

Package ‘PowerUpR’

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Type Package

Title R version of PowerUp!

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Description

R version of PowerUp! allows calculation of statistical power, minimum detectable effect size, and constrained optimal sample allocation for main, and moderator effects in various multilevel randomized experiments.

URL <https://github.com/metinbulus/PowerUpR>

BugReports <https://github.com/metinbulus/PowerUpR/issues>

Depends nloptr(>= 1.0.4)

Suggests knitr, rmarkdown

VignetteBuilder knitr

License GPL (>= 3)

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introduction	<i>Introduction to PowerUpR</i>
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Description

PowerUpR is an implementation of *PowerUp!*, and *PowerUp!-Moderator* in R environment (R Core Team, 2017). *PowerUp!* series consist of convenient excel based functions to conduct statistical power analysis for various experimental and quasi-experimental designs (Dong & Maynard, 2013). It also enables users to conduct statistical power analysis for moderator effects in two- and three-level cluster randomized trials (Dong, Kelcey, & Spybrook, in press; Spybrook, Kelcey, & Dong, in press), and for mediator effects in two-level cluster randomized trials (Kelcey, Dong, Spybrook, & Cox, 2017; Kelcey, Dong, Spybrook, & Shen, in press).

The PowerUpR package bases its framework on three fundamental concepts in statistical power analysis; statistical power calculation, minimum detectable effect size calculation, and constrained optimal sample allocation (COSA; Hedges & Borenstein, 2014; Raudenbush, 1997; Raudenbush & Liu, 2000). COSA problems can be solved in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i, ii or iii options.

A design parameter (one of the MDES, power, or COSA) can be requested by using appropriate function given design characteristics.

Each function begins with an **output** name, followed by a period, an **effect** (for moderator only), followed by a period, and a **design** name.

There are three types of output; mdes, power, and optimal, and 14 types of design; ira1r1, bira2r1, bira2f1, bira2c1, cra2r2, bira3r1, bcra3r2, bcra3f2, cra3r3, bira4r1, bcra4r2, bcra4r3, bcra4f3, and cra4r4. The first three or four letters of the design stands for the type of assignment, for individual random assignment ira, for blocked individual random assignment bira, for cluster random assignment cra, and for blocked cluster random assignment bcra. It is followed by a number indicating number of levels. A single letter followed by a number indicates whether a block is considered to be r, random; f, fixed; or c, constant and the level at which random assignment takes place.

A function with two keywords (output.design) returns results for main effect. For moderator effect, there is an additional keyword so the function has three keywords (output.effect.design). There are three moderator effects available for design cra2r2 and five moderator effect available for design cra3r3. In total there are six moderator effects; mod1n, mod1r, mod2, mod2n, mod2r, and mod3. The number and the single letter at the end stands for the level of moderator variable and whether it varies randomly or non-randomly across higher level unit.

So, to find MDES for main effect in two-level cluster randomized design where random assignment is at level-2, function `mdes.cra2r2` is used. Similarly, to find MDES for a non-randomly varying moderator effect at level-1 for the same design, function `mdes.mod1n.cra2r2` is used.

Each function requires slightly different arguments depending on the output it produces and the design. Most of the arguments have default values to provide users a starting point, which can be found in *usage* section of the documentation. For all functions default values are

- `mdes = .25`
- `power (1 - β) = .80`
- `alpha (α) = .05`
- `two.tail = TRUE`
- `P = .50`

and depending on the effect and design

- any of one of `g1`, `g2`, `g3`, `g4 = 0`
- any sequence of `R12`, `R22`, `R32`, `R42 = 0`
- any sequence of `RT22`, `RT32`, `RT42 = 0`
- `Q = NULL`, implies continuous moderator

Users should be aware of default values and change them if necessary. Depending on the function minimum required arguments are

- any sequence of `rho2`, `rho3`, `rho4`
- any sequence of `omega2`, `omega3`, `omega4`
- any one of, any sequence of, or any combination of `n`, `J`, `K`, `L`

For definition of above-mentioned parameters, statistical models and formulas see Dong and Maynard (2013), Dong, Kelcey, and Spybrook (in press), Spybrook, Kelcey, and Dong (in press), Kelcey, Dong, Spybrook, and Cox (2017), and Kelcey, Dong, Spybrook, and Shen (in press).

For reference intraclass correlation (`rho2`, `rho3`) values see Dong, Reinke, Herman, Bradshaw, and Murray (2016), Hedberg and Hedges (2014), Hedges and Hedberg (2007, 2013), Kelcey, and Phelps (2013), Schochet (2008), Spybrook, Westine, and Taylor (2016). For reference variance (`R12`, `R22`, `R32`) values see Bloom, Richburg-Hayes, and Black (2007), Deke et al. (2010), Dong et al. (2016), Hedges and Hedberg (2013), Kelcey, and Phelps (2013), Spybrook, Westine, and Taylor (2016), Westine, Spybrook, and Taylor (2013). Users can also obtain design parameters for various levels using publicly available state or district data.

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mdes.bcra3f2

*MDES Calculator for Three-Level Fixed Effects Blocked Cluster Random Assignment Design, Treatment at Level-2***Description**

mdes.bcra3f2 calculates minimum detectable effect size (MDES) for designs with three-levels where level-2 units are randomly assigned to treatment and control groups within level-3 units (fixed blocks).

Usage

```
mdes.bcra3f2(power=.80, alpha=.05, two.tail=TRUE,
             rho2, P=.50, g2=0, R12=0, R22=0,
             n, J, K, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
P	average proportion of level-2 units randomly assigned to treatment within level-3 units.
g2	number of covariates at level-2.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.bcra3f2](#), [optimal.bcra3f2](#)

Examples

```
## Not run:

mdes.bcra3f2(rho2=.10, n=20,
             J=44, K=5)

## End(Not run)
```

mdes.bcra3r2

*MDES Calculator for Three-Level Random Effects Blocked Cluster
Random Assignment Designs, Treatment at Level-2*

Description

mdes.bcra3r2 calculates minimum detectable effect size (MDES) for designs with three-levels where level-2 units are randomly assigned to treatment and control groups within level-3 units (random blocks).

Usage

```
mdes.bcra3r2(power=.80, alpha=.05, two.tail=TRUE,
             rho2, rho3, omega3,
             P=.50, g3=0, R12=0, R22=0, RT32=0,
             n, J, K, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
P	average proportion of level-2 units randomly assigned to treatment within level-3 units.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.bcra3r2](#), [optimal.bcra3r2](#)

Examples

```
## Not run:

mdes.bcra3r2(rho3=.13, rho2=.10, omega3=.40,
             n=10, J=6, K=24)

## End(Not run)
```

mdes.bcra4f3

MDES Calculator for Four-Level Fixed Effects Blocked Cluster Random Assignment Designs, Treatment at Level-3

Description

mdes.bcra4f3 calculates minimum detectable effect size (MDES) for designs with four-levels where level-3 units are randomly assigned to treatment and control groups within level-4 units (fixed blocks).

Usage

```
mdes.bcra4f3(power=.80, alpha=.05, two.tail=TRUE,
             rho2, rho3,
             P=.50, R12=0, R22=0, R32=0, g3=0,
             n, J, K, L, ...)
```

Arguments

power	statistical power $(1 - \beta)$.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	average proportion of level-3 units randomly assigned to treatment within level-4 units.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.

R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.bcra4f3](#), [optimal.bcra4f3](#)

Examples

```
## Not run:

mdes.bcra4f3(rho3=.15, rho2=.15,
             n=10, J=4, K=4, L=15)

## End(Not run)
```

mdes.bcra4r2	<i>MDES Calculator for Four-Level Random Effects Block Random Assignment Designs, Treatment at Level-2</i>
--------------	--

Description

mdes.bcra4r2 calculates minimum detectable effect size (MDES) for designs with four-levels where level-2 units are randomly assigned to treatment and control groups within level-3 units (random blocks).

Usage

```
mdes.bcra4r2(power=.80, alpha=.05, two.tail=TRUE,
             rho2, rho3, rho4, omega3, omega4,
             P=.50, R12=0, R22=0, RT32=0, RT42=0, g4=0,
             n, J, K, L, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
omega4	treatment effect heterogeneity as ratio of treatment effect variance among level-4 units to the residual variance at level-4.
P	average proportion of level-2 units randomly assigned to treatment within level-3 units.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
RT42	proportion of treatment effect variance among level-4 units explained by level-4 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.bcra4r2](#), [optimal.bcra4r2](#)

Examples

```
## Not run:

mdes.bcra4r2(rho4=.05, rho3=.15, rho2=.15,
             omega4=.50, omega3=.50,
             n=10, J=4, L=27, K=4)

## End(Not run)
```

mdes.bcra4r3

*MDES Calculator for Four-Level Random Effects Blocked Cluster
Random Assignment Designs, Treatment at Level-3*

Description

mdes.bcra4r3 calculates minimum detectable effect size (MDES) for designs with four-levels where level-3 units are randomly assigned to treatment and control groups within level-4 units (random blocks).

Usage

```
mdes.bcra4r3(power=.80, alpha=.05, two.tail=TRUE,
             rho2, rho3, rho4, omega4,
             P=.50, R12=0, R22=0, R32=0, RT42=0, g4=0,
             n, J, K, L, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
omega4	treatment effect heterogeneity as ratio of treatment effect variance among level-4 units to the residual variance at level-4.
P	average proportion of level-3 units randomly assigned to treatment within level-4 units.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
RT42	proportion of treatment effect variance among level-4 units explained by level-4 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and 95% lower and upper confidence limits.

