Prediction of Infectious Disease Epidemics via Weighted Density Ensembles

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Abstract

Introduction

- 7 The practice of combining predictions from different models has been used for decades by climatologists and
- geophysical scientists. These methods have subsequently been adapted and extended by statisticians and computer
- 9 scientists in diverse areas of scientific inquiry. In recent years, these "ensemble" forecasting approaches are
- 10 frequently among the top methods used in prediction challenges across a wide range of applications.
- 11 Ensembles are a natural choice for noisy, complex, and interdependent systems that evolve over time. In these
- settings, no one model is likely to be able to capture and predict the full set of complex relationships that drive
- future observations from a particular system of interest. Instead "specialist" or "component" models can be relied
- 14 on to capture distinct features or signals from a system which, when combined, represent a nearly complete range
- of possible outcomes.
- $_{16}$ Using component models that generate predictive densities for outcomes of interest, we have implemented a series
- of ensembles using different methods for choosing the weights for each model.
- Specifically, we compare three different approaches. The first approach simply takes an equally weighted average
- 19 of all models. The second approach estimates constant but not necessarily equal weights for each model. The
- third approach is a novel method for determining optimal weights based on features of the system at the time
- predictions are made. The overarching goal of this study is to create a systematic comparison between increasingly
- 22 complex ensemble methods to begin to study the benefits of including increasing complexity in ensemble weighting
- 23 schemes
- 24 This paper presents a novel ensemble method that determines optimal model combinations based on observed
- ²⁵ data and aspects of the predictive distributions obtained from those component models. We refer to models built
- using this approach as "feature-weighted" ensembles. This approach fuses aspects of different ensemble methods:
- 27 it uses model stacking [Wolpert, 1992], combines predictive densities as in Bayesian Model Averaging [Madigan
- et al., 1998], and estimates model weights based on features of the system [Sill et al., 2009] using gradient tree
- boosting [Friedman, 2001].
- To illustrate these ensemble methods, we present time-series forecasts for infectious disease, specifically for in-
- fluenza in the U.S. For millenia, infectious diseases have been one of the central existential threats to humankind.
- The international significance of emerging epidemic threats in recent decades, including HIV/AIDS since the
- 1980s, SARS in 2003, H1N1 in 2009, and Ebola and MERS in 2014-2015, has also increased public awareness of
- the importance of understanding and being able to predict infectious disease dynamics. With the revolution in

- data-driven science also occurring in the past few decades, there is now an increased focus on and hope for using statistics to inform public health policy and decision-making in ways that could impact future outbreaks. Some of the largest public health agencies in the world, including the US Centers for Disease Control and Prevention (CDC) have openly endorsed using models to inform decision making, saying "with models, decision-makers can look to the future with confidence in their ability to respond to outbreaks and public health emergencies." [Centers for Disease Control and Prevention, 2016a]
- Development of the methods presented in this manuscript was motivated by the observation that certain prediction models for infectious disease consistently performed better than other models at certain times of year.
- We observed in earlier work that early in the U.S. influenza season, simple models of historical incidence often outperformed more standard time-series prediction models such as a seasonal auto-regressive integrated moving average (SARIMA) model[?]. However, in the middle of the season, the time-series models showed improved accuracy. We set out to determine whether ensemble methods could use this information about past model performance to improve predictions.
- [TODO: Insert 1-paragraph ensemble methods literature review here.]
- While there are many different methods for combining models, all ensemble models discussed in this paper use an approach called stacking.
- In this approach, each of the component models is trained separately in a first stage, and cross-validated measures of performance of those component models are obtained.
- Then, in a second stage, a stacking model is trained using the cross-validated performance measures to learn how to optimally combine predictions from the component models.
- Using seasonal influenza outbreaks in the US health regions as a case-study, we developed and applied our ensemble models to predict several attributes of the influenza season at each week during the season. By illustrating the utility of these approaches to ensemble forecasting in a setting with complex population dynamics, this work highlights the importance of continued innovation in ensemble methodology.

Methods

This paper presents a comparison of methods for determining weights for stacked density ensembles, applied to forecasting specific features of influenza seasons in the U.S. First, we present a description of the influenza data we use in our application and the prediction targets. Next, we discuss the three component models utilized by the ensemble framework. We then turn to the ensemble framework itself, describing the different ensemble model specifications used. Finally, we present the results of our application of these methods to the influenza data and conclude with a discussion.

