How to use RSGHB

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Abstract

This vignette describes the process for specifying, estimating and analyzing the output of a choice model with RSGHB. The document is structured into two case studies using different model structures. The synthetic choice data used in this document (as well as number of other examples using different model structures) can be downloaded from RSGHB github page - https://github.com/jeffdumont/RSGHB

RSGHB modeling file structure

The typical RSGHB model file has the following 4 main sections. We will walk through each of these 4 sections in the examples that follow.

- 1. Setup and data preparation
- 2. Setting the controls for model estimation
- 3. Defining the likelihood function
- 4. Calling the doHB function to start the estimation process

EXAMPLE 1: MNL Model with Fixed Parameters

In this section, the code for estimating a multinomial logit model with fixed (non-random) parameters is explained. In this example, synthetic respondents were presented with a choice between two travel alternatives - one that is toll free but slower and one that was priced but faster. Each respondent was presented with a panel of 8 choice tasks.

Setup and Data Preparation

- > library(RSGHB)
- > # load example data
- > data(choicedata)
- > # We typically work with one one row per choice observations. This isn't necessary however but it does lend > head(choicedata)

ID thecount tt1 tt2 tol12 asc1 Choice 1 8738 1 60 51 1.25 1 2 8738 2 60 51 0.75 1 3 8738 3 63 59 0.50 1 2 4 8738 60 0.75 1 1 5 2 5 8738 60 54 0.50 1 6 8738 6 63 54 0.75 1

- > # We can then specify any variables from the choicedata data.frame that you'd like to use in the
- > # utility equations in the likelihood function below. These can be any variables within the data or transfor
- > TT1 <- choicedata\$tt1
- > TT2 <- choicedata\$tt2

```
> TOLL2 <- choicedata$tol12
> # Here we specify the choice vectors. Note in this example there are only two alternatives. Also, dummying of
> choice1
            <- (choicedata$Choice==1)
            <- (choicedata$Choice==2)
> choice2
> # Frequency of choice for the first alternative
> table(choice1)
choice1
FALSE TRUE
3560 6682
> # Frequency of choice for the second alternative.
> table(choice2)
choice2
FALSE TRUE
6682 3560
```

Controling the Estimation Process

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There are number of options for controling the estimation process. Please see the help file for doHB or the final section of this document for more details. Note that a number of controls have default values and do not need to be directly specified if the default is acceptable.

```
> # ESTIMATION CONTROL
> # -----
> # Setting control list for estimation (see ?doHB for more estimation options)
> # modelname is used for naming the output files
> modelname <- "MNL"
> # gVarNamesFixed contains the names for the fixed (non-random) variables in your model. This will be used in
> gVarNamesFixed <- c("ASC1","BTime","BCost")</pre>
> # FC contains the starting values for the fixed coefficients.
> FC \leftarrow c(0,0,0)
> # ITERATION SETTINGS
> # gNCREP contains the number of iterations to use prior to convergence
> gNCREP
            <- 30000
> # gNEREP contains the number of iterations to keep for averaging after convergence has been reached
> gNEREP
            <- 20000
> # gNSKIP contains the number of iterations to do in between retaining draws for averaging
> # gINFOSKIP controls how frequently to print info about the iteration process
> gINFOSKIP <- 250
> # To simplify the doHB functional call, we put all of the control parameters into a single list that can be
> control <- list(</pre>
      modelname=modelname,
       gVarNamesFixed=gVarNamesFixed,
      FC=FC,
      gNCREP=gNCREP,
      gNEREP=gNEREP,
      gNSKIP=gNSKIP,
      gINFOSKIP=gINFOSKIP
```

Writing the likelihood function

RSGHB is expecting the user-specificed likelihood function to take the parameters fc and b (even if they are not used within the function calculate the likelihood). The fc parameter is a vector of fixed coefficients (they do not vary across individuals in your data). The b parameter is a matrix of individual coefficients which are generated from the random coefficients in the model. In this example, we only focus on the fc vector.