See Also

[power.bcra4r3](#), [optimal.bcra4r3](#)

Examples

```
## Not run:

mdes.bcra4r3(rho4=.05, rho3=.15, rho2=.15,
             omega4=.50,
             n=10, J=4, L=27, K=4)

## End(Not run)
```

mdes.bira2c1	<i>MDES Calculator for Two-Level Constant Effects Blocked Individual Random Assignment Designs, Treatment at Level-1</i>
--------------	--

Description

mdes.bira2c1 calculates minimum detectable effect size (MDES) for designs with two-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (school intercepts only).

Usage

```
mdes.bira2c1(power=.80, alpha=.05, two.tail=TRUE,
             P=.50, g1=0, R12=0,
             n, J, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g1	number of covariates at level-1.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.bira2c1](#), [optimal.bira2c1](#)

Examples

```
## Not run:

mdes.bira2c1(n=55, J=3)

## End(Not run)
```

mdes.bira2f1	<i>MDES Calculator for Two-Level Fixed Effects Blocked Individual Random Assignment Designs, Treatment at Level-1</i>
--------------	---

Description

mdes.bira2f1 calculates minimum detectable effect size (MDES) for designs with two-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (fixed blocks).

Usage

```
mdes.bira2f1(power=.80, alpha=.05, two.tail=TRUE,
             P=.50, g1=0, R12=0,
             n, J, ...)
```

Arguments

power	statistical power $(1 - \beta)$.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g1	number of covariates at level-1.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.bira2f1](#), [optimal.bira2f1](#)

Examples

```
## Not run:

mdes.bira2f1(n=55, J=3)

## End(Not run)
```

mdes.bira2r1	<i>MDES Calculator for Two-Level Random Effects Blocked Individual Random Assignment Designs, Individuals Randomized within Blocks</i>
--------------	--

Description

mdes.bira2r1 calculates minimum detectable effect size (MDES) for designs with two-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (random blocks).

Usage

```
mdes.bira2r1(power=.80, alpha=.05, two.tail=TRUE,
             rho2, omega2,
             P=.50, g2=0, R12=0, RT22=0,
             n, J, ...)
```

Arguments

power	statistical power $(1 - \beta)$.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
omega2	treatment effect heterogeneity as ratio of treatment effect variance among level-2 units to the residual variance at level-2.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g2	number of covariates at level-2.

R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of treatment effect variance among level-2 units explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.bira2r1](#), [optimal.bira2r1](#)

Examples

```
## Not run:

mdes.bira2r1(rho2=.35, omega2=.10,
             n=83, J=480)

## End(Not run)
```

mdes.bira3r1	<i>MDES Calculator for Three-Level Random Effects Blocked Individual Random Assignment Design, Individuals Randomized within Blocks</i>
--------------	---

Description

mdes.bira3r1 calculates minimum detectable effect size (MDES) for designs with three-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (random blocks).

Usage

```
mdes.bira3r1(power=.80, alpha=.05, two.tail=TRUE,
             rho2, rho3, omega2, omega3,
             P=.50, R12=0, RT22=0, RT32=0, g3=0,
             n, J, K, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega2	treatment effect heterogeneity as ratio of treatment effect variance among level-2 units to the residual variance at level-2.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of treatment effect variance among level-2 units explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.bira3r1](#), [optimal.bira3r1](#)

Examples

```
## Not run:

mdes.bira3r1(rho3=.20, rho2=.15, omega3=.10, omega2=.10,
             n=69, J=10, K=100)

## End(Not run)
```


mdes.bira4r1

MDES Calculator for Four-Level Random Effects Blocked Individual Random Assignment Design, Individuals Randomized within Blocks

Description

mdes.bira4r1 calculates minimum detectable effect size (MDES) for designs with four-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (random blocks).

Usage

```
mdes.bira4r1(power=.80, alpha=.05, two.tail=TRUE,
             rho2, rho3, rho4, omega2, omega3, omega4,
             P=.50, R12=0, RT22=0, RT32=0, RT42=0, g4=0,
             n, J, K, L, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
omega2	treatment effect heterogeneity as ratio of treatment effect variance among level-2 units to the residual variance at level-2.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
omega4	treatment effect heterogeneity as ratio of treatment effect variance among level-4 units to the residual variance at level-4.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of treatment effect variance among level-2 units explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
RT42	proportion of treatment effect variance among level-4 units explained by level-4 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.bira4r1](#), [optimal.bira4r1](#)

Examples

```
## Not run:

mdes.bira4r1(rho4=.05, rho3=.15, rho2=.15,
             omega4=.50, omega3=.50, omega2=.50,
             n=10, J=4, L=27, K=4)

## End(Not run)
```

mdes.cra2r2	<i>MDES Calculator for Main Effect in Two-Level Cluster Random Assignment Design, Treatment at Level-2</i>
-------------	--

Description

mdes.cra2r2 calculates minimum detectable effect size (MDES) for main effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups.

Usage

```
mdes.cra2r2(power=.80, alpha=.05, two.tail=TRUE,
            rho2,
            P=.50, g2=0, R12=0, R22=0,
            n, J, ...)
```

Arguments

power	statistical power $(1 - \beta)$.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
g2	number of covariates at level-2.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.cra2r2](#), [optimal.cra2r2](#)

Examples

```
## Not run:

mdes.cra2r2(rho2=.20,
            n=4, J=20)

## End(Not run)
```

mdes.cra3r3

MDES Calculator for Main Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3

Description

mdes.cra3r3 calculates minimum detectable effect size (MDES) for main effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups.

Usage

```
mdes.cra3r3(power=.80, alpha=.05, two.tail=TRUE,
            rho2, rho3, P=.50, g3=0, R12=0, R22=0, R32=0,
            n, J, K, ...)
```

Arguments

power	statistical power $(1 - \beta)$.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.

n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.cra3r3](#), [optimal.cra3r3](#)

Examples

```
## Not run:

mdes.cra3r3(rho3=.13, rho2=.10, omega3=.40,
            n=10, J=6, K=24)

## End(Not run)
```

mdes.cra4r4

MDES Calculator for Four-Level Cluster Random Assignment Designs, Treatment at Level-4

Description

mdes.cra4r4 calculates minimum detectable effect size (MDES) for designs with four-levels where level-4 units are randomly assigned to treatment and control groups.

Usage

```
mdes.cra4r4(power=.80, alpha=.05, two.tail=TRUE,
            rho2, rho3, rho4,
            P=.50, R12=0, R22=0, R32=0, R42=0, g4=0,
            n, J, K, L, ...)
```

Arguments

power	statistical power $(1 - \beta)$.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.

rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
P	proportion of level-4 units randomly assigned to treatment.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
R42	proportion of level-4 variance in the outcome explained by level-4 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.cra4r4](#), [optimal.cra4r4](#)

Examples

```
## Not run:

mdes.cra4r4(rho4=.05, rho3=.05, rho2=.10,
            n=10, J=2, K=3, L=20)

## End(Not run)
```

mdes.ira1r1	<i>MDES Calculator for Individual Random Assignment Designs, Completely Randomized Controlled Trials</i>
-------------	--

Description

mdes.ira1r1 calculates minimum detectable effect size (MDES) for completely randomized controlled trials where individuals are randomly assigned to treatment or control groups.

Usage

```
mdes.ira1r1(power=.80, alpha=.05, two.tail=TRUE,
            P=.50, g1=0, R12=0,
            n, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
P	proportion of units randomly assigned to treatment.
g1	number of covariates.
R12	proportion of variance in the outcome explained by covariates.
n	sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.ira1r1](#), [optimal.ira1r1](#)

Examples

```
## Not run:

mdes.ira1r1(n=55)

## End(Not run)
```

mdes.mod1n.cra2r2	<i>MDES Calculator for Non-Randomly Varying Moderator Effect in Two-Level Cluster Random Assignment Design, Treatment at Level-2, Moderator at Level-1</i>
-------------------	--

Description

mdes.mod1n.cra2r2 calculates minimum detectable effect size (MDES) for non-randomly varying moderator effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups and moderator is at level-1.

Usage

```
mdes.mod1n.cra2r2(power=.80, alpha=.05, two.tail=TRUE,
  rho2, P=.50, Q=NULL, g1=0, R12=0,
  n, J, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.mod1n.cra2r2](#), [optimal.mod1n.cra2r2](#)

Examples

```
## Not run:

mdes.mod1n.cra2r2(rho2=.20,
                  n=4, J=20)

## End(Not run)
```

mdes.mod1n.cra3r3	<i>MDES Calculator for Non-Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Design, Treatment at Level-3, Moderator at Level-1</i>
-------------------	--

Description

`mdes.mod1n.cra3r3` calculates minimum detectable effect size (MDES) for non-randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-1.

Usage

```
mdes.mod1n.cra3r3(power=.80, alpha=.05, two.tail=TRUE,
                  rho2, rho3, P=.50, Q=NULL, g1=0, R12=0,
                  n, J, K, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.mod1n.cra3r3](#), [optimal.mod1n.cra3r3](#)

Examples

```
## Not run:

mdes.mod1n.cra3r3(rho3=.13, rho2=.10, omega3=.40,
                  n=10, J=6, K=24)

## End(Not run)
```

mdes.mod1r.cra2r2	<i>MDES Calculator for Randomly Varying Moderator Effect in Two-Level Cluster Random Assignment Design, Treatment at Level-2, Moderator at Level-1</i>
-------------------	--

Description

mdes.mod1r.cra2r2 calculates minimum detectable effect size (MDES) for randomly varying moderator effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups and moderator is at level-1.

