convert them to a cubemap for OpenGL!
- Resources:
 - <http://paulbourke.net/panorama/cubemaps/>
 - <https://stackoverflow.com/questions/34250742/converting-a-cubemap-into-equirectangular-panorama>



APPENDIX 0: MULTIPLE TEXTURE, TEXTURE UNIT AND TEXTURE



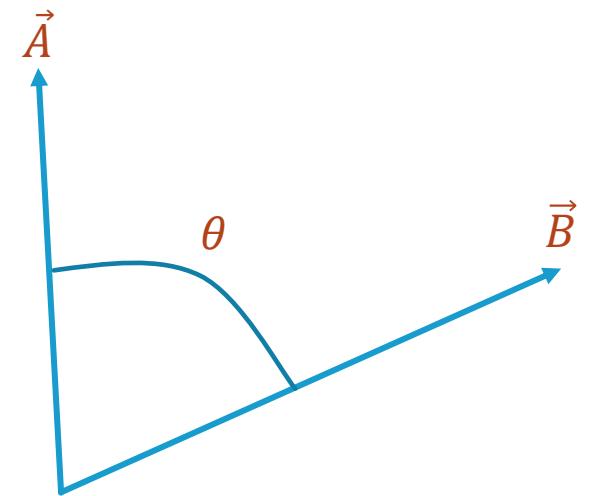
Additional resource:

<https://stackoverflow.com/a/55800428>

[https://www.khronos.org/opengl/wiki/Sampler_\(GLSL\)#Binding_textures_to_samplers](https://www.khronos.org/opengl/wiki/Sampler_(GLSL)#Binding_textures_to_samplers)

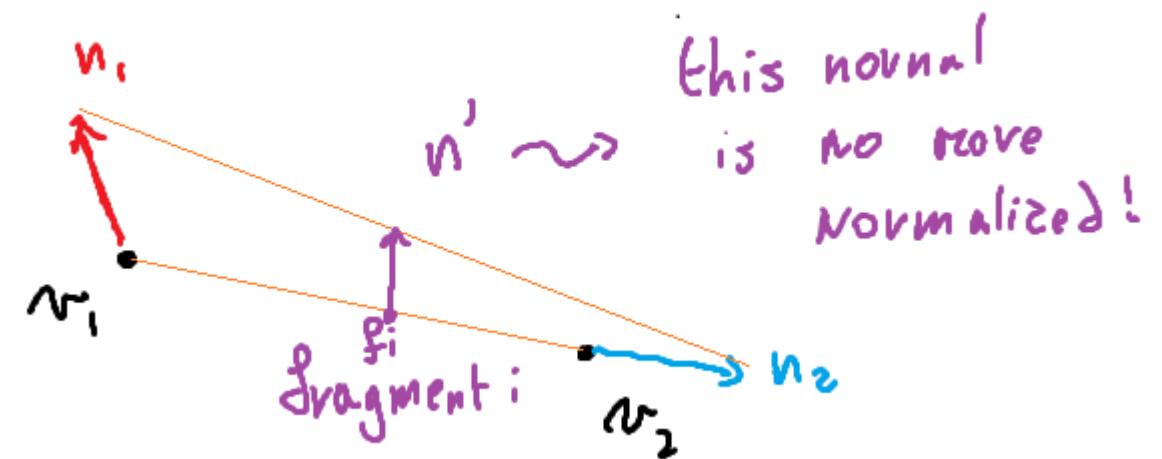
APPENDIX 1: COSINE BETWEEN NORMALIZED VECTORS

- $\text{norm}(\vec{A}) = 1$ and $\text{norm}(\vec{B}) = 1$
- $\text{dot}(\vec{A}, \vec{B}) = \text{norm}(\vec{A}) \cdot \text{norm}(\vec{B}) \cdot \cos \theta = 1 \cdot 1 \cdot \cos \theta = \cos \theta$
- $\Rightarrow \cos \theta = \text{dot}(\vec{A}, \vec{B})$



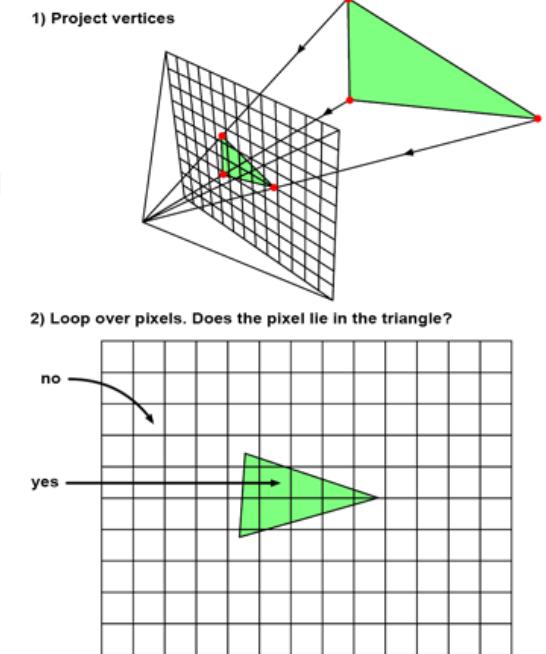
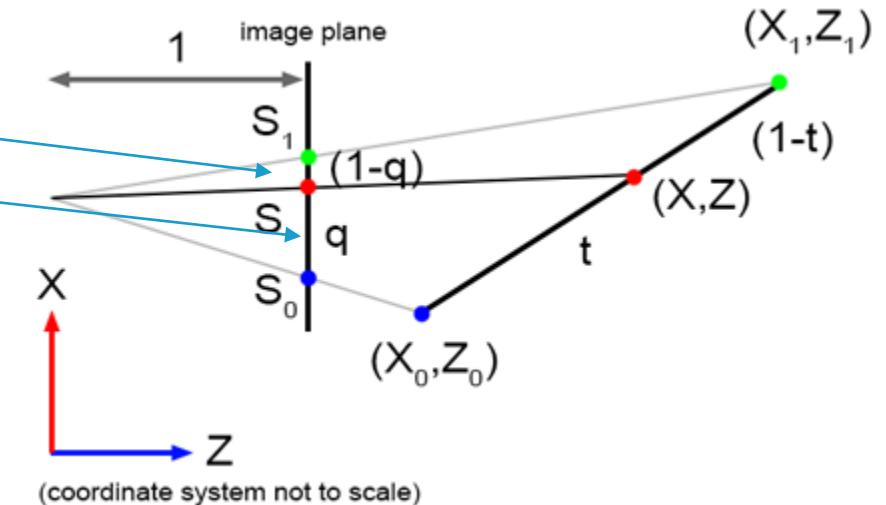
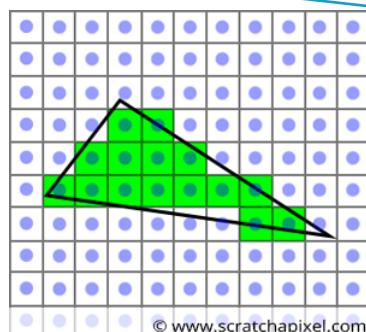
APPENDIX 2: PHONG AND THE NON NORMALIZED NORMALS

- When you interpolate a normal between the vertex and the fragment shader
 - The “normality” condition is not necessarily fulfilled
 - You need to re-normalize your normal when you receive them in the fragment shader!
 - $n = \text{normalize}(n)$



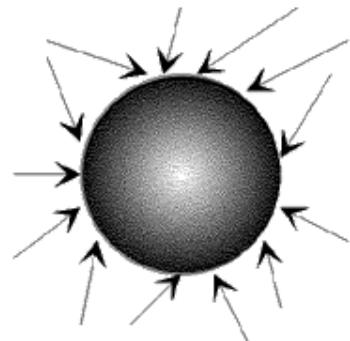
APPENDIX 3: HOW MANY FRAGMENTS - RASTERIZATION

- The screen is a discretized grid, you need to map 3D objects to it
- The projection of 3D elements change using the depth of the points!
 - Less fragments for far away points
 - More fragments for closer points