Data and prediction targets

We obtained publicly available data on seasonal influenza activity in the United States between 1997 and 2016 from the U.S. Centers for Disease Control and Prevention (CDC) (Figure 1). For each of the 10 Health and Human Services regions in the country in addition to the nation as a whole, the CDC calculates and publishes each week a measure called the weighted influenza-like illness (wILI) index. The wILI for a particular region is calculated as

the average proportion of doctor visits with influenza-like illness for each state in the region, weighted by state population. During the CDC-defined influenza season (between Morbidity and Mortality Weekly Report [MMWR] week 40 of one year and 20 of the next year), the CDC publishes updated influenza data on a weekly basis. This includes "current" wILI data from two weeks prior to the reporting date, as well as updates to previously reported numbers as new data becomes available. For this analysis, we use only the final reported wILI measures to train and predict from our models.

The CDC defines the influenza season onset as the first of three successive weeks of the season for which wILI is greater than or equal to a threshold that is specific to the region and season. This threshold is the mean percent of patient visits where the patient had ILI during low incidence weeks for that region in the past three seasons, plus two standard deviations [Centers for Disease Control and Prevention, 2016b]. The CDC provides historical threshold values for each region going back to the 2007/2008 season [{Centers for Disease Control and Prevention}, 2016]. Additionally, we define two other metrics specific to a region-season. The peak incidence is the maximum observed wILI measured in a season. The peak week is the week at which the maximum wILI for the season is observed.

Each predictive distribution was represented by probabilities assigned to bins associated with different possible outcomes. For onset week, the bins are represented by integer values for each possible season week plus a bin for "no onset". For peak week, the bins are represented by integer values for each possible season week. For peak incidence, the bins capture incidence rounded to a single decimal place, with a single bin to capture all incidence over 13.05. Formally, the incidence bins are as follows: [0, 0.05), [0.05, 0.15), ..., [12.95, 13.05), $[13.05, \infty)$.

These bins were used in the 2016-2017 influenza prediction contest run by the CDC (cite something).

We measure the accuracy of predictive distributions using the log score. The log score is a proper scoring rule [Gneiting and Raftery, 2007], calculated in our setting as the natural log of the probability assigned to the bin containing the true observation. Proper scoring rules are preferred for measuring the quality of predictive distributions because the expected score is optimized by the true probabilty distribution. We note that for peak week, in some region-seasons the same peak incidence was achieved in multiple weeks (after rounding to one decimal place). In those cases, we calculated the log score as the log of the sum of the probabilities assigned to those weeks; this is consistent with scoring procedures used in the 2016-2017 flu prediction contest run by the CDC (cite something).

Gomponent models

We used three component models to generate probabilistic predictions of the three prediction targets. The first model was a seasonal average model that utilized kernel density estimation (KDE) to estimate a predictive distribution for each target. The second model utilized kernel conditional density estimation (KCDE) and copulas to create a joint predictive distribution for incidence in all remaining weeks of the season, conditional on recent observations of incidence.[[Cite Evan's paper on arxiv!]] By calculating appropriate integrals of this joint distribution, we constructed predictive distributions for each of the seasonal targets. The third model used a standard seasonal auto-regressive integrated moving average (SARIMA) implementation. All models were fit independently on data within each region.

108 Kernel Density Estimation (KDE)

The simplest of the component models uses kernel density estimation [Silverman, 1986] to estimate a distribution for each target based on observed values of that target in previous seasons within the region of interest. We used Gaussian kernels and the default KDE settings from the density function in the stats package for R [R Core Team, 2016] to estimate the bandwidth parameter. For the peak incidence target, we fit to log-transformed observations of historical peak incidence. For the onset week prediction target, we estimated the probability of no onset as the proportion of region-seasons in all regions in the training phase where no week in the season met the criteria for being a season onset.

To create an empirical predictive distribution of size N from a KDE fit based on a data vector $\mathbf{y}_{1:K}$ (for example, 116 this might be the vector of peak week values from the K training seasons), we first drew N samples with 117 replacement from $\mathbf{y}_{1:K}$, yielding a new vector $\tilde{\mathbf{y}}_{1:N}$. We then drew a single psuedo-random deviates from each 118 of N truncated Gaussian distributions centered at $\tilde{\mathbf{y}}_{1:N}$ with the bandwidth estimated by the KDE algorithm. 119 The Gaussians we sampled from were truncated at the lower and upper bounds of possible values for the given 120 prediction target. Finally, we discretized the sampled values to the target-specific bins. These sampled points then make up the empirical predictive distribution from a KDE model. We set the sample size to $N=10^5$. In 122 theory, this model assigns non-zero probability to every possible outcome; however, in a few cases the empirical 123 predictive distribution resulting from this Monte Carlo sampling approach assigned probability zero to some of the 125

lt is important to note that the predictions from this model do not change as new data are observed over the course of the season.

