PCRedux Package - An Overview

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0.1 Analysis of Simgmoid Shaped Curves for Data Mining and Machine Learning Applications: An Introduction

PCRedux is an open source software package for the analysis and numerical description of sigmoid curves. The descriptors (features) (subsection 0.4) can be used for applications such as data mining, automatic classification (e. g., positive, negative). This is in useful for applications in machine learning.

In the following chapters information are provided, which can be used for the analysis and numerical description of quantitative real-time PCR amplification curves. The determination of quantification points such as the Cq value is dealt with only marginally (e. g., subsubsection 0.1.3 ff.), since specific software packages and analysis procedures have already been described in other studies (subsubsection 0.1.4).

Instead, characteristics of amplification curves and sigmoid functions that can be used for the statistical and analytical description are discussed (subsubsection 0.4.2). The examples described in the following focus on the binary classification as positive of negative. Further, chapters describe the implementation of the hypotheses in the PCRedux package. This includes technologies used for quality control of the PCRedux package.

The availability of classified amplification curve datasets and technologies for the classification of amplification curves is of high importance to train and validate models. This is dealt with in subsection 0.3 and subsubsection 0.3.2, respectively.

0.1.1 Why is there is need for this software?

A classification as negative or positive amplification curve is feasible using bioanalytical methods such as melting curve analysis or an electrokinetic separation. However, this is not always possible or desirable. For example,

- Melting curves cannot be obtained with certain detection chemistries. For example, Taqman probes get hydrolyzed. An electrokinetic separation often requires too much effort for experiments with high sample throughput. A classification must also be carried out for both melting curve analysis and electrokinetic separation.
- There are algorithms such as linreg (J M Ruijter et al. 2009) that require information on whether an amplification curve is negative or positive for subsequent calculation.
- The mere classification into positive or negative is not necessarily the only aim of the PCRedux package. Instead, it is aimed that users and developers have tools to classify amplification curves automatically by any category conceivable. This can be for example a description of the amplification curve quality.

0.1.2 Technologies for Working with Amplification Curve Data

Data mining algorithms and machine learning can be used for descriptive and predictive tasks during the analysis of complex datasets. Data mining uses specific methods from statistical interference, software engineering and domain knowledge to

- obtain a better understanding of the data and
- to extract hidden knowledge

from the pre-processed data (Herrera et al. 2016). All this implies that a human being interacts with the data at the different stages of the whole process. The human being is therefore always a part of the workflow in data mining. Parts of the data mining process are

- the pre-processing of the data subsection 0.3,
- the description of the data,
- the exploration of the data and
- the search for connections and causes.

In contrast, machine learning uses instructions and data in software modules to create models that can be used to make predictions on novel data. In machine learning, the human being is much less necessary in the entire process. During machine learning, processes (algorithms) are used to create models with tunable parameters. These models automatically adapt their performance to the information (features) from the data. Well-known examples of machine learning technologies are Decision Trees (DT), Boosting, Random Forests (RF), Support Vector Machines (SVM), generalized linear models (GLM), logistic regression (LR) and deep neural networks (DNN) (Lee 2010). Recently, Reinforcement Learning has become more and more the focus of interest. The three following classes of machine learning are classically described in the literature:

- Supervised learning: These algorithms (e. g., logistic regression, SVM, DT, RF) learn from a training dataset of labeled and annotated data (e. g., "positive" and "negative"). It is used for building a generalized model of all data. These algorithms use error or reward signals to evaluate the quality of a solution found (Bischl et al. 2010, Greene et al. (2014), Igual and Seguí (2017)).
- Unsupervised learning: Algorithms, such as k-means clustering, kernel density estimation, LDA or PCA learn from training datasets of unlabeled or non-annotated data to find hidden structures according to geometric or statistical criteria (Bischl et al. 2010, Greene et al. (2014), Igual and Seguí (2017)).
- Reinforcement Learning: The algorithms learn by reinforcement from criticism. The criticisms inform the algorithm about the quality of the solution found. But the criticism says nothing about how to improve. These algorithms iteratively search the improved solution in the entire solution space (Bischl et al. 2010, Igual and Seguí (2017)).

Decision trees are a classic approach to machine learning (Quinlan 1986). Here relatively simple algorithms and simple tree structures are used to create a model. R offers several packages like party (Hothorn, Hornik, and Zeileis 2006) and rpart (Therneau, Atkinson, and Ripley 2017) for creating decision trees. Graphical user interface like Rattle (Williams 2009) offer convenient user interfaces for data mining with R. Applications of decision trees are shown in later chapters.

Binomial logistic regression¹ is used in data science and machine learning to gain knowledge about a binary relationship. In specific, Binomial logistic regression can be used to fit a regression model, y = f(x) if y is a categorical variable with two states (e. g., negative, positive). Thus, binary variables have exactly two values (negative $\to 0$, positive $\to 1$). Typically, this model is used for predicting y with n predictors $x_{i1}, \ldots, x_{k1}, (i = 1, \ldots, n)$. The predictors can be a mixture of continuous and categorical. The logit model is a robust and versatile classification method that can be used to explain a dependent binary variable. Their codomain of real numbers is limited to [0,1]. Probabilities can therefore be utilized. Logistical distribution function $F(\eta)$, also known as the response function, is strictly monotone increasing and limited to this range.

 η_i establishes the link between the probability of the occurrence and the independent variables. For this reason, η_i is referred to as a link function. The distribution function of the normal distribution is an

 $^{^{1}}$ Logistical regression can also be used to predict a dependent variable that can assume more than two states. In this case, it is called a multinomial logistic regression. An example would be the classification y of amplification curves as *slightly noisy*,*medium noisy* or *heavily noisy*.

alternative to the logistical distribution function. By using the normal distribution, the Probit model is obtained. However, since this is more difficult to interpret, it is less widely used in practice. Since probabilities are used, it is possible to make a prediction about the probability of occurrence of an event. When analyzing amplification curves, a diagnosis can be made whether a reaction was unsuccessful (0) or successful (1). For the prediction independent metric variables are used. The metric variables have interpretable distances with a defined order. Their codomain is $[-\infty,\infty]$. The logistic distribution function on the independent variables can be used to determine the probability for $Y_i = 0$ or $Y_i = 1$. A logistic regression model can be formulated as follows:

$$F(\eta) = \frac{1}{1 + exp(-\eta)}$$

The logistic regression analysis is based on the maximum-likelihood estimation (MLE). In contrast to linear regression, the probability for Y = 1 is not modeled from explanatory variables. Rather, the logarithmic chance (logit) is used for the occurrence of Y = 1. The term *chance* refers to the ratio of the probability of occurrence of an event (e. g., amplification curve is positive) and the counter-probability (e. g., amplification curve is negative) of an event.

In the ideal case, this should achieve a high degree of objectivity and reproducibility. It is not always possible to justify this ideal, because the algorithms can be biased as the human. One reason is that humans design the algorithms and curate the dataset used for the learning. In particular, datasets can be biased if the human expert excludes seemingly problematic data.

The model should then be able to bring new unknown data into a meaningful context. The selected features have a significant influence on the accuracy of the model. In machine learning, variables are features that are used to train a model (Saeys, Inza, and Larranaga 2007). Therefore, it is important to identify or generate new features potential features and to test them intensively. Regarding amplification curves, only a few features have been described in the literature so far. They are described in the following sections. Dedicated applications and descriptions of features in the peer-reviewed literature is not described.

Since machine learning algorithm for the analysis of amplification curve data were not available in the literature, it was necessary to speculate, which characteristics should be extracted by the processing algorithm and broken down into characteristic vectors. The number of proposed features that can be created with the algorithms of the PCRedux package was presumably the most extensive collection at the time of first release in summer 2017. Previously, only a few characteristics of amplification curves were described in the literature. Thus, it would be too few to use them extensively for machine learning with qPCR data. An application of those for machine learning could also not be found.

The algorithms of machine learning consist of several steps including careful data pre-processing and quality management. In a first step, relatively large datasets of known characteristic vectors have to be collected, measured and calculated as raw data. In a second step, these characteristics are used to classify unknown feature vectors using the machine learning algorithm. For example, the amplification curves would have to be divided into training data and test data from the entire dataset at random.

0.1.3 Relevance of Amplification Curve Data Analysis

PCRedux is an R package for the analysis of sigmoid curves. Data with sigmoid curves are common in many biological experiments. A widely used bioanalytical method is the quantitative real-time PCR (qPCR). qPCRs are applied in human diagnostics, life sciences and forensics (Martins et al. 2015, Sauer, Reinke, and Courts (2016)).

qPCRs are performed in thermo-cyclers, which are equipped with a real-time monitoring technology. There are numerous manufactures, which produce thermo-cyclers as commercial products or as part of scientific projects. An example for a thermo-cycler that originated in scientific project is the VideoScan technology (Rödiger et al. 2013).

Predefined temperatures can be set in thermo-cyclers to amplify DNA segments using the polymerase chain reaction (PCR). Most of the thermo-cyclers have a thermal block with wells at certain positions. Reaction vessels containing the PCR mix are inserted into these wells. There are also thermo-cyclers that use capillary tubes (e. g., Roche Light Cycler 1.5). The capillaries are heated and cooled by air. The thermo cycler raises and lowers the temperature in the reaction vessels in discrete, pre-programmed steps

so that the PCR reaction can take place. The instruments with a real-time monitoring function sensors to measure changes of the fluorescence intensity in the reaction vessel. All thermo-cycler systems have software that processes and outputs the measured data. Plots of the fluorescence observations versus cycle number obtained from two different qPCR systems is shown in Figure 1A and B. The thermo-cyclers produce different amplification curve shapes even with the same sample material and PCR mastermix because of their technical design, sensors and software. These factors need to be considered during the development of analysis algorithms.

Sigmoid functions are non-linear, real-valued, have a S-shaped curvature (Figure 1) and are are differentiable (e. g., first derivative maximum, with one local minimum and one local maximum). For this purpose, a sigmoid function can fitted to the dataset. With the model obtained, predictions can be made. For example, the position of the second derivative maximum can be calculated from this (Figure 3). In the context of amplification curves, the second derivative maximum is commonly used to describe the relationship between the cycle number and the PCR product formation (Equation 2).

The analysis of sigmoid data (e. g., quantitative PCR) it is a manageable task if the data volume is low, or dedicated analysis software is available. An example such a scenario (low number of amplification curves) is shown in Figure 1A. All 65 curves exhibit a sigmoid curve shape. In contrast, the vast number of amplification curves in Figure 1B is barely manageable with a reasonable effort by simple visual inspection. These data originate from a high-throughput experiment that encompasses in total 8858 amplification curves. Moreover, a manual analysis of the data is time-consuming and prone to errors.

During the setup of a qPCR assay, a manual analysis is a justified and reasonable approach to get acquainted with the characteristics and challenges of the qPCR data. At least hypothetically, it can hardly be denied that the trained human expert can best interpret the dataset. In particular, artifacts and outliers in a series of measurements can usually be readily identified by humans. When large amounts of data need to be processed, however, manual analysis is unfavorable. In addition, the objectivity of an expert can be questioned. It is an open secret that data from quantitative real-time PCRs are occasionally subject to problematic post-processing. In particular, the reproducible and objective analysis of the amplification curve data exposes challenges to inexperienced users. Even among peers is not uncommon that they judge (classify) results differently. An example on this problem is given in Figure 1.

0.1.4 Software for the Analysis of Amplification Curve Data

There are several open source and closed source software tools, which can be used for the analysis of qPCR data (Pabinger et al. 2014). A large proportion of the algorithms is implemented in the R statistical computing language. However, more dedicated literature is available from peer-reviewed publications and textbooks. The software packages deal for example with

- missing values and non-detects (McCall et al. 2014),
- noise and artifact removal (Rödiger, Burdukiewicz, and Schierack 2015, Rödiger et al. (2015), Spiess et al. (2016)),
- inter run calibration (Jan M. Ruijter et al. 2015),
- normalization (Rödiger, Burdukiewicz, and Schierack 2015, Jan M. Ruijter et al. (2013), Feuer et al. (2015), Matz, Wright, and Scott (2013)),
- quantification cycle estimation (Ritz and Spiess 2008, Jan M. Ruijter et al. (2013)),
- amplification efficiency estimation (Ritz and Spiess 2008, Jan M. Ruijter et al. (2013)),
- data exchange (Lefever et al. 2009, Perkins et al. (2012), Rödiger et al. (2017)),
- relative gene expression analysis (Dvinge and Bertone 2009, Pabinger et al. (2009), Neve et al. (2014)) and
- data analysis pipelines (Pabinger et al. 2009, Ronde et al. (2017), Mallona, Weiss, and Egea-Cortines (2011), Mallona et al. (2017)).

All softwares assume that the amplification resemble a sigmoid curve shape (ideal positive amplification reaction), or a flat low line (ideal negative amplification reaction). For example, Ritz and Spiess (2008) published the qpcR R package that contains functions to fit several multi-parameter models. This includes the five-parameter Richardson function (Richards 1959), which is often used for the analysis of qPCR data.

Researchers have found many solutions to challenges that were daunting the users of the qPCR methodology

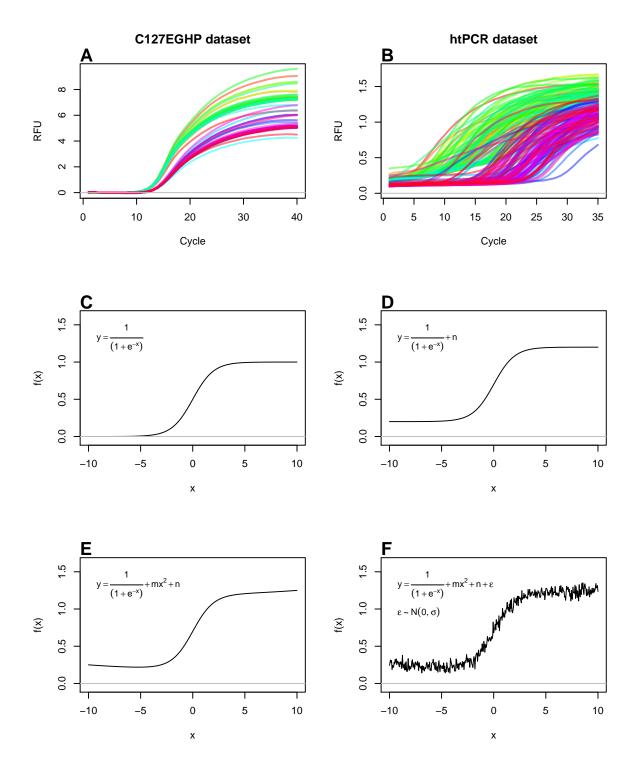


Figure 1: Amplification curve data from an iQ5 (Bio-Rad) thermo-cycler and a high throughput experiment in the Biomark HD (Fluidigm). A) The C127EGHP dataset (chipPCR package, (Rödiger, Burdukiewicz, and Schierack 2015)) with 64 amplification curves was produced in conventional thermo-cycler with a 8 x 12 PCR grid. B) The htPCR dataset (qpcR package, (Ritz and Spiess 2008)), which contains 8858 amplification curves, was produced in a 95 x 96 PCR grid. Only 200 amplification curves are shown. In contrast to A) have all amplification curves in B) an off-set (intercept) of circa 0.25 RFU. C) Model function of a one-parameter sigmoid function. D) Model function of a sigmoid function with an intercept n = 0.2 RFU. E) Model function of a sigmoid function with an intercept n = 0.2 RFU. E) Model function of a sigmoid function with an intercept n = 0.2 RFU and a square portion $n = x^2$. F) Model function of a sigmoid function with an intercept n = 0.2 RFU and a square portion of n = 0.2 RFU and a square portion of n = 0.2 RFU and additional noise n = 0.2 RFU distributed).

in the past. For example selected qPCR systems have a periodicity in the amplification curve data (Spiess et al. 2016). Presence a periodicity exposes the risk of introducing artificially shifts in the Cq values. Another commonly employed pre-processing step of qPCR is smoothing and filtering. Both approaches cause alterations to the raw data that affects both the estimation of the Cq value and the amplification efficiency. The particular the cycle threshold method (Ct method) (Figure 3) is affected by these factors (Spiess et al. 2015, Spiess et al. (2016)). Provided that such challenges are addressed, many algorithms for the processing of the positive amplification curves are available.

Most software packages do not make a classification if an amplification curve. For example, a classification could be if the amplification curve is negative or positive. An other classification could indicate whether the quality of the amplification curve is poor (much noise) or good (low noise). Specialized software that can distinguish the amplification curves automatically is needed. A classification of amplification curves is needed for later data processing steps. For example, the linreg method by J M Ruijter et al. (2009) requires a decision, if an amplification curve is positive or negative. The qpcR package (Ritz and Spiess 2008) contains an amplification curve test via the modlist() function. The parameter check="uni2" offers an analytical approach, as part of a method for the kinetic outlier detection. It checks for a sigmoid structure of the amplification curve. Then it tests for the location of the first derivative maximum and the second derivative maximum. However, multi-parameter functions fit "successful" in most cases including noise and give false positive results. This will be shown on later sections.

Sometimes it is difficult even for a human expert to classify the amplification curves unambiguously and reproducible. To illustrate this an example for the analysis and classification of the htPCR dataset is given in Figure 5.

A bottleneck of qPCR data analysis is the lack of features that can be used to build classifiers for amplification curve data. A classifier herein refer to a vector of features that can be used to distinguish the amplification curves by their shape only.

One reason for this is the lack of features that are known for amplification curve data. Only few features for amplification curves are described in the literature. An example example is the amptester() function, which is part of the chipPCR package (Rödiger, Burdukiewicz, and Schierack 2015). This function uses static thresholds and frequentist inference to identify amplification curves that exceed the threshold. These are then classified as positive. However, it can also lead to false-positive classifications as exemplified in Figure 6.

0.1.5 Principles of Amplification Curve Data Analysis

The shape of a positive amplification curve follows in most cases a sigmoid shape. The curvature of the amplification curve can be used as a quality measure. For example, fragmentation, inhibitors and sample material handling errors during the extraction can be identified. The kinetic of fluoresce emission is proportional to the quantity of the synthesized DNA. Typical amplification curves have three phases.

1. Ground phase: This phase occurs during the first cycles of the PCR. The fluorescence emission is in most cases flat. During the ground phase, only a weak fluorescence signal is generated that cannot be detected by the sensor system. This is often referred to as baseline or background signal. Fragmentation, inhibitors and sample handling errors would result in a prolonged ground phase. Apparently, there is only a phase shift or no signal at all. This is primarily due to the limited sensitivity of the instrument. Even in a perfect PCR reaction (double amplification per cycle), qPCR instruments cannot detect the fluorescence signal from the amplification. In these early cycles, the fluorescence signals only produce a fluorescence background signal. The PCR product signal is an insignificantly small component of the total signal. Nevertheless, this phase may indicate some typical properties. For example, the increase and signal variation can be characteristic of the qPCR system or probe system. In many instruments, this phase is used to determine the Ct threshold (a statistically relevant increase outside the noise range). A signal that is far enough above this threshold is considered as coming from the amplicon. It is assumed that this early cycle phase is flat in the amplification curve. In some qPCR systems a flat amplification curve is expected in this phase. Slight deviations from this trend are presumed to be due to changes (e. g., disintegration of probes) in the fluorophores. Background correction algorithms are often used here to ensure that flat amplification curves without slope are generated. This can lead to errors and inevitably leads to a loss of information via the waveform of the raw data (Nolan, Hands, and Bustin 2006).

- 2. Exponential phase: This phase follows the ground phase and is also called log phase. This phase is characterized by a strong increase of the emitted fluorescence. In this phase, the amount doubles in each cycle under ideal conditions. The amount of the synthesized fluorescent labeled PCR product is high enough to be detected by the sensor system. This phase is used for the calculation of the quantification point (Cq) and for the calculation of the curve specific amplification efficiency. Fragmentation, inhibitors and sample handling errors would decrease the slop of the amplification curve (Spiess, Feig, and Ritz 2008, Ritz and Spiess (2008)).
- 3. Plateau phase: This phase follows the exponential phase. The cause for this lies in the exploitation of the limited resources (incl. primers, nucleotides, enzyme activity) in the reaction vessel. This limits the amplification reaction, so that the theoretical maximum amplification efficiency (doubling per cycle) no longer prevails. This turning point and the progressive limitation of resources finally leads to a plateau. In the plateau phase, there is sometime a signal decrease called hook effect (Isaac 2009).

If the amplification curve has only a slight positive slope and no perceptible exponential phase, it can be assumed that the amplification reaction did not occur. Causes may include poor specificity of the PCR primers, degraded sample material, degraded probes or detector problems. Such a curve can also occur if non-specific PCR products are created at different points in time. In this case, the superimposed signals can generate such a signal progression. If there is a lot of start DNA (detectable amplification in the first cycles) and the instrument software makes a background correction, amplification curves with a strongly negative trend can be erroneously generated.

Such phases can be roughly considered as regions of interest (ROI). As an example, the *ground phase* is in the head area, while the *plateau phase* is in the tail area. The *exponential phase* is located between these two ROIs.

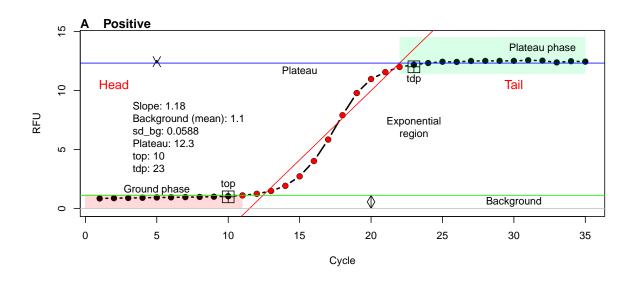
Numerous qPCR systems do not display the raw data of the amplification curves on the screen. Instead, the raw data is usually processed by the instrument software to remove fluorophore-specific effects and background noise. The ordinate often does not display absolute fluorescence, but rather the change in fluorescence per cycle. Smoothing algorithms may also have been used (Spiess et al. 2015). When using the PCRedux package, it is therefore advisable to clarify beforehand, which processing steps the amplification curves have been subjected to until data export. Failure to do so may result in misinterpretations and incorrect models (Nolan, Hands, and Bustin 2006, Rödiger et al. (2015), Rödiger, Burdukiewicz, and Schierack (2015), Spiess et al. (2015)).

