title: "Exam One(Redo for HW)" author: "Collin Rafferty" date: "10/22/2021" output: pdf_document

Question One:

$$H_0: P_A - P_B = 0$$
 $H_A: P_A - P_B \neq 0$

Where P_A is the proportion of people with at least some college in the Northeastern and Western regions of the U.S. that have been vaccinated, P_B is the proportion of people with a high school diploma in the Midwestern and Southern regions of the U.S. that have been vaccinated.

$$P_{A} \ Estimate = \frac{23,363}{25,907} = 90.18\% \quad P_{B} \ Estimate = \frac{3,478}{4,678} = 74.35\%$$

$$SE = \sqrt{\frac{\widehat{P_{A}}(1-\widehat{P_{A}})}{n_{1}} + \frac{\widehat{P_{B}}(1-\widehat{P_{B}})}{n_{2}}} = \sqrt{\frac{.9018(1-.9018)}{25,907} + \frac{.7435(1-.7435)}{4,678}} = .009$$

$$t - stat = \frac{\bar{X}}{SE} = \frac{.9018 - .7435}{.009} = 17.58889$$

I chose to use a .05 significance level. This means the results are significant at p < .05, and the p-value is < .00001, so the results are highly statistically significant. This means we succeeded in rejecting the null and showing sufficient evidence there is a statistically significant difference between the vaccination rates of the two samples.

Confidence Interval:
$$(.9018 - .7435 \pm .009) = (.1493, .1676)$$

We are 95% confident that the average difference between the vaccination rate of sample A and sample B is between 14.93% and 16.73%

Question Two:

$$H_0: P_A-P_B=0$$
 $H_A: P_A-P_B\neq 0$

 P_A is the proportion of males with an associate degree or less who have been vaccinated, and P_B is the proportion of people who identify as transgender or other and have a bachelor's degree or great and have been vaccinated.

$$P_{A} \ Estimate = \frac{8,486}{10,290} = 82.45\% \quad P_{B} \ Estimate = \frac{313}{389} = 80.46\%$$

$$SE = \sqrt{\frac{\widehat{P_{A}}(1-\widehat{P_{A}})}{n_{1}} + \frac{\widehat{P_{B}}(1-\widehat{P_{B}})}{n_{2}}} = \sqrt{\frac{.8245(1-.8245)}{10,290} + \frac{.8046(1-.8046)}{389}} = .0201$$

$$t - stat = \frac{\bar{X}}{SE} = \frac{.8245 - .8046}{.0201} = .99$$

I chose to use a .10 significance level. This means the results are significant at p < .10, and the p-value is .322197, so the results are not statistically significant. This means we failed to reject the null hypothesis, which means there was not sufficient evidence to conclude the vaccination rate between these two groups was statistically significant.

```
Confidence Interval: (.8245 - .8046 \pm .0210) = (-.0011, .0409)
```

We are 95% confident that the average difference between the vaccination rate of sample A and sample B is between -.11% and 4.09%

These were not expected results. I thought because of their educational attainment levels, sample A would have a much higher vaccination rate than sample B. One explanation for this disparity may be the difference in the sizes of the samples. Sample A is only about 4% the size of sample B

Question Three:

A)

```
load("/cloud/project/Household Pulse data.RData")
#Creation of Subgroup
attach(Household Pulse data)
use_varb <- ((RRACE=="White") | (RRACE=="Black")) & (INCOME== "HH income $75 -</pre>
99.9") & (RHISPANIC== "Not Hispanic") & ((EEDUC=="adv deg") | (EEDUC=="bach d
eg"))
sub1 <- subset(Household Pulse data,use varb)</pre>
detach(Household Pulse data)
attach(sub1)
# Summary Statistics
summary(sub1)
##
           RHISPANIC
                          RRACE
                                              EEDUC
                                                                 MS
##
   Not Hispanic:5996
                        White:5684
                                     less than hs:
                                                                     20
                                                         NA
   Hispanic
                        Black: 312
                                                         married
                                                                 :4525
##
                                     some hs
                                                     0
##
                        Asian:
                                     HS diploma :
                                                     0
                                                        widowed : 204
##
                        Other:
                                     some coll
                                                     0
                                                        divorced: 502
##
                                     assoc deg :
                                                     0
                                                         separated: 52
##
                                     bach deg
                                                :3005
                                                         never
                                                                 : 693
                                               :2991
##
                                     adv deg
                                          SEXUAL ORIENTATION
##
   EGENID BIRTH
                      GENID DESCRIBE
   male :2560
                  NA
                                                   : 49
##
                            : 32
                                     NA
   female:3436
##
                 male
                             :2525
                                     gay or lesbian: 206
##
                  female
                           :3394
                                     straight
                                                  :5501
##
                                     bisexual
                                                   : 158
                 transgender:
                                6
##
                  other
                                39
                                     something else:
                                                      46
##
                                     dont know :
                                                      36
```

```
##
##
                         KIDS LT5Y
                                                            KIDS 5 11Y
##
    NA
                               :5268
                                       NA
                                                                 :4984
##
   Yes children under 5 in HH: 728
                                       Yes children 5 - 11 in HH:1012
##
##
##
##
##
##
                        KIDS 12 17Y
                                                                     ENROLLNONE
                               :5074
##
    NA
                                       NA
                                                                          :5501
##
   Yes children 12 - 17 in HH: 922
                                       children not in any type of school: 495
##
##
##
##
##
                  RECVDVACC
##
                                                     DOSESRV
##
    NA
                       : 13
                                NA
                                                         : 330
                                                          :5570
##
   yes got vaxx
                       :5682
                                yes got all doses
##
   no did not get vaxx: 301
                               yes plan to get all doses: 83
##
                                no will not get all doses:
##
##
##
##
                        GETVACRV
                                                                    KIDDOSES
##
                                     NA
    NA
                            :5687
                                                                        :5078
##
    definitely will get vaxx:
                                     Yes kids got or will get all doses: 701
                               15
##
    probably will get vaxx :
                                23
                                     no kids did not or will not
                                                                        : 217
   unsure about vaxx
                                67
##
    probably not
                                82
##
    definitely not
                            : 122
##
##
                       KIDGETVAC
                                                          HADCOVID
##
   NA
                             :5776
                                     NA
                                                              : 17
    definitely will get vaxx:
                                31
                                     yes doctor told had covid: 670
##
    probably will get vaxx :
                                28
                                     no did not
                                                               :5288
##
    unsure about vaxx
                                46
                                     not sure
                                                               : 21
##
    probably not
                                44
##
    definitely not
                                58
    dont know yet
                                13
##
                     WRKLOSSRV
                                                             ANYWORK
##
    NA
                                   NA
                          : 10
   yes recent HH job loss: 349
                                   yes employment in last 7 days:4113
##
##
    no recent HH job loss :5637
                                  no employment in last 7 days :1874
##
##
##
##
##
                   KINDWORK
                                          RSNNOWRKRV
```

```
##
   NA
                       :1916
                               NA
                                              :4144
## work for govt
                       : 943
                               retired
                                              :1378
## work for private co:1937
                               other
                                              : 176
## work for nonprofit : 734
                               caring for kids: 103
## self employed
                  : 409
                               did not want
                                              : 78
##
   work in family biz : 57
                               laid off
                                                 51
##
                               (Other)
                                                 66
##
                                         CHLDCARE
## NA
                                             :4806
   yes impacts to childcare because pandemic: 287
##
   no
                                             : 903
##
##
##
##
                             CURFOODSUF
##
##
   NA
                                  : 13
## had enough food
                                  :5615
##
   had enough but not what wanted: 344
   sometimes not enough food : 22
## often not enough food
                                     2
##
##
##
                                                  CHILDFOOD
##
                                                       :5814
   NA
## often kids not eating enough because couldnt afford: 3
   sometimes kids not eating enough
                                                       : 22
## kids got enough food
                                                       : 157
##
##
##
##
                                               ANXIOUS
##
   NA
## no anxiety over past 2 wks
                                                   :2721
## several days anxiety over past 2 wks
                                                   :2088
   more than half the days anxiety over past 2 wks: 543
##
   nearly every day anxiety
                                                   : 636
##
##
##
                                                WORRY
## NA
                                                       9