It is important to note that the computation of the likelihood is the most computational taxing part of the estimation process. So coding the likelihood efficiently is essential to reduce run time of the model.

```
> # likelihood
> # -----
> likelihood <- function(fc,b)
+ {
    # defining the parameters
    # using cc var to index the fc vector simplifies the addition/subtraction of new parameters
    cc <- 1
    ASC1 <- fc[cc];cc <- cc+1
    Btime <- fc[cc];cc <- cc+1</pre>
    Btoll <- fc[cc];cc <- cc+1</pre>
    # utility functions
    v1 <- ASC1
                     + Btime * TT1
    v2 <-
                       Btime * TT2 + Btoll * TOLL2
    # mnl probability statement
      \leftarrow (exp(v1)*choice1 + exp(v2)*choice2) / (exp(v1) + exp(v2))
    return(p)
```

Estimating the model

To start the model estimation process, the analyst needs to call the doHB function passing in the likelihood function, the choicedata data.frame and the control list.

```
doHB(likelihood, choicedata, control)
```

RSGHB will first perform a series of diagnostics on your model to catch common errors in model setup. In addition, it will provide you with some basice summary statistics on your choice data and model. Before estimation begins, RSGHB will present you with a confirmation prompt allowing you to cancel the model estimation.

During the estimation, current estimates of the markov chains will be plotted to the screen. This plot is updated based on the control parameter gINFOSKIP (see figure 1). In addition, it will provide numerical iteration details in the R Console.

Evaluating the output

There are two main output files for this particular model - log file and the $_F$ file. RSGHB comes with some basic tools for plotting the contents of these files.

The .log file contains some statistics that can be used to understand if model convergence has been reached. Because this model contains only fixed coefficients, the log file contains just the root likelihood (RLH) and log-likelihood at each iteration defined by qINFOSKIP - see figure 2.

The $_F$ file contains the set of fixed (non-random) coefficients for each iteration after convergence of the markov chain.

```
> data(Example1_F)
> head(Example1_F)
```

Figure 1: Plotting of the Markov Chains during estimation

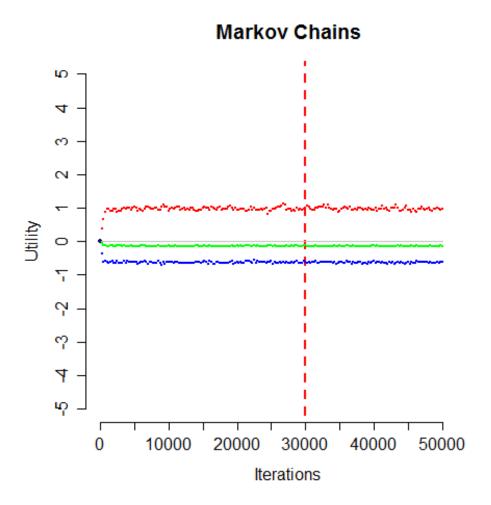
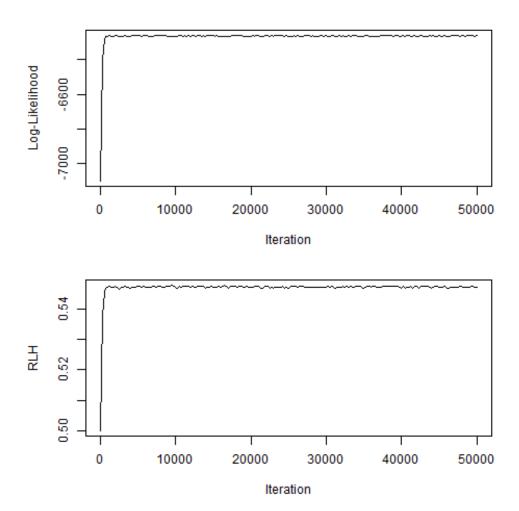


Figure 2: Plotting of the Log file



EXAMPLE 2: MNL Model with Random Coefficients

In this section, we expand on the model estimated in EXAMPLE 1 by allowing the coefficients to vary across the individuals in our dataset. This type of model is referred to by many names - Random Coefficients Logit, Random Parameters Logit or Mixed Logit.

Setup and Data Preparation

The setup and data preparation are very similar to the first model.

```
> library(RSGHB)
> # load example data
> data(choicedata)
> # We typically work with one one row per choice observations. This isn't necessary however but it does lend
> head(choicedata)
    ID thecount tt1 tt2 tol12 asc1 Choice
1 8738
             1 60 51 1.25
2 8738
              2 60 51 0.75
                                 1
3 8738
              3 63 59 0.50
                                 1
                                        2
4 8738
              4 60 54 0.75
                                 1
                                        1
              5
                                        2
5 8738
                60
                    54
                        0.50
                                 1
6 8738
              6
                63 54
                        0.75
> # We can then specify any variables from the choicedata data.frame that you'd like to use in the
> # utility equations in the likelihood function below. These can be any variables within the data or transfor
> TT1
          <- choicedata$tt1
> TT2
          <- choicedata$tt2
> TOLL2
         <- choicedata$to112</pre>
> # Here we specify the choice vectors. Note in this example there are only two examples. Also, dummying codin
> choice1
            <- (choicedata$Choice==1)
> choice2
             <- (choicedata$Choice==2)
> # Frequency of choice for the first alternative
> table(choice1)
choice1
FALSE TRUE
3560 6682
> # Frequency of choice for the second alternative.
> table(choice2)
choice2
FALSE TRUE
6682 3560
```