The most important measurement from qPCRs is the cycle of quantification (Cq), which signifies at which PCR cycle the fluorescence exceeds a threshold value. There is an ongoing debate as to what a significant and robust threshold value is since there are several mathematical methods to calculate the Cq. The classical threshold value (cycle threshold, Ct) is a straight horizontal line, which intersects with the quasi-linear phase in the exponential amplification phase of the PCR. Another Cq method uses the maximum of second derivative (SDM) (Rödiger et al. 2015). Figure 3 illustrates the calculation of Cq values and Ct values. The threshold based method is claimed to be a simple yet effective approach. This method requires that amplification curves are properly base-lined prior to the analysis. This is not always desirable. An overview and performance comparison is given in Jan M. Ruijter et al. (2013).

In all cases the Cq value can be used to calculate the concentration of target sequence in a sample (low $Cq \rightarrow high$ target concentration). In contrast, negative or ambiguous amplification curves loosely resemble noise. This noise may appear linear or exhibit a curvature (Figure 6). Many factors, such as the sample quality, qPCR chemistry, and technical problems (e. g., sensor errors) contribute to various curve shapes. A common phenomenon of amplification curve shapes is the 'hook effect' (Barratt and Mackay 2002, Jan M. Ruijter et al. (2014)). This however, may result in faulty interpretation of the amplification curves.

This means that the amplification curve shape, the amplification efficiency and the Cq value are prerequisites to judge the outcome of a qPCR reaction. In all phases of PCR the curves should be smooth. Possible peaks in the curves may be due to unstable light sources from the instrument or problems during sample preparation, such as the presence of bubbles in the reaction vessel.

An important step in the qPCR workflow is data analysis. Progress has been made in qPCR data analysis, primarily due to the availability of sophisticated data analysis pipelines and software packages (e. g., Jan M. Ruijter et al. (2013), Jan M. Ruijter et al. (2015), Rödiger et al. (2015), Spiess et al. (2015), Spiess et al. (2016)). At this stage amplification curve (Rödiger, Burdukiewicz, and Schierack 2015) and melting curve pre-processing (Rödiger, Böhm, and Schimke 2013) needs to be performed to continue



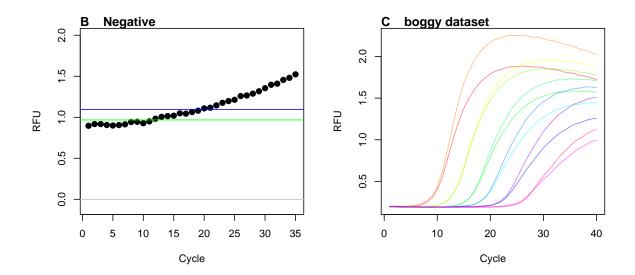


Figure 2: Regions of interest in amplification curves. A) In general, the fluorescence emitted (RFU, relative fluoresce units) by the reporter dye (e.g., SYBR Green, EvaGreen) is plotted against cycle number. The amplification curve data was taken from the testdat dataset (qpcR package). More generally, amplification curves can be divided into three regions of interest. These are the ground phase, exponential phase and plateau phase. top, takeoff point. tdp, takdown point. sd_bg is the standard deviation within the ground phase. The exponential region (red dots) can be used to determine the Cq values and estimates of amplification efficiency. The straight red line is the regression line of a linear model. In principle, after further processing steps (e.g., logarithmetic), slopes in this range can be determined. B) PCRs without amplification reaction are usually characterized by a flat (non-sigmoid) signal. C) The exponential phase of PCR reactions may vary considerably. Ideally, the slopes are the same for all reactions. This would be synonymous with the same amplification efficiency in all reactions. However, in practice, amplification curves with different increases are usually found. In particular, amplification curves that become detectable in later cycles often have lower increases.

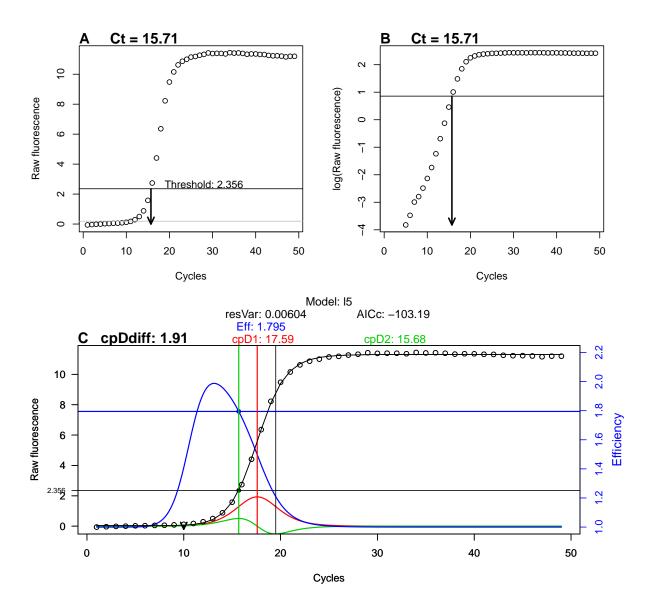


Figure 3: Commonly used methods for the analysis of quantification points. A) Linear plot of an amplification curve with a typical sigmoid shape. The Grey horizontal line is the threshold as determined by the 68-95-99.7 rule from the fluoresce emission of cycle 1 to 10. The black horizontal line is the user defined threshold in the log-linear range of the amplification curve. The Ct is calculated from the intersection of the horizontal line and a quadratic polynomial fitted in to the amplification curve (see Rödiger, Burdukiewicz, and Schierack (2015) for details). B) The Amplification curve plot with a logarithmic ordinate visualizes the linear phase. C) Analysis of the amplification curve by fitting with a five parameter model (black line) (Equation 2). The red line is the first derivative of the amplification curve, with the maximum at 17.59 cycles. The maximum is used in selected system as Cq value and referred to as first derivative maximum (cpD1). The green line is the derivative of the amplification curve, with the maximum at 15.68 cycles a minimum approximately at 19.5 cycles. The maximum is used in selected system as Cq value and referred to as second derivative maximum (cpD2). The blue line is the amplification efficiency that is estimated from the trajactory of the exponential region. The Eff value 1.795 means that the amplification efficiency is approximately 89%. cpDdiff is the difference between the Cq values calculated from the first and the second derivative maximum (cpD1) from the fitted model.

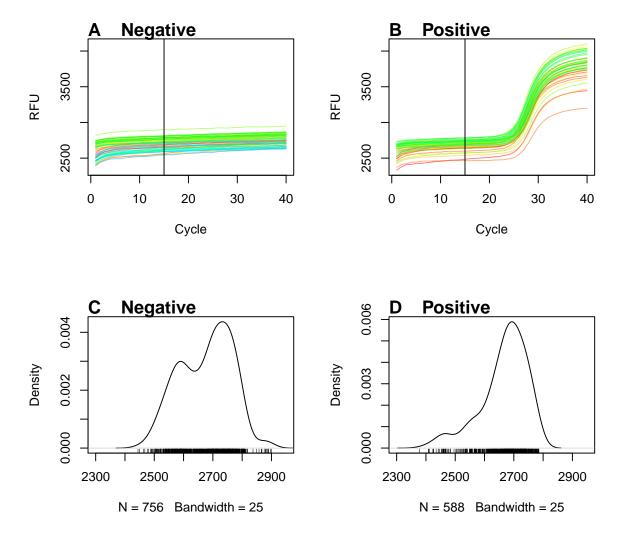


Figure 4: Amplification curves of the RASO02 dataset. All amplification curves of the RASO02 dataset were manually classified (negative,positive). A) The negative amplification curves have no sigmoid curve progression. Two groups with different signal levels form the amplification curves. B) All positive amplification curves have a sigmoid curve shape and a similar ground signal. C) The density function of the RFU values from the first 15 PCR cycles shows a bimodal distribution. Based on these data, it is easy to divide them into two groups. Both groups' density functions appear to be symmetrical. D) The density function from the RFU values of the first 15 PCR cycles shows a monomodal distribution. It seems that the density function of the RFU values is left-skewed.

next with the feature extraction from the curvatures. Several studies have been done, which discuss the pre-processing and post-processing of qPCR data (Rödiger, Burdukiewicz, and Schierack 2015, Spiess et al. (2015), Spiess et al. (2016)). In this work the focus is on amplification curve data. Amplification curves can be difficult to interpret and analyze if the curvature deviates from the ideal sigmoid shape, or the volume of curve data is to large for an economic manual analysis. Moreover, amplification curves may look acceptable for an inexperienced use but unacceptable for an expert. Therefore, there is a need for method of statistical interrogation and objective interpretation of results.

The quantification of nucleic acids by curve parameters like the quantification point (Cq) and the amplification efficiency (AE) is only meaningful if the kinetic of the amplification curve follows a sigmoid structure according to the model the qPCR (Jan M. Ruijter et al. 2013, Jan M. Ruijter et al. (2014), Ritz and Spiess (2008)). In qPCRs is sigmoid shape is characterized by a baseline region, an exponential region and a (maximum) plateau phase. The magnitude of the raw fluorescence and the shape of the amplification curve vary naturally between detection probe systems and devices. Therefore, it is challenging identifying negative curves which appear to be positive but just an artifact of scaling.

Most assays have an intrinsic property, which can be used to decide if an amplification reaction is positive, negative or ambiguous. Melting curve analysis belongs to the commonly used approaches (Rödiger, Böhm, and Schimke 2013). For example qPCRs monitored with unspecific dyes (e. g., EvaGreen) use melting curve analysis is a post-processing method to identify PCR reactions which contain DNA (positive). Some detection probe systems like hydrolysis probes do not permit such methods.

A typical situation is that results samples may positive, negative or ambiguous. The later are most problematic because both outcomes (positive and negative) might be true. However, in most cases the user is interested in an automatic distinction between positive and negative samples. This is import in screening applications.

Provided that the rules are strict and transparent, such a routine can be used for quality management. This is also in conformance with the philosophy that software in research and diagnostics should be a foundation for reproducible research (Rödiger et al. 2015).

The Ct method appears to be the most widely used method despite the fact that this method was shown to be unreliable (Jan M. Ruijter et al. 2013, Spiess et al. (2015), Spiess et al. (2016)). Presumably this due to the familiarity of users with this approach since it is also known from chemical analysis procedures or basic calculus. Another reason might be that the Ct method is easy to implement and to understand.

This kind of calculation strongly dependents on the user, who has to adjust the threshold level manually. Thus, the Ct method is not stable in predictions if several users are given the same dataset to be analyzed. Moreover, the Ct method makes the assumption that the amplification efficiency (~ slope in the log-linear phase) is equal across all amplification curves compared (Jan M. Ruijter et al. 2013). Evidently, this is not always case as exemplified in Figure 2C.

Another approach is to use non-linear model to fit the amplification curve. For example, five-parameter Richardson functions (Equation 2, Richards (1959)) are often used (Spiess et al. 2015).

A comment on noise in sigmoid amplification cures: Noise in amplification curves can have very different causes. Among them are incorrectly assigned dye detectors, errors during the calibration of dyes for the instrument, errors during the preparation of the PCR master mix, sample degradation, lack of a sample in the PCR, too much sample material in the PCR mix or a low detection probe concentration.

0.2 Development, Implementation and Installation

PCRedux is an open source software package for the statistical computing language R. This software is published under the terms of the MIT license². PCRedux contains function for the calculation of features from amplification curves and classified datasets for machine learning applications.

Reproducibility is a foundation of research. All technical and experimental aspects should be performed under principles that follow good practices of reproducible research. Numerous authors addressed the matter for experimental design and data report. Examples are the *Minimum Information for Publication of Quantitative PCR Experiments* guidelines (MIQE) and the *Real-time PCR Data Markup Language* (RDML). MIQE is a recommended standard of the minimum information for publication of quantitative real-time PCR experiments guidelines and RDML is a data exchange format (S. A. Bustin 2014, S. Bustin (2017), Rödiger et al. (2015), Rödiger et al. (2017), Wilson et al. (2017)). Both MIQE and RDML, are widely used to preform quantitative real-time PCRs (Pabinger et al. 2014).

The development of scientific software is a complex process. In particular, if the development is carried out by teams who work in different time zones and where no face-to-face meetings a possible. End users need releases with stable software that delivers reproducible results. Developers need well documented software the adopt the software according to their needs.

Under the umbrella Agile Software Development and Extreme Programming, several principles were proposed to deliver high quality software, which meet the needs of end users and developers. This includes version control, collaborative editing, unit testing and continuous integration (Lanubile et al. 2010, Myers et al. (2004), Rödiger et al. (2015)). The following paragraphs describe methods implemented in the PCRedux package to ensure high software quality.

0.2.1 Version Control and Continuous Integration

The development of the PCRedux package started 2017 with the submission of a functional, yet immature source code, to GitHub (GitHub, Inc.). GitHub is a web-based version control repository hosting service. Both distributed version control and source code management are based on Git. (Lanubile et al. 2010). Additional functionality of GitHub includes the administration of access management, bug tracking, moderation of feature requests, task management, some metrics for the software development, and wikis. The source code of PCRedux is available at:

https://github.com/devSJR/PCRedux/

In continuous integration development team members commit and integrate their contributions several times a day. Team members may include coders, artists and translators. An automated build and test system verifies each integration and gives the development team members a timely feedback about the effect of their commit. In contrast to deferred integration leads this to a reduced number of integration problems and less workload because most erros are solved shortly after they were integrated (Myers et al. 2004).

TrivsCI was chosen as continues integration service for PCRedux. The TravisCI server communicates with the GitHub version control system and manages the PCRedux package building process. Currently the continuous interaction is available for the R releases *oldrel*, *release* and *devel*. The history of the build tests are available at

https://travis-ci.org/devSJR/PCRedux

0.2.2 Naming Convention and Literate Programming

The PCRedux software is provided as an R (\geq v. 3.3.3) package. PCRedux is written as S3 object system. S3 has characteristics of object orientated programming but eases the development due to the use of the naming conventions (Brito 2008). In most places function and parameter names are written as underscore separated (underscore_sep), which is a widely used style in R packages (Bååth 2012). This convention had to be violated in coding sections where functionality from other packages was used.

²https://opensource.org/licenses/MIT

Literate programming, as proposed by Knuth (1984), is a concept where the logic of the source code and documentation is integrated in a single file. Markup conventions (e. g., '#') tell in literate programming how to typeset the documentation. This produces outputs in a typesetting language such as the lightweight markup language **Markdown**, or the document preparation system IAT_FX.

The roxygen2, rmarkdown and knitr packages were used to write the documentation in-line with code for the PCRedux package.

0.2.3 Installation of the PCRedux Package

The development version of the package can be installed using the The developer version of the package can be installed using the devtools package.

```
# Install devtools, if not already installed.
install.packages("devtools")

library(devtools)
install_github("devSJR/PCRedux")
```

PCRedux is available as stable version from the Comprehensive R Archive Network (CRAN) at https://CRAN.R-project.org/package=PCRedux. Package published at CRAN undergo intensive checking procedures. In addition, CRAN tests whether the package can be built for common operating systems and whether all version dependencies are solved. To install PCRedux first install R (\geq v. 3.3.3). Then start R and type in the prompt:

```
# Select your local mirror
install.packages("PCRedux")
```

The PCRedux package should just install. If this fails make sure you that write access is permitted to the destination directory.

```
# The following command points to the help for download and install of packages
# from CRAN-like repositories or from local files.
?install.packages()
```

If this fails try to follow the instructions given by De Vries and Meys (2012).

R CMD check

Results from CRAN check can be found at

http://cran.us.r-project.org/web/checks/check results PCRedux.html.

0.2.4 Unit Testing of the PCRedux Package

Modules testing, better known as unit testing, is an approach to simplify the refactoring of source code during software development. The goal is to minimize errors and regressions. It is also intended to ensure that the numerical results from the calculations are reproducible and of high quality. An unintended behavior of the software should be detected at the latest during the package building process. Please note that Unit Testing is not a guarantee for error-free software (Myers et al. 2004).

The basic concept is to use checkpoints to check whether the software performs calculations and data transformations correctly for all builds. For this, numerous (logical) queries have to be defined by the developer in advance. They are refereed to *expectations*. It should be ensured that as many errors as possible are covered. A logical query can be, for example, whether the calculation has a numeric or Boolean value as output. If the data type is incorrect during output, this is a sufficient termination criterion. Or it can be checked whether the length of the result vector is correct after the calculation. There are different approaches for unit tests in R. This also includes testing of units from the packages RUnit, covr, svUnit and testthat. (Wickham (2011)).

The package testthat was used in PCRedux because it could be well implemented and its maintenance is relatively simple. The logic is that an *expectation* defines how the result, class or error in the corresponding

unit (e. g., function) should behave. Unit tests can be found in the /test/testthat subdirectory of the PCRedux package. The unit tests always run automatically during the creation of the package. The following is an example of the function qPCR2fdata(). The details of how qPCR2fdata() works are detailed in the paragraph 0.4.1.4 section. The function test_that(), from the testthat package, is given several expectations. The qPCR2fdata() function when processing the amplification curves check whether:

- an object of the class *fdata* is created (see Febrero-Bande and Oviedo de la Fuente (2012) for details of the class *fdata*),
- the parameter rangeval has a length of two,
- is the second value of parameter rangeval 49 (last cycle number) and *whether the object structure of the function qPCR2fdata() does not change if the parameter preprocess=TRUE is set.

```
library(PCRedux)

context("qPCR2fdata")

test_that("qPCR2fdata gives the correct dimensions and properties", {
   library(qpcR)
   res_fdata <- qPCR2fdata(testdat)
   res_fdata_preprocess <- qPCR2fdata(testdat, preprocess = TRUE)

expect_that(res_fdata, is_a("fdata"))
   expect_that(length(res_fdata$rangeval) == 2 &&
    res_fdata$rangeval[2] == 49, is_true())

expect_that(res_fdata_preprocess, is_a("fdata"))
   expect_that(length(res_fdata_preprocess$rangeval) == 2 &&
    res_fdata_preprocess$rangeval[2] == 49, is_true())
}</pre>
```

Similar unit tests were implemented for all functions of the PCRedux package. The coverage by PCRedux package can be calculated by the package_coverage() function from the covr package or visual analyzed at

https://codecov.io/gh/devSJR/PCRedux/list/master/.

0.3 Technologies for Amplification Curve Classification and Classified Amplification Curves

An extensive literature research showed that in the field of qPCR there are no openly accessible datasets. Open Data is meant in the sense that data are freely available, free of charge, free to use and that data can be republished, without restrictions from copyright, patents or other mechanisms of control (Kitchin 2014). Furthermore, only a few attributes of amplification curves are discussed among peers. These include:

- the signal height and the slope in the baseline region (gradient and intersection),
- the starting point of amplification,
- the Cq value and amplification efficiency, and
- the signal level including the slope of the plateau phase (slope, intercept).

However, these alone are presumably not enough to describe amplification curves sufficiently. Furthermore, there are no references to further algorithms that can be used to calculate additional features from amplification curves. All these facts make further studies on machine learning and modeling difficult. A feature can be described as an entity that characterizes an object. The number of features should be large enough to describe the object accurately and small enough not to interfere with the learning process with redundant or information.

Bellman coined the so-called *Curse of Dimensionality* in 1961, when he dealt with adaptive control processes. It vague describes the practical difficulties encountered in high-dimensional analysis and estimation. It states that for a given sample size, there is a maximum number of features from which the performance of an algorithm degrades rather than improves. As a consequence, many data mining algorithms fail when the dimensionality is high, because the data points are sparsely populated and far apart (Herrera et al. 2016).

Therefore, a large number of records with amplification curves and their classification (negative, ambiguous, positive) were included in the PCRedux package. Another objective was the development of new algorithms and the transfer of algorithms from other domains (e. g., from digital image processing) to qPCR datasets. A central goal was therefore to develop attributes to enable the classification of amplification curves in categories such as positive, negative and ambiguous.

0.3.1 Classified Amplification Curves

It is worth noting that the classifications of amplification curves in Table 1 were made on the basis of empirical values. For the amplification curves, only an assessment was made to see if the curves are approximately sigmoid or resemble a negative amplification reaction with a flat curve shape. Consequently, this does not answer the question of if a specific amplification product has been synthesized, if a contamination has been amplified or if only primer-dimers have been amplified. To answer this question, other methods such as melting curve analysis should be used.

Amplification curves from different sources had to be classified manually. Amplification curves from the qpcR, chipPCR, PCRedux and RDML packages were classified with the humanrater(), as described in Rödiger, Burdukiewicz, and Schierack (2015) and with the tReem() function from the PCRedux package. The subsubsection 0.3.2 describes approaches that can be used to classify amplification curves.

Data preparation is an important step, that includes data cleansing, data transformation and data integration (Herrera et al. 2016). The xray package (Seibelt 2017) can used to analyze the distribution form and variables in records for anomalies such as missing values, zeros, infinite values and their categories. The anomalies() function from the xray package can be used to search for anomalies (including missing values (NA), zero values (Zero), blank strings (Blank) and infinite numbers (Inf)). Users of the PCRedux package should use such tools before continuing to work with the records. Although most records in the PCRedux package have the same data structure, some records contain missing values or have different dimensions (compare data from Figure 1). For example, the dataset C127EGHP spans a matrix of 40 x 66 (35 cycles x observations (65 amplification curves)), while the htPCR dataset comprises a matrix of 35 x 8859.

Raw data were exported as comma separated values from the thermo-cyclers. Some records have been exported from the devices using the RDML package and transformed into RDML format. A detailed

description can be found in Rödiger et al. (2017). The Real-time PCR Data Markup Language (RDML) is data exchange format for quantitative Real-Time PCR Experiments. RDML is a human readable file format and is based on XML (eXtensible Markup Language) and was created to enable the exchange of data across different information systems (Lefever et al. 2009). The following code section describes the import of an RDML file from the PCRedux package. The RDML file contains amplification curve data of a duplex qPCR (HPV 16 & HPV 18) performed in the CFX96 (Bio-Rad).

```
library(RDML)
# Load the RDML package and use its functions to import the amplification curve
# data
library(RDML)
filename <- system.file("RAS002.rdml", package = "PCRedux")
raw_data <- RDML$new(filename = filename)</pre>
```

The further processing of the amplification data took place as described in Rödiger, Burdukiewicz, and Schierack (2015), Rödiger et al. (2015), Spiess et al. (2015) and Spiess et al. (2016). An introduction to the use of R for the analysis of melting curves (MBmca package, (Rödiger, Böhm, and Schimke 2013)) and the calculation of Cq values (chipPCR package, (Rödiger, Burdukiewicz, and Schierack 2015)) is shown in detail in Rödiger et al. (2015). Unless otherwise stated, the Cq values were determined using the second maximum derivative method.

The following example shows the export of the RASO02.rdml file from the RDML format to the csv format.

Selected amplification cure datasets were stored in the RDML format as described in (Rödiger et al. 2015, Rödiger et al. (2017)).