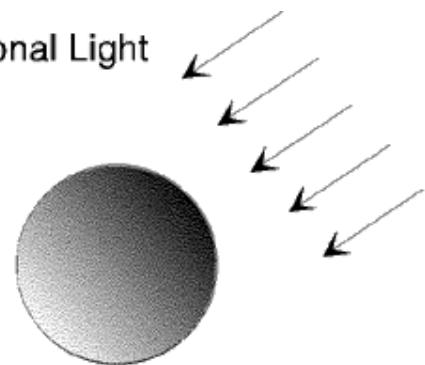


APPENDIX 4 : KIND OF LIGHT SOURCES

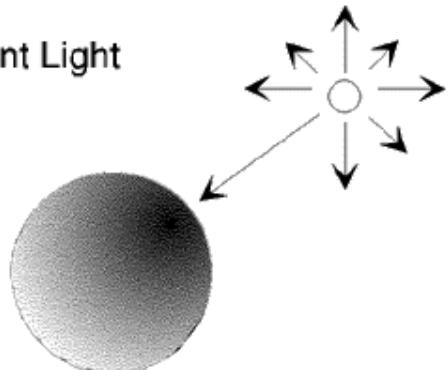
Ambient Light



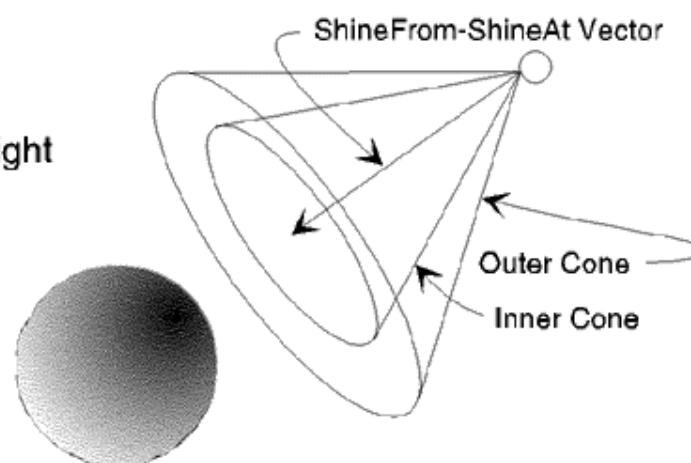
Directional Light



Point Light



Spot Light



3D Lighting: History, Concepts, and Techniques
Arnold Gallardo
2000

Digital Lighting and Rendering
Jeremy Birn
2013

APPENDIX 5 : RENDERING EQUATION NOT ENOUGH

Although the equation is very general, it does not capture every aspect of light reflection. Some missing aspects include the following:

- **Transmission**, which occurs when light is transmitted through the surface, such as when it hits a **glass** object or a **water** surface,
- **Subsurface scattering**, where the spatial locations for incoming and departing light are different. Surfaces rendered without accounting for subsurface scattering may appear unnaturally opaque — however, it is not necessary to account for this if transmission is included in the equation, since that will effectively include also light scattered under the surface,
- **Polarization**, where different light polarizations will sometimes have different reflection distributions, for example when light bounces at a water surface,
- **Phosphorescence**, which occurs when light or other **electromagnetic radiation** is **absorbed** at one moment in time and emitted at a later moment in time, usually with a longer **wavelength** (unless the absorbed electromagnetic radiation is very intense),
- **Interference**, where the wave properties of light are exhibited,
- **Fluorescence**, where the absorbed and emitted light have different **wavelengths**,
- **Non-linear** effects, where very intense light can increase the **energy level** of an **electron** with more energy than that of a single **photon** (this can occur if the electron is hit by two photons at the same time), and **emission** of light with higher frequency than the frequency of the light that hit the surface suddenly becomes possible, and
- **Relativistic Doppler effect**, where light that bounces on an object that is moving in a very high speed will get its wavelength changed; if the light bounces at an object that is moving towards it, the impact will compress the **photons**, so the wavelength will become shorter and the light will be **blueshifted** and the photons will be packed more closely so the photon flux will be increased; if it bounces at an object that is moving away from it, it will be **redshifted** and the photons will be packed more sparsely so the photon flux will be decreased.

For scenes that are either not composed of simple surfaces in a vacuum or for which the travel time for light is an important factor, researchers have generalized the rendering equation to produce a **volume rendering equation**^[5] suitable for **volume rendering** and a **transient rendering equation**^[6] for use with data from a **time-of-flight camera**.

APPENDIX 6 : LIGHT EQUATION – OTHER MODELS

- The Blinn-Phong model we saw is just **one** visually pleasing **model!**
- There is always a tradeoff between visual accuracy and difficulty to compute

- Lambertian:

$$f(\omega_i, x, \omega_o) = \frac{a}{\pi}$$

- Lafourture:

$$f(\omega_i, x, \omega_o) = \frac{a}{\pi} + b(-\omega_i^T A \omega_o)^k$$

- Blinn:

$$f(\omega_i, x, \omega_o) = \frac{a}{\pi} + b \cos^c b \langle \omega_i | \omega_o \rangle$$

- Phong:

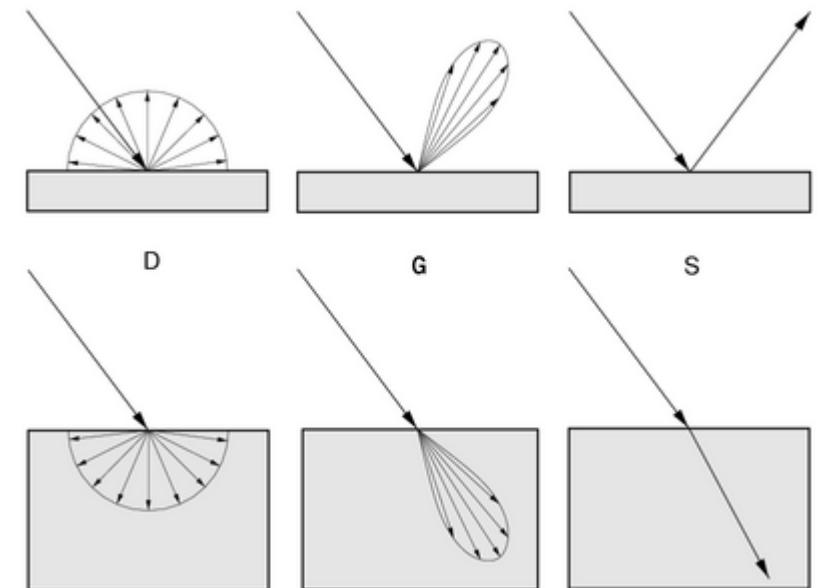
$$f(\omega_i, x, \omega_o) = \frac{a}{\pi} + b \cos^c (2 \langle \omega_i | n \rangle \langle \omega_o | n \rangle - \langle \omega_i | \omega_o \rangle)$$

- Ward:

$$f(\omega_i, x, \omega_o) = \frac{a}{\pi} + \frac{b}{4\pi c^2 \sqrt{\langle \omega_i | n \rangle \langle \omega_o | n \rangle}} \exp\left(-\frac{\tan^2 b \langle \omega_i | \omega_o \rangle}{c^2}\right)$$

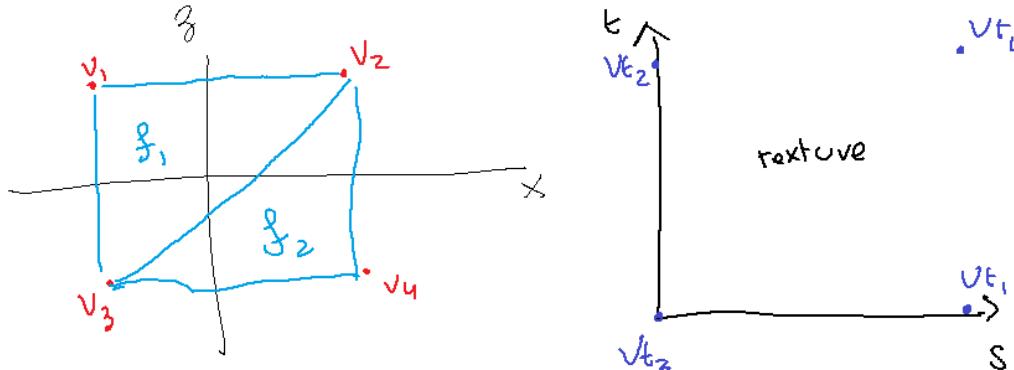
APPENDIX 7 : BRDF NOT ALONE

- BRDF is for Reflectance
- BTDF is for Transmittance (light inside the material!)
- BSDF is both of them

