# Package 'OptimaRegion'

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Title Confidence Regions for Optima	
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<b>Description</b> Computes confidence regions on the location of response surface optima.	
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# Description

OptimaRegion is a package for the computation of confidence regions on the location of the optima of response surface models. Both parametric (quadratic polynomial) and nonparametric (thin plate spline) models are supported. The confidence regions obtained do not rely on any distributional assumption, such as Normality of the response, and are obtained by bootstrapping. The resulting regions are both valid and unbiased, and have a size that rapidly decreases as the sample size

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increases. Regions are obtained both numerically (as a set of points) and graphically, as the convex hull of the points. Functionality for the computation of a bootstrap confidence interval on the distance between the optima of two different response surfaces is included.

# Author(s)

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## References

Del Castillo, E., Hunt, J., Rapkin, J., and Zarmehri, S., "Confidence regions for the location of response surface optima: the R package OptimaRegion".

CRcompare	Computes bootstrapped confidence intervals for the distance between two response surface optima

#### **Description**

Computes bootstrapped confidence intervals for the mean and median distance between the optima of two response surface models. Models can be thin plate splines or quadratic polynomials.

#### Usage

CRcompare(X1,y1,X2,y2,lambda=0.04,responseType='TPS',nosim1and2=200, alpha=0.05,LB1,UB1,triangularRegion1=FALSE, vertex11=NULL, vertex21=NULL, maximization1=TRUE,outputPDFFile1="CR\_plot1.pdf",outputOptimafile1="Optima1.txt",LB2,UB2,triangularRegion2=FALSE, vertex12=NULL, vertex22=NULL, maximization2=TRUE,outputPDFFile2="CR\_plot2.pdf",outputOptimafile2="Optima2.txt",xlab1and2="Protein eaten (mg)",ylab1and2="Carbohydrates eaten (mg)")

## **Arguments**

X1	$nx2\ matrix$ with the values of the 2 regressors (experimental factors) in the n observations associated with response 1
y1	nx1 vector of response no. 1 value observations
X2	$nx2\ matrix$ with the values of the 2 regressors (experimental factors) in the n observations associated with response 2
y2	nx1 vector of response no. 2 value observations
lambda	smoothing penalty if a TPS model is selected (default=0.04)
responseType	use 'TPS' if fitting thin plate spline responses, 'Quad' if fitting quadratic polynomials
nosim1and2	number of simulations (default=200)
alpha	confidence level (0 <alpha<1; default="0.05)&lt;/td"></alpha<1;>
LB1,UB1	2x1 vectors of lower and upper bounds for search region where optima may lie for response 1

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triangularRegion1

logical: if TRUE it will constrain the optimum points of response 1 to lie inside a triangle defined by the coordinates (0,0), and those in "vertex11", and "vertex21", see below). NOTE: use TRUE when the treatments form a triangular experimental region in shape. If FALSE, maxima will only be constrained to lie inside the rectangular region defined by LB1 and UB1. Default is FALSE.

vertex11, vertex21

2x1 vectors with coordinates defining two of the 3 vertices of a triangular region for searching the optima of response 1. Must be provided if triangularRegion is TRUE (NOTE: vertices numbered clockwise, vertex0=c(0,0) always)

maximization1 logical: if TRUE (default) it maximizes response 1, if FALSE it minimizes it

outputPDFFile1 name of the PDF file where the CR plot of response 1 is saved (default: "CR-plot1.pdf")

outputOptimafile1

name of text file for saving the coordinates of the optima of response 1 (default: "Optima1.txt")

LB2, UB2 2x1 vectors of lower and upper bounds for search region where optima may lie for response 2

triangularRegion2

logical: if TRUE it will constrain the optimum points of response 2 to lie inside a triangle defined by the coordinates (0,0), and those in "vertex12", and "vertex22", see below (in addition to being constrained to lie inside the region defined by LB and UB). NOTE: use TRUE when the treatments form a triangular experimental region in shape. If FALSE, maxima will only be constrained to lie inside the rectangular region defined by LB2 and UB2. Default is FALSE.

vertex12 see vertex22

vertex22 2x1 vectors with coordinates defining two of the 3 vertices of a triangular region

for searching the optima of response 2. Must be provided if triangularRegion is TRUE (NOTE: vertices numbered clockwise, vertex0=c(0,0) always)

maximization 2 logical: if TRUE (default) it maximizes response 2 if FALSE it minimizes it

