# Package 'ForImp'

June 10, 2011

Type Package	
Title Imputation of missing values through a forward imputation algorithm	
Version 1.0	
<b>Date</b> 2011-05-24	
Author Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari	
Maintainer Alessandro Barbiero <alessandro @unimi="" barbiero=""></alessandro>	
<b>Description</b> Imputation of missing values in datasets of ordinal variables through a forward imputation algorithm	
License GPL	
LazyLoad yes	
<b>Depends</b> homals, sampling	
R topics documented:	
ForImp-package	2
ForImp	3
ld	4
<b>r</b>	5
<u>r</u>	6
6	7
e e e e e e e e e e e e e e e e e e e	8
8	9
modeimp	
rancatmat	_
vcosw	
Index 1	

2 ForImp-package

ForImp-package

Forward Imputation

## **Description**

The package contains a function for the imputation of missing values in matrices of ordinal data, called Forward Imputation, and other functions for generating ordinal data or imputing missing values.

#### **Details**

Package: ForImp Type: Package Version: 1.0

Date: 2011-05-24 License: GPL LazyLoad: yes

#### Author(s)

Alessandro Barbiero<alessandro.barbiero@unimi.it>, Giancarlo Manzi<giancarlo.manzi@unimi.it>, Pier Alda Ferrari<pieralda.ferrari@unimi.it>

Maintainer: Alessandro Barbiero<alessandro.barbiero@unimi.it>, Giancarlo Manzi<giancarlo.manzi@unimi.it>, Pier Alda Ferraripieralda.ferrari@unimi.it>

#### References

Ferrari P.A., Annoni P., Barbiero A., Manzi G. (2011) An imputation method for categorical variables with application to nonlinear principal component analysis, Computational Statistics & Data Analysis, vol. 55, issue 7, pages 2410-2420

```
http://ideas.repec.org/a/eee/csdana/v55y2011i7p2410-2420.html http://www.sciencedirect.com/science/article/pii/S0167947311000521
```

Ferrari P.A., Barbiero A., Manzi G.: Handling missing data in presence of ordinal variables: a new imputation procedure. In "New Perspectives in Statistical Modeling and Data Analysis", S. Ingrassia, R. Rocci, M. Vichi, Eds., Springer, 2011

Little, R.J.A., Rubin, D.B., 2002. Statistical Analysis with Missing Data, 2nd ed. John Wiley & Sons, Inc.

ForImp 3

FΟ	r	Γmn

Forward Imputation procedure

#### **Description**

Forward Imputation of missing data

#### Usage

```
For Imp (mat, p=2)
```

#### **Arguments**

mat a matrix/dataframe

p the parameter for computing the Minkowski distance used in the nearest neigh-

bor procedure for missing value imputation. p can be any positive number (p=2 gives the euclidean distance); if a negative number or Inf is entered, the proce-

dure will use the maximum distance (or supremum norm)

#### **Details**

The function implements the Forward Imputation algorithm (see reference) on a matrix of ordinal data with missing values. The algorithm alternates NonLinear Principal Component Analysis (NLPCA) on a subset of the data with no missing data and sequential imputations of missing values by the nearest neighbor method. This sequential process starts from the units with the lowest number of missing values and ends with the units with the highest number of missing values.

#### Value

the imputed matrix

#### Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari

## References

Ferrari P.A., Annoni P., Barbiero A., Manzi G. (2011) An imputation method for categorical variables with application to nonlinear principal component analysis, Computational Statistics & Data Analysis, vol. 55, issue 7, pages 2410-2420

```
http://ideas.repec.org/a/eee/csdana/v55y2011i7p2410-2420.html http://www.sciencedirect.com/science/article/pii/S0167947311000521
```

Ferrari P.A., Barbiero A., Manzi G.: Handling missing data in presence of ordinal variables: a new imputation procedure. In "New Perspectives in Statistical Modeling and Data Analysis", S. Ingrassia, R. Rocci, M. Vichi, Eds., Springer, 2011

