

# **MODULE 8**

## **MULTILEVEL MEDIATION**

# OUTLINE

- 1 Mediation Overview
- 2 1-1-1 Model With Random Intercepts
- 3 1-1-1 Model With Random Slopes
- 4 Moderation on the  $\alpha$  or  $\beta$  paths

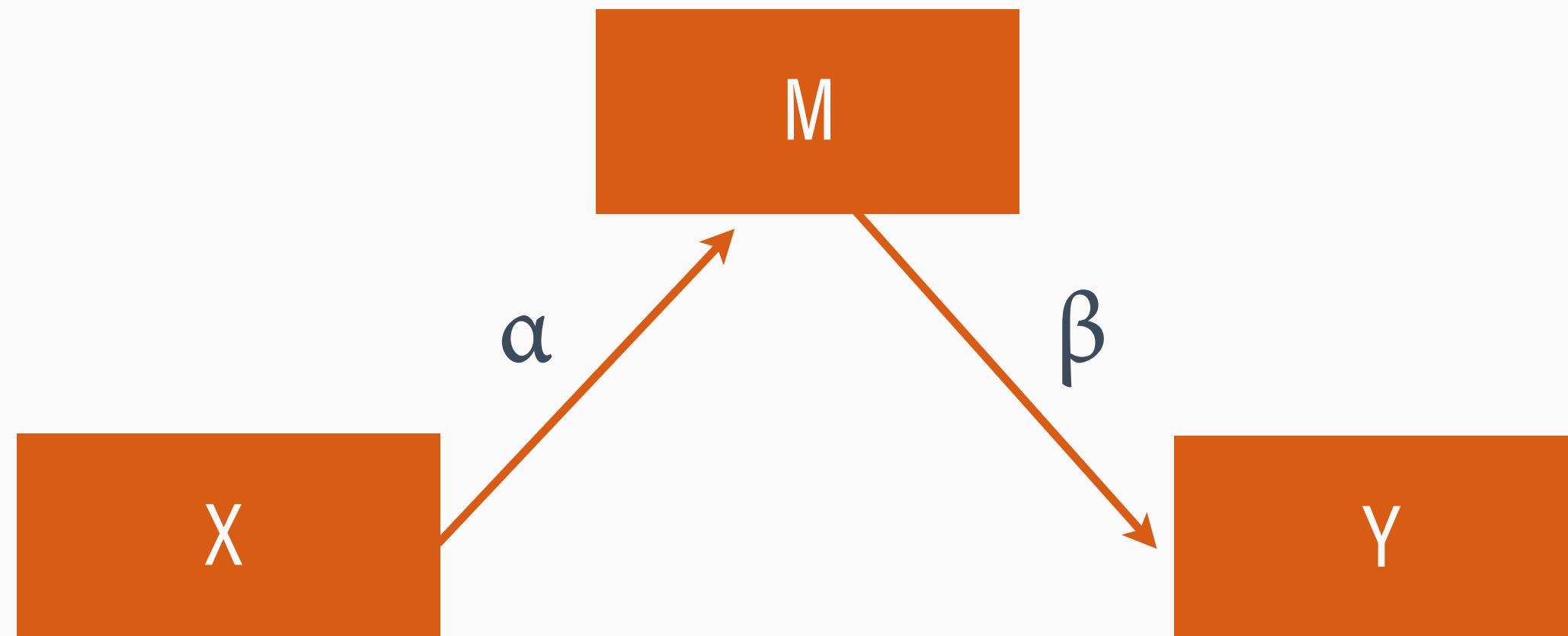
# MEDIATION

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- A mediation analysis attempts to clarify the mechanism through which two variables are related
- A typical model features an explanatory variable affecting an intervening variable (the mediator) that, in turn, transmits the predictor's influence to the outcome

# PATH DIAGRAMS

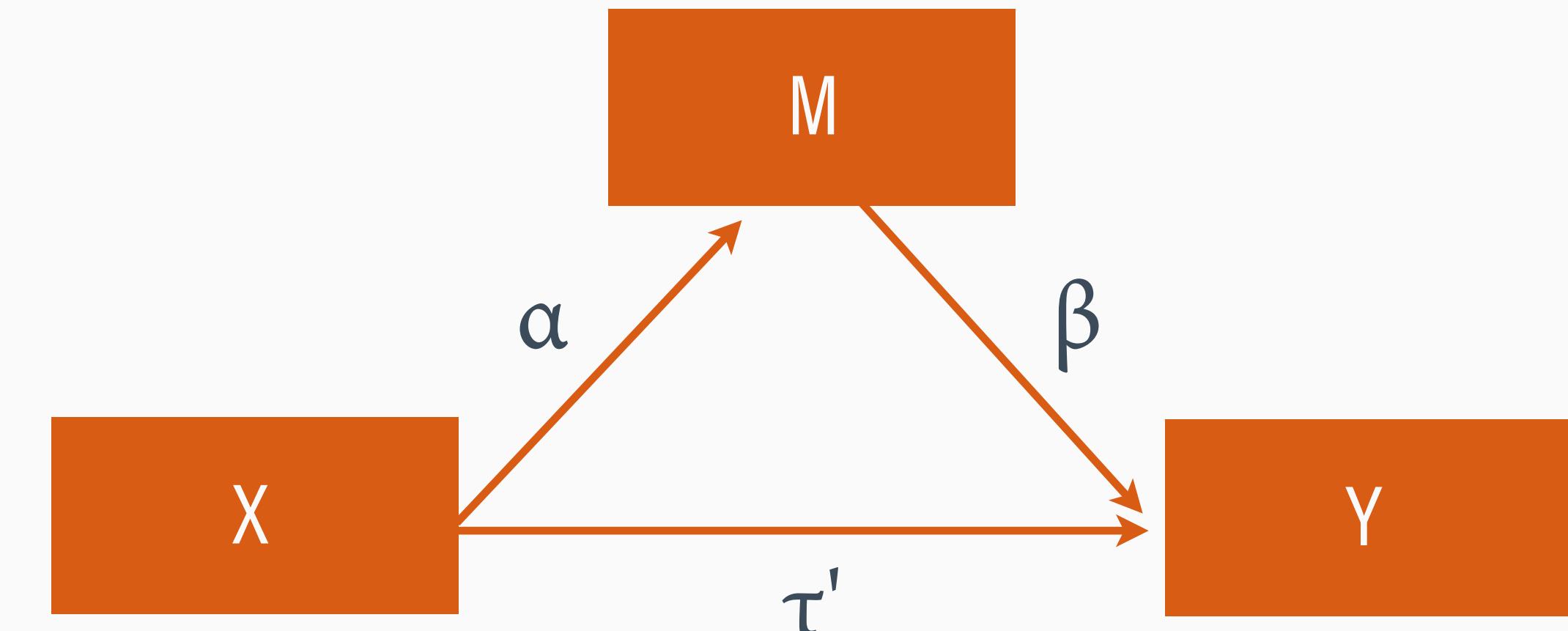
X-Y relation completely explained by indirect effect via M



$$M_i = I_M + \alpha(X_i) + \varepsilon_{Mi}$$

$$Y_i = I_Y + \beta(M_i) + \varepsilon_{Yi}$$

X-Y relation comprised of indirect and direct effect



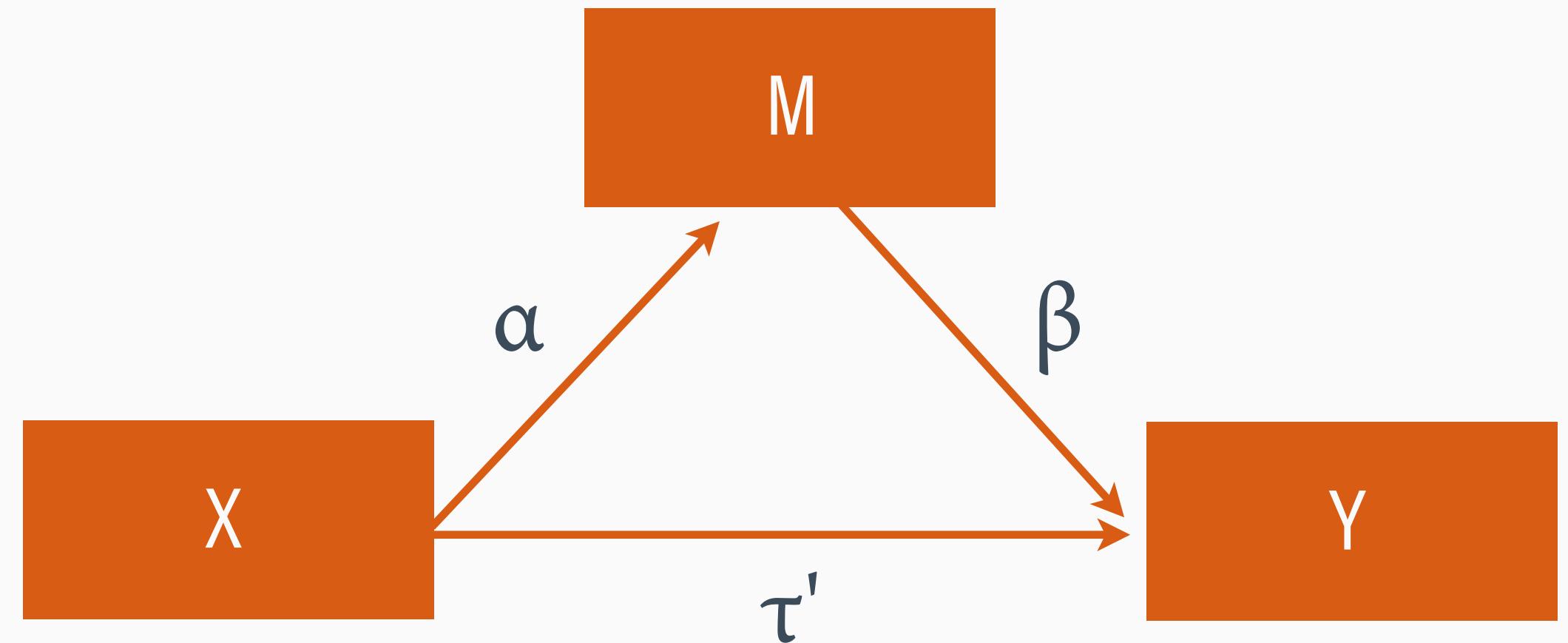
$$M_i = I_M + \alpha(X_i) + \varepsilon_{Mi}$$

$$Y_i = I_Y + \beta(M_i) + \tau'(X_i) + \varepsilon_{Yi}$$

# PRODUCT OF COEFFICIENTS ESTIMATOR

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- Multiplying the  $\alpha$  and  $\beta$  slopes (i.e., the indirect pathways) defines the so-called product of coefficients estimator
- The  $\alpha\beta$  product quantifies the influence of  $X$  on  $Y$  via the mediator  $M$
- The total  $X-Y$  association is  $\alpha\beta + \tau'$



# MEDIATION INFERENCE

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- Mediation inference is challenging because the sampling distribution of  $\alpha\beta$  can be quite nonnormal
- Using familiar test statistics to get a p-value can lead to incorrect conclusions about the mediated effect
- Bootstrap confidence intervals or MCMC are recommended because they can be asymmetric around the point estimate

# MULTILEVEL MEDIATION

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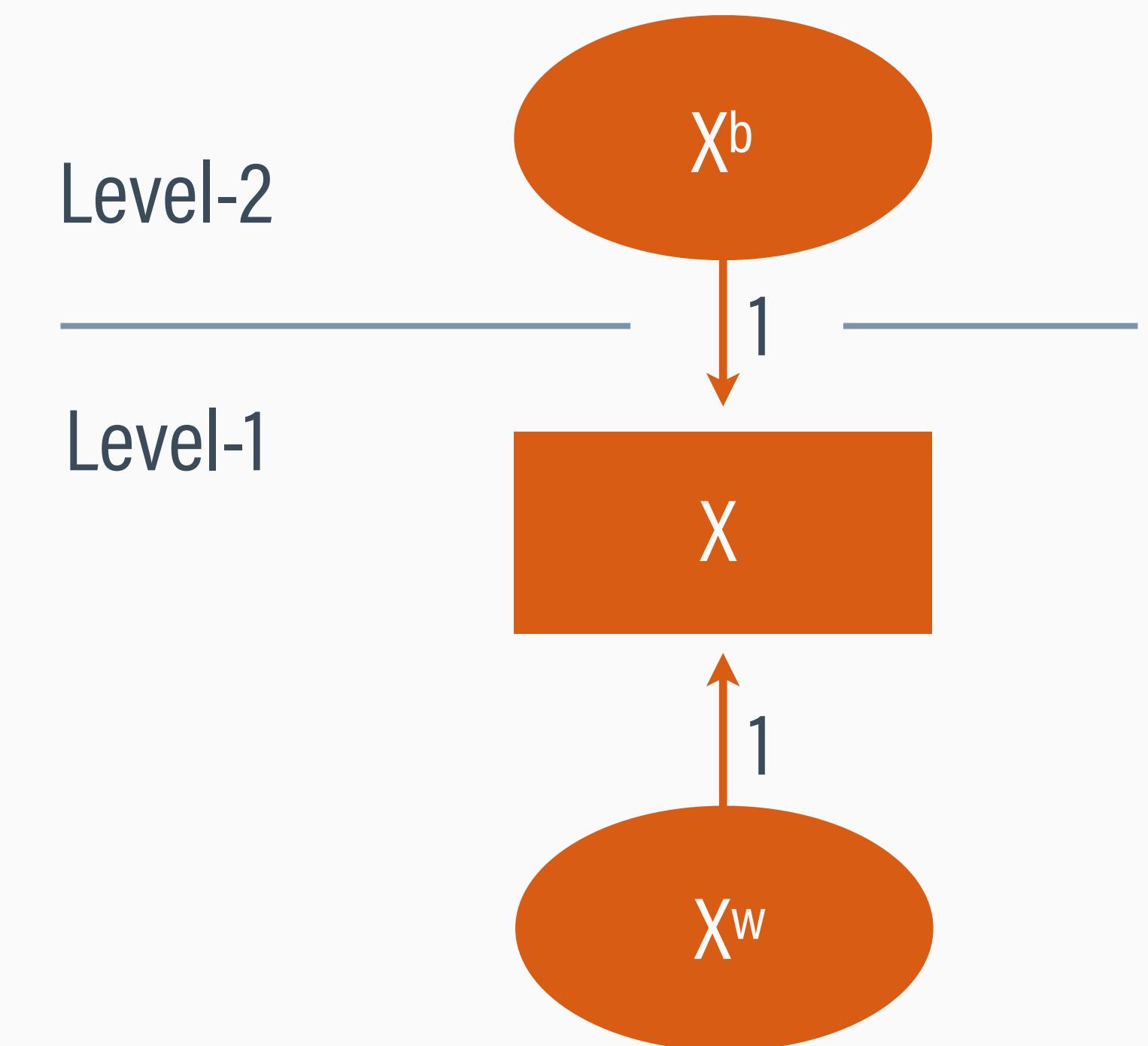
- Multilevel mediation incorporates associations at multiple levels of the data hierarchy
- Variables measured at level-1 have two sources of variation, and mediation can occur at the within and between levels
- Variables measured at level-2 have only level-2 associations

# DISAGGREGATION PATH DIAGRAM

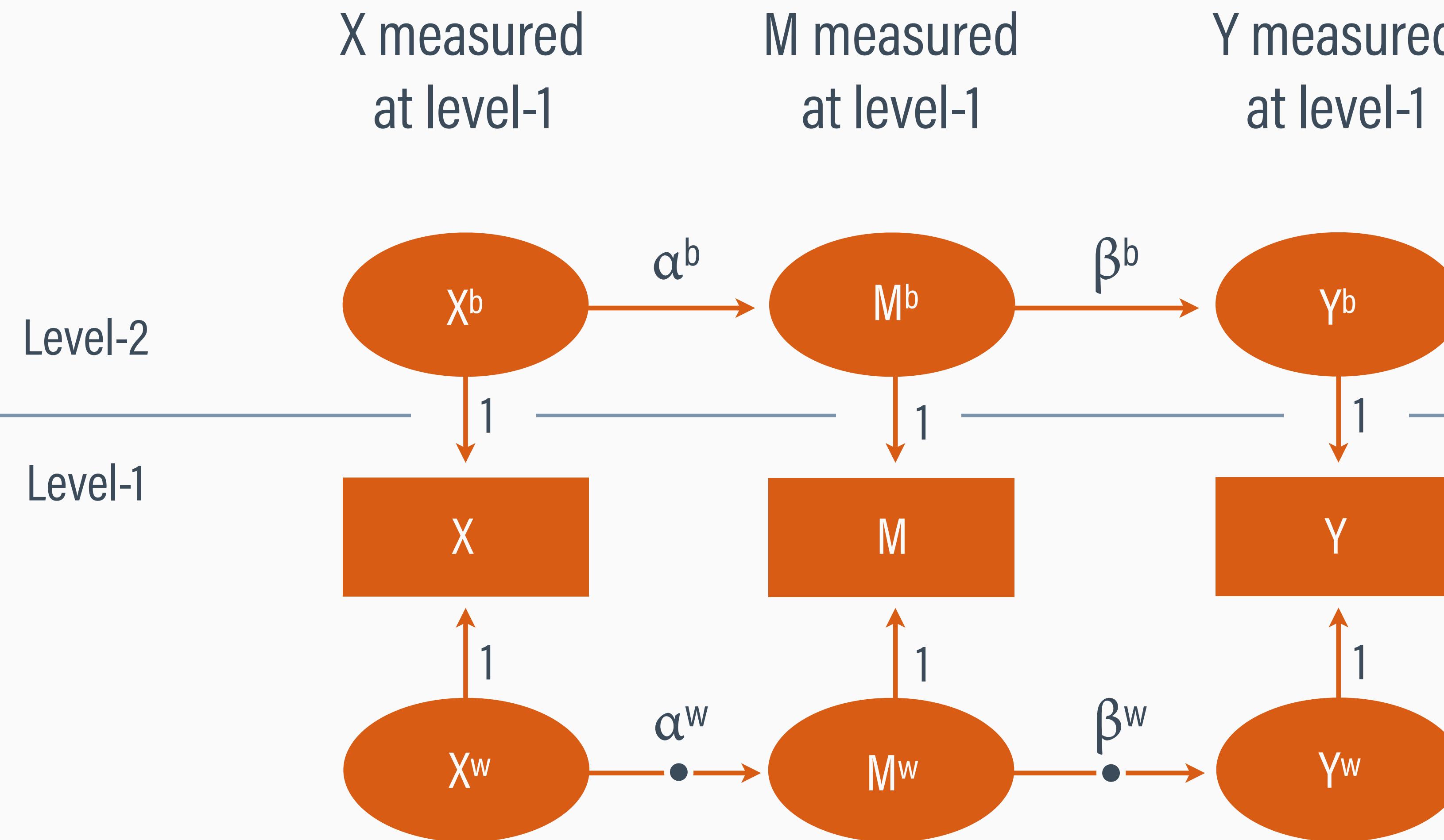
- A variable  $X$  is disaggregated into the sum of a cluster mean and within-cluster deviation

$$X_{ij} = X_j^b + X_{ij}^w = \text{cluster mean} + \text{within-cluster deviation}$$