 $\hbox{outputPDFFile2} \quad \hbox{name of the PDF file where the $CR$ plot of response 2 is saved (default: "CR-value") and the position of the PDF file where the $CR$ plot of response 2 is saved (default: "CR-value").}$ 

plot2.pdf")

outputOptimafile2

name of text file for saving the coordinates of the optima of response 2 (default:

"Optima2.txt")

xlab1and2 text label for x axis in confidence region plot for the optima of each response

(default: "Protein eaten, mg")

ylab1and2 text label for y axis in confidence region plot for the optima of each response

(default: "Carbohydrates eaten, mg")

## Details

Computes distribution-free bootstrapped confidence intervals on the mean and median distance between the optima of two different responses. The responses can be Thin Plate Spline models or Quadratic polynomial models. Program calls OptRegionTps.R or OptRegionQuad.R to compute confidence regions on the optima of each response, next computes all pairwise distances between points in each CR, and finally bootstraps the distances to compute bca bootstrapped confidence intervals for the mean and median distance.

Usage assuming all default options:

out<-CRcompare(X1=X1,y1=y1,X2=X2,y2=y2,LB1=LB1,UB1=UB1,LB2=LB2,UB2=UB2)

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#### Value

dist vector of distances between pairs of points taken from each set of optima
mean mean of all pairwise distances

median of all pairwise distances

ciMean (1-alpha)\*100% confidence interval for the mean of the distances using bca

bootstrapping

ciMedian (1-alpha)\*100% confidence interval for the mean of the distances using bca

bootstrapping.

Note: ciMean and ciMedian are vectors with 5 columns, containing the significance level, the next two containing the indices of the order statistics used in the

calculations and the final two the calculated endpoints of the CI's.

#### Note

Upon completion, PDF files containing the CR plots of the optima of each response with name as set in ouputPDFFile1 and outPDFFile2 are created. Two text files named as set in outputOptimaFile1 and outputOptimaFile2 are also created. These contain all the individual optima of each response in each CR.

## Author(s)

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#### References

Del Castillo, E., Hunt, J., Rapkin, J., and Zarmehri, S. , "Confidence regions for the location of response surface optima: the R package OptimaRegion".

## **Examples**

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Drug	Mixture-amount experiment	

# Description

A pharmaceutical mixture-amount experiment in two components

# Usage

```
data("Drug")
```

#### **Format**

A data frame with 360 observations on the following 3 variables.

```
'Component_1' Component 1 amount (mg)
'Component_2' Component 2 amount (mg)
Percent Percent of cells killed (response)
```

# **Examples**

```
plot(Drug[,1:2])
```

OptRegionQuad	Computes Confidence Regions of Optima of Quadratic Polynomial Models
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# Description

Computes and displays the confidence region on the location of the optima of a quadratic response surface in 2 factors using bootstrapping.

# Usage

```
OptRegionQuad(X, y, nosim=200, alpha=0.05, LB, UB, triangularRegion=FALSE, vertex1=NULL, vertex2=NULL, maximization=TRUE, xlab="Protein eaten, mg", ylab="Carbohydrates eaten, mg", outputPDFFile="CRplot.pdf")
```

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#### **Arguments**

X nx2 matrix with the values of the 2 regressors (experimental factors) in the n

observations

y nx1 vector of response value observations

nosim number of simulations (default=200)

alpha confidence level (0<alpha<1; default=0.05)

LB, UB 2x1 vectors of lower and upper bounds for search region where optima may lie

triangularRegion

logical: if TRUE it will constrain the optimum points to lie inside a triangle defined by the coordinates (0,0), and those in "vertex1", and "vertex2", see below (in addition to being constrained to lie inside the region defined by LB and UB). NOTE: use TRUE when the treatments form a triangular experimental region in shape. If FALSE, maxima will only be constrained to lie inside the rectangular

region defined by LB and UB. Default is FALSE.

vertex1, vertex2

2x1 vectors with coordinates defining two of the 3 vertices of a triangular region. Must be provided if triangularRegion is TRUE (NOTE: vertices numbered

clockwise, vertex0=c(0,0) always)

maximization logical: if TRUE (default) it maximizes it FALSE it minimizes

xlab text label for x axis in confidence region plot (default: "Protein eaten, mg")

ylab text label for y axis in confidence region plot (default: "Carbohydrates eaten,

mg")

outputPDFFile name of the PDF file where the CR plot is saved (default: "CRplot.pdf")

