# Package 'OncoBayes2'

May 2, 2022

```
Type Package
Title Bayesian Logistic Regression for Oncology Dose-Escalation Trials
Description Bayesian logistic regression model with optional
                   EXchangeability-NonEXchangeability parameter modelling for flexible
                   borrowing from historical or concurrent data-sources. The safety model
                   can guide dose-escalation decisions for adaptive oncology Phase I
                   dose-escalation trials which involve an arbitrary number of
                   drugs. Please refer to Neuenschwander et al. (2008)
                   <a href="https://doi:10.1002/sim.3230"><a href="https://doi:10.1002/sim.3230">><a href="https://doi:10.1002/
                   <doi:10.1080/19466315.2016.1174149> for details on the methodology.
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Imports methods,
                   Rcpp (>= 0.12.0),
                   RcppParallel (>= 5.0.1),
                   rstan (>= 2.19.3),
                   rstantools (\geq 2.1.1),
                   assertthat (\geq 0.2.1),
                   checkmate,
                   Formula,
                   bayesplot (>= 1.4.0),
                   ggplot2 (>= 2.2.1),
                   dplyr (>= 0.8.0),
                   tibble,
                   tidyr (>= 1.0.0),
                   abind,
                   scales,
                   rlang (>= 0.3.0),
                   tidyselect,
                   utils,
                   stats
LinkingTo BH (>= 1.72.0),
                   Rcpp (>= 0.12.0),
```

```
RcppEigen (>= 0.3.3.3.0),
     RcppParallel (>= 5.0.1),
     rstan (>= 2.19.3),
     StanHeaders (\geq 2.19.0)
License GPL (>=3)
LazyData true
NeedsCompilation yes
Suggests rmarkdown,
     knitr,
     testthat (>= 2.0.0),
     mvtnorm,
     vdiffr,
     cmdstanr (>= 0.4.0)
VignetteBuilder knitr
Biarch true
SystemRequirements GNU make, pandoc (>= 1.12.3), pandoc-citeproc
Encoding UTF-8
RoxygenNote 7.1.1
```

# **R** topics documented:

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bind\_rows\_0

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bind\_rows\_0

Bind rows of multiple data frames with zero fill

## **Description**

A version of bind\_rows out of dplyr that fills non-common columns with zeroes instead of NA. Gives an error if any of the input data contains NA already.

## Usage

```
bind_rows_0(...)
```

## **Arguments**

... Data frames to combine, passed into bind\_rows (see dplyr documentation)

blrm\_exnex

Bayesian Logistic Regression Model for N-compounds with EXNEX

## Description

Bayesian Logistic Regression Model (BLRM) for N compounds using EXchangability and NonEXchangability (EXNEX) modeling.

## Usage

```
blrm_exnex(
  formula,
  data,
  prior_EX_mu_mean_comp,
  prior_EX_mu_sd_comp,
  prior_EX_tau_mean_comp,
  prior_EX_tau_sd_comp,
 prior_EX_corr_eta_comp,
  prior_EX_mu_mean_inter,
  prior_EX_mu_sd_inter,
  prior_EX_tau_mean_inter,
  prior_EX_tau_sd_inter,
  prior_EX_corr_eta_inter,
  prior_is_EXNEX_inter,
  prior_is_EXNEX_comp,
  prior_EX_prob_comp,
  prior_EX_prob_inter,
  prior_NEX_mu_mean_comp,
  prior_NEX_mu_sd_comp,
  prior_NEX_mu_mean_inter,
  prior_NEX_mu_sd_inter,
  prior_tau_dist,
  iter = getOption("OncoBayes2.MC.iter", 2000),
  warmup = getOption("OncoBayes2.MC.warmup", 1000),
  save_warmup = getOption("OncoBayes2.MC.save_warmup", TRUE),
  thin = getOption("OncoBayes2.MC.thin", 1),
  init = getOption("OncoBayes2.MC.init", 0.5),
  chains = getOption("OncoBayes2.MC.chains", 4),
  cores = getOption("mc.cores", 1L),
  control = getOption("OncoBayes2.MC.control", list()),
  backend = getOption("OncoBayes2.MC.backend", "rstan"),
  prior_PD = FALSE,
  verbose = FALSE
)
## S3 method for class 'blrmfit'
print(x, ..., prob = 0.95, digits = 2)
```

#### **Arguments**

formula

the model formula describing the linear predictors of the model. The lhs of the formula is a two-column matrix which are the number of occured events and the number of times no event occured. The rhs of the formula defines the linear predictors for the marginal models for each drug component, then the interaction model and at last the grouping and optional stratum factors of the models. These elements of the formula are separated by a vertical bar. The marginal models must follow a intercept and slope form while the interaction model must not include an interaction term. See the examples below for an example instantiation.

data

optional data frame containing the variables of the model. If not found in data, the variables are taken from environment(formula).

prior\_EX\_mu\_mean\_comp, prior\_EX\_mu\_sd\_comp

Mean and sd for the prior on the mean parameters  $\mu_i = (\mu_{\alpha i}, \mu_{\beta i})$  of each component. Two column matrix (intercept, log-slope) with one row per component.

prior\_EX\_tau\_mean\_comp, prior\_EX\_tau\_sd\_comp

Prior mean and sd for heterogeniety parameter  $\tau_{si} = (\tau_{\alpha si}, \tau_{\beta si})$  of each stratum. If no differential discounting is required (i.e. if there is only one stratum s=1), then it is a two-column matrix (intercept, log-slope) with one row per component. Otherwise it is a three-dimensional array whose first dimension indexes the strata, second dimension indexes the components, and third dimension of length two for (intercept, log-slope).

prior\_EX\_corr\_eta\_comp

Prior LKJ correlation parameter for each component given as numeric vector. If missing, then a 1 is assumed corresponding to a marginal uniform prior of the correlation.

prior\_EX\_mu\_mean\_inter, prior\_EX\_mu\_sd\_inter

Prior mean and sd for population mean parameters  $\mu_{\eta k}$  of each interaction parameter. Vector of length equal to the number of interactions.

prior\_EX\_tau\_mean\_inter, prior\_EX\_tau\_sd\_inter

Prior mean and sd for heterogeniety parameter  $\tau_{\eta sk}$  of each stratum. Matrix with one column per interaction and one row per stratum.

prior\_EX\_corr\_eta\_inter

Prior LKJ correlation parameter for interaction given as numeric. If missing, then a 1 is assumed corresponding to a marginal uniform prior of the correlations.

prior\_is\_EXNEX\_inter

Defines if non-exchangability is admitted for a given interaction parameter. Logical vector of length equal to the number of interactions. If missing FALSE is assumed for all interactions.

prior\_is\_EXNEX\_comp

Defines if non-exchangability is admitted for a given component. Logical vector of length equal to the number of components. If missing TRUE is assumed for all components.

prior\_EX\_prob\_comp

Prior probability  $p_{ij}$  for exchangability of each component per group. Matrix with one column per component and one row per group. Values must lie in [0-1] range.

prior\_EX\_prob\_inter

Prior probability  $p_{\eta kj}$  for exchangability of each interaction per group. Matrix with one column per interaction and one row per group. Values must lie in [0-1] range.

prior\_NEX\_mu\_mean\_comp, prior\_NEX\_mu\_sd\_comp

Prior mean  $m_{ij}$  and sd  $s_{ij} = \text{diag}(S_{ij})$  of each component for non-exchangable case. Two column matrix (intercept, log-slope) with one row per component. If missing set to the same prior as given for the EX part. It is required that the specification be the same across groups j.

prior\_NEX\_mu\_mean\_inter, prior\_NEX\_mu\_sd\_inter

Prior mean  $m_{\eta kj}$  and sd  $s_{\eta kj}$  for each interaction parameter for non-exchangable case. Vector of length equal to the number of interactions. If missing set to the same prior as given for the EX part.

prior\_tau\_dist Defines the distribution used for heterogeniety parameters. Choices are 0=fixed

to it's mean, 1=log-normal, 2=truncated normal.

iter number of iterations (including warmup).

warmup number of warmup iterations.

save\_warmup samples (TRUE / FALSE). Only if set to TRUE, then all random vari-

ables are saved in the posterior. This substantially increases the storage needs of

the posterior.

thin period of saving samples.

init positive number to specify uniform range on unconstrained space for random

initialization. See stan.

chains number of Markov chains.

cores number of cores for parallel sampling of chains.
control additional sampler parameters for NuTS algorithm.

backend sets Stan backend to be used. Possible choices are "rstan" (default) or "cmdstanr".

prior\_PD Logical flag (defaults to FALSE) indicating if to sample the prior predictive dis-

tribution instead of conditioning on the data.

verbose Logical flag (defaults to FALSE) controlling if additional output like stan progress

is reported.

x blrmfit object to print
... not used in this function

prob central probability mass to report, i.e. the quantiles 0.5-prob/2 and 0.5+prob/2

are displayed. Multiple central widths can be specified.

digits number of digits to show

#### Details

blrm\_exnex is a flexible function for Bayesian meta-analytic modeling of binomial count data. In particular, it is designed to model counts of the number of observed dose limiting toxicities (DLTs) by dose, for guiding dose-escalation studies in Oncology. To accommodate dose escalation over more than one agent, the dose may consist of combinations of study drugs, with any number of treatment components.

In the simplest case, the aim is to model the probability  $\pi$  that a patient experiences a DLT, by complementing the binomial likelihood with a monotone logistic regression

$$logit \pi(d) = log \alpha + \beta t(d),$$

where  $\beta > 0$ . Most typically, d represents the dose, and t(d) is an appropriate transformation, such as  $t(d) = \log(d/d^*)$ . A joint prior on  $\theta = (\log \alpha, \log \beta)$  completes the model and ensures monotonicity  $\beta > 0$ .

Many extensions are possible. The function supports general combination regimens, and also provides framework for Bayesian meta-analysis of dose-toxicity data from multiple historical and concurrent sources.

For an example of a single-agent trial refer to example-single-agent.

#### Value

The function returns a S3 object of type blrmfit.

#### Methods (by generic)

• print: print function.

#### Combination of two treatments

For a combination of two treatment components, the basic modeling framework is that the DLT rate  $\pi(d_1,d_2)$  is comprised of (1) a "no-interaction" baseline model  $\tilde{\pi}(d_1,d_2)$  driven by the single-agent toxicity of each component, and (2) optional interaction terms  $\gamma(d_1,d_2)$  representing synergy or antagonism between the drugs. On the log-odds scale,

$$logit \pi(d_1, d_2) = logit \tilde{\pi}(d_1, d_2) + \eta \gamma(d_1, d_2).$$

The "no interaction" part  $\tilde{\pi}(d_1, d_2)$  represents the probability of a DLT triggered by either treatment component acting *independently*. That is,

$$\tilde{\pi}(d_1, d_2) = 1 - (1 - \pi_1(d_1))(1 - \pi_2(d_2)).$$

In simple terms, P(no DLT for combination) = P(no DLT for drug 1) \* P(no DLT from drug 2). To complete this part, the treatment components can then be modeled with monotone logistic regressions as before.

$$logit \pi_i(d_i) = log \alpha_i + \beta_i t(d_i),$$

where  $t(d_i)$  is a monotone transformation of the doses, such as  $t(d_i) = \log(d_i/d_i^*)$ .

The inclusion of an interaction term  $\gamma(d_1,d_2)$  allows DLT rates above or below the "no-interaction" rate. The magnitude of the interaction term may also be made dependent on the doses (or other covariates) through regression. As an example, one could let

$$\gamma(d_1, d_2) = \frac{d_1}{d_1^*} \frac{d_1}{d_2^*}.$$

The specific functional form is specified in the usual notation for a design matrix. The interaction model must respect the constraint that whenever any dose approaches zero, then the interaction term must vanish as well. Therefore, the interaction model must not include an intercept term which would violate this consistency requirement. A dual combination example can be found in example-combo2.