128 Kernel Conditional Density Estimation (KCDE)

We used kernel conditional density estimation and copulas to estimate a joint predictive distribution for flu incidence in each future week of the season, and then calculated predictive distributions for each target from that joint distribution. [[Cite Evan's paper]] In our implementation, we first used KCDE to obtain separate predictive densities for flu incidence in each future week of the season. Each of these predictive densities gives a conditional distribution for incidence at one future time point given recent observations of incidence and the current week of the season. KCDE can be viewed as a distribution-based analogue of nearest-neighbors regression. We then used a copula to model dependence among those individual predictive densities, thereby obtaining a joint predictive density, or a distribution of incidence trajectories in all future weeks.

To predict seasonal quantities (onset, peak timing, and peak incidence), we simulate $N=10^5$ trajectories of disease incidence from this joint predictive distribution. For each simulated incidence trajectory, we compute the onset week, peak week, and peak incidence. We then aggregate these values to create predictive distributions for each target. This procedure for obtaining predictive distributions for the targets of interest can be formally justified as an appropriate Monte Carlo integral of the joint predictive distribution for disease incidence in future weeks (see [?] for details).

Seasonal auto-regressive integrated moving average (SARIMA)

We fit seasonal ARIMA models [Box et al., 2015] to wILI observations transformed to be on the natural log scale.
We manually performed first-order seasonal differencing and used the stepwise procedure from the auto.arima
function in the forecast package [Hyndman and Khandakar, 2008] for R to select the specification of the
auto-regressive and moving average terms.

Similar to KCDE, forecasts were obtained by sampling $N=10^5$ trajectories of wILI values over the rest of the season (using the simulate.Arima function from the forecast package), and predictive distributions of the targets were computed from these sampled trajectories as described above.

151 Component model training

We used data from 14 seasons (1997/1998 through 2010/2011) to train the models. Data from five seasons (2011/2012 through 2015/2016) were held out when fitting the models and used exclusively in the testing phase.
To avoid overfitting our models, we made predictions for the test phase only once [Hastie et al., 2011].

Estimation of the ensemble models (discussed in the next subsection) requires cross-validated measures of performance of each of the component models in order to accurately gauge their relative performance. For each region, we estimated the parameters of each component model 15 times: 14 fits were obtained excluding one training season at a time, and another fit used all of the training data. For each fit obtained leaving one season out, we generated a set of three predictive distributions, one for each of the prediction targets in the held-out season. We were not able to generate predictions from the SARIMA and KCDE models for some seasons in the training phase because those models used lagged observations from previous seasons that were missing in our data set. The component model fits based on all of the training data were used to generate predictions for the test phase.

163 Ensemble models

All of the ensemble models we consider in this article work by averaging predictions from the component models to obtain the ensemble prediction. Additionally, these methods are stacked model ensembles because they use leave-one-season-out predictions from the independently estimated component models as inputs to estimate the model weights. [Wolpert, 1992] We begin our discussion of ensemble methods with a general overview, introducing a common set of notation and giving a broad outline of the ensemble models we will use in this article. We then describe our proposed feature-weighted stacking ensemble model specification in more detail.

170 Overview of ensemble models

A single set of notation can be used to describe all of the ensemble frameworks implemented here. Let $f_m(y|\mathbf{x}^{(m)})$ denote the predictive density from component model m for the value of the scalar random variable Y conditional on observed variables $\mathbf{x}^{(m)}$. For example, Y could represent the peak incidence for a given season and region. In the context of time series predictions, the covariate vector $\mathbf{x}^{(m)}$ may include time-varying covariates such as the week at which the prediction is made or lagged incidence; we suppress that dependence on time in our notation for the sake of simplicity. The superscript $^{(m)}$ reflects the fact that each component model may use a different set of covariates.

The combined predictive density $f(y|\mathbf{x})$ for a particular target can be written as

$$f(y|\mathbf{x}) = \sum_{m=1}^{M} \pi_m(\mathbf{x}) f_m(y|\mathbf{x}^{(m)}).$$
(1)

In Equation (1) the π_m are the model weights, which are allowed to vary as a function of observed features in \mathbf{x} . We define \mathbf{x} to be a vector of all observed quantities that are used by any of the component models or in calculating the model weights. In order to guarantee that $f(y|\mathbf{x})$ is a probability distribution we require that $\sum_{m=1}^{M} \pi_m(\mathbf{x}) = 1$ for all \mathbf{x} . Figure 2 illustrates the concept of stacking the predictive densities for each component model.