RDML data file	Device	Target gene	Detection chemistry
RAS002.rdml RAS003.rdml hookreg.rdml	CFX96 CFX96 Bio-Rad	HPV16, HPV18, HPRT1 HPV16, HPV18, HPRT1 various	Taqman Taqman, DNA binding dyes

32HCU: VideoScan (Attomol GmbH), CFX96: Bio-Rad.

Table_human_rated.xlsx

0.3.2 Graphical User Interfaces for Amplification Curve Classification

For machine learning and method validation it was important to classify the amplification curves individually. However, the availability of comprehensively annotated datasets of amplification curves was a bottleneck so far. In Rödiger, Burdukiewicz, and Schierack (2015) the humanrater() function was introduced. This function was developed to assist the human expert during the classification of amplification curves and melting curves. The human expert has to define classes (e. g., negative ("n"), ambiguous ("a"), positive ("p")) which get assigned to an amplification curve after expert has entered

Table 1: Classified amplification curve datasets.

Decision Datasets in PCRedux	qPCR Dataset	Package
decision_res_RAS002.csv	RAS002.rdml	PCRedux
$decision_res_RAS003.csv$	RAS003.rdml	PCRedux
$decision_res_batsch1.csv$	batsch1	qpcR
$decision_res_batsch2.csv$	batsch2	qpcR
$decision_res_batsch3.csv$	batsch3	qpcR
$decision_res_batsch4.csv$	batsch4	qpcR
$decision_res_batsch5.csv$	batsch5	qpcR
$decision_res_lc96_bACTXY.csv$	$lc96_bACTXY.rdml$	RDML
$decision_res_boggy.csv$	boggy	qpcR
$decision_res_C126EG595.csv$	C126EG595	${\tt chipPCR}$
$decision_res_C127EGHP.csv$	C127EGHP	${\tt chipPCR}$
${\rm decision_res_C316.amp.csv}$	C316.amp	${\tt chipPCR}$
${\rm decision_res_C317.amp.csv}$	C317.amp	${\tt chipPCR}$
$decision_res_C60.amp.csv$	C60.amp	${\tt chipPCR}$
$decision_res_CD74.csv$	CD74	${\tt chipPCR}$
$decision_res_competimer.csv$	competimer	qpcR
$decision_res_dil4reps94.csv$	dil4reps94	qpcR
$decision_res_guescini1.csv$	guescini1	qpcR
$decision_res_guescini2.csv$	guescini2	qpcR
$decision_res_htPCR.csv$	htPCR	qpcR
$decision_HCU32_aggR.csv$	$HCU32_aggR.csv$	PCRedux
$decision_res_karlen1.csv$	karlen1	qpcR
$decision_res_karlen2.csv$	karlen2	qpcR
$decision_res_karlen3.csv$	karlen3	qpcR
decision_res_lievens1.csv	lievens1	qpcR
$decision_res_lievens2.csv$	lievens2	qpcR
$decision_res_lievens3.csv$	lievens3	qpcR
$decision_res_reps.csv$	reps	qpcR
$decision_res_reps2.csv$	reps2	qpcR
$decision_res_reps3.csv$	reps3	qpcR
$decision_res_reps384.csv$	reps384	qpcR
${\rm decision_res_rutledge.csv}$	$\operatorname{rutledge}$	qpcR
$decision_res_stepone_std.csv$	$stepone_std$	RDML
$decision_res_testdat.csv$	testdat	qpcR
${\rm decision_res_vermeulen1.csv}$	vermeulen1	qpcR
$decision_res_vermeulen2.csv$	vermeulen2	qpcR
$_decision_res_VIMCFX96_60.csv$	VIMCFX96_60	${\tt chipPCR}$

the class in input mask. All amplification curve datasets listed in Table 1 were classified in interactive, semi-blinded sessions. humanrater() was set to randomly select individual amplification curves. All classifications were done in at least three repeats. The classification of the htPCR dataset (Figure 1B) was done in total eight times (see Figure 5) because most of the amplification curves are neither unequivocal classifiable as positive or negative.

```
# Suppress messages and load the packages for reading the data of the classified
# amplification curves.
options(warn = -1)
suppressMessages(library(data.table))
library(PCRedux)
# Load the decision_res_htPCR.csv dataset from a csv file.
filename <- system.file("decision_res_htPCR.csv", package = "PCRedux")</pre>
decision_htPCR <- fread(filename, data.table = FALSE)</pre>
par(mfrow = c(2, 4))
for (i in 2L:9) {
 data_tmp <- table(as.factor(decision_htPCR[, i]))</pre>
 barplot(data_tmp, col = adjustcolor("grey", alpha.f = 0.5),
      xlab = "Class", ylab = "Counts")
 text(c(0.7, 1.9, 3.1), rep(quantile(data_tmp, 0.25), 3), data_tmp, srt = 90)
 mtext(LETTERS[i-1], cex = 1.2, side = 3, adj = 0, font = 2)
}
```

The humanrater() function(Rödiger, Burdukiewicz, and Schierack 2015) was developed with the aim that amplification curves are taken individually (randomly) from the datasets and presented by a human expert for classification. On the basis of his or her knowledge, the human expert is then able to undertake a classification. This approach is well suited and has been applied to classify a variety of amplification curves during the development of the PCRedux package. This methodological approach can, however, be very time-consuming, depending on the size of the dataset. In addition, this approach can also be tiring for large datasets, especially when the amplification curves are very similar. A high similarity between amplification curves exists, for example, in replicates and negative controls.

In theory, the similarity between the amplification curves can be used to form groups with very similar curves. The amplification curves in the groups can then be classified together in one run. In this way, a higher throughput can be achieved for classification. This approach has not yet been described for the analysis of qPCR data in the literature.

The tReem() function was developed to perform a curve-shape based classification. Two algorithms have been integrated in the tReem() function to quantify the similarity between amplification curves. The interface of the tReem() function is similar to that of the humanrater() function. The function tReem() needs a data structure where the first column contains the qPCR cycles and all other columns contain the amplification curves. After a chain of processing steps, the tReem() function presents the human expert with a series of plots with a single amplification curve (no similarity to other curves) or groups of amplification curves (within a group there is a high similarity). The corresponding classes can then be assigned to the groups of amplification curves by the human expert using an input mask.

In the first method (standard), the correlation coefficients (r) are determined in pairs according to Pearson for all combinations of amplification curves. The correlation calculation is used to describe the strength of the correlation between the two variables in a statistical measure. Consequently, the correlation coefficient r can be regarded as a distance between the amplification curves. r is a dimensionless value and only takes values between -1 and 1. If r=-1, there is a maximum reciprocal relationship. If r=0 there is no correlation between the two variables. If r=1, there is a maximum rectified correlation.

In the second method, the Hausdorff distance is used to determine the similarity between amplification curves. The Hausdorff distance is the "the maximum of the distances from a point in any of the sets to the nearest point in the other set" (Rote 1991, Herrera et al. (2016)). The amplification curves are converted within the tReem() function using the qPCR2data() function.

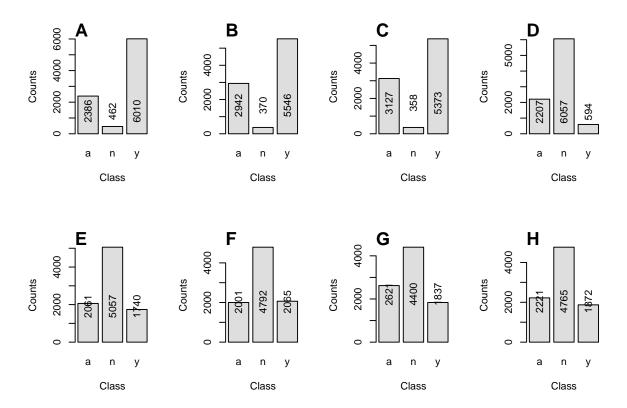


Figure 5: Classification of amplification curves. The availability of classified amplification curves is an important prerequisite for the development of methods based on monitored learning. Amplification curves (n = 8858) from the htPCR dataset (qpcR package, (Ritz and Spiess 2008)) were classified in total eight time at different time points by a human eight times with the classes ambiguous (a), positive (y) or negative (n). The classification is subject to the subjectivity of the human expert, classified with the humanrater() function. Consequently, the amplification curves were selected randomly so that systematic errors in classification should be minimized. With this example, it becomes evident that even with the same dataset, different class assignments can occur. While in the first three rounds (A-C) only a few amplification curves were classified as negative. Their proportion is increased nearly tenfold (D-H) in subsequent classifications.

Both methods process the distances in the same steps. This involves the calculation of the distance matrix using the Euclidean distances of all distance measures to determine the distance between the lines of the data matrix. This is used to perform a hierarchical cluster analysis. In the last step, the cluster is divided into groups based on a user-defined k value. For example, two groups are created for k=2. If the amplification curves are very different, a larger k should be used.

As a rule, the grouping of the amplification curves using the Pearson correlation coefficient as a distance measure is faster than the Hausdorff distance. Nevertheless, it is up to the user to find the optimal method for his task.

Ideally, only a few iterations are necessary to complete the classification of a dataset. However, a prerequisite for this is that the amplification curves are similar.

```
# Classify amplification curve data by correlation coefficients (r)
library(qpcR)
tReem(testdat[, 1:15], k = 3)
```

0.4 Functions of the PCRedux Package

The PCRedux package contains functions for analyzing amplification curves. In the following, these are distinguished into helper functions (subsubsection 0.4.1) and analysis functions (subsubsection 0.4.2).

The helper functions can be used to manually classify amplification curves, convert them into other data formats or to visualize data structures.

The analysis functions are used to calculate specific characteristic values (features) from the amplification curves. For example, these are slopes, turning points and change points.

0.4.1 Helper Functions of the PCRedux Package

0.4.1.1 decision_modus() - A Function to Get a Decision (Modus) from a Vector of Classes

Many approaches to machine learning exist. The subject is very rich. One method is supervised machine learning, where the goal is to derive a property from user-defined (classified) training data. Classified training data can be created by one or more individuals. Categories such as negative, ambiguous or positive are assigned depending on the form of the amplification curve, similar to what was described in subsubsection 0.1.3 and subsubsection 0.1.5 and on the opinion of the individual(s).

For example, the amplification curves in (Figure 6) were taken from the htPCR dataset (see Figure 1B). Assuming that the classification of the amplification curves is delegated to different users, it is likely that the amplification curve (P06.W47, Figure 6) are considered ambiguous or even positive (positive \leftrightarrow ambivalent) by the users. A classification experiment was carried out for the complete htPCR dataset. For this purpose, the amplification curves were classified at different time points as described in Rödiger, Burdukiewicz, and Schierack (2015).

Table 3 shows from a total of 8858 amplification curves the first 25 lines classified as negative (conformity=TRUE) and the first 25 lines classified as positive. In total, the curves were classified eight times (test.result.1 ... test.result.8), resulting in a whole of 70864 individually analyzed amplification curves for this dataset. All the raw data is included in the CSV file.

This example shows that the amplification curves have been classified differently in 94.5% of the cases (e. g., line 1 "P01. W01"). While for other amplification curves all classifications were the same (e. g., line 8856 "P95. W94").

For the systematic statistical analysis of classification datasets, the decision_modus() function has been developed. This allows the most common decision (mode) to be determined. This feature is useful if you want to consolidate large collections of different decisions into a single decision.

```
Observed: "a", "a", "a", "a", "a", "n", "n", "n" \rightarrow frequencies 5 x "a", 3 x "n" \rightarrow mode: "a"
```

Since the class names are known, they only have to be interpreted by the user (e. g., "a","n","y" -> "ambivalent", "negative", "positive").

The decision_modus() function was applied to the record decision_res_htPCR.csv with all classification rounds (columns 2 to 9) and the mode was determined for each amplitude curve.

```
# Use decision_modus() to go through each row of all classification done by
# a human.

dec <- lapply(1L:nrow(decision_res_htPCR), function(i) {
    decision_modus(decision_res_htPCR[i, 2:9])
}) %>% unlist()

names(dec) <- decision_res_htPCR[, 1]

# Show statistic of the decisions
summary(dec)</pre>
```

Table 3: Results of the 'htPCR' data set classification. All amplification curves of the 'htPCR' dataset were classified as 'negative', 'ambiguous' and 'positive' by individuals in eight analysis cycles ('test.result.1' . . . 'test.result.8'). If an amplification curve has always been classified with the same class, the last column ('conformity') shows 'TRUE'. As an example, the table shows 25 amplification curves with consistent classes and 25 amplification curves with differing classes ('conformity = FALSE').

htPCR	test.result.1	test.result.2	test.result.3	test.result.4	test.result.5	test.result.6	test.result.7	test.result.8	conformity
P01.W01	у	a	a	n	n	n	a	n	FALSE
P01.W02	a	y	a	n	n	n	n	n	FALSE
P01.W03	у	a	a	n	n	n	n	n	FALSE
P01.W04	У	a	a	n	n	n	n	n	FALSE
P01.W05	У	a	a	n	n	n	a	n	FALSE
P01.W06	a	a	a	n	n	n	n	n	FALSE
P01.W07	a	a	a	n	n	n	n	n	FALSE
P01.W08	у	a	a	n	n	n	n	n	FALSE
P01.W09	у	a	a	n	n	n	n	n	FALSE
P01.W10	n	a	a	n	n	n	n	n	FALSE
P01.W11	у	У	a	У	У	У	a	У	FALSE
P01.W12	a	a	a	n	n	n	n	n	FALSE
P01.W13	у	a	у	n	n	n	n	n	FALSE
P01.W14	y	a	y	n	n	n	n	n	FALSE
P01.W15	y	a	y	n	n	n	n	n	FALSE
P01.W16	y	a	a	n	n	n	n	n	FALSE
P01.W17	y	a	a	n	n	n	n	n	FALSE
P01.W17	a a	a	a	n	n	n	n	n	FALSE
P01.W19	v V	a		n		n	a	n	FALSE
P01.W19			a		n				FALSE
	У	a	a	У	a	a	У	a	FALSE
P01.W21	a	a	a	n	n	n	n	n	
P01.W22	У	a	a	n	n	n	n	n	FALSE
P01.W23	У	a	a	n	n	n	n	n	FALSE
P01.W24	У	a	a	n	n	n	a	n	FALSE
P01.W25	У	a	a	n	n	n	n	n	FALSE
P01.W58	n	n	n	n	n	n	n	n	TRUE
P02.W09	У	У	У	У	У	У	У	У	TRUE
P02.W19	У	У	У	y	У	y	У	У	TRUE
P02.W31	У	У	У	y	У	y	У	У	TRUE
P02.W41	У	У	y	y	y	y	y	y	TRUE
P02.W72	У	У	У	y	У	y	У	У	TRUE
P02.W81	У	У	У	У	У	У	y	У	TRUE
P02.W84	n	n	n	n	n	n	n	n	TRUE
P03.W09	У	У	У	У	У	У	У	У	TRUE
P03.W21	у	У	y	y	y	y	У	y	TRUE
P03.W22	у	У	y	y	y	y	У	y	TRUE
P03.W31	у	y	y	y	y	y	y	y	TRUE
P03.W32	У	y	У	y	y	y	У	y	TRUE
P03.W39	У	У	У	y	y	y	y	y	TRUE
P03.W56	У	y	У	y	y	y	У	y	TRUE
P03.W59	У	У	У	у	у	у	У	у	TRUE
P03.W68	У	У	У	у	У	у	У	у	TRUE
P03.W72	у	У	y	y	y	y	У	y	TRUE
P03.W73	y	y	y	y	y	y	y	y	TRUE
P04.W19	y	У	y	у	y	у	у	у	TRUE
P04.W31	y	У	y	у	y	у	у	у	TRUE
P04.W66	y Y	У	y	y	y	y	y	y	TRUE
P04.W81	y Y	У	y	y	y	y	y	y	TRUE
P04.W91									TRUE
1 U4. W 91	У	y	У	У	У	У	y	У	TRUE

```
## a n y
## 1847 4847 3343
```

Another usage mode decision_modus() function is to set the parameter max_freq=FALSE. That option specifies the number of all classifications.

```
library(PCRedux)
# Decisions for observation P01.W06
res_dec_P01.W06 <- decision_modus(decision_res_htPCR[
   which(decision_res_htPCR[["htPCR"]] == "P01.W06"),
   2L:9
], max_freq = FALSE)
print(res_dec_P01.W06)</pre>
```

```
## variable freq
## 1 a 3
## 2 n 5
```

This amplification curve P01. W06 was classified as a=3 times and as n=5 times. Therefore, the decision would turn into a negative decision.

0.4.1.2 visdat_pcrfit() - A Function to Visualize the Content of Data From an Analysis with the pcrfit_single() Function

In all data science projects it is important to look at a new dataset to gain an insight into what is contained therein and which potential problems might emerge during the further analysis. The pcrfit_single() function uses various algorithms to calculate values that are returned as factors (e. g., adapted model)

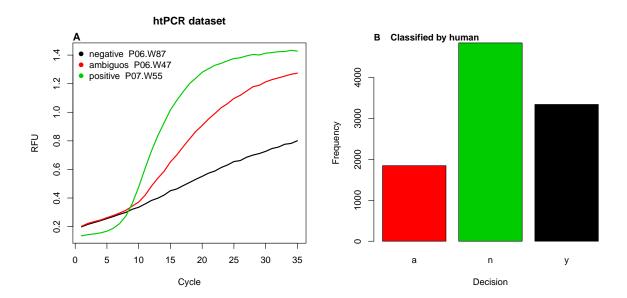


Figure 6: A) Comparison of amplification curves. Examples of a negative (black), ambiguous (red) and positive (green) amplification curve were selected from the htPCR dataset (qpcR package, Ritz and Spiess (2008)). The negative amplification curve is not sigmoid and shows a strong positive trend. The ambiguous amplification curve approaches a sigmoid from, but shows a positive slope in the background (cycle $1 \rightarrow 5$). The positive amplification curve is sigmoid. It begins in the background phase (cycle $1 \rightarrow 5$) with a flat baseline, and shortly thereafter the exponential phase follows (cycle $5 \rightarrow 25$) followed by a plateau phase (cycle $26 \rightarrow 35$). B) Summary of frequencies of all classes of the htPCR record. negative, black; ambiguous, red; positive, green.

or numbers (e. g., Cq value). Contrary to what the user expects, it is also possible that the algorithms cannot calculate certain values and that missing values (NA) are output instead. This may occur if the amplification curves have an unusual characteristic. In the analysis of large datasets, this can be a major problem that could be detected in advance.

The visdat_pcrfit() function makes use of the vis_dat function from the visdat package by N. Tierney (2017) to create heatmap-like visualizations. The Heatmapt displays each amplification curve line by line and reads from top to bottom. The characteristics are presented column by column. In principle, the structure of the output is the same as for the pcrfit_single() function.

The observations "A01", "A02", "A04" and "B04" from the C126EG685 of the chipPCR package were analyzed with the encu() function. Finally, the data can be visualized with the visdat_pcrfit() function. In this example the static plot is shown (Figure 7). It is also possible to run the function interactively by setting the parameter interactive=TRUE. In this case starts an interactive, browser-based charting library that uses ECMA Script. The interactive plot are rendered entirely locally, through a HTML widgets framework

```
# Calculate curve features of an amplification curve dataset.
# Use the C126EG685 dataset from the chipPCR package and analyze the observations
# A01, A02, A04 and B05.

library(chipPCR)

res <- encu(C126EG685[, c(1,2,3,5,17)])

## Loading required package: bcp

## Loading required package: grid
# Show all results in a plot. Not that the interactive parameter is set to
# FALSE.

visdat_pcrfit(res, type = "all", interactive = FALSE)</pre>
```

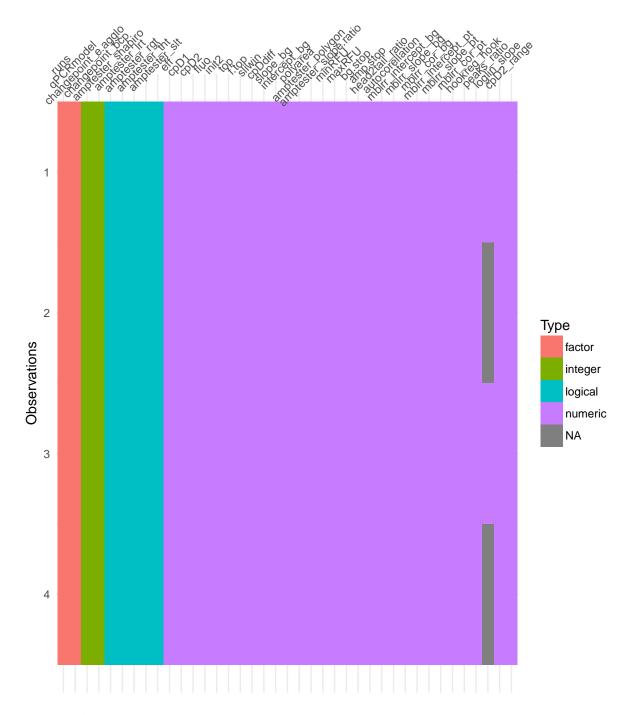


Figure 7: Application of visdat_pcrfit() for the visualization of the data structure after an analysis by pcrfit_single(). The amplification curves (A01 = 1, A02 = 2, A04 = 3, B04 = 4) from the C126EG685 dataset were analyzed with the pcrfit_single() function and then visualized with the visdat_pcrfit() function. For each observation, the classes (factor, integer, logical, numeric, NA) are presented. For the observations 2 and 4 the parameter loglin_slope could not be calculated (returned NA).

0.4.1.3 performer() - Performance Analysis for Binary Classification

Statistical modeling and machine learning can be powerful but expose a risk to the user by introducing an unexpected bias. This may lead to an overestimation of the performance. The assessment of the performance by the sensitivity and specificity is fundamental to characterize the performance of a classifier or screening test (G. James et al. 2013). Sensitivity is the percentage of true decisions that are identified and specificity is the percentage of negative decision that are correctly identified.

An example for the application of the performeR() function is shown in paragraph 0.4.2.4.