#### General combinations

The model is extended to general combination treatments consisting of N components by expressing the probability  $\pi$  on the logit scale as

$$\operatorname{logit} \pi(d_1, \dots, d_N) = \operatorname{logit} \left( 1 - \prod_{i=1}^N (1 - \pi_i(d_i)) \right) + \sum_{k=1}^K \eta_k \, \gamma_k(d_1, \dots, d_N),$$

Multiple drug-drug interactions among the N components are now possible, and are represented through the K interaction terms  $\gamma_k$ .

Regression models can be again be specified for each  $\pi_i$  and  $\gamma_k$ , such as

$$logit \pi_i(d_i) = log \alpha_i + \beta_i t(d_i)$$

Interactions for some subset  $I(k) \subset \{1, ..., N\}$  of the treatment components can be modeled with regression as well, for example on products of doses,

$$\gamma_k(d_1,\ldots,d_N) = \prod_{i \in I(k)} \frac{d_i}{d_i^*}.$$

For example,  $I(k) = \{1, 2, 3\}$  results in the three-way interaction term

$$\frac{d_1}{d_1^*} \frac{d_2}{d_2^*} \frac{d_3}{d_3^*}$$

for drugs 1, 2, and 3.

For a triple combination example please refer to example-combo3.

#### Meta-analytic framework

Information on the toxicity of a drug may be available from multiple studies or sources. Furthermore, one may wish to stratify observations within a single study (for example into groups of patients corresponding to different geographic regions, or multiple dosing dose\_info corresponding to different schedules).

blrm\_exnex provides tools for robust Bayesian hierarchical modeling to jointly model data from multiple sources. An additional index  $j=1,\ldots,J$  on the parameters and observations denotes the J groups. The resulting model allows the DLT rate to differ across the groups. The general N-component model becomes

$$\log \operatorname{it} \pi_j(d_1, \dots, d_N) = \operatorname{logit} \left( 1 - \prod_{i=1}^N (1 - \pi_{ij}(d_i)) \right) + \sum_{k=1}^K \eta_{kj} \, \gamma_k(d_1, \dots, d_N),$$

for groups  $j=1,\ldots,J$ . The component toxicities  $\pi_{ij}$  and interaction terms  $\gamma_k$  are modelled, as before, through regression. For example,  $\pi_{ij}$  could be a logistic regression on  $t(d_i) = \log(d_i/d_i^*)$  with intercept and log-slope  $\theta_{ij}$ , and  $\gamma_k$  regressed with coefficient  $\eta_{kj}$  on a product  $\prod_{i\in I(k)}(d_i/d_i^*)$  for some subset I(k) of components.

Thus, for  $j=1,\ldots,J$ , we now have group-specific parameters  $\boldsymbol{\theta}_{ij}=(\log \alpha_{ij},\log \beta_{ij})$  and  $\boldsymbol{\nu}_j=(\eta_{1j},\ldots,\eta_{Kj})$  for each component  $i=1,\ldots,N$  and interaction  $k=1,\ldots,K$ .

The structure of the prior on  $(\theta_{i1}, \dots, \theta_{iJ})$  and  $(\nu_1, \dots, \nu_J)$  determines how much information will be shared across groups j. Several modeling choices are available in the function.

• EX (Full exchangeability): One can assume the parameters are conditionally exchangeable given hyperparameters

$$\theta_{ij} \sim N(\mu_{\boldsymbol{\theta}i}, \Sigma_{\boldsymbol{\theta}i}),$$

independently across groups  $j=1,\ldots,J$  and treatment components  $i=1,\ldots,N$ . The covariance matrix  $\Sigma_{\theta i}$  captures the patterns of cross-group heterogeneity, and is parametrized with standard deviations  $\tau_{\theta i}=(\tau_{\alpha i},\tau_{\beta i})$  and the correlation  $\rho_i$ . Similarly for the interactions, the fully-exchangeable model is

$$oldsymbol{
u}_j \sim \mathrm{N}ig(oldsymbol{\mu_{
u}}, oldsymbol{\Sigma_{
u}}ig)$$

for groups  $j=1,\ldots,J$  and interactions  $k=1,\ldots,K$ , and the prior on the covariance matrix  $\Sigma_{\nu}$  captures the amount of heterogeneity expected in the interaction terms a-priori. The covariance is again parametrized with standard deviations  $(\tau_{\eta 1},\ldots,\tau_{\eta K})$  and its correlation matrix.

• Differential discounting: For one or more of the groups  $j=1,\ldots,J$ , larger deviations of  $\theta_{ij}$  may be expected from the mean  $\mu_i$ , or of the interactions  $\eta_{kj}$  from the mean  $\mu_{\eta,k}$ . Such differential heterogeneity can be modeled by mapping the groups  $j=1,\ldots,J$  to strata through  $s_j \in \{1,\ldots,S\}$ , and modifying the model specification to

$$oldsymbol{ heta}_{ij} \sim \mathrm{N}ig(oldsymbol{\mu}_{oldsymbol{ heta}i}, oldsymbol{\Sigma}_{oldsymbol{ heta}ij}ig),$$

where

$$\boldsymbol{\Sigma}_{\boldsymbol{\theta}ij} = \left( \begin{array}{cc} \tau_{\alpha s_{j}i}^{2} & \rho_{i}\tau_{\alpha s_{j}i}\tau_{\beta s_{j}i} \\ \rho_{i}\tau_{\alpha s_{j}i}\tau_{\beta s_{j}i} & \tau_{\beta s_{i}i}^{2} \end{array} \right).$$

For the interactions, the model becomes

$$u_j \sim \mathrm{N}(\mu_{\nu}, \Sigma_{\nu j}),$$

where the covariance matrix  $\Sigma_{\nu j}$  is modelled as stratum specific standard deviations  $(\tau_{\eta 1 s_j}, \ldots, \tau_{\eta K s_j})$  and a stratum independent correlation matrix. Each stratum  $s=1,\ldots,S$  then corresponds to its own set of standard deviations  $\tau$  leading to different discounting per stratum. Independent priors are specified for the component parameters  $\tau_{\alpha si}$  and  $\tau_{\beta si}$  and for the interaction parameters  $\tau_{\eta sk}$  for each stratum  $s=1,\ldots,S$ . Inference for strata s where the prior is centered on larger values of the  $\tau$  parameters will exhibit less shrinkage towards the the means,  $\mu_{\theta i}$  and  $\mu_{\nu}$  respectively.

• EXNEX (Partial exchangeability): Another mechansim for increasing robustness is to introduce mixture priors for the group-specific parameters, where one mixture component is shared across groups, and the other is group-specific. The result, known as an EXchangeable-NonEXchangeable (EXNEX) type prior, has a form

$$\theta_{ij} \sim p_{\theta ij} \, \mathrm{N}(\mu_{\theta i}, \Sigma_{\theta i}) + (1 - p_{\theta ij}) \, \mathrm{N}(m_{\theta ij}, S_{\theta ij})$$

when applied to the treatment-component parameters, and

$$\boldsymbol{\nu}_{kj} \sim p_{\boldsymbol{\nu}_{kj}} \, \mathrm{N} \big( \mu_{\boldsymbol{\nu}}, \boldsymbol{\Sigma}_{\boldsymbol{\nu}} \big)_k + (1 - p_{\boldsymbol{\nu}_{kj}}) \, \mathrm{N} (m_{\boldsymbol{\nu}_{kj}}, s_{\boldsymbol{\nu}_{kj}}^2)$$

when applied to the interaction parameters. The exchangeability weights  $p_{\theta ij}$  and  $p_{\nu_{kj}}$  are fixed constants in the interval [0,1] that control the degree to which inference for group j is informed by the exchangeable mixture components. Larger values for the weights correspond to greater exchange of information, while smaller values increase robustness in case of outlying observations in individual groups j.

#### References

Neuenschwander, B., Roychoudhury, S., & Schmidli, H. (2016). On the use of co-data in clinical trials. *Statistics in Biopharmaceutical Research*, 8(3), 345-354.

Neuenschwander, B., Wandel, S., Roychoudhury, S., & Bailey, S. (2016). Robust exchangeability designs for early phase clinical trials with multiple strata. *Pharmaceutical statistics*, 15(2), 123-134.

Neuenschwander, B., Branson, M., & Gsponer, T. (2008). Critical aspects of the Bayesian approach to phase I cancer trials. *Statistics in medicine*, 27(13), 2420-2439.

Neuenschwander, B., Matano, A., Tang, Z., Roychoudhury, S., Wandel, S. Bailey, Stuart. (2014). A Bayesian Industry Approach to Phase I Combination Trials in Oncology. In *Statistical methods in drug combination studies* (Vol. 69). CRC Press.

blrm\_formula\_linear 11

```
# summary of posterior for DLT rate by dose for new set of covariate levels
newdata <- expand.grid(</pre>
  stratum_id = "BID", group_id = "Combo",
  drug_A = 400, drug_B = 800, drug_C = c(320, 400, 600, 800),
  stringsAsFactors = FALSE
)
summ_pred <- summary(blrmfit, newdata = newdata, interval_prob = c(0, 0.16, 0.33, 1))</pre>
print(cbind(newdata, summ_pred))
# update the model after observing additional data
newdata$num_patients <- rep(3, nrow(newdata))</pre>
newdatanum_toxicities <- c(0, 1, 2, 2)
library(dplyr)
blrmfit_new <- update(blrmfit,</pre>
                       data = rbind(hist_combo3, newdata) %>%
                                arrange(stratum_id, group_id))
# updated posterior summary
summ_upd <- summary(blrmfit_new, newdata = newdata, interval_prob = c(0, 0.16, 0.33, 1))
print(cbind(newdata, summ_upd))
## Recover user set sampling defaults
options(.user_mc_options)
```

blrm\_formula\_linear

Build a BLRM formula with linear interaction term in logit-space

#### Description

blrm\_formula\_linear is a convenience function for generating a formula for blrm\_trial and blrm\_exnex with an interaction of the form:

$$\eta \prod_{i=1}^{N} (d_i/d_i^*))$$

## Usage

```
blrm_formula_linear(
  ref_doses,
  max_interaction_level = 2,
  specific_interaction_terms = NULL
)
```

#### **Arguments**

ref\_doses Numeric vector of reference doses with names corresponding to drug names max\_interaction\_level

Highest interaction order to consider [1 - Inf]. Default: 2

```
specific_interaction_terms
List of custom interaction terms to generate (e.g. list(c("drug1"
```

List of custom interaction terms to generate (e.g. list(c("drug1", "drug2"), c("drug1", "drug3"))). Default: NULL

#### Value

The function returns an object of class blrm\_formula.

# Examples

```
ref_doses <- c(drug_A=10, drug_B=20)
# can be used with blrm_trial
blrm_formula_linear(ref_doses)</pre>
```

blrm\_formula\_saturating

Build a BLRM formula with saturating interaction term in logit-space

## **Description**

blrm\_formula\_saturating is a convenience function for generating a formula for blrm\_trial and blrm\_exnex with an interaction of the form:

$$2\eta \frac{\prod_{i=1}^{N} (d_i/d_i^*)}{1 + \prod_{i=1}^{N} (d_i/d_i^*)}$$

## Usage

```
blrm_formula_saturating(
  ref_doses,
  max_interaction_level = 2,
  specific_interaction_terms = NULL
)
```

#### **Arguments**

Highest interaction order to consider [1 - Inf]. Default: 2

specific\_interaction\_terms

List of custom interaction terms to generate (e.g. list(c("drug1", "drug2"), c("drug1", "drug3"))). Default: NULL

#### Value

The function returns an object of class blrm\_formula.