Usage

```
mdes.mod1r.cra2r2(power=.80, alpha=.05, two.tail=TRUE,
                  rho2, omega2, RT22=0, P=.50, Q=NULL, g1=0, R12=0,
                  n, J, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
omega2	moderator effect heterogeneity (unconditional) across level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of level-2 variance in the moderator effect explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.mod1r.cra2r2](#), [optimal.mod1r.cra2r2](#)

Examples

```
## Not run:

mdes.mod1r.cra2r2(rho2=.2, omega2=.2, RT22=.2, n=4, J=20)

## End(Not run)
```

mdes.mod1r.cra3r3	<i>MDES Calculator for Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3, Moderator at Level-1</i>
-------------------	---

Description

mdes.mod1r.cra3r3 calculates minimum detectable effect size (MDES) for randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-1.

Usage

```
mdes.mod1r.cra3r3(power=.80, alpha=.05, two.tail=TRUE,
                  rho2, rho3, omega2, omega3, P=.50, Q=NULL,
                  g1=0, R12=0, RT22=0, RT32=0,
                  n, J, K, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega2	moderator effect heterogeneity (unconditional) across level-2 units.
omega3	moderator effect heterogeneity (unconditional) across level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of level-2 variance in the moderator effect explained by level-2 covariates.
RT32	proportion of level-3 variance in the moderator effect explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.mod1r.cra3r3](#), [optimal.mod1r.cra3r3](#)

Examples

```
## Not run:

mdes.mod1r.cra3r3(rho3=.05, rho2=.12, omega2=.08, omega3=.07,
                  P=.4, Q=.7, g1=1, R12=.20, RT22=0, RT32=0,
                  n=20, J=4, K=60)

## End(Not run)
```

mdes.mod2.cra2r2	<i>MDES Calculator for Moderator Effect in Two-Level Cluster Random Assignment Design, Treatment and Moderator at Level-2</i>
------------------	---

Description

mdes.mod2.cra2r2 calculates minimum detectable effect size (MDES) for moderator effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups and moderator is at level-2.

Usage

```
mdes.mod2.cra2r2(power=.80, alpha=.05, two.tail=TRUE,
                  rho2, P=.50, Q=NULL, g2=0, R12=0, R22=0,
                  n, J, ...)
```

Arguments

power	statistical power $(1 - \beta)$.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g2	number of covariates at level-2 excluding moderator.

R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.mod2.cra2r2](#), [optimal.mod2.cra2r2](#)

Examples

```
## Not run:  
  
mdes.mod2.cra2r2(rho2=.20, n=4, J=20, Q=.5)  
  
## End(Not run)
```

mdes.mod2n.cra3r3	<i>MDES Calculator for Non-Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Design, Treatment at Level-3, Moderator at Level-2</i>
-------------------	--

Description

mdes.mod2n.cra3r3 calculates minimum detectable effect size (MDES) for non-randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-2.

Usage

```
mdes.mod2n.cra3r3(power=.80, alpha=.05, two.tail=TRUE,  
                  rho2, rho3, P=.50, Q=NULL, g2=0, R12=0, R22=0,  
                  n, J, K, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g2	number of covariates at level-2 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.mod2n.cra3r3](#), [optimal.mod2n.cra3r3](#)

Examples

```
## Not run:

mdes.mod2n.cra3r3(rho3=.10, rho2=.10, Q=.5, g2=1,
                  R12=.30, R22=.40, n=20, J=4, K=60)

## End(Not run)
```

mdes.mod2r.cra3r3	<i>MDES Calculator for Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3, Moderator at Level-2</i>
-------------------	---

Description

mdes.mod2r.cra3r3 calculates minimum detectable effect size (MDES) for randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-2.

Usage

```
mdes.mod2r.cra3r3(power=.80, alpha=.05, two.tail=TRUE,
                  rho2, rho3, omega3, P=.50, Q=NULL, g2=0, R12=0, R22=0, RT32=0,
                  n, J, K, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega3	moderator effect heterogeneity (unconditional) across level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g2	number of covariates at level-2 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
RT32	proportion of level-3 variance in the moderator effect explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.mod2r.cra3r3](#), [optimal.mod2r.cra3r3](#)

Examples

```
## Not run:

mdes.mod2r.cra3r3(rho3=.10, rho2=.10, omega3=.05, Q=.5, g2=1,
                  R12=.30, R22=.40, RT32=0, n=20, J=4, K=60)

## End(Not run)
```

mdes.mod3.cra3r3

MDES Calculator for Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment and Moderator at Level-3

Description

mdes.mod3.cra3r3 calculates minimum detectable effect size (MDES) for moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-3.

Usage

```
mdes.mod3.cra3r3(power=.80, alpha=.05, two.tail=TRUE,
                  rho2, rho3, P=.50, Q=NULL, g3=0, R12=0, R22=0, R32=0,
                  n, J, K, ...)
```

Arguments

power	statistical power ($1 - \beta$).
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g3	number of covariates at level-3 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in MDES calculation.
ncp	noncentrality parameter.
mdes	minimum detectable effect size and $(1 - \alpha)\%$ lower and upper confidence limits.

See Also

[power.mod3.cra3r3](#), [optimal.mod3.cra3r3](#)

Examples

```
## Not run:

mdes.mod3.cra3r3(rho3=.1, rho2=.1, omega3=.05, Q=.5,
                 g3=1, R12=.3, R22=.4, R32=.5, n=20, J=4, K=60)

## End(Not run)
```

mdes.to.pctl	<i>MDES to Percentiles</i>
--------------	----------------------------

Description

mdes.to.pctl converts MDES values returned from mdes function into percentile values.

Usage

```
mdes.to.pctl(x)
```

Arguments

x	an object returned from mdes function or a numeric value in standard deviation units.
---	---

Details

mdes.to.pctl converts MDES values returned from mdes function into percentile values. Values should be interpreted as percentile increase with reference to 50th percentile.

See Also

[optimal.to.mdes](#)

Examples

```
## Not run:

# MDES values returned from mdes function
design1 <- mdes.cra3r3(power=.80, rho2=.06, rho3=.18,
                     g3=1, R12=.55, R22=.50, R32=.45,
                     P=.40, n=10, J=2, K=83)
# convert MDES values into percentiles
percentiles <- mdes.to.pctl(design1)

## End(Not run)
```

mdes.to.power	<i>MDES to power</i>
---------------	----------------------

Description

mdes.to.power converts an object returned from mdes function into an object returned from power function.

Usage

```
mdes.to.power(x)
```

Arguments

x an object returned from one of the mdes functions.

Details

mdes.to.power converts an object returned from mdes function into an object returned from power function by passing parameters through power function.

See Also

[optimal.to.mdes](#), [power.to.mdes](#)

Examples

```
## Not run:

# object returned from power function
design1 <- mdes.bira2r1(rho2=.35, omega2=.10, n=83, J=10)
# convert the object into an object returned from mdes function
design2 <- mdes.to.power(design1)

## End(Not run)
```

optimal.bcra3f2

COSA Solver for Main Effect in Three-Level Fixed Effects Blocked Cluster Random Assignment Designs, Treatment at Level-2

Description

optimal.bcra3f2 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with three-levels where level-2 units are randomly assigned to treatment and control groups within level-3 units (fixed blocks). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bcra3f2(cn=0, cJ=0, cK=0, cost=NULL, n=NULL, J=NULL, K=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJK0=c(10,10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho2,
               P=.50, g2=0, R12=0, R22=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJK0	vector with a length of three to specify starting values for level-1, level-2, and level-3 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.

P	average proportion of level-2 units randomly assigned to treatment within level-3 units.
g2	number of covariates at level-2.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bcra3f2](#), [power.bcra3f2](#)

Examples

```
## Not run:

    optimal.bcra3f2(cn=1, cJ=10, cK=100, cost=5600,
                   constrain="cost",
                   rho2=.10)

## End(Not run)
```

optimal.bcra3r2	<i>COSA Solver for Main Effect in Three-Level Random Effects Blocked Cluster Random Assignment Designs, Treatment at Level-2</i>
-----------------	--

Description

optimal.bcra3r2 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with three-levels where level-2 units are randomly assigned to treatment and control groups within level-3 units (random blocks). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bcra3r2(cn=0, cJ=0, cK=0, cost=NULL, n=NULL, J=NULL, K=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJK0=c(10,10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho2, rho3, omega3,
               P=.50, g3=0, R12=0, R22=0, RT32=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJK0	vector with a length of three to specify starting values for level-1, level-2, and level-3 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
P	average proportion of level-2 units randomly assigned to treatment within level-3 units.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bcra3r2](#), [power.bcra3r2](#)

Examples

```
## Not run:

optimal.bcra3r2(cn=1, cJ=10, cK=100, cost=5600,
               constrain="cost",
               rho3=.13, rho2=.10, omega3=.40)

## End(Not run)
```

optimal.bcra4f3	<i>COSA Solver for Main Effect in Four-Level Fixed Effects Blocked Cluster Random Assignment Designs, Treatment at Level-3</i>
-----------------	--

Description

optimal.bcra4f3 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with four-levels where level-3 units are randomly assigned to treatment and control groups within level-4 units (fixed blocks). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bcra4f3(cn=0, cJ=0, cK=0, cL=0, cost=NULL,
               n=NULL, J=NULL, K=NULL, L=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJKL=c(10,10,10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho3, rho2,
               P=.50, g3=0, R32=0, R22=0, R12=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cL	marginal cost per level-4 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
power	statistical power (1 - type II error).