Controling the Estimation Process

To allow for mixing of the parameters, we need to specify a few more controls to pass into the doHB function.

```
> # ESTIMATION CONTROL
> # Setting control list for estimation (see ?doHB for more estimation options)
> # modelname is used for naming the output files
> modelname <- "MNL"
> # gVarNamesNormal provides names for the random parameters
> gVarNamesNormal <- c("ASC1","BTime","BCost")</pre>
> # gDIST specifies the type of continuous distribution to use for the random parameters. gDIST must have an e
> # The options are:
> # 1. normal
> # 2. log-nomal
> # 3. negative log-normal
> # 4. normal with all values below zero massed at zero
> # 5. Johnson SB with a specified min and max
> # In this example, we use normal distributions for all 3 of the parameters.
> gDIST <- c(1,1,1)
> # svN contains the starting values for the means of the normal distributions for each of the random parameter
> svN \leftarrow c(0,0,0)
> # ITERATION SETTINGS
> # gNCREP contains the number of iterations to use prior to convergence
> gNCREP
            <- 30000
> # gNEREP contains the number of iterations to keep for averaging after convergence has been reached
> # gNSKIP contains the number of iterations to do in between retaining draws for averaging
> gNSKIP
> # gINFOSKIP controls how frequently to print info about the iteration process
> gINFOSKIP <- 250
> # To simplify the doHB functional call, we put all of the control parameters into a single list that can be
> control <- list(</pre>
       modelname=modelname,
       gVarNamesNormal=gVarNamesNormal,
       gDIST=gDIST,
       svN=svN,
       gNCREP=gNCREP,
       gNEREP=gNEREP,
       gNSKIP=gNSKIP,
       gINFOSKIP=gINFOSKIP
+ )
```

Writing the likelihood function

To introduce mixing into the model, we switch from using fc vector to using the b matrix in the coding of the likelihood. The b matrix contains the individual conditionals for the sample-level random coefficients. The matrix b has one row per observation (an individual's coefficients are repeated across their choice observations automatically by RSGHB) and one column for each of the random parameters.

```
> likelihood <- function(fc,b)
+ {</pre>
```

Section 4: Estimating the model

Again, to start the model estimation process, the analyst needs to call the doHB function passing in the likelihood function, the choicedata data.frame and the control list.

```
doHB(likelihood, choicedata, control)
```

Evaluating the output

As in the first example, current estimates of the markov chains will be plotted to the screen - see figure 3. In this model, these represent the means of the underlying normals for the random parameters.

There are more output files for this model. RSGHB comes with some basic tools for plotting the contents of these files.

The .log file contains some statistics that can be used to understand if model convergence has been reached. Because this model includes random coefficients, the log file now contains the average variance and parameter root mean square (RMS) at each iteration - see figure 4.

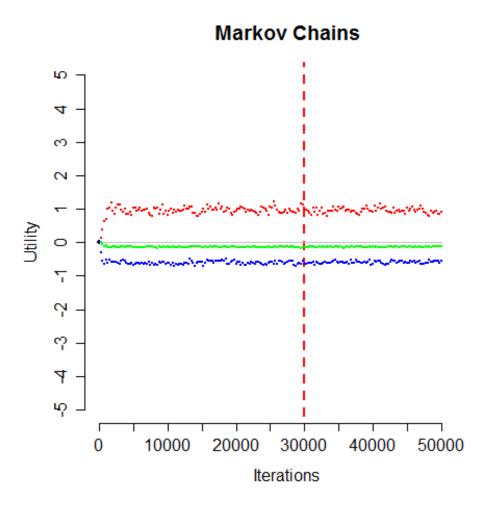
The _A file contain the sample-level means of the underlying normal at each iteration.