#### **Examples**

```
ref_doses <- c(drug_A=10, drug_B=20)
# can be used with blrm_trial
blrm_formula_saturating(ref_doses)</pre>
```

blrm\_trial

Dose-Escalation Trials guided by Bayesian Logistic Regression Model

### **Description**

blrm\_trial facilitates the conduct of dose escalation studies guided by Bayesian Logistic Regression Models (BLRM). While the blrm\_exnex only fits the BLRM model to data, the blrm\_trial function standardizes the specification of the entire trial design and provides various standardized functions for trial data accrual and derivation of model summaries needed for dose-escalation decisions.

## Usage

```
blrm_trial(
  data,
  dose_info,
  drug_info,
  simplified_prior = FALSE,
  EXNEX\_comp = FALSE,
  EX_prob_comp_hist = 1,
  EX_prob_comp_new = 0.8,
  EXNEX_inter = FALSE,
  EX_prob_inter = 1,
  formula_generator = blrm_formula_saturating,
  interval_prob = c(0, 0.16, 0.33, 1),
 interval_max_mass = c(prob_underdose = 1, prob_target = 1, prob_overdose = 0.25),
)
## S3 method for class 'blrm_trial'
print(x, ...)
```

#### Arguments

data dose-toxicity data available at design stage of trial

dose\_info specificaion of the dose levels as planned for the ongoing trial arms.

drug\_info specification of drugs used in trial arms.

simplified\_prior

logical (defaults to FALSE) indicating whether a simplified prior should be employed based on the reference\_p\_dlt values provided in drug\_info. **Warning:** The simplified prior will change between releases. Please read instructions below in the respective section for the simplified prior.

EXNEX\_comp

logical (default to TRUE) indicating whether EXchangeable-NonEXchangeable priors should be employed for all component parameters

EX\_prob\_comp\_hist

prior weight ([0,1], default to 1) on exchangeability for the component parameters in groups representing historical data

EX\_prob\_comp\_new

prior weight ([0,1], default to 0.8) on exchangeability for the component parameters in groups representing new or concurrent data

EXNEX\_inter

logical (default to FALSE) indicating whether EXchangeable-NonEXchangeable priors should be employed for all interaction parameters

EX\_prob\_inter

prior weight ([0,1], defaults to 0.8) on exchangeability for the interaction parameters

formula\_generator

formula generation function (see for example blrm\_formula\_linear or blrm\_formula\_saturating). The formula generator defines the employed interaction model.

interval\_prob

defines the interval probabilities reported in the standard outputs. Defaults to c(0,0.16,0.33,1).

interval\_max\_mass

named vector defining for each interval of the interval\_prob vector a maxmimal admissable probability mass for a given dose level. Whenever the posterior probability mass in a given interval exceeds the threshold, then the Escalation With Overdose Control (EWOC) criterion is considered to be not fullfilled. Dose levels not fullfilling EWOC are ineligible for the next cohort of patients. The default restricts the overdose probability to less than 0.25.

Additional arguments are forwarded to blrm\_exnex, i.e. for the purpose of prior specification.

x blrm\_trial object to print

#### **Details**

blrm\_trial constructs an object of class blrm\_trial which stores the compelte information about the study design of a dose-escalation trial. The study design is defined through the data sets (see sections below for a definition of the columns):

data (historical data) The data argument defines available dose-toxicity data at the design stage of the trial. Together with the prior of model (without any data) this defines the prior used for the trial conduct.

**dose\_info** Definition of the pre-specified dose levels explored in the ongoing trial arms. Thus, all dose-toxcitiy trial data added to the object is expected correspond to one of the dose levels in the pre-defined set of dose\_info.

**drug\_info** Determines the drugs used in the trial, their units, reference dose level and optionally defines the expected probability for a toxicity at the reference dose.

Once the blrm\_trial object is setup the complete trial design is specified and the model is fitted to the given data. This allows evaluation of the pre-specified dose levels of the trial design wrt. to safety, i.e. whether the starting dose of the trial fullfills the escalate with overdose criterion (EWOC) condition.

The blrm\_trial trial can also be constructed in a 2-step process which allows for a more convenient specification of the prior since meta data like number of drugs and the like can be used. See the example section for details.

After setup of the initial blrm\_trial object additional data is added through the use of the update method which has a add\_data argument intended to add data from the ongoing trial. The summary function finally allows to extract various model summaries. In particular, the EWOC criterion can be calculated for the pre-defined dose levels of the trial.

#### Value

The function returns an object of class blrm\_trial.

#### Methods (by generic)

• print: print function.

## Simplified prior

As a convenience for the user, a simplified prior can be specifed whenever the reference\_p\_dlt column is present in the drug\_info data set. However, the user is **warned** that the simplified prior will change in future releases of the package and thus **we strongly discourage the use of the simplified prior for setting up trial designs**. The functionality is intended to provide the user a quick start and as a starting point. The actually instantiated prior can be seen as demonstrated below in the examples.

## Input data

The data given to the data argument of blrm\_trial is considered as the available at design stage of the trial. The collected input data thus does not necessarily need to have the same dose levels as the pre-specified dose\_info for the ongoing trial(s). It's data columns must include, but are not limited to:

group\_id study

stratum\_id optional, only required for differential discounting of groups

num\_patients number of patients

num\_toxicities number of toxicities

**drug\_A** Columns for the dose of each treatment component, with column names matching the drug\_name values specified in the drug\_info argument of blrm\_trial

## Drug info data

The drug information data-set defines drug properties. The fields included are:

drug\_name name of drug which is also used as column name for the dose

```
dose_ref reference dose
dose_unit units used for drug amounts
reference_p_dlt optional; if provided, allows setup of a simplified prior
```

#### Dose info data

The drug\_info data-set pre-specifies the dose levels of the ongoing trial. Thus, all data added to the blrm\_trial through the update command must be consistent with the pre-defined dose levels as no other than those pre-specified ones can be explored in an ongoing trial.

**dose\_id** optional column which assigns a unique id to each group\_id/dose combination. If not specified the column is internally generated.

```
group_id study
```

drug\_A Columns for the dose of each treatment component, with column names matching the drug\_name values specified in the drug\_info argument of blrm\_trial

#### References

Babb, J., Rogatko, A., & Zacks, S. (1998). Cancer phase I clinical trials: efficient dose escalation with overdose control. *Statistics in medicine*, 17(10), 1103-1120.

Neuenschwander, B., Roychoudhury, S., & Schmidli, H. (2016). On the use of co-data in clinical trials. *Statistics in Biopharmaceutical Research*, 8(3), 345-354.

#### See Also

Other blrm\_trial combo2 example: dose\_info\_combo2, drug\_info\_combo2, example-combo2\_trial

```
## Setting up dummy sampling for fast execution of example
## Please use 4 chains and 100x more warmup & iter in practice
.user_mc_options <- options(OncoBayes2.MC.warmup=10, OncoBayes2.MC.iter=20, OncoBayes2.MC.chains=1,
                            OncoBayes2.MC.save_warmup=FALSE)
# construct initial blrm_trial object from built-in example datasets
combo2_trial_setup <- blrm_trial(</pre>
 data = hist_combo2,
 dose_info = dose_info_combo2,
 drug_info = drug_info_combo2,
 simplified_prior = TRUE
)
# extract blrm_call to see setup of the prior as passed to blrm_exnex
summary(combo2_trial_setup, "blrm_exnex_call")
# Warning: The simplified prior will change between releases!
# please refer to the combo2_trial example for a complete
# example. You can obtain this example with
# ?example-combo2_trial
```

codata\_combo2

```
# or by running
# example_model("combo2_trial")

## Recover user set sampling defaults
options(.user_mc_options)
```

codata\_combo2

Dataset: historical and concurrent data on a two-way combination

## **Description**

One of two datasets from the application described in Neuenschwander et al (2016). In the study trial\_AB, the risk of DLT was studied as a function of dose for two drugs, drug A and drug B. Historical information on the toxicity profiles of these two drugs is available from single agent trials trial\_A and trial\_B. Another study IIT was run concurrently to trial\_AB, and studies the same combination. A second dataset hist\_combo2 is available from this example, which includes only the data from the single agent studies, prior to the initiation of trial\_AB and IIT.

## Usage

codata\_combo2

## Format

A data frame with 20 rows and 5 variables:

```
group_id study
drug_A dose of Drug A
drug_B dose of Drug B
num_patients number of patients
num_toxicities number of DLTs
cohort_time cohort number of patients
```

#### References

Neuenschwander, B., Roychoudhury, S., & Schmidli, H. (2016). On the use of co-data in clinical trials. *Statistics in Biopharmaceutical Research*, 8(3), 345-354.

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```
num_comp <- 2 # two investigational drugs</pre>
num_inter <- 1 # one drug-drug interaction needs to be modeled</pre>
num_groups <- nlevels(codata_combo2$group_id) # no stratification needed</pre>
num_strata <- 1 # no stratification needed</pre>
blrmfit <- blrm_exnex(</pre>
  cbind(num_toxicities, num_patients - num_toxicities) ~
      1 + I(log(drug_A / dref[1])) |
      1 + I(log(drug_B / dref[2])) |
      0 + I(drug_A/dref[1] *drug_B/dref[2]) |
      group_id,
  data = codata_combo2,
  prior_EX_mu_mean_comp = matrix(
     c(logit(0.2), 0, \# hyper-mean of (intercept, log-slope) for drug A
       logit(0.2), 0), # hyper-mean of (intercept, log-slope) for drug B
       nrow = num_comp,
       ncol = 2,
       byrow = TRUE
      ),
  prior_EX_mu_sd_comp = matrix(
     c(2.0, 1, # hyper-sd of mean mu for (intercept, log-slope) for drug A
       2.0, 1), # hyper-sd of mean mu for (intercept, log-slope) for drug B
       nrow = num_comp,
       ncol = 2,
       byrow = TRUE
      ),
  prior_EX_tau_mean_comp = matrix(
     c(\log(0.25), \log(0.125),
       log(0.25), log(0.125)),
       nrow = num_comp,
       ncol = 2,
       byrow = TRUE
      ),
  prior_EX_tau_sd_comp = matrix(
     c(log(4) / 1.96, log(4) / 1.96,
       log(4) / 1.96, log(4) / 1.96),
       nrow = num_comp,
       ncol = 2,
       byrow = TRUE
      ),
  prior_EX_mu_mean_inter = 0,
  prior_EX_mu_sd_inter = 1.121,
  prior_EX_tau_mean_inter = matrix(log(0.125), nrow = num_inter, ncol = num_strata),
  prior_EX_tau_sd_inter = matrix(log(4) / 1.96, nrow = num_inter, ncol = num_strata),
  prior_is_EXNEX_comp = rep(FALSE, num_comp),
  prior_is_EXNEX_inter = rep(FALSE, num_inter),
  prior_EX_prob_comp = matrix(1, nrow = num_groups, ncol = num_comp),
  prior_EX_prob_inter = matrix(1, nrow = num_groups, ncol = num_inter),
  prior_tau_dist = 1
## Recover user set sampling defaults
options(.user_mc_options)
```

critical\_quantile 19

critical\_quantile

Critical quantile

# Description

Calculates the critical value of a model covariate for which a fixed quantile of the crude rate is equal to the specified (tail or interval) probability. The specified quantile can relate to the posterior or the predictive distribution of the response rate.

## Usage