In the following subsection, we propose a framework for estimating feature-dependent weights for a stacked 184 ensemble model. By feature-dependent we mean that the weights associated with different component models are driven by observed features or covariates. Although we illustrate the method in the context of time-series 186 predictions, the method could be used in any setting where we wish to combine distribution estimates from 187 multiple models. Features could include observed data from the system being predicted (such as recent wILI measurements or the time of year at which predictions are being made), observed data from outside the system 189 (for example, recent weather observations), or features of the predictions themselves (e.g. summaries of the 190 predictive distributions from the component models, such as a measure of spread in the distribution, or the time 191 until a predicted peak). Based on exploration of training phase data and a priori knowledge of the disease system, 192 we chose three features of the system to illustrate the proposed "feature-weighting" methodology: week of season, 193 component model uncertainty (defined as the minimum number of predictive distribution bins required to cover 90% probability), and wILI measurement at the time of prediction. These features were chosen prior to and not 195 changed after implementing test-phase predictions. 196

197 We used four distinct methodologies to define weights to use for the stacking models:

- 1. Equal Weights (EW): $\pi_m(\mathbf{x}) = 1/M$. In this scenario, each model contributes the same weight for each target and for all values of \mathbf{x} .
- 20. Constant model weights via degenerate EM (**dEM**): $\pi_m(\mathbf{x}) = c_m$, a constant where $\sum_{m=1}^M c_m = 1$ but the constants are not necessarily the same for each model. These weights are estimated using the degenerate estimation-maximization (dEM) algorithm [Lin and Zhu, 2004]. A separate set of weights is estimated for each region and prediction target.
 - 3. Feature-weighted (**FW**): $\pi_m(\mathbf{x})$ depends on features including week of the season and model uncertainty for the KCDE and SARIMA models. A separate set of weighting functions is estimated for each region and prediction target.
 - 4. Feature-weighted with regularization: $\pi_m(\mathbf{x})$ depends on features, but with regularization discouraging the weights from taking extreme values or from varying too quickly as a function of \mathbf{x} . A separate set of weighting functions is estimated for each region and prediction target. We fit three variations on this ensemble model, using different sets of features:
 - a. (FW-reg-w) week of the season;

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b. (FW-reg-wu) week of the season and model uncertainty for the KCDE and SARIMA models;

c. (FW-reg-wui) week of the season, model uncertainty for the KCDE and SARIMA models, and incidence (wILI) in the most recent week.

All in all, this leads to 6 ensemble models, summarized in Table 1. The first three of these models (EW, dEM, and FW) can be viewed as variations on FW-reg-wu if we vary the amount and type of regularization imposed on the FW-reg-wu model. Thus, comparisons among these four models will allow us to explore the benefits of allowing the model weights to depend on covariates while imposing an appropriate amount of rigidity on the model weight functions $\pi_m(\mathbf{x})$. We will discuss the regularization strategies used in FW-reg-wu further in the next subsection. Meanwhile, comparisons among the FW-reg-w, FW-reg-wu, and FW-reg-wui models will allow us to explore the relative contributions to predictive performance that can be achieved by allowing the model weights to depend on different features.

	Component Model Weights Vary with					
		Prediction	Week of	SARIMA	KCDE	Current
Model	Region	Target	Season	Uncertainty	Uncertainty	wILI
EW						
dEM	Χ	X				
FW	Χ	X	Χ	X	X	
FW-reg-w	Χ	X	X			
FW-reg-wu	Χ	X	X	Χ	X	
FW-reg-wui	X	Χ	Χ	Χ	X	X

Table 1: Summary of ensemble methods and what the model weights depend on.

Each of the six ensemble models, along with the three component models, are used to generate predictions in every season-week of each of the five testing seasons, assuming perfect reporting. These predictions are then used to evaluate the prospective predictive performance of each of the ensemble methods. In total, we evaluate 9 models in 11 regions over 5 years and 3 targets of interest.

Feature-weighted stacking framework

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In this section we introduce the particular specification of the parameter weight functions $\pi_m(\mathbf{x})$ that we use and discuss estimation.

In order to ensure that the the π_m are non-negative and sum to 1 for all values of ${\bf x}$, we parameterize them in terms of the softmax transformation of real-valued latent functions ρ_m :

$$\pi_m(\mathbf{x}) = \frac{\exp\{\rho_m(\mathbf{x})\}}{\sum_{m'=1}^M \exp\{\rho_{m'}(\mathbf{x})\}}.$$
 (2)

For a pair of models $l, m \in \{1, ..., M\}$, $\rho_l(\mathbf{x}) > \rho_m(\mathbf{x})$ indicates that model l has more weight than model m for predictions at the given value of \mathbf{x} .