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJKL0	vector with a length of four to specify starting values for level-1, level-2, level-3, and level-4 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	average proportion of level-3 units randomly assigned to treatment within level-4 units.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bcra4f3](#), [power.bcra4f3](#)

Examples

```
## Not run:

  optimal.bcra4f3(cn=1, cJ=10, cK=100, cL=1000, cost=75600,
                 constrain="cost",
                 rho3=.15, rho2=.20)

## End(Not run)
```

optimal.bcra4r2	<i>COSA Solver for Main Effect in Four-Level Random Effects Block Random Assignment Designs, Treatment at Level-2</i>
-----------------	---

Description

optimal.bcra4r2 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with four-levels where level-2 units are randomly assigned to treatment and control groups within level-3 units (random blocks). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bcra4r2(cn=0, cJ=0, cK=0, cL=0, cost=NULL,
               n=NULL, J=NULL, K=NULL, L=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJKL0=c(10,10,10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho4, rho3, rho2, omega4, omega3,
               P=.50, g4=0, RT42=0, RT32=0, R22=0, R12=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cL	marginal cost per level-4 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJKL0	vector with a length of four to specify starting values for level-1, level-2, level-3, and level-4 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".

optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
omega4	treatment effect heterogeneity as ratio of treatment effect variance among level-4 units to the residual variance at level-4.
P	average proportion of level-2 units randomly assigned to treatment within level-3 units.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
RT42	proportion of treatment effect variance among level-4 units explained by level-4 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bcra4r2](#), [power.bcra4r2](#)

Examples

```
## Not run:

  optimal.bcra4r2(cn=1, cJ=10, cK=100, cL=1000, cost=75600,
    constrain="cost",
    rho4=.10, rho3=.15, rho2=.20,
    omega4=.50, omega3=.50)

## End(Not run)
```


optimal.bcra4r3

COSA Solver for Main Effect in Four-Level Random Effects Blocked Cluster Random Assignment Designs, Treatment at Level-3

Description

optimal.bcra4r3 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with four-levels where level-3 units are randomly assigned to treatment and control groups within level-4 units (random blocks). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bcra4r3(cn=0, cJ=0, cK=0, cL=0, cost=NULL,
               n=NULL, J=NULL, K=NULL, L=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJKL0=c(10,10,10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho4, rho3, rho2, omega4,
               P=.50, g4=0, RT42=0, R32=0, R22=0, R12=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cL	marginal cost per level-4 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJKL0	vector with a length of four to specify starting values for level-1, level-2, level-3, and level-4 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".

optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
omega4	treatment effect heterogeneity as ratio of treatment effect variance among level-4 units to the residual variance at level-4.
P	average proportion of level-3 units randomly assigned to treatment within level-4 units.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
RT42	proportion of treatment effect variance among level-4 units explained by level-4 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bcra4r3](#), [power.bcra4r3](#)

Examples

```
## Not run:

  optimal.bcra4r3(cn=1, cJ=10, cK=100, cL=1000, cost=75600,
                 constrain="cost",
                 rho4=.10, rho3=.15, rho2=.20,
                 omega4=.50)

## End(Not run)
```

optimal.bira2c1	<i>COSA Solver for Main Effect in Two-Level Constant Effects Blocked Individual Random Assignment Designs, Treatment at Level-2</i>
-----------------	---

Description

optimal.bira2c1 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with two-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (school intercepts only). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bira2c1(cn=0, cJ=0, cost=NULL, n=NULL, J=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJ0=c(10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               P=.50, g1=0, R12=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJ0	vector with a length of two to specify starting values for level-1 and level-2 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g1	number of covariates at level-1.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bira2c1](#), [power.bira2c1](#)

Examples

```
## Not run:

  optimal.bira2c1(cn=1, cJ=10, cost=560,
                 constrain="cost")

## End(Not run)
```

optimal.bira2f1	<i>COSA Solver for Main Effect in Two-Level Fixed Effects Blocked Individual Random Assignment Designs, Treatment at Level-1</i>
-----------------	--

Description

optimal.bira2f1 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with two-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (fixed blocks). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bira2f1(cn=0, cJ=0, cost=NULL, n=NULL, J=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJ0=c(10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               P=.50, g1=0, R12=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJ0	vector with a length of four to specify starting values for level-1 and level-2 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g1	number of covariates at level-1.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bira2f1](#), [power.bira2f1](#)

Examples

```
## Not run:

    optimal.bira2f1(cn=1, cJ=10, cost=560,
                   constrain="cost")

## End(Not run)
```

optimal.bira2r1	<i>COSA Solver for Main Effect in Two-Level Random Effects Blocked Individual Random Assignment Designs, Individuals Randomized within Blocks</i>
-----------------	---

Description

optimal.bira2r1 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with two-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (random blocks). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bira2r1(cn=0, cJ=0, cost=NULL, n=NULL, J=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJ0=c(10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho2, omega2,
               P=.50, g2=0, R12=0, RT22=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJ0	vector with a length of two to specify starting values for level-1 and level-2 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
omega2	treatment effect heterogeneity as ratio of treatment effect variance among level-2 units to the residual variance at level-2.

P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g2	number of covariates at level-2.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of treatment effect variance among level-2 units explained by level-2 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bira2r1](#), [power.bira2r1](#)

Examples

```
## Not run:

    optimal.bira2r1(cn=1, cJ=10, cost=560,
                   constrain="cost", rho2=.20, omega2=.50)

## End(Not run)
```

optimal.bira3r1	<i>COSA Solver for Main Effect in Three-Level Random Effects Blocked Individual Random Assignment Design, Individuals Randomized within Blocks</i>
-----------------	--

Description

optimal.bira3r1 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with three-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (random blocks). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bira3r1(cn=0, cJ=0, cK=0, cost=NULL, n=NULL, J=NULL, K=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJK0=c(10,10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho2, rho3, omega2, omega3,
               P=.50, g3=0, R12=0, RT22=0, RT32=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJK0	vector with a length of three to specify starting values for level-1, level-2, and level-3 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega2	treatment effect heterogeneity as ratio of treatment effect variance among level-2 units to the residual variance at level-2.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of treatment effect variance among level-2 units explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bira3r1](#), [power.bira3r1](#)

Examples

```
## Not run:

optimal.bira3r1(cn=1, cJ=10, cK=100, cost=5600,
               constrain="cost",
               rho3=.20, rho2=.15, omega3=.10, omega2=.10)

## End(Not run)
```

optimal.bira4r1	<i>COSA Solver for Main Effect in Four-Level Random Effects Blocked Individual Random Assignment Design, Individuals Randomized within Blocks</i>
-----------------	---

Description

optimal.bira4r1 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with four-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (random blocks). COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.bira4r1(cn=0, cJ=0, cK=0, cL=0, cost=NULL,
               n=NULL, J=NULL, K=NULL, L=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJKL0=c(10,10,10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho4, rho3, rho2, omega4, omega3, omega2,
               P=.50, g4=0, RT42=0, RT32=0, RT22=0, R12=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cL	marginal cost per level-4 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJKL0	vector with a length of four to specify starting values for level-1, level-2, level-3, and level-4 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
omega2	treatment effect heterogeneity as ratio of treatment effect variance among level-2 units to the residual variance at level-2.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
omega4	treatment effect heterogeneity as ratio of treatment effect variance among level-4 units to the residual variance at level-4.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of treatment effect variance among level-2 units explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
RT42	proportion of treatment effect variance among level-4 units explained by level-4 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.bira4r1](#), [power.bira4r1](#)

Examples

```
## Not run:

    optimal.bira4r1(cn=1, cJ=10, cK=100, cL=1000, cost=75600,
                    constrain="cost",
                    rho4=.10, rho3=.15, rho2=.20,
                    omega4=.50, omega3=.50, omega2=.50)

## End(Not run)
```

optimal.cra2r2	<i>COSA Solver for Main Effect in Two-Level Cluster Random Assignment Design, Treatment at Level-2</i>
----------------	--

Description

optimal.cra2r2 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.cra2r2(cn=0, cJ=0, cost=NULL, n=NULL, J=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJ0=c(10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho2, P=.50, g2=0, R12=0, R22=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJ0	vector with a length of two to specify starting values for level-1 and level-2 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
g2	number of covariates at level-2.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.cra2r2](#), [power.cra2r2](#)

Examples

```
## Not run:

  optimal.cra2r2(cn=1, cJ=10, cost=560,
               constrain="cost", rho2=.20)

## End(Not run)
```

optimal.cra3r3

*COSA Solver for Main Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3***Description**

optimal.cra3r3 finds constrained optimal sample allocation (COSA) solutions for main effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.cra3r3(cn=0, cJ=0, cK=0, cost=NULL,
               n=NULL, J=NULL, K=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJK0=c(10,10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho2, rho3,
               P=.50, g3=0, R12=0, R22=0, R32=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJK0	vector with a length of three to specify starting values for level-1, level-2, and level-3 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.

rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.cra3r3](#), [power.cra3r3](#)