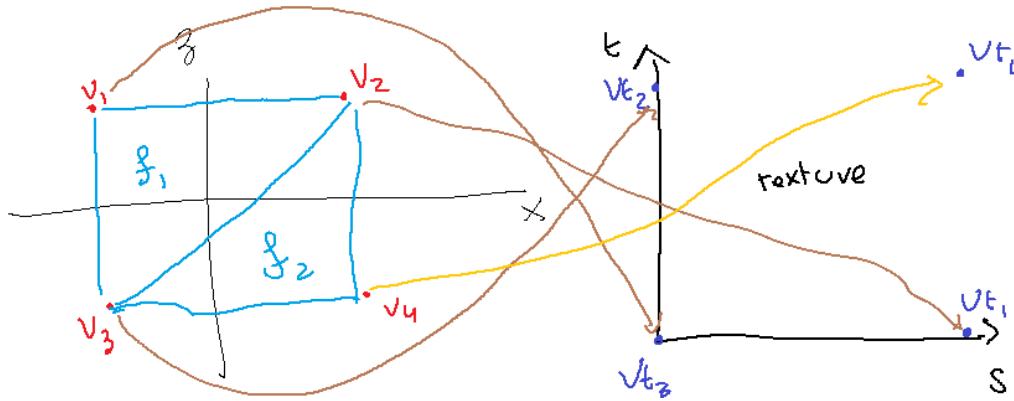


APPENDIX 8 : MATERIAL FILE - SOLUTION

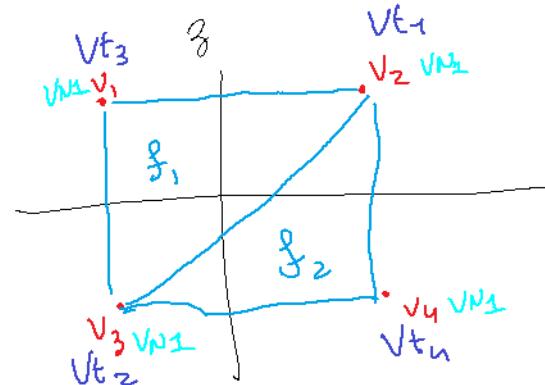
```
plane.obj (D:\VR2020\LAB03\objects) - GVIM1
Fichier Edition Outils Syntaxe Tampons F
# Blender v2.81 (sub 16) OBJ File:
# www.blender.org
v -1.000000 0.000000 1.000000 1
v 1.000000 0.000000 1.000000 2
v -1.000000 0.000000 -1.000000 3
v 1.000000 0.000000 -1.000000 4
vt 1.000000 0.000000 1
vt 0.000000 1.000000 2
vt 0.000000 0.000000 3
vt 1.000000 1.000000 4
vn 0.0000 1.0000 0.0000 1
s off
F 2/1/1 3/2/1 1/3/1
F 2/1/1 3/4/1 3/2/1
```



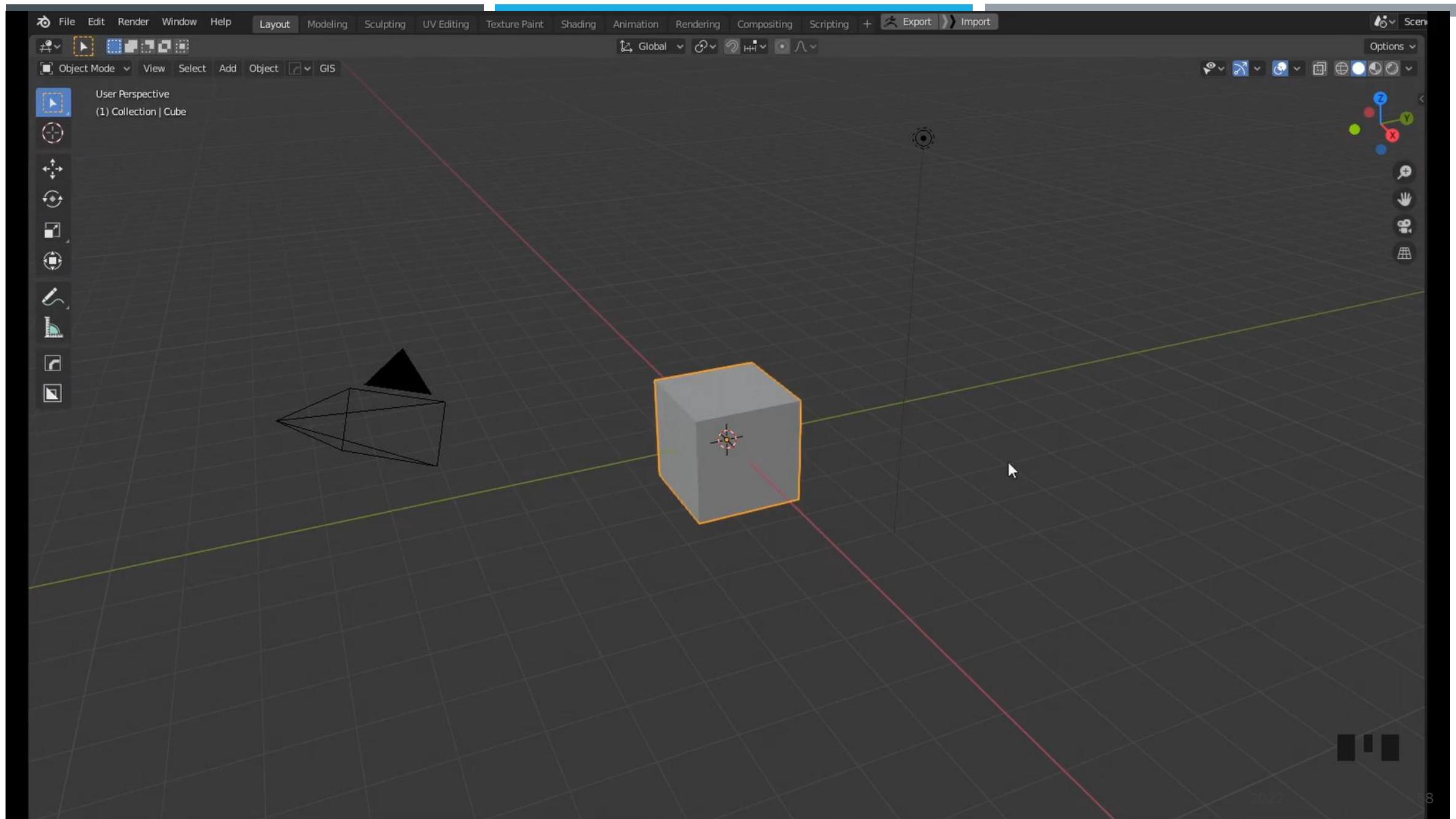
```
plane.obj (D:\VR2020\LAB03\objects) - GVIM1
Fichier Edition Outils Syntaxe Tampons F
# Blender v2.81 (sub 16) OBJ File:
# www.blender.org
v -1.000000 0.000000 1.000000 1
v 1.000000 0.000000 1.000000 2
v -1.000000 0.000000 -1.000000 3
v 1.000000 0.000000 -1.000000 4
vt 1.000000 0.000000 1
vt 0.000000 1.000000 2
vt 0.000000 0.000000 3
vt 1.000000 1.000000 4
vn 0.0000 1.0000 0.0000 1
s off
F 2/1/1 3/2/1 1/3/1
F 2/1/1 3/4/1 3/2/1
```



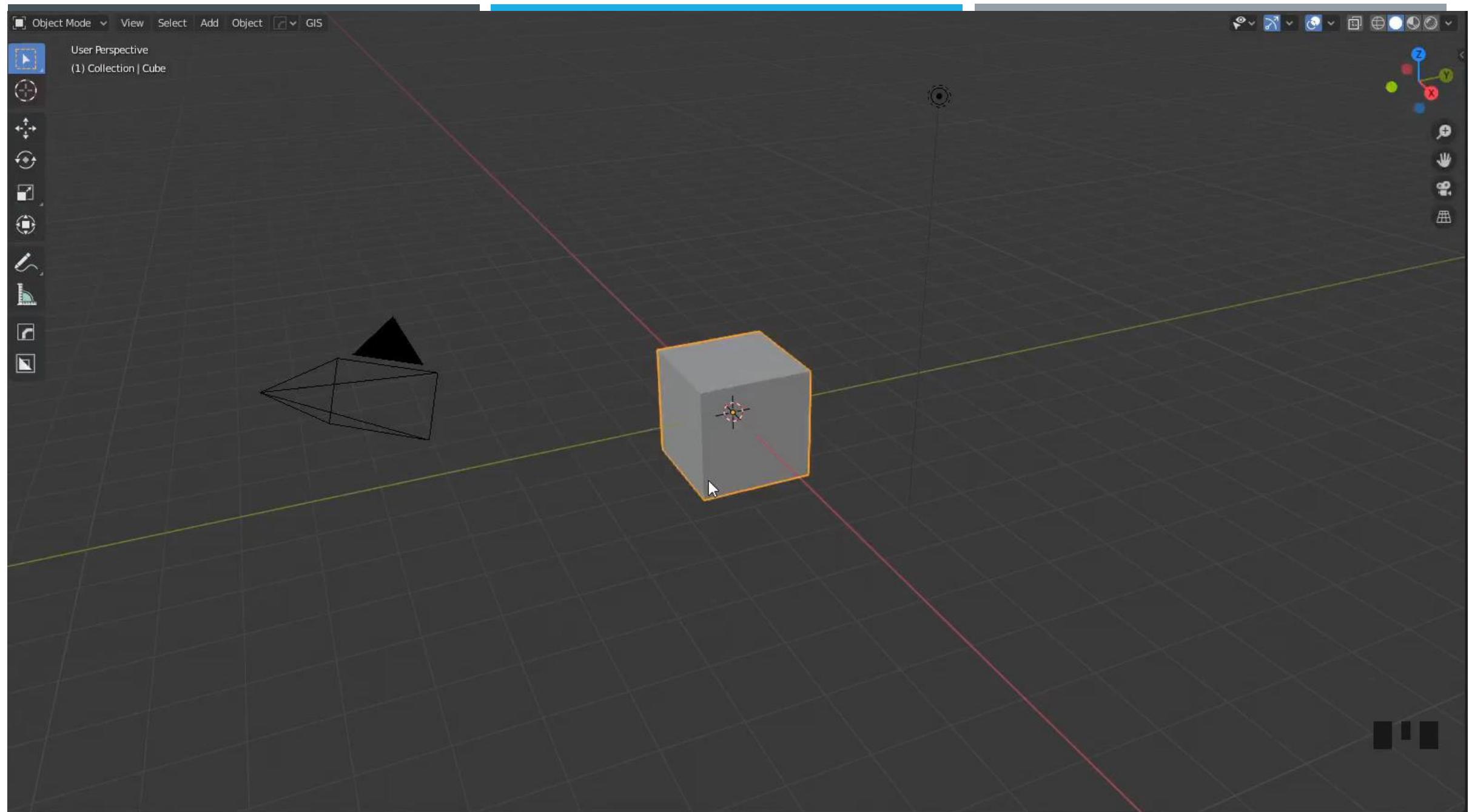
```
plane.obj (D:\VR2020\LAB03\objects) - GVIM1
Fichier Edition Outils Syntaxe Tampons F
# Blender v2.81 (sub 16) OBJ File:
# www.blender.org
v -1.000000 0.000000 1.000000 1
v 1.000000 0.000000 1.000000 2
v -1.000000 0.000000 -1.000000 3
v 1.000000 0.000000 -1.000000 4
vt 1.000000 0.000000 1
vt 0.000000 1.000000 2
vt 0.000000 0.000000 3
vt 1.000000 1.000000 4
vn 0.0000 1.0000 0.0000 1
s off
F 2/1/1 3/2/1 1/3/1
F 2/1/1 3/4/1 3/2/1
```