##
   no worry over past 2 wks
                                                   :3501
   several days worried over past 2 wks
                                                  :1711
   more than half the days worried over past 2 wks: 388
##
   nearly every day worry
                                                   : 387
##
##
##
                              TENURE
##
   NA
## housing owned free and clear :1752
```

```
housing owned with mortgage
                                  :3548
##
    housing rented
                                  : 664
##
    housing occupied without rent:
                                     21
##
##
##
                                    LIVQTRRV
                                                            RENTCUR
    live in detached 1 family
                                         :4875
                                                                 :5332
                                                 NA
    live in bldg w 5+ apts
##
                                         : 470
                                                 current on rent: 654
    live in 1 family attached to others: 444
                                                 behind on rent: 10
##
    live in building with 3-4 apts
                                            80
    live in bldg w 2 apartments
                                            68
##
   live in mobile home
                                            30
##
    (Other)
                                            29
##
                   MORTCUR
                                                                         EVICT
##
    NA
                        :2449
                                NA
                                                                            :598
6
##
    current on mortgage:3475
                                very likely evicted in next 2 months
1
##
    behind on mortgage: 72
                                somewhat likely evicted in next 2 months
0
##
                                not very likely evicted in next 2 months
4
##
                                not at all likely evicted in next 2 months:
5
##
##
##
                                               FORCLOSE
                                                                   EST ST
##
    NA
                                                   :5924
                                                           California: 337
##
    very likely forclosed in next 2 months
                                                       5
                                                           Texas
                                                                      : 272
    somewhat likely forclosed in next 2 months
                                                       8
                                                           Washington: 233
    not very likely forclosed in next 2 months
                                                      17
                                                           Florida
                                                                      : 201
##
    not at all forclosed evicted in next 2 months:
                                                           Maryland
                                                                      : 201
##
                                                           Utah
                                                                      : 196
##
                                                           (Other)
                                                                      :4556
##
                       PRIVHLTH
                                                     PUBHLTH
                                                                        REGION
##
    has private health ins:5420
                                   has public health ins:1779
                                                                  Northeast:1013
##
    no private health ins : 459
                                   no public health ins :3852
                                                                  South
                                                                           :1899
##
    NA
                           : 117
                                   NA
                                                         : 365
                                                                  Midwest
                                                                           :1305
##
                                                                  West
                                                                           :1779
##
##
##
##
                                     Num kids Pub School Num kids Priv School
                          INCOME
##
   HH income $75 - 99.9
                             :5996
                                     Min.
                                             :0.000
                                                          Min.
                                                                  :0.000
##
                                     1st Qu.:1.000
                                 0
                                                          1st Qu.:0.000
##
    HH income less than $25k:
                                     Median :2.000
                                                          Median :1.000
##
    HH income $25k - $34.9k :
                                 0
                                     Mean
                                             :1.748
                                                          Mean
                                                                  :1.011
   HH income $35k - 49.9
                                     3rd Ou.:2.000
                                                          3rd Qu.:2.000
##
    HH income $50k - 74.9
                                     Max.
                                             :4.000
                                                          Max.
                                                                  :2.000
    (Other)
                                     NA's :4685
                                                          NA's
                                                                 :5727
```

```
Num kids homeschool
                               Works_onsite
                                                       works remote
           :0.00
## Min.
                        NA
                                      : 94
                                              NA
                                                              : 182
## 1st Qu.:0.00
                        worked onsite:3579
                                              worked remotely:3109
## Median :1.00
                                      :2323
                        no
   Mean
           :0.72
##
##
    3rd Qu.:1.00
   Max.
           :2.00
##
    NA's
           :5839
##
             Shop_in_store
                                             eat_in_restaurant
##
    NA
                    : 86
                            NA
                                                      : 104
    shopped in store:5485
                            eat at restaurant indoors:3394
##
##
                    : 425
                                                      :2498
##
##
##
##
round(prop.table(table(RRACE=="White", ANXIOUS)),2)
##
          ANXIOUS
##
             NA no anxiety over past 2 wks several days anxiety over past 2 w
ks
##
     FALSE 0.00
                                       0.03
                                                                             0.
02
##
     TRUE 0.00
                                       0.43
                                                                             0.
33
          ANXIOUS
##
##
           more than half the days anxiety over past 2 wks
     FALSE
##
                                                       0.09
##
     TRUE
##
          ANXIOUS
##
           nearly every day anxiety
##
     FALSE
                                0.00
     TRUE
                                0.10
##
round(prop.table(table(RRACE=="Black", ANXIOUS)),2)
##
          ANXIOUS
##
             NA no anxiety over past 2 wks several days anxiety over past 2 w
ks
##
     FALSE 0.00
                                       0.43
                                                                             0.
33
##
     TRUE 0.00
                                       0.03
                                                                             0.
02
##
          ANXIOUS
##
           more than half the days anxiety over past 2 wks
##
     FALSE
                                                       0.09
                                                       0.00
##
     TRUE
          ANXIOUS
##
##
           nearly every day anxiety
```