Abbreviations: TP, true positive; FP, false positive; TN, true negative; FN, false negative

Measure	Formula
Sensitivity - TPR, true positive rate	$TPR = \frac{TP}{TP+FN}$ $SPC = \frac{TN}{TN+FP}$ $PPV = \frac{TP}{TP+FP}$ $NPV = \frac{TN}{TN+FN}$
Specificity - SPC, true negative rate	$SPC = \frac{TN}{TN + FP}$
Precision - PPV, positive predictive value	$PPV = \frac{TTP}{TP+FP}$
Negative predictive value - NPV	$NPV = \frac{T'N}{TN + FN}$
Fall-out, FPR, false positive rate	$FPR = \frac{FP}{FP + TN} = 1 - SPC$
False negative rate - FNR	$FNR = \frac{FN}{TN + FN} = 1 - TPR$
False discovery rate - FDR	$FDR = \frac{TN + FP}{TP + FP} = 1 - PPV$
Accuracy - ACC	$ACC = \frac{(\hat{T}P + TN)}{(TP + FP + FN + TN)}$
F1 score - F1	$F1 = \frac{2TP}{(2TP+FP+FN)}$
Matthews correlation coefficient - MCC	$MCC = \frac{(TP*TN-FP*FN)}{\sqrt{(TP+FP)*(TP+FN)*(TN+FP)*(TN+FN)}}$
Likelihood ratio positive - LRp	$LRp = \frac{TPR}{1-SPC}$
Cohen"s kappa (binary classification)	$\kappa = \frac{p_0 - p_c}{1 - p_0}$

0.4.1.4 qPCR2fdata() - A Helper Function to Convert Amplification Curve Data to the fdata Format

qPCR2fdata() is a helper function to convert qPCR data to the functional fdata class as published by Febrero-Bande and Oviedo de la Fuente (2012). This function prepares the data for further analysis, which includes utilities for functional data analysis. For example, it this can be used to determine the similarity measures between amplification curves shapes by the Hausdorff distance. Similarity herein refers to the difference in spatial location of two *objects* (e. g., amplification curves). Objects with a close distance are presumably more similar. For single objects (e. g., points) one can use a vector distance, such as the Euclidean distance. The Hausdorff distance is an approximation of a shape metrics to define similarity measures between shapes. (Charpiat, Faugeras, and Keriven 2003). Several variants of the Hausdorff distance have been described (e. g., Minimal Hausdorff distance, Average Hausdorff distance, k-th ranked Hausdorff distance) (Herrera et al. 2016).

The qPCR2fdata() function takes a dataset containing the amplification cycles (first column) and the fluorescence amplitudes (subsequent columns) as input. Noise and missing values may affect the analysis adversely. Therefore, an instance of the CPP() function (chipPCR package (Rödiger, Burdukiewicz, and Schierack 2015)) was integrated in qPCR2fdata(). If preprocess=TRUE in qPCR2fdata(), then all curves are smoothed (Savitzky-Golay smoother), missing values are imputated and outliers in the ground phase get removed as described in Rödiger, Burdukiewicz, and Schierack (2015). The non-smoothed amplification curves (Figure 8A) have slightly more noise than the smoothed amplification curves (Figure 8C).

The following example illustrates the usage for the testdat dataset. Hierarchical cluster analysis is widely applied in data analysis. This method uses the elements of a proximity matrix to generate a dendrogram. The dendrogram can can be used to further analyze the clusters. Although there are methods to determine the number of clusters k in the present workflow the number of clusters was determined visually (Cook and Swayne 2007).

Since the distance based on the Hausdorff metric was already done the next steps involved the cutree() function from the stats package to split the dendrogram into smaller junks. A priori was defined that two classes (positive & negative) are expected. Therefore, the group parameter was set to k=2 in the cutree().

```
# Calculate the Hausdorff distance of the amplification curves
# cluster the curves.
# Load additional packages for data and pipes.
options(warn = -1)
library(qpcR)
library(chipPCR)
suppressMessages(library(fda.usc))
library(magrittr)
# Convert the qPCR dataset to the fdata format
# Use unprocessed data from the testdat dataset
res_fdata <- qPCR2fdata(testdat)
# Extract column names and create rainbow color to label the data
columnames <- testdat[-1] %>% colnames()
data_colors <- rainbow(length(columnames), alpha = 0.5)</pre>
# Calculate the Hausdorff distance (fda.usc) package and plot the distances
# as clustered data.
res_fdata_hclust <- metric.hausdorff(res_fdata)</pre>
res_hclust <- hclust(as.dist(res_fdata_hclust))</pre>
# Cluster of the unprocessed amplification curves
res_cutree <- cutree(res_hclust, k = 2)</pre>
res_cutree <- factor(res_cutree)</pre>
levels(res_cutree) <- list(y = "1", n = "2")</pre>
```

The results of the cluster analysis led two large clusters. A deeper inspection shows that the observations are correctly assigned to a cluster of positive or negative amplification curves. Moreover, the later increase of the fluorescence is reflected in the positive cluster (Figure 8).

```
# Plot the converted qPCR data
par(mfrow = c(1, 2))
res_fdata %>% plot(
    ., xlab = "Cycle", ylab = "RFU", main = "", type = "1",
   lty = 1, lwd = 2, col = data_colors
)
legend(
    "topleft", paste0(as.character(columnames), ": ", res_cutree),
       pch = 19, col = data_colors, bty = "n", ncol = 2, cex = 0.7
)
mtext("A", cex = 1.2, side = 3, adj = 0, font = 2)
plot(res hclust, main = "", xlab = "", sub="")
mtext("B", cex = 1.2, side = 3, adj = 0, font = 2)
rect(0.5, -3.5, 12.25, 0.5, border = "red")
text(7, 1, "negative", col = "red")
rect(12.5, -3.5, 24.5, 0.5, border = "green")
text(14, 1, "positive", col = "green", cex = 0.9)
```

Clusters of the amplification curves after an analysis using the Hausdorff distance. The amplification curves of the testdat dataset remained as raw data or were pre-processed (smoothed). Subsequent, the amplification curves were converted by the qPCR2fdata(). The converted data were subjected to a cluster analysis (Hausdorff distance). All observations were correctly assigned to cluster 1 (positive) or cluster 2 (negative).

This workflow can be used to cluster amplification curve data according to their shape into smaller groups of similar amplification curves. Classification tasks can be preformed in batches of amplification curves.

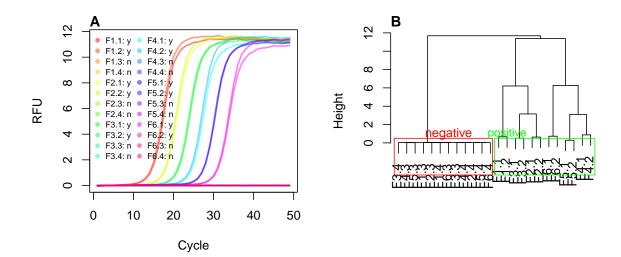


Figure 8: Shape based grouping of amplification curves. Grouping of amplification curves of the testdat dataset via Hausdorff distance. A) The amplification curves were converted with the qPCR2fdata() function. B) Subsequent they were processed by a cluster analysis using the Hausdorff distance. Faultless differentiation was achieved between negative amplification curves (n) and positive amplification curves (y).

It is worth to mention that the calculation of the distances is a computing expensive step dependent on the number of amplification curves. Other distance metric than the Hausdorff distance should also be considered. For example, Luo, Lin, and Chao (2010) showed how for image data how shape models using local curve segments with multiple types of distance metrics can improve the shape classification and detection results.

The following example illustrates the usage for the HCU32_aggR.csv dataset from the 32 channel VideoScan heating and cooling unit. In this experiment the bacterial gene aggR from $E.\ coli$ was amplified in 32 replicate qPCR reactions. Details of the experiment are described in the manual of the PCRedux package. The ambition was to test if the 32 amplification curves of the qPCR reaction are identical. As before, the data were processed with the qPCR2fdata() function and compared by the Hausdorff distance. Ideally, the amplification curves form only few clusters.

```
# Calculate slope and intercept on positive amplification curve data from the
# VideoScan 32 cavity real-time PCR device.
# Load additional packages for data and pipes.
options(warn = -1)
library(data.table)
library(fda.usc)
library(magrittr)

# Load the qPCR data from the HCU32_aggR.csv dataset
# Convert the qPCR dataset to the fdata format

filename <- system.file("HCU32_aggR.csv", package = "PCRedux")
data_32HCU <- fread(filename, data.table = FALSE)

res_fdata <- qPCR2fdata(data_32HCU)
# Extract column names and create rainbow color to label the data
columnames <- data_32HCU[-1] %>% colnames()
data_colors <- rainbow(length(columnames), alpha = 0.55)</pre>
```

In advance the the Cq values were calculated by the following code:

```
# Load the qpcR package to calculate the Cq values by the second derivative
# maximum method.
options(warn = -1)
library(qpcR)
res_Cq <- sapply(2L:ncol(data_32HCU), function(i) {</pre>
    efficiency(pcrfit(data_32HCU, cyc = 1, fluo = i, model = 16))
})
data.frame(
    obs = colnames(data_32HCU)[-1],
           Cq = unlist(res_Cq["cpD2", ]), eff = unlist(res_Cq["eff", ])
)
#
         Results
# obs
         Cq
                 eff
# 1
         A1 14.89 1.092963
# 2
         B1 15.68 1.110480
# 3
         C1 15.63 1.111474
# ...
# 30
         F4 15.71 1.109634
# 31
         G4 15.70 1.110373
# 32
         H4 15.73 1.117827
```

Next, the amplification curves (Figure 9A), the differences between baseline region and plateau region (Figure 9B), the correlation between the Cq value and amplification efficiency (Figure 9C) and the clusters based on the Hausdorff distance (Figure 9 were taken into account. In total, 32 real-time PCR reactions for the bacterial gen aggR were measured in the VideoScan system.

Note: The raw data has not been modified to retain all characteristics of the amplification curves.

Some amplification curves (Figure 9A) showed stronger fluctuations and therefore no ideal sigmoid curve progression. In addition, it can be seen that the amplification curves in the baseline area have a negative non-linear trend and a shift around the zero point. By contrast, the trend in the plateau region appears to be positive. This is similar to the curve shown in Figure 1. The comparison of the baseline region and the plateau region showed a difference between the 32 amplification curves. The observations E1, F1 and H1 had the lowest differences between the baseline and plateau regions. The comparison of Cq values and amplification efficiency showed that most amplification curves exhibit similar behavior. Since there are 32 replicates, the similarity of the Cq values and amplification efficiencies was to be expected. However, there are also amplification curves that show a greater deviation from the median of all Cq values (Figure 9C). The analysis by clustering of the Hausdorff distance did not yield any specific pattern (Figure 9D).

```
library(fda.usc)
library(magrittr)

# To save computing time, the Cq values and amplification efficiencies were
# calculated beforehand and transferred as a hard copy here.

calculated_Cqs <- c(
    14.89, 15.68, 15.63, 15.5, 15.54, 15.37, 15.78, 15.24, 15.94,
    15.88, 15.91, 15.77, 15.78, 15.74, 15.84, 15.78, 15.64, 15.61,
    15.66, 15.63, 15.77, 15.71, 15.7, 15.79, 15.8, 15.72, 15.7, 15.82,
    15.62, 15.71, 15.7, 15.73
)</pre>
```

```
1.09296326515231, 1.11047987547324, 1.11147389307153, 1.10308929700635,
    1.10012176315852, 1.09136717687619, 1.11871308210321, 1.08006168654712,
    1.09500422011318, 1.1078777171126, 1.11269436700649, 1.10628580163733,
    1.1082009954558, 1.11069683827291, 1.11074914659374, 1.10722949813473,
    1.10754282514113, 1.10098387264025, 1.1107026749644, 1.11599641663658,
    1.11388510347017, 1.11398547396991, 1.09410798249025, 1.12422338092929,
    1.11977386646464, 1.11212436173214, 1.12145338871426, 1.12180879952503,
    1.1080276005651, 1.10963449004393, 1.11037302758388, 1.11782689816295
)
# Plot the converted qPCR data
layout(matrix(c(1, 2, 3, 4, 4, 4), 2, 3, byrow = TRUE))
res_fdata %>% plot(
    ., xlab = "Cycle", ylab = "RFU", main = "HCU32_aggR", type = "l",
    lty = 1, lwd = 2, col = data_colors
)
legend(
    "topleft", as.character(columnames), pch = 19,
       col = data_colors, bty = "n", ncol = 4
mtext("A", cex = 1.2, side = 3, adj = 0, font = 2)
# Plot the background and plateau phase.
boxplot(
    data_32HCU[, -1] - apply(data_32HCU[, -1], 2, min),
        col = data_colors, las = 2, main = "Signal to noise ratio",
        xlab = "Sample", ylab = "RFU"
)
mtext("B", cex = 1.2, side = 3, adj = 0, font = 2)
# Plot the Cqs and the amplification efficiencies.
# Determine the median of the Cq values and label all Cqs, which a less 0.1 Cqs
# of the median or more then 0.1 Cqs of the median Cq.
plot(
    calculated_Cqs, calculated_effs, xlab = "Cq (SDM)",
     ylab = "eff", main = "Cq vs. Amplification Efficiency",
     type = "p", pch = 19, lty = 1, lwd = 2, col = data_colors
)
median_Cq <- median(calculated_Cqs)</pre>
abline(v = median_Cq)
text(median_Cq + 0.01, 1.085, expression(paste(tilde(x))))
    which(calculated_Cqs < median_Cq - 0.1),</pre>
             which(calculated_Cqs > median_Cq + 0.1)
)
text(
    calculated_Cqs[labeled], calculated_effs[labeled],
     as.character(columnames)[labeled]
)
mtext("C", cex = 1.2, side = 3, adj = 0, font = 2)
# Calculate the Hausdorff distance using the fda.usc package and cluster the
# the distances.
```

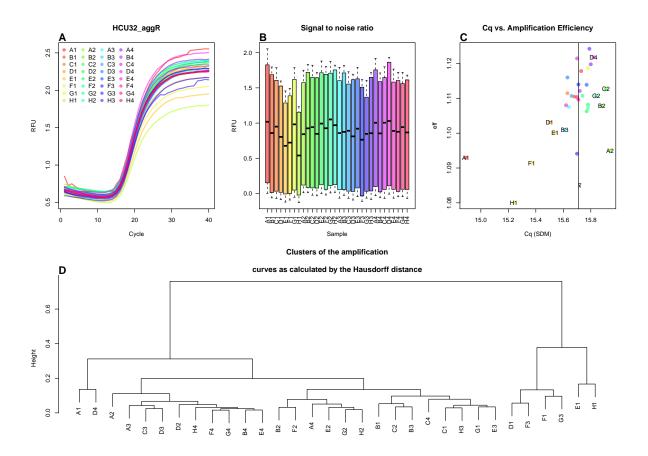


Figure 9: Clustering of amplification curves. The amplification curves from the 32HCU were processed with the qPCR2fdata() function and subsequent processed by a cluster analysis and Hausdorff distance analysis. A) Amplification curves were plotted from the raw data. B) Overall, the signal to noise ratios of the amplification curves were comparable between all cavities. C) The Cqs (Second Derivative Maximum) and the amplification efficiency (eff) were calculated with the efficiency(pcrfit()) functions from the qpcR package. The median Cq is indicated as vertical line. Cqs larger or less than 0.1 of the Cq \tilde{x} are indicated with the labels of the corresponding observation. D) The clusters according to the Hausdorff distance show no specific pattern regarding the amplification curve signals. It appears that the observations D1, E1, F1, F3, G3 and H1 deviate most from the other amplification curves.

```
res_fdata_hclust <- metric.hausdorff(res_fdata)
cluster <- hclust(as.dist(res_fdata_hclust))

# plot the distances as clustered data and label the leafs with the Cq values
# and colored dots.

plot(cluster, main = "Clusters of the amplification\n
curves as calculated by the Hausdorff distance", xlab = "", sub="")
mtext("D", cex = 1.2, side = 3, adj = 0, font = 2)</pre>
```

The analysis gives an overview of the variation of the amplification curve data.

0.4.2 Amplification Curve Analysis Functions of the PCRedux package

There are a number of ROIs (see Figure 2) in an amplification curve that are potentially useful for calculating characteristics for the classification of amplification curves. Amplification curves can have unique shapes and deviate from the ideal sigmoid models (compare Figure 1A and Figure 1B) of qPCRs. For instance, some amplification curves are only flat or have a rise with positive or negative signs without sigmoid curvature. In the case of sigmoid amplification curves, there are turning points which can be characteristic for positive amplification curves. Such differences are interesting candidates to calculate features for machine learning.

On the basis of this observation, various concepts were developed and implemented in algorithms to describe amplification curves. The intent of Gunay, Goceri, and Balasubramaniyan (2016) was to improve the determination of the Cq values. They postulated that they can achieve an improved prediction of Cq values using a modified sigmoid function (three parameters). An assumption of their approach is, that this model can be applied to any dataset. There are several reasons why such an assumption is not valid. In the chapters paragraph 0.4.2.7, for example, the functions hookreg() and hookregNL() are briefly displayed. These amplification curves deviate significantly from a three-parameter model. Figure 11 shows the distribution of models fitted to amplification curves. In most case models with six and seven parameters were automatically selected. In addition, non-linear functions also tend to fit models to noise (Figure 10). It becomes clear in Figure 12 that for a considerable proportion of manually negatively classified amplification curves a Cq value could be calculated. A computer-assisted decision would be helpful.

```
# Load the gpcR package for the model fit.
suppressMessages(library(qpcR))
library(chipPCR)
# Select one positive and one negative amplification curve from the PCRedux
# package.
amp_data <- RASO02[, c("cyc", "A01_gDNA.._unkn_B.Globin", "B07_gDNA.._unkn_HPRT1")]
# Arrange graphs in an matrix and set the plot parameters. An plot the positive
# and negative amplification curve.
layout(matrix(c(1, 1, 2, 3), 2, 2, byrow = TRUE), respect = TRUE)
matplot(amp_data[,1], amp_data[, -1], pch = 19, lty = 1, type = "l",
        xlab = "Cycle", ylab = "RFU", main = "")
mtext("A", cex = 1.2, side = 3, adj = 0, font = 2)
# Apply the the amptester function from the chipPCR package to the amplification
# curve data and write the results to the main of the plots.
for (i in 2:3) {
   res.ampt <- suppressMessages(amptester(amp_data[, i]))</pre>
    # Make a logical connection by two tests (shap.noisy, lrt.test and
    # tht.dec) of amptester to decide if an amplification reaction is
    # positive or negative.
   decision <- ifelse(!res.ampt@decisions[1] &&</pre>
   res.ampt@decisions[2] &&
   res.ampt@decisions[4],
    "positive", "negative"
    # The amplification curves were fitted (17 model) with pcrfit() function. The
    # Cq was determined with the efficiency() function.
   fit <- pcrfit(data = amp_data, cyc = 1, fluo = i, model = 17)</pre>
```

Therefore, several characteristics of an amplification curve should be recorded first and then checked for their usefulness. There, it becomes clear that a three-parameter model adaptation can be adapted to noise and thus provides unreliable predictions.

As shown in Figure 4 have positive amplification curves a typical sigmoid shape, while negative curves resemble random noise.

Many properties (e. g., experiment condition (hydrolysis probe, DNA binding dye)) can be converted to binary classifiers (no == 0, yes == 1). From the amplification curve one can calculate the signal range before and after the amplification process.

Next follows a brief introduction of the feature engineering process of this work. For doing this a set features which characterize amplification curves was needed. In total seven function were generated and integrated in PCRedux package. These functions features have not been described before in the literature for the classification of amplification curves.

The function described following are aimed for experimental studies. It is important to note that the features proposed herein emerged during a critical reasoning process. The aim of the package is to propose a set of features, functions and data for an independent research.

0.4.2.1 pcrfit_single() - A Function to Calculate Features from an Amplification Curve

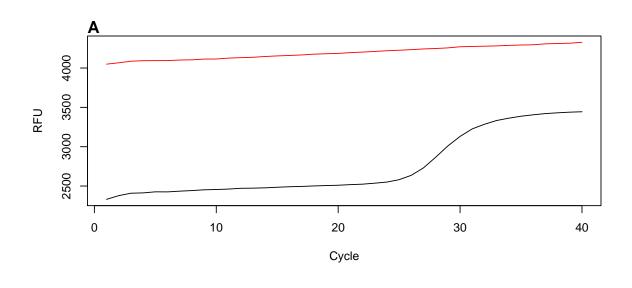
The following chapter includes on **exemplary applications** of feature vectors from amplification curves, which can be used for automatic classification by machine learning. The focus is mainly on, the concise description of the algorithms of the pcrfit_single() function. The underlying hypotheses are formulated and supported by exemplary analysis.

Some algorithms have been implemented as standalone functions (e. g., earlyreg()) to make them available for other applications. The goal is not to examine the limits of their applicability, but rather to prove their basic functionality. Based on considerations and experience the algorithms of the pcrfit_single() function are restricted to ROIs (Figure 2) in order to calculate specific features. In order to bring a systematic into the algorithms, the functions with similar approaches are summarized in groups. Due to the number of algorithms, it is not possible to provide a detailed description with examples in every place.