- The rectangle represents the original variable, circles are the disaggregated components, and the 1s on the arrows convey that  $X^b$  and  $X^w$  contribute equally to  $X$

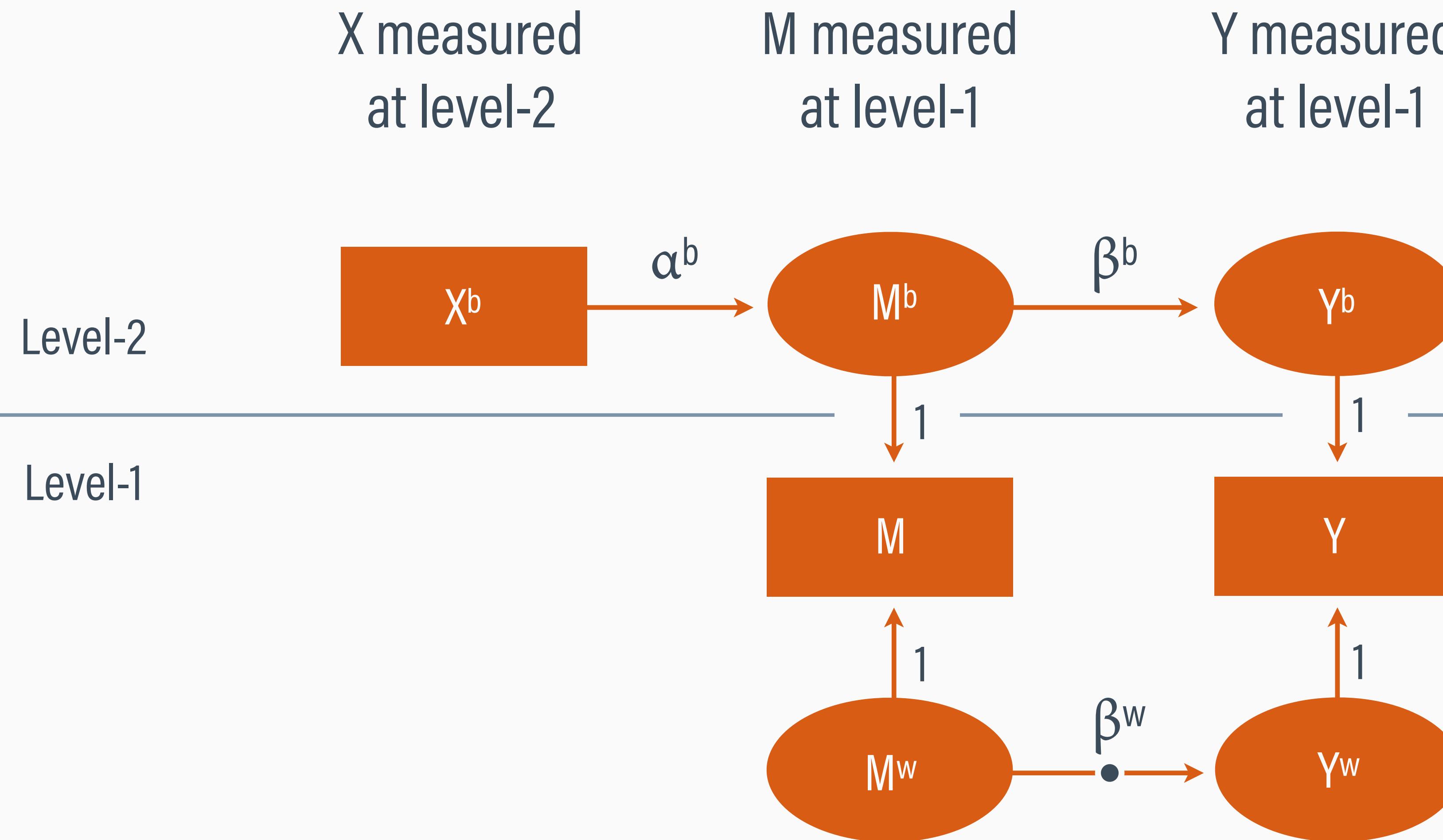


# 1-1-1 PATH DIAGRAM



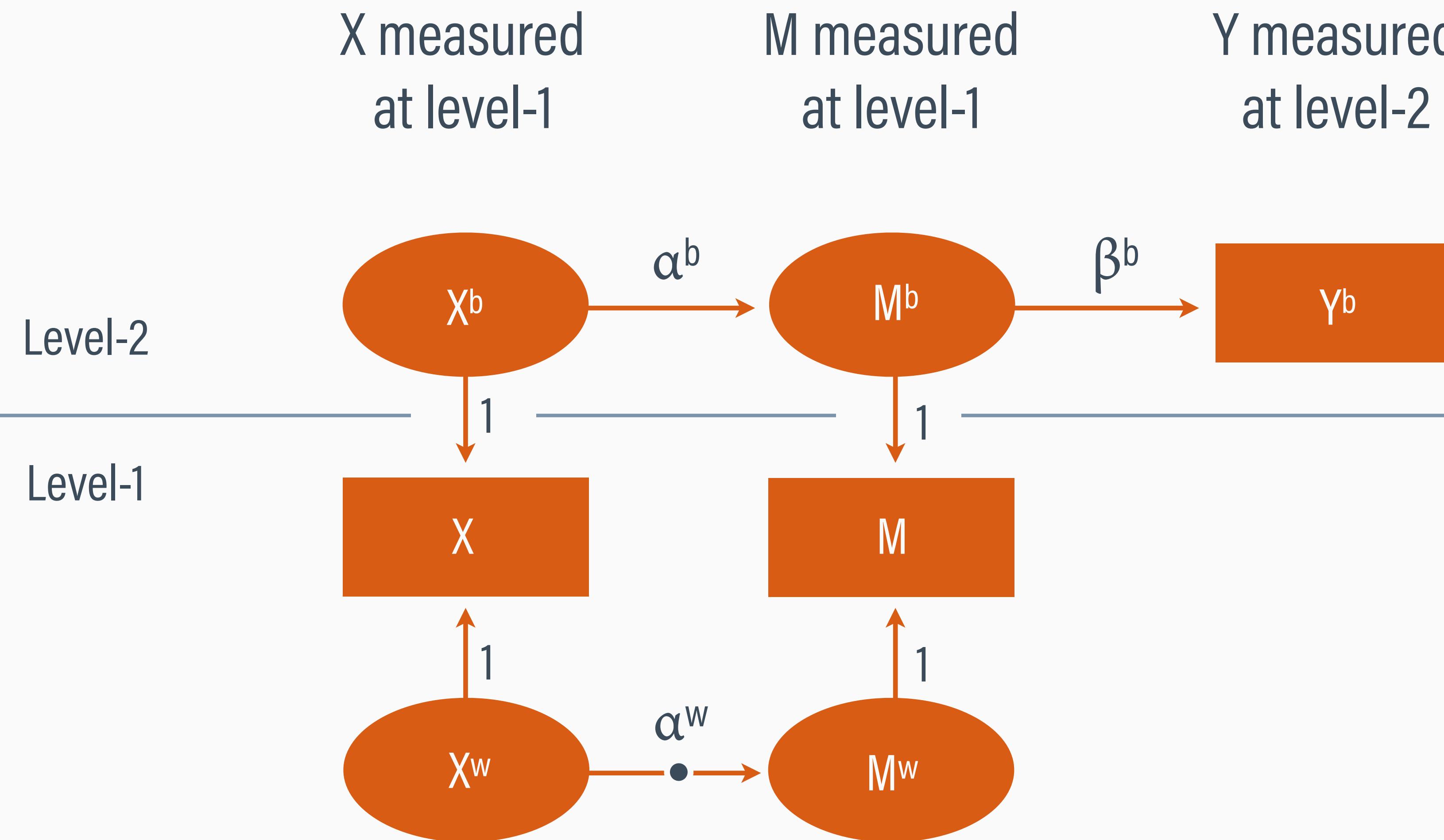
- level-1 slopes may or may not be random

# 2-1-1 PATH DIAGRAM



- level-1 slopes may or may not be random

# 1-1-2 PATH DIAGRAM



- level-1 slopes may or may not be random

# MLM MEDIATION INFERENCE

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- Bootstrapping is complex with multilevel data because there are multiple approaches to resampling
- Resample only level-2 units; resample level-2 units, then resample level-1 units within each chosen level-2 unit
- Bayesian MCMC estimation automatically provides appropriate asymmetric 95% limits

# RANDOM SLOPE VARIATION

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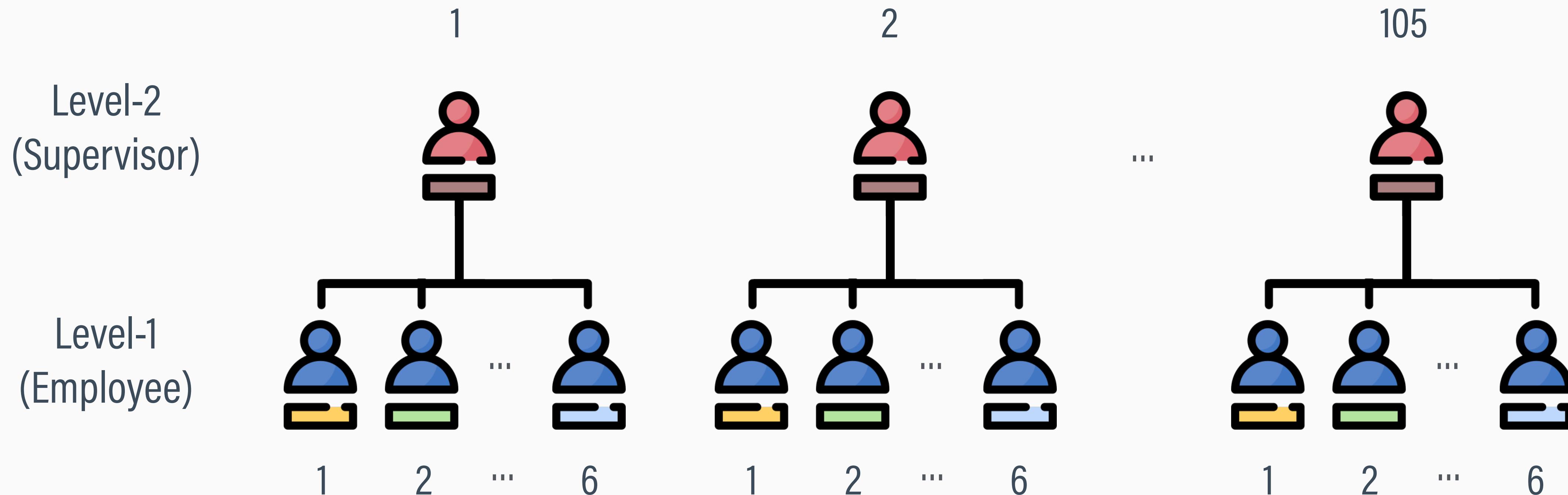
- Cluster-specific  $\alpha$  and  $\beta$  paths (i.e., random slopes in the M and Y models) imply that  $\alpha\beta$  can vary across level-2 units
- The product of coefficients estimator changes when both  $\alpha$  and  $\beta$  have random slope variation
- We need to use multilevel structural equation modeling ...

# OUTLINE

- 1 Mediation Overview
- 2 1-1-1 Model With Random Intercepts
- 3 1-1-1 Model With Random Slopes
- 4 Moderation on the  $\alpha$  or  $\beta$  paths

# ORGANIZATIONAL APPLICATION

- $n_j = 6$  employees at level-1 nested within  $J = 105$  teams or workgroups at level-2 ( $N = 630$  data records in total)



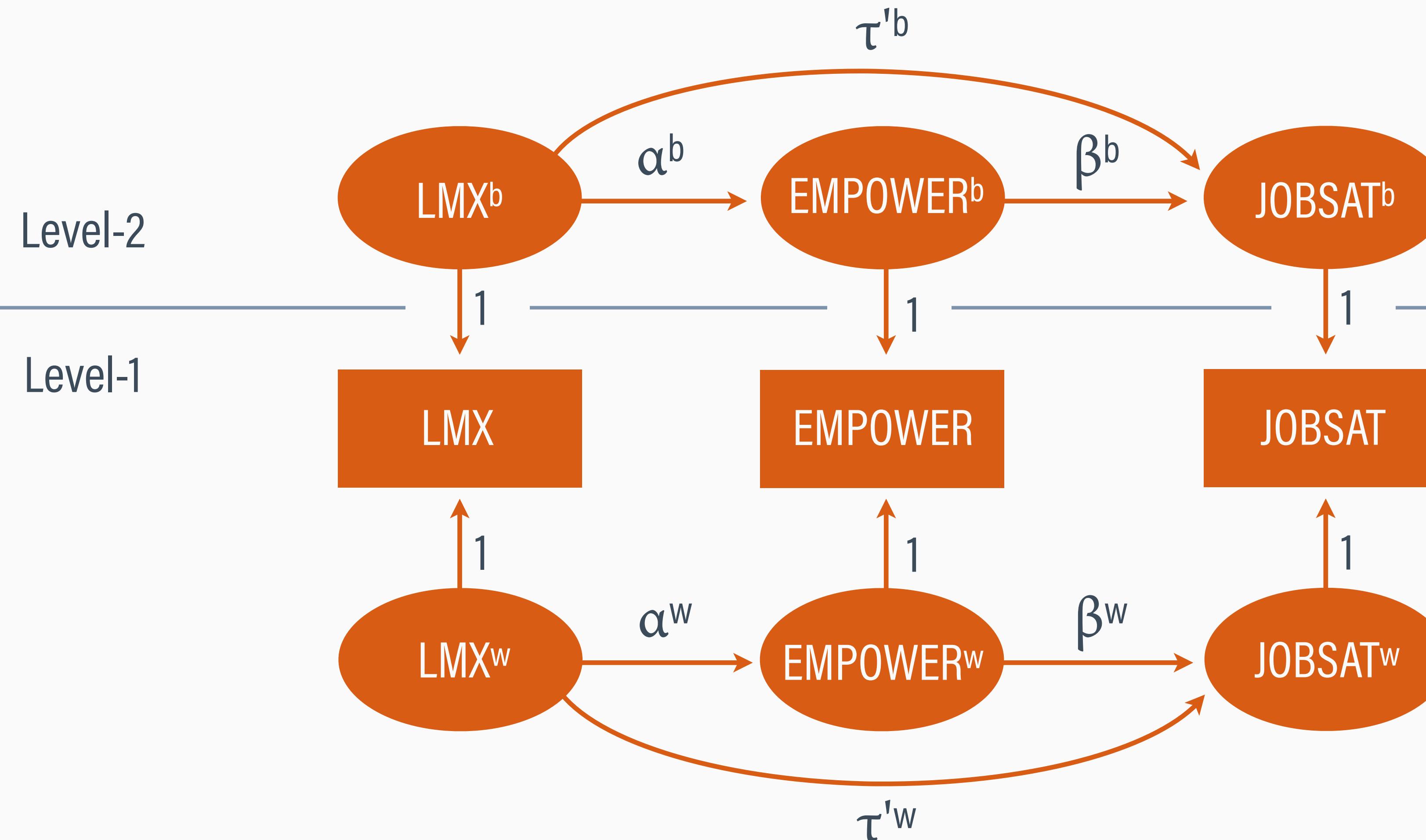
# VARIABLE INFORMATION

- Predictor
- Mediator
- Outcome

Variable	Definition	Level	Scale
Team	Team-level (level-2) identifier	2	Integers (1 to 105)
LMX	Leader-member exchange (relationship quality)	1	Numeric (0 to 17)
Empower	Employee empowerment	1	Numeric (14 to 42)
Jobsat	Job satisfaction rating	1	Numeric (0 to 17)