| ## | FALSE | 0.10 |
|----|-------|------|
| ## | TRUE | 0.00 |

The subgroup I created is revealing because it looks at how upper-middle-class college-educated whites have coped with the pandemic compared to upper-middle-class college-educated African Americans. If you look at the proportion tables of how the anxious levels differ between the two groups, it is very eye-opening. For example, 43% of African Americans in this subgroup reported feeling no anxiety over the past two weeks compared to 43% of whites that reported feeling anxiety over the past two weeks. In the very next factor level, however, these two groups' anxiety levels flip. Much of the pandemic pernicious effects disproportionally affected the poor and underrepresented, but it is also important to remember that it has had a profound impact on every level of society. I think my subgroup helps to show that.

B) I thought it would be interesting to look how the percentage of people with private health insurance differs between the subgroup, and the larger sample.

$$H_0: P_A = P_B$$
 $H_A: P_A \neq P_B$

Where P_A is the proportion of people in the subgroup who have private health insurance, and P_B is the proportion of people in the greater sample that has private health insurance.

summary(sub1\$PRIVHLTH)

has private health ins no private health ins NA
5420 459 117

summary(Household_Pulse_data\$PRIVHLTH)

has private health ins no private health ins NA
46869 11275 10970

$$P_{A} \ Estimate = \frac{5,420}{5,996} = 90.39\% \quad P_{B} \ Estimate = \frac{46,869}{69,114} = 67.81\%$$

$$SE = \sqrt{\frac{\widehat{P_{A}}(1-\widehat{P_{A}})}{n_{1}} + \frac{\widehat{P_{B}}(1-\widehat{P_{B}})}{n_{2}}} = \sqrt{\frac{.9039(1-.9039)}{5,996} + \frac{.6781(1-.6781)}{69,114}} = .0042$$

$$t - stat = \frac{\overline{X}}{SE} = \frac{.9039 - .6781}{.0042} = 53.76$$

I chose to use a .05 significance level. This means the results are significant at p < .05, and the p-value is < .00001, so the results are highly statistically significant. This means we succeeded in rejecting the null and showing sufficient evidence there is a statistically significant difference between the percentage of people with private health insurance in the subgroup compared to the larger sample.

Confidence Interval:
$$(.9036 - .6781 \pm .0042) = (.2216, .23)$$

We are 95% confident that the average difference between the people with private health insurance in the subgroup and the larger sample is between 22.16% and 23%.