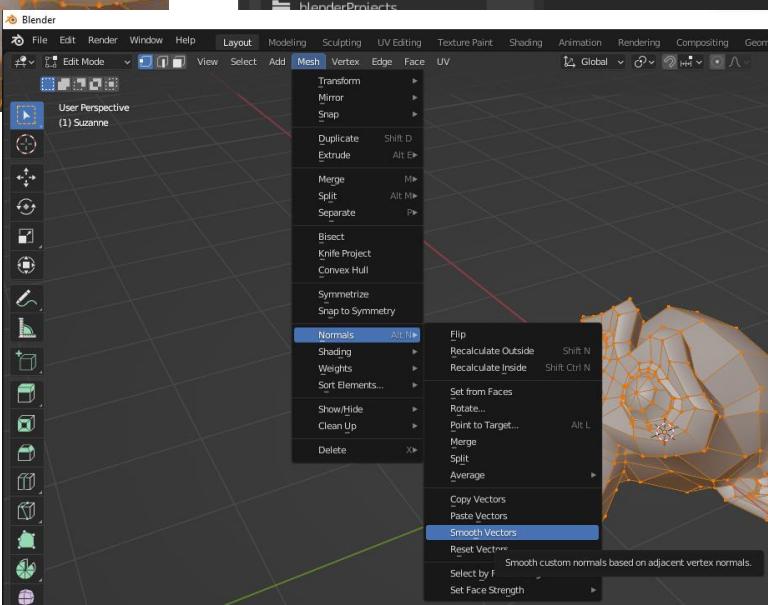
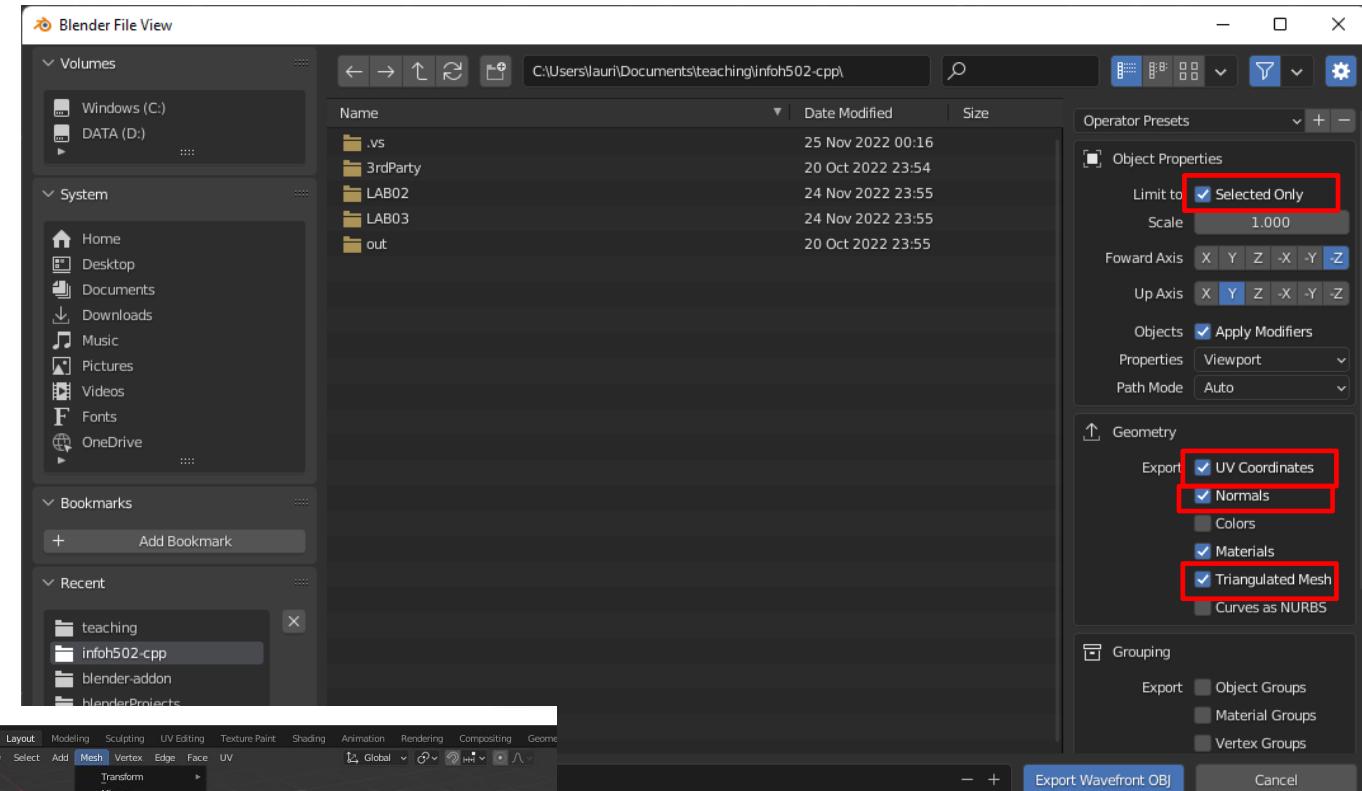
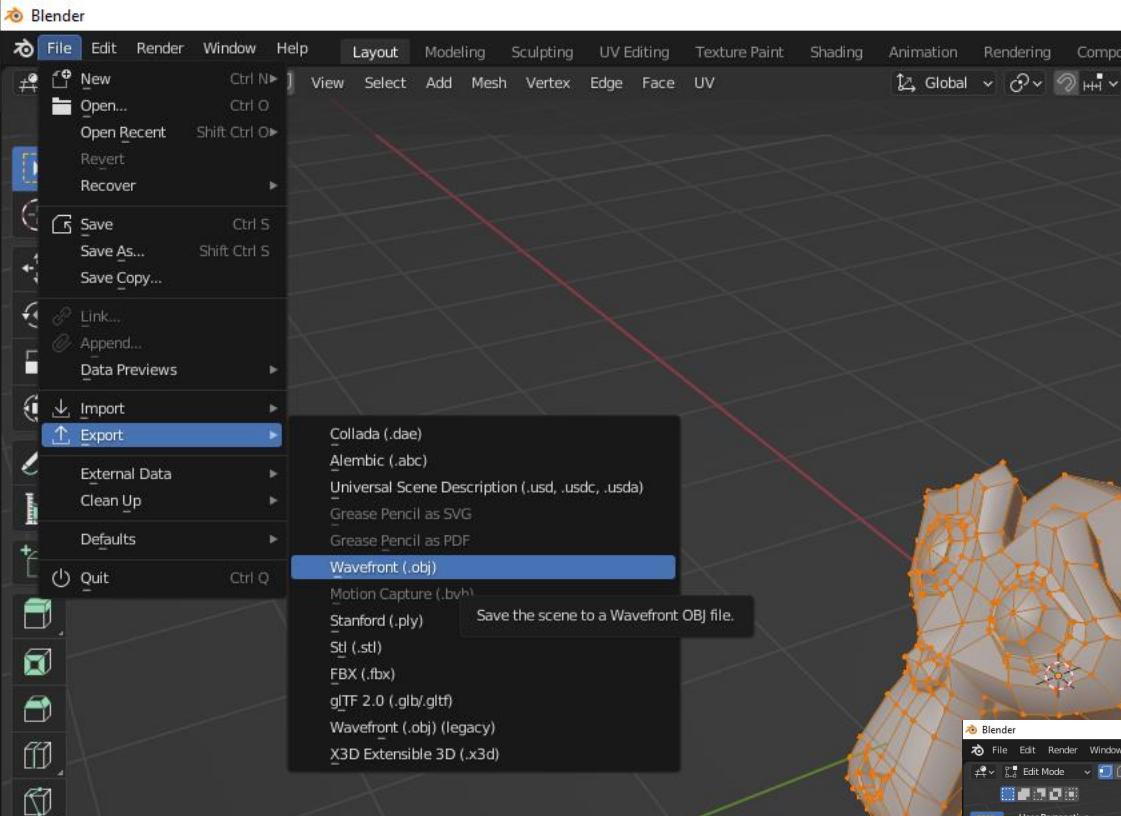
APPENDIX 9: CREATE AN OBJECT WITH BLENDER AND EXPORT IT