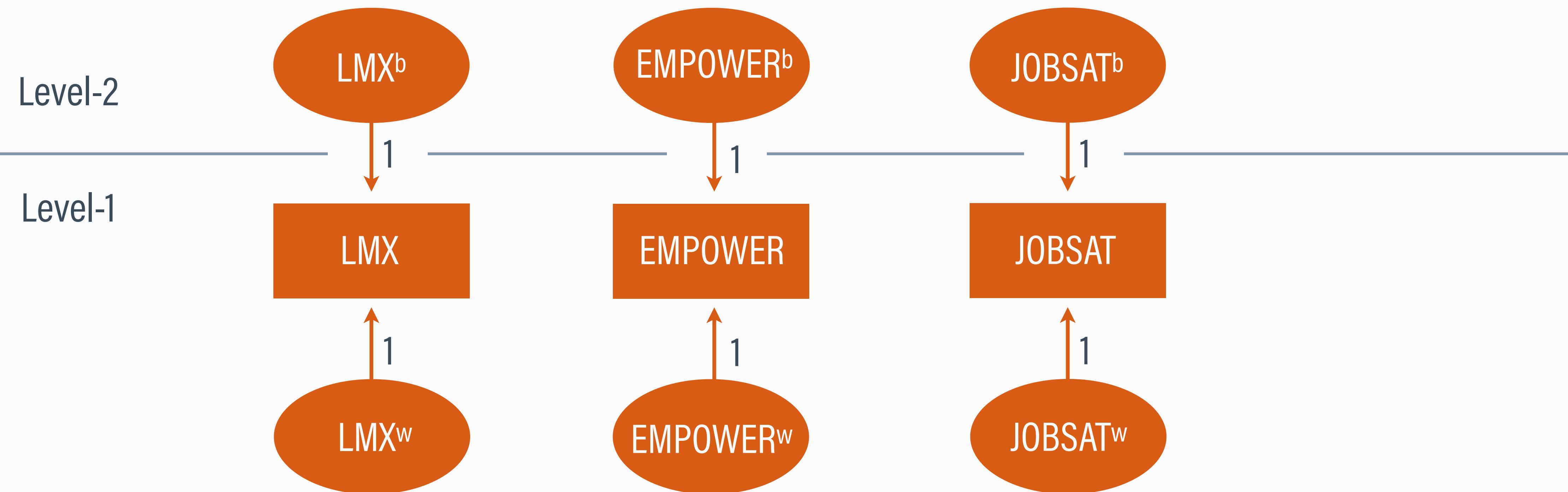
# PATH DIAGRAM

- Within- and between-cluster mediation at level-1 and level-2



# STARTING SIMPLE: EMPTY MODELS

- Disaggregated level-1 variables with no associations



# WITHIN-CLUSTER (LEVEL-1) MODELS

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- Each level-1 score is the sum of a level-2 cluster (team) average and a within-cluster residual

$$lmx_{ij} = lmx_j^b + \varepsilon_{ij}(lmx)$$

$$\text{empower}_{ij} = \text{empower}_j^b + \varepsilon_{ij}(\text{empower})$$

$$\text{jobsat}_{ij} = \text{jobsat}_j^b + \varepsilon_{ij}(\text{jobsat})$$

- The cluster means are level-2 latent variables (i.e., random intercepts or random effects) instead of arithmetic means

# BLIMP SCRIPT 7.1 EXCERPT

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$$lmx_{ij} = lmx_j^b + \varepsilon_{ij}(lmx)$$

$$empower_{ij} = empower_j^b + \varepsilon_{ij}(empower)$$

$$jobsat_{ij} = jobsat_j^b + \varepsilon_{ij}(jobsat)$$

**CLUSTERID:** Team;

**LATENT:** Team = LMX\_b Empower\_b JobSat\_b; # define team-level latent variables

**MODEL:**

LMX ~ intercept@LMX\_b; # set level-1 equation's intercept to the level-2 cluster mean

Empower ~ intercept@Empower\_b;

JobSat ~ intercept@JobSat\_b;

# BETWEEN-CLUSTER (LEVEL-2) MODELS

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- Each level-2 cluster mean is the sum of a grand mean and a level-2 residual

$$lmx_j^b = \beta_0(lmx) + u_{0j}(lmx)$$

$$empower_j^b = \beta_0(empower) + u_{0j}(empower)$$

$$jobsat_j^b = \beta_0(jobsat) + u_{0j}(jobsat)$$

- The cluster means are normally distributed level-2 latent variables (i.e., random intercepts or random effects)

# BLIMP SCRIPT 7.1 EXCERPT

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$$lmx_j^b = \beta_0(lmx) + u_{0j}(lmx)$$

$$empower_j^b = \beta_0(empower) + u_{0j}(empower)$$

$$jobsat_j^b = \beta_0(jobsat) + u_{0j}(jobsat)$$

**CLUSTERID:** Team;

**LATENT:** Team = LMX\_b Empower\_b JobSat\_b; # define team-level latent variables

**MODEL:**

LMX\_b ~ intercept; # empty level-2 equations

Empower\_b ~ intercept;

JobSat\_b ~ intercept;

LMX ~ intercept@LMX\_b; # set level-1 equation's intercept to the level-2 cluster mean

Empower ~ intercept@Empower\_b;

JobSat ~ intercept@JobSat\_b;

# OUTPUT HOUSEKEEPING

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**CLUSTERID:** Team;

**LATENT:** Team = LMX\_b Empower\_b JobSat\_b; # define team-level latent variables

**MODEL:**

**level2:** # arbitrary label that groups summary tables for a set of models

LMX\_b ~ intercept;

Empower\_b ~ intercept;

JobSat\_b ~ intercept;

**level1:** # arbitrary label that groups summary tables for a set of models

LMX ~ intercept@LMX\_b;

Empower ~ intercept@Empower\_b;

JobSat ~ intercept@JobSat\_b;

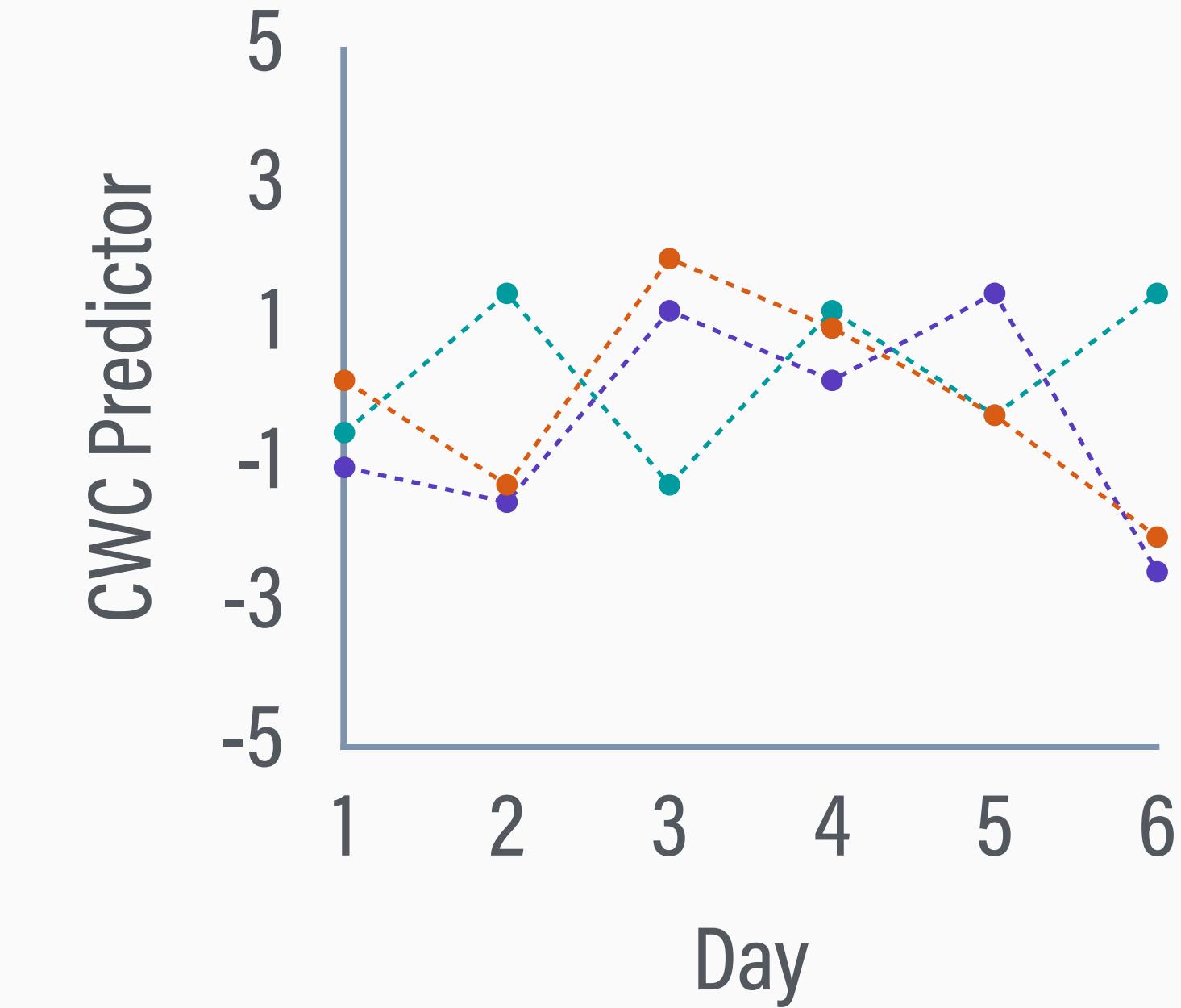
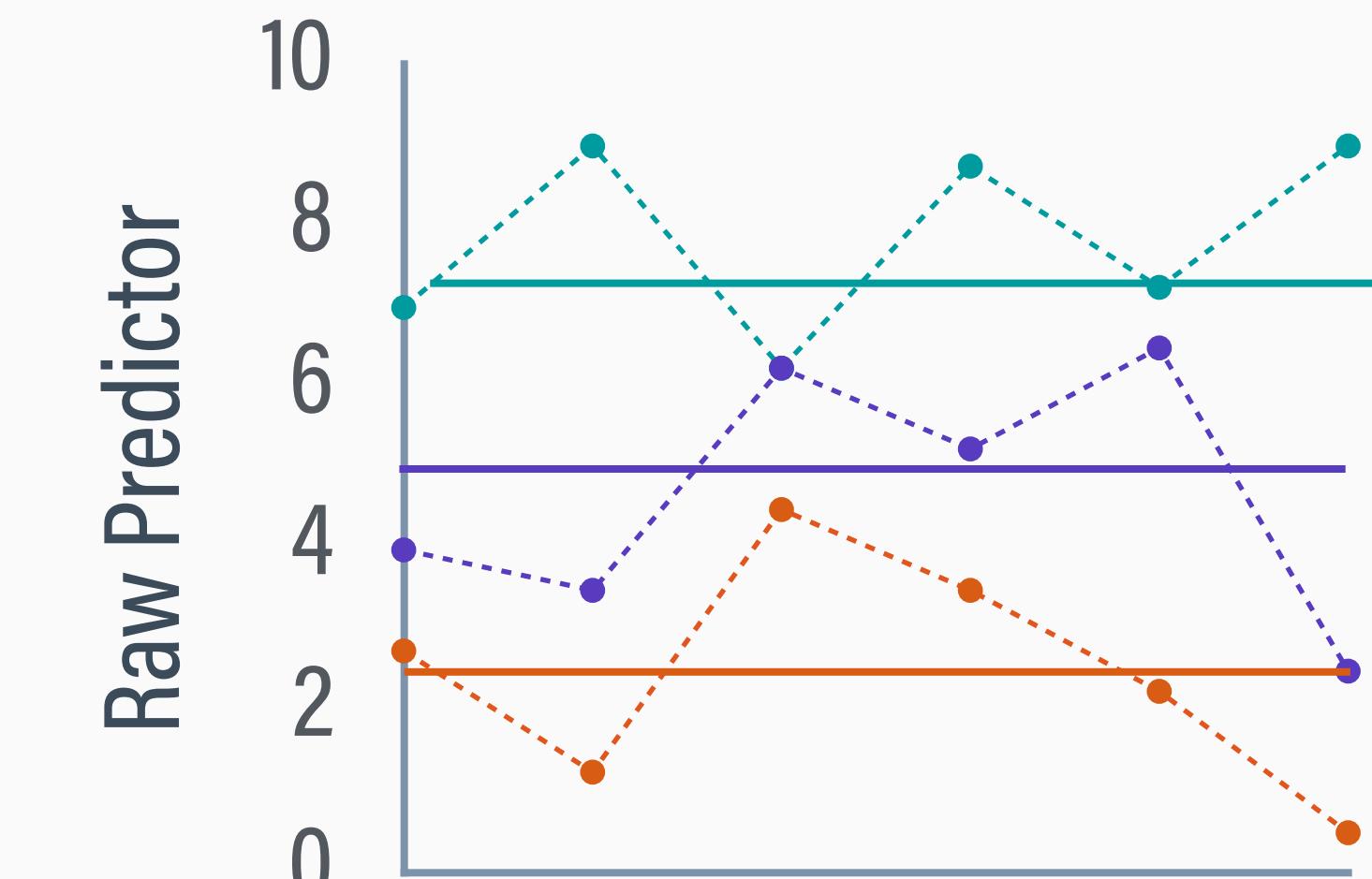
# CENTERING LEVEL-1 PREDICTORS

- Pure within-cluster predictors are created by deviating (centering) each person's score at its level-2 team mean

$$lmx_{ij}^w = lmx_{ij} - lmx_j^b$$

$$\text{empower}_{ij}^w = \text{empower}_{ij} - \text{empower}_j^b$$

- The resulting deviation scores contain only within-team (level-1) variation



# BLIMP SCRIPT 7.1 EXCERPT

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$$lmx_{ij}^w = lmx_{ij} - lmx_j^b$$

$$empower_{ij}^w = empower_{ij} - empower_j^b$$

**CLUSTERID:** Team;

**LATENT:** Team = LMX\_b Empower\_b JobSat\_b;

**MODEL:**

LMX\_w = LMX - LMX\_b; # text substitution alias to simplify the equations

Empower\_w = Empower - Empower\_b; # text substitution alias to simplify the equations

level2:

LMX\_b ~ intercept;

Empower\_b ~ intercept;

JobSat\_b ~ intercept;

level1:

LMX ~ intercept@LMX\_b;

Empower ~ intercept@Empower\_b;

JobSat ~ intercept@JobSat\_b;

# WITHIN-CLUSTER MEDIATION MODELS

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- Level-1 slopes represent “pure’ within-team associations

$$lmx_{ij} = lmx_j^b + \varepsilon_{ij}(lmx)$$

$$\text{empower}_{ij} = \text{empower}_j^b + \alpha^w(lmx_{ij}^w) + \varepsilon_{ij}(\text{empower})$$

$$\text{jobsat}_{ij} = \text{jobsat}_j^b + \tau'^w(lmx_{ij}^w) + \beta^w(\text{empower}_{ij}^w) + \varepsilon_{ij}(\text{jobsat})$$

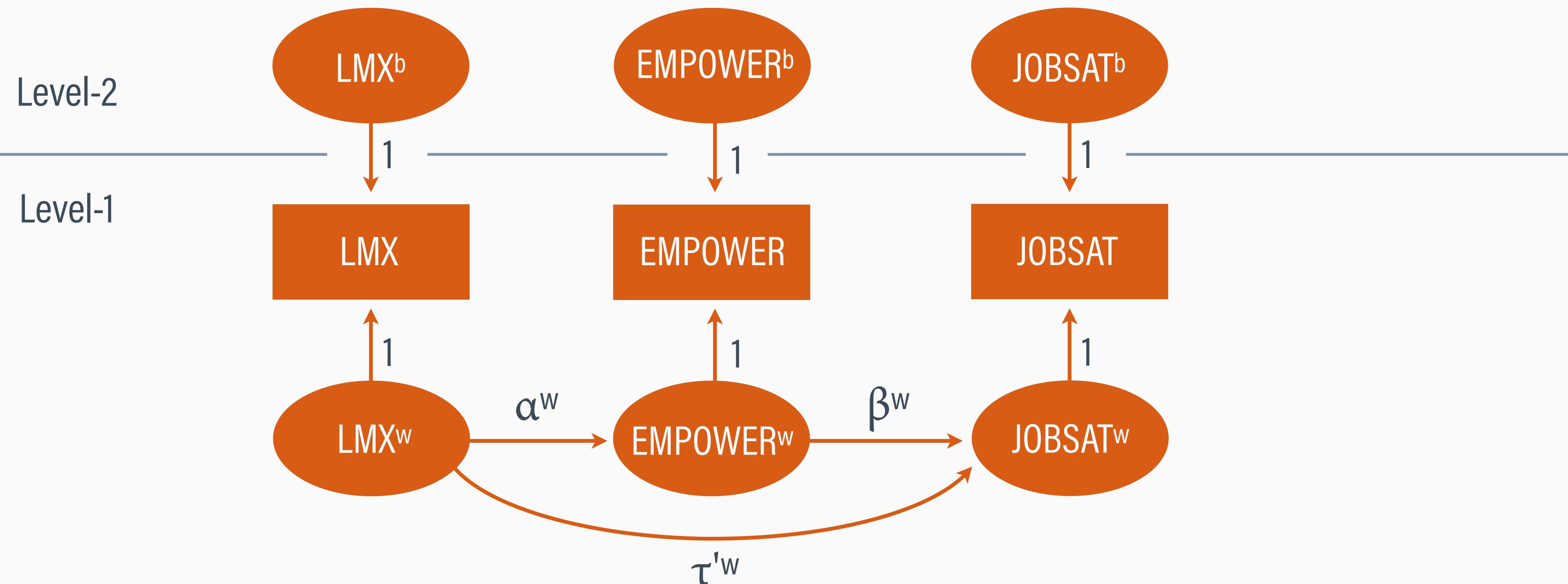
- The random intercepts (team averages) vary across teams

# PATH DIAGRAM

$$lmx_{ij} = lmx_j^b + \varepsilon_{ij}(lmx)$$

$$\text{empower}_{ij} = \text{empower}_j^b + \alpha^w(lmx_{ij}^w) + \varepsilon_{ij}(\text{empower})$$

$$\text{jobsat}_{ij} = \text{jobsat}_j^b + \tau'^w(lmx_{ij}^w) + \beta^w(\text{empower}_{ij}^w) + \varepsilon_{ij}(\text{jobsat})$$



# BLIMP SCRIPT 7.1 EXCERPT

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**CLUSTERID:** Team;

**LATENT:** Team = LMX\_b Empower\_b JobSat\_b;

**MODEL:**

LMX\_w = LMX - LMX\_b; # text substitution alias to simplify the equations

Empower\_w = Empower - Empower\_b; # text substitution alias to simplify the equations

**level2:**

...