#### See Also

modeimp, medianimp, meanimp

4 ld

#### **Examples**

```
library(mvtnorm)
set.seed(1)
# correlation matrix
\# generate a 500*4 matrix from a multivariate normal
matc<-rmvnorm(n=500, mean=rep(0,4), sigma=sigma)</pre>
# transform the numerical values into ordinal categories (Likert scale)
# obtaining matrix mato
mato<-transfmatcat(matc, 4)</pre>
# set the number of desired missing values
nummissing<-100
# create the random missing values, obtaining matrix mat
{\tt mat<-missingmat}\,({\tt mato},\ {\tt nummissing},\ {\tt pattern="r"})
\# use function \code{ForImp} to impute missing values, obtaining matrix mati
mati<-ForImp(mat)</pre>
# number of correct imputations
nummissing-sum(mati!=mato)
```

ld

Listwise deletion

## **Description**

Listwise deletion

#### Usage

ld(mat)

## **Arguments**

mat

a matrix or a dataframe

#### **Details**

This function implements the listwise deletion on a given dataset, removing all the rows or units containing at least one missing value

#### Value

The matrix/dataframe in input with the rows/units with missing values removed

## Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari

#### See Also

```
meanimp, modeimp, medianimp
```

meanimp 5

## **Examples**

```
n<-10
m<-4
mat<-matrix(rnorm(n*m),n,m)
mat[c(3,6),1]<-NA
mat[10,2]<-NA
mat
ld(mat)</pre>
```

meanimp

Mean imputation

## Description

Mean imputation

## Usage

```
meanimp(mat)
```

## **Arguments**

mat

A numerical matrix

#### **Details**

The function implements the unconditional mean imputation on a numerical matrix with missing values, substituting to each missing value the arithmetic mean of the corresponding variable

## Value

The imputed matrix

## Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari

## See Also

```
modeimp, medianimp
```

```
set.seed(1)
n<-10
m<-3
mat<-matrix(rnorm(n*m),n,m)
matm<-mat
matm[1,1]<-NA
matm[2,2:3]<-NA
# matrix with missing values
matm
# imputed matrix</pre>
```

6 medianimp

```
meanimp(mat)
# original matrix with no missing values
mat
```

medianimp

Median imputation

#### **Description**

Median imputation

## Usage

```
medianimp(mat)
```

## Arguments

mat

A matrix of ordinal values, ordered according to the Likert scale (1, 2, 3,...)

#### **Details**

The function implements the median imputation on a matrix of ordinal data with missing values. The function substitutes to each missing value the median of the corresponding variable.

## Value

The imputed matrix

## Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari

#### See Also

```
modeimp, meanimp
```

```
set.seed(1)
n<-10
m<-3
mat<-matrix(ceiling(runif(n*m)*4),n,m)
matm<-mat
matm[1,3]<-NA
matm[9:10,1]<-NA
# matrix with missing values
matm
# imputed matrix
medianimp(matm)
# original matrix with no missing values</pre>
```

missingmat 7

missingmat	Random generation of missing values	
------------	-------------------------------------	--

#### **Description**

Random generation of missing values in matrices of numerical data or preferably categorical data coded as integers

## Usage

```
missingmat(mat, nummissing, pattern = "r", nk = 1, p = 0.1, w = 3)
```

#### **Arguments**

mat	A matrix of numerical values
nummissing	number of missing values
pattern	pattern of missing values ("r" random, "l" lowest value, "b" block, "n" not at random)
nk	category
р	percentage of missing values
W	weight for the lowest category in pps sampling (pattern "n")

#### **Details**

The function generates random missing values on a matrix of categorical data according to a specific pattern. "r" is the random pattern, "l" generates a percentage p of missing values on the lowest values of variable nk, "b" generates random blocks of missing values on the group of variables indexed by nk, "n" generates a kind of not at random missing values: specifically, lowest values are more likely to be missing, since they are assigned a weight w (greater than 1, the default is 3) and the values are sampled according to an unequal probability sampling design (pivotal, see the reference for more details)

#### Value

The original matrix with the desired number of values randomly substituted by missing values

## Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari

#### References

Ferrari P.A., Annoni P., Barbiero A., Manzi G. (2011) An imputation method for categorical variables with application to nonlinear principal component analysis, Computational Statistics & Data Analysis, vol. 55, issue 7, pages 2410-2420, http://www.sciencedirect.com/science/article/pii/S0167947311000521

8 missingmat2

#### **Examples**

```
library (mvtnorm)
set.seed(1)
# correlation matrix
sigma < -matrix(c(1,0.5,0.5,0.5,0.5,1,0.5,0.5,0.5,1,0.5,0.5,1,0.5,0.5,0.5,0.5,1),4,4)
# generate a n*m matrix from a multivariate normal
n < -500
m < -4
matc<-rmvnorm(n, mean=rep(0,m), sigma=sigma)</pre>
# transform the numerical values into ordinal categories (Likert scale)
# obtaining matrix mato
mato<-transfmatcat(matc,c(2,3,4,5))</pre>
# set the number of desired missing values
nummissing<-150
# create the random missing values
# random missing values
matc<-missingmat(mato, nummissing, pattern= "r")</pre>
\# random blocks of missing values on variables 1,2 and 3
matc < -missing mat (mato, nummissing, pattern= "b", <math>nk=c(2,3))
\# missing values on lowest category of variable 4
matl<-missingmat(mato, nummissing, pattern= "1", nk=4, p=0.1)</pre>
matl
# not at random missing values on variable 4
matn<-missingmat (mato, nummissing, pattern= "n", nk=4, w=4)
```

missingmat2

Random generation of missing values

## Description

Random generation of missing values in matrices

## Usage

```
missingmat2(mat, missing)
```

## **Arguments**

```
mat a matrix (n rows, m columns)

missing a vector: element i contains the desired number of rows with i missing values (1<=i<=m)
```

## Value

a matrix with the specified pattern of missing values

## Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari

missingness 9

#### See Also

```
missingmat, missingness
```

#### **Examples**

```
mat<-matrix(rnorm(500),100,5)
# if you want 20 rows with 1 missing, 10 rows with 2 missing, 4 rows with 3 missing, 1 ro
missing<-c(20,10,4,1)
matm<-missingmat2(mat, missing)
matm
# check that the function works
missingness(matm)</pre>
```

missingness

Missing values

## Description

Summary for the missing values in a matrix

#### Usage

```
missingness (mat)
```

#### **Arguments**

mat

a matrix/dataframe with missing values

## **Details**

The function provides a summary for the missing values in a matrix (units for variables)

#### Value

## Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari

```
n<-100
m<-3
mat<-matrix(rnorm(n*m),n,m)
nummissing<-50
index<-sample(n*m,nummissing,replace=FALSE)
mat[index]<-NA
missingness(mat)</pre>
```

10 modeimp

modeimp

Mode imputation

## **Description**

Mode imputation

#### Usage

```
modeimp(mat)
```

## **Arguments**

mat

A matrix of categorical or ordinal values, coded as integer values (1, 2, 3, ...)

## **Details**

The function implements the mode imputation on a matrix of categorical or ordinal data with missing values. The function substitutes to each missing value the mode of the corresponding variable.

#### Value

The imputed matrix

## Author(s)

Alessandro barbiero, Giancarlo Manzi, Pier Alda Ferrari

## See Also

```
medianimp, modeimp
```

```
set.seed(1)
n<-10
m<-3
mat<-matrix(ceiling(runif(n*m)*4),n,m)
matm<-mat
matm[1,3]<-NA
matm[9:10,1]<-NA
# matrix with missing values
matm
# imputed matrix
modeimp(mat)
# original matrix with no missing values
mat</pre>
```

rancatmat 11

rancatmat

Generating a random matrix of ordinal variables

## Description

The function generates a random matrix of integer (ordinal) variables, with independent and uniform marginal distributions

## Usage

```
rancatmat(n, m, cat = 3)
```

## **Arguments**

n number of rows/units

m number of columns, variables

cat number of categories for each variable

## **Details**

The function generates a random matrix of integer (ordinal) variables (coded with 1, 2, 3...), with independent and uniform marginal distributions