Examples

```
## Not run:

    optimal.cra3r3(cn=1, cJ=10, cK=100, cost=5600,
                  constrain="cost",
                  rho3=.06, rho2=.17)

## End(Not run)
```

<code>optimal.cra4r4</code>	<i>COSA Solver for Main Effect in Four-Level Cluster Random Assignment Designs, Treatment at Level-4</i>
-----------------------------	--

Description

`optimal.cra4r4` finds constrained optimal sample allocation (COSA) solutions for main effect in designs with four-levels where level-4 units are randomly assigned to treatment and control groups. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.cra4r4(cn=0, cJ=0, cK=0, cL=0, cost=NULL,
               n=NULL, J=NULL, K=NULL, L=NULL,
               power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
               nJKL0=c(10,10,10,10), ncase=10, gm=2,
               constrain="power", optimizer="auglag_cobyla",
               rho4, rho3, rho2,
               P=.50, g4=0, R42=0, R32=0, R22=0, R12=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cL	marginal cost per level-4 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJKL0	vector with a length of four to specify starting values for level-1, level-2, level-3, and level-4 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDSE. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
P	proportion of level-4 units randomly assigned to treatment.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
R42	proportion of level-4 variance in the outcome explained by level-4 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.cra4r4](#), [power.cra4r4](#)

Examples

```
## Not run:

optimal.cra4r4(cn=1, cJ=10, cK=100, cL=1000, cost=75600,
               constrain="cost",
               rho4=.05, rho3=.05, rho2=.10)

## End(Not run)
```

optimal.ira1r1	<i>Sample Size Calculator for Main Effect in Individual Random Assignment Designs, Completely Randomized Controlled Trials</i>
----------------	--

Description

optimal.ira1r1 calculates minimum required sample size for main effect in completely randomized controlled trials where individuals are randomly assigned to treatment or control groups.

Usage

```
optimal.ira1r1(mdes=.25, power=.80, alpha=.05, two.tail=TRUE,
               n0=10, tol=.10,
               P=.50, g1=0, R12=0)
```

Arguments

power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
n0	starting value for sample size.
tol	tolerance.

P	average proportion of units randomly assigned to treatment.
g1	number of covariates.
R12	proportion of variance in the outcome explained by covariates.

Value

fun	function name.
parms	list of parameters used in the function.
n	sample size.

See Also

[mdes.ira1r1](#), [power.ira1r1](#)

Examples

```
## Not run:

    optimal.ira1r1(R12=.50)

## End(Not run)
```

optimal.mod1n.cra2r2	<i>COSA Solver for Non-randomly Varying Moderator Effect in Two-Level Cluster Random Assignment Design, Treatment at level-2 and Moderator at Level-1</i>
----------------------	---

Description

optimal.mod1n.cra2r2 finds constrained optimal sample allocation (COSA) solutions for non-randomly varying moderator effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups and moderator is at level-1. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.mod1n.cra2r2(cn=0, cJ=0, cost=NULL, n=NULL, J=NULL,
    power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
    nJ0=c(10,10), ncase=10, gm=2,
    constrain="power", optimizer="auglag_coby1a",
    rho2, P=.50, Q=NULL, g1=0, R12=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJ0	vector with a length of two to specify starting values for level-1 and level-2 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.mod1n.cra2r2](#), [power.mod1n.cra2r2](#)

Examples

```
## Not run:

    optimal.mod1n.cra2r2(cn=1, cJ=10, cost=560,
                        constrain="cost", rho2=.20)

## End(Not run)
```

optimal.mod1n.cra3r3	<i>COSA Solver for Non-randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3 and Moderator at Level-1</i>
----------------------	--

Description

optimal.mod1n.cra3r3 finds constrained optimal sample allocation (COSA) solutions for non-randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-1. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.mod1n.cra3r3(cn=0, cJ=0, cK=0, cost=NULL,
                    n=NULL, J=NULL, K=NULL,
                    power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
                    nJK0=c(10,10,10), ncase=10, gm=2,
                    constrain="power", optimizer="auglag_cobyla",
                    rho2, rho3, P=.50, Q=NULL, g1=0, R12=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJK0	vector with a length of three to specify starting values for level-1, level-2, and level-3 sample sizes.

n case	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.mod1n.cra3r3](#), [power.mod1n.cra3r3](#)

Examples

```
## Not run:

optimal.mod1n.cra3r3(cn=1, cJ=10, cK=100, n=10, constrain="mdes",
                    rho2=.20, rho3=.10)

## End(Not run)
```

optimal.mod1r.cra2r2	<i>COSA Solver for Randomly Varying Moderator Effect in Two-Level Cluster Random Assignment Design, Treatment at level-2 and Moderator at Level-1</i>
----------------------	---

Description

optimal.mod1r.cra2r2 finds constrained optimal sample allocation (COSA) solutions for randomly varying moderator effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups and moderator is at level-1. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.mod1r.cra2r2(cn=0, cJ=0, cost=NULL, n=NULL, J=NULL,
  power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
  nJ0=c(10,10), ncase=10, gm=2,
  constrain="power", optimizer="auglag_cobyla",
  rho2, omega2, P=.50, Q=NULL, g1=0, R12=0, RT22=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJ0	vector with a length of two to specify starting values for level-1 and level-2 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
omega2	moderator effect heterogeneity (unconditional) across level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of level-2 variance in the moderator effect explained by level-2 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.mod1r.cra2r2](#), [power.mod1r.cra2r2](#)

Examples

```
## Not run:

optimal.mod1r.cra2r2(cn=1, cJ=10, cost=560,
                    constrain="cost", rho2=.20, omega=.20)

## End(Not run)
```

optimal.mod1r.cra3r3	<i>COSA Solver for Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3 and Moderator at Level-1</i>
----------------------	--

Description

optimal.mod1r.cra3r3 finds constrained optimal sample allocation (COSA) solutions for randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-1. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.mod1r.cra3r3(cn=0, cJ=0, cK=0, cost=NULL,
                    n=NULL, J=NULL, K=NULL,
                    power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
                    nJK0=c(10,10,10), ncase=10, gm=2,
                    constrain="power", optimizer="auglag_cobyla",
                    rho2, rho3, omega2, omega3, P=.50, Q=NULL,
                    g1=0, R12=0, RT22=0, RT32=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJK0	vector with a length of three to specify starting values for level-1, level-2, and level-3 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega2	moderator effect heterogeneity (unconditional) across level-2 units.
omega3	moderator effect heterogeneity (unconditional) across level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of level-2 variance in the moderator effect explained by level-2 covariates.
RT32	proportion of level-3 variance in the moderator effect explained by level-3 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.mod1r.cra3r3](#), [power.mod1r.cra3r3](#)

Examples

```
## Not run:

optimal.mod1r.cra3r3(cn=1, cJ=10, cK=100, n=10, constrain="mdes",
                    rho2=.20, rho3=.10, omega2=.10, omega3=.10)

## End(Not run)
```

optimal.mod2.cra2r2	<i>COSA Solver for Moderator Effect in Two-Level Cluster Random Assignment Design, Treatment and Moderator at Level-2</i>
---------------------	---

Description

optimal.mod2.cra2r2 finds constrained optimal sample allocation (COSA) solutions for moderator effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups and moderator is at level-2. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.mod2.cra2r2(cn=0, cJ=0, cost=NULL, n=NULL, J=NULL,
                   power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
                   nJ0=c(10,10), ncase=10, gm=2,
                   constrain="power", optimizer="auglag_cobyla",
                   rho2, P=.50, Q=NULL, g2=0, R12=0, R22=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJ0	vector with a length of two to specify starting values for level-1 and level-2 sample sizes.

ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g2	number of covariates at level-2 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.mod2.cra2r2](#), [power.mod2.cra2r2](#)

Examples

```
## Not run:

optimal.mod2.cra2r2(cn=1, cJ=10, cost=560,
                    constrain="cost", rho2=.20)

## End(Not run)
```

optimal.mod2n.cra3r3	<i>COSA Solver for Non-Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3 and Moderator at Level-2</i>
----------------------	--

Description

optimal.mod2n.cra3r3 finds constrained optimal sample allocation (COSA) solutions for non-randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-2. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.mod2n.cra3r3(cn=0, cJ=0, cK=0, cost=NULL,
  n=NULL, J=NULL, K=NULL,
  power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
  nJK0=c(10,10,10), ncase=10, gm=2,
  constrain="power", optimizer="auglag_cobyla",
  rho2, rho3, P=.50, Q=NULL, g2=0, R12=0, R22=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJK0	vector with a length of three to specify starting values for level-1, level-2, and level-3 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g2	number of covariates at level-2 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.

round.optim solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

integer.optim best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.mod2n.cra3r3](#), [power.mod2n.cra3r3](#)

Examples

```
## Not run:

optimal.mod2n.cra3r3(cn=1, cJ=10, cK=100, n=10, constrain="mdes",
                    rho2=.20, rho3=.10)

## End(Not run)
```

optimal.mod2r.cra3r3	<i>COSA Solver for Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3 and Moderator at Level-2</i>
----------------------	--

Description

optimal.mod2r.cra3r3 finds constrained optimal sample allocation (COSA) solutions for randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-2. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.mod2r.cra3r3(cn=0, cJ=0, cK=0, cost=NULL,
                    n=NULL, J=NULL, K=NULL,
                    power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
                    nJK0=c(10,10,10), ncase=10, gm=2,
                    constrain="power", optimizer="auglag_cobyla",
                    rho2, rho3, omega3, P=.50, Q=NULL,
                    g2=0, R12=0, R22=0, RT32=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).