C)

```
##require(tidyverse)
HH1 <-
Household Pulse data%>%mutate(INCOME5=as.numeric(INCOME),INCOME5=case when(IN
COME5==5~NA integer ,TRUE~as##.integer(INCOME5)))
HH2 <-
Household_Pulse_data%>%mutate(GEN1=as.numeric(GENID_DESCRIBE),GEN1=case_when(
GEN1==1~NA_integer_,TRUE~as. integer(GEN1)))
HH3 <- Household Pulse data%>%mutate(VAX1=as.numeric(RECVDVACC),
##VAX1=case when(VAX1==1~NA integer ,TRUE~as.integer(VAX1)))
HH4 <- Household Pulse data%>%mutate(ANX2=as.numeric(ANXIOUS),
ANX2=case when(ANX2==2~NA integer ,TRUE~as.integer(ANX2)))
H5 <- Household Pulse data%>%mutate(EEDUC3=as.numeric(EEDUC),
##EEDUC3=case_when(EEDUC3==3~NA_integer_,TRUE~as.integer(EEDUC3)))
norm_varb <- function(X_in) {(X_in - min(X_in, na.rm = TRUE))/( max(X_in,</pre>
##na.rm = TRUE) - min(X in, na.rm = TRUE) )}
##norm INCOME5 <- norm varb(HH1$INCOME5)</pre>
##norm_GEN1 <- norm_varb(HH2$GEN1)</pre>
##norm_VAX1<- norm_varb(HH3$VAX1)</pre>
##norm ANX2 <- norm varb(HH4$ANX2)</pre>
##norm EEDUC3<- norm varb(HH5$EEDUC3)</pre>
##data use <- data.frame(norm INCOME5,norm GEN1,norm VAX1,norm ANX2,</pre>
##norm_EEDUC3)
##good obs data use <- complete.cases(data use,PUBHLTH)</pre>
##dat_use <- subset(data_use,good_obs_data_use)</pre>
##y use <- subset(PUBHLTH,good obs data use)</pre>
```

```
##set.seed(12345)
##NN_obs <- sum(good_obs_data_use == 1)
##select1 <- (runif(NN_obs) < 0.8)

##train_data <- subset(dat_use,select1)
##test_data <- subset(dat_use,(!select1))
##cl_data <- y_use[select1]
##true_data <- y_use[!select1]</pre>
```

```
##summary(cl data)
has public health ins no public health ins
                                                               NA
7146
                     12890
                                            6319
prop.table(summary(cl_data))
has public health ins no public health ins
                                                                NA
0.2711440
                      0.4890913
                                            0.2397648
summary(train data)
norm INCOME5
                  norm GEN1
                                   norm VAX1
                                                     norm ANX2
norm_EEDUC3
Min.
      :0.0000
                 Min.
                        :0.0000
                                  Min.
                                         :0.0000
                                                    Min.
                                                           :0.0000
                                                                     Min.
:0.0000
1st Qu.:0.0000
                 1st Qu.:0.0000
                                  1st Qu.:0.0000
                                                    1st Qu.:0.5000
                                                                     1st
Qu.:0.5000
Median :0.2857
                 Median :0.3333
                                  Median :0.0000
                                                    Median :0.5000
                                                                     Median
:0.8333
       :0.3629
                        :0.2307
                                         :0.1101
                                                           :0.5475
                                                                     Mean
Mean
                 Mean
                                  Mean
                                                    Mean
:0.7538
3rd Qu.:0.7143
                 3rd Qu.:0.3333
                                  3rd Qu.:0.0000
                                                    3rd Qu.:0.7500
                                                                     3rd
Qu.:1.0000
       :1.0000
Max.
                 Max.
                        :1.0000
                                  Max.
                                          :1.0000
                                                    Max.
                                                           :1.0000
                                                                     Max.
:1.0000
```

```
require(class)
for (indx in seq(1, 9, by= 2)) {
pred_PUBHLTH <- knn(train_data, test_data, cl_data, k = indx, l = 0, prob =
FALSE, use.all = TRUE)}</pre>
```

```
num_correct_labels <- sum(pred_PUBHLTH == true_data)

correct_rate <- num_correct_labels/length(true_data)

print(c(indx,correct_rate))

> print(c(indx,correct_rate))

[1] 9.0000000 0.7019365
```

With the predictor variables I included in the classifier, it had an accuracy of 70% of determining if a person has public health insurance or not. 70% is not terrible, but it could be improved. If I were to do another iteration, I would include the variables of ANYWORK,RSNNOWRKRV, and KINDWORK because if a person is a government employee, unemployed, or retired, they would be more likely to have public health insurance.

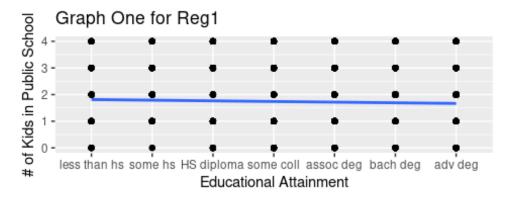
D)

