SKAT Package

Seunggeun (Shawn) Lee

January 15, 2023

1 Overview

SKAT package has functions to 1) test for associations between SNP sets and continuous/binary phenotypes with adjusting for covariates and kinships and 2) to compute power/sample size for future studies.

2 Association test

An example dataset (SKAT.example) has a genotype matrix (Z) of 2000 individuals and 67 SNPs, vectors of continuous (y.c) and binary (y.b) phenotypes, and a covariates matrix (X).

```
> library(SKAT)
> data(SKAT.example)
> names(SKAT.example)

[1] "Z" "X" "y.c" "y.b"
> attach(SKAT.example)
```

To test for associations, SKAT_Null_Model function should be used in prior to run SKAT to estimate parameters under the null model of no associations.

```
> # continuous trait
> obj<-SKAT_Null_Model(y.c ~ X, out_type="C")
> out.c<-SKAT(Z, obj)
> out.c$p.value

[1] 0.002877041

> # dichotomous trait
> obj<-SKAT_Null_Model(y.b ~ X, out_type="D")
> out.b<-SKAT(Z, obj)
> out.b$p.value

[1] 0.1401991
```

The returned object from SKAT has many information, such as number of markers in Z and number of markers to be used for the test. The version 2.1.0 has test.snp.mac which has MAC of each markers used in the test.

```
> out.c$param
$liu_pval
[1] 0.002938438
$Is_Converged
[1] 1
$n.marker
[1] 67
$n.marker.test
[1] 67
> out.c$test.snp.mac
       VAR2
              VAR3
                    VAR4
                           VAR.5
                                  VAR6
                                        VAR7
                                               VAR8
                                                     VAR9 VAR10 VAR11 VAR12 VAR13
 VAR1
                                                         2
                 2
                        4
                            577
                                   432
                                                                3
                                                                      2
                                                                             1
VAR14 VAR15 VAR16 VAR17 VAR18 VAR19 VAR20 VAR21 VAR22 VAR23 VAR24 VAR25 VAR26
  657
                82
                        1
                             25
                                   328
                                          465
                                                  2
                                                         4
                                                              85
                                                                    430
VAR27 VAR28 VAR29 VAR30 VAR31 VAR32 VAR33 VAR34 VAR35 VAR36 VAR37 VAR38 VAR39
         82
                        1
                               1
                                    15
                                           19
                                                  1
                                                       657
                                                                1
                                                                     35
VAR40 VAR41 VAR42 VAR43 VAR44 VAR45
                                      VAR46 VAR47 VAR48 VAR49 VAR50 VAR51 VAR52
         913
                      423
                              2
                                     2
                                            1
                                                  1
                                                        29
                                                                2
                                                                      1
                                                                           527
                                                                                  10
VAR53 VAR54 VAR55 VAR56 VAR57 VAR58 VAR59 VAR60 VAR61 VAR62 VAR63 VAR64 VAR65
  527
           8
                 3
                        2
                            200
                                     3
                                            1
                                                  1
                                                        15
                                                                1
                                                                      1
                                                                             3
VAR66 VAR67
    2
>
```

When the trait is binary and the sample size is small, SKAT can produce conservative results. We developed a moment matching adjustment (MA) that adjusts the asymptotic null distribution by estimating empirical variance and kurtosis. By default, SKAT will conduct the MA adjustment when the sample size < 2000. In the following code, we use only 200 samples to run SKAT.

```
> IDX<-c(1:100,1001:1100)
> # With-adjustment
> obj.s<-SKAT_Null_Model(y.b[IDX] ~ X[IDX,],out_type="D")

Sample size (non-missing y and X) = 200, which is < 2000. The small sample adjustment is appli
> SKAT(Z[IDX,], obj.s, kernel = "linear.weighted")$p.value
```

```
[1] 0.1338658
```

>

If you don't want to use the adjustment, please set Adjustment=FALSE in the SKAT_Null_Model function.

```
> # Without-adjustment
> obj.s<-SKAT_Null_Model(y.b[IDX] ~ X[IDX,],out_type="D", Adjustment=FALSE)
> SKAT(Z[IDX,], obj.s, kernel = "linear.weighted")$p.value
[1] 0.147093
```