APPENDIX 9: SPHERE COARSE VS SMOOTH



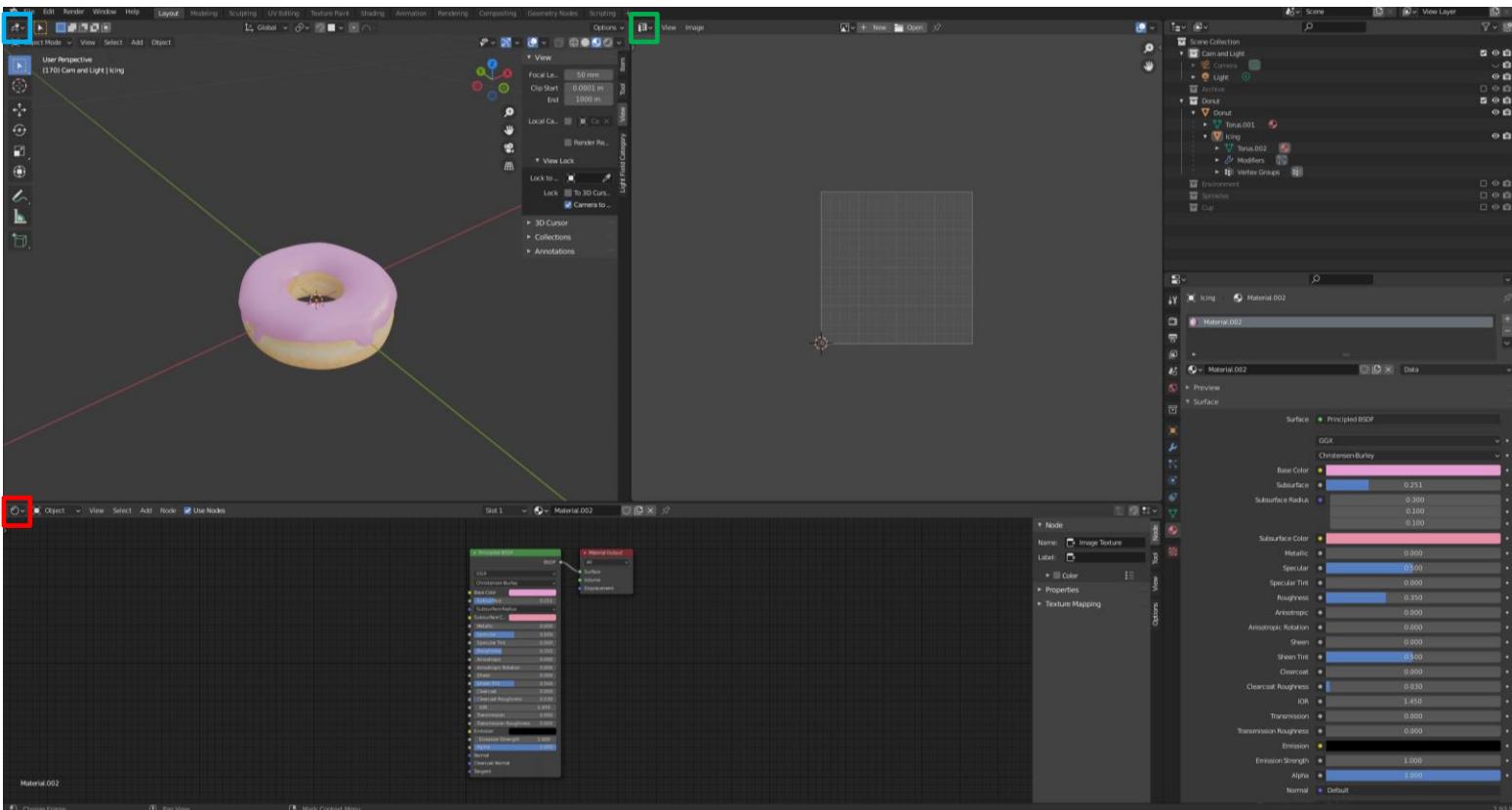
APPENDIX 9: USE BLENDER TO CREATE .OBJ FILES



(optional) if you want vertices to have different normal in a same face

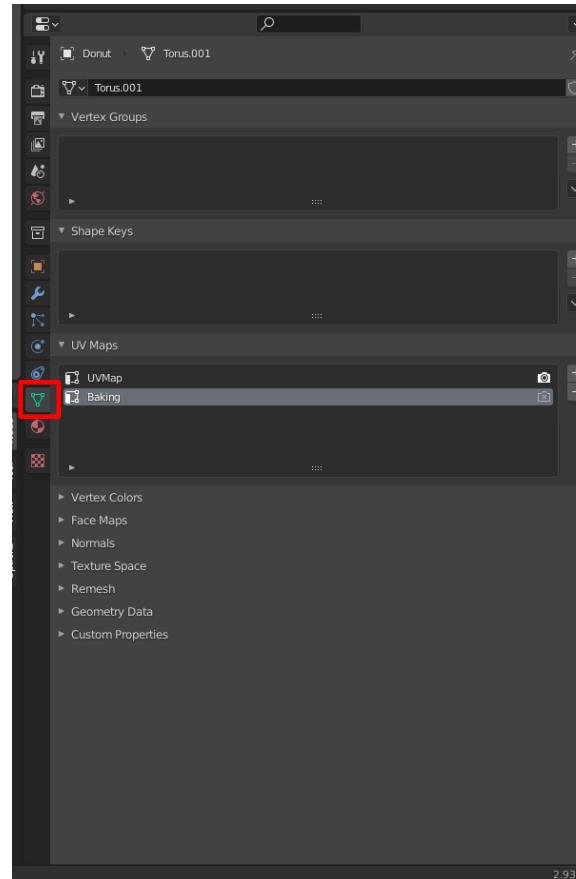
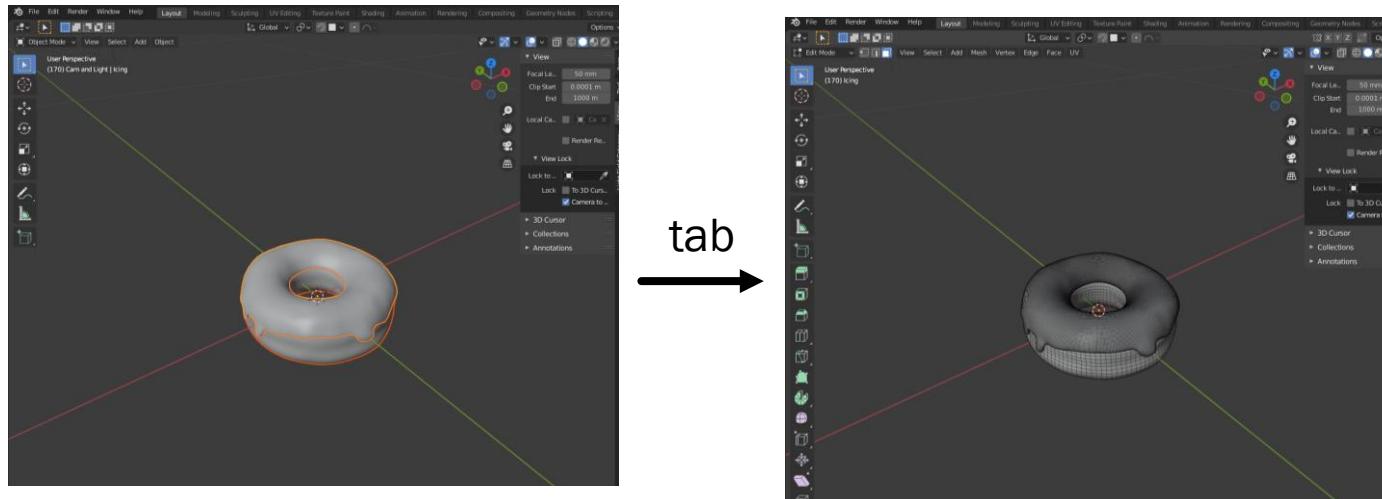
APPENDIX 10 : BAKING TEXTURE (BLENDER 2.9)