```
critical_quantile(object, ...)
## S3 method for class 'blrmfit'
critical_quantile(
  object,
  newdata,
  х,
  p,
  qc,
  lower.tail,
  interval.x,
  extendInt.x = c("auto", "no", "yes", "downX", "upX"),
  log.x,
  predictive = FALSE,
  maxiter = 100,
)
## S3 method for class 'blrm_trial'
critical_quantile(
  object,
  newdata,
  Х,
  p,
  qc,
  lower.tail,
  interval.x,
  extendInt.x = c("auto", "no", "yes", "downX", "upX"),
  log.x,
  predictive = FALSE,
 maxiter = 100,
)
```

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## **Arguments**

| object      | fitted model object  |
|-------------|--|
|             | not used in this function  |
| newdata     | optional data frame specifying for what to predict; if missing, then the data of the input model object is used  |
| X           | character giving the covariate name which is being search for to meet the critical conditions. This also supports 'tidy' parameter selection by specifying x = vars(), where is specified the same way as in dplyr::select() and similar functions. Examples of using x in this way can be found in the examples. For blrm_trial methods, it defaults to the first entry in summary(blrm_trial, "drug_info")\$drug_name. |
| p           | cumulative probability corresponding to the critical quantile range.   |
| qc          | if given as a sorted vector of length 2, then the two entries define the interval on the response rate scale which must correspond to the cumulative probability p. In this case lower.tail must be NULL or left missing. If qc is only a single number, then lower.tail must be set to complete the specification of the tail area.   |
| lower.tail  | defines if probabilities are lower or upper tail areas. Must be defined if qc is a single number and must not be defined if qc denotes an interval.  |
| interval.x  | interval the covariate x is searched. Defaults to the minimal and maximal value of x in the data set used. Whenever lower.tail is set such that it is known that a tail area is used, then the function will automatically attempt to enlarge the search interval since the direction of the inverted function is determined around the critical value.  |
| extendInt.x | controls if the interval given in interval.x should be extended during the root finding. The default "auto" attempts to guess an adequate setting in cases thats possible. Other possible values are the same as for the extendInt argument of the stats::uniroot() function.  |
| log.x       | determines if during the numerical search for the critical value the covariate space is logarithmized. By default x is log transformed whenever all values are positive.   |
| predictive  | logical indicates if the critical quantile relates to the posterior (FALSE) or the predictive (TRUE) distribution. Defaults to FALSE.  |
| maxiter     | maximal number of iterations for root finding. Defaults to 100.  |

## **Details**

The function searches for a critical value  $x_c$  of the covariate x (x) at which the integral over the model response in the specified interval  $\pi_1$  to  $\pi_2$  (qc) is equal to the given probability p (p). The given interval is considered a tail area when lower.tail is used such that  $\pi_1=0$  for TRUE and  $\pi_2=1$  for FALSE. At the critical value  $x_c$  the equality holds

$$p = \int_{\pi_1}^{\pi_2} p(\pi|x_c) \, d\pi.$$

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Note that a solution not guranteed to exist under all circumstances. However, for a single agent model and when requesting a tail probability then a solution does exist. In case an interval probability is specified, then the solution may not necessarily exist and the root finding is confined to the range specified in interval.x.

In case the solution is requested for the predictive distribution (predictive=TRUE), then the respective problem solved leads to the equality of

$$p = \sum_{y=r_1=\lceil n \, \pi_1 \rceil}^{r_2=\lceil n \, \pi_1 \rceil} \int p(y|\pi, n) \, p(\pi|x_c) \, d\pi.$$

Furthermore, the covariate space is log transformed by default whenever all values of the covariate x are positive in the data set. Values of 0 are shifted into the positive domain by the machine precision to avoid issues with an ill-defined  $\log(0)$ .

For blrm\_trial objects the default arguments for p, qc and lower.tail are set to correspond to the highest interval of interval\_prob to be constrained by the respective interval\_max\_mass (which are defined as part of the blrm\_trial objects). This will in the default case correspond to the EWOC metric. These defaults are only applied if p, qc and lower.tail are missing.

#### Value

Vector of length equal to the number of rows of the input data set with the critical value for the covariate specified as x which fullfills the requirements as detailled above. May return NA for cases where no solution is found on the specified interval interval.x.

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dose\_info\_combo2

Dataset: trial dose information for a dual-agent combination study

#### **Description**

The data set defines all pre-defined dose-levels which can be explored in the dual-agent example trial.

## Usage

```
dose_info_combo2
```

#### **Format**

An object of class tbl\_df (inherits from tbl, data.frame) with 42 rows and 4 columns.

#### **Details**

```
group_id studydrug_A drug A dose amountdrug_B drug B dose amountdose_id unique id of record
```

#### See Also

Other blrm\_trial combo2 example: blrm\_trial(), drug\_info\_combo2, example-combo2\_trial

drug\_info\_combo2

Dataset: drug information for a dual-agent combination study

## **Description**

Data set describing the two drugs involved in the example for a dual-agent combination study.

#### Usage

```
drug_info_combo2
```

## **Format**

A tibble with 2 rows (one per durg) and 4 columns:

```
drug_name name of drug
dose_ref reference dose
dose_unit units used for drug amounts
reference_p_dlt a-priori probability for a DLT at the reference dose
```

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#### See Also

Other blrm\_trial combo2 example: blrm\_trial(), dose\_info\_combo2, example-combo2\_trial

example-combo2

Two-drug combination example

#### **Description**

Example using a combination of two experimental drugs.

#### **Details**

The following example is described in the reference Neuenschwander, B. et al (2016). The data are described in the help page for codata\_combo2. In the study trial\_AB, the risk of DLT was studied as a function of dose for two drugs, drug A and drug B. Historical information on the toxicity profiles of these two drugs was available from single agent trials trial\_A and trial\_B. Another study IIT was run concurrently to trial\_AB, and studies the same combination.

The model described in Neuenschwander, et al (2016) is adapted as follows. For groups  $j = 1, \dots, 4$  representing each of the four sources of data mentioned above,

$$\operatorname{logit} \pi_{1j}(d_1) = \log \, \alpha_{1j} + \beta_{1j} \, \log \left( \frac{d_1}{d_1^*} \right),$$

and

$$\operatorname{logit} \pi_{2j}(d_2) = \log \, \alpha_{2j} + \beta_{2j} \, \log \left( \frac{d_2}{d_2^*} \right),$$

are logistic regressions for the single-agent toxicity of drugs A and B, respectively, when administered in group j. Conditional on the regression parameters  $\theta_{1j} = (\log \alpha_{1j}, \log \beta_{1j})$  and  $\theta_{2j} = (\log \alpha_{2j}, \log \beta_{2j})$ , the toxicity  $\pi_j(d_1, d_2)$  for the combination is modeled as the "no-interaction" DLT rate,

$$\tilde{\pi}_j(d_1, d_2) = 1 - (1 - \pi_{1j}(d_1))(1 - \pi_{2j}(d_2))$$

with a single interaction term added on the log odds scale,

$$\operatorname{logit} \pi_{j}(d_{1}, d_{2}) = \operatorname{logit} \tilde{\pi}_{j}(d_{1}, d_{2}) + \eta_{j} \frac{d_{1}}{d_{1}^{*}} \frac{d_{2}}{d_{2}^{*}}.$$

A hierarchical model across the four groups j allows dose-toxicity information to be shared through common hyperparameters.

For the component parameters  $\theta_{ij}$ ,

$$\theta_{ij} \sim \text{BVN}(\boldsymbol{\mu}_i, \boldsymbol{\Sigma}_i).$$

For the mean, a further prior is specified as

$$\boldsymbol{\mu}_i = (\mu_{\alpha i}, \mu_{\beta i}) \sim \text{BVN}(\boldsymbol{m}_i, \boldsymbol{S}_i),$$

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while in the manuscript the prior  $m_i = (\text{logit } 0.1, \log 1)$  and  $S_i = \text{diag}(3.33^2, 1^2)$  for each i = 1, 2 is used, we deviate here and use instead  $m_i = (\text{logit } 0.2, \log 1)$  and  $S_i = \text{diag}(2^2, 1^2)$ . For the standard deviations and correlation parameters in the covariance matrix,

$$oldsymbol{\Sigma}_i = \left(egin{array}{cc} au_{lpha i}^2 & 
ho_i au_{lpha i} au_{eta i} \ 
ho_i au_{lpha i} au_{eta i} & au_{eta i}^2 \end{array}
ight),$$

the specified priors are  $\tau_{\alpha i} \sim \text{Log-Normal}(\log 0.25, ((\log 4)/1.96)^2),$ 

$$\tau_{\beta i} \sim \text{Log-Normal}(\log 0.125, ((\log 4)/1.96)^2), \text{ and } \rho_i \sim \text{U}(-1, 1) \text{ for } i = 1, 2.$$

For the interaction parameters  $\eta_i$  in each group, the hierarchical model has

$$\eta_i \sim N(\mu_n, \tau_n^2),$$

for j = 1, ..., 4, with  $\mu_{\eta} \sim N(0, 1.121^2)$  and  $\tau_{\eta} \sim \text{Log-Normal}(\log 0.125, ((\log 4)/1.96)^2)$ .

Below is the syntax for specifying this fully exchangeable model in blrm\_exnex.

#### References

Neuenschwander, B., Roychoudhury, S., & Schmidli, H. (2016). On the use of co-data in clinical trials. *Statistics in Biopharmaceutical Research*, 8(3), 345-354.

```
## Setting up dummy sampling for fast execution of example
## Please use 4 chains and 100x more warmup & iter in practice
.user_mc_options <- options(OncoBayes2.MC.warmup=10, OncoBayes2.MC.iter=20, OncoBayes2.MC.chains=1,
                             OncoBayes2.MC.save_warmup=FALSE)
dref <- c(6, 960)
num_comp <- 2 # two investigational drugs</pre>
num_inter <- 1 # one drug-drug interaction needs to be modeled
num_groups <- nlevels(codata_combo2$group_id) # no stratification needed</pre>
num_strata <- 1 # no stratification needed
blrmfit <- blrm_exnex(</pre>
  cbind(num_toxicities, num_patients - num_toxicities) ~
      1 + I(log(drug_A / dref[1])) |
      1 + I(log(drug_B / dref[2])) |
      0 + I(drug_A/dref[1] *drug_B/dref[2]) |
      group_id,
  data = codata_combo2,
  prior_EX_mu_mean_comp = matrix(
     c(logit(0.2), 0, # hyper-mean of (intercept, log-slope) for drug A
       logit(0.2), 0), # hyper-mean of (intercept, log-slope) for drug B
       nrow = num_comp,
       ncol = 2,
       byrow = TRUE
      ),
  prior_EX_mu_sd_comp = matrix(
     c(2.0, 1, # hyper-sd of mean mu for (intercept, log-slope) for drug A
```

```
2.0, 1), # hyper-sd of mean mu for (intercept, log-slope) for drug B
       nrow = num_comp,
       ncol = 2,
       byrow = TRUE
     ),
 prior_EX_tau_mean_comp = matrix(
    c(\log(0.25), \log(0.125),
       log(0.25), log(0.125)),
       nrow = num_comp,
       ncol = 2,
       byrow = TRUE
     ),
 prior_EX_tau_sd_comp = matrix(
     c(log(4) / 1.96, log(4) / 1.96,
       log(4) / 1.96, log(4) / 1.96),
       nrow = num_comp,
       ncol = 2,
       byrow = TRUE
     ),
 prior_EX_mu_mean_inter = 0,
 prior_EX_mu_sd_inter = 1.121,
 prior_EX_tau_mean_inter = matrix(log(0.125), nrow = num_inter, ncol = num_strata),
 prior_EX_tau_sd_inter = matrix(log(4) / 1.96, nrow = num_inter, ncol = num_strata),
 prior_is_EXNEX_comp = rep(FALSE, num_comp),
 prior_is_EXNEX_inter = rep(FALSE, num_inter),
 prior_EX_prob_comp = matrix(1, nrow = num_groups, ncol = num_comp),
 prior_EX_prob_inter = matrix(1, nrow = num_groups, ncol = num_inter),
 prior_tau_dist = 1
## Recover user set sampling defaults
options(.user_mc_options)
```

example-combo2\_trial Two-drug combination example using BLRM Trial

#### **Description**

Example using blrm\_trial to guide the built-in two-drug combination study example.

#### **Details**

blrm\_trial is used to collect and store all relevant design information for the example. Subsequent use of the update.blrm\_trial command allows convenient model fitting via blrm\_exnex. The summary.blrm\_trial method allows exploration of the design and modeling results.

To run this example, use example\_model("combo2\_trial"). See example\_model.

#### See Also

Other blrm\_trial combo2 example: blrm\_trial(), dose\_info\_combo2, drug\_info\_combo2

