Payment mechanisms and risk-aversion in electricity markets with uncertain supply

Ryan Cory-Wright
Joint work with Golbon Zakeri
(thanks to Andy Philpott)

ISMP, Bordeaux, July 2018.

ORC, Massachusetts Institute of Technology Work performed at Electric Power Optimization Centre, University of Auckland

A problem: The cost of being deterministic is increasing

- Historically, electricity markets comprised hydro+thermal generators
 - Dispatch participants deterministically.
- Wind, solar not known apriori.

Common solution: two markets; forward + real-time. (C.f. PJM)

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Some problems with this approach:

- If the forward market is deterministic, wind causes pricing inconsistencies between the markets (Zavala et al, 2017).
- If the forward market is deterministic, then generators may not achieve cost recovery, even in expectation.
- Efficiency cost in being deterministic.
 - Leaving money on the table.
 - Economic & political pressure to invest in wind & solar generation;
 the cost of being deterministic is increasing.

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- First stage: minimize expected cost of generation plus deviating from a setpoint, provide setpoint to generators.
- Nature selects a realisation of wind generation.
- Second stage: minimize generation cost plus cost of deviating from setpoint, implement dispatch policy.

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 - Do we retain revenue adequacy and cost recovery?
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- 3. What happens if participants are risk-averse?
 - Do consumers or generators bear the resultant efficiency losses?
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Reminder: How to price electricity without uncertainty

The market clearing problem:

Min
$$c^{\top}X$$

s.t.
$$\sum_{i \in T(n)} X_i + \tau_n(F) \ge D_n,$$

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Pricing relatively straightforward.

- Apply second welfare theorem.
 - Take Lagrangian by dualizing supply-demand balance.
 - Decouple Lagrangian by participant.
 - Yields revenue adequate, cost recovering uniform price.

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 - Take Lagrangian by dualizing supply-demand balance.
 - Decouple Lagrangian by participant.
 - Yields revenue adequate, cost recovering uniform price.
- Can we take the Lagrangian and decouple with uncertainty?

The stochastic dispatch mechanism (Zakeri et al, 2018)

The stochastic market clearing problem:

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$$\mathbb{E}_{\omega}[c^TX(\omega) + r_u^TU(\omega) + r_v^TV(\omega)]$$

s.t. $\sum_{i \in \mathcal{T}(n)} X_i(\omega) + \tau_n(F(\omega)) \ge D_n(\omega), \qquad \forall \omega, [\mathbb{P}(\omega)\lambda_n(\omega)],$
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- x is the forward setpoint, $X(\omega)$ is the dispatch in scenario ω .
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- Nonanticipativity is new. Should we dualize it?

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See (Cory-Wright, Philpott & Zakeri 2018) for more details.

Assumption for rest of talk: using first payment mechanism (simpler).

Three key questions:

- 1. How do we pay participants? ✓
 - Take Lagrangian of forward market clearing problem.
 - With RN generators, dualize supply-demand and obtain revenue adequacy+expected cost recovery.
 - With RN ISO, dualize supply-demand, nonanticipativity and obtain expected revenue adequacy+cost recovery.
- 2. Does implementing SDM cause one-sided wealth transfers?
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- Value of Stochastic Solution a.s. non-negative in long-run.
 - And \$63,000-\$410,000 in NZEM.
 - See (Cory-Wright & Zakeri 2018) for more on this.
 - How are these savings allocated between generators and consumers?
 - Under what conditions?

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 - Savings to generators 70 times system savings (when K=10), almost entirely at expense of consumers.
- Overall: implementing SDM equivalent to one-sided wealth transfer.
 - Generators earn 10 times VSS, at expense of consumers.
- Mechanism for this behaviour arises from SDM's Lagrangian.
 - Nonanticipativity multiplier + nodal price +... = constant.
 - Nonanticipativity multiplier is monotone operator w.r.t pre-commitment.

Why don't we constrain pre-commitment to expected demand?