The following output shows all features and their data type (num, numeric; int, integer; Factor, factor; logi, boolean) which are determined from the second amplification curve of the RASO02 dataset with the pcrfit_single() function.

```
library(PCRedux)
str(pcrfit_single(RAS002[, 2]))
```

```
## 'data.frame': 1 obs. of 48 variables:
## $ cpD1 : num 28.1
## $ cpD2 : num 25.9
## $ eff : num 1.02
```



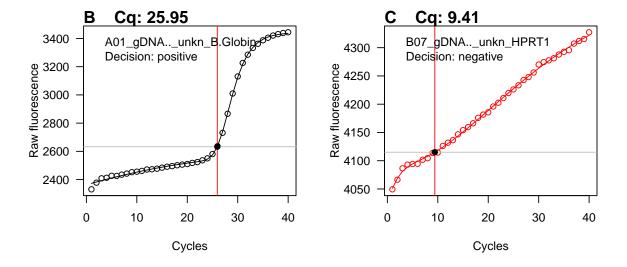


Figure 10: Positive and negative Amplification curves from the RASO02 dataset. A positive amplification curve (black) and a negative amplification curve (red) were selected from the RASO02 dataset. The positive amplification curve has a baseline signal of approximately 2500 RFU and shows an unambiguous sigmoidal shape. The negative amplification curve has a baseline signal of approximately 4200 RFU, shows moderately positive slope and has no sigmoidal shape. B) A logistical function with seven parameters (17) was adapted to the positive amplification curve. A Cq value of 25.95 was determined using the method of the maximum of the second derivative. The calculated Cq value appears to be correct. C) The negative amplification curve was also fitted with a seven parameter logistical function (17). The second derivation method was used to determine the Cq value. Though a Cq value of 9.41 was calculated, it is clear that the model adaptation is not appropriate to calculate a trustworthy Cq value. If such a calculation would be done automatically, without human interaction, a false-positive result could be interpreted.

```
##
   $ sliwin
                          : num 1.04
   $ cpDdiff
##
                         : num 2.19
   $ loglin_slope
                         : num 0.0343
   $ cpD2_range
                         : num 4.48
##
   $ top
                         : num 25
##
   $ f.top
                          : num 0.748
##
   $ tdp
                          : num 35
##
   $ f.tdp
                          : num 1.65
##
   $ bg.stop
                          : num 15
                         : num 40
##
   $ amp.stop
##
   $ b_slope
                         : num -13.6
   $ f_intercept
##
                         : num 3.17
##
   $ convInfo_iteratons : int 14
##
   $ qPCRmodel
                          : Factor w/ 1 level "17": 1
   $ qPCRmodelRF
                          : Factor w/ 1 level "17": 1
##
   $ minRFU
                          : num 0.682
##
   $ maxRFU
                          : num 1
##
  $ init2
                         : num 0.419
##
  $ fluo
                         : num 0.765
   $ slope_bg
                         : num 0.00658
##
   $ intercept_bg
                        : num 0.675
                         : num 0.0939
##
   $ sd_bg
   $ head2tail_ratio : num 0.704
$ mblrr_slope_pt : num 0.005
##
##
                         : num 0.00586
##
   $ mblrr_intercept_bg : num 0.693
##
   $ mblrr_slope_bg : num 0.00202
##
   $ mblrr cor bg
                         : num 0.91
##
   $ mblrr_intercept_pt : num 0.774
##
   $ mblrr_cor_pt : num 0.942
##
   $ polyarea
                          : num 0.0409
                          : num 0.0117
##
   $ peaks_ratio
                         : num 0.765
   $ autocorellation
   $ changepoint_e.agglo : int 2
##
##
   $ changepoint_bcp : int 10
   $ amptester_shapiro : logi FALSE
   $ amptester_lrt : logi TRUE
$ amptester_rgt : logi TRUE
##
##
   $ amptester_tht
$ amptester slt
                         : logi TRUE
##
                         : logi TRUE
##
   $ amptester slt
   $ amptester_polygon : num 1.55
##
##
   $ amptester_slope.ratio: num 0
##
   $ hookreg_hook
                     : num 0
   $ hookreg hook slope : num 0
   $ hookreg_hook_delta : num 0
   $ number_of_cycles
                          : int 40
```

To underscore the usability of the algorithms and their features, 3302 observations (471 negative amplification curves, 2831 positive amplification curves) from the batsch1, boggy, C126EG595, competimer, dil4reps94, guescini1, karlen1, lievens1, reps384, rutledge, testdat, vermeulen1, VIMCFX96_60, stepone_std, RAS002, RAS003, HCU32_aggR and lc96_bACTXY were analyzed with the encu() function and the results (features) were combined in the file data_sample.rda. The algorithms are divided into the following broad categories:

- algorithms that determine increases, signal levels,
- algorithms that determine turning points and
- algorithms that determine areas.

Users of this function should independently verify and validate the results of the methods for their applications. The encu() function is based on the pcrfit_single() function. Contrary to the pcrfit_single() function, the encu() function can be used to process large records of amplification curve data arranged in columns. The progress of processing is displayed in the form of a progress bar and the estimated run-time. The encu() function is not discussed in more detail. Additionally, the encu() allows to specify which monitoring chemistry (e. g., DNA binding dye, sequence specific probes) and which thermo-cycler was used. Such information may well be relevant for data analysis (subsubsection 0.1.3). Jan M. Ruijter et al. (2014) have shown, among other things, that monitoring chemistry of the type of input DNA (single stranded, double stranded) can be important when analysing qPCR data.

Amplification Curve Pre-processing

The pcrfit_single() function and the encu() function perform two pre-processing steps before each calculation. That includes checking whether an amplification curve contains missing values. Missing values (NA) are measuring points in a dataset where no measured values are available or if they have been removed arbitrarily. Causes of this can be found, for example, in case that no measurement has been carried out (e. g., defective detector) or lengths of the vectors differ (number of cyles) between the observation. Missing values are automatically imputed by spline interpolation as described in Rödiger, Burdukiewicz, and Schierack (2015). The pcrfit_single() function and the encu() function will only terminate with an error message in extreme cases. In the next step, all values of an amplification curve are normalized to the 99% quantile. The normalization is necessary, because the amplitudes of amplification curves depend on the used detection chemistry and thermo-cycler (sensor technology, software processing). As a result considerable differences between the maximum values of raw data are the norm. Users of the PCRedux package are advised to take a look at the datasets of amplification curves before starting complex analyses. In order to compare amplification curves from different thermo-cyclers, the values should always be scaled systematically using the same method. Although there are other normalization methods (e. g., minimum-maximum normalization, see Rödiger, Burdukiewicz, and Schierack (2015)), the normalization by means of the 99% quantile should ensure that the information about the height of the background signal is not lost. That would be the case with a Min-Max-standardization. A normalization to the maximum is not recommended, because outliers could have an unintentional influence on the normalization. Consequently, the 99% quantile is a pragmatic compromise to take the aforementioned aspects into account in the processing chain. For example, the data in Figure 17D show that the maxRFU values after normalization are approximately 1. There is no statistical significant difference between maxRFU values of positive and negative amplification curves. Inspired by maxRFU value, the minimum of the amplification curve is determined by the 1% quantile to minimize the influence of outliers. It is referred to as minRFU (Figure 17C). Selected algorithms of the pcrfit_single() function use the CPP() function from the chipPCR package to pre-process (e. g., baselining, smoothing, imputation of missing values) the amplification curves. Further details are given in Rödiger, Burdukiewicz, and Schierack (2015).

Handling of Missing Features

Missing values (NA) of features can occur in case that a calculation of a specified value is not possible. It can occur, for example, if a logistical function is to be adapted to a measurement series, but the raw data is too noisy to allow model adaptation. As a consequence, no parameters would be determined from this model. The apparent lack of information is nevertheless still useful in the context of data analysis. For the case described above, it could be deduced from the missing values that the data series does not show a sigmoid curve progression. In this regard, NAs nonetheless provide an informational basis.

However, NAs pose a difficulty in many analyses. Before an analysis is carried out, it must be clarified how to deal with the missing values. Under the term "imputation" there are a number of procedures based on statistical methods (e. g., neighboring median, spline interpolation) or on user-defined rules. Such a rule could, for example, consist of setting one of the slope parameters of a model to zero when it cannot be determined (Williams 2009, Cook and Swayne (2007), Hothorn and Everitt (2014)). The application of fixed rules brings the advantage that the user is relieved of the decision as to how to deal with missing values. The disadvantage is that certain rules do not necessarily have to reflect a natural process.

The NAs were left unchanged in the PCRedux package up to version 0.2.5-1. Since version 0.2.6, however, the NAs have been replaced by numerical values (e. g., total number of cycles) or factors (e. g., lNA for non-fitted model).

0.4.2.2 Model Selection

In subsubsection 0.1.3, it was postulated that a sigmoid curve can be fitted using logistic functions. There are four³ functions used in the PCRedux package, that were previously descried by Spiess, Feig, and Ritz (2008) and Ritz and Spiess (2008). This model is used as the starting point for to fit a model with four (l4, Equation 1), five (l5, Equation 2) or six parameters (l6, Equation 3). The optimal model is selected on the basis of the Akaike information criterion. This model is used for all further calculations. The pcrfit_single() function returns qPCRmodel as a factor (l4, l5, l6, l7). The model found can also be interpreted as the quality of an amplification curve, since a model with many parameters differs more from an ideal sigmoid model. For instance, a four-parameter model, unlike the seven-parameter model, does not have a square component. The four-parameter model would be suitable for amplification curves with a very slight increase in the ground phase and plateau phase. This would correspond to a simple sigmoid amplification curve. In case no model could be fitted, an lNA is returned.

l4:

$$f(x) = c + \frac{d - c}{1 + exp(b(log(x) - log(e)))}$$

$$\tag{1}$$

• 15:

$$f(x) = c + \frac{d - c}{(1 + exp(b(log(x) - log(e))))^f}$$

$$\tag{2}$$

• **16**:

$$f(x) = c + k \cdot x + \frac{d - c}{(1 + exp(b(log(x) - log(e))))^f}$$

$$\tag{3}$$

• 17:

$$f(x) = c + k1 \cdot x + k2 \cdot x^2 + \frac{d - c}{(1 + exp(b(log(x) - log(e))))^f}$$
(4)

The pcrfit_single() function starts by adjusting a seven-parameter model. As a matter of fact, models with many parameters adapt adapt easier to an dataset. From that model, the pcrfit_single() function outputs the variables b_slope and f_intercept, which describe the increase and the intercept. The number of iterations required to adapt the model is also stored. That value is returned by the pcrfit_single() function as convInfo_iteratons. The higher the convInfo_iteratons value, the more iterations were necessary to converge from the start parameters (Figure 14D). Hence, a low convInfo_iteratons value implies a sigmoid curve and a high number of iterations implies a noisy or non-sigmoid curve.

0.4.2.3 Quantification Points, Ratios and Slopes

In the literature, statistical methods are described which can be used to describe quantitatively the product formation in a qPCR (Rödiger, Burdukiewicz, and Schierack 2015, Jan M. Ruijter et al. (2013)). As illustrated in Figure 3 are these the Ct value, the first derivative maximum (cpD1) and the second derivative maximum (cpD2). The pcrfit_single() function calculates the cpD1 and cpD2 (Figure 12). Both quantification points are not directly useful to distinguish between a positive and negative amplification curve. However, low cpD1 and cpD2 values (< 5 cycles) indicate that the PCR reaction was negative or that the amount of input DNA was to high. The Ct value is not calculate for the reasons discussed in subsubsection 0.1.4. No further information shall be provided about these typical procedures.

Further features from the pcrfit_single() function are:

 $^{^3}$ Up to PCRedux package version 0.2.5-1 more models were calculated. But to increase the speed they were excluded in newer package versions.

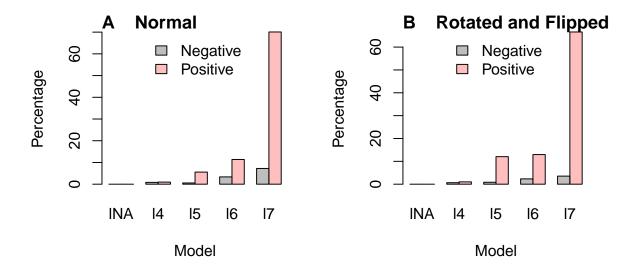


Figure 11: Distribution of models of amplification curves. The competimer, dil4reps94, guescini1, HCU32_aggR, karlen1, lc96_bACTXY, lievens1, RAS002, RAS003, reps384, rutledge, stepone_std, testdat, vermeulen1, VIMCFX96_60 datasets were analyzed with the encu() function. For each amplification curve, the optimal model was selected on the basis of the Akaike information criterion. A) Model functions of the raw amplification curve. B) Model functions of the rotated and flipped amplification curves. lNA, no model fitted. l4...l7, model with four to seven parameters.

- eff is the optimized PCR efficiency found within a sliding window (Figure 3C). A linear model of cycles versus log(Fluorescence) is fit within a sliding window (for details see sliwin() function from the qpcR package). The comparison of positive and negative amplification curves in Figure 14A demonstrates that the classes are significantly different from each other.
- sliwin is the PCR efficiency by the 'window-of-linearity' method (Spiess, Feig, and Ritz 2008).
- cpDdiff is the the difference between the Cq values calculated from the first and the second derivative maximum (cpDdiff = |cpD1 cpD2|) from the fitted model (Figure 3C). Provided that a model can be exactly fitted, the estimates of the difference are reliable. Higher cpDdiff values indicate a negative amplification reaction or a very low amplification efficiency. The comparison of positive and negative amplification curves in Figure 14C demonstrates that the classes are significantly different from each other. In the event that the cpDdiff value cannot be determined (NA), it is replaced by zero.
- cpD2_range is the absolute value of the difference between the minimum and the maximum of the second derivative maximum (cpD2_range = |mincpD2 maxcpD2|) from the diffQ2() function (no model fitted) (Figure 13). The cpD2_range value does not require an adjustment of a multiparametric model. The approximate first and second derivatives are determined using a five-point stencil (Rödiger, Burdukiewicz, and Schierack 2015). The comparison of positive and negative amplification curves in Figure 14E shows that the classes differ significantly from each other. In the event that the cpD2_range value cannot be determined (NA), it is replaced by zero.
- bg.stop (Figure 13) is the end of the ground phase estimated by the bg.max() function (Rödiger, Burdukiewicz, and Schierack 2015).
- amp.stop (Figure 13) is the end of the exponential phase estimated by the bg.max() function (Rödiger, Burdukiewicz, and Schierack 2015).

Another method is the takeoff point (top) according to Tichopad et al. (2003). The top is calculated using externally studentized residuals, which tested to be an outlier in terms of the t-distribution. The top signifies to first PCR cycle entering the exponential phase. The takedown point (tdp) is an implementation in the pcrfit_single() function, which uses the rotated $f(x) \mapsto f_1(f(x))$ and flipped g(x) = -(x) amplification curve for calculation Figure 2A describes the location of top and tdp exemplarily. The position (f.top, f.tdp) on the ordinate is also determined from these points. If an amplification curve

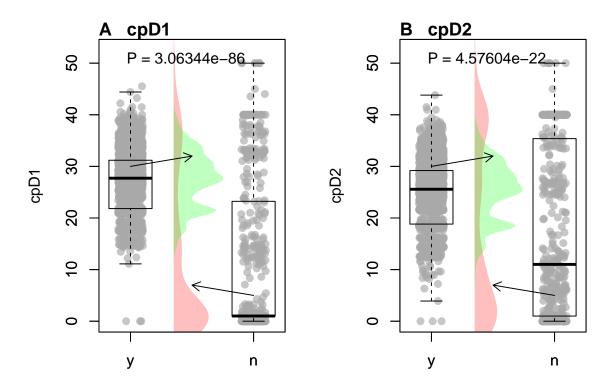


Figure 12: Distribution of Cq values of positive and negative amplification curves. All Cq values were calculated from 3302 amplification curves after fitting the optimal multi-parametric models. The Cqs of positive amplification curves heaped up in the range between 10 and 35 PCR cycles. This differs from the distribution of negative amplification curves. The Cqs of negative amplification curves were calculate over the entire range. Note: The Cqs of the negative amplification curves are false positive. A) The maximum of the first derivative cpD1. B) The maximum of the second derivative (cpD2).

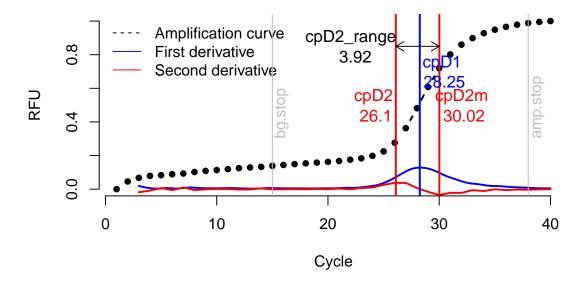


Figure 13: Both the minimum (cpD2m) and the maximum (cpD2) of the second derivative were determined numerically using the diffQ2() function. In addition, the function returns the maximum of the first derivative (cpD1). The difference of cpD2 and cpD2m results in the cpD2_range. Large cpD2_range values indicate a low amplification efficiency or negative amplification reaction. bg.start provides an estimate for the end of the ground phase. The following formula is used for the calculation: bg.start = cpD1 - f*(cpD2m - cpD2). The distance between cpD1 and cpD2 is multiplied by a factor. bg.stop provides an estimate for the end of the exponential phase. The following formula is used for the calculation: bg.start = cpD1 + f*(cpD2m - cpD2). f is a factor (default 0.6) (see manual of bg.max() for details).

is negative or neither top nor tdp can be calculated, then top & tdp will be assigned the number of cycles and f.top & f.tdp the value 1. The distribution of top, tdp, f.top and f.tdp is shown in Figure 14I-L. This figure shows that a top value and a tdp value enable a qualitative classification of the amplification reaction. An interesting aspect is that the positive f.top values are markedly lower than the negative f.top values (Figure 14J). The same applies inversely to the tdp values (Figure 14L). In this way, amplification curves can be classified according to these values.

In Figure 2 it was postulated that an amplification curve can be divided into different regions. One assumption is that the slope and intercept of positive amplification curves are markedly different in head (ground phase) and tail (plateau phase). The intercept in the head should be lower than in the tail. In a negative amplification curve, the intercept should be nearly identical. The slope in the tail should also provide some indication to determine whether the amplification reaction is completed. In order to quantify these values, a linear regression model can be used in these ROIs.

An example is given for the internal parameter <code>loglin_slope</code> which is calculated from the slope determined by a linear model of the data points from the fluorescence at the minimum and maximum of the second derivative (Figure 15). The coordinates of the minimum and the maximum were determined as described in Rödiger, Böhm, and Schimke (2013). This feature uses the exponential phase as ROI. Provided that the locations of the minimum of the second derivative and the maximum of the second derivative yield a suitable interval. As a precaution, the algorithm checks, for example, whether the distance between the minimum of the second derivative and the maximum of the second derivative is not more than nine PCR cycles. Failing this, the <code>loglin_slope</code> value is set to zero (no slope). In the following example, the data Figure 15.

All manufacturers of thermo-cyclers use different sensors and data processing algorithms in their systems. Hence it can be assumed that the signal variation in the ground phase (Figure 1F) differs between the different systems. Moreover, users make use of different detection chemistries (e. g., hydrolysis probes, reporter dyes). However, the latter will not be discussed here. For the distinction between negative and positive amplification curves, it should be checked whether a difference can be determined on the basis of the standard deviation of the background fluorescence.

After analyzing all amplification curves with the pcrfit_single() function, the sd_bg feature was analyzed. The feature sd_bg is the standard deviation from the first PCR cycle to the takeoff point (Figure 2A). If no takeoff point can be determined from an amplification curve, the value for sd_bg is calculated from the first to the eighth PCR cycle. The feature sd_bg in Figure 16 is broken down by the thermo-cycler and the output of the amplification reaction (negative, positive). It can be seen that the signal variation between the thermo-cyclers seems to be different. There is also a difference between negative and positive amplification curves. This is also in accordance with the observations from Figure 4.

The aim was to predict, based on the polyarea feature, whether an amplification curve is positive or negative. The computation of polyarea is based on the Gauss polygon area formula. The feature polyarea has been selected to show that the area under an amplification curve can be used to distinguish positive and negative amplification curves. The hypothesis is that positive amplification curves have a larger area than negative amplification curves. As shown in Figure 28C, there is a statistically significant difference between positive and negative amplification curves. Also shown are the values of another method to calculate the area under an amplification curve. This method is called amptester_polygon. amptester_polygon⁴ is part of the amptester() function from the chipPCR package (Rödiger, Burdukiewicz, and Schierack 2015). In contrast to the implementation in the amptester() is the amptester_polygon value normalized to the total number of cycles. It is expected that this method allows comparable predictions (Figure 28Ds). However, this question is not to be dealt with in the following example.

The batsch1, HCU32_aggR, stepone_std, RAS002, RAS003, lc96_bACTXY datasets were used for the calculation of the polyarea values for all amplification curves. A binomial logistic regression (aka logit regression or logit model) was used to analyze the relationship between the polyarea value and the decision (negative, positive). This dataset contains almost equal proportions of positive and negative amplification curves (Figure 18A). Prior to this, the amplification curves were analyzed with the encu() function (paragraph 0.4.2.1) and stored in the data_sample.rda file to save computing time. The file is

⁴This feature is determines from the points in an amplification curve (like a polygon, in particular non-convex polygons) are in a 'clockwise' order. The sum over the edges result in a positive value if the amplification curve is 'clockwise' and is negative if the curve is 'counter-clockwise'.

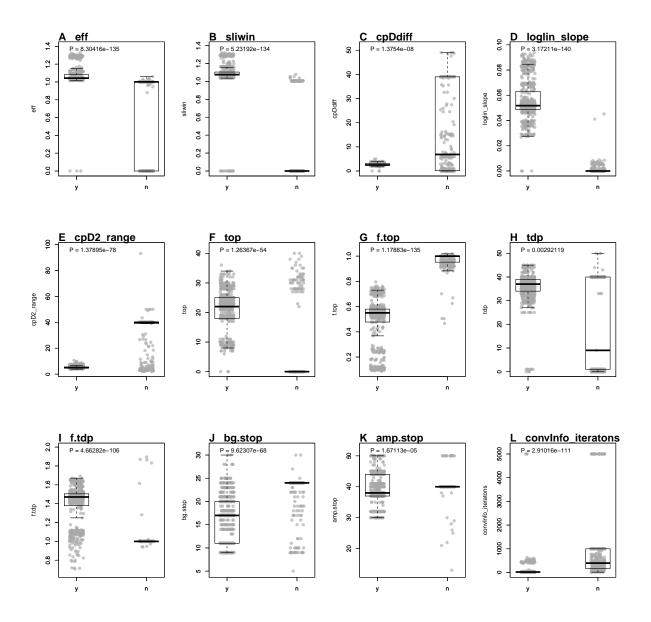


Figure 14: Analysis of location features. Amplification curves from the datasets stepone_std, RAS002, RAS003, 1c96_bACTXY, C126EG595 and dil4reps94 were analyzed with the encu() function. These datasets contain positive and negative amplification curves. Furthermore, the meta dataset contains amplification curves that exhibit a hook effect or non-sigmoid shapes, for instance. All amplification curves are manually classified. Altogether 626 positive and 317 negative amplification curves were included in the analysis. A) eff, optimized PCR efficiency found within a sliding window. B) sliwin, PCR efficiency by the 'window-of-linearity' method. C) cpDdiff, difference between the Cq values calculated from the first and the second derivative maximum. D) loglin_slope, slope from the cycle at the second derivative maximum to the second derivative minimum. E) cpD2_range, absolute value of the difference between the minimum and the maximum of the second derivative maximum. F) top, takeoff point. G) f.top, fluorescence intensity at takeoff point. H) tdp, takedown point. I) f.tdp, fluorescence intensity at takedown point. J) bg.stop, estimated end of the ground phase. K) amp.stop, estimated end of the exponential phase. L) convInfo_iteratons, number of iterations until convergence.

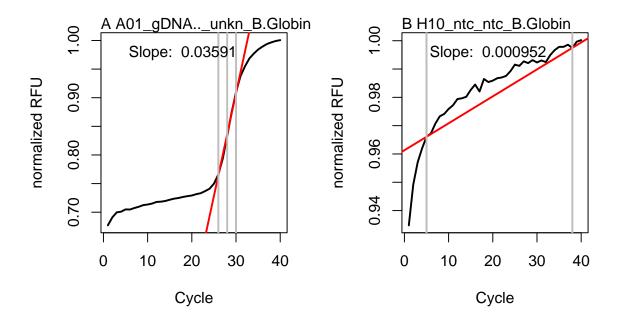


Figure 15: Concept of the <code>loglin_slope</code> feature. The algorithm determines the fluorescence values of the raw data at the approximate positions of the maximum of the first derivative, the minimum of the second derivative and the maximum of the second derivative, which are in the exponential phase of the amplification curve. A linear model is created from these parameter sets and the slope is determined. A) Positive amplification curves have a clearly positive slope. B) Negative amplification curves usually have a low, sometimes negative slope. The data were taken from the RASO02 dataset.