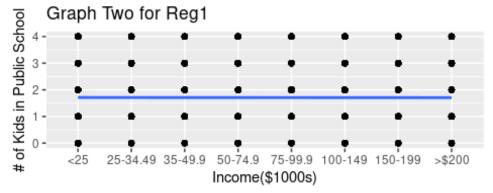
```
attach(Household_Pulse_data)
## The following objects are masked from sub1:
##
##
       ANXIOUS, ANYWORK, CHILDFOOD, CHLDCARE, CURFOODSUF, DOSESRV,
       eat_in_restaurant, EEDUC, EGENID_BIRTH, ENROLLNONE, EST_ST, EVICT,
##
       FORCLOSE, GENID_DESCRIBE, GETVACRV, HADCOVID, INCOME, KIDDOSES,
##
       KIDGETVAC, KIDS_12_17Y, KIDS_5_11Y, KIDS_LT5Y, KINDWORK, LIVQTRRV,
##
       MORTCUR, MS, Num kids homeschool, Num kids Priv School,
##
##
       Num kids Pub School, PRIVHLTH, PUBHLTH, RECVDVACC, REGION, RENTCUR,
##
       RHISPANIC, RRACE, RSNNOWRKRV, SEXUAL_ORIENTATION, Shop_in_store,
       TENURE, Works_onsite, works_remote, WORRY, WRKLOSSRV
##
reg1<- lm(as.numeric(Num kids Pub School) ~ INCOME+EEDUC+CHLDCARE+Works onsit
e)
require(stargazer)
## Loading required package: stargazer
##
## Please cite as:
```

```
## Hlavac, Marek (2018). stargazer: Well-Formatted Regression and Summary St
atistics Tables.
## R package version 5.2.2. https://CRAN.R-project.org/package=stargazer
stargazer(reg1,type = "text", title = "Table 1: Regression Results",out = "ta
ble1.txt")
##
## Table 1: Regression Results
##
                                                   Dependent variable
:
##
##
                                              as.numeric(Num kids Pub
School)
## -----
                                                        -0.087**
## 25k
##
                                                         (0.037)
##
                                                         -0.028
## 34.9k
##
                                                         (0.032)
##
## 35k - 49.9
                                                         -0.048*
##
                                                         (0.028)
##
## 50k - 74.9
                                                         -0.031
##
                                                         (0.028)
##
## 75 - 99.9
                                                          0.026
##
                                                         (0.025)
##
## 100k - 149
                                                          0.021
##
                                                         (0.031)
##
## 150 - 199
                                                          0.040
##
                                                         (0.029)
##
                                                         -0.151
## EEDUCsome hs
##
                                                         (0.101)
##
                                                        -0.291***
## EEDUCHS diploma
##
                                                         (0.087)
##
## EEDUCsome coll
                                                        -0.365***
##
                                                         (0.086)
##
```

```
## EEDUCassoc deg
                                                              -0.316***
##
                                                              (0.088)
##
                                                              -0.403***
## EEDUCbach deg
##
                                                              (0.086)
##
                                                              -0.412***
## EEDUCadv deg
##
                                                              (0.087)
##
                                                             0.101***
## CHLDCAREyes impacts to childcare because pandemic
##
                                                              (0.026)
##
                                                             0.212***
## CHLDCAREno
##
                                                              (0.016)
##
                                                              -0.057**
## Works onsiteworked onsite
                                                              (0.029)
##
                                                              -0.114***
## Works onsiteno
##
                                                              (0.030)
##
                                                              2.059***
## Constant
##
                                                              (0.087)
##
## Observations
                                                              14,006
## R2
                                                               0.018
## Adjusted R2
                                                               0.017
                                                        0.878 (df = 13988)
## Residual Std. Error
## F Statistic
                                                     15.008*** (df = 17; 13)
988)
======
## Note:
                                                       *p<0.1; **p<0.05; **
*p<0.01
require(ggplot2)
## Loading required package: ggplot2
require(ggthemes)
## Loading required package: ggthemes
Graph1 <-ggplot(Household Pulse data, aes(y=Num_kids_Pub_School, x= EEDUC, gr
oup=1))+geom point()+geom smooth(method=lm)+labs(x="Educational Attainment",y
="# of Kids in Public School", title = "Graph One for Reg1")
Graph2 <-ggplot(Household Pulse data, aes(y=Num_kids_Pub_School, x= INCOME, g
roup=1))+geom_point()+geom_smooth(method=lm)+labs(x="Income($1000s)", y="# of
```

```
Kids in Public School", title = "Graph Two for Reg1") + scale_x_discrete(labe
ls = c('<25','25-34.49','35-49.9', '50-74.9','75-99.9','100-149','150-199','>
$200' ))
gridExtra::grid.arrange(Graph1,Graph2)
## `geom_smooth()` using formula 'y ~ x'
## Warning: Removed 55108 rows containing non-finite values (stat_smooth).
## Warning: Removed 55108 rows containing missing values (geom_point).
## `geom_smooth()` using formula 'y ~ x'
## Warning: Removed 55108 rows containing non-finite values (stat_smooth).
## Warning: Removed 55108 rows containing missing values (geom_point).
```





The regression

provides some revealing insights about the data. For example, the number of children in public is negatively correlated with educational attainment level after a person graduates high school. A person with an advanced degree has -.412 fewer children in public school than someone who does not have an advanced degree. Of course, you can't have a proportion of a child, but it helps to show the picture. This result was to be expected, but what was interesting was how income affects the number of children a person has in public school. The coefficients of income are negative until 75K than positive for the rest of the income levels. Intuitively, you would think the opposite would be true: as income increases,

| the number of children a person has in public school decreases because these high earners have fewer children or send their children to private school. | |
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