**level1:**

LMX ~ intercept@LMX\_b;

Empower ~ intercept@Empower\_b LMX\_w@apath\_w; # @ labels the within-cluster slopes

JobSat ~ intercept@JobSat\_b LMX\_w@tpath\_w Empower\_w@bpath\_w; # @ labels the within-cluster slopes

$$lmx_{ij} = lmx_j^b + \varepsilon_{ij}(lmx)$$

$$empower_{ij} = empower_j^b + \alpha^w(lmx_{ij}^w) + \varepsilon_{ij}(empower)$$

$$jobsat_{ij} = jobsat_j^b + \tau'^w(lmx_{ij}^w) + \beta^w(empower_{ij}^w) + \varepsilon_{ij}(jobsat)$$

# BETWEEN-CLUSTER MEDIATION MODELS

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- Level-1 slopes represent “pure’ within-team associations

$$lmx_j^b = \beta_0(lmx) + u_{0j}(lmx)$$

$$empower_j^b = \beta_0(empower) + \alpha^b(lmx_j^b) + u_{0j}(empower)$$

$$jobsat_j^b = \beta_0(jobsat) + \tau'^b(lmx_j^b) + \beta^b(empower_j^b) + u_{0j}(jobsat)$$

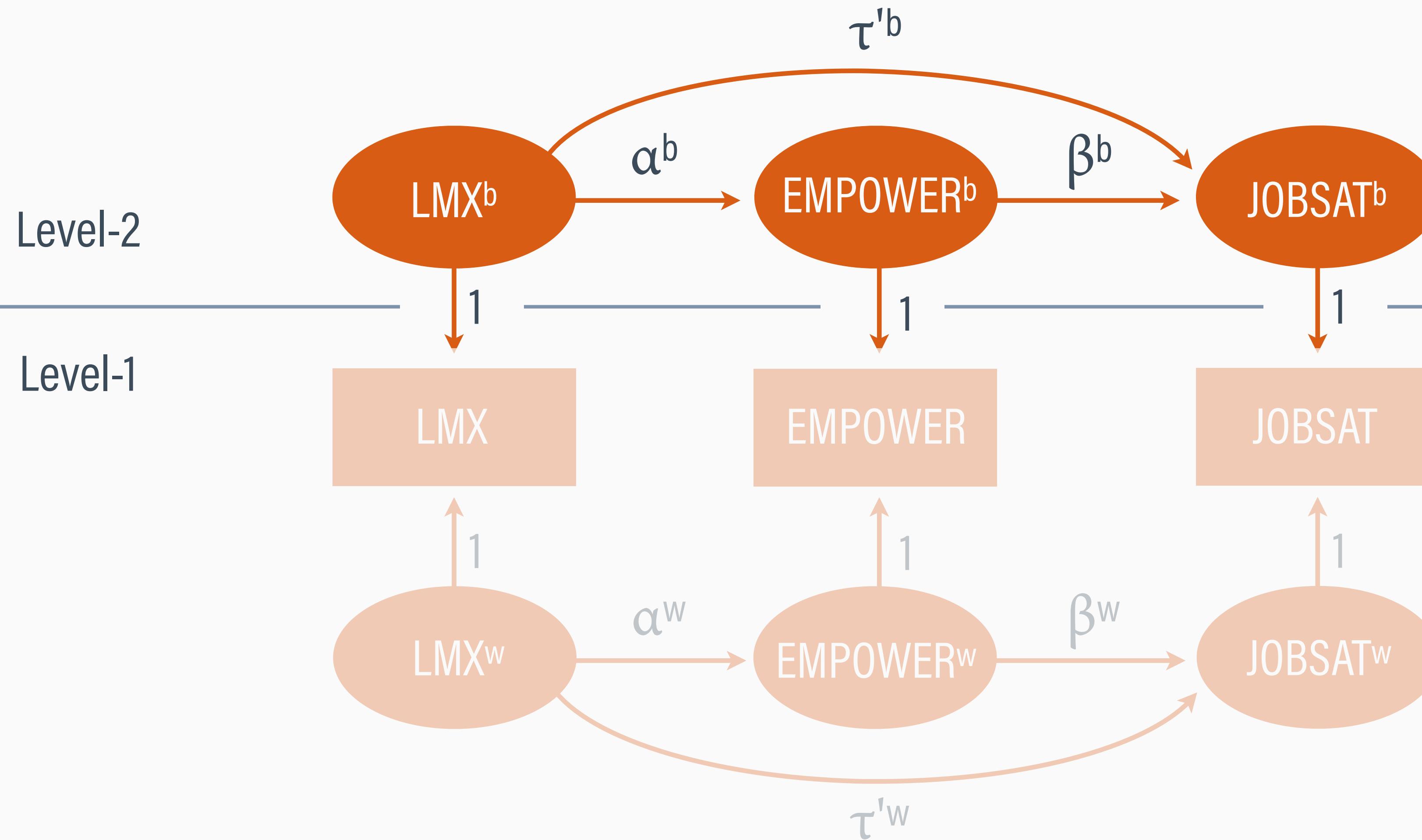
- The random intercepts (team averages) vary across teams

# PATH DIAGRAM

$$lmx_j^b = \beta_0(lmx) + u_{0j}(lmx)$$

$$empower_j^b = \beta_0(empower) + \alpha^b(lmx_j^b) + u_{0j}(empower)$$

$$jobsat_j^b = \beta_0(jobsat) + \tau'^b(lmx_j^b) + \beta^b(empower_j^b) + u_{0j}(jobsat)$$



# BLIMP SCRIPT 7.1 EXCERPT

---

**CLUSTERID:** Team;

**LATENT:** Team = LMX\_b Empower\_b JobSat\_b;

**MODEL:**

...

**level2:**

LMX\_b ~ intercept;

Empower\_b ~ intercept LMX\_b@apath\_b; # @ labels the between-cluster slopes

JobSat\_b ~ intercept LMX\_b@tpath\_b Empower\_b@bpath\_b; # @ labels the between-cluster slopes

**level1:**

...

$$lmx_j^b = \beta_0(lmx) + u_{0j}(lmx)$$

$$empower_j^b = \beta_0(empower) + \alpha^b(lmx_j^b) + u_{0j}(empower)$$

$$jobsat_j^b = \beta_0(jobsat) + \tau'^b(lmx_j^b) + \beta^b(empower_j^b) + u_{0j}(jobsat)$$

# INDIRECT EFFECT ESTIMATES

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- An indirect effect is the product of its component slopes

$$\text{Between-cluster indirect effect} = \alpha^b \times \beta^b$$

$$\text{Within-cluster indirect effect} = \alpha^w \times \beta^w$$

- The indirect effect is not an estimated parameter, but rather a deterministic function of two estimated slopes
- MCMC produces a distribution of the indirect effect

# BLIMP SCRIPT 7.1 EXCERPT

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## MODEL:

```
LMX_w = LMX - LMX_b; # text substitution alias to simplify the equations  
Empower_w = Empower - Empower_b;  
level2: # arbitrary label that groups summary tables for a set of models  
LMX_b ~ intercept;  
Empower_b ~ intercept LMX_b@apath_b; # @ labels the between-cluster slopes  
JobSat_b ~ intercept LMX_b@tpath_b Empower_b@bpath_b;  
level1: # arbitrary label that groups summary tables for a set of models  
LMX ~ intercept@LMX_b;  
Empower ~ intercept@Empower_b LMX_w@apath_w; # @ labels the within-cluster slopes  
JobSat ~ intercept@JobSat_b LMX_w@tpath_w Empower_w@bpath_w;
```

## PARAMETERS:

```
ab_w = apath_w * bpath_w; # use slope labels to define the indirect effect estimates  
ab_b = apath_b * bpath_b;
```

# RBLIMP SCRIPT 7 (MODEL 1) EXCERPT

```
model1 <- rblimp(...  
  latent = 'Team = LMX_b Empower_b JobSat_b',  
  model = '  
    LMX_w = LMX - LMX_b; # text substitution alias to simplify the equations  
    Empower_w = Empower - Empower_b;  
    level2: # arbitrary label that groups summary tables for a set of models  
    LMX_b ~ intercept;  
    Empower_b ~ intercept LMX_b@apath_b; # @ labels the between-cluster slopes  
    JobSat_b ~ intercept LMX_b@tpath_b Empower_b@bpath_b;  
    level1: # arbitrary label that groups summary tables for a set of models  
    LMX ~ intercept@LMX_b;  
    Empower ~ intercept@Empower_b LMX_w@apath_w; # @ labels the within-cluster slopes  
    JobSat ~ intercept@JobSat_b LMX_w@tpath_w Empower_w@bpath_w;',  
  parameters = '  
    ab_w = apath_w * bpath_w; # use slope labels to define the indirect effect estimates  
    ab_b = apath_b * bpath_b; ...)  
output(model1)  
plot_posterior(model1, 'ab_w') # plot distribution of indirect effect parameter  
plot_posterior(model1, 'ab_b')
```

# WITHIN-CLUSTER $\alpha^w$ PATH

 = level-2 estimate  
 = level-1 estimate

Outcome Variable: Empower

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
Variances:							
Residual Var.	14.436	0.899	12.820	16.320	---	---	6508.903
<hr/>							
Coefficients:							
Empower_b	@ 1.000	---	---	---	---	---	---
LMX_w	<b>0.687</b>	0.059	0.570	0.801	135.816	0.000	5674.431
<hr/>							
Standardized Coefficients:							
LMX_w	0.453	0.033	0.385	0.515	186.307	0.000	4602.107
<hr/>							
Proportion Variance Explained							
by Coefficients	0.205	0.030	0.148	0.265	---	---	4523.272
by Residual Variation	0.795	0.030	0.735	0.852	---	---	4523.272

# WITHIN-CLUSTER $\beta^w$ AND $\tau'^w$ PATHS

 = level-2 estimate  
 = level-1 estimate

Outcome Variable: JobSat

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
Variances:							
Residual Var.	1.173	0.071	1.043	1.322	---	---	6223.732
<hr/>							
Coefficients:							
JobSat_b	@ 1.000	---	---	---	---	---	---
LMX_w	<b>0.161</b>	0.019	0.124	0.198	72.366	0.000	8556.982
Empower_w	<b>0.019</b>	0.012	-0.005	0.044	2.486	0.115	8322.604
<hr/>							
Standardized Coefficients:							
LMX_w	0.380	0.041	0.297	0.458	84.752	0.000	8271.061
Empower_w	0.069	0.044	-0.016	0.155	2.502	0.114	8480.419
<hr/>							
Proportion Variance Explained							
by Coefficients	0.175	0.029	0.120	0.233	---	---	5032.537
by Residual Variation	0.825	0.029	0.767	0.880	---	---	5032.537

# INTERPRETATIONS

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- $\alpha^w = 0.69$  is the expected empowerment difference between two people *from the same team* with LMX scores that differ by one point
- $\beta^w = 0.02$  is the expected job satisfaction difference between two people from the same team with empowerment scores that differ by one point, holding constant LMX at any value

# BETWEEN-CLUSTER $\alpha^b$ PATH

□ = level-2 estimate  
□ = level-1 estimate

Latent Variable: Empower\_b

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
Variances:							
Residual Var.	2.400	0.832	1.018	4.255	---	---	542.191
Coefficients:							
Intercept	29.167	3.379	23.373	36.720	75.607	0.000	522.201
LMX_b	-0.057	0.351	-0.846	0.546	0.053	0.817	520.579
Standardized Coefficients:							
LMX_b	-0.040	0.226	-0.520	0.353	0.056	0.813	477.866
Proportion Variance Explained							
by Coefficients	0.024	0.077	0.000	0.273	---	---	498.597
by Residual Variation	0.976	0.077	0.727	1.000	---	---	498.597

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# BETWEEN-CLUSTER $\beta^b$ AND $\tau'^b$ PATHS

 = level-2 estimate  
 = level-1 estimate

Latent Variable: JobSat\_b

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
Variances:							
Residual Var.	0.059	0.044	0.003	0.168	---	---	239.018
<hr/>							
Coefficients:							
Intercept	-2.992	2.347	-9.284	0.381	2.021	0.155	196.419
LMX_b	<b>0.205</b>	0.091	0.053	0.414	5.423	0.020	345.646
Empower_b	<b>0.178</b>	0.066	0.078	0.344	7.973	0.005	195.484
<hr/>							
Standardized Coefficients:							
LMX_b	0.514	0.184	0.145	0.878	7.743	0.005	414.852
Empower_b	0.649	0.165	0.293	0.949	15.207	0.000	230.355
<hr/>							
Proportion Variance Explained							
by Coefficients	0.669	0.200	0.243	0.984	---	---	186.171
by Residual Variation	0.331	0.200	0.016	0.757	---	---	186.171

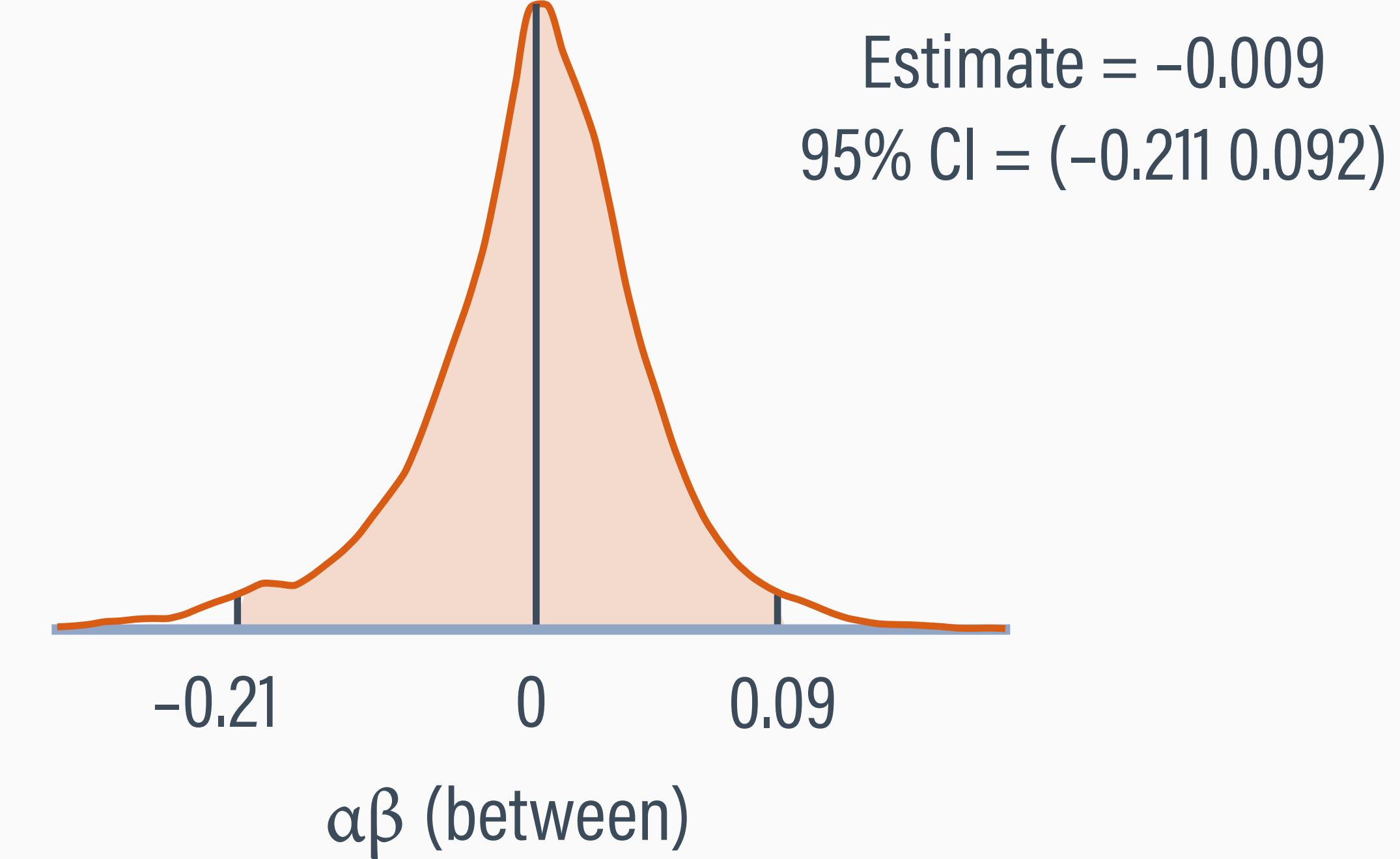
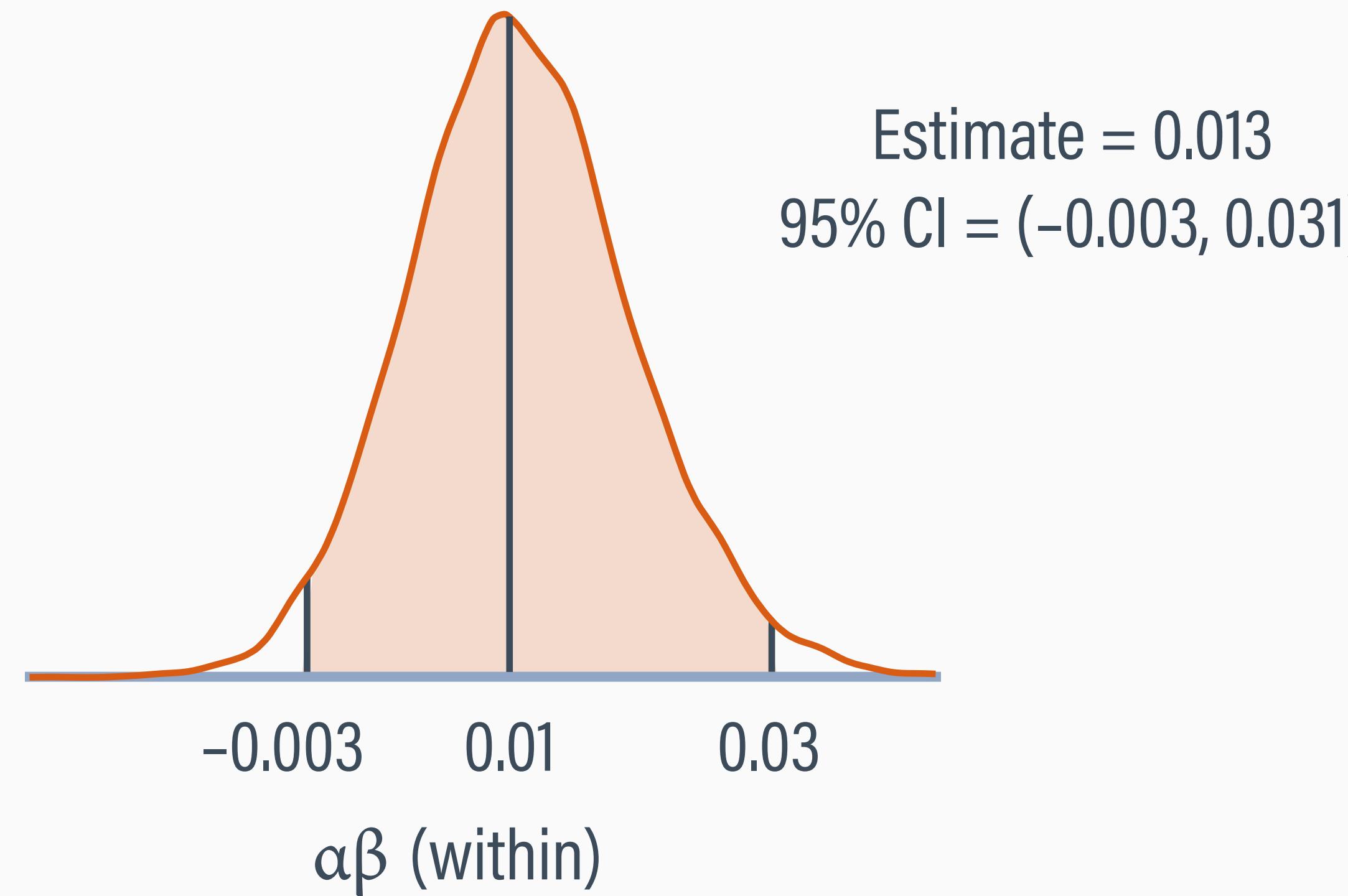
# INTERPRETATIONS

