# Interpreting large quartet distances

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## 1 Properties of the quartet distance

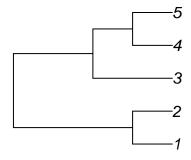
Properties of the quartet distance are explored fully in Steel (1993).

As quartet distances of 1 can only be accomplished for small trees (five or fewer tips), it is perhaps more appropriate to consider whether or not trees are more dissimilar than a pair of random trees, whose distance will be, on average, 2/3.

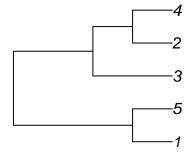
### 1.1 Minimum quartet distance

When there are six or more tips in a bifurcating tree, some quartets are necessarily shared between trees.

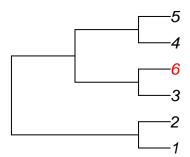
Consider the tree:



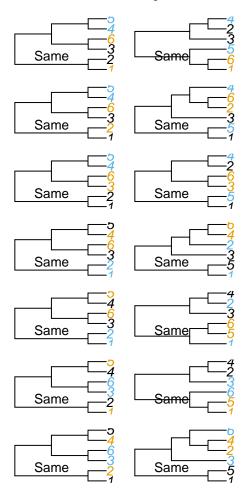
The only trees with no quartets in common with Tree A are symmetric with



Now create Tree C by adding a 6th tip as a sister to tip 3 on Tree A.



There's nowhere to add tip 6 to Tree B without creating a quartet that exists in Tree C.



### 1.2 Quartet distance in a pair of random trees

On average, 1/3 of the quartets resolved in a pair of random trees will match. This is because there are three quartets involving any set of four tips, each of which is equally likely to occur on a truly random tree.

The below code calculates the mean proportion of matching quartets for random trees with 4 to 20 tips, and the corresponding standard deviation.

#### References

Steel, M. A., & Penny, D. (1993). Distributions of tree comparison metrics—some new results. Systematic Biology, 42(2), 126-141. doi: 10.1093/sysbio/42.2.126