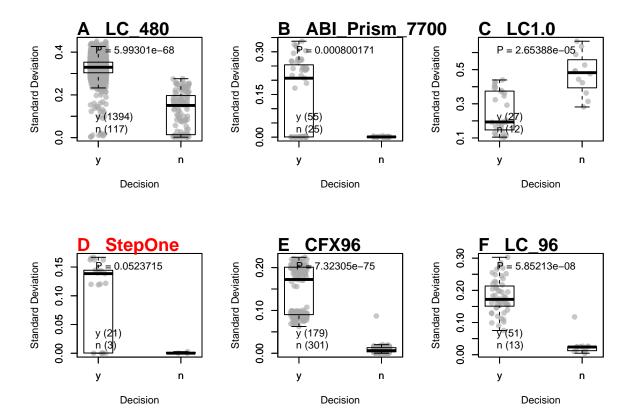


Figure 16: Standard deviation in the ground phase of various qPCR devices. The sd_bg feature was used to determine if the standard deviation between the thermo-cyclers and between positive and negative amplification curves was different. The standard deviation was determined from the fluorescence values from the first cycle to the takeoff point. If the takeoff point could not be determined, the standard deviation from the first cycle to the eighth cycle was calculated. The Mann-Whitney test was used to compare the medians of the two populations (y, positive; n, negative). The differences were significant for A) LC_480 (Roche), B) ABI_Prism_7700 (ABI), C) LC1.0 (Roche), E) CFX96 (Bio-Rad) and F) LC96 (Roche). The difference was not significant for D) StepOne (Thermo Fisher).

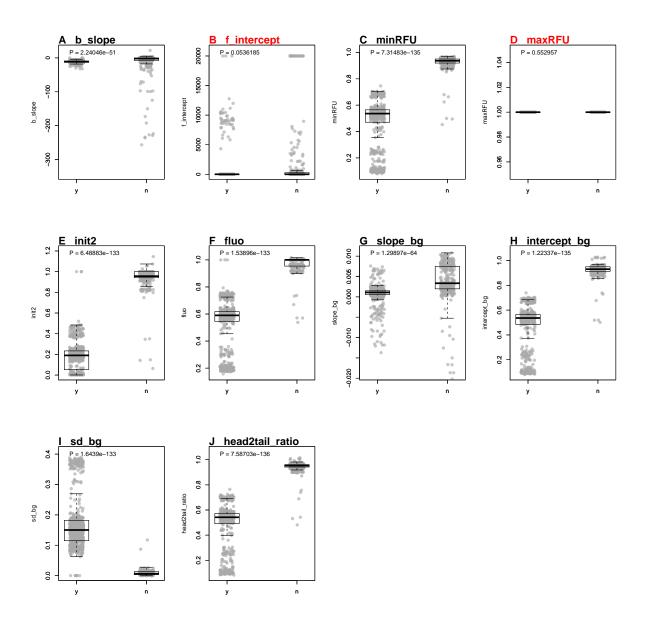


Figure 17: Analysis of slope and ratio features. Amplification curves from the datasets stepone_std, RAS002, RAS003, 1c96_bACTXY, C126EG595 and dil4reps94 were analyzed with the encu() function. These datasets contain positive and negative amplification curves. Furthermore, the meta dataset contains amplification curves that exhibit a hook effect or non-sigmoid shapes, for instance. All amplification curves are manually classified. Altogether 626 positive and 317 negative amplification curves were included in the analysis. A) b_slope, B) f_intercept, C) minRFU is the minimum (1% qantile) of the amplification curve, D) maxRFU is the maximum (99% qantile) of the amplification curve, E) init2 is the initial template fluorescence from an exponential model, F) fluo is the raw fluorescence value at the second derivative maximum, G) slope_bg is the slope calculated be the earlyreg() function, H) intercept_bg is the intercept calculated be the earlyreg() function, I) sd_bg is the standard deviation of the ground phase and J) head2tail_ratio is the between the RFU values of the head and the tail, normalized to the slope from the head to the tail.

part of the PCRedux package. The dataset was split into two chunks. This is an important step during such applications. One chunk is for adapting, i. e. training, the model and the other chunk for testing the model. Typically, 70% to 80% of the data is used for training (Walsh, Pollastri, and Tosatto 2015, Kuhn (2008)). The binomial logistic regression model was adapted using the function glm() by using the parameter family = binomial(link = 'logit'). To objectify the splitting, the sample() function was used.

```
options(warn = -1)
library(PCRedux)
data <- data_sample[data_sample$dataset %in%</pre>
                 c("batsch1",
                   "HCU32_aggR",
                   "lc96 bACTXY",
                   "RAS002",
                   "RAS003".
                   "stepone_std"), ]
n_positive <- sum(data[["decision"]] == "y")</pre>
n_negative <- sum(data[["decision"]] == "n")</pre>
dat <- data.frame(polyarea = data[, "polyarea"],</pre>
                   decision = as.numeric(factor(data$decision,
                                           levels = c("n", "y"),
                                           label = c(0, 1)) - 1)
# Select randomly observations from 70% of the data for training.
# n_train is the number of observations used for training.
n_train <- round(nrow(data) * 0.7)</pre>
# index_test is the index of observations to be selected for the training
index_test <- sample(1L:nrow(dat), size = n_train)</pre>
# index test is the index of observations to be selected for the testing
index_training <- which(!(1L:nrow(dat) %in% index_test))</pre>
# train_data contains the data used for training
train_data <- dat[index_test, ]</pre>
# test_data contains the data used for training
test_data <- dat[index_training, ]</pre>
# Fit the binomial logistic regression model
model_glm <- glm(decision ~ polyarea, family=binomial(link='logit'),</pre>
                  data = train_data)
predictions <- ifelse(predict(model_glm,</pre>
                                   newdata = test_data, type = 'response') > 0.5,
                           1, 0)
res_performeR <- performeR(predictions, test_data[["decision"]])[, c(1:10, 12)]</pre>
```

The 'summary() function returns the results of the model fitting. This can be analysed and interpreted.

summary(model_glm)

```
##
## Call:
## glm(formula = decision ~ polyarea, family = binomial(link = "logit"),
##
       data = train_data)
##
## Deviance Residuals:
##
      Min
                 1Q
                                   30
                                          Max
                     Median
## -5.2389
           -0.3226 -0.1584
                               0.0235
                                        1.7325
##
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
                         0.3171 -8.923
                                            <2e-16 ***
## (Intercept) -2.8294
               91.4661
                           9.8540
                                    9.282
                                            <2e-16 ***
## polyarea
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 489.25
                              on 362 degrees of freedom
## Residual deviance: 154.60
                             on 361 degrees of freedom
## AIC: 158.6
## Number of Fisher Scoring iterations: 7
```

Based on the results it can be concluded that the parameters (Intercept) and polyarea are statistically significant (P < 2e-16). This indicates a strong association between polyarea and the probability that an amplification curve is positive.

In order to apply the model to a new dataset, further steps are necessary. predict() is a generic function for prediction from the results of a model fitting function. All previously split test data is passed to the function argument newdata. By setting the type = 'response' parameter, the predict() function returns probabilities in the form of P(y=1|X). In the case in hand, it was decided that a decision limit of 0.5 is to be applied. If P(y=1|X) < 0.5 then y=0 (amplification curve negative), otherwise y=1 (amplification curves positive).

```
options(warn = -1)
library(PCRedux)
par(mfrow = c(1,2))
# Plot train_data (grey points) and the predicted model (blue)
plot(train_data$polyarea, train_data$decision, pch = 19,
     xlab = "polyarea", ylab = "Probability",
     col = adjustcolor("grey", alpha.f = 0.9), cex = 1.5)
mtext("A", cex = 1.2, side = 3, adj = 0, font = 2, las = 0)
abline(h = 0.5, col = "grey")
curve(predict(model_glm, data.frame(polyarea = x), type = "resp"),
      add = TRUE, col = "blue")
# Plot test data (red)
points(test_data$polyarea, test_data$decision, pch = 19,
       col = adjustcolor("red", alpha.f = 0.3))
legend("right", paste("Positive: ", n_positive,
                      "\nNegative: ", n_negative), bty = "n")
```

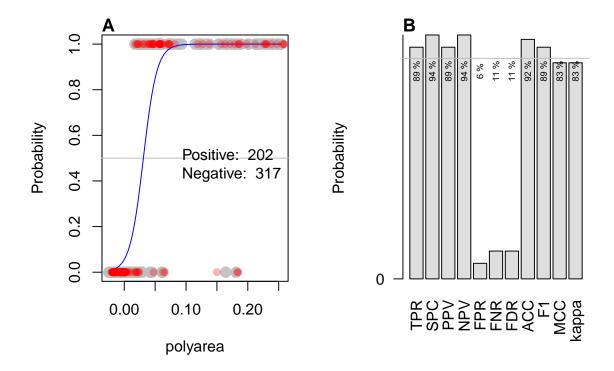


Figure 18: Binomial logistic regression for the polyarea feature. A) binomial logistic regression model for the response variable Y (decision) is categorical and must be converted into a numerical value. This regression calculation makes it possible to estimate the probability of a categorical response using predictor variables X. In this case, the predictor variable is polyarea. Gray dots are the value values used for training. Red dots are the values used for testing. The regression curve of the binomial logistic regression is shown in blue. At 0.5, the gray horizontal line marks the threshold value of probability used to determine whether an amplification curve is negative or positive. B) The measure were determined with the performance() function from the PCRedux package. Sensitivity, TPR; Specificity, SPC; Precision, PPV; Negative predictive value, NPV; Fall-out, FPR; False negative rate, FNR; False discovery rate, FDR; Accuracy, ACC; F1 score, F1; Matthews correlation coefficient, MCC, Cohen's kappa (binary classification), kappa (κ).

The sensitivity, specificity and further parameters for estimating the prediction were calculated using the performeR() function (paragraph 0.4.1.3). The results indicate that the sensitivity and specificity for the test dataset provides a good result. However, the results in this case depend heavily on the computer-aided random sampling of the training data and the total size of the dataset. Over-fitting and under-fitting and other problems need to be addressed (Walsh, Pollastri, and Tosatto 2015).

To proof the results, further methods such as Likelihood Ratio Test, McFadden's \mathbb{R}^2 , k-fold cross-validation, Receiver Operating Characteristic (ROC) analysis and model interpretation should be used (Arlot and Celisse 2010, McFadden (1974), Sing et al. (2005)).

0.4.2.4 autocorrelation_test() - A Function to Detect Positive Amplification Curves

Autocorrelation analysis is a technique that is used in the field of time series analysis. It can be used to reveal regularly occurring patterns in one-dimensional data (Spiess et al. 2016). The autocorrelation measures the correlation of a signal f(t) with itself shifted by some time delay $f(t-\tau)$.

The autocorrelation_test() function coercers the amplification curve data to an object of the class "zoo" (zoo package) as indexed totally ordered observations. Next follows the computation of a lagged version of the amplification curve data. The shifting the amplification curve data is based back by a given number of observations (default $\tau = 12$).

Then follows a significance test for correlation between paired observations (amplification curve data & lagged amplification curve data). The hypothesis is that the paired observation of positive amplification curves has a significant correlation (stats::cor.test, significance level is 0.01) in contrast to negative amplification curves (noise). The application of the autocorrelation_test() function is shown in the following example.

In addition, the the decisions file decision_res_RAS002.csv from the human expert was analyzed for the most frequent decision (modus) using the decision modus() function (paragraph 0.4.1.1).

```
# Test for autocorrelation in amplification curve data
# Load the libraries magrittr for pipes and the amplification curve the data
\mbox{\it \# The amplification curve data from the `RASOO2` dataset was used.}
# The data.table package was used for fast import of the csv data
options(warn = -1)
library(magrittr)
library(PCRedux)
suppressMessages(library(data.table))
data <- RAS002
# Test for autocorrelation in the RASOO2 dataset
res_ac <- sapply(2:ncol(data), function(i) {</pre>
  autocorrelation_test(data[, i], ns_2_numeric = TRUE)
})
# Curves classified by a human after analysis of the overview. 1 = positive,
# 0 = negative
human_classification <- fread(system.file(</pre>
  "decision_res_RAS002.csv",
  package = "PCRedux"
))
head(human_classification)
```

```
RAS002 test.result.1 test.result.2 test.result.3
## 1: A01_gDNA.._unkn_B.Globin
                                             У
                                                            У
                                                                          У
         A01_gDNA.._unkn_HPRT1
## 2:
                                             n
                                                            n
                                                                          n
## 3: A02_gDNA.._unkn_B.Globin
                                             У
                                                            У
                                                                          У
         A02_gDNA.._unkn_HPRT1
## 4:
                                             n
                                                            n
                                                                          n
## 5: A03_gDNA.._unkn_B.Globin
                                             У
                                                            У
                                                                          У
## 6:
         A03_gDNA.._unkn_HPRT1
                                             n
                                                                          n
##
      conformity
            TRUE
## 1:
```

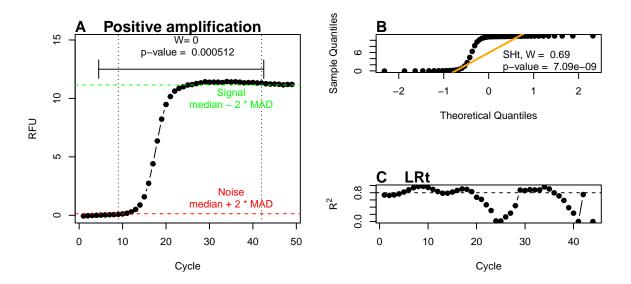


Figure 19: The positive amplification curve F1.1 (testdat dataset) was analyzed with algorithms of the amptester() function. A) The Threshold test (THt) is based on the Wilcoxon rank sum test. The test compares 20% of the head to 15% of the tail region. A significant difference (p-value=0.000512) between the two regions was found for the amplification curve F1.1. This is indicative of a positive amplification reaction. B) Quantile-Quantile plot (Q-Q plot) of the the amplification curve. A Q-Q plot is a probability plot for a graphical comparison of two probability distributions by plotting their quantiles against each other. In this study the probability distribution of the amplification curve is compared to a theoretical normal distribution. The orange line is the theoretical normal quantile-quantile plot which passes through the probabilities of the first and third quartiles. The Shapiro-Wilk test (SHt) of normality checks whether the underlying population of a sample (amplification curve) is significantly ($\alpha \leq 5e^{-4}$) normal distributed. Since the p-value is $7.09e^{-9}$ the null hypothesis can be rejected. C) The Linear Regression test (LRt). This test determines the coefficient of determination (R^2) by an ordinary least squares linear (OLS) regression. Usually the non-linear part of an amplification curve has an R^2 smaller than 0.8.

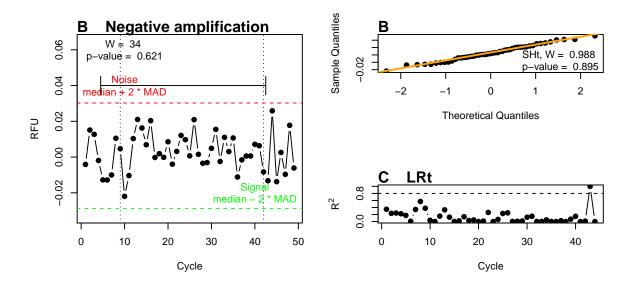


Figure 20: The negative amplification curve F1.3 (testdat dataset) was analyzed with algorithms of the amptester() function. A) The Threshold test (THt) is based on the Wilcoxon rank sum test. The test compares 20% of the head to 15% of the tail region. No significant difference between the two regions was found for the amplification curve F1.3. Since the p-value is 0.621 the null hypothesis cannot be rejected. This is indicative of a negative amplification reaction. B) Quantile-Quantile plot (Q-Q plot) of the the amplification curve. A Q-Q plot is a probability plot for a graphical comparison of two probability distributions by plotting their quantiles against each other. In this study the probability distribution of the amplification curve is compared to a theoretical normal distribution. The orange line is the theoretical normal quantile-quantile plot which passes through the probabilities of the first and third quartiles. The Shapiro-Wilk test (SHt) of normality checks whether the underlying population of a sample (amplification curve) is significantly ($\alpha \le 5e^{-4}$) normal distributed. Since the p-value is 0.895 the null hypothesis cannot be rejected. C) The Linear Regression test (LRt). This test determines the coefficient of determination (R^2) by an ordinary least squares linear (OLS) regression. Usually the non-linear part of an amplification curve has an R^2 smaller than 0.8.

```
## 2:
            TRUE
## 3:
            TRUE
## 4:
            TRUE
## 5:
            TRUE
            TRUE
## 6:
decs <- sapply(1L:nrow(human_classification), function(i) {</pre>
 res <- decision_modus(human_classification[i, 2L:(ncol(human_classification) - 1)])
 if (length(res) > 1) res[[1]] <- "n"
 res[[1]]
}) %>% unlist()
# Plot curve data as overview
# Names of the observations
layout(matrix(c(1, 2, 3, 1, 4, 4), 2, 3, byrow = TRUE))
matplot(
  data[, 1], data[, -1], xlab = "Cycle", ylab = "RFU",
 main = "", type = "1", lty = 1,
  col = decs, lwd = 2
)
legend("topleft", c("positive", "negative"), pch = 19, col = c(1, 2), bty = "n")
          RAS002 dataset", cex = 1.2, side = 3, adj = 0, font = 2)
# Convert the n.s. (not significant) in 0 and others to 1.
# Combine the results of the aromatic autocorrelation_test as variable "ac",
# the human classified values as variable "hc" in a new data frame (res_ac_hc).
cutoff <- 0.8
res_ac_hc <- data.frame(</pre>
 ac = ifelse(res_ac > cutoff, 1, 0),
 hc = as.numeric(as.factor(decs)) - 1
) %>% as.matrix()
res_performeR <- performeR(res_ac_hc[, "ac"], res_ac_hc[, "hc"])</pre>
plot(density(res_ac), ylab = "Autocorrelation", main = "")
rug(res_ac)
abline(v = cutoff)
mtext("B", cex = 1.2, side = 3, adj = 0, font = 2, las = 0)
cdplot(
  as.factor(decs) ~ res_ac, xlab = "Autocorrelation",
  ylab = "Decision"
mtext("C", cex = 1.2, side = 3, adj = 0, font = 2, las = 0)
 as.matrix(res_performeR[, c(1:10, 12)]), yaxt = "n", ylab = "",
 main = "Performance of autocorrelation_test",
 col = adjustcolor("grey", alpha.f = 0.5)
)
```

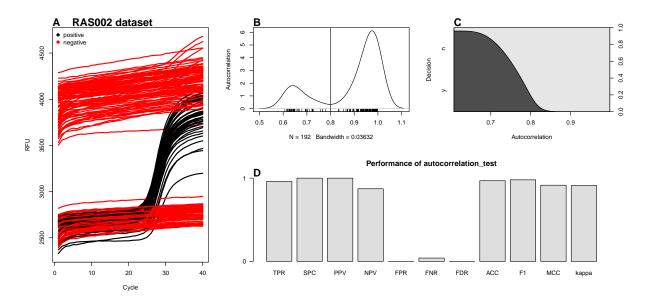


Figure 21: Autocorrelation analysis for amplification curves of the RASO02 dataset (PCRedux package). A) Plot of all amplification curves of the RASO02 dataset. B) Density plot of B) Positive curves and negative curves as determined by the autocorrelation_test() and a human expert. C) Performance analysis by the performeR() function (see paragraph 0.4.1.3 for details).

```
axis(2, at = c(0, 1), labels = c("0", "1"), las = 2)

mtext("D", cex = 1.2, side = 3, adj = 0, font = 2, las = 0)
```

As shown in this example, the autocorrelation_test() function is able to distinguish between positive and negative amplification curves. Negative amplification curve were in all cases non-significant. In contrast, the coefficients of correlation for positive amplification curves ranged between 0.607 and 0.999 at a significance level of 0.01 and a lag of 3.

0.4.2.5 earlyreg() - A Function to Calculate the Slope and Intercept in the Ground Phase of an Amplification Curve

The signal height and the slope in the first amplification curve cycles are helpful information for the analysis of amplification curves. Some qPCR systems calibrate themselves according to the measured values in the first cycles. This is noticeable in the form of strong signal changes which appear spontaneously between the first and second cycle. For another, the signal level can be used to determine which background signal is present and whether the ground phase already has a slope. From the slope it could be deduced whether amplification has already started (see subsubsection 0.1.5).

In addition, the function earlyreg() was developed. This function uses an ordinary least squares linear regression within a limited number of cycles. As ROI, the first 10 cycles were defined. This restriction is based on empirical data suggesting that during the first ten cycles only a significant increase in signal strength can be measured within few qPCRs. However, earlyreg() does not ignore the first cycle, as many thermo-cyclers use this cycle for sensor calibration. Extreme values are therefore included. As standard, the next nine amplitude values are used for the linear regression. The number of cycles can also be adjusted via the parameter range. Since all amplification curves are normalized to the 99%-percentile, there is also a comparability between the background signals and the slopes.