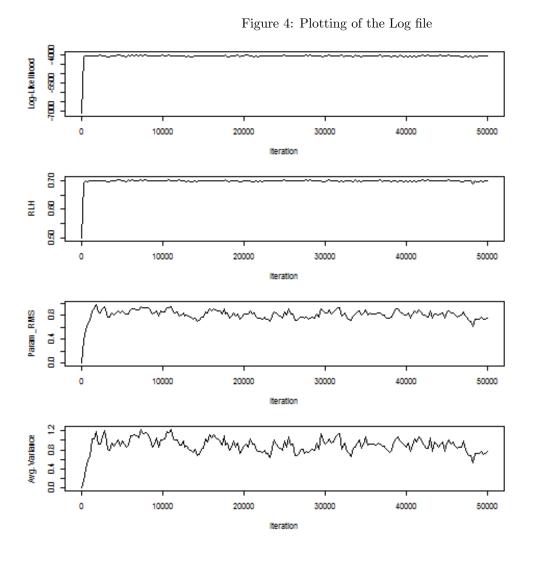
```
> data(Example2_A)
> head(Example2_A)
  iteration
                 ASC1
                           BTime
                                       BCost
          1 0.9502366 -0.1249110 -0.5975124
          2 0.9192204 -0.1345303 -0.6016621
2
3
          3 0.9334093 -0.1275589 -0.5894570
          4 0.9543322 -0.1385718 -0.5932009
4
          5 0.9487994 -0.1187152 -0.5894714
5
          6 0.9398888 -0.1178337 -0.5912138
6
```

The $_B$ file contains the average across iterations of the individual level draws for the underlying normals for the random parameters. The $_Bsd$ file provides the standard deviations of those individual draws.

```
> data(Example2_B)
> head(Example2_B)
  Respondent
                  ASC1
                             BTime
                                         BCost
        8738 1.2065722 -0.01700429 -0.6706683
2
        8740 1.1856822 -0.01574887 -0.5232470
3
        8741 0.7790173 -0.57719452 -0.4940480
4
        8742 1.1593141 -0.27220298 -0.6376389
        8744 0.5109336 -0.02024900 -0.5083203
5
        8745 1.0067985 -0.29565492 -0.5574964
6
```

Figure 3: Plotting of the Markov Chains during estimation





```
> data(Example2_Bsd)
> head(Example2_Bsd)
  Respondent
                  ASC1
                           BTime
                                      BCost
        8738 0.6500682 0.1615823 0.4068272
1
2
        8740 0.6821484 0.1692862 0.4069139
        8741 0.6917361 0.2080046 0.4230185
3
4
        8742 0.6380699 0.1567093 0.4001571
5
        8744 0.7008824 0.1650231 0.4296362
        8745 0.6259956 0.1675564 0.4018320
6
```

The $_C$ file contains the average across iterations of the individual level draws for the random parameters including the appropriate transformations. The $_C$ file also contains individual-specific measures of model fit (Root Likelihoods). The $_Csd$ file provides the standard deviations of those individual draws. These two files are equivalent to the conditional distributions from models estimated using Maximum Simulated Likelihood methods.

```
> data(Example2_C)
> head(Example2_C)
  Respondent
                   R.L.H
                             ASC1
                                        BTime
                                                   BCost
        8738 0.6762416 1.2065722 -0.01700429 -0.6706683
2
        8740 0.6325542 1.1856822 -0.01574887 -0.5232470
3
        8741 0.8420089 0.7790173 -0.57719452 -0.4940480
4
        8742 0.5145232 1.1593141 -0.27220298 -0.6376389
        8744 0.4780804 0.5109336 -0.02024900 -0.5083203
5
6
        8745 0.4919669 1.0067985 -0.29565492 -0.5574964
> data(Example2_Csd)
> head(Example2_Csd)
  Respondent
                  ASC1
                            BTime
                                      BCost
        8738 0.6500682 0.1615823 0.4068272
1
2
        8740 0.6821484 0.1692862 0.4069139
3
        8741 0.6917361 0.2080046 0.4230185
4
        8742 0.6380699 0.1567093 0.4001571
5
        8744 0.7008824 0.1650231 0.4296362
6
        8745 0.6259956 0.1675564 0.4018320
```

> data(Example2_D)