The functions $\rho_m(\mathbf{x})$ could be parameterized and estimated using many different techniques, such as a linear specification in the features, splines, or so on. We have chosen to estimate the functions $\rho_m(\mathbf{x})$ using gradient tree boosting.

Gradient tree boosting uses a forward stagewise additive modeling algorithm to iteratively and incrementally construct a series of regression trees that, when added together, create a function designed to minimize a given loss function. In our application, the algorithm builds up the $\rho_m(\mathbf{x})$ that minimize the negative cross-validated log-score of the stacked prediction $f(y|\mathbf{X})$. We have used the xgb.train function in the xgboost package for R to perform this estimation.[Chen et al., 2016]

Specifically, we define a single tree as

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$$T(\mathbf{x}; \boldsymbol{\theta}) = \sum_{j=1}^{J} \gamma_j I_{R_j}(\mathbf{x}), \tag{3}$$

where the R_j are a set of disjoint regions that comprise a partition of the space $\mathcal X$ of feature values $\mathbf x$, and I is the indicator function taking the value 1 if $\mathbf x \in R_j$ and 0 otherwise. The parameters $\boldsymbol \theta = (\boldsymbol \psi, \boldsymbol \gamma)$ for the tree are the split points $\boldsymbol \psi$ partitioning $\mathcal X$ into the regions R_j and the regression constants $\boldsymbol \gamma$ associated with each region. The function $\rho_m(\mathbf x)$ is obtained as the sum of B trees:

$$\rho_m(\mathbf{x}; \Theta_m) = \sum_{b=1}^B T(\mathbf{x}; \boldsymbol{\theta}_{m,b}). \tag{4}$$

In each iteration b of the boosting process, we estimate M new regression trees, one for each component model.

These trees are estimated so as to minimize a local approximation to the loss function around the weight functions that were obtained after the previous boosting iteration.

Gradient tree boosting is appealing as a method for estimating the functions ρ_m because it offers a great deal of flexibility in how the weights can vary as a function of the features x. On the other hand, this flexibility can lead to overfitting the training data. In order to limit the chances of overfitting, we have explored the use of four regularization parameters:

- 1. The number of boosting iterations B. As B increases, more extreme weights (close to 0 or 1) and more rapid changes in the weights as x varies are possible.
 - 2. An L_1 penalty on the number of tree leaves, J. A large penalty encourages the regression trees to have fewer leaves, so that there is less flexibility for the model weights to vary as a function of \mathbf{x} .
 - 3. The maximum depth of the regression trees; i.e., how many times the same region may be successively split. Similarly to the L_1 penalty on the number of tree leaves, this controls how much flexibility there is for the model weights to vary in \mathbf{x} . Additionally, the maximum depth controls the number of interactions. For instance, a maximum depth of 2 indicates that there can be at most two-way interactions between different features in setting model weights.
 - 4. An L_1 penalty on the regression constants γ_j . A large penalty encourages these constants to be small, so that the overall model weights change less in each boosting iteration.

We selected values for these regularization parameters using a grid search optimizing leave-one-season-out crossvalidated model performance.

Software and code

We used R version 3.2.4 (2016-03-10) for all analyses. [R Core Team, 2016] All data and code used for this analysis is freely available in an R package online at https://github.com/reichlab/adaptively-weighted-ensemble and may be installed in R directly. Predictions generated in real-time with early development versions of this model during the 2016/2017 influenza season may be viewed at https://reichlab.github.io/flusight/. To maximize reproducibility of our work, we have set seeds prior to running code that relies on stochastic simulations using the rstream package. [Leydold, 2015]

Additionally, the manuscript itself was dynamically generated using RMarkdown.

76 Results

To evaluate overall model performance, we computed log scores for all predictions made by each model across all regions and test phase seasons. We also examined results for predictions made before the peak week (for predictions of peak timing or peak incidence) or the season onset (for predictions of onset timing). These predictions are the most relevant to decision makers using predictions as inputs to set public policy. The relative performance of the modeling approaches considered here is similar for predictions made over the course of the entire season (Supplemental Figure [[TODO: reference supplemental figure with overall B-W plot]]).