```
## Setting up dummy sampling for fast execution of example
## Please use 4 chains and 100x more warmup & iter in practice
.user_mc_options <- options(OncoBayes2.MC.warmup=10, OncoBayes2.MC.iter=20, OncoBayes2.MC.chains=1,
                            OncoBayes2.MC.save_warmup=FALSE)
library(tibble)
library(dplyr)
library(tidyr)
# Combo2 example using blrm_trial functionality
# construct initial blrm_trial object from built-in example datasets
combo2_trial_setup <- blrm_trial(</pre>
  data = hist_combo2,
  dose_info = dose_info_combo2,
  drug_info = drug_info_combo2,
  simplified_prior = FALSE
)
dims <- summary(combo2_trial_setup, "dimensionality")</pre>
# Fit the initial model with the historical data and fully specified prior
combo2_trial_start <- update(</pre>
  combo2_trial_setup,
  prior_EX_mu_mean_comp = matrix(
    c(logit(0.2), 0, # hyper-mean of (intercept, log-slope) for drug A
      logit(0.2), 0), # hyper-mean of (intercept, log-slope) for drug B
   nrow = dims$num_components,
   ncol = 2,
   byrow = TRUE
  ),
  prior_EX_mu_sd_comp = matrix(
    c(2.0, 1, # hyper-sd of mean mu for (intercept, log-slope) for drug A
      2.0, 1), # hyper-sd of mean mu for (intercept, log-slope) for drug B
   nrow = dims$num_components,
   ncol = 2,
   byrow = TRUE
  ),
  prior_EX_tau_mean_comp = matrix(
    c(\log(0.25), \log(0.125),
     log(0.25), log(0.125)),
   nrow = dims$num_components,
   ncol = 2,
   byrow = TRUE
  prior_EX_tau_sd_comp = matrix(
   c(\log(4) / 1.96, \log(4) / 1.96,
      log(4) / 1.96, log(4) / 1.96),
    nrow = dims$num_components,
    ncol = 2,
    byrow = TRUE
```

```
),
 prior_EX_mu_mean_inter = 0,
 prior_EX_mu_sd_inter = 1.121,
 prior_EX_tau_mean_inter = matrix(log(0.125),
                                   nrow = dims$num_interaction_terms,
                                   ncol = dims$num_strata),
 prior_EX_tau_sd_inter = matrix(log(4) / 1.96,
                                 nrow = dims$num_interaction_terms,
                                 ncol = dims$num_strata),
 prior_is_EXNEX_comp = rep(FALSE, dims$num_components),
 prior_is_EXNEX_inter = rep(FALSE, dims$num_interaction_terms),
 prior_EX_prob_comp = matrix(1,
                              nrow = dims$num_groups,
                              ncol = dims$num_components),
 prior_EX_prob_inter = matrix(1,
                               nrow = dims$num_groups,
                               ncol = dims$num_interaction_terms),
 prior_tau_dist = 1
)
# print summary of prior specification
prior_summary(combo2_trial_start)
# summarize inference at observed dose levels
summary(combo2_trial_start, "data_prediction")
# summarize inference at specified dose levels
summary(combo2_trial_start, "dose_prediction")
# Update again with new data
# using update() with data argument supplied
# dem <- update(combo2_trial_start, data = codata_combo2)</pre>
# alternate way using update() with add_data argument for
# new observations only (those collected after the trial
# design stage).
new_data <- filter(codata_combo2, cohort_time > 0)
combo2_trial <- update(combo2_trial_start, add_data = new_data)</pre>
summary(combo2_trial, "data") # cohort_time is tracked
summary(combo2_trial, "data_prediction")
summary(combo2_trial, "dose_prediction")
rm(dims, new_data)
## Recover user set sampling defaults
options(.user_mc_options)
```

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example-combo3

Three-drug combination example

#### **Description**

Example using a combination of two experimental drugs, with EXNEX and differential discounting.

#### **Details**

This dataset involves a hypothetical dose-escalation study of combination therapy with three treatment components. From two previous studies HistAgent1 and HistAgent2, historical data is available on each of the treatments as single-agents, as well as two of the two-way combinations. However, due to a difference in treatment schedule between the Combo study and the historical studies, a stratification (through stratum\_id) is made between the groups to allow differential discounting of the alternate-schedule data. The association is as below.

| group_id (j):  | stratum_id (s_j): |
|----------------|-------------------|
| Combo (1)      | BID (1)           |
| HistAgent1 (2) | QD (2)            |
| HistAgent2 (3) | QD (2)            |

For additional robustness, EXNEX priors are used for all group-level treatment components while not for the interaction parameters. This is to limit the amount of borrowing in case of significant heterogeneity across groups.

The complete model is as follows. As a function of doses  $d_1, d_2, d_3$ , the DLT rate in group j is, for j = 1, ..., 3,

$$\operatorname{logit} \pi_j(d_1,d_2,d_3) = \operatorname{logit} \Bigl(1 - \prod_{i=1}^3 (1 - \pi_{ij}(d_i)) \Bigr) + \eta_j^{(12)} \frac{d_1}{d_1^*} \frac{d_2}{d_2^*} + \eta_j^{(13)} \frac{d_1}{d_1^*} \frac{d_3}{d_3^*} + \eta_j^{(23)} \frac{d_2}{d_2^*} \frac{d_3}{d_3^*} + \eta_j^{(123)} \frac{d_1}{d_1^*} \frac{d_2}{d_2^*} \frac{d_3}{d_3^*} + \eta_j^{(123)} \frac{d_1}{d_2^*} \frac{d_2}{d_3^*} \frac{d_3}{d_3^*} + \eta_j^{(123)} \frac{d_1}{d_3^*} \frac{d_2}{d_3^*} \frac{d_3}{d_3^*} + \eta_j^{(123)} \frac{d_1}{d_3^*} \frac{d_2}{d_3^*} \frac{d_3}{d_3^*} \frac{d_3}{d_3^*}$$

In group j each treatment component i toxicity is modeled with logistic regression,

$$\operatorname{logit} \pi_{ij}(d_i) = \log \, \alpha_{ij} + \beta_{ij} \, \log \left( \frac{d_i}{d_i^*} \right).$$

The intercept and log-slope parameters  $\theta_{ij} = (\log \alpha_{ij}, \log \beta_{ij})$  are are given an EXNEX prior

$$\theta_{ij} \sim p_{ij} \text{BVN}(\boldsymbol{\mu}_i, \boldsymbol{\Sigma}_{ij}) + (1 - p_{ij}) \text{BVN}(\boldsymbol{m}_{ii}, \boldsymbol{S}_{ij}),$$

where the exchangeability weights are all  $p_{ij}=0.9$ . The NEX parameters are set to  $m_{ij}=(\log i (1/3), \log 1)$ ,  $S_{ij}=\operatorname{diag}(2^2,1^2)$  for all components i=1,2,3 and groups j=1,2,3, and the EX parameters are modeled hierarchically. The mean of the exchangeable part has the distribution

$$\boldsymbol{\mu}_i = (\mu_{\alpha i}, \mu_{\beta i}) \sim \text{BVN}(\boldsymbol{m}_i, \boldsymbol{S}_i),$$

example-combo3 29

with  $m_i = (\log i(1/3), \log 1)$  and  $S_i = \operatorname{diag}(2^2, 1^2)$  for each component i = 1, 2, 3. For differentially discounting data from each schedule (QD and BID), the covariance parameters for the exchangeable part

$$\Sigma_{ij} = \begin{pmatrix} \tau_{\alpha s_j i}^2 & \rho_i \tau_{\alpha s_j i} \tau_{\beta s_j i} \\ \rho_i \tau_{\alpha s_j i} \tau_{\beta s_j i} & \tau_{\beta s_i i}^2 \end{pmatrix}.$$

are allowed to vary across groups j depending on their mapping to strata s(j) as described above. For stratum s=1 (BID, which contains only the group j=1 (Combo)), the standard deviations are modeled as

$$\tau_{\alpha 1i} \sim \text{Log-Normal}(\log 0.25, (\log 4/1.96)^2)$$
  
 $\tau_{\beta 1i} \sim \text{Log-Normal}(\log 0.125, (\log 4/1.96)^2).$ 

Whereas in stratum s=2 (QD, which contains the historical groups j=2,3 (HistData1, HistData2)), the standard deviations are

$$\tau_{\alpha 2i} \sim \text{Log-Normal}(\log 0.5, (\log 4/1.96)^2)$$

$$\tau_{\beta 2i} \sim \text{Log-Normal}(\log 0.25, (\log 4/1.96)^2).$$

For all interaction parameters  $\eta_j^{(12)}$ ,  $\eta_j^{(13)}$ ,  $\eta_j^{(23)}$ , and  $\eta_j^{(123)}$  (j=1,2,3), the following prior is assumed:

$$\eta_j^{(\cdot)} \sim \mathcal{N}(\mu_{\eta}^{(\cdot)}, \tau_{\eta s_j}^{(\cdot)}^2).$$

The exchangeability weights are  $p_{\eta j}^{(\cdot)}=0.9$  for all parameters with EXNEX. Here, for each  $\mu_{\eta}^{(12)}$ ,  $\mu_{\eta}^{(13)}$ ,  $\mu_{\eta}^{(23)}$ , and  $\mu_{\eta}^{(123)}$ , we take

$$\mu_{\eta}^{(\cdot)} \sim N(0, 1/2),$$

and for each  $\tau_{\eta s}^{(12)},$   $\tau_{\eta s}^{(13)},$   $\tau_{\eta s}^{(23)},$  and  $\tau_{\eta s}^{(123)},$ 

$$\tau_{\eta s}^{(\cdot)} \sim \text{Log-Normal}(\log(0.25), (\log 2/1.96)^2),$$

for both strata s = 1, 2.

Below is the syntax for specifying this model in blrm\_exnex.

## References

Neuenschwander, B., Roychoudhury, S., & Schmidli, H. (2016). On the use of co-data in clinical trials. *Statistics in Biopharmaceutical Research*, 8(3), 345-354.

#### **Examples**

## example combo3

library(abind)

dref <- c(500, 500, 1000)

example-single-agent

