

6. 3, 5, 7 is the only prime triple (three primes, each 2 from the next).

Proof:

Lemma: For any integer n , at least one of the integers n , $n + 2$, $n + 4$ is divisible by 3 (for proof see question 5).

Assume there are 3 primes, each 2 from the next. So n , $n + 2$, $n + 4$ are all prime.

But if $n > 3$, this means that at least one of n , $n + 2$, $n + 4$ is not prime (since at least one is divisible by 3). This is a contradiction.

Therefore, 3, 5, 7 is the only prime triple.