The following example illustrates a possible use of the function earlyreg(). For that purpose amplification curves from the RAS002 dataset were analysed. In figure Figure 22A the amplification curves for all cycles are shown. Next, the earlyreg() function was used to determine the slope and the intercept in the range of the first ten PCR cycles. The results were used in a cluster analysis using k-means clustering (Figure 22B). Therefore, the increase seems to be an indicator of differences between the amplification curves. The Figure 22C shows the first 15 cycles colored according to their cluster. After the cluster analysis this could also be observed (Figure 22D-F). Hence, it can be postulated that the increase in the background phase is helpful for the classification of amplification curves.

```
options(warn = -1)
library(PCRedux)
data <- RAS002
well <- substr(colnames(data)[-1], 1, 10)</pre>
# Normalize each amplification curve to their 0.99 percentile and use the
# earlyreg function to determine the slope and intercept of the first
# 5 cycles
res_earlyreg <- do.call(rbind, lapply(2L:ncol(data), function(i) {</pre>
  earlyreg(x = data[, 1], y = data[, i], range = 5, normalize = FALSE)
}))
# Label the observation with their original names
rownames(res_earlyreg) <- colnames(data)[2:ncol(data)]</pre>
cl <- kmeans(res_earlyreg, 5)</pre>
rownames(res_earlyreg) <- well</pre>
par(fig = c(0,1,0,1), las = 0, bty = "o", oma = c(0, 0, 0, 0))
matplot(
 data[, 1], data[, -1], pch = 19, lty = 1, type = "l",
 xlab = "Cycle", ylab = "RFU", main = "", col = cl[["cluster"]]
)
mtext("A", cex = 1.2, side = 3, adj = 0, font = 2)
abline(v = c(1,5))
rect(20.5,3500,45,4700, col = "white", border = NA)
```

```
text(3, 3250, "ROI")

par(fig = c(0.525, 0.99, 0.5, 0.95), new = TRUE)
plot(res_earlyreg, col = cl[["cluster"]], pch = 19)
mtext("B     k-means, k = 5", cex = 1.2, side = 3, adj = 0, font = 2)
```

0.4.2.6 head2tailratio() - A Function to Calculate the Ratio of the Head and the Tail of a Quantitative PCR Amplification Curve

The ratios from the ground and plateau phase can be used to search for patterns in amplification curves. Positive amplification curves have different slopes and intercepts at the start of the amplification curve (head, background region) and the end of the amplification curve (tail, plateau region). Therefore, these regions are potentially useful to extract a feature for an amplification curve classification. Negative amplification curves - without an increase - are assumed to have a ratio of about 1. In contrast, positive amplification curves should have a ratio of less than 1.

The head2tailratio() function calculates the ratio of the head and the tail of a quantitative PCR amplification curve. As ROI, the areas in the ground phase (head) and plateau phases (tail) are used (Figure 2A). For the calculation, the median from the first six data points of the amplification curve and the median from the last six data points are used. The determination of six data points in both regions was made on the basis of *empirical experience*. As a rule, no increase in amplification signals can be measured in the first six cycles and in the last six cycles, the amplification curve is usually about to transition into the plateau. This assumption is sometimes violated and might lead to false estimates. For example, the amplification curves in Figure 23 show an increase within the first three cycles and the amplification curves in Figure 24 have a negative slope in the tail. The median is used to minimize the influence of outliers.

```
options(warn = -1)
library(PCRedux)
# Load the RAS002 dataset and assign it to the object data
data <- RAS002
data_decisions <- RAS002_decisions
# Calculate the head2tailratio of all amplification curves
res_head2tailratio <- lapply(2L:ncol(data), function(i) {</pre>
  head2tailratio(
    y = data[, i], normalize = TRUE, slope_normalizer = TRUE,
    verbose = TRUE
  )
})
# Fetch all values of the head2tailratio analysis for a later comparison
# by a boxplot.
res <- sapply(1L:length(res_head2tailratio), function(i)</pre>
  res_head2tailratio[[i]]$head_tail_ratio)
data normalized <- cbind(</pre>
  data[, 1],
  sapply(2L:ncol(data), function(i) {
    data[, i] / quantile(data[, i], 0.99)
  })
# Assign color to the positive and negative decisions
```

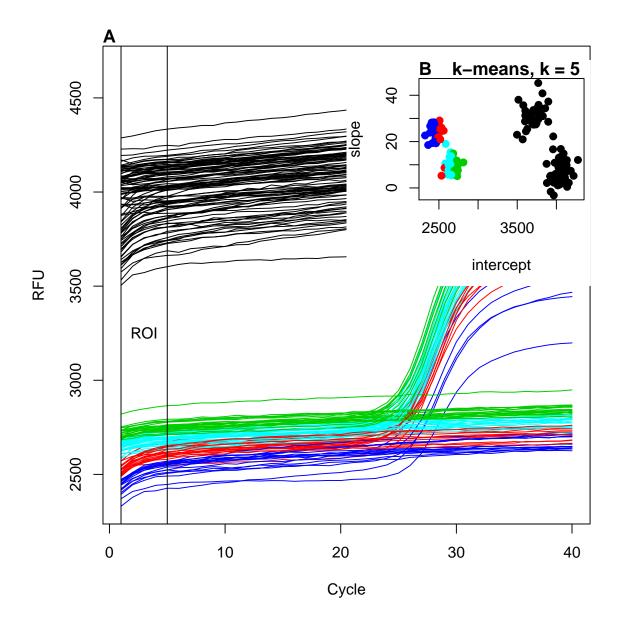


Figure 22: Analysis of the ground phase with the earlyreg() function. A) The amplification curves show different slopes and intercepts in the early ground phase (ROI: cycle 1 to 5) of the qPCR. Amplification curves (n = 192) from the RAS002 dataset were used. B) Both the slope and the intercept were used for a cluster analysis (k-means, Hartigan-Wong algorithm, number of centers k = 5). The amplification curves were separated into three clusters dependent on their slope and intercept (colored in red, green, cyan, balck).

```
colors <- as.character(factor(</pre>
  data_decisions, levels = c("y", "n"),
  labels = c(
      adjustcolor("black", alpha.f = 0.25), adjustcolor("red", alpha.f = 0.25))
))
res_wilcox.test <- stats::wilcox.test(res ~ data_decisions)</pre>
h <- max(na.omit(res))
h_{\text{text}} \leftarrow \text{rep}(h * 0.976, 2)
# Plot the results of the analysis
par(mfrow = c(1, 2), las = 0, bty = "o", oma = c(0, 0, 0, 0))
matplot(
  data_normalized[, 1], data_normalized[, -1],
  xlab = "Cycle", ylab = "normalized RFU", main = "RAS002 dataset",
  type = "1", lty = 1, lwd = 2, col = colors
for (i in 1L:(ncol(data_normalized) - 1)) {
    res_head2tailratio[[i]]$x_roi, res_head2tailratio[[i]]$y_roi,
    col = colors[i], pch = 19, cex = 1.5
  abline(res_head2tailratio[[i]]$fit, col = colors[i], lwd = 2)
mtext("A", cex = 1.2, side = 3, adj = 0, font = 2)
# Boxplot of the head2tail ratios of the positive and negative
# amplification curves.
boxplot(res ~ data_decisions, col = unique(colors), ylab = "Head to Tail Ratio")
lines(c(1, 2), rep(h * 0.945, 2))
text(1.5, h_text, paste0("P = ", signif(res_wilcox.test[["p.value"]])),
     cex = 1)
mtext("B", cex = 1.2, side = 3, adj = 0, font = 2)
```

Figure 6 shows that negative amplification curves can have a trend. The trend may be positive or negative. In subsubsection 0.1.5 some reasons were mentioned. How to deal with this is the question. One possible solution could be to include this factor in the ratio calculation. The head2tailratio() function uses a linear model that calculates the slope between the ground and plateau phases. If the slope of the model is significant, then the ratio from the head and tail is normalized to this slope. This requires setting the slope normalizer parameter in the head2tailratio() function. By default, this parameter is not set.

0.4.2.7 hookreg() and hookregNL() - Functions to Detect Hook Effekt-like Curvatures

hookreg() and hookregNL() are functions to detect amplification curves bearing a hook effect (Barratt and Mackay 2002,) or negative slope at the end of the amplification curve. Both functions calculate the slope and intercept of an amplification curve data. The idea is that a strong negative slope at the end of an amplification curve is indicative for a hook effect. hookreg() and hookregNL() are currently undergoing a review process. For this reason, the functions will not be discussed in detail here. More information is given in the vignette and manual of both functions.

Amplification curves with a hook effect like curvature are characterized by a negative trend in the late phase of the amplification reaction (Figure 24 A, curve F1.1, F1.2, F2.1, F2.2, F3.1 and F3.2).

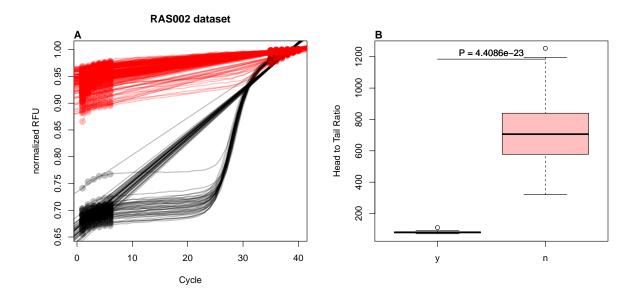


Figure 23: Calculation of the ratio between the head and the tail of a quantitative PCR amplification curve. A) Plot of quantile normalized amplification curves from the RASO02 dataset. ROIs of the head and tail are highlighted by circles. The ranges for performing Robust Linear Regression are automatically selected using the 25% and 75% quantiles. Therefore not all data points are used in the regression model. The straight line is the regression line from the robust linear model. The slopes of the positive and negative amplification curves differ. B) Boxplot for the comparison of the head to tailratio. Positive amplification curves have a lower ratio than negative curves. The difference between the classes is significant.

```
# Calculate slope and intercept on noise (negative) amplification curve data
# for the last eight cycles.
options(warn = -1)
library(qpcR)
library(magrittr)

res_hook <- sapply(2:ncol(boggy), function(i) {
  hookreg(x = boggy[, 1], y = boggy[, i])
}) %>%
  t() %>%
  data.frame(obs = colnames(boggy)[-1], .)
```

The results of the hookreg() analysis were transferred to a tabular format.

Table 5: Screening results for the analysis with the hookreg algorithm. Samples withe a value of 1 in the hook column had all a hook effect like curvature. The observations F4.1, F4.2, F5.1, F5.2, F6.1 and F6.2 miss entries because the hoogreg algorithm could not fit a linear model. This is an expected behavior, since these amplification curves did not have a hook effect like curvature.

obs	intercept	slope	hook.start	hook.delta	p.value	CI.low	CI.up	hook.fit	hook.CI	hook
F1.1	1.17	-0.01	26.00	15.00	0.00	-0.01	-0.01	1.00	1.00	1.00
F1.2	1.20	-0.01	26.00	15.00	0.00	-0.01	-0.01	1.00	1.00	1.00
F2.1	1.16	-0.01	32.00	9.00	0.00	-0.01	-0.00	1.00	1.00	1.00
F2.2	1.17	-0.01	32.00	9.00	0.00	-0.01	-0.00	1.00	1.00	1.00
F3.1	1.05	-0.00	35.00	6.00	0.05	-0.00	0.00	0.00	0.00	0.00
F3.2	1.08	-0.00	35.00	6.00	0.02	-0.01	0.00	0.00	0.00	0.00
F4.1	0.00	0.00	0.00	0.00				0.00	0.00	0.00
F4.2	0.00	0.00	0.00	0.00				0.00	0.00	0.00
F5.1	0.00	0.00	0.00	0.00				0.00	0.00	0.00
F5.2	0.00	0.00	0.00	0.00				0.00	0.00	0.00
F6.1	0.00	0.00	0.00	0.00				0.00	0.00	0.00
F6.2	0.00	0.00	0.00	0.00				0.00	0.00	0.00

In Table 5 is shown that the first amplification curves (F1.1, F1.2, F2.1, F2.2, F3.1 and F3.2) appear to have a hook effect-like curvature ("hook" column=1.00). The function estimate reliably the start of the hook effect-like region.

The clusters for amplification curve were determined by k-means clustering in this example. Next we plot

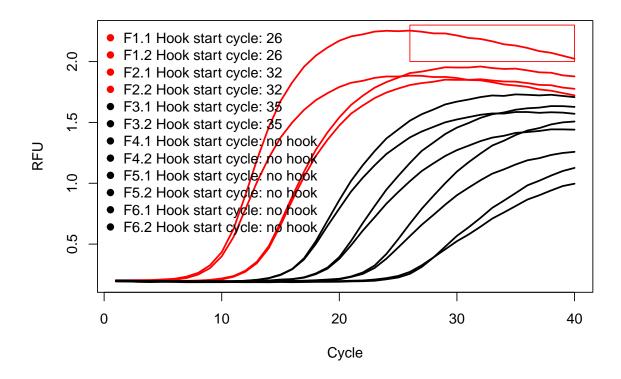


Figure 24: Detection of the hook effect in amplification curves. Amplification curves of the boggy dataset (qpcR) were analyzed using the hookreg() function. The hook effect is characterized by a negative slope in the supposed plateau phase. Samples F1.1, F1.2, F2.1 and F2.2 (red) show a statistically significant negative slope. In the red rectangle the area of the hook effect is highlighted exemplarily for the sample F1.1. No statistically significant negative slope (no hook effect) could be observed for the remaining amplification curves (black).

the results of the analysis (Figure 24). For the visualization the intercepts was plotted against the slope with the clusters as determined by k-means clustering.

```
matplot(
    x = boggy[, 1], y = boggy[, -1], xlab = "Cycle", ylab = "RFU",
    main = "", type = "l", lty = 1, lwd = 2, col = res_hook$hook + 1
)

res_hook$hook.start[res_hook$hook.start == 0] <- "no hook"

legend(
    "topleft", paste(as.character(res_hook$obs), "Hook start cycle:", res_hook$hook.start), pch = 19, col = res_hook$hook + 1, bty = "n"
)
rect(26,2,40,2.3, border = "red")</pre>
```

0.4.2.8 mblrr() - A Function Perform the Quantile-filter Based Local Robust Regression

mblrr() is a function to perform the Median based Local Robust Regression (m blrr) from a quantitative PCR experiment. In detail, this function attempts to break the amplification curve in two ROIs (head (~background) and tail (~plateau)). As opposed to the earlyreg() function, the mblrr() function does not use a fixed interval. Instead, themblrr()function dynamically determines cut points for each amplification curve. For the ``mblrr() function was defined:

- The 25% quantile is the value for which 25% of all values are smaller than this value.
- The 75% quantile is the value for which 75% of all values are greater than this value.

Subsequent, a robust linear regression analysis (lmrob()) is preformed individually on both regions of the amplification curve. The rationale behind this analysis is that the slope and intercept of an amplification curve differ in the background and plateau region. This is also shown bey the simulations in Figure 1C-E. In the example shown below, the observations "P01.W19", "P06.W35", "P33.W66", "P65.W90", "P71.W23" and "P87.W01" were arbitrarily selected for demonstration purposes Figure 25. Another example is shown in Figure 9A. Those amplification curves have a slight negative trend in the baseline region and a positive trend in the plateau region.

The correlation coefficient⁵ is a measure to quantify the dependence on variables (e. g., number of cycles, signal height). The correlation coefficient is always between -1 and 1, with a value close to -1 describing a strong-negative dependency and close to 1 describing a strong-positive dependency; if the value is 0, there is no dependency between the variables. The most frequently used correlation coefficient to describe a linear dependency is the Pearson correlation coefficient r.

The correlation coefficient can also be used as a feature. Because similar data structures will have similar correlation coefficients. Correlation coefficients are between -1 and +1, with -1 being a strong negative correlation and 1 a strong positive correlation. The values of -1 and 1 have a perfect correlation. If the value is 0, there is no correlation between the two variables. However, variables that are not strongly correlated can also be important for modeling.

```
options(warn = -1)
library(PCRedux)
# Select four amplification curves from the RASOO2 dataset
data \leftarrow RAS002[, c(1, 2, 3, 4, 5)]
par(mfrow = c(2, 2))
for (i in 2L:ncol(data)) {
 x <- data[, 1]
 y_tmp <- data[, i] / quantile(data[, i], 0.99)</pre>
 res_q25 <- y_tmp < quantile(y_tmp, 0.25)</pre>
 res_q75 <- y_tmp > quantile(y_tmp, 0.75)
 res_q25_lm <- try(
    suppressWarnings(lmrob(y_tmp[res_q25] ~ x[res_q25])),
    silent = TRUE
 )
 res_q75_lm <- try(
    suppressWarnings(lmrob(y_tmp[res_q75] ~ x[res_q75])),
    silent = TRUE
 plot(x, y_tmp, xlab = "Cycle", ylab = "RFU (normalized)",
    main = "", type = "b", pch = 19)
 mtext(paste0(LETTERS[i], " ", colnames(data)[i]), cex = 1, side = 3,
        adj = 0, font = 2)
  abline(res_q25_lm, col = "red")
 points(x[res_q25], y_tmp[res_q25], cex = 2.5, col = "red")
 abline(res q75 lm, col = "green")
 points(x[res_q75], y_tmp[res_q75], cex = 2.5, col = "green")
}
```

Finally, the results of the analysis were printed in a tabular format.

⁵Pearson's product moment correlation coefficient

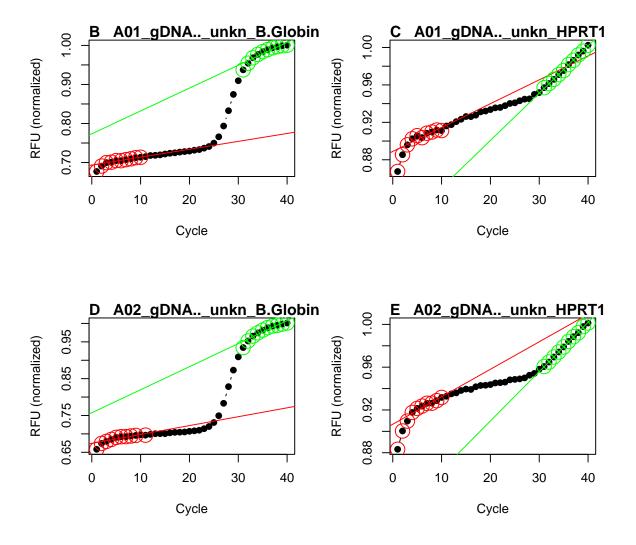


Figure 25: Robust local regression to analyze amplification curves. The amplification curves were arbitrarily selected from the RASO02 dataset. Not the differences in slopes and intercepts (red and green lines). The mblrr() function is presumably useful for datasets which are accompanied by noise and artifacts.m, slop; n, intercept.

```
# Load the xtable library for an appealing table output
library(xtable)
# Analyze the data via the mblrr() function
res_mblrr <- do.call(cbind, lapply(2L:ncol(data), function(i) {</pre>
  suppressMessages(mblrr(
    x = data[, 1], y = data[, i],
    normalize = TRUE
  )) %>% data.frame()
}))
colnames(res_mblrr) <- colnames(data)[-1]</pre>
# Transform the data for a tabular output and assign the results to the object
# output_res_mblrr.
output_res_mblrr <- res_mblrr %>% t()
# The output variable names of the mblrr() function are rather long. For better
# readability the variable names were changed to "nBG" (intercept of head region),
# "mBG" (slope of head region), "rBG" (Pearson correlation of head region),
# "nTP" (intercept of tail region), "mTP" (slope of tail region), "rBG" (Pearson
# correlation of tail region)
colnames(output_res_mblrr) <- c(</pre>
  "nBG", "mBG", "rBG",
  "nTP", "mTP", "rTP"
print(xtable(
  output_res_mblrr, caption = "mblrr() text intro. nBG, intercept of
             head region; mBG, slope of head region; rBG, Pearson
             correlation of head region; nTP, intercept of tail region; mTP,
             slope of tail region; rBG, Pearson correlation of tail region",
  label = "tablemblrrintroduction"
), comment = FALSE, caption.placement = "top")
```

Table 6: mblrr() text intro. nBG, intercept of head region; mBG, slope of head region; rBG, Pearson correlation of head region; nTP, intercept of tail region; mTP, slope of tail region; rBG, Pearson correlation of tail region

	nBG	mBG	rBG	nTP	mTP	rTP
A01_gDNAunkn_B.Globin	0.69	0.00	0.91	0.77	0.01	0.94
A01_gDNAunkn_HPRT1	0.89	0.00	0.87	0.80	0.01	1.00
A02_gDNAunkn_B.Globin	0.67	0.00	0.88	0.76	0.01	0.95
A02_gDNAunkn_HPRT1	0.91	0.00	0.90	0.82	0.00	1.00

In another example, the results from the mblrr() function were combined with the classifications (positive, negative) by a human to apply them in an analysis with Fast and Frugal Trees (FFTrees). A general introduction to decision trees is given in (Quinlan 1986, Luan, Schooler, and Gigerenzer (2011)). FFTrees belong to class of simple decision rules. In many situations, FFTrees make fast decisions based on a few features (N = 1 - 5). In this example six features were used for the analysis.

The FFTrees package (Phillips et al. 2017) provides an implementation for the R statistical computing language. All that is needed for the present example are:

- the data assessed by the mblrr() function,
- the classification of the amplification curve data by a human,
- and a standard formula, which looks like $outcome \leftarrow var1 + var2 + \dots$ along with the data arguments. The function FFTrees() returns a fast and frugal tree object. This rich object contains

the underlying trees and many classification statistics (similar to paragraph 0.4.1.3). In the following example, the RASO02 dataset from the qpcR package was used.

```
# Load the xtable library for an appealing table output
options(warn = -1)
suppressMessages(library(FFTrees))
library(PCRedux)
# The RASOO2 amplification curves were analyzed with the mblrr() function
# to save computing time and the.results of this analysis are stored in the
# `data_sample` dataset.
data <- data_sample[data_sample$dataset == "RAS002", c("mblrr_intercept_bg",</pre>
                                                         "mblrr_slope_bg",
                                                         "mblrr_cor_bg",
                                                         "mblrr_intercept_pt",
                                                         "mblrr_slope_pt",
                                                         "mblrr_cor_pt")]
# The output variable names of the mblrr() function are rather long. For better
# readability the variable names were changed to "nBG" (intercept of head
# region), "mBG" (slope of head region), "rBG" (Pearson correlation of head
# region), "nTP" (intercept of tail region), "mTP" (slope of tail region),
# "rBG" (Pearson correlation of tail region).
res_mblrr <- data.frame(</pre>
    class = as.numeric(as.character(factor(RAS002 decisions,
                                            levels = c("y", "n"),
                                            label = c(1, 0))),
  data
)
colnames(res_mblrr) <- c("class", "nBG", "mBG", "rBG", "nTP", "mTP", "rTP")</pre>
res_mblrr.fft <- suppressMessages(</pre>
            FFTrees(formula = class ~., data = res_mblrr)
```

Figure 26 shows the Fast and Frugal Trees by using the features nBG (intercept of head region), mBG (slope of head region), rBG (Pearson correlation of head region), nTP (intercept of tail region), mTP (slope of tail region), and rBG (Pearson correlation of tail region).