- Split your workspace into 3 panels
- **Upper-left** panel shows the 3D viewport, **upper-right** panel shows the uv Editor, **bottom** panel shows the shader editor



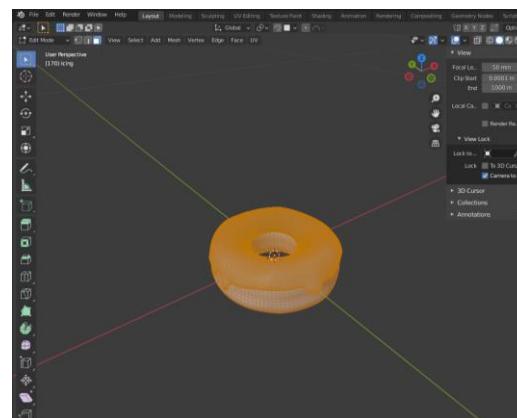
APPENDIX 10 : BAKING TEXTURE

- For each part of your object, go to the **Object Data Properties tab** and create a new uv map called Baking
- Then select all your object and go into edit mode (tab key)

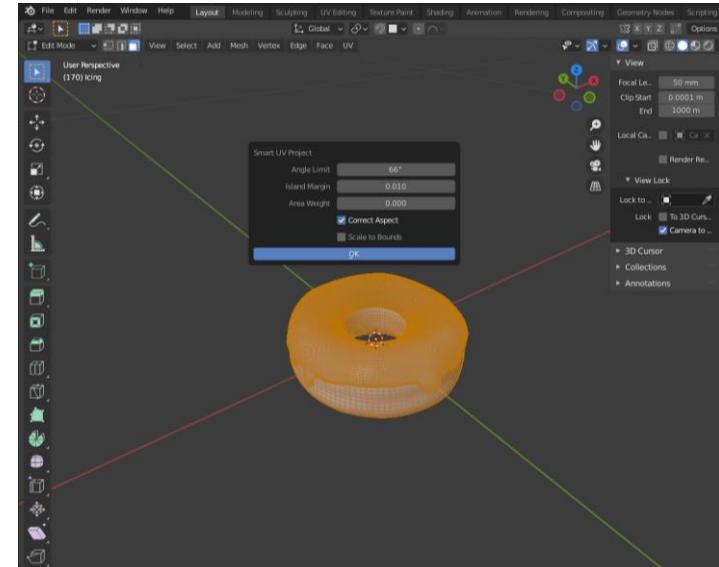
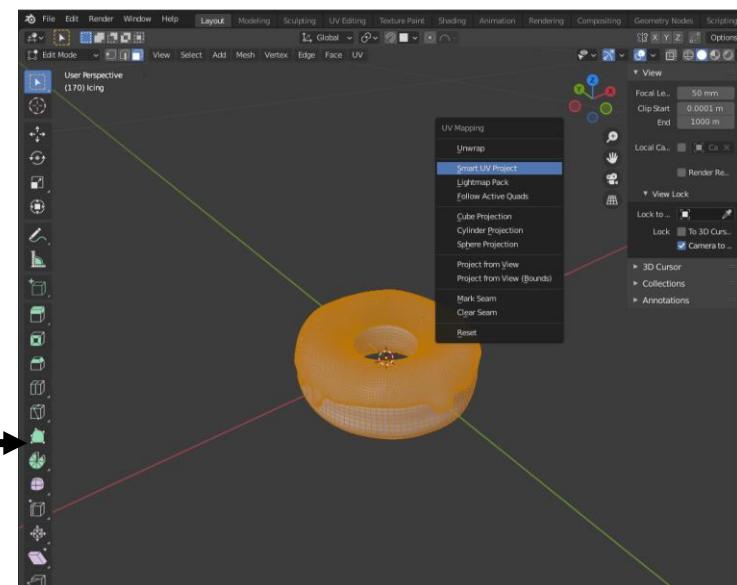


APPENDIX 10: BAKING TEXTURE

- Select all vertices with key « a » then use key « u » to show the unwrapping menu
- Select the smart uv project option
- Change the Island Margin to 0.01 and click OK

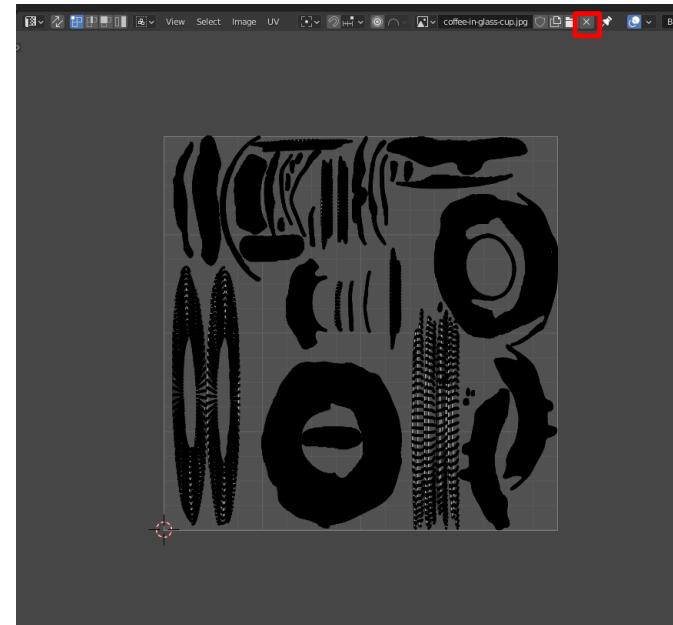
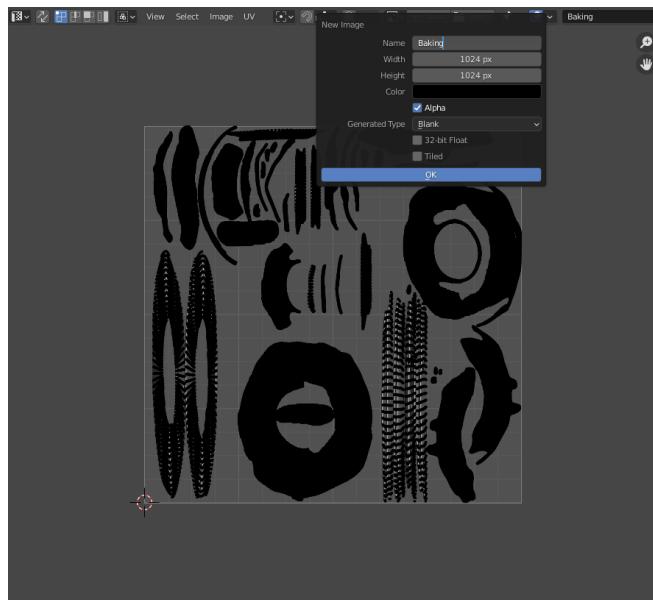