```
num\_comp <- 3
num\_inter <- choose(3,2) + 1
num_strata <- nlevels(hist_combo3$stratum_id)</pre>
num_groups <- nlevels(hist_combo3$group_id)</pre>
blrmfit <- blrm_exnex(</pre>
  cbind(num_toxicities, num_patients-num_toxicities) ~
    1 + I(log(drug_A/dref[1])) |
    1 + I(log(drug_B/dref[2])) |
    1 + I(log(drug_C/dref[3])) |
  + I(drug_A/dref[1] * drug_B/dref[2])
  + I(drug_A/dref[1] * drug_C/dref[3])
  + I(drug_B/dref[2] * drug_C/dref[3])
  + I(drug_A/dref[1] * drug_B/dref[2] * drug_C/dref[3]) |
    stratum_id/group_id,
  data = hist_combo3,
  prior_EX_mu_mean_comp = matrix(c(logit(1/3), 0), nrow = num_comp, ncol = 2, TRUE),
  prior_EX_mu_sd_comp = matrix(c(2, 1), nrow = num_comp, ncol = 2, TRUE),
 prior_EX_tau_mean_comp = abind(matrix(log(c(0.25, 0.125)), nrow = num_comp, ncol = 2, TRUE),
                             matrix(log(2*c(0.25, 0.125)), nrow = num\_comp, ncol = 2, TRUE),
                                    along = 0),
  \label{eq:prior_EX_tau_sd_comp} \texttt{prior}_\texttt{EX\_tau\_sd\_comp} \texttt{= abind}(\texttt{matrix}(\log(4) \ / \ 1.96, \ \mathsf{nrow} \texttt{= num\_comp}, \ \mathsf{ncol} \texttt{= 2}, \ \mathsf{TRUE}),
                                  matrix(log(4) / 1.96, nrow = num\_comp, ncol = 2, TRUE),
                                  along = 0),
  prior_EX_mu_mean_inter = rep(0, num_inter),
  prior_EX_mu_sd_inter = rep(sqrt(2) / 2, num_inter),
  prior_EX_tau_mean_inter = matrix(log(0.25), nrow = num_strata, ncol = num_inter),
  prior_EX_tau_sd_inter = matrix(log(2) / 1.96, nrow = num_strata, ncol = num_inter),
  prior_EX_prob_comp = matrix(0.9, nrow = num_groups, ncol = num_comp),
  prior_EX_prob_inter = matrix(1.0, nrow = num_groups, ncol = num_inter),
  prior_is_EXNEX_comp = rep(TRUE, num_comp),
  prior_is_EXNEX_inter = rep(FALSE, num_inter),
  prior_tau_dist = 1,
  prior_PD = FALSE
)
## Recover user set sampling defaults
options(.user_mc_options)
```

example-single-agent Single Agent Example

#### Description

Example using a single experimental drug.

#### **Details**

The single agent example is described in the reference Neuenschwander, B. et al (2008). The data are described in the help page for hist\_SA. In this case, the data come from only one study, with the

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treatment being only single agent. Hence the model specified does not involve a hierarchical prior for the intercept and log-slope parameters. The model described in Neuenschwander, et al (2008) is adapted as follows:

$$\operatorname{logit} \pi(d) = \log \alpha + \beta \log \left(\frac{d}{d^*}\right),$$

where  $d^* = 250$ , and the prior for  $\theta = (\log \alpha, \log \beta)$  is

$$\theta \sim N(m, S)$$
,

and  $m = (\text{logit } 0.5, \log 1)$  and  $S = \text{diag}(2^2, 1^2)$  are constants.

In the blrm\_exnex framework, in which the prior must be specified as a hierarchical model  $\theta \sim N(\mu, \Sigma)$  with additional priors on  $\mu$  and  $\Sigma$ , the simple prior distribution above is accomplished by fixing the diagonal elements  $\tau_{\alpha}^2$  and  $\tau_{\beta}^2$  of  $\Sigma$  to zero, and taking

$$\mu \sim N(m, S)$$
.

The arguments prior\_tau\_dist and prior\_EX\_tau\_mean\_comp as specified below ensure that the  $\tau$ 's are fixed at zero.

#### References

Neuenschwander, B., Branson, M., & Gsponer, T. (2008). Critical aspects of the Bayesian approach to phase I cancer trials. *Statistics in medicine*, 27(13), 2420-2439.

```
## Setting up dummy sampling for fast execution of example
## Please use 4 chains and 100x more warmup & iter in practice
.user_mc_options <- options(OncoBayes2.MC.warmup=10, OncoBayes2.MC.iter=20, OncoBayes2.MC.chains=1,
                             OncoBayes2.MC.save_warmup=FALSE)
## Example from Neuenschwander, B., et al. (2009). Stats in Medicine
num_comp <- 1 # one investigational drug</pre>
num_inter <- 0 # no drug-drug interactions need to be modeled</pre>
num_groups <- nlevels(hist_SA$group_id) # no stratification needed</pre>
num_strata <- 1 # no stratification needed
dref <- 50
## Since there is no prior information the hierarchical model
## is not used in this example by setting tau to (almost) 0.
blrmfit <- blrm_exnex(</pre>
 cbind(num_toxicities, num_patients - num_toxicities) ~
    1 + log(drug_A / dref) |
    0 |
    group_id,
 data = hist_SA,
 prior_EX_mu_mean_comp = matrix(
    c(logit(1/2), # mean of intercept on logit scale
```

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```
log(1)),
                 # mean of log-slope on logit scale
   nrow = num_comp,
   ncol = 2
 ),
 prior_EX_mu_sd_comp = matrix(
   c(2, # sd of intercept
     1), # sd of log-slope
   nrow = num_comp,
   ncol = 2
 ),
 ## Here we take tau as known and as zero.
 ## This disables the hierarchical prior which is
 ## not required in this example as we analyze a
 ## single trial.
 prior_EX_tau_mean_comp = matrix(
   c(0, 0),
   nrow = num_comp,
   ncol = 2
 ),
 prior_EX_tau_sd_comp = matrix(
   c(1, 1),
   nrow = num_comp,
   ncol = 2
 prior_EX_prob_comp = matrix(1, nrow = num_comp, ncol = 1),
 prior_tau_dist = 0,
 prior_PD = FALSE
)
## Recover user set sampling defaults
options(.user_mc_options)
```

example\_model

Runs example models

## **Description**

Runs example models

## Usage

```
example_model(topic, envir = parent.frame(), silent = FALSE)
```

## **Arguments**

| topic  | example to run  |
|--------|---|
| envir  | environment which the example is loaded into. Defaults to the caller environment. |
| silent | logical controlling if execution is run silently (defaults to FALSE)              |

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#### Value

When topic is not specified a list of all possible topics is return. Whenever a valid topic is specified, the function inserts the example into the environment given and returns (invisibly) the updated environment.

### **Examples**

hist\_combo2

Dataset: historical data on two single-agents to inform a combination study

#### Description

One of two datasets from the application described in Neuenschwander et al (2016). The risk of DLT is to be studied as a function of dose for two drugs, drug A and drug B. Historical information on the toxicity profiles of these two drugs is available from single agent trials trial\_A and trial\_B. A second dataset codata\_combo2 is available from this application, which includes additional dose-toxicity data from trial\_AB and IIT of the combination of Drugs A and B.

#### Usage

hist\_combo2

#### **Format**

A tibble with 11 rows and 5 variables:

```
group_id study
drug_A dose of Drug A
drug_B dose of Drug B
num_patients number of patients
num_toxicities number of DLTs
cohort_time cohort number of patients
```

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#### References

Neuenschwander, B., Roychoudhury, S., & Schmidli, H. (2016). On the use of co-data in clinical trials. *Statistics in Biopharmaceutical Research*, 8(3), 345-354.

hist\_combo3

Dataset: historical and concurrent data on a three-way combination

## **Description**

This dataset involves a hypothetical dose-escalation study of combination therapy with three treatment components. From two previous studies HistAgent1 and HistAgent2, historical data is available on each of the treatments as single-agents, as well as two of the two-way combinations. However, due to a difference in treatment schedule between the Combo study and the historical studies, a stratification (through stratum\_id) is made between the groups to allow differential discounting of the alternate-dose data.

#### Usage

hist\_combo3

#### **Format**

A data frame with 18 rows and 7 variables:

```
group_id study
drug_A dose of Drug A
drug_B dose of Drug B
drug_C dose of Drug C
num_patients number of patients
num_toxicities number of DLTs
stratum_id stratum for group_id's used for differential discounting
```

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```
num_strata <- nlevels(hist_combo3$stratum_id)</pre>
num_groups <- nlevels(hist_combo3$group_id)</pre>
blrmfit <- blrm_exnex(</pre>
 cbind(num_toxicities, num_patients-num_toxicities) ~
    1 + I(log(drug_A/dref[1])) |
   1 + I(log(drug_B/dref[2])) |
   1 + I(log(drug_C/dref[3])) |
 + I(drug_A/dref[1] * drug_B/dref[2])
 + I(drug_A/dref[1] * drug_C/dref[3])
 + I(drug_B/dref[2] * drug_C/dref[3])
 + I(drug_A/dref[1] * drug_B/dref[2] * drug_C/dref[3]) |
    stratum_id/group_id,
 data = hist_combo3,
 prior_EX_mu_mean_comp = matrix(c(logit(1/3), 0), nrow = num_comp, ncol = 2, TRUE),
 prior_EX_mu_sd_comp = matrix(c(2, 1), nrow = num_comp, ncol = 2, TRUE),
 prior_EX_tau_mean_comp = abind(matrix(log( c(0.25, 0.125)), nrow = num_comp, ncol = 2, TRUE),
                           matrix(log(2*c(0.25, 0.125)), nrow = num\_comp, ncol = 2, TRUE),
                                 along = 0),
 prior_EX_tau_sd_comp = abind(matrix(log(4) / 1.96, nrow = num_comp, ncol = 2, TRUE),
                               matrix(log(4) / 1.96, nrow = num\_comp, ncol = 2, TRUE),
                               along = 0),
 prior_EX_mu_mean_inter = rep(0, num_inter),
 prior_EX_mu_sd_inter = rep(sqrt(2) / 2, num_inter),
 prior_EX_tau_mean_inter = matrix(log(0.25), nrow = num_strata, ncol = num_inter),
 prior_EX_tau_sd_inter = matrix(log(2) / 1.96, nrow = num_strata, ncol = num_inter),
 prior_EX_prob_comp = matrix(0.9, nrow = num_groups, ncol = num_comp),
 prior_EX_prob_inter = matrix(1.0, nrow = num_groups, ncol = num_inter),
 prior_is_EXNEX_comp = rep(TRUE, num_comp),
 prior_is_EXNEX_inter = rep(FALSE, num_inter),
 prior_tau_dist = 1,
 prior_PD = FALSE
## Recover user set sampling defaults
options(.user_mc_options)
```

hist\_SA

Single-agent example

# Description

Example data from the application in Neuenschwander, et. al. 2008, from an "open-label, multicenter, non-comparative, dose-escalation cancer trial to characterize the safety, tolerability, and pharmacokinetic profile of a drug and to determine its MTD."

## Usage

hist\_SA

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#### **Format**

```
A data frame with 5 rows and 4 variables:

group_id study
drug_A dose
num_patients number of patients
num_toxicities number of events
```

#### References

Neuenschwander, B., Branson, M., & Gsponer, T. (2008). Critical aspects of the Bayesian approach to phase I cancer trials. *Statistics in medicine*, 27(13), 2420-2439.

```
## Setting up dummy sampling for fast execution of example
## Please use 4 chains and 100x more warmup & iter in practice
.user_mc_options <- options(OncoBayes2.MC.warmup=10, OncoBayes2.MC.iter=20, OncoBayes2.MC.chains=1,
                             OncoBayes2.MC.save_warmup=FALSE)
## Example from Neuenschwander, B., et al. (2009). Stats in Medicine
num_comp <- 1 # one investigational drug</pre>
num_inter <- 0 # no drug-drug interactions need to be modeled</pre>
num_groups <- nlevels(hist_SA$group_id) # no stratification needed</pre>
num_strata <- 1 # no stratification needed</pre>
dref <- 50
## Since there is no prior information the hierarchical model
## is not used in this example by setting tau to (almost) 0.
blrmfit <- blrm_exnex(</pre>
  cbind(num_toxicities, num_patients - num_toxicities) ~
    1 + log(drug_A / dref) |
   0 |
    group_id,
  data = hist_SA,
  prior_EX_mu_mean_comp = matrix(
    c(logit(1/2), \# mean of intercept on logit scale
                # mean of log-slope on logit scale
      log(1)),
   nrow = num_comp,
   ncol = 2
  ),
  prior_EX_mu_sd_comp = matrix(
    c(2, # sd of intercept
      1), # sd of log-slope
   nrow = num_comp,
   ncol = 2
  ),
  ## Here we take tau as known and as zero.
```

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```
## This disables the hierarchical prior which is
  ## not required in this example as we analyze a
  ## single trial.
  prior_EX_tau_mean_comp = matrix(
   c(0, 0),
   nrow = num_comp,
   ncol = 2
  ),
  prior_EX_tau_sd_comp = matrix(
   c(1, 1),
   nrow = num_comp,
   ncol = 2
  ),
  prior_EX_prob_comp = matrix(1, nrow = num_comp, ncol = 1),
  prior_tau_dist = 0,
  prior_PD = FALSE
)
## Recover user set sampling defaults
options(.user_mc_options)
```

lodds

 $Logit\ (log-odds)\ and\ inverse-logit\ function.$ 

# **Description**

Calculates the logit (log-odds) and inverse-logit.