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- $\alpha^b = 0.06$  is the expected empowerment mean difference between two teams with average LMX values that differ by one point, controlling for team-average LMX
- $\beta^b = 0.18$  is the expected job satisfaction mean difference between two teams with average empowerment values that differ by one point, controlling for team-average LMX

# DISTRIBUTIONS OF INDIRECT EFFECTS

- Indirect effects are computed at each MCMC iteration, producing a distribution of plausible mediated effects at each level



# INDIRECT EFFECTS OUTPUT

□ = level-2 estimate

■ = level-1 estimate

GENERATED PARAMETERS:

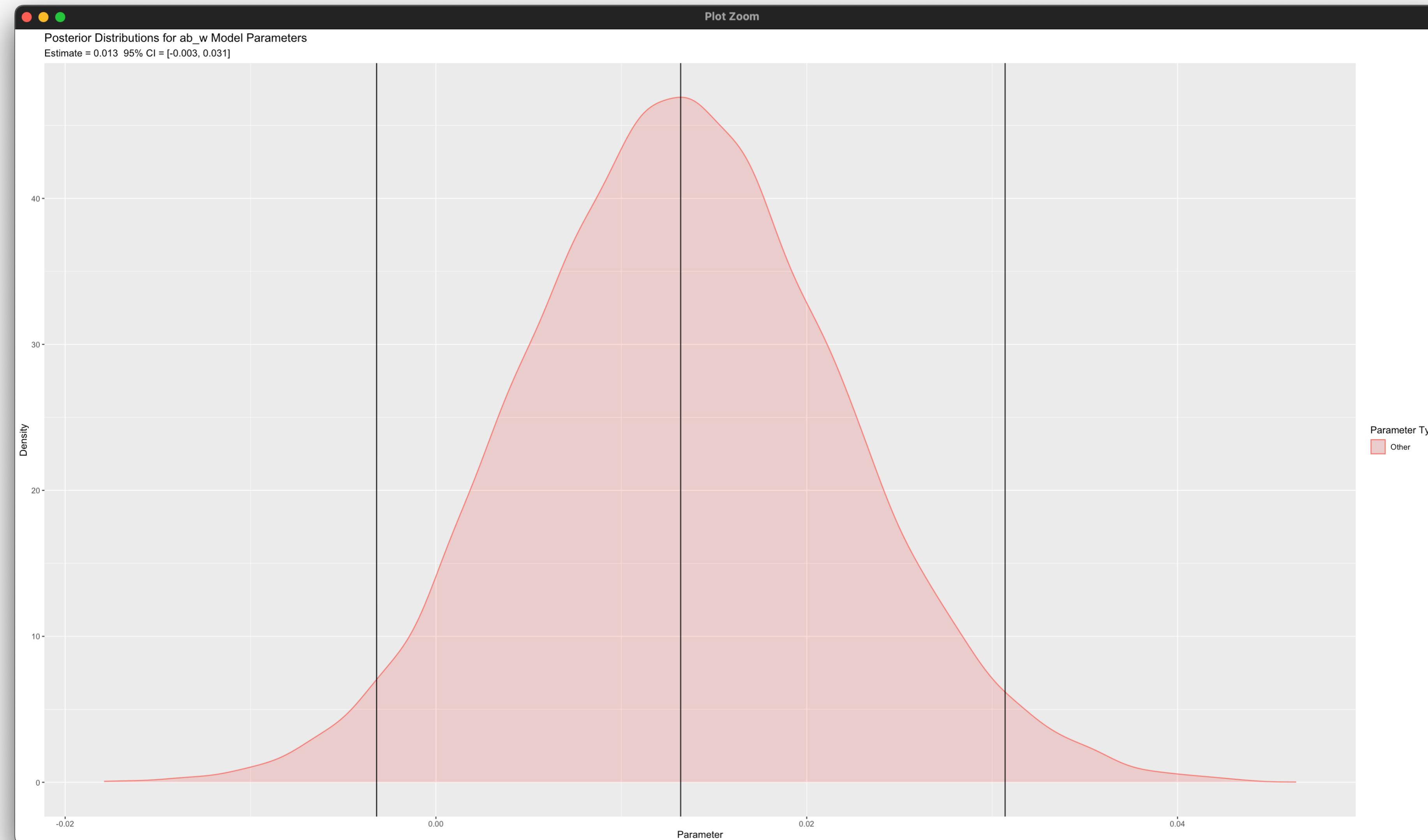
Standard test statistics are inappropriate  
for evaluating mediated effects!

Summaries based on 20000 iterations using 2 chains.

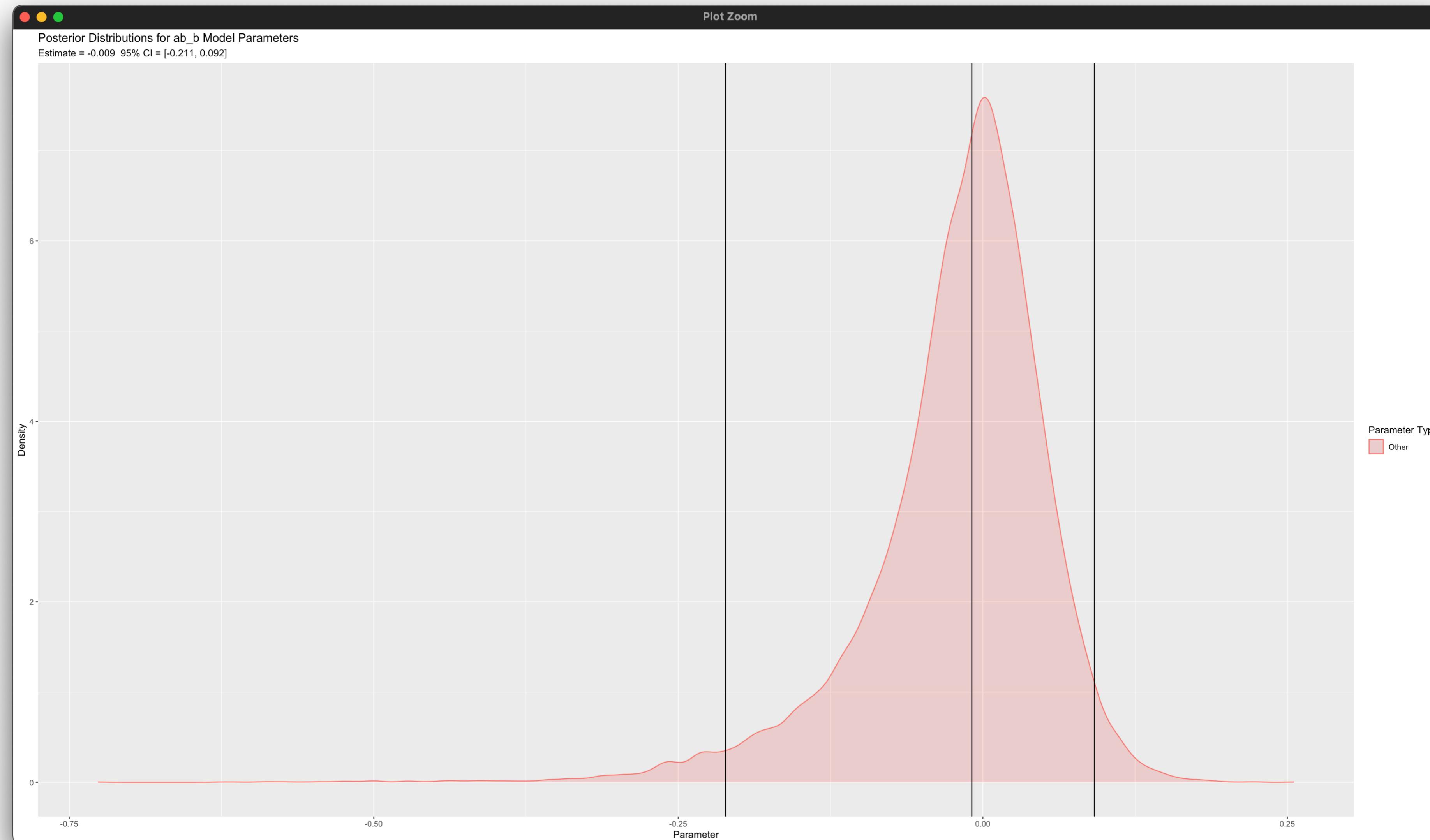
NOTE: Estimate column based on posterior median.

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
ab_w	0.013	0.009	-0.003	0.031	2.4	.120	8417.097
ab_b	-0.009	0.075	-0.211	0.092	0.0	.776	368.719

# DISTRIBUTION OF $\alpha\beta^w$ (RBLIMP ONLY)



# DISTRIBUTION OF $\alpha\beta^b$ (RBLIMP ONLY)



# INTERPRETATIONS

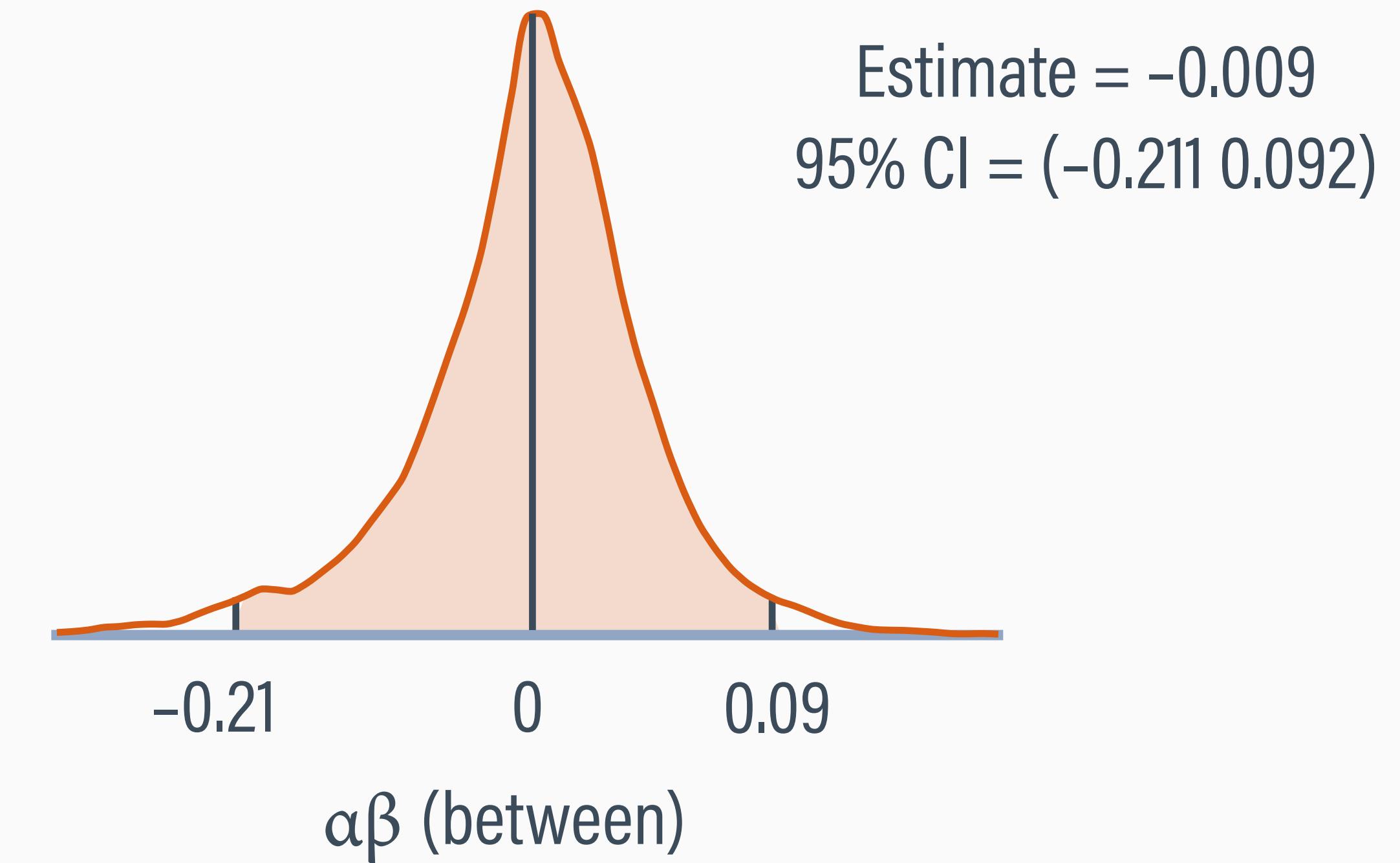
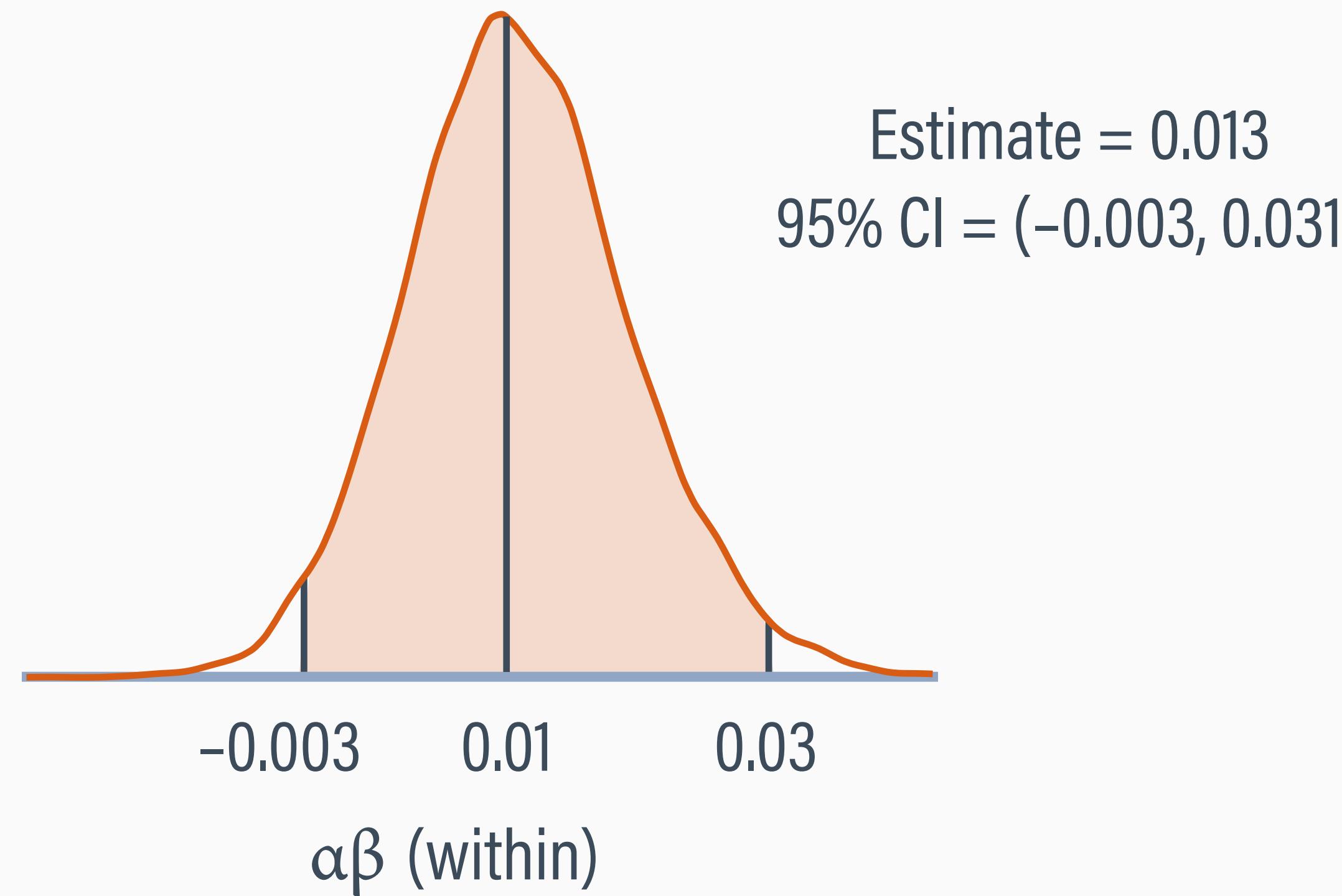
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- $\alpha\beta^w = .013$  is the effect of a one-point within-team difference on LMX that gets transmitted to job satisfaction via a one-point within-team difference in empowerment (the mediator)
- $\alpha\beta^b = -0.01$  is the effect of a one-point between-team mean difference on LMX that gets transmitted to job satisfaction via a one-point mean difference in empowerment (the mediator)