U



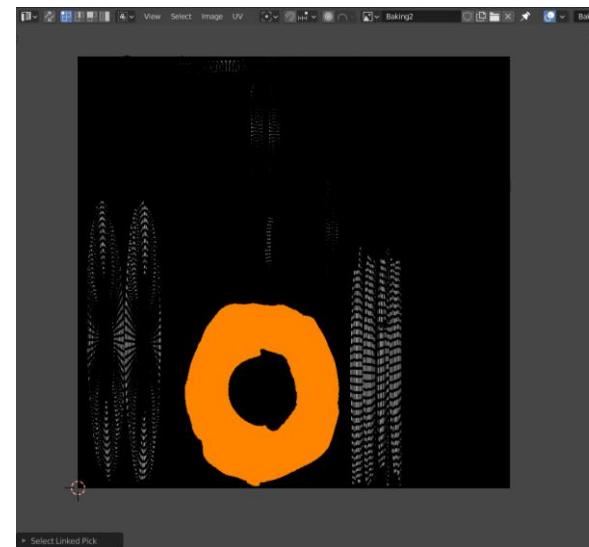
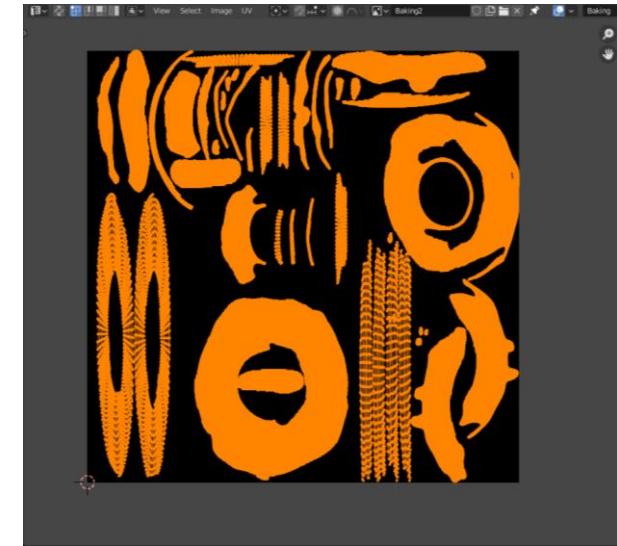
APPENDIX 10: BAKING TEXTURE

- In the uv editor panel you will sell your object « flattened »
- Remove the current texture
- Create a new image with the name baking and the dimension you want



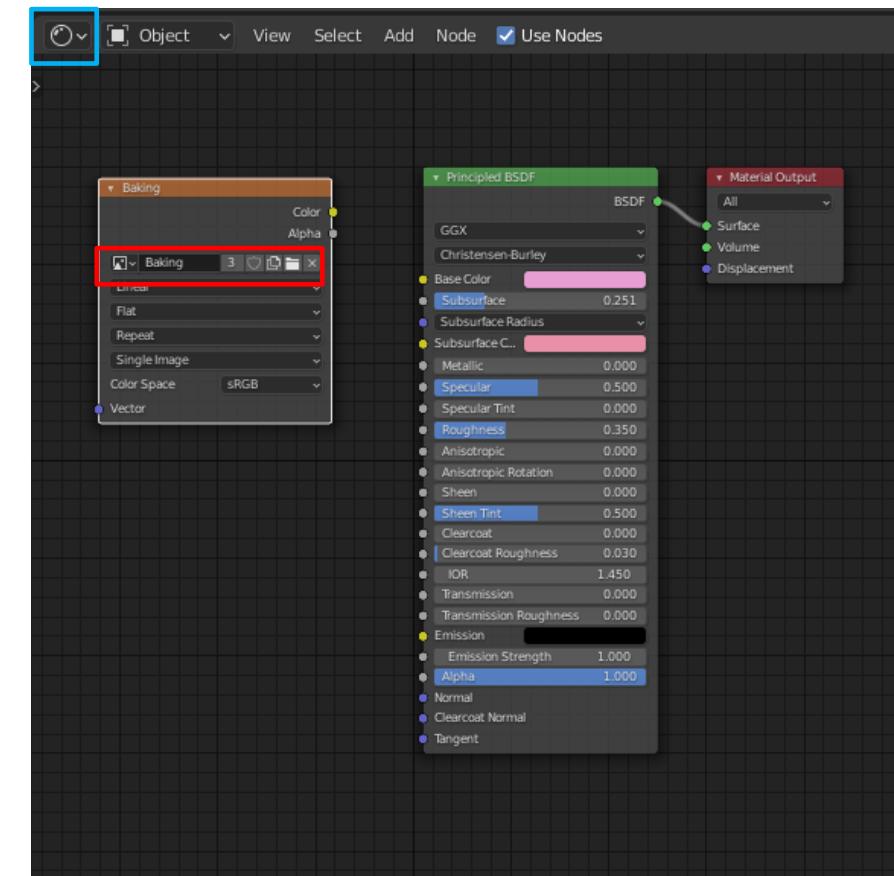
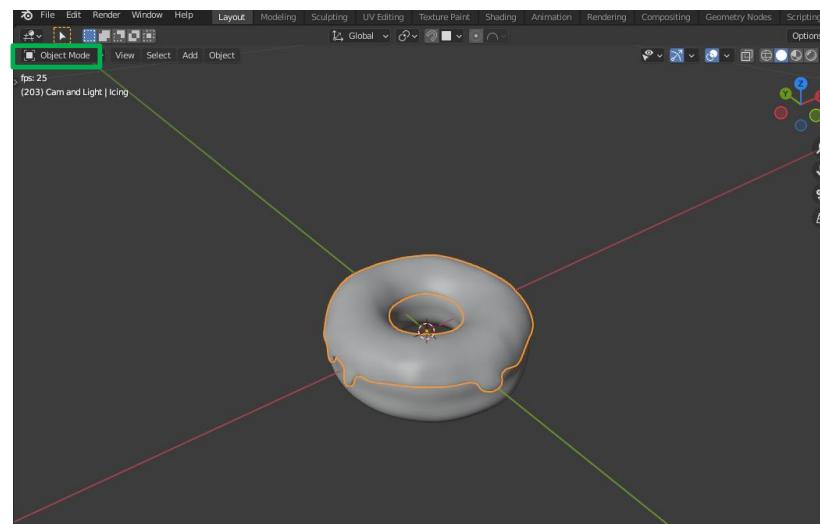
APPENDIX 10: BAKING TEXTURE

- Press « a » to select all points
- Press « l » to select a block of linked vertices
- Move the blocks around (key « g », « r », « s ») to optimize the space, you want to take as much space as possible in the image without having overlapping block



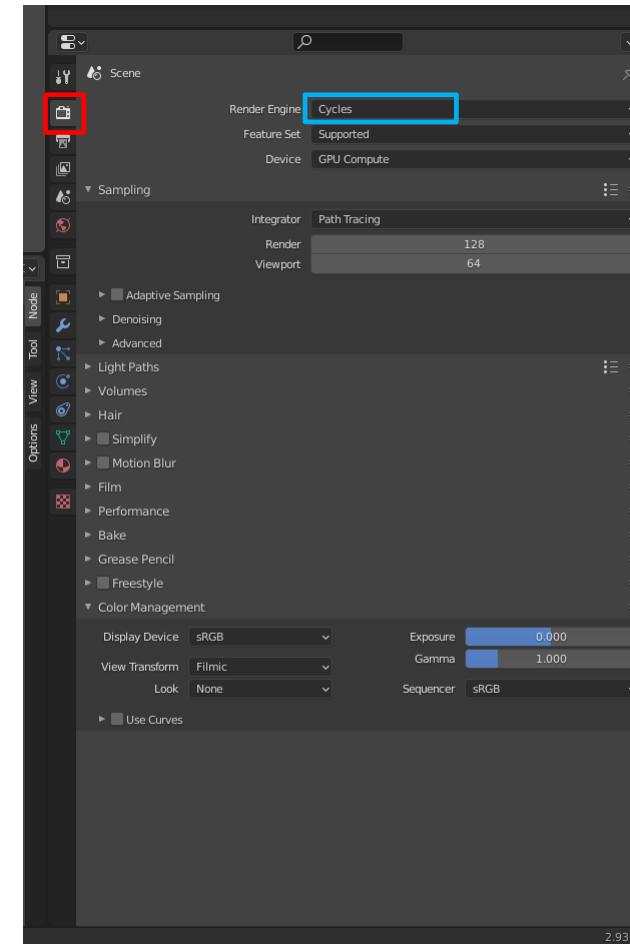
APPENDIX 10: BAKING TEXTURE

- Go back to **object mode** (tab)
- For each material, add a **texture image** node in the **shader editor**
- Use the **baking texture** you have just created
- ! This node must be unconnected to the reste of the nodes presents