#### **Details**

Computes and displays an approximated 100\*(1-alpha) percent confidence region (CR) for the linear-constrained maximum of a quadratic polynomial regression model in 2 controllable factors. Grey region on output plot is the approximate CR. The CR is computed as the convex hull of the coordinates of the optima found from bootstrapping nosim quadratic polynomial regressions to the data (therefore, it is an approximate CR). The mean value of the optimum is shown as a red point, and a smoothed contour plot of the X,y data obtained via thin plate splines is shown as well.

Usage assuming all default options:

out<-OptRegionQuad(X=X,y=y,LB=LB,UB=UB)

# Value

meanPoint a 2x1 vector with the coordinates of the mean optimum point

xin an mx2 matrix with the x,y coordinates of all simulated #points that belong to

the confidence region (dim(m) is (1-alpha)\*nosim)

#### Note

Upon completion, a PDF file containing the CR plot with name as set in ouputPDFFile is created. To help visualization of the CR and the experimental response data, the plot also shows contours of a smoothed approximation to the response values, note this is not the quadratic polynomial that was fit (it is actually a TPS model).

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#### Author(s)

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#### References

Del Castillo, E., Hunt, J., Rapkin, J., and Zarmehri, S., "Confidence regions for the location of response surface optima: the R package OptimaRegion".

## **Examples**

```
## Example 1: randomly generated 2-variable response surface data

X<-cbind(runif(100,-2,2),runif(100,-2,2))

y<-as.matrix(72-11.78*X[,1]+0.74*X[,2]-7.25*X[,1]^2-7.55*X[,2]^2-4.85*X[,1]*X[,2]+
rnorm(100,0,8))

## Find a 95 percent confidence region for the maximum of a quadratic polynomial

## fitted to these data

out<-OptRegionQuad(X=X,y=y,nosim=200,LB=c(-2,-2),UB=c(2,2), xlab="X1",ylab="X2")

## Example 2: a mixture-amount experiment in two components (Drug dataset) with

## non-normal data. Note triangular experimental region. Resulting 95%

## confidence region is pushed against the constraint and results in a

## "thin line"

out<-OptRegionQuad(X=Drug[,1:2],y=Drug[,3],nosim=500,LB=c(0,0),UB=c(0.08,11),
    xlab="Component 1 (mg.)",ylab="Component 2 (mg.)",triangularRegion = TRUE,
    vertex1 = c(0.02,11),vertex2 = c(0.08,1.8),outputPDFFile="Mixture_plot.pdf")</pre>
```

OptRegionTps

Computes Confidence Regions of Optima of Thin Plate Spline Models

# Description

Computes and displays the confidence region on the location of the optima of a thin plate spline surface in 2 factors using bootstrapping.

## Usage

```
OptRegionTps(X, y, lambda=0.04, nosim=1000, alpha=0.05, LB, UB, triangularRegion=FALSE, vertex1=NULL, vertex2=NULL, maximization=TRUE, xlab="Protein eaten, mg",ylab="Carbohydrate eaten, mg",outputPDFFile="CRplot.pdf",outputOptimaFile="Optima.txt")
```

OptRegionTps

#### **Arguments**

x nx2 matrix with the values of the 2 regressors (experimental factors) in the n

observations

y nx1 vector of response value observations

lambda penalization parameter (larger values implies more smoothing). Default is 0.04

nosim number of simulations (default=1000)

alpha confidence level (0<alpha<1; default=0.05)

LB, UB 2x1 vectors of lower and upper bounds for search region where optima may lie

triangularRegion

logical: if TRUE it will constrain the optimum points to lie inside a triangle defined by the coordinates (0,0), and those in "vertex1", and "vertex2", see below (in addition to being constrained to lie inside the region defined by LB and UB). NOTE: use TRUE when the treatments form a triangular experimental region in shape. If FALSE, maxima will only be constrained to lie inside the rectangular

region defined by LB and UB. Default is FALSE.