# 95% ASYMMETRIC INTERVALS

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- Zero is inside both 95% intervals (just barely at level-1), implying that the data could have originated from a population with no mediation



# OUTLINE

- 1 Mediation Overview
- 2 1-1-1 Model With Random Intercepts
- 3 1-1-1 Model With Random Slopes
- 4 Moderation on the  $\alpha$  or  $\beta$  paths

# WITHIN-CLUSTER MEDIATION MODELS

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- Level-1 slopes represent “pure’ within-team associations

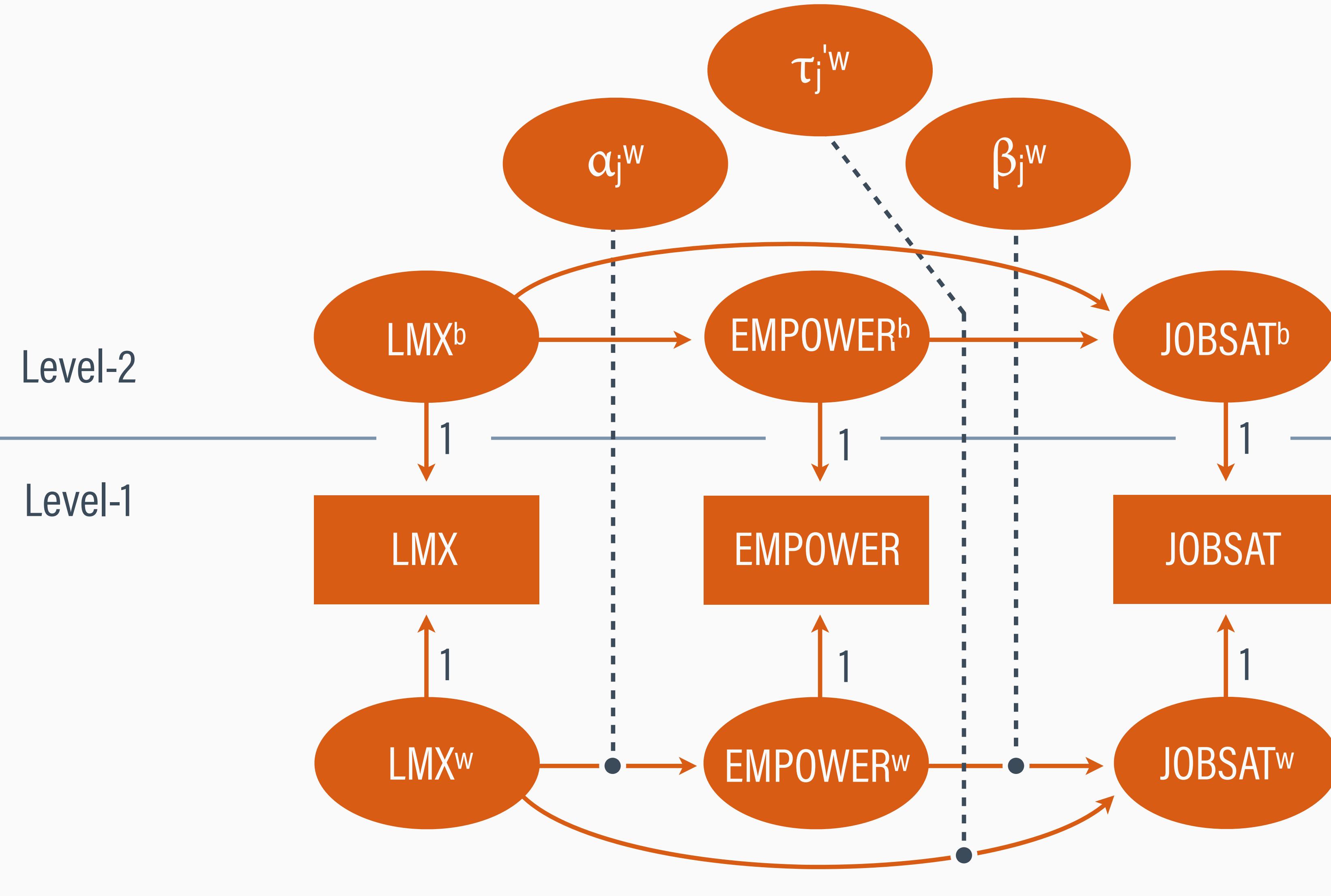
$$lmx_{ij} = lmx_j^b + \varepsilon_{ij}(lmx)$$

$$\text{empower}_{ij} = \text{empower}_j^b + \alpha_j^w(lmx_{ij}^w) + \varepsilon_{ij}(\text{empower})$$

$$\text{jobsat}_{ij} = \text{jobsat}_j^b + \tau_j^w(lmx_{ij}^w) + \beta_j^w(\text{empower}_{ij}^w) + \varepsilon_{ij}(\text{jobsat})$$

- Intercepts (team averages) and slopes vary across teams

# PATH DIAGRAM



# INDIRECT EFFECT ESTIMATES

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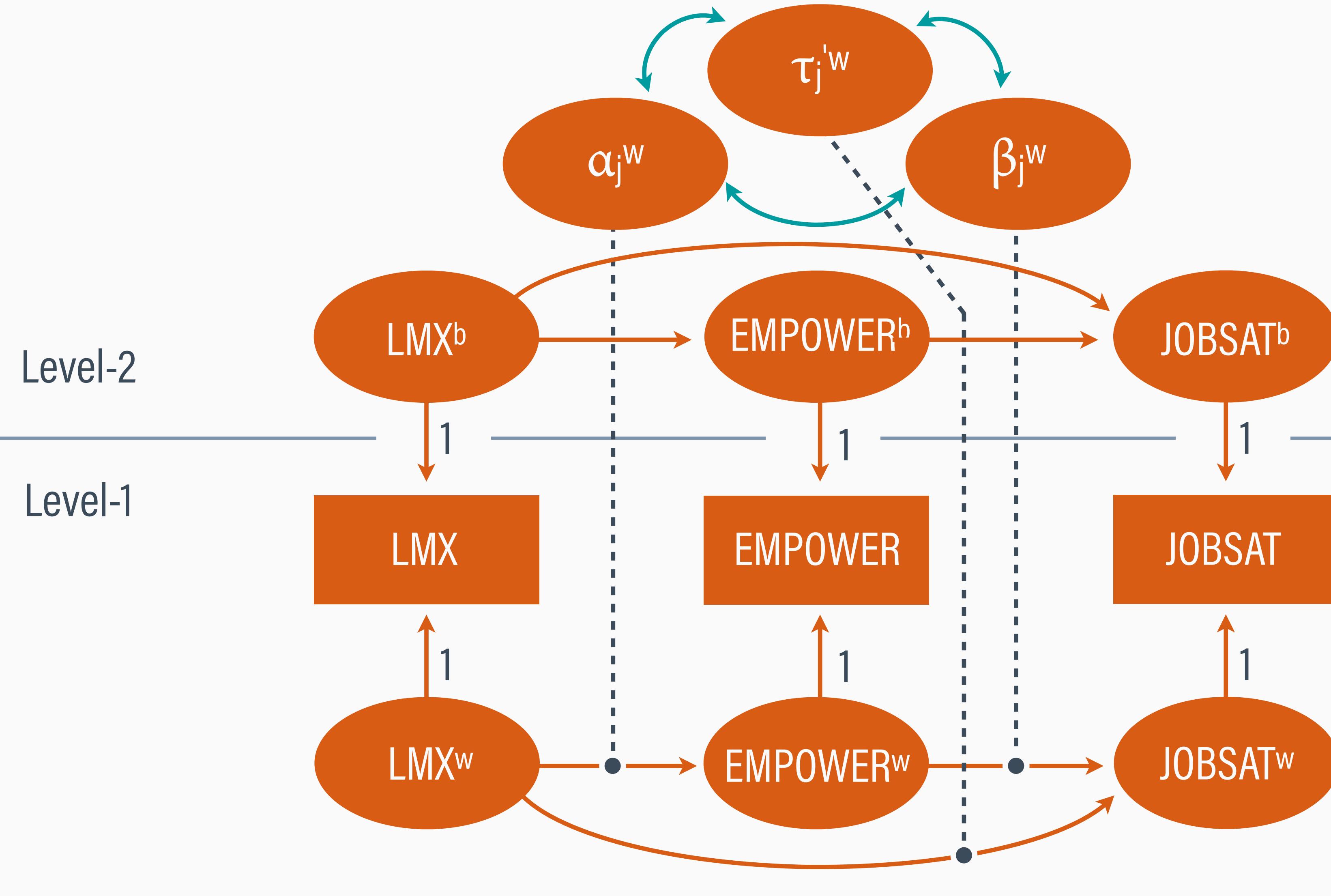
- In a model with random slopes, the within-cluster indirect effect equals the product of  $\alpha^w$  and  $\beta^w$  *plus* the covariance (unstandardized correlation) between the random slopes

$$\text{Between-cluster indirect effect} = \alpha^b \times \beta^b$$

$$\text{Within-cluster indirect effect} = \alpha^w \times \beta^w + \text{cov}(\alpha^w, \beta^w)$$

- Correlating slopes in a multilevel SEM is vital for obtaining unbiased indirect effects (Kenny, Korchmaros, & Bolger, 2003)

# PATH DIAGRAM



● = random slope

# BLIMP SCRIPT 7.2 EXCERPT

**LATENT:** Team = LMX\_b Empower\_b JobSat\_b apath\_w bpath\_w tpath\_w; # define random slope latent variables

**MODEL:**

...

level2:

LMX\_b ~ intercept;

Empower\_b ~ intercept LMX\_b@apath\_b;

JobSat\_b ~ intercept LMX\_b@tpath\_b Empower\_b@bpath\_b;

apath\_w ~ intercept@apathw\_mean; # random slope latent variables with their means labeled

bpath\_w ~ intercept@bpathw\_mean;

tpath\_w ~ intercept;

apath\_w ~~ bpath\_w@ab\_corr; # correlate random a and b paths and attach a label;

apath\_w bpath\_w ~~ tpath\_w; # correlate remaining random slopes

...

# BLIMP SCRIPT 7.2 EXCERPT

**LATENT:** Team = LMX\_b Empower\_b JobSat\_b apath\_w bpath\_w tpath\_w; # define random slope latent variables

**MODEL:**

```
...  
apath_w ~ intercept@apathw_mean;  
bpath_w ~ intercept@bpathw_mean;  
tpath_w ~ intercept;  
apath_w ~~ bpath_w@ab_corr; # correlate random a and b paths and attach a label;  
apath_w bpath_w ~~ tpath_w; # correlate remaining random slopes
```

**level1:**

```
LMX ~ intercept@LMX_b;
```

```
Empower ~ intercept@Empower_b LMX_w@apath_w; # @ sets the LMX_w slope to its level-2 latent variable
```

```
JobSat ~ intercept@JobSat_b LMX_w@tpath_w Empower_w@bpath_w; # @ sets slopes to their latent variables
```

$$\text{empower}_{ij} = \text{empower}_j^b + \alpha_j^w(\text{LMX}_{ij}^w) + \varepsilon_{ij}(\text{empower})$$

$$\text{jobsat}_{ij} = \text{jobsat}_j^b + \tau_j^w(\text{LMX}_{ij}^w) + \beta_j^w(\text{empower}_{ij}^w) + \varepsilon_{ij}(\text{jobsat})$$

# BLIMP SCRIPT 7.2 EXCERPT

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## MODEL:

```
...  
level2:  
LMX_b ~ intercept;  
Empower_b ~ intercept LMX_b@apath_b;  
JobSat_b ~ intercept LMX_b@tpath_b Empower_b@bpath_b;  
apath_w ~ intercept@apathw_mean;  
bpath_w ~ intercept@bpathw_mean;  
tpath_w ~ intercept;  
apath_w ~~ bpath_w@ab_corr; # correlate random a and b paths and attach a label;  
apath_w bpath_w ~~ tpath_w; # correlate remaining random slopes
```

...

## PARAMETERS:

```
ab_cov = ab_corr * sqrt(apath_w.totalvar * bpath_w.totalvar); # covariance between random slopes uses .totalvar to get the variance  
ab_w = apathw_mean * bpathw_mean + ab_cov;  
ab_b = apath_b * bpath_b;
```

# WITHIN-CLUSTER $\alpha^w$ PATH

 = level-2 estimate

 = level-1 estimate

Latent Variable: apath\_w

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
Variances:							
Residual Var.	0.182	0.077	0.068	0.367	---	---	689.181
<hr/>							
Coefficients:							
Intercept	0.662	0.073	0.515	0.803	81.727	0.000	1491.264
<hr/>							
Proportion Variance Explained							
by Coefficients	0.000	0.000	0.000	0.000	---	---	nan
by Residual Variation	1.000	0.000	1.000	1.000	---	---	nan

# WITHIN-CLUSTER $\beta^w$ PATH

 = level-2 estimate

 = level-1 estimate

Latent Variable: bpath\_w

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
Variances:							
Residual Var.	0.005	0.003	0.001	0.012	---	---	196.246
<hr/>							
Coefficients:							
Intercept	0.025	0.015	-0.005	0.053	2.730	0.098	348.833
<hr/>							
Proportion Variance Explained							
by Coefficients	0.000	0.000	0.000	0.000	---	---	nan
by Residual Variation	1.000	0.000	1.000	1.000	---	---	nan

# INTERPRETATIONS

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- $\alpha^w = 0.66$  is the expected empowerment difference between two people *from the same team* with LMX scores that differ by one point
- $\beta^w = 0.03$  is the expected job satisfaction difference between two people from the same team with empowerment scores that differ by one point, holding constant LMX at any value

# BETWEEN-CLUSTER $\alpha^b$ PATH

 = level-2 estimate  
 = level-1 estimate

Latent Variable: Empower\_b

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
Variances:							
Residual Var.	2.457	0.810	1.049	4.233	---	---	526.462
Coefficients:							
Intercept	28.583	3.322	22.984	36.210	75.351	0.000	593.906
LMX_b	<b>0.005</b>	0.346	-0.790	0.585	0.004	0.948	585.287
Standardized Coefficients:							
LMX_b	0.003	0.226	-0.515	0.377	0.005	0.945	423.151
Proportion Variance Explained							
by Coefficients	0.022	0.077	0.000	0.272	---	---	273.546
by Residual Variation	0.978	0.077	0.728	1.000	---	---	273.546

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# BETWEEN-CLUSTER $\beta^b$ AND $\tau'^b$ PATHS

 = level-2 estimate  
 = level-1 estimate

Latent Variable: JobSat\_b

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
Variances:							
Residual Var.	0.064	0.045	0.005	0.171	---	---	274.358
<hr/>							
Coefficients:							
Intercept	-2.843	2.350	-8.407	0.697	1.731	0.188	194.582
LMX_b	<b>0.199</b>	0.090	0.046	0.399	5.199	0.023	318.385
Empower_b	<b>0.173</b>	0.067	0.070	0.329	7.183	0.007	209.485
<hr/>							
Standardized Coefficients:							
LMX_b	0.501	0.187	0.121	0.851	7.063	0.008	325.075
Empower_b	0.628	0.167	0.277	0.912	13.785	0.000	277.072
<hr/>							
Proportion Variance Explained							
by Coefficients	0.661	0.206	0.205	0.974	---	---	240.927
by Residual Variation	0.339	0.206	0.026	0.795	---	---	240.927