APPENDIX 10: BAKING TEXTURE

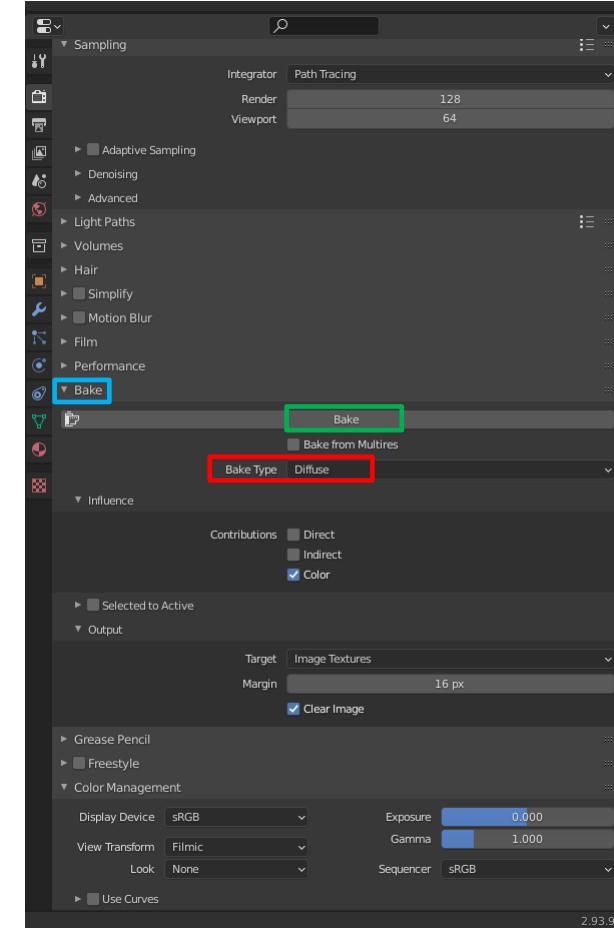
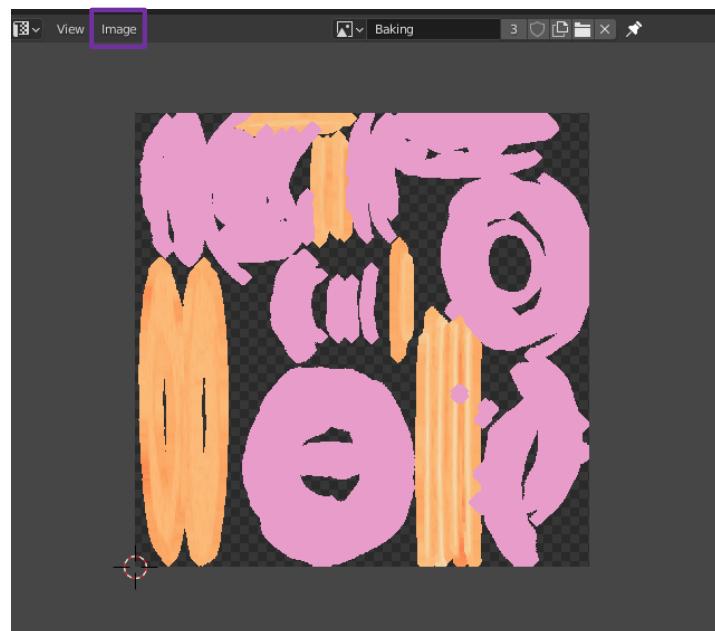
- Make sure all objects that goes together are selected (here the donut and the icing)
- For each object, make sure you added the baking image texture and it is selected (white border)
- For each object make sure the baking uv map is selected
- Go to **render properties** and select the **Cycles** render engine



APPENDIX 10: BAKING TEXTURE

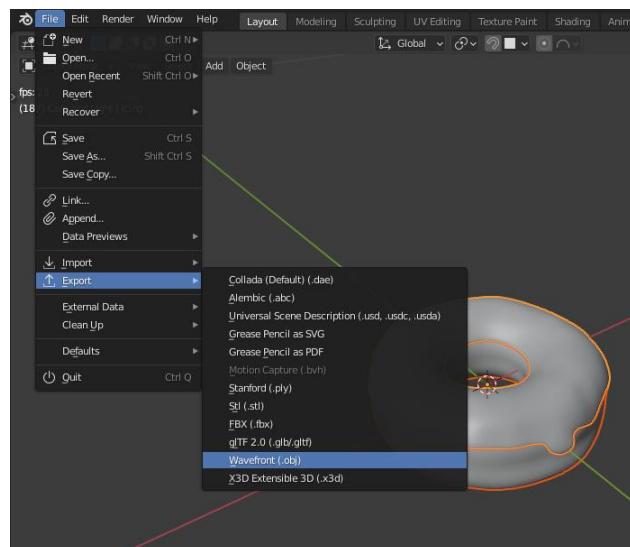
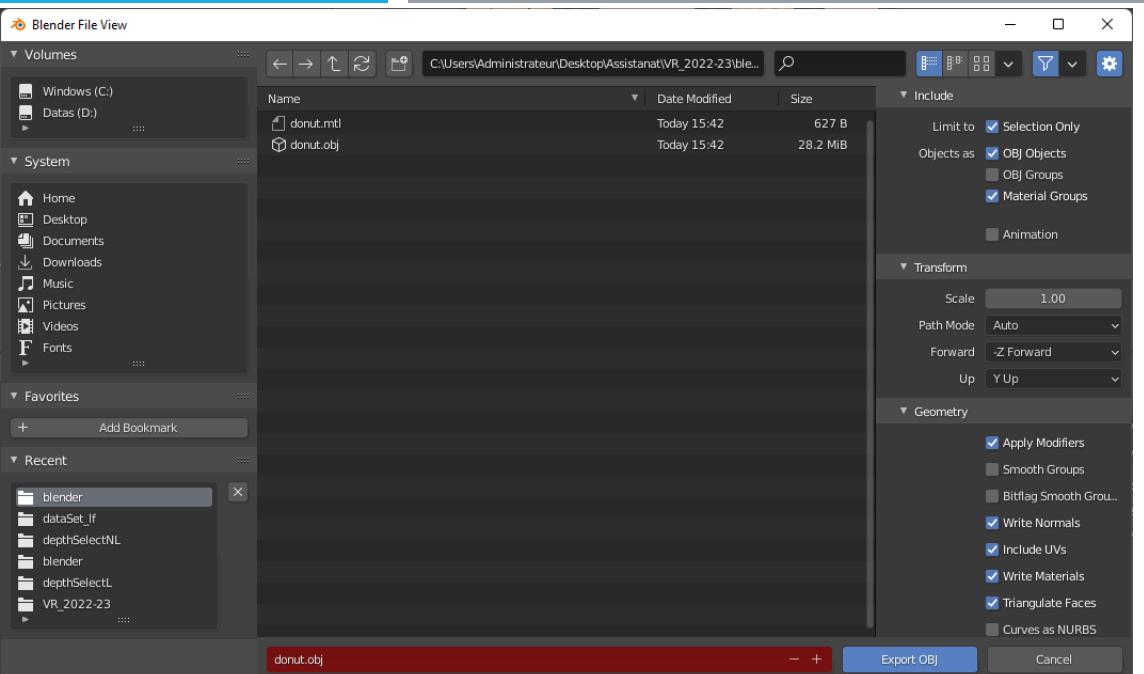
- Go to the **bake** section
- Put bake type as **diffuse** then click on **bake**
- A few moment later you should see your texture image, **save it** as a jpg

Note : here you can see some blocks of vertices overlap, try to avoid this



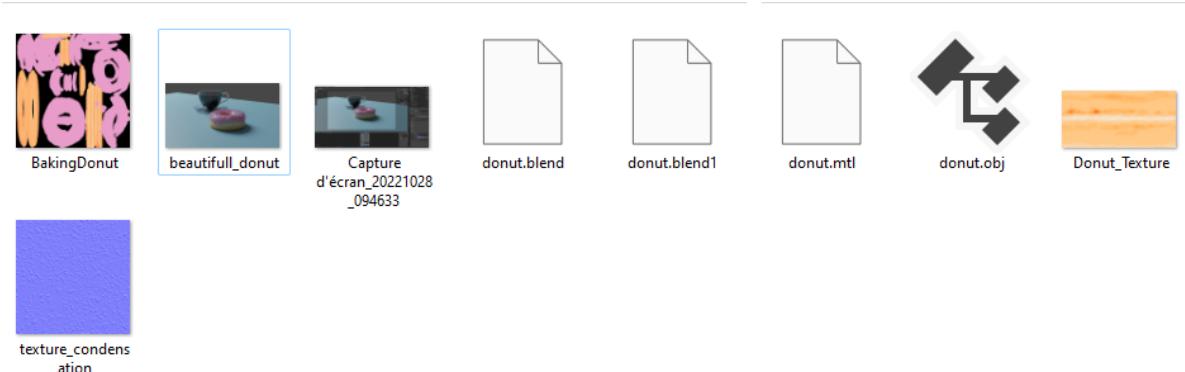
APPENDIX 10: BAKING TEXTURE

- Go to file -> Export -> Wavefront (.obj)
- Select « Material Groups » and « Triangulate Faces » in the option
- Choose the name and export your object



APPENDIX 10: BAKING TEXTURE

- Now you have a .obj file with a texture image that you can use in opengl
- This is a summary, more detail here :
<https://www.youtube.com/watch?v=wG6ON8wZYLc>



APPENDIX 10: DIFFERENCE SMOOTH AND NON SMOOTH SPHERE

- Even with Phong shading, in “non smooth” sphere you see the triangles!
- This happens because the normals on the sphere are not smooth
- Each vertex uses the same normal as the face’s normal
- In blender, when we **smooth** the mesh, what we are doing is to set at each vertex the mean normal between adjacent faces