J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJK0	vector with a length of three to specify starting values for level-1, level-2, and level-3 sample sizes.
ncase	number of cases to show in the output.
gm	grid multiplier to increase the range of sample size search for each level.
constrain	one of the followings can be constrained at a specified cost or value: "cost", "power", or "mdes".
optimizer	algorithm to find optimal sample sizes given total cost, power, or MDES. Available algorithms: "auglag_cobyla", "auglag_lbfgs", "auglag_mma", or "auglag_slsqp".
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega3	moderator effect heterogeneity (unconditional) across level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g2	number of covariates at level-2 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
RT32	proportion of level-3 variance in the moderator effect explained by level-3 covariates.

Value

fun	function name.
parms	list of parameters used in the function.
nloptr	list of nloptr log and output.
round.optim	solution after rounding. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).
integer.optim	best integer solutions around round.optim solution. MDES is calculated at the specified power (default .80), and power is calculated at the specified MDES (default .25).

See Also

[mdes.mod2r.cra3r3](#), [power.mod2r.cra3r3](#)

Examples

```
## Not run:

optimal.mod2r.cra3r3(cn=1, cJ=10, cK=100, n=10, constrain="mdes",
                    rho2=.20, rho3=.10, omega3=.10)

## End(Not run)
```

optimal.mod3.cra3r3	<i>COSA Solver for Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment and Moderator at Level-3</i>
---------------------	--

Description

optimal.mod3.cra3r3 finds constrained optimal sample allocation (COSA) solutions for moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-3. COSA can be found in the following forms, (i) under budgetary constraints given marginal costs per unit, (ii) under power constraints given marginal costs per unit, (iii) under MDES constraints given marginal costs per unit, and (iv) under sample size constraints for one or more levels along with any of the i,ii, or iii options.

Usage

```
optimal.mod3.cra3r3(cn=0, cJ=0, cK=0, cost=NULL,
                   n=NULL, J=NULL, K=NULL,
                   power=.80, mdes=.25, alpha=.05, two.tail=TRUE,
                   nJK0=c(10,10,10), ncase=10, gm=2,
                   constrain="power", optimizer="auglag_cobyla",
                   rho2, rho3, P=.50, Q=NULL,
                   g3=0, R12=0, R22=0, R32=0)
```

Arguments

cn	marginal cost per level-1 unit.
cJ	marginal cost per level-2 unit.
cK	marginal cost per level-3 unit.
cost	total cost or budget.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
power	statistical power (1 - type II error).
mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
nJK0	vector with a length of three to specify starting values for level-1, level-2, and level-3 sample sizes.

optimal.to.mdes	<i>Optimal to MDES</i>
-----------------	------------------------

Description

optimal.to.mdes converts an object returned from optimal function into an object returned from mdes function.

Usage

```
optimal.to.mdes(x)
```

Arguments

x an object returned from one of the optimal functions.

Details

optimal.to.mdes converts an object returned from optimal function into an object returned from mdes function by passing parameters through mdes function.

See Also

[optimal.to.power](#)

Examples

```
## Not run:

# object returned from optimal function
design1 <- optimal.bira2r1(cn=1, cJ=10, cost=560,
                        constrain="cost", rho2=.20, omega2=.50)
# convert the object into an object returned from mdes function
design2 <- optimal.to.mdes(design1)

## End(Not run)
```

optimal.to.power	<i>Optimal to Power</i>
------------------	-------------------------

Description

optimal.to.power converts an object returned from optimal function into an object returned from power function.

Usage

```
optimal.to.power(x)
```

Arguments

x an object returned from one of the optimal functions.

Details

optimal.to.power converts an object returned from optimal function into an object returned from power function by passing parameters through power function.

See Also

[optimal.to.mdes](#)

Examples

```
## Not run:

# object returned from optimal function
design1 <- optimal.bira2r1(cn=1, cJ=10, cost=560,
                        constrain="cost", rho2=.20, omega2=.50)
# convert the object into an object returned from power function
design2 <- optimal.to.power(design1)

## End(Not run)
```

power.bcra3f2	<i>Statistical Power Calculator for Three-Level Fixed Effects Blocked Cluster Random Assignment Design, Treatment at Level-2</i>
---------------	--

Description

power.bcra3f2 calculates statistical power for designs with three-levels where level-2 units are randomly assigned to treatment and control groups within level-3 units (fixed blocks).

Usage

```
power.bcra3f2(mdes=.25, alpha=.05, two.tail=TRUE,
              rho2,
              P=.50, g2=0, R12=0, R22=0,
              n, J, K, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
P	average proportion of level-2 units randomly assigned to treatment within level-3 units.
g2	number of covariates at level-2.

R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.bcra3f2](#), [optimal.bcra3f2](#)

Examples

```
## Not run:

power.bcra3f2(rho2=.10,
              n=20, J=44, K=5)

## End(Not run)
```

power.bcra3r2	<i>Statistical Power Calculator for Three-Level Random Effects Blocked Cluster Random Assignment Designs, Treatment at Level-2</i>
---------------	--

Description

power.bcra3r2 calculates statistical power for designs with three-levels where level-2 units are randomly assigned to treatment and control groups within level-3 units (random blocks).

Usage

```
power.bcra3r2(mdes=.25, alpha=.05, two.tail=TRUE,
              rho2, rho3, omega3,
              P=.50, g3=0, R12=0, R22=0, RT32=0,
              n, J, K, ...)
```

Arguments

mde	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
P	average proportion of level-2 units randomly assigned to treatment within level-3 units.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.bcra3r2](#), [optimal.bcra3r2](#)

Examples

```
## Not run:

power.bcra3r2(rho3=.13, rho2=.10, omega3=.40,
              n=10, J=6, K=24)

## End(Not run)
```

power.bcra4f3	<i>Statistical Power Calculator for Four-Level Fixed Effects Blocked Cluster Random Assignment Designs, Treatment at Level-3</i>
---------------	--

Description

power.bcra4f3 calculates statistical power for designs with four-levels where level-3 units are randomly assigned to treatment and control groups within level-4 units (fixed blocks).

Usage

```
power.bcra4f3(mdes=.25, alpha=.05, two.tail=TRUE,
              rho2, rho3,
              P=.50, R12=0, R22=0, R32=0, g3=0,
              n, J, K, L, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	average proportion of level-3 units randomly assigned to treatment within level-4 units.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.bcra4f3](#), [optimal.bcra4f3](#)

Examples

```
## Not run:

power.bcra4f3(rho3=.15, rho2=.15,
              n=10, J=4, K=4, L=15)

## End(Not run)
```

power.bcra4r2	<i>Statistical Power Calculator for Four-Level Random Effects Block Random Assignment Designs, Treatment at Level-2</i>
---------------	---

Description

power.bcra4r2 calculates statistical power for designs with four-levels where level-2 units are randomly assigned to treatment and control groups within level-3 units (random blocks).

Usage

```
power.bcra4r2(mdes=.25, alpha=.05, two.tail=TRUE,
              rho2, rho3, rho4, omega3, omega4,
              P=.50, R12=0, R22=0, RT32=0, RT42=0, g4=0,
              n, J, K, L, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
omega4	treatment effect heterogeneity as ratio of treatment effect variance among level-4 units to the residual variance at level-4.
P	average proportion of level-2 units randomly assigned to treatment within level-3 units.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
RT42	proportion of treatment effect variance among level-4 units explained by level-4 covariates.

n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.bcra4r2](#), [optimal.bcra4r2](#)

Examples

```
## Not run:

power.bcra4r2(rho4=.05, rho3=.15, rho2=.15,
              omega4=.50, omega3=.50,
              n=10, J=4, L=27, K=4)

## End(Not run)
```

power.bcra4r3	<i>Statistical Power Calculator for Four-Level Random Effects Blocked Cluster Random Assignment Designs, Treatment at Level-3</i>
---------------	---

Description

power.bcra4r3 calculates statistical power for designs with four-levels where level-3 units are randomly assigned to treatment and control groups within level-4 units (random blocks).

Usage

```
power.bcra4r3(mdes=.25, alpha=.05, two.tail=TRUE,
              rho2, rho3, rho4, omega4,
              P=.50, R12=0, R22=0, R32=0, RT42=0, g4=0,
              n, J, K, L, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
omega4	treatment effect heterogeneity as ratio of treatment effect variance among level-4 units to the residual variance at level-4.
P	average proportion of level-3 units randomly assigned to treatment within level-4 units.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
RT42	proportion of treatment effect variance among level-4 units explained by level-4 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power $(1 - \beta)$.

See Also

[mdes.bcra4r3](#), [optimal.bcra4r3](#)

Examples

```
## Not run:

power.bcra4r3(rho4=.05, rho3=.15, rho2=.15,
              omega4=.50,
              n=10, J=4, L=27, K=4)

## End(Not run)
```

power.bira2c1	<i>Statistical Power Calculator for Two-Level Constant Effects Blocked Individual Random Assignment Designs, Treatment at Level-1</i>
---------------	---

Description

power.bira2c1 calculates statistical power for designs with two-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (school intercepts only).