vertex1, vertex2

2x1 vectors with coordinates defining two of the 3 vertices of a triangular region. Must be provided if triangularRegion is TRUE (NOTE: vertices numbered

clockwise, vertex0=c(0,0) always)

maximization logical: if TRUE (default) it maximizes it FALSE it minimizes

xlab text label for x axis in confidence region plot (default: "Protein eaten, mg")

ylab text label for y axis in confidence region plot (default: "Carbohydrates eaten,

mg")

outputPDFFile name of the PDF file where the CR plot is saved (default: "CRplot.pdf")

outputOptimaFile

name of the text file containing the coordinates of all the optima found (same

information as in output vector xin, see below)

#### **Details**

This program approximates the confidence region (CR) of the location of the optimum of a Thin Plate Spline (TPS) in 2 regressors x constrained inside a rectangular region defined by LB and UB. If triangularRegion=TRUE it will also contain the optimum to lie inside the experimental region assumed to be well approximated by a triangle. The CR is generated point wise by bootstrapping the residuals of a TPS fit to the given (X,y) data, refitting Tps models, and solving the corresponding constrained maximization (or minimization) problems. The confidence region is approximated by the convex hull of all the solutions (x1\*,x2\*) found.

Usage assuming all default options:

out<-OptRegionTps(X=X,y=y,LB=LB,UB=UB)

### Value

meanPoint a 2x1 vector with the coordinates of the mean optimum point

xin an mx2 matrix with the x,y coordinates of all simulated #points that belong to

the confidence region (dim(m) is (1-alpha)\*nosim)

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#### Note

Upon completion, a PDF file containing the CR plot with name as set in outputPDFFile is created. A text file named as set in outputOptimaFile with all xin values is created too.

#### Author(s)

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#### References

Del Castillo, E., Hunt, J., Rapkin, J., and Zarmehri, S., "Confidence regions for the location of response surface optima: the R package OptimaRegion".

## **Examples**

```
## Not run:
## Example 1: randomly generated 2-variable response surface data
X<-cbind(runif(100,-2,2),runif(100,-2,2))</pre>
y<-as.matrix(72-11.78*X[,1]+0.74*X[,2]-7.25*X[,1]^2-7.55*X[,2]^2-4.85*X[,1]*X[,2]+2.55*X[,1]^2-1.85*X[,2]^2-1.85*X[,1]*X[,2]+2.85*X[,1]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,2]^2-1.85*X[,
rnorm(100,0,8))
## Find a 95 percent confidence region for the maximum of a Thin Plate Spline
model fitted to these data
\verb|out<-OptRegionTps(X=X,y=y,nosim=200,LB=c(-2,-2),UB=c(2,2), xlab="X1",ylab="X2")|\\
## Example 2: a mixture-amount experiment in two components (Drug dataset) with
non-normal data. Note triangular experimental region. Resulting 95p confidence
region of the maxima of a TPS model has area > 0. Contrast with region for
quadratic polynomial model. Note: 500 bootstrap iterations may take a few minutes.
out<-OptRegionTps(X=Drug[,1:2],y=Drug[,3],nosim=500,lambda=0.05,LB=c(0,0),UB=
   c(0.08,11), xlab="Component 1 (mg.)",ylab="Component 2 (mg.)",triangularRegion
   = TRUE, vertex1 = c(0.02,11), vertex2 = c(0.08,1.8), outputPDFFile=
   "Mixture_plot.pdf")
## End(Not run)
```

plotConvexHull

Computes and displays the convex hull of a set of 2-dimensional points

# Description

Given a vector of 2-dimensional coordinates, computes and displays the convex hull formed by these points.

## Usage

```
plotConvexHull(xin, LB, UB, xlab, ylab)
```

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## **Arguments**

xin	n x 2 vector of coordinate points
LB	2x1 vector of lower bounds for the x,y region where the convex hull is to be plot. Required.
UB	2x1 vector of lower bounds for the x,y region where the convex hull is to be plot. Required.
xlab	Label for x axis.
ylab	Label for y axis.

## Value

An integer vector giving the indices of the unique points lying on the convex hull, in clockwise order. (The first will be returned for duplicate points.). Same as returned by chull(xin).

## Note

Function also plots the convex hull upon return.

## Author(s)

E. del Castillo

# **Examples**

```
## Not run:
## Generate some random 2-dimensional point set

X<-cbind(runif(100,-2,2),runif(100,-2,2))

## Compute and plot convex hull

plotConvexHull(xin=X, LB=c(-4,-4), UB=c(4,4), xlab='X', ylab='Y')

## End(Not run)</pre>
```

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