# Usage

```
logit(mu)
inv_logit(eta)
```

# Arguments

| mu  | A numeric object with probabilies, with values in the in the range [0,1]. Missing values (NAs) are allowed.   |
|-----|---|
| eta | A numeric object with log-odds values, with values in the range [-Inf,Inf]. Missing values (NAs) are allowed. |

### **Details**

Values of mu equal to 0 or 1 will return -Inf or Inf respectively.

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#### Value

A numeric object of the same type as mu and eta containing the logits or inverse logit of the input values. The logit and inverse transformation equates to

$$logit(\mu) = log(\mu/(1-\mu))$$
$$logit^{-1}(\eta) = exp(\eta)/(1 + exp(\eta)).$$

# **Examples**

```
logit(0.2)
inv_logit(-1.386)
```

nsamples.blrmfit

Return the number of posterior samples

# **Description**

Return the number of posterior samples

# Usage

```
## S3 method for class 'blrmfit'
nsamples(object, ...)
```

# Arguments

object fitted model object
... not used in this function

OncoBayes2 39

|--|

#### Description

Bayesian logistic regression model with optional EXchangeability-NonEXchangeability parameter modelling for flexible borrowing from historical or concurrent data-sources. The safety model can guide dose-escalation decisions for adaptive Oncology phase I dose-escalation trials which involve an arbitrary number of drugs.

# **Global Options**

| Option                    | Default   | Description                                  |
|---------------------------|---|--|
| OncoBayes2.MC.warmup      | 1000  | MCMC warmup iterations                       |
| OncoBayes2.MC.iter        | 2000  | total MCMC iterations                        |
| OncoBayes2.MC.save_warmup | TRUE  | save warmup samples                          |
| OncoBayes2.MC.chains      | 4   | MCMC chains                                  |
| OncoBayes2.MC.thin        | 1   | MCMC thinning                                |
| OncoBayes2.MC.control     | <pre>list(adapt_delta=0.99,     stepsize=0.1)</pre> | sets control argument for Stan call          |
| OncoBayes2.MC.backend     | rstan   | Backend used to run Stan (rstan or cmdstanr) |
| OncoBayes2.abbreviate.min | 0   | Minimal length of variable names             |
|                           |   | when abbreviating variable names.            |
|                           |   | The default 0 disables abbreviation.         |

## References

Neuenschwander, B., Roychoudhury, S., & Schmidli, H. (2016). On the use of co-data in clinical trials. *Statistics in Biopharmaceutical Research*, 8(3), 345-354.

Neuenschwander, B., Wandel, S., Roychoudhury, S., & Bailey, S. (2016). Robust exchangeability designs for early phase clinical trials with multiple strata. *Pharmaceutical statistics*, 15(2), 123-134.

Neuenschwander, B., Branson, M., & Gsponer, T. (2008). Critical aspects of the Bayesian approach to phase I cancer trials. *Statistics in medicine*, 27(13), 2420-2439.

Neuenschwander, B., Matano, A., Tang, Z., Roychoudhury, S., Wandel, S. Bailey, Stuart. (2014). A Bayesian Industry Approach to Phase I Combination Trials in Oncology. In *Statistical methods in drug combination studies* (Vol. 69). CRC Press.

Stan Development Team (2019). RStan: the R interface to Stan. R package version 2.19.2. https://mc-stan.org

plot\_blrm

Plot a fitted model

# Description

**Warning**: these methods are at an experimental stage of development, and may change with future releases.

Plotting methods for blrmfit and blrm\_trial objects.

# Usage

```
plot_toxicity_curve(object, ...)
plot_toxicity_intervals(object, ...)
plot_toxicity_intervals_stacked(object, ...)
## S3 method for class 'blrmfit'
plot_toxicity_curve(
 object,
  newdata,
  Х,
  group,
  xlim,
 ylim,
  transform = TRUE,
  prob = 0.5,
  prob_outer = 0.95,
  size = 0.75,
  alpha = 1,
  facet_args = list(),
  hline_at = c(0.16, 0.33),
  grid_length = 100,
)
## S3 method for class 'blrm_trial'
plot_toxicity_curve(
  object,
  newdata,
  Х,
  group,
  xlim,
  ylim,
  transform = TRUE,
  prob = 0.5,
```

```
prob_outer = 0.95,
  size = 0.75,
  alpha = 1,
  facet_args = list(),
  hline_at,
  grid_length = 100,
  ewoc_shading = TRUE,
)
## S3 method for class 'blrmfit'
plot_toxicity_intervals(
 object,
  newdata,
 Х,
  group,
  interval_prob = c(0, 0.16, 0.33, 1),
  interval_max_mass = c(NA, NA, 0.25),
  ewoc_colors = c("green", "red"),
)
## S3 method for class 'blrm_trial'
plot_toxicity_intervals(
 object,
  newdata,
 х,
  group,
  interval_prob,
  interval_max_mass,
  ewoc_colors = c("green", "red"),
)
## S3 method for class 'blrmfit'
plot_toxicity_intervals_stacked(
 object,
  newdata,
  х,
  group,
  xlim,
 ylim = c(0, 0.5),
  predictive = FALSE,
  transform = !predictive,
  interval_prob,
  grid_length = 100,
  facet_args = list(),
  . . .
```

```
)
## S3 method for class 'blrm_trial'
plot_toxicity_intervals_stacked(
  object,
 newdata,
 х,
  group,
 xlim,
 ylim = c(0, 0.5),
 predictive = FALSE,
  transform = !predictive,
  interval_prob,
  grid_length = 100,
  ewoc_shading = TRUE,
  facet_args = list(),
)
```

# **Arguments**

prob\_outer

alpha, size

| Ę | guments   |   |
|---|-----------|---|
|   | object    | fitted model object   |
|   | • • •     | currently unused  |
|   | newdata   | optional data frame specifying for what to predict; if missing, then the data of the input model object is used. If object is a blrmfit object, newdata defaults to the data argument. If object is a blrm_trial, it defaults to summary(object, "dose_info").  |
|   | X         | Character giving the parameter name to be mapped to the x-axis. This also supports 'tidy' parameter selection by specifying x = vars(), where is specified the same way as in dplyr::select() and similar functions. Examples of using x in this way can be found in the examples. For blrm_trial methods, it defaults to the first entry in summary(blrm_trial, "drug_info")\$drug_name. |
|   | group     | Grouping variable(s) whose levels will be mapped to different facets of the plot. group can be a character vector, tidy parameter(s) of the form group = vars(), or a formula to be passed directly to ggplot2::facet_wrap(). For blrm_trial methods, it defaults to group_id, plus all entries of summary(blrm_trial, "drug_info")\$c except the first, which is mapped to x.            |
|   | xlim      | x-axis limits   |
|   | ylim      | y-axis limits on the probability scale  |
|   | transform | logical (defaults to FALSE) indicating if the linear predictor on the logit link scale is transformed with inv_logit to the 0-1 response scale.   |
|   | prob      | central probability mass to report for the inner ribbon, i.e. the quantiles 0.5-prob/2  |

central probability mass to report for the outer ribbon, i.e. the quantiles 0.5-prob/2

Arguments passed to geoms. For this plot, alpha is passed to ggplot2::geom\_ribbon(),

and 0.5+prob/2 are displayed.

and 0.5+prob/2 are displayed.

and size is passed to ggplot2::geom\_line().

facet\_args A named list of arguments (other than 'facets') passed to ggplot2::facet\_wrap().

hline\_at Location(s) of horizontal guide lines (passed to bayesplot::hline\_at()).

grid\_length
Number of grid points within xlim for plotting.

ewoc\_shading logical indicates if doses violating EWOC should be shaded in gray. Applies

only to blrm\_trial methods. Defaults to TRUE.

interval\_prob defines the interval probabilities reported in the standard outputs. Defaults to

c(0,0.16,0.33,1), when predictive = FALSE and/or transform = TRUE, or to intervals giving 0, 1, or 2+ DLTs when predictive = TRUE and transform =

FALSE. For blrm\_trial methods, this is taken from summary(blrm\_trial, "interval\_prob")

by default.

interval\_max\_mass

vector defining for each interval of the interval\_prob vector a maximal admissible probability mass for a given dose level. Whenever the posterior probability mass in a given interval exceeds the threshold, then the Escalation With Overdose Control (EWOC) criterion is considered to be not fulfilled. Dose levels not fulfilling EWOC are ineligible for the next cohort of patients. The default restricts the overdose probability to less than 0.25. For blrm\_trial methods, this is taken from summary(blrm\_trial, "interval\_max\_mass") by default.

ewoc\_colors Fill colors used for bars indicating EWOC OK or not. Vector of two charac-

ters, each of which must correspond to bayesplot-package color schemes (see

?bayesplot::color\_scheme\_get())

predictive logical indicates if the posterior predictive is being summarized. Defaults to

FALSE.

## Details

plot\_toxicity\_curve plots continuous profiles of the dose-toxicity curve.

plot\_toxicity\_intervals plots the posterior probability mass in subintervals of [0,1], at a discrete set of provisional doses.

plot\_toxicity\_intervals\_stacked is similar to plot\_toxicity\_intervals, but over a continuous range of doses.

### Value

A ggplot object that can be further customized using the ggplot2 package.

```
plot_toxicity_curve(blrmfit,
                    x = "drug_A",
                    group = ~ group_id * drug_B,
                    newdata = subset(dose_info_combo2, group_id == "trial_AB"),
                    facet_args = list(ncol = 4))
# Plot posterior DLT-rate-interval probabilities at discrete dose levels
plot_toxicity_intervals(blrmfit,
                        x = "drug_A",
                        group = ~ group_id * drug_B,
                        newdata = subset(dose_info_combo2, group_id == "trial_AB"))
# Plot posterior DLT-rate-interval probabilities over continuous dose
plot_toxicity_intervals_stacked(blrmfit,
                                x = "drug_A",
                                group = ~ group_id * drug_B,
                             newdata = subset(dose_info_combo2, group_id == "trial_AB"))
# Plot predictive distribution probabilities over continuous dose
plot_toxicity_intervals_stacked(blrmfit,
                                x = "drug_A",
                                group = ~ group_id * drug_B,
                                predictive = TRUE,
                                interval_prob = c(-1, 0, 1, 6),
                                newdata = transform(subset(dose_info_combo2,
                                                           group_id == "trial_AB"),
                                                    num_patients = 6,
                                                    num_toxicities = 0))
## Recover user set sampling defaults
options(.user_mc_options)
```

posterior\_interval.blrmfit

Posterior intervals

#### **Description**

Posterior intervals of all model parameters.

### Usage

```
## S3 method for class 'blrmfit'
posterior_interval(object, prob = 0.95, ...)
```

## **Arguments**

object fitted model object

prob central probability mass to report, i.e. the quantiles 0.5-prob/2 and 0.5+prob/2

are displayed. Multiple central widths can be specified.