Usage

```
power.bira2c1(mdes=.25, alpha=.05, two.tail=TRUE,
              P=.50, g1=0, R12=0,
              n, J, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g1	number of covariates at level-1.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.bira2c1](#), [optimal.bira2c1](#)

Examples

```
## Not run:

power.bira2c1(n=55, J=3)

## End(Not run)
```

power.bira2f1	<i>Statistical Power Calculator for Two-Level Fixed Effects Blocked Individual Random Assignment Designs, Treatment at Level-1</i>
---------------	--

Description

power.bira2f1 calculates statistical power for designs with two-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (fixed blocks).

Usage

```
power.bira2f1(mdes=.25, alpha=.05, two.tail=TRUE,
              P=.50, g1=0, R12=0,
              n, J, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g1	number of covariates at level-1.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.bira2f1](#), [optimal.bira2f1](#)

Examples

```
## Not run:

power.bira2f1(n=55, J=3)

## End(Not run)
```

power.bira2r1	<i>Statistical Power Calculator for Two-Level Random Effects Blocked Individual Random Assignment Designs, Individuals Randomized within Blocks</i>
---------------	---

Description

power.bira2r1 calculates statistical power for designs with two-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (random blocks).

Usage

```
power.bira2r1(mdes=.25, alpha=.05, two.tail=TRUE,
              rho2, omega2,
              g2=0, P=.50, R12=0, RT22=0,
              n, J, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
omega2	treatment effect heterogeneity as ratio of treatment effect variance among level-2 units to the residual variance at level-2.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g2	number of covariates at level-2.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of treatment effect variance among level-2 units explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.bira2r1](#), [optimal.bira2r1](#)

Examples

```
## Not run:

power.bira2r1(rho2=.35, omega2=.10,
              n=83, J=480)

## End(Not run)
```

power.bira3r1	<i>Statistical Power Calculator for Three-Level Random Effects Blocked Individual Random Assignment Design, Individuals Randomized within Blocks</i>
---------------	--

Description

power.bira3r1 calculates statistical power for designs with three-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (random blocks).

Usage

```
power.bira3r1(mdes=.25, alpha=.05, two.tail=TRUE,
              rho2, rho3, omega2, omega3,
              P=.50, R12=0, RT22=0, RT32=0, g3=0,
              n, J, K, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega2	treatment effect heterogeneity as ratio of treatment effect variance among level-2 units to the residual variance at level-2.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of treatment effect variance among level-2 units explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).

J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.bira3r1](#), [optimal.bira3r1](#)

Examples

```
## Not run:

power.bira3r1(rho3=.20, rho2=.15, omega3=.10, omega2=.10,
              n=69, J=10, K=100)

## End(Not run)
```

power.bira4r1	<i>Statistical Power Calculator for Four-Level Random Effects Blocked Individual Random Assignment Design, Individuals Randomized within Blocks</i>
---------------	---

Description

power.bira4r1 calculates statistical power for designs with four-levels where level-1 units are randomly assigned to treatment and control groups within level-2 units (random blocks).

Usage

```
power.bira4r1(mdes=.25, alpha=.05, two.tail=TRUE,
              rho2, rho3, rho4, omega2, omega3, omega4,
              P=.50, R12=0, RT22=0, RT32=0, RT42=0, g4=0,
              n, J, K, L, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.

rho4	proportion of variance in the outcome explained by level-4 units.
omega2	treatment effect heterogeneity as ratio of treatment effect variance among level-2 units to the residual variance at level-2.
omega3	treatment effect heterogeneity as ratio of treatment effect variance among level-3 units to the residual variance at level-3.
omega4	treatment effect heterogeneity as ratio of treatment effect variance among level-4 units to the residual variance at level-4.
P	average proportion of level-1 units randomly assigned to treatment within level-2 units.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of treatment effect variance among level-2 units explained by level-2 covariates.
RT32	proportion of treatment effect variance among level-3 units explained by level-3 covariates.
RT42	proportion of treatment effect variance among level-4 units explained by level-4 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.bira4r1](#), [optimal.bira4r1](#)

Examples

```
## Not run:

power.bira4r1(rho4=.05, rho3=.15, rho2=.15,
              omega4=.50, omega3=.50, omega2=.50,
              n=10, J=4, L=27, K=4)

## End(Not run)
```

power.cra2r2	<i>Statistical Power Calculator for Main Effect in Two-Level Cluster Random Assignment Design, Treatment at Level-2</i>
--------------	---

Description

power.cra2r2 calculates statistical power for main effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups.

Usage

```
power.cra2r2(mdes=.25, alpha=.05, two.tail=TRUE,
             rho2, g2=0, P=.50, R12=0, R22=0,
             n, J, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
g2	number of covariates at level-2.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.cra2r2](#), [optimal.cra2r2](#)

Examples

```
## Not run:

power.cra2r2(rho2=.20,
             n=4, J=20)

## End(Not run)
```

power.cra3r3	<i>Statistical Power Calculator for Main Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3</i>
--------------	--

Description

power.cra3r3 calculates statistical power for main effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups.

Usage

```
power.cra3r3(mdes=.25, alpha=.05, two.tail=TRUE,
             rho2, rho3,
             P=.50, g3=0, R12=0, R22=0, R32=0,
             n, J, K, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
g3	number of covariates at level-3.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.cra3r3](#), [optimal.cra3r3](#)

Examples

```
## Not run:

power.cra3r3(rho3=.06, rho2=.17,
             n=15, J=3, K=60)

## End(Not run)
```

power.cra4r4	<i>Statistical Power Calculator for Four-Level Cluster Random Assignment Designs, Treatment at Level-4</i>
--------------	--

Description

power.cra4r4 calculates statistical power for designs with four-levels where level-4 units are randomly assigned to treatment and control groups.

Usage

```
power.cra4r4(mdes=.25, alpha=.05, two.tail=TRUE,
             rho2, rho3, rho4,
             P=.50, R12=0, R22=0, R32=0, R42=0, g4=0,
             n, J, K, L, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
rho4	proportion of variance in the outcome explained by level-4 units.
P	proportion of level-4 units randomly assigned to treatment.
g4	number of covariates at level-4.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.

R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
R42	proportion of level-4 variance in the outcome explained by level-4 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	harmonic mean of level-3 units across level-4 units (or simple average).
L	number of level-4 units.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.cra4r4](#), [optimal.cra4r4](#)

Examples

```
## Not run:

power.cra4r4(rho4=.05, rho3=.05, rho2=.10,
             n=10, J=2, K=3, L=20)

## End(Not run)
```

power.ira1r1	<i>Statistical Power Calculator for Individual Random Assignment Designs, Completely Randomized Controlled Trials</i>
--------------	---

Description

power.ira1r1 calculates statistical power for completely randomized controlled trials where individuals are randomly assigned to treatment or control groups.

Usage

```
power.ira1r1(mdes=.25, alpha=.05, two.tail=TRUE,
             P=.50, g1=0, R12=0,
             n, ...)
```


Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
P	proportion of units randomly assigned to treatment.
g1	number of covariates.
R12	proportion of variance in the outcome explained by covariates.
n	sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.ira1r1](#), [optimal.ira1r1](#)

Examples

```
## Not run:

power.ira1r1(n=55)

## End(Not run)
```

power.mod1n.cra2r2	<i>Statistical Power Calculator for for Non-Randomly Varying Moderator Effect in Two-Level Cluster Random Assignment Design, Treatment at Level-2, Moderator at Level-1</i>
--------------------	---

Description

power.mod1n.cra2r2 calculates statistical power for non-randomly varying moderator effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups and moderator is at level-1.

Usage

```
power.mod1n.cra2r2(mdes=.25, alpha=.05, two.tail=TRUE,
  rho2, P=.50, Q=NULL, g1=0, R12=0,
  n, J, ...)
```

Arguments

mde	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.mod1n.cra2r2](#), [optimal.mod1n.cra2r2](#)

Examples

```
## Not run:

power.mod1n.cra2r2(rho2=.20,
                   n=4, J=20)

## End(Not run)
```

power.mod1n.cra3r3	<i>Statistical Power Calculator for Non-Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Design, Treatment at Level-3, Moderator at Level-1</i>
--------------------	---

Description

power.mod1n.cra3r3 calculates statistical power for non-randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-1.

Usage

```
power.mod1n.cra3r3(mdes=.25, alpha=.05, two.tail=TRUE,
                   rho2, rho3, P=.50, Q=NULL, g1=0, R12=0,
                   n, J, K, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.mod1n.cra3r3](#), [optimal.mod1n.cra3r3](#)

Examples

```
## Not run:

power.mod1n.cra3r3(rho3=.06, rho2=.17,
                   n=15, J=3, K=60)

## End(Not run)
```

power.mod1r.cra2r2	<i>Statistical Power Calculator for Randomly Varying Moderator Effect in Two-Level Cluster Random Assignment Design, Treatment at Level-2, Moderator at Level-1</i>
--------------------	---

Description

power.mod1r.cra2r2 calculates statistical power for randomly varying moderator effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups and moderator is at level-1.

Usage

```
power.mod1r.cra2r2(mdes=.25, alpha=.05, two.tail=TRUE,
                   rho2, omega2, RT22=0, P=.50, Q=NULL, g1=0, R12=0,
                   n, J, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
omega2	moderator effect heterogeneity (unconditional) across level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of level-2 variance in the moderator effect explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.mod1r.cra2r2](#), [optimal.mod1r.cra2r2](#)

Examples

```
## Not run:

power.mod1r.cra2r2(rho2=.2, omega2=.2, RT22=.2, n=4, J=20)

## End(Not run)
```

power.mod1r.cra3r3	<i>Statistical Power Calculator for Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3, Moderator at Level-1</i>
--------------------	--

Description

power.mod1r.cra3r3 calculates statistical power for randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-1.

