

$$\begin{aligned}
\nabla \psi(\vec{x}) &= (-E_y(\vec{x}), E_x(\vec{x})) \\
\psi(\vec{x}) &= \int_{\gamma} \nabla \psi(\vec{s}) \cdot d\vec{s} \\
\psi(\vec{0}) &= 0 \\
\text{let } \vec{r}(t) &= \hat{x}t, \vec{r} : [0, \|\vec{x}\|] \rightarrow \mathbb{R}^2 \\
\vec{r}'(t) &= \hat{x} \\
\psi(\vec{x}) &= \int_0^{\|\vec{x}\|} -\hat{x}_x E_y(\hat{x}t) + \hat{x}_y E_x(\hat{x}t) dt
\end{aligned} \tag{1}$$