... not used in this function

# **Details**

Reports the quantiles of posterior parameters which correspond to the central probability mass specified. The output includes the posterior of the hyper-parameters and the posterior of each group estimate.

#### Value

Matrix of two columns for the central probability interval prob for all parameters of the model.

#### **Examples**

```
posterior_linpred.blrmfit
```

Posterior of linear predictor

# Description

Calculates the posterior of the linear predictor.

# Usage

```
## S3 method for class 'blrmfit'
posterior_linpred(object, transform = FALSE, newdata, draws, ...)
```

### **Arguments**

| object    | fitted model object   |
|-----------|---|
| transform | logical (defaults to FALSE) indicating if the linear predictor on the logit link scale is transformed with inv_logit to the 0-1 response scale. |
| newdata   | optional data frame specifying for what to predict; if missing, then the data of the input model object is used                                 |
| draws     | number of returned posterior draws; by default the entire posterior is returned   |
|           | not used in this function   |

#### **Details**

Simulates the posterior of the linear predictor of the model object for the specified data set.

#### Value

Matrix of dimensions draws by nrow(newdata) where row correspond to a draw of the posterior and each column corresponds to a row in newdata. The columns are labelled with the row.names of newdata.

### Group and strata definitions

The groups and strata as defined when running the blrm\_exnex analysis cannot be changed at a later stage. As a result no evaluations can be performed for groups which have not been present in the data set used for running the analysis. However, it is admissible to code the group (and/or stratum) column as a factor which contains empty levels. These groups are thus not contained in the fitting data set and they are assigned by default to the first stratum. In addition priors must be setup for these groups (and/or strata). These empty group (and/or strata) levels are then allowed in subsequent evaluations. This enables the evaluation of the hierarchical model in terms of representing a prior for future groups.

```
## Setting up dummy sampling for fast execution of example
## Please use 4 chains and 100x more warmup & iter in practice
.user_mc_options <- options(OncoBayes2.MC.warmup=10, OncoBayes2.MC.iter=20, OncoBayes2.MC.chains=1,
                            OncoBayes2.MC.save_warmup=FALSE)
## run single-agent analysis which defines blrmfit model object
example_model("single_agent", silent=TRUE)
## obtain posterior of linear prediction on 0-1 scale
post_prob_dlt <- posterior_linpred(blrmfit, TRUE, newdata=hist_SA)</pre>
## name columns to obtain nice bayesplot labels
colnames(post_prob_dlt) <- hist_SA$drug_A
library(bayesplot)
library(ggplot2)
mcmc_intervals(post_prob_dlt, prob=0.5, prob_outer=0.95) +
    coord_flip() +
   vline_at(c(0.16, 0.33), linetype=2) +
   ylab("Dose [mg]") +
   ggtitle("Posterior Probability of a DLT") +
    scale_x_continuous(breaks=c(0.1,0.16,0.33, 0.5, 0.75))
## Recover user set sampling defaults
options(.user_mc_options)
```

## Description

Simulation of the predictive distribution.

#### Usage

```
## S3 method for class 'blrmfit'
posterior_predict(object, newdata, draws, ...)
```

## **Arguments**

object fitted model object

newdata optional data frame specifying for what to predict; if missing, then the data of

the input model object is used

draws number of returned posterior draws; by default the entire posterior is returned

... not used in this function

#### **Details**

Simulates the posterior predictive of the model object for the specified data set.

# Value

Matrix of dimensions draws by nrow(newdata) where row correspond to a draw of the posterior and each column corresponds to a row in newdata. The columns are labelled with the row.names of newdata.

#### Group and strata definitions

The groups and strata as defined when running the blrm\_exnex analysis cannot be changed at a later stage. As a result no evaluations can be performed for groups which have not been present in the data set used for running the analysis. However, it is admissible to code the group (and/or stratum) column as a factor which contains empty levels. These groups are thus not contained in the fitting data set and they are assigned by default to the first stratum. In addition priors must be setup for these groups (and/or strata). These empty group (and/or strata) levels are then allowed in subsequent evaluations. This enables the evaluation of the hierarchical model in terms of representing a prior for future groups.

### **Examples**

```
## Setting up dummy sampling for fast execution of example
 ## Please use 4 chains and 100x more warmup & iter in practice
 .user_mc_options <- options(OncoBayes2.MC.warmup=10, OncoBayes2.MC.iter=20, OncoBayes2.MC.chains=1,
                              OncoBayes2.MC.save_warmup=FALSE)
 example_model("single_agent", silent=TRUE)
 post_pred <- posterior_predict(blrmfit)</pre>
 ## turn DLT counts into DLT rates
 post_pred_rate <- sweep(post_pred, 2, hist_SA$num_patients, "/")</pre>
 library(bayesplot)
 library(ggplot2)
 ## compare posterior predictive of the model for the response rates
 ## with observed data
 with(hist_SA,
    ppc_intervals(num_toxicities / num_patients, post_pred_rate, x=drug_A, prob_outer=0.95)) +
     xlab("Dose [mg]")
 ## Recover user set sampling defaults
 options(.user_mc_options)
predictive_interval.blrmfit
                         Posterior predictive intervals
```

### Description

Posterior predictive intervals of the model.

# Usage

```
## S3 method for class 'blrmfit'
predictive_interval(object, prob = 0.95, newdata, ...)
```

#### **Arguments**

object fitted model object

prob central probability mass to report, i.e. the quantiles 0.5-prob/2 and 0.5+prob/2 are displayed. Multiple central widths can be specified.

newdata optional data frame specifying for what to predict; if missing, then the data of the input model object is used

not used in this function

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#### **Details**

Reports for each row of the input data set the predictive interval according to the fitted model.

#### Value

Matrix with as many rows as the input data set and two columns which contain the lower and upper quantile corresponding to the central probability mass prob for the number of responses of the predictive distribution.

#### **Examples**

```
prior_summary.blrmfit Summarise model prior
```

#### **Description**

Extracts a summary of the prior in a structured data format.

#### Usage

```
## S3 method for class 'blrmfit'
prior_summary(object, digits = 2, ...)
```

# **Arguments**

```
object blrmfit (blrm_trial) object as returned from blrm_exnex (blrm_trial) analysis

digits number of digits to show

... ignored by the function
```

#### **Details**

The summary of the prior creates a structured representation of the specified prior from a blrm\_exnex (blrm\_trial) analysis.

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#### Value

Returns an analysis specific list, which has it's own print function. The returned list contains arrays which represent the prior in a structured format.

## **Examples**

summary.blrm\_trial

Summarise trial

# **Description**

Provides model summaries for blrm\_trial analyses.

### Usage

```
## S3 method for class 'blrm_trial'
summary(
  object,
  summarize = c("blrmfit", "blrm_exnex_call", "data", "drug_info", "dose_info",
    "dose_prediction", "data_prediction", "newdata_prediction", "dimensionality",
        "interval_prob", "interval_max_mass"),
        ...
)
```

# **Arguments**

```
object blrm_trial object
summarize one of the following options:
```

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- blrmfit: summary of the underlying blrmfit object with further arguments ...
- blrm\_exnex\_call: blrm\_exnex call used to create the blrmfit object
- drug\_info: drug\_info for the trial, contains drugs, reference doses and units
- · dose\_info: dose info that were defined
- dose\_prediction prediction for the defined dose\_info
- data: data that were observed
- data\_prediction: prediction for the observed data
- newdata\_prediction: prediction for data provided with the newdata= argument
- dimensionality: numeric vector with entries "num\_components", "num\_interaction\_terms", "num\_groups", "num\_strata"
- interval\_prob: interval probabilities reported in the standard outputs
- interval\_max\_mass: named vector defining for each interval of the interval\_prob vector a maxmimal admissable probability mass for a given dose level

further arguments for summary.blrmfit

#### **Examples**

summary.blrmfit

Summarise model results

### **Description**

Provides model summaries for blrm\_exnex and blrm\_trial analyses.

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#### Usage

```
## S3 method for class 'blrmfit'
summary(
  object,
  newdata,
  transform = !predictive,
  prob = 0.95,
  interval_prob,
  predictive = FALSE,
  ...
)
```

### **Arguments**

object fitted model object

newdata optional data frame specifying for what to predict; if missing, then the data of

the input model object is used

transform logical (defaults to FALSE) indicating if the linear predictor on the logit link scale

is transformed with inv\_logit to the 0-1 response scale.

prob central probability mass to report, i.e. the quantiles 0.5-prob/2 and 0.5+prob/2

are displayed. Multiple central widths can be specified.

interval\_prob optional vector of sorted quantiles for which the interval probabilities are calcu-

lated

predictive logical indicates if the posterior predictive is being summarized. Defaults to

FALSE.

... not used in this function

#### **Details**

The calculated posterior summaries are returned as a data.frame and contain optional interval probabilities for the specified vector of sorted quantiles. These summaries are calculated on the response scale by default and can be obtained on the link scale when setting transform=FALSE.

When the results are requested for the predictive distribution with predictive=TRUE, then the link scale refers to the total counts while the transformed scale divides the (predictive) counts by the number of trials such that results are on the 0-1 scale.

#### Value

Returns a data.frame of the key summaries of the posterior mean, standard deviation, central probability interval, median and optional interval probabilities. Each row of the data.frame corresponds to the respective input data which is by default the same data set as used for the blrm\_exnex analysis or the data specified in the newdata argument.

```
## Setting up dummy sampling for fast execution of example
## Please use 4 chains and 100x more warmup & iter in practice
```

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```
.user_mc_options <- options(OncoBayes2.MC.warmup=10, OncoBayes2.MC.iter=20, OncoBayes2.MC.chains=1,
                            OncoBayes2.MC.save_warmup=FALSE)
example_model("single_agent", silent=TRUE)
## obtain underdosing (0-0.16), target dosing (0.16-0.33) and
## overdosing (0.33-1) probabilities
summary(blrmfit, interval_prob=c(0,0.16,0.33,1))
## obtain predictive distribution for respective cohorts and
## calculate probability for no event, 1 event or >1 event
## note that this does the calculation for the cohort sizes
## as put into the data-set
summary(blrmfit, interval_prob=c(-1,0,1,10), predictive=TRUE)
## to obtain the predictive for a cohort-size of 6 for all patients
## in the data-set one would need to use the newdata argument, e.g.
summary(blrmfit, newdata=transform(hist_SA, num_patients=6),
                 interval_prob=c(-1,0,1,10), predictive=TRUE)
## Recover user set sampling defaults
options(.user_mc_options)
```

update.blrm\_trial

Update data and/or prior of a BLRM trial

#### **Description**

\* Adds data rows to a blrm\_trial object (add\_data argument) \* Replaces data of a blrm\_trial object (data argument) \* Sets the prior of a blrm\_trial object (... argument will be passed to blrm\_exnex)

### Usage

```
## S3 method for class 'blrm_trial'
update(object, ...)
```

# **Arguments**

```
object blrm_trial object
... passed to default update command of blrm_exnex
```

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```
# the combo2_trial example demonstrates the use of add_data of
# update.blrmfit
example_model("combo2_trial")

## Recover user set sampling defaults
options(.user_mc_options)
```

update.blrmfit

Update data of a BLRM analysis

## **Description**

Adds data rows to a blrm\_exnex or blrm\_trial analysis object.

#### Usage

```
## S3 method for class 'blrmfit'
update(object, ..., add_data)
```

# Arguments

object blrmfit analysis object

... passed to default update command

The data in add\_data will be combined with data in object using bind\_rows. The indices for groups and stratums (if defined) are matched between add\_data

and the data of the analysis object.

Note that the add\_data argument must be named explicitly as demonstrated in

the example.

add\_data additional data added to analysis data of object

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## Recover user set sampling defaults
options(.user\_mc\_options)