Feature-Weighted Ensemble Model Weights Reflect Trends in Component Model Log Scores

Figure ?? displays variation in leave-one-season-out log scores from the three component models over the course of the training phase seasons, along with the corresponding model weight estimates from the CW and FW-reg-w 286 models. In general, average performance of the SARIMA and KCDE models track each other closely over the 287 course of the season, with performance improving as more data become available. In the training seasons, average performance of the KDE model tends to be better than KCDE and SARIMA during the first few weeks of the 289 season. Near the beginning of some seasons, predictions from the SARIMA model are quite a bit worse than 290 predictions from the other two component models. Supplemental Figure [[TODO: Insert figure number]] shows 291 that performance of the component models also varies with the model's uncertainty, as measured by the number 292 of bins required to cover 90% in the predictive distribution. 293

Figure 3 displays the estimated component model weights from the **CW** and **FW-reg-w** methods for predictions of season onset for each week in the season. As expected, near the beginning of the season the **FW-reg-w** ensemble assigns higher weight to the **KDE** model than the **CW** ensemble. The weights assigned to the component model track the relative performance of those models in the training phase fairly well.

The Best 7 of 9 Models Have Similar Performance in Aggregate

Box and Whiskers plot

We estimated mean performance of each component model for predictions made before the season peak (for predictions of peak incidence or peak timing) or before the season onset (for predictions of season onset) (Figure

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Ensemble Methods Have More Stable Performance Across Seasons

- Comparison of ranked log-score performance (heatmap)
 - worst performing model always a component model, never KCDE
 - ensemble models, esp. regularized, show less variability
 - CW best ensemble across each metric

Interpret results of best overall FW model for each metric (plot to come)

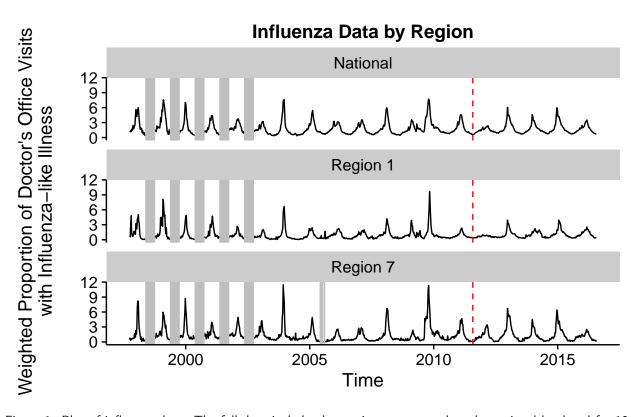


Figure 1: Plot of influenza data. The full data include observations aggregated to the national level and for 10 smaller regions. Here we plot only the data at the national level and in two of the smaller regions; data for the other regions are qualitatively similar. Missing data are indicated with vertical grey lines. The vertical red dashed lines indicate the cutoff time between the training and testing phases; 5 seasons of data were held out for testing.

Conclusion

Achievements

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• developed ensemble framework that makes [[better]] predictions on average than component models

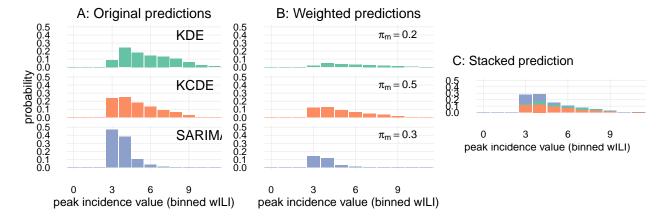


Figure 2: Conceptual diagram of how the stacking models operate on probabilistic predictive distributions. The distributions illustrated here have density bins of 1 wlLl unit, which differs from those used in the manuscript for illustrative purposes only. Panel A shows the predictive distributions from three component models. Panel B shows scaled versions of the distributions from A, after being multiplied by model weights. In Panel C, the scaled distributions are literally stacked to create the final ensemble predictive distribution.

- ensemble method uses novel method to estimate feature-dependent weights
- predictions disseminated and updated weekly

314 Strengths/novelty

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- feature-weighting works regardless of discrete/continuous covariate
- operates on predictive distributions, not just point-estimates
- General framework (not just time-series or infectious disease)
- framework could be used to answer epidemiologically relevant questions: when do certain models contain
 information that substantially improve predictions, e.g. adding weather, mechanistic models, strain specific
 models, etc...

[[TODO: Discuss how varying some of these regularization parameters can give the simpler EW and dEM models??

Or ignore? Or defer to supplement?]]

323 Limitations

• illustration only includes simple models and simple features

References

- George EP Box, Gwilym M Jenkins, Gregory C Reinsel, and Greta M Ljung. *Time series analysis: forecasting and control.* John Wiley & Sons, 2015.
- Centers for Disease Control and Prevention. Staying Ahead of the Curve: Modeling and Public Health Decision-Making, 2016a. URL http://www.cdc.gov/cdcgrandrounds/archives/2016/january2016.htm.