- Imposing additional constraints causes efficiency losses.
 - (Zakeri et al. 2018) has an example where imposing a first-stage constraint causes a 2% efficiency loss.
 - Unclear whether paying this "price of fairness" is worthwhile.
- With a first-stage constraint, we can do no better than expected revenue adequacy and expected cost recovery.
 - Assuming we are social-welfare maximizing.
 - If we attack KKT conditions directly, can obtain both, with system efficiency losses (c.f. Kazempour et al. 2018)

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 - Risk aversion causes efficiency losses.
 - Does it also cause a wealth transfer? Under what conditions?

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- Endow all generation agents with coherent risk measures.
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 - Total system welfare lower than RN competitive equilibrium.
- Dispatch participants by solving a complimentarity problem.
- Want to perform sensitivity analysis.
 - To determine if SDM is robust to risk-averse generators.

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 - Need to establish an existence result.

Theorem

Let the sample space be finite, and assume nodal prices capped by VOLL. Then, the risk-averse competitive equilibrium admits a solution.

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- Proof: introduce market-clearing agent, apply Rosen's theorem.
- Solution may not be unique.
 - C.f. Henri Gerard's talk yesterday.

Risk-aversion: What happens to pre-commitment?

Theorem

Let generator i's real-time dispatch be $X_i(\omega)$ in each scenario ω . Endow generator i with risk measure ρ , which has Kusuoka representation:

$$\rho(Z) = -\mathbb{E}[Z] + \kappa \sup_{\mu \in D} \int_{\beta=0}^{\beta=1} \frac{1}{\beta} r_{\beta}[Z] \mu d\beta.$$

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$$\begin{split} \textbf{x}_{i}^{*} &= \textit{F}_{\textit{X}_{i}(\omega)}^{-1} \Big(\frac{\textit{r}_{\textit{u},i}}{\left(\textit{r}_{\textit{u},i} + \textit{r}_{\textit{v},i}\right) \! \left(1 + \kappa \! \left(1 - \overline{\beta}\right)\right)} \Big), \\ \textit{where:} \quad \bar{\beta} &= \int_{0}^{1} \mu^{\textit{RN}} \beta \, d\beta; \ \kappa \in [0, \frac{1}{\overline{\beta}}]. \end{split}$$

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Interpretation: Risk-aversion emphasises low payoffs in high wind periods, decreasing pre-commitment.

Theorem

Let generator be net-pivotal & risk-averse, collect risk-aversion in term $\alpha_i := \frac{1}{1+\kappa_i(1-\bar{\beta}_i)}$, where $\bar{\beta}_i := \int_0^1 \mu^{RN} \beta_i d\beta_i$, $\kappa_i \in [0,\frac{1}{\bar{\beta}_i}]$. Then, generator's expected risk-neutral profit is $(1-\alpha_i)r_{u,i}x_i^*$.

Expected profit is:

- 1. Zero if generator is risk-neutral.
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One answer: Introduce risk trading.

Case II: Risk-aversion with risk-trading

The setup (C.f. Ralph+Smeers 2015):

- Endow all generation agents with coherent risk measures.
- Assume risk sets intersect.
- Allow participants to trade Arrow-Debreu securities on exchange.
- Second welfare theorem applies.
 - Solution exists, can solve via convex programming.
 - More welfare than no risk-trading, but less than RN equilibrium.

Theorem

Let generator i's real-time dispatch be $X_i(\omega)$ in each scenario ω . Endow generator i with risk measure ρ , which has Kusuoka representation:

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Interpretation: Arrow-Debreu securities re-align incentives, emphasising high system costs in low wind periods & increasing pre-commitment.

- Being risk-averse decreases pre-commitment without a risk market.
- But increases pre-commitment with a risk market.
- More pre-commitment corresponds to lower prices.

- Being risk-averse decreases pre-commitment without a risk market.
- But increases pre-commitment with a risk market.
- More pre-commitment corresponds to lower prices.
- With risk-trading, can tell if net-pivotal generator is risk-averse or exercising market power.