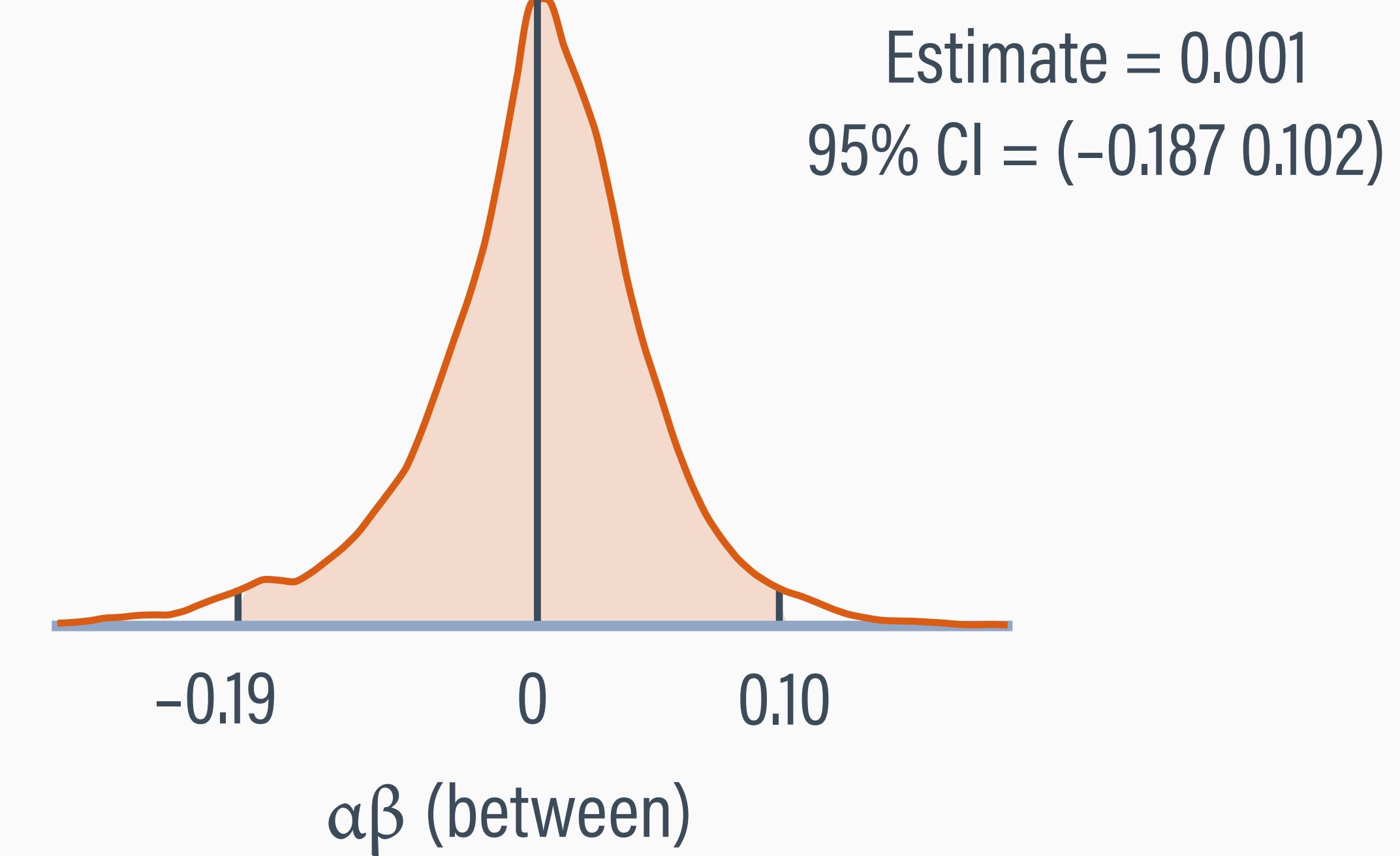
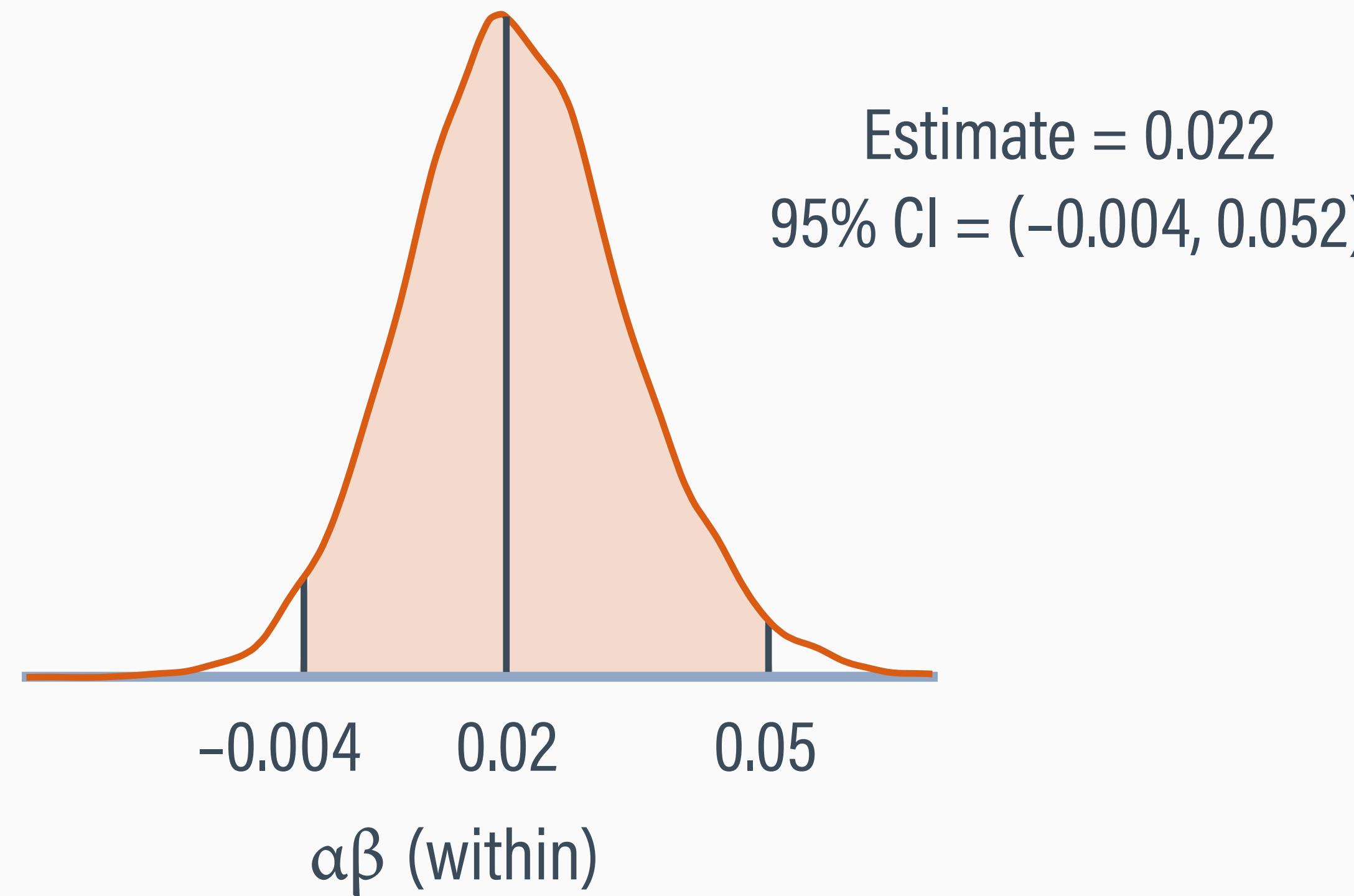
# INTERPRETATIONS

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- $\alpha^b = 0.005$  is the expected empowerment mean difference between two teams with average LMX values that differ by one point, controlling for team-average LMX
- $\beta^b = 0.17$  is the expected job satisfaction mean difference between two teams with average empowerment values that differ by one point, controlling for team-average LMX

# DISTRIBUTIONS OF INDIRECT EFFECTS

- Indirect effects are computed at each MCMC iteration, producing a distribution of plausible mediated effects at each level



# INDIRECT EFFECTS OUTPUT

■ = level-2 estimate  
□ = level-1 estimate

GENERATED PARAMETERS:

Standard test statistics are inappropriate  
for evaluating mediated effects!

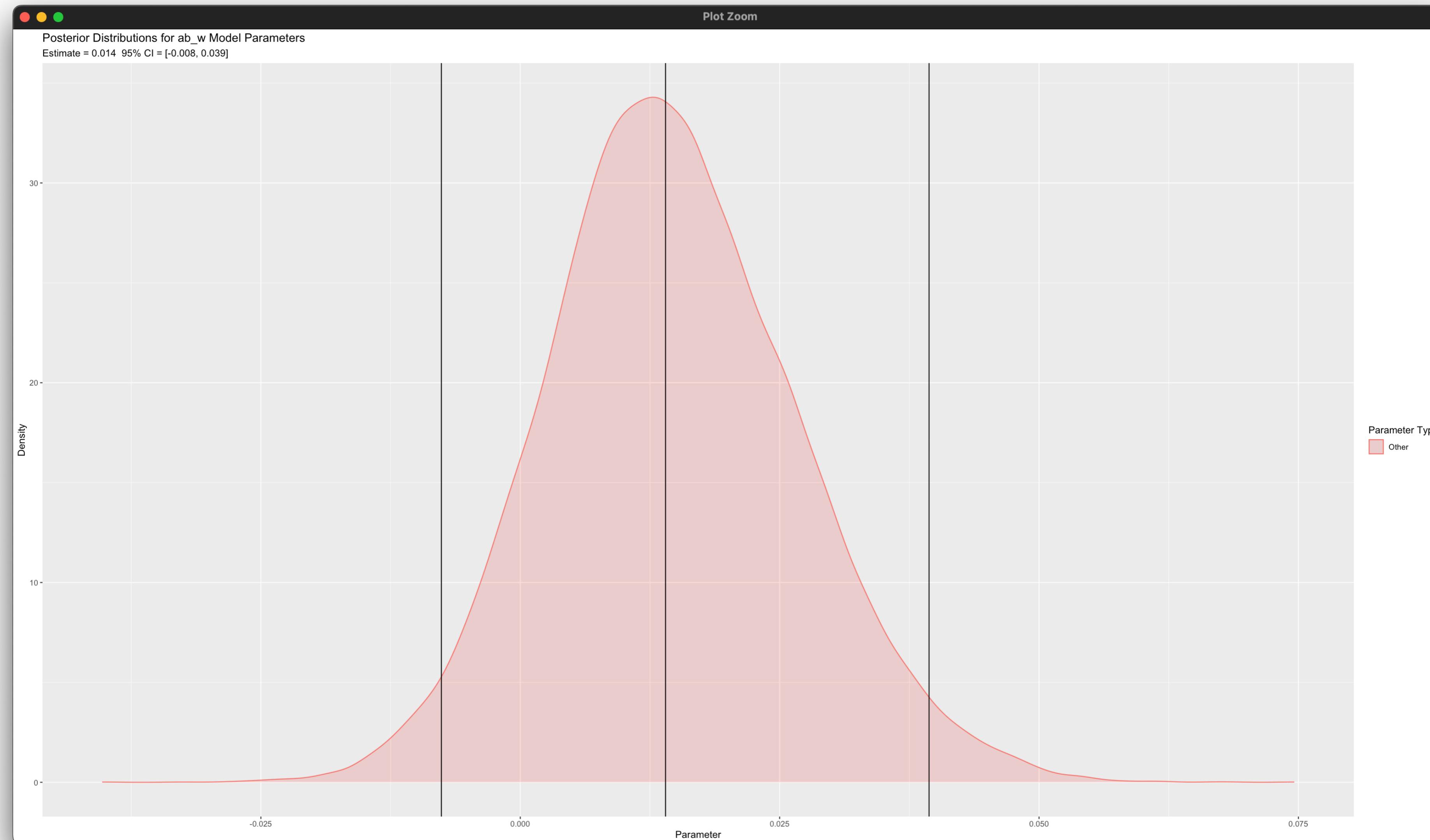
Summaries based on 20000 iterations using 2 chains.

NOTE: Estimate column based on posterior median.

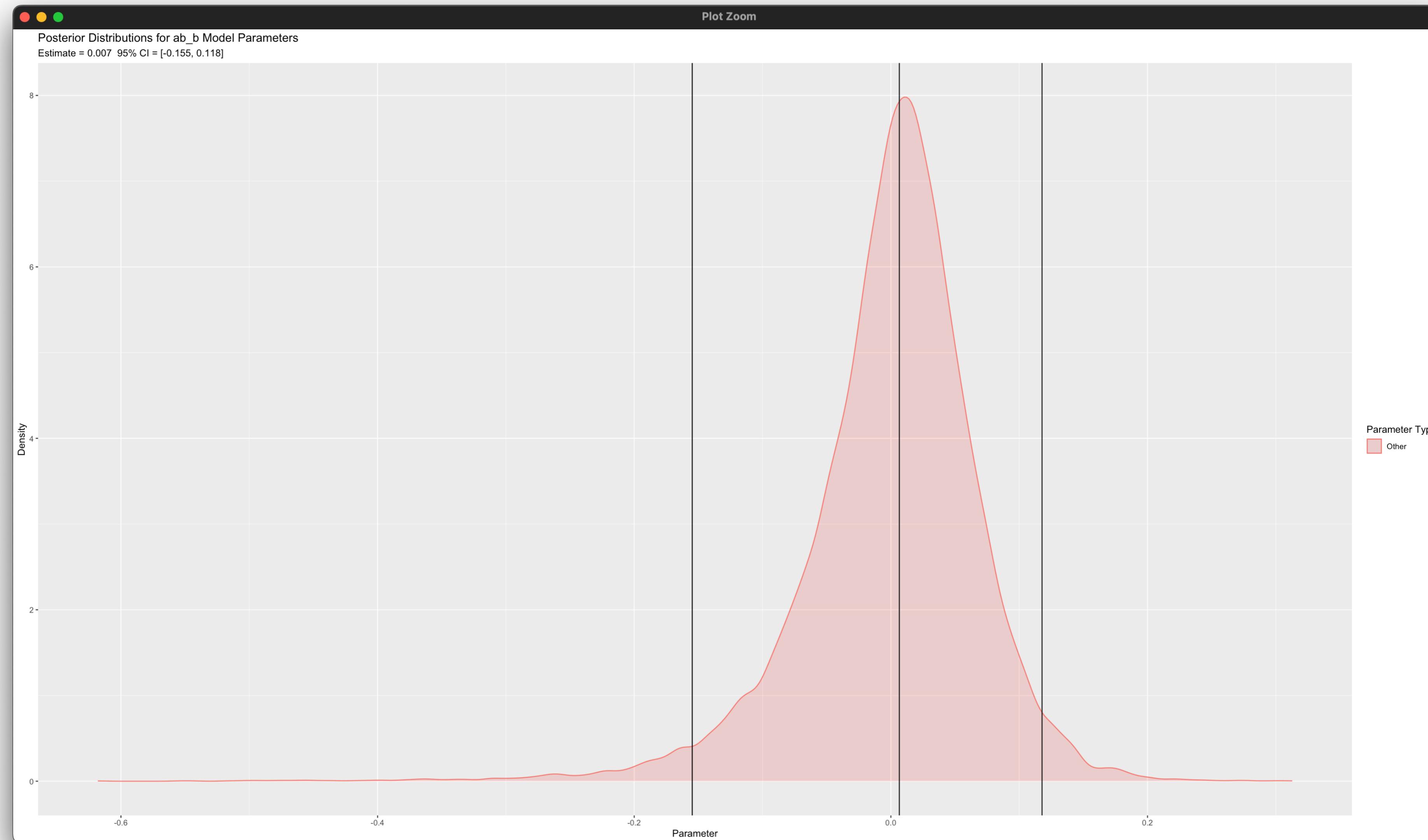
Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
ab_cov	0.007	0.010	-0.012	0.027	0.4	.494	320.266
ab_w	0.022	0.014	-0.004	0.052	2.6	.105	243.150
ab_b	0.001	0.073	-0.187	0.102	0.0	.895	261.393
<hr/>							