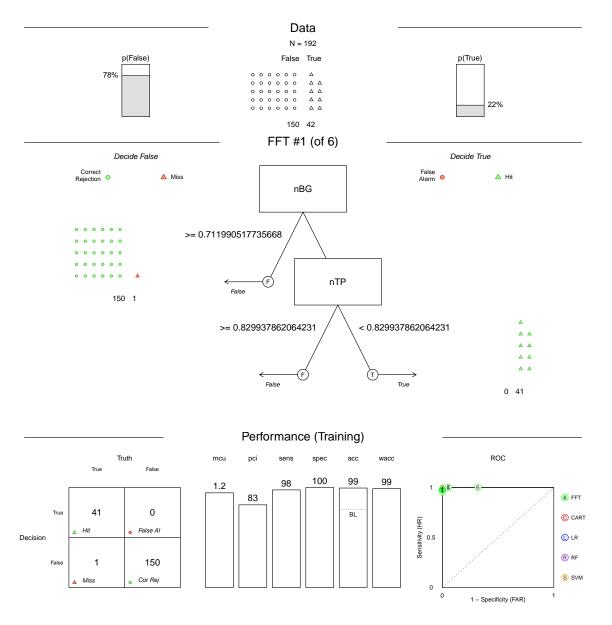


Figure 26: Visualization of FFTrees of a mblrr() function analysis. Top row Data) Overview of the dataset, with displaying the total number of observations (N = 192) and percentage of positive (22%) and negative (78%) amplification curves. Middle row FFT #1 (of 6)) Decision Tree with the number of observations classified at each level of the tree. For the analysis, six features (nBG, intercept of head region; mBG, slope of head region; rBG, Pearson correlation of head region; nTP, intercept of tail region; mTP, slope of tail region; rBG, Pearson correlation of tail region) have been used for the analysis. After two tree levels (nBG, nTP) already the decision tree is created. All positive amplification curves (N = 40) are correctly classified. Two observations are classified as false-negative in the negative amplification curves. Lower row Performance) The FFTrees() function determines several performance statistics. For the training data, there is a classification table on the left side showing the relationship between tree decision and the truth. The correct rejection (Cor Rej) and Hit are the right decisions. Miss and false alarm (False A1) are wrong decisions. The centre shows the cumulative tree performance in terms of mean of used cues (mcu), Percent of ignored cues (pci), sensitivity (sens), specificity (spec), accuracy (acc) and weighted Accuracy (wacc). The receiver operating characteristic (ROC) curve on the right-hand side compares the performance of all trees in the FFTrees object. The system also displays the performance of the fast frugal trees (#, green), CART (C, red), logistical regression (L, blue), random forest (R, violet) and the support vector machine (S, yellow).

0.4.2.9 Change point analysis

Change point analysis (CPA) encompasses methods to identify or estimate single or multiple locations of distributional changes in a series of data points indexed in time order. A change herein refers to a statistical property. There exist several change point algorithms such as the binary segmentation algorithm (A. J. Scott and Knott 1974). In the change point analysis one assumes independent ordered observations $X_1, X_2, \ldots, X_n \in \mathbb{R}^d$ (N. A. James and Matteson 2013). The the case of qPCR this is simply the cycle-dependent fluorescence. This is be used to create k homogeneous subsets of unknown size (Erdman, Emerson, and others 2007). While frequentist methods make an estimation of the parameter at the location (e. g., mean, variance) of the change points at specific points, change point analysis using the Bayesian method produces a probability for the occurrence of a change point at certain points. CPA is used for example in econometrics and bioinformatics (Killick and Eckley 2014, Erdman, Emerson, and others (2007)). For the analysis of the amplification curves it was hypothesized that the number of change points differs between positive (sigmoidal) and negative (noise) amplification curves.

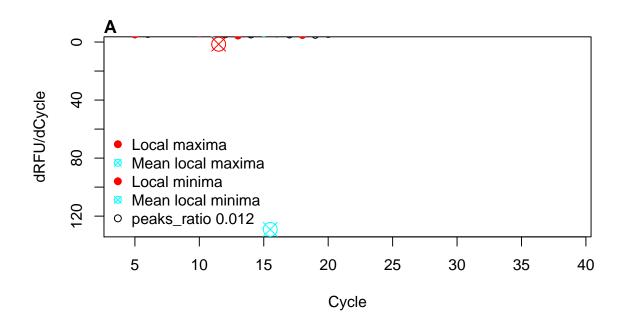
The pcrfit_single() function uses two independent approaches for change point analysis. These are the bcp() function from the bcp package (Erdman, Emerson, and others 2007) and the e.agglo() function from the ecp package (N. A. James and Matteson 2013). The e.agglo() function performs a non-parametric change point analysis based on agglomerative hierarchical estimation and is useful to "detect changes within the marginal distributions" (N. A. James and Matteson 2013). Measurement from the qPCR systems typically shows noise that typically has rapidly changing components. Differentiators amplify these rapidly changing noise components (Rödiger, Böhm, and Schimke 2013). Therefore, the first derivation of the amplification curve was used for both change point analyses. It was assumed for the change point analysis of amplification curves that this leads to larger differences between positive and negative amplification curves. An example is shown on Figure 29. In contrast the bcp() [bcp] function performs a change point analysis based on a Bayesian approach. This method can detect changes in the mean of independent Gaussian observations. As result the analysis returns the posterior probability of a change point at each X_i . An example is shown on Figure 29. Both the change point analysis methods provide additional information to distinguish positive and negative amplification curves Figure 28E & F).

Loading required package: Rcpp

0.4.2.10 Test of an amplification reaction

A part of the pcrfit_single() function is the amptester() function from the chipPCR package. This function contains tests to determine whether an amplification curve is positive or negative. The input values for the function differ due to the different pre-processing steps in the pcrfit_single() function. Therefore, the concepts of the tests are briefly described below.

- The first test, designated as SHt, is based on this Shapiro-Wilk test of normality. This relatively simple procedure can be used to check whether the underlying population of a sample (amplification curve) is significantly ($\alpha \le 5e 04$) normal distributed. In Figure 4 it can be seen that negative amplification curves resemble a normal distribution, but positive amplification curves are deviating from the normal distribution. The output is binary coded (negative = 0, positive = 1). The name of the output of the pcrfit_single() function is amptester_shapiro.
- The second test is the *Resids growth test* (RGt), which tests if the fluorescence values in linear phase are stable. Whenever no amplification occurs, fluorescence values quickly deviate from linear model. Their standardized residuals will be strongly correlated with their value. For real amplification curves, situation is much more stable. Noise (that means deviations from linear model) in background do not correlate strongly with the changes in fluorescence. The decision is based on the threshold value (here 0.5). The output is binary coded (negative = 0, positive = 1). The output name of the pcrfit_single() function is amptester_rgt.
- The third test is the *Linear Regression test* (LRt). This test determines the coefficient of determination (R^2) by an ordinary least squares linear (OLS) regression. The R^2 are determined from a run of circa 15% range of the data. If a sequence of more than six R^2 s is larger than 0.8 is found that is likely a nonlinear signal. This is a bit counter intuitive because R^2 of nonlinear data should be low. The output is binary coded (negative = 0, positive = 1). The output name of the pcrfit_single() function is amptester_lrt.
- The fourth test is called *Threshold test* (THt), which is based on the Wilcoxon rank sum test. As a simple rule the first 20% (head) and the last 15% (tail) of an amplification curve are used as



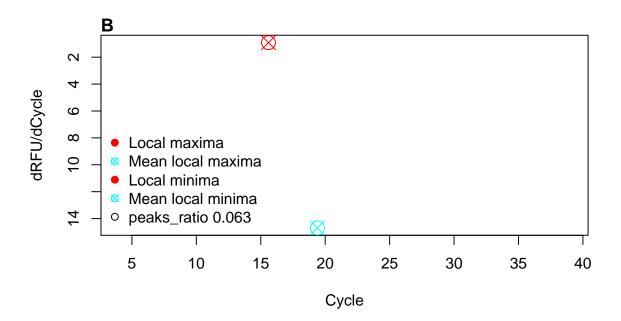


Figure 27: Principle behind the peaks_ratio feature. The computation is based on a sequential linking of functions. The diffQ() function (MBmca) determines numerically the first derivative of an amplification curve. This derivative is passed to the mcaPeaks() function (MBmca). In the output all minima and all maxima are contained. The ranges are calculated from the minima and maxima. The Lagged Difference is determined from the ranges of the minima and maxima. Finally, the ratio of the differences (maximum/minimum) is calculated.

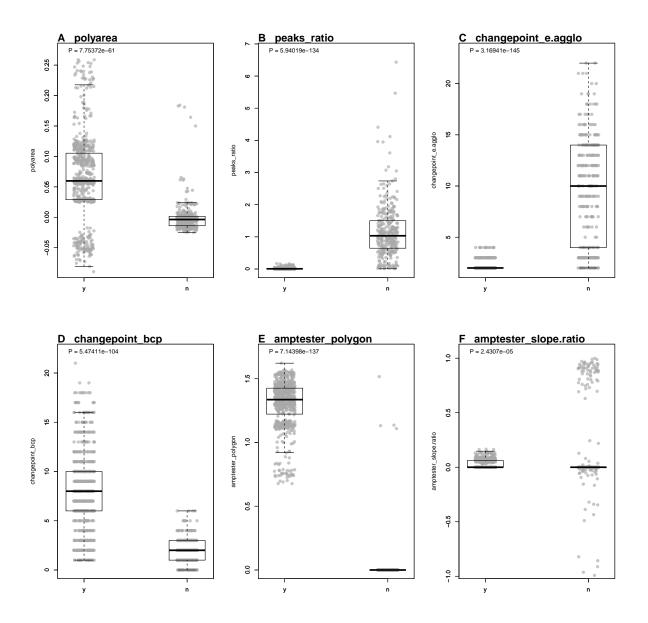


Figure 28: Analysis of area and changepoint features. Amplification curves from the datasets stepone_std, RASO02, RASO03, 1c96_bACTXY, C126EG595 and dil4reps94 were analyzed with the encu() function. These datasets contain positive and negative amplification curves. Furthermore, the meta dataset contains amplification curves that exhibit a hook effect or non-sigmoid shapes, for instance. All amplification curves are manually classified. Altogether 626 positive and 317 negative amplification curves were included in the analysis. A) polyarea, is the area under the amplification curve determined by the Gauss polygon area formula. B) peaks_ratio, is the ratio of the local minima and the local maxima. C) changepoint_e.agglo, makes use of energy agglomerative clustering. Positive amplification curves have fewer change points than negative amplification curves. These two change point analyses generally separate positive and negative amplification curves. D) changepoint_bcp, analyses change points by a Bayesian approach. Positive amplification curves appear to contain more change points than negative amplification curves. Nevertheless, there is an overlap between the positive and negative amplification curves in both methods. This can lead to false-positive or false-negative classifications. E) amptester_polygon, is the cycle normalized order of a polygon. F) amptester_slope.ratio, is the slop (linear model) of the raw fluorescence values at the approximate first derivate maximum, second derivative minimum and second derivative maximum.

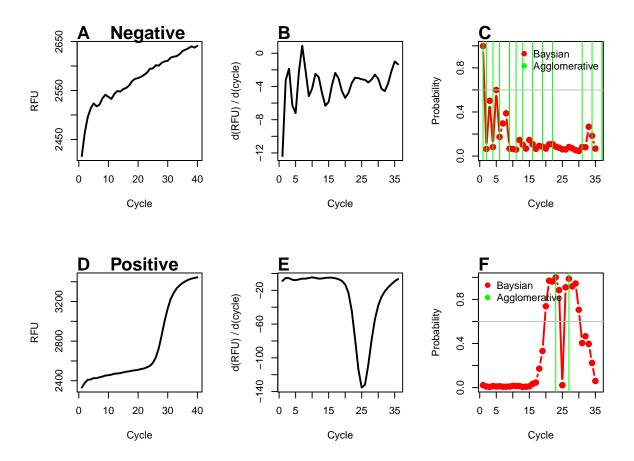


Figure 29: Application of Bayesian change point analysis and energy agglomerative change point analysis methods to the RASO02 dataset. An analysis of a negative and a positive amplification curve from the RASO02 dataset was performed using the pcrfit_single() function. In this process, the amplification curves were analysed for change points using Bayesian change point analysis and energy agglomerative clustering. A) The negative amplification curve has a base signal of cica 2450 RFU and only a small signal increase to 2650 RFU. There is a clear indication of the signal variation (noise). B) The first negative derivative amplifies the noise so that some peaks are visible. C) The change point analysis shows changes in energy agglomerative clustering at several positions (green vertical line). The Bayesian change point analysis rarely exceeds a probability of 0.6 (grey vert line). D) The positive amplification curve has a lower base signal (~ 2450 RFU) and increases up to the 40th cycle (~3400 RFU). A sigmoid shape of the curve is clearly visible. E) The first negative derivation of the positive amplification curve shows a distinctive peak with a minimum at cycle 25. F) The change point analysis in energy agglomerative clustering shows changes (green vertical line) only at two positions. The Bayesian change point analysis shows a probability higher then 0.6 (grey horizontal line) at several positions.

- input data. From that a one-sided Wilcoxon rank sum tests of the head versus the tail is performed $(\alpha \le 1e-02)$. The output is binary coded (negative = 0, positive = 1). The output name of the pcrfit_single() function is amptester_tht.
- The fifth test is called *Signal level test* (SLt). he test compares the signals of the head and the tail by a robust "sigma" rule (median + 2 * median absolute deviation) and the the comparison of the head/tail ratio. If the returned value is less than 1.25 (25 percent), then the amplification curve is likely negative. The output is binary coded (negative = 0, positive = 1). The output name of the pcrfit_single() function is amptester_slt.
- The sixth test is called *Polygon test* (pco). The pco test determines if the points in an amplification curve (like a polygon) are in a "clockwise" order. The sum over the edges result in a positive value if the amplification curve is "clockwise" and is negative if the curve is counter-clockwise. From experience is noise positive and "true" amplification curves "highly" negative. In contrast to the implementation in the amptester() function, the result is normalized by a division to the number of PCR cycles. The output is numeric. The output name of the pcrfit_single() function is amptester_polygon.
- The seventh test is the *Slope Ratio test* (SIR). This test uses the approximated first derivative maximum, the second derivative minimum and the second derivative maximum of the amplification curve. Next the raw fluorescence at the approximated second derivative minimum and the second derivative maximum are taken from the original dataset. The fluorescence intensities are normalized to the maximum fluorescence of this data. This data is used for a linear regression. Where the slope is used. The output is numeric. The output name of the pcrfit_single() function is amptester_slope.ratio.

Application of the "amptester()" Features

Random Forest is an enhancement of decision tree algorithms. Random Forest uses n random data subsets. The subset is to be used to capture trends precisely without taking into account the whole data. In order to do this, an ensemble consisting of n small decision trees is generated. Each decision tree contains a biased classifier. The majority of the previous classes are then selected for classification. Compared to a single tree classifier, the Random Forest has a high robustness against noise, outliers and over-fitting (Williams 2009, Breiman (2001)).

In the following example, the randomForest() function from the randomForest package (Liaw and Wiener 2002) was used for the classification. The aim was to classify positive and negative amplification curves. As response vector (y) served decision with its possible states "positive" and "negative" (factor). The features amptester_shapiro, amptester_lrt, amptester_rgt, amptester_tht, amptester_slt, amptester_polygon and amptester_slope.ratio served as a matrix of predictors describing the model to be adapted. The batsch1, HCU32_aggR, stepone_std, RAS002, RAS003, lc96_bACTXY datasets were used for the analysis. This dataset contains almost equal proportions of positive and negative amplification curves (Figure 18A). Prior to this, the amplification curves were analyzed with the encu() function (paragraph 0.4.2.1) and stored in the data_sample.rda file to save computing time. The file is part of the PCRedux package.

```
dat <- data.frame(data[, c("amptester_shapiro",</pre>
                            "amptester_lrt",
                            "amptester_rgt",
                            "amptester_tht",
                            "amptester_slt",
                            "amptester_polygon",
                            "amptester_slope.ratio")],
                  decision = as.numeric(factor(data$decision,
                                          levels = c("n", "y"),
                                           label = c(0, 1)) - 1)
# Select randomly observations from 70% of the data for training.
# n_train is the number of observations used for training.
n_train <- round(nrow(data) * 0.7)</pre>
# index_test is the index of observations to be selected for the training
index_test <- sample(1L:nrow(dat), size = n_train)</pre>
# index_test is the index of observations to be selected for the testing
index_training <- which(!(1L:nrow(dat) %in% index_test))</pre>
# train_data contains the data used for training
train_data <- dat[index_test, ]</pre>
# test_data contains the data used for training
test_data <- dat[index_training, ]</pre>
model_rf = randomForest(decision ~ ., data = train_data, ntree = 4000,
                         importance = TRUE)
# Determine variable importance
res_importance <- importance(model_rf)</pre>
par(mfrow = c(1,3))
plot(model_rf, main = "", las = 2)
mtext("A", cex = 1.2, side = 3, adj = 0, font = 2, las = 0)
rownames(res_importance) <- substr(rownames(res_importance), 11, 22)</pre>
barplot(t(as.matrix(sort(res_importance[, 1]))),
        ylab = "%IncMSE", main = "", las = 2,
        col = adjustcolor("grey", alpha.f = 0.5))
mtext("B", cex = 1.2, side = 3, adj = 0, font = 2, las = 0)
barplot(t(as.matrix(sort(res_importance[, 2]))),
        ylab = "IncNodePurity", main = "", las = 2,
        col = adjustcolor("grey", alpha.f = 0.5))
mtext("C", cex = 1.2, side = 3, adj = 0, font = 2, las = 0)
```

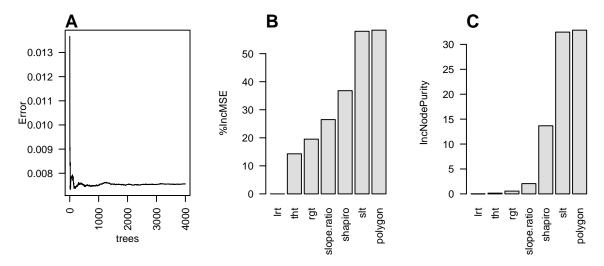


Figure 30: Random Forest.

0.4.2.11 Parallel Programming

pcrfit_single() is a function, which calculates 48 potential features from an amplification curve. This comes at a cost, since several internal functions are computational very intensive (Porzelius, Knaus, and Schwarzer 2009, Schmidberger et al. (2009)). For example, pcrfit() function (qpcR package) in pcrfit_single() fits and optimizes eight non-linear (sigmoid) models to the amplification curve data. encu() (ENcode CUrves) is a relative of the pcrfit_single() function. Similarly, this function calculates numerous but with an emphasis on features extraction of large amplification curve datasets.

The pcrfit_single() function is performing the analysis for a single process and the pblapply() function from the pbapply package is used internally to is delivers a progress bar and leverages parallel processing. Examples are given in the documentation of the encu() function. Parallel computing technologies saves scientists time in their routine tasks of analyzing experimental data. Information about parallel computing technologies in R are available from Eddelbuettel (2017).

To process high data volumes and to deal with speed issues several R packages for parallelization were evaluated (Vera, Jansen, and Suppi 2008, Porzelius, Knaus, and Schwarzer (2009), Boehringer (2013)). For the calculation of the curve parameters the custom-made function pcrfit_parallel() was developed. In particular, to benchmark and evaluate the performance of multiple learners on multiple tasks studies quickly become resource-demanding. Therefore, packages such as mlr support natively parallelization (Bischl et al. 2010).

The code block below shows an example for a parallelized version of pcrfit_single(). This function is called pcrfit_parallel(), which is intended for users who wish to calculate the features of a large amplification curve dataset. This function appears to be works on Linux systems. On Windows systems error messages were reported. pcrfit_parallel() makes use of parallelized code to make use of multicore architectures. In this function we import from the parallel package the detectCores() function. This function determines the number of available cores. Function from the foreach package (e. g., %dopar%, foreach()) are used for the further organization of the CPU usage. The pcrfit_single() performs the analysis for a single process.

- The parameter data is the dataset containing the cycles and fluorescence amplitudes.
- The parameter n_cores defines the numbers of cores that should be left unused by this function.

By default, pcrfit_parallel() is using only one core (n_cores=1). n_cores="all" uses all available cores. The output of the pcrfit_parallel() function is similar to the pcrfit_single() function.

```
# Copy and paste the code to an R console to evaluate it
library(parallel)
library(doParallel)
```

```
pcrfit_parallel <- function(data, n_cores=1) {</pre>
    # Determine the number of available cores and register them
    if (n_cores == "all") {
        n_cores <- detectCores()</pre>
    registerDoParallel(n cores)
    # Prepare the data for further processing
    # Normalize RFU values to the alpha percentile (0.99)
    cycles <- data.frame(cycles = data[, 1])</pre>
    data_RFU <- data.frame(data[, -1])</pre>
    data_RFU_colnames <- colnames(data_RFU)</pre>
    data_RFU <- sapply(1L:ncol(data_RFU), function(i) {</pre>
        data_RFU[, i] / quantile(data_RFU[, i], 0.99, na.rm = TRUE)
    colnames(data_RFU) <- data_RFU_colnames</pre>
    # just to shut RCHeck for NSE we define ith_cycle
    ith_cycle <- 1
    run_res <- foreach::foreach(</pre>
        ith_cycle = 1L:ncol(data_RFU),
                                  .packages = c(
                                      "bcp", "changepoint", "chipPCR", "ecp", "MBmca",
                                      "PCRedux", "pracma", "qpcR", "robustbase",
                                      "zoo"
                                  ),
                                  .combine = rbind
    ) %dopar% {
        suppressMessages(pcrfit_single(data_RFU[, ith_cycle]))
    res <- cbind(runs = colnames(data_RFU), run_res)</pre>
    rownames(res) <- NULL</pre>
    res
}
# Calculate curve features of an amplification curve data. Note: Not all
\# CPU cores are used. If need set "all" to use all available cores.
# In this example the testdat dataset from the qpcR package is used.
# The observations F1.1 and F1.2 are positive amplification curves. The observations
# F1.3 and F1.4 are negative.
options(warn = -1)
library(qpcR)
res_pcrfit_parallel <- pcrfit_parallel(testdat[, 1:5])</pre>
res_pcrfit_parallel
```

1 Summary and Conclusions

The PCRedux enables the user to extract features from amplification curve data. Numerous features can be extracted from the amplification curve. Some of them have not been described in the literature. We consider PCRedux as enabling technology for further research. For example, the proposed features are useable for machine learning applications or quality assessment of data.

Such software can be used in high-throughput applications in combination with other technologies, such as next generation sequencing. Next generation sequencing depends on pre-tests of the input DNA, prior to sequencing and is also used for confirmatory experiments after RNA-Seq quantification. To this end automatized quality control and decision support are conceivable applications.

The pcrfit_single() function is an extendable wrapper function for several algorithm. Currently, 48 features can be calculated from an amplification curve.

Of note, we would like to emphasis that the functionality of this package is not limited to amplification curve data from qPCR experiments. As stated before, amplification curves have a sigmoid curve shape. Presumably, this can also be used for melting curve analysis.

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