An alternative to risk-trading

Alternatively, use cost-recovering payment mechanism derived earlier. In the presence of risk-averse generators, this:

- Removes incentive for a risk-averse net-pivotal generator to deviate.
- Corresponds to uniform price with feasible allocation of ADBs.
 - Higher social welfare than no risk-trading with uniform pricing.
 - But lower social welfare than fully liquid risk market.
 - Also corresponds to ISO assuming risk for free. Who pays for this?

Summary: How does stochastic dispatch work in practise?

How do we implement a stochastic dispatch mechanism?

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Open guestion: How much of this translates to stoch. unit commitment?

For more on this, see:

- R. Cory-Wright, A. Philpott, and G. Zakeri. Payment mechanisms for electricity markets with uncertain supply. Operations Research Letters 46(1) 116-121, 2018.
- R. Cory-Wright and G. Zakeri. On efficiency savings, wealth transfers and risk-aversion in electricity markets with uncertain supply. Working paper, available at Optimization Online.
- Andy Philpott's plenary (Thursday 1:30-2:30 pm).

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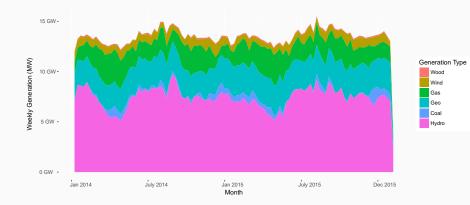
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Thank You!

Questions?

Appendix A: Methodology

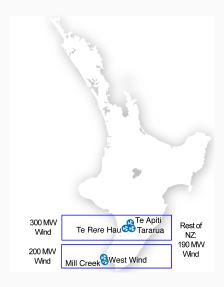
Composition of the NZEM in 2014 - 2015: By week



Hydro dominated (55%) with geothermal (21%), gas (15%), wind (5.7%), coal (2.6%), and wood (0.8%).

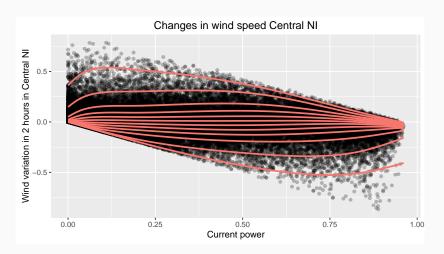
Scenario generation I: Wind farms modelled

CNI, Wellington: assume conditionally independent.



Scenario generation II

Ensemble forecasting via quantile regression



How to estimate the marginal deviation costs:

Costs of deviation are modelled by:

$$\begin{split} r_u &= \frac{\mathit{K}}{\mathit{Generator}} \, \mathit{Ramp} \, \mathit{Up} \, \mathit{Rate}}, \\ r_v &= \frac{\mathit{K}}{\mathit{Generator}} \, \mathit{Ramp} \, \mathit{Down} \, \mathit{Rate}}. \end{split}$$

Reserve prices indicate that $K \in [10, 100]$.

See (Khazaei et al. 2014, Zakeri et al. 2018) for details.

Appendix B: Sensitivity

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for each generator i; α 's are dual multipliers for $0 \le X \le G$.

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 x, real-time prices decrease, savings allocated to consumers.
- Result #2: if implementing SDM decreases pre-commitment decision x, real-time prices decrease, savings allocated to generators.

Appendix C: Risk-Aversion

Theorem

Let generator be net-pivotal & risk-averse, collect risk-aversion in term $\alpha_i := \frac{1}{1+\kappa_i(1-\bar{\beta}_i)}$, where $\bar{\beta}_i := \int_0^1 \mu^{RN} \beta_i d\beta_i$, $\kappa_i \in [0,\frac{1}{\bar{\beta}_i}]$. Then, generator's expected risk-neutral profit is $-(1-\alpha)r_{v,i}x_i^*$. Expected profit is zero if generator is risk-neutral, and negative if generator is risk-averse.

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N.b. Arrow-Debreu securities still ensure overall expected cost recovery.

Thank You!

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