Component Model Weights and Training Phase Log Scores – National A: Onset Timing

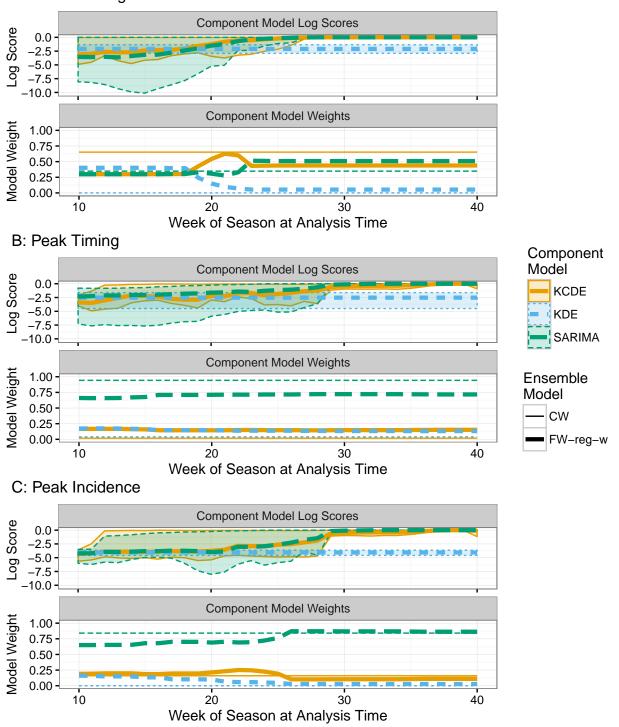


Figure 3: Example of component model weights from the **CW** and **FW-reg-w** models for National predictions. The upper plot within each panel shows mean, minimum, and maximum log scores achieved by each component model for predictions of the given prediction target at the national level in each week of the season, summarizing across all seasons in the training phase when all three component models produced predictions. The lower plot within each panel shows model weights from the **CW** and **FW-reg-w** ensemble methods at each week in the season.

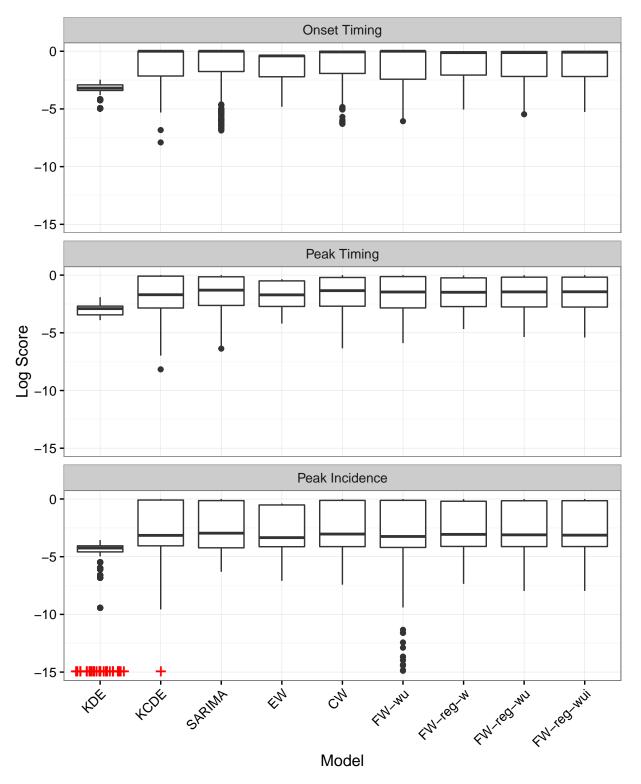


Figure 4: Test phase log scores summary v1. Log scores across all seasons/season weeks represented in box plots. Log scores of -Infinity are represented with a cross at -15.