The $_D$ file contains a row-based representation of the sample covariance for each iteration. Note the use below of the xpnd function to convert to a matrix representation of the sample covariance.

```
> head(Example2_D)
  iteration
                 ASC1 ASC1xBTime ASC1xBCost
                                                      BTime BTimexBCost
                                                                             BCost
          1 0.1995635 -0.02084866 0.06611205 -0.012268437 0.03470861 0.1829551
          2 0.2068453 -0.02099142 0.06574671 -0.005313839
                                                             0.03062937 0.1854261
3
          3 0.2206137 -0.01672801 0.06778255 -0.000827184
                                                             0.03580280 0.1872543
4
          4 0.2135790 -0.02085852 0.06905407 0.005535069
                                                             0.03119758 0.1801005
5
          5 0.2376300 -0.01937409 0.06593123 -0.005413533
                                                             0.02932449 0.1752125
          6 0.2234180 -0.02707077 0.07340550 -0.012843845 0.03041234 0.1790798
> # building the covariance matrix
> covMat <- xpnd(colMeans(Example2_D[-1]))</pre>
> rownames(covMat) <- c("ASC1", "BTime", "BCost")</pre>
> colnames(covMat) <- c("ASC1", "BTime", "BCost")</pre>
> covMat
```

```
ASC1 BTime BCost
ASC1 0.44636341 -0.06659140 -0.05475239
BTime -0.06659140 0.07915122 0.03122776
BCost -0.05475239 0.03122776 0.17247616
```

RSGHB Control Parameters

Here is a list of the user-specified control parameters.

gVarNamesNormal - A vector of charater-based names for the random parameters.

Default: NULL

gVarNamesFixed - A vector of character-based names for the fixed parameters.

Default: NULL

gDIST - A vector of integers (1-5) which indicate which type of distribution should be applied to the random coefficients - 1 = Normal, 2 = Postive Log-Normal, 3 = Negative Log-Normal, 4 = Censored Normal, 5 = Johnson SB. There should be an element for each name in gVarNamesNormal. Default: NULL.

FC - A vector of starting values for the fixed coefficients. There should be an element for each name in gVarNamesFixed.

Default: NULL

svN - A vector of starting values for the means of the underlying normals for the random parameters. There should be an element for each name in gVarNamesNormal.

Default: NULL

 ${\bf gNCREP}\,$ - Number of burn-in iterations to use prior to convergence.

Default: 100000

gNEREP - Number of iterations to keep for averaging after convergence has been reached.

Default: 100000

 ${\bf gNSKIP}\,$ - Number of iterations in between retaining draws for averaging.

Default: 1

gINFOSKIP - Number of iterations in between printing/saving information about the iteration process.

Default: 250

modelname - The model name which is used for creating output files.

Default: paste("HBModel",round(runif(1)*10000000,0),sep=""))

gSIGDIG - The number of significant digits for reporting purposes.

Default: 10

 ${\bf priorVariance}\,$ - The amount of prior variance assumed.

Default: 2.0

degreesOfFreedom - Additional degrees of freedom for the prior covariance matrix (not including the number of parameters.

Default: 5

rho - The initial proportionality fraction for the jumping distribution for the Metropolis-Hastings algorithm for the random parameters. This fraction is adjusted by the program after each iteration to attain an acceptance rate of about 0.3.

Default: 0.1

rhoF - The proportionality fraction for the jumping distribution for the Metropolis-Hastings algorithm for the fixed parameters. Unlike rho, this value is not adjusted as the markov chain proceeds. Default: 0.0001

gFULLCV - A number that indicates if a full or independent covariance structure should be used for the random parameters. A value of 1 indicated full and 0 for an independent structure. Default: 1

gMINCOEF - A vector of minimums for the Johnson SB distributions. If Johnson SB is used, each random parameter needs an element but only the elements that correspond to a 5 in gDIST are used.

Default: 0

gMAXCOEF - Like gMINCOEF but for the maximum of the Johnson SB distribution.

Default: 0

gStoreDraws - A boolean value to store the draws for the individual level coefficients.

Default: F

 $\mathbf{gSeed}\,$ - The random seed.

Default: 0

constraintsNorm - This is a list of monotonic constraints to be applied during estimation. The structure of the constraints is c(param1number - inequality - param2number). For constraints relative to 0, use 0 instead of the param2number. For the inequality, use 1 for < and 2 for >. Example

constraintsNorm <- list(c(5,1,0),c(6,1,5),c(7,1,6),c(8,1,7))

would constrain the 5th parameter < 0, the 6th parameter < 5th parameter, the 7th parameter < the 6th parameter, etc.

Default: NULL

nodiagnostics - If set to TRUE, the diagnostic report will not be reported to the screen with a prompt to continue. This makes batch processing easier to implement.

Default: FALSE