Usage

```
power.mod1r.cra3r3(mdes=.25, alpha=.05, two.tail=TRUE,
                   rho2, rho3, omega2, omega3, P=.50, Q=NULL,
                   g1=0, R12=0, RT22=0, RT32=0,
                   n, J, K, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega2	moderator effect heterogeneity (unconditional) across level-2 units.
omega3	moderator effect heterogeneity (unconditional) across level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g1	number of covariates at level-1 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
RT22	proportion of level-2 variance in the moderator effect explained by level-2 co-variates.
RT32	proportion of level-3 variance in the moderator effect explained by level-3 co-variates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.mod1r.cra3r3](#), [optimal.mod1r.cra3r3](#)

Examples

```
## Not run:

power.mod1r.cra3r3(rho3=.05, rho2=.12, omega2=.08, omega3=.07,
                  P=.4, Q=.7, g1=1, R12=.20, RT22=0, RT32=0,
                  n=20, J=4, K=60)

## End(Not run)
```

power.mod2.cra2r2	<i>Statistical Power Calculator for Moderator Effect in Two-Level Cluster Random Assignment Design, Treatment and Moderator at Level-2</i>
-------------------	--

Description

power.mod2.cra2r2 calculates statistical power for moderator effect in designs with two-levels where level-2 units are randomly assigned to treatment and control groups and moderator is at level-2.

Usage

```
power.mod2.cra2r2(mdes=.25, alpha=.05, two.tail=TRUE,
                  rho2, P=.50, Q=NULL, g2=0, R12=0, R22=0,
                  n, J, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
P	proportion of level-2 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g2	number of covariates at level-2 excluding moderator.

R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	level-2 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.mod2.cra2r2](#), [optimal.mod2.cra2r2](#)

Examples

```
## Not run:

power.mod2.cra2r2(rho2=.20, n=4, J=20, Q=.5)

## End(Not run)
```

power.mod2n.cra3r3	<i>Statistical Power Calculator for Non-Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Design, Treatment at Level-3, Moderator at Level-2</i>
--------------------	---

Description

power.mod2n.cra3r3 calculates statistical power for non-randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-2.

Usage

```
power.mod2n.cra3r3(mdes=.25, alpha=.05, two.tail=TRUE,
                   rho2, rho3, P=.50, Q=NULL, g2=0, R12=0, R22=0,
                   n, J, K, ...)
```

Arguments

<code>mdes</code>	minimum detectable effect size.
<code>alpha</code>	probability of type I error.
<code>two.tail</code>	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
<code>rho2</code>	proportion of variance in the outcome explained by level-2 units.
<code>rho3</code>	proportion of variance in the outcome explained by level-3 units.
<code>P</code>	proportion of level-3 units randomly assigned to treatment.
<code>Q</code>	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
<code>g2</code>	number of covariates at level-2 excluding moderator.
<code>R12</code>	proportion of level-1 variance in the outcome explained by level-1 covariates.
<code>R22</code>	proportion of level-2 variance in the outcome explained by level-2 covariates.
<code>n</code>	harmonic mean of level-1 units across level-2 units (or simple average).
<code>J</code>	harmonic mean of level-2 units across level-3 units (or simple average).
<code>K</code>	level-3 sample size.
<code>...</code>	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

<code>fun</code>	function name.
<code>parms</code>	list of parameters used in power calculation.
<code>ncp</code>	noncentrality parameter.
<code>power</code>	statistical power ($1 - \beta$).

See Also

[mdes.mod2n.cra3r3](#), [optimal.mod2n.cra3r3](#)

Examples

```
## Not run:

power.mod2n.cra3r3(rho3=.10, rho2=.10, Q=.5, g2=1,
                   R12=.30, R22=.40, n=20, J=4, K=60)

## End(Not run)
```

power.mod2r.cra3r3	<i>Statistical Power Calculator for Randomly Varying Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment at Level-3, Moderator at Level-2</i>
--------------------	--

Description

power.mod2r.cra3r3 calculates statistical power for randomly varying moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-2.

Usage

```
power.mod2r.cra3r3(mdes=.25, alpha=.05, two.tail=TRUE,
                   rho2, rho3, omega3, P=.50, Q=NULL, g2=0, R12=0, R22=0, RT32=0,
                   n, J, K, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
omega3	moderator effect heterogeneity (unconditional) across level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g2	number of covariates at level-2 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
RT32	proportion of level-3 variance in the moderator effect explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.mod2r.cra3r3](#), [optimal.mod2r.cra3r3](#)

Examples

```
## Not run:

power.mod2r.cra3r3(rho3=.10, rho2=.10, omega3=.05, Q=.5, g2=1,
                  R12=.30, R22=.40, RT32=0, n=20, J=4, K=60)

## End(Not run)
```

power.mod3.cra3r3

Statistical Power Calculator for Moderator Effect in Three-Level Cluster Random Assignment Designs, Treatment and Moderator at Level-3

Description

power.mod3.cra3r3 calculates statistical power for moderator effect in designs with three-levels where level-3 units are randomly assigned to treatment and control groups and moderator is at level-3.

Usage

```
power.mod3.cra3r3(mdes=.25, alpha=.05, two.tail=TRUE,
                  rho2, rho3, P=.50, Q=NULL, g3=0, R12=0, R22=0, R32=0,
                  n, J, K, ...)
```

Arguments

mdes	minimum detectable effect size.
alpha	probability of type I error.
two.tail	logical; TRUE for two-tailed hypothesis testing, FALSE for one-tailed hypothesis testing.
rho2	proportion of variance in the outcome explained by level-2 units.
rho3	proportion of variance in the outcome explained by level-3 units.
P	proportion of level-3 units randomly assigned to treatment.
Q	proportion of level-1 units within moderator subgroup. NULL implies continuous moderator.
g3	number of covariates at level-3 excluding moderator.
R12	proportion of level-1 variance in the outcome explained by level-1 covariates.
R22	proportion of level-2 variance in the outcome explained by level-2 covariates.
R32	proportion of level-3 variance in the outcome explained by level-3 covariates.
n	harmonic mean of level-1 units across level-2 units (or simple average).
J	harmonic mean of level-2 units across level-3 units (or simple average).
K	level-3 sample size.
...	to handle extra parameters passed from other functions, do not define any additional parameters.

Value

fun	function name.
parms	list of parameters used in power calculation.
ncp	noncentrality parameter.
power	statistical power ($1 - \beta$).

See Also

[mdes.mod3.cra3r3](#), [optimal.mod3.cra3r3](#)

Examples

```
## Not run:

power.mod3.cra3r3(rho3=.1, rho2=.1, omega3=.05, Q=.5,
                  g3=1, R12=.3, R22=.4, R32=.5, n=20, J=4, K=60)

## End(Not run)
```

power.to.mdes	<i>power to MDES</i>
---------------	----------------------

Description

power.to.mdes converts an object returned from power function into an object returned from mdes function.

Usage

```
power.to.mdes(x)
```

Arguments

x an object returned from one of the power functions.

Details

power.to.mdes converts an object returned from power function into an object returned from mdes function by passing parameters through mdes function.

See Also

[optimal.to.mdes](#)

Examples

```
## Not run:

# object returned from power function
design1 <- power.bira2r1(mdes=.15, rho2=.35, omega2=.10, n=83, J=10)
# convert the object into an object returned from mdes function
design2 <- power.to.mdes(design1)

## End(Not run)
```

PowerUpR-deprecated *Deprecated and Defunct functions in 'PowerUpR'*

Description

Deprecated functions are provided for compatibility purposes and will be defunct in the next 'PowerUpR' release. Defunct functions are no longer supported.

Format

Deprecated functions are no longer documented, please use documentation for new functions.

Details

Deprecated and defunct functions and their replacement are as follows:

- `mrss.ira1r1` is deprecated, use [optimal.ira1r1](#)
- `mrss.cra2r2` is deprecated, use [optimal.cra2r2](#)
- `mrss.cra3r3` is deprecated, use [optimal.cra3r3](#)
- `mrss.cra4r4` is deprecated, use [optimal.cra4r4](#)
- `mrss.bcra3f2` is deprecated, use [optimal.bcra3f2](#)
- `mrss.bcra3r2` is deprecated, use [optimal.bcra3r2](#)
- `mrss.bcra4r2` is deprecated, use [optimal.bcra4r2](#)
- `mrss.bcra4f3` is deprecated, use [optimal.bcra4f3](#)
- `mrss.bcra4r2` is deprecated, use [optimal.bcra4r2](#)
- `mrss.bira4r1` is deprecated, use [optimal.bira4r1](#)
- `mrss.bira3r1` is deprecated, use [optimal.bira3r1](#)
- `mrss.bira2c1` is deprecated, use [optimal.bira2c1](#)
- `mrss.bira2f1` is deprecated, use [optimal.bira2f1](#)
- `mrss.bira2r1` is deprecated, use [optimal.bira2r1](#)
- `mrss.to.mdes` is defunct, use [optimal.to.mdes](#)
- `mrss.to.power` is defunct, use [optimal.to.power](#)
- `t1t2.error` is defunct, there is no replacement function
- `plot.pars` is defunct, there is no replacement function

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