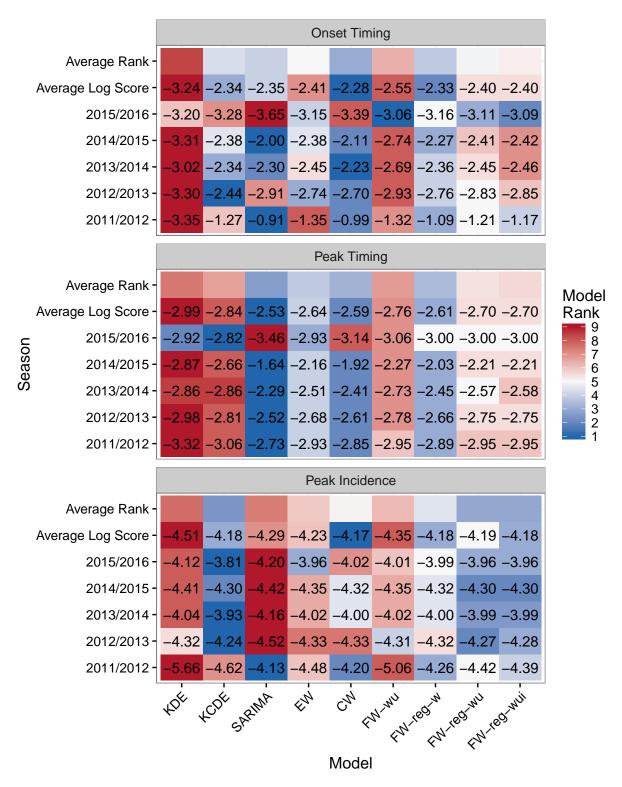


Figure 5: Model performance ranked by mean log score within each of the five test seasons for predictions made before the target (season onset or peak) occurred.

- Centers for Disease Control and Prevention. Overview of Influenza Surveillance in the United States, 2016b. URL
 https://www.cdc.gov/flu/weekly/overview.htm.
- {Centers for Disease Control and Prevention}. Regional baseline values for influenza-like illness, 2016. URL https://github.com/cdcepi/FluSight-forecasts/blob/master/wILI{_}}Baseline.csv.
- Tianqi Chen, Tong He, and Michael Benesty. *xgboost: Extreme Gradient Boosting*, 2016. URL https://CRAN.

 R-project.org/package=xgboost. R package version 0.4-4.
- Jerome H Friedman. Greedy function approximation: a gradient boosting machine. *Annals of statistics*, pages 1189–1232, 2001.
- Tilmann Gneiting and Adrian E Raftery. Strictly proper scoring rules, prediction, and estimation. Journal of the American Statistical Association, 102(477):359–378, 2007. URL http://gateway.webofknowledge.com/gateway/Gateway.cgi?GWVersion=2{&}SrcAuth=mekentosj{&}SrcApp=
- ${\tt Papers \& DestLink Type=Full Record \& Dest App=WOS \& Key UT=000244361000032 papers 2://English States and States and States are also supported by the property of the prop$
- publication/doi/10.1198/016214506000001437.
- Trevor Hastie, Robert Tibshirani, and Jerome Friedman. *The Elements of Statistical Learning: Data Mining, Inference, and Prediction*. Springer, second edition, 2011. URL http://www.amazon.com/
 Elements-Statistical-Learning-Prediction-Statistics/dp/0387848576/ref=sr{_}}1{_}}14?ie=UTF8{&}qid=
 1429565346{&}sr=8-14{&}keywords=machine+learning.
- Rob J. Hyndman and Yeasmin Khandakar. Automatic time series forecasting: The forecast package for R. Journal Of Statistical Software, 27(3):C3–C3, 2008. ISSN 10411135. doi: 10.18637/jss.v027.i03. URL http://www.robjhyndman.com/papers/forecastpackage.pdf.
- Josef Leydold. *rstream: Streams of Random Numbers*, 2015. URL https://CRAN.R-project.org/package=rstream.

 R package version 1.3.4.
- Xiaodong Lin and Yu Zhu. Degenerate Expectation-Maximization Algorithm for Local Dimension Reduction. In *Classification, Clustering, and Data Mining Applications*, pages 259–268. Springer Berlin Heidelberg, Berlin, Heidelberg, 2004. doi: 10.1007/978-3-642-17103-1_25. URL http://link.springer.com/10.1007/978-3-642-17103-1{_}}25.
- David Madigan, A Raftery, Volinsky, and J Hoeting. Bayesian Model Averaging. *Proceedings of the AAAI*Workshop on Integrating Multiple Learned Models, Portland, OR., (9814), 1998.
- R Core Team. *R: A Language and Environment for Statistical Computing*. R Foundation for Statistical Computing, Vienna, Austria, 2016. URL https://www.R-project.org/.
- Joseph Sill, Gabor Takacs, Lester Mackey, and David Lin. Feature-Weighted Linear Stacking. nov 2009. URL http://arxiv.org/abs/0911.0460.
- 362 Bernard W Silverman. Density estimation for statistics and data analysis, volume 26. CRC press, 1986.
- David H Wolpert. Stacked generalization. *Neural Networks*, 5(2):241–259, 1992. URL http: //pubget.com/site/paper/2a043750-5667-424d-94f1-2e4e39fccbcc?institution=papers2://publication/doi/ 10.1016/S0893-6080(05)80023-1.