#### Value

a matrix of ordinal values

#### Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pieralda Ferrari

#### See Also

```
transfmatcat
```

```
n<-500
m<-3
mat<-rancatmat(n,m,c(3,4,5))
# let's check the marginal distributions...
apply(mat,2,tabulate)
#... should be "quite" uniform</pre>
```

12 transfmatcat

## Description

The function transforms a matrix of continuous numerical values into a matrix of integer (ordinal) values, with uniform marginal distributions and the desired number of categories

## Usage

```
transfmatcat(mat, cat = 3)
```

## **Arguments**

mat a matrix or a dataframe

the number of categories, one for each column/variable of the matrix/dataframe

#### **Details**

The function converts the matrix in input, containing continuous numerical values, into a matrix of ordinal values (1,2,3,... i.e.: Likert scale) according to the cat-1 normal quantiles corresponding to each variable (column) of mat.

#### Value

the matrix of ordinal values

#### Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari

#### References

Ferrari P.A., Barbiero A., Manzi G.: Handling missing data in presence of ordinal variables: a new imputation procedure. In "New Perspectives in Statistical Modeling and Data Analysis", S. Ingrassia, R. Rocci, M. Vichi, Eds., Springer, 2011

Ferrari P.A., Annoni P., Barbiero A., Manzi G. (2011) An imputation method for categorical variables with application to nonlinear principal component analysis, Computational Statistics & Data Analysis, vol. 55, issue 7, pages 2410-2420, http://www.sciencedirect.com/science/article/pii/S0167947311000521

#### See Also

rancatmat

vcosw 13

#### **Examples**

```
# generate a 40*3 matrix from a multivariate normal r.v.

# whose independent components have mean 10 and standard deviation 4

mat<-matrix(rnorm(40,3),10,4)

# transform the matrix of normal data into a matrix of ordinal data

transfmatcat(mat, cat=c(2,3,4,3))
```

VCOSW

Cosine of the angle between two vectors

## Description

The function calculates the cosine of the angle between two vectors, defined as the inner product of the vectors divided by the product of their euclidean norms

#### Usage

```
vcosw(v, w)
```

## **Arguments**

```
v a vector
w a vector, of the same length of v
```

#### Value

The cosine of the angle between the two vectors

## Author(s)

Alessandro Barbiero, Giancarlo Manzi, Pier Alda Ferrari

#### See Also

Ferrari P.A., Annoni P., Barbiero A., Manzi G. (2011) An imputation method for categorical variables with application to nonlinear principal component analysis, Computational Statistics & Data Analysis, vol. 55, issue 7, pages 2410-2420, http://www.sciencedirect.com/science/article/pii/S0167947311000521

```
a<-1:10
b<-2:11
vcosw(a,b)
#
e<-c(1,2,3)
f<-c(3,-3,1)
vcosw(e,f)
# e and f are orthogonal vectors!</pre>
```

## **Index**

```
*Topic datagen
    ForImp, 3
    ld, 4
    meanimp, 5
    medianimp, 6
    missingmat, 7
    {\tt missingmat2,8}
    missingness, 9
    modeimp, 10
    rancatmat, 11
    transfmatcat, 12
    vcosw, 13
*Topic multivariate
    ForImp, 3
    ld, 4
    meanimp, 5
    medianimp, 6
    {\tt missingmat}, {\color{red} 7}
    missingmat2,8
    missingness, 9
    {\tt modeimp}, {\tt 10}
    rancatmat, 11
    transfmatcat, 12
    vcosw, 13
*Topic package
    ForImp-package, 2
ForImp, 3
ForImp-package, 2
1d, 4
meanimp, 3, 4, 5, 6
medianimp, 3-5, 6, 10
missingmat, 7,9
missingmat2,8
{\tt missingness}, {\color{red} 9}, {\color{gray} 9}
modeimp, 3-6, 10, 10
rancatmat, 11, 12
transfmatcat, 11, 12
vcosw, 13
```