# DISTRIBUTION OF $\alpha\beta^w$ (RBLIMP ONLY)



# DISTRIBUTION OF $\alpha\beta^b$ (RBLIMP ONLY)



# INTERPRETATIONS

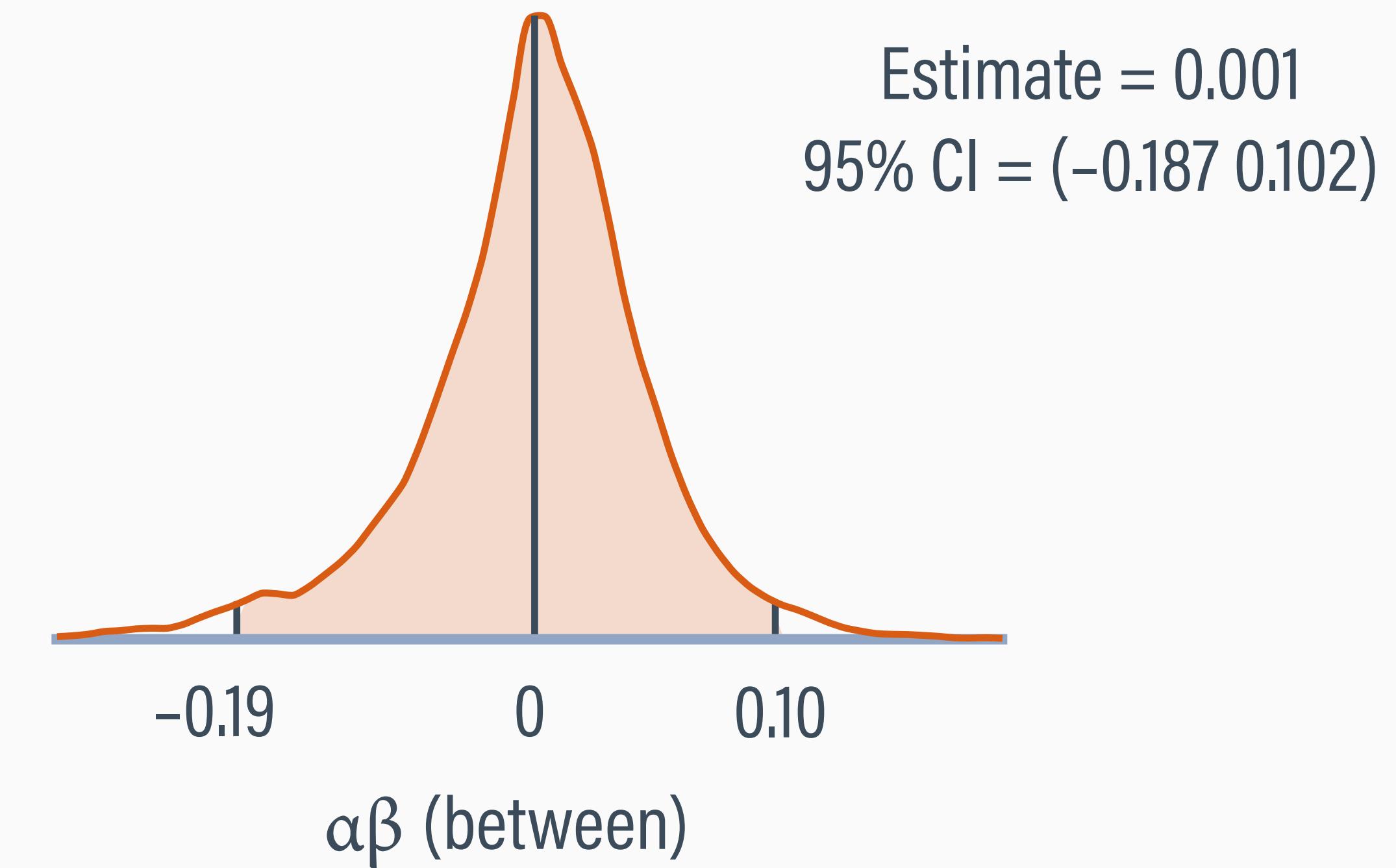
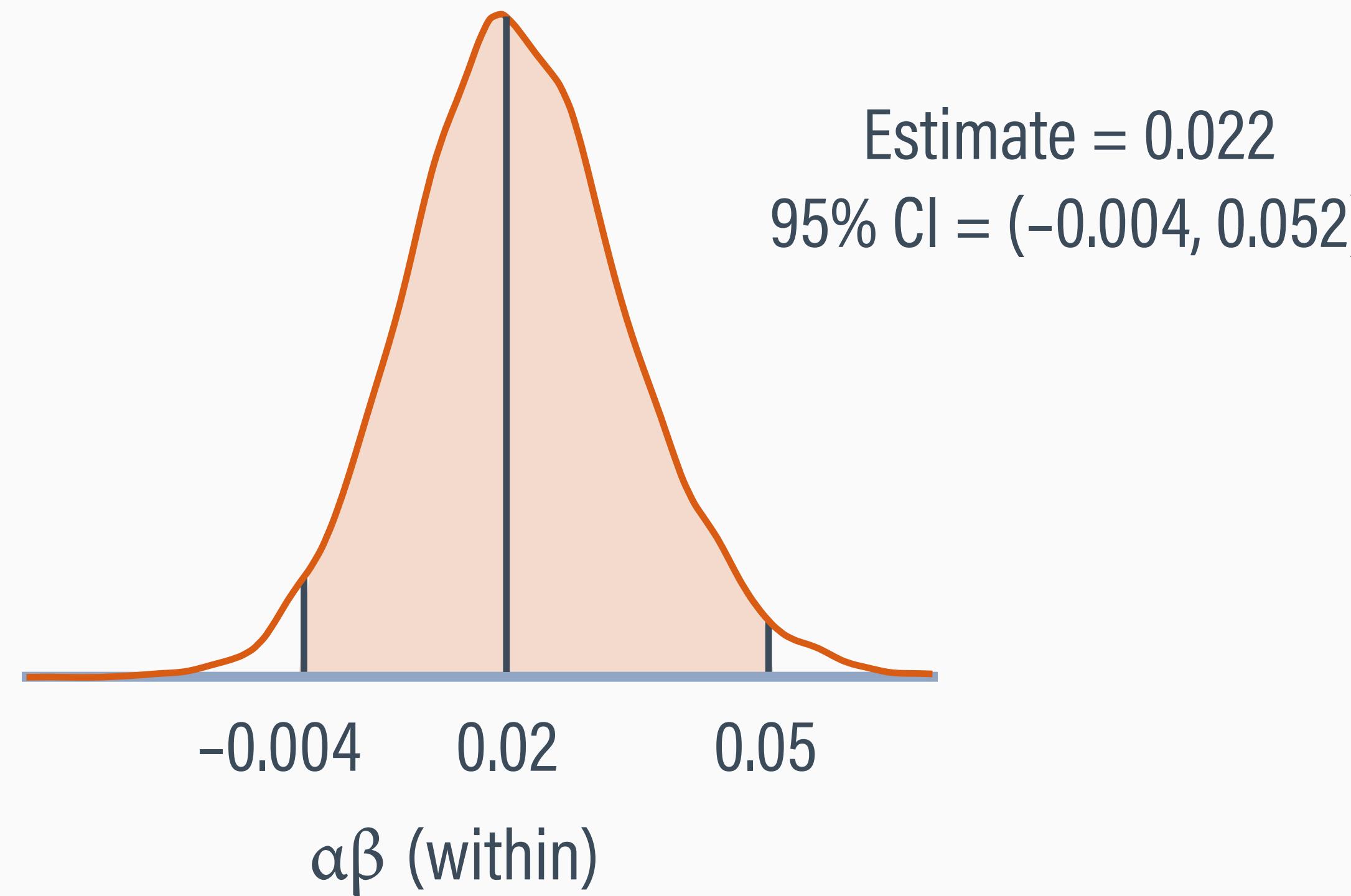
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- $\alpha\beta^w = .022$  is the effect of a one-point within-team difference on LMX that gets transmitted to job satisfaction via a one-point within-team difference in empowerment (the mediator)
- $\alpha\beta^b = 0.001$  is the effect of a one-point between-team mean difference on LMX that gets transmitted to job satisfaction via a one-point mean difference in empowerment (the mediator)

# 95% ASYMMETRIC INTERVALS

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- Zero is inside both 95% intervals (just barely at level-1), implying that the data could have originated from a population with no mediation

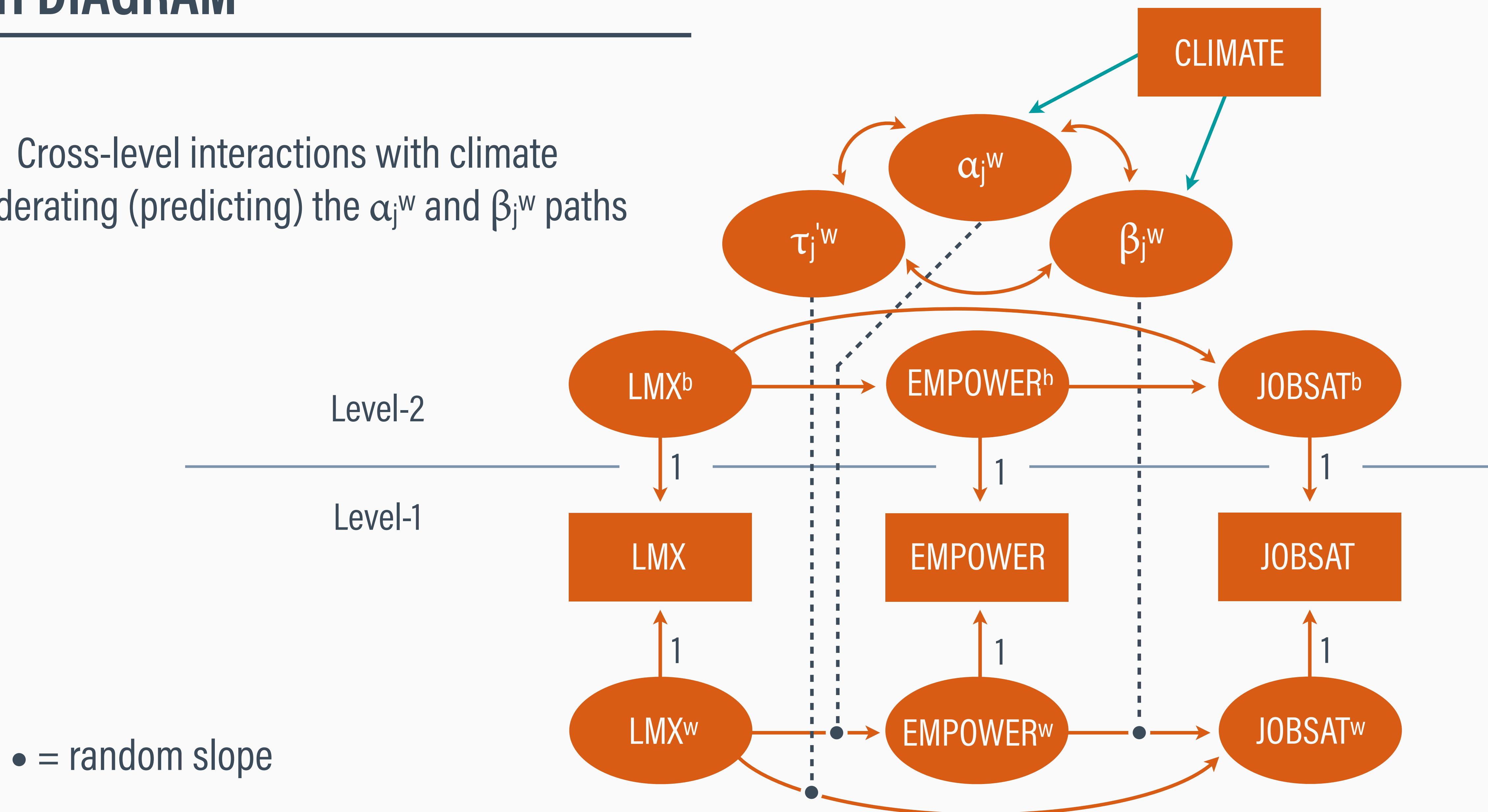


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- 4 Moderation on the  $\alpha$  or  $\beta$  paths

# PATH DIAGRAM

Cross-level interactions with climate  
moderating (predicting) the  $\alpha_j^w$  and  $\beta_j^w$  paths



# BLIMP SCRIPT 7.3 EXCERPT

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**LATENT:** Team = LMX\_b Empower\_b JobSat\_b apath\_w bpath\_w tpath\_w;

**CENTER:** grandmean = Climate;

**MODEL:**

...

**level2:**

Climate ~ intercept;

LMX\_b ~ intercept;

Empower\_b ~ intercept LMX\_b@apath\_b Climate;

JobSat\_b ~ intercept LMX\_b@tpath\_b Empower\_b@bpath\_b Climate;

apath\_w ~ intercept@apathw\_mean climate@apathw\_mod; # random slope predicted by level-2 moderator

bpath\_w ~ intercept@bpathw\_mean climatebpathw\_mod; # random slope predicted by level-2 moderator

tpath\_w ~ intercept;

apath\_w ~~ bpath\_w@ab\_corr; # correlate random a and b paths and attach a label;

apath\_w bpath\_w ~~ tpath\_w; # correlate remaining random slopes

...

# BLIMP SCRIPT 7.3 EXCERPT

---

Conditional mediated effects and different values of the moderator (team-level climate)

## PARAMETERS:

```
ab_cov = ab_corr * sqrt(apath_w.totalvar * bpath_w.totalvar); # covariance between random slopes  
a_hi = apathw_mean + apathw_mod*sqrt(climate.totalvar); # a path at different values of the moderator  
a_mean = apathw_mean;  
a_lo = apathw_mean - apathw_mod*sqrt(climate.totalvar);  
b_hi = bpathw_mean + bpathw_mod*sqrt(climate.totalvar); # b path at different values of the moderator  
b_mean = bpathw_mean;  
b_lo = bpathw_mean - bpathw_mod*sqrt(climate.totalvar);  
ab_w_hi = a_hi*b_hi + ab_cov; # within-cluster mediated effect at different values of the moderator  
ab_w_mean = a_mean*b_mean + ab_cov;  
ab_w_lo = a_lo*b_lo + ab_cov;  
ab_b = apath_b*bpath_b; # between-cluster mediated effect
```

# INDIRECT EFFECTS OUTPUT

■ = level-2 estimate

□ = level-1 estimate

GENERATED PARAMETERS:

Summaries based on 20000 iterations using 2 chains.

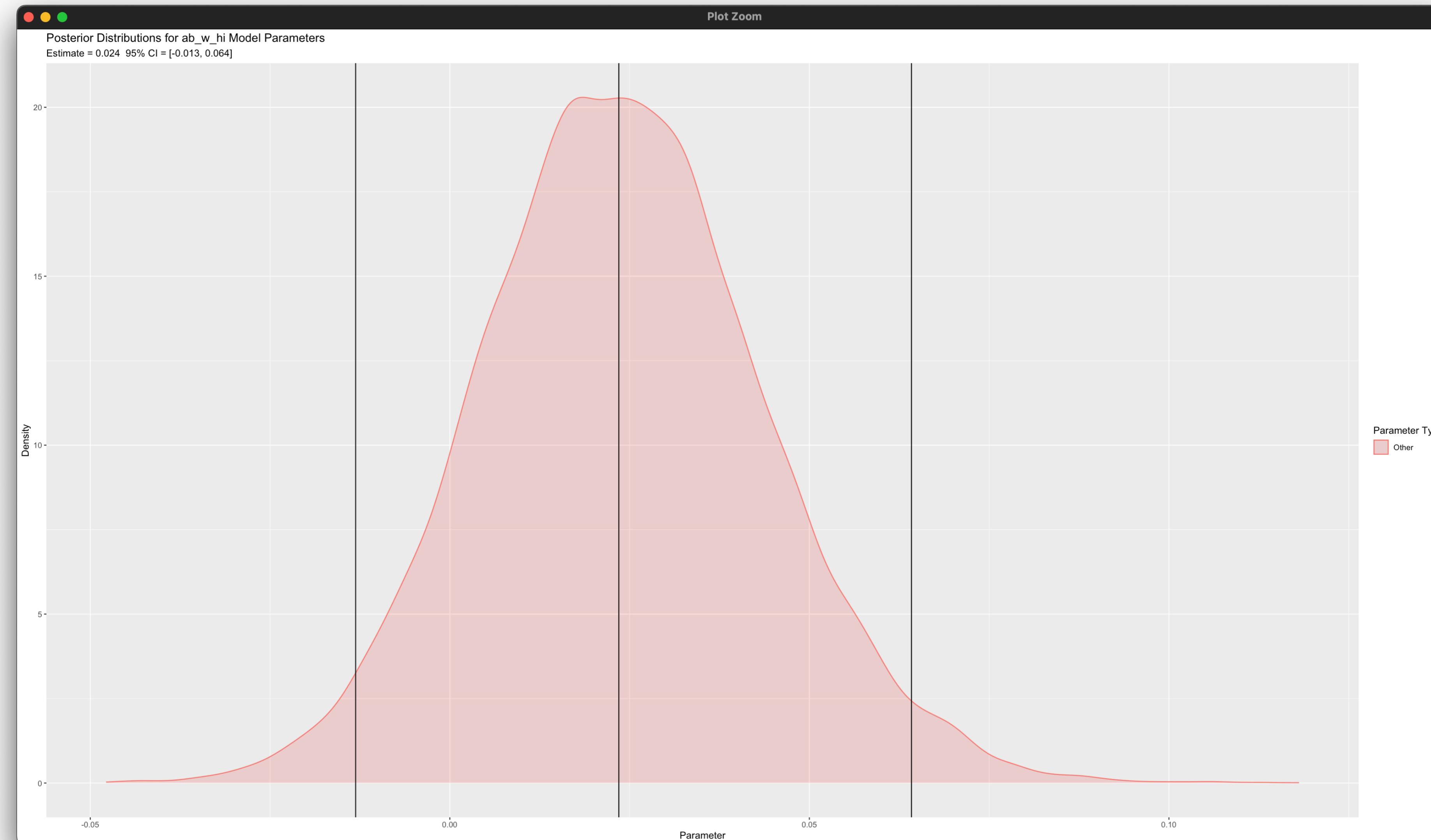
NOTE: Estimate column based on posterior median.

Standard test statistics are inappropriate  
for evaluating mediated effects!

Parameters	Estimate	StdDev	2.5%	97.5%	ChiSq	PValue	N_Eff
<hr/>							
ab_cov	0.008	0.010	-0.012	0.028	0.651	0.420	526.299
a_hi	0.849	0.103	0.651	1.053	67.974	0.000	723.826
a_mean	0.655	0.073	0.510	0.797	80.705	0.000	830.976
a_lo	0.462	0.104	0.254	0.663	19.685	0.000	863.252
b_hi	0.019	0.019	-0.018	0.058	0.934	0.341	311.687
b_mean	0.025	0.016	-0.004	0.058	2.711	0.096	359.128
b_lo	0.033	0.020	-0.005	0.073	2.600	0.103	566.367
ab_w_hi	<b>0.024</b>	0.020	<b>-0.013</b>	<b>0.064</b>	1.505	0.220	463.559
ab_w_mean	<b>0.025</b>	0.015	<b>-0.003</b>	<b>0.055</b>	2.930	0.087	494.087
ab_w_lo	<b>0.023</b>	0.015	<b>-0.004</b>	<b>0.054</b>	2.577	0.108	539.407
ab_b	<b>0.008</b>	0.066	<b>-0.158</b>	<b>0.108</b>	0.000	0.991	513.172

# DISTRIBUTION OF $\alpha\beta^w$ (RBLIMP ONLY)

Conditional mediated effect at +1 SD  
above team-level climate mean



# DISTRIBUTION OF $\alpha\beta^w$ (RBLIMP ONLY)

Conditional mediated effect at the team-level climate mean



# DISTRIBUTION OF $\alpha\beta^w$ (RBLIMP ONLY)

Conditional mediated effect at -1 SD  
above team-level climate mean