Resampling based approaches to adjust for binary traits have been developed and implemented in SKATBinary function. When you use the SKATBinary function, Adjustment=TRUE in SKAT_Null_Model is not necessary. Implemented methods are 1) Efficient resampling (ER); 2) ER with adaptive resampling (ER.A); 3) Quantile adjusted moment matching (QA); 4) Moment matching adjustment (MA); 5) No adjustment (UA); and 6) Hybrid. "Hybrid" (default method) selects a method based on the total minor allele count (MAC), the number of individuals with minor alleles (m), and the degree of case-control imbalance. Detailed description of these methods can be found in the following reference:

Lee, S., Fuchsberger, C., Kim, S., Scott, L. (2016) An efficient resampling method for calibrating single and gene-based rare variant association analysis in case–control studies. *Biostatistics* (2016) 17 (1): 1-15.

```
> # default hybrid approach
> out<-SKATBinary(Z[IDX,], obj.s, kernel = "linear.weighted")
> out$p.value
[1] 0.147093
```

>

We have recently developed more scalable and accurate method for binary traits, which is implemented in SKATBinary_Robust function. Detailed description of these methods can be found in the following reference:

Zhao, Z., Bi, W., Zhou, W., VanderHaar, P., Fritsche, L.G., Lee, S. (2020) UK Biobank Whole-Exome Sequence Binary Phenome Analysis with Robust Region-based Rare-Variant Test. *AJHG*, 106: 3-12, doi:https://doi.org/10.1016/j.ajhg.2019.11.012

```
> # Robust approach
> out<-SKATBinary_Robust(Z[IDX,], obj.s, kernel = "linear.weighted")
> out$p.value
[1] 0.1511284
```

>

2.1 Assign weights for each SNP

It is assumed that rarer variants are more likely to be causal variants with large effect sizes. To incorporate this assumption, the linear weighted kernel uses a weighting scheme and is formulated as ZWWZ', where Z is a genotype matrix, and $W = diag\{w_1, \ldots, w_m\}$ is a weight matrix. In the previous examples, we used the default beta(1,25) weight, $w_i = dbeta(p_i, 1, 25)$, where dbeta is a beta density function, and p_i is a minor allele frequency (MAF) of SNP i. Different parameters for the beta weight can be used by changing weights.beta. For example, weight.beta=c(0.5,0.5) will use the Madsen and Browning weight.

```
> SKAT(Z, obj, kernel = "linear.weighted", weights.beta=c(0.5,0.5))$p.value
[1] 0.4931639
```

You can use your own weight vector by using the weights parameter. For the logistic weight, we provide a function to generate the weight.

```
> # Shape of the logistic weight
>
> MAF<-1:1000/1000
> W<-Get_Logistic_Weights_MAF(MAF, par1=0.07, par2=150)
> par(mfrow=c(1,2))
> plot(MAF,W,xlab="MAF",ylab="Weights",type="1")
> plot(MAF[1:100],W[1:100],xlab="MAF",ylab="Weights",type="1")
> par(mfrow=c(1,2))
> # Use logistic weight
> weights<-Get_Logistic_Weights(Z, par1=0.07, par2=150)
> SKAT(Z, obj, kernel = "linear.weighted", weights=weights)$p.value
[1] 0.3293643
```

2.2 SKAT-O: Combined Test of burden test and SKAT

A test statistic of the combined test is

$$Q_{\rho} = (1 - \rho)Q_S + \rho Q_B,$$

where Q_S is a test statistic of SKAT, and Q_B is a score test statistic of the burden test. The ρ value can be specified by using the r.corr parameter (default: r.corr=0).

```
> #rho=0, SKAT
> SKAT(Z, obj, r.corr=0)$p.value
[1] 0.1401991
> #rho=0.9
> SKAT(Z, obj, r.corr=0.9)$p.value
[1] 0.06031026
```

```
> #rho=1, Burden test
> SKAT(Z, obj, r.corr=1)$p.value
[1] 0.06095529
```

If method="optimal.adj" or "SKATO" (both are equivalent), SKAT-O method will be performed, which computes p-values with eight different values of $\rho = (0, 0.1^2, 0.2^2, 0.3^2, 0.4^2, 0.5^2, 0.5, 1)$ and then uses the minimum p-value as a test statistic. If you want to use the original implementation of SKAT-O, use method="optimal", which uses eleven equally spaced ρ values from 0 to 1 as a grid of ρ s. We recommend to use "SKATO" or "optimal.adj", since it has a better type I error control.

```
> #Optimal Test
> SKAT(Z, obj, method="SKATO")$p.value
[1] 0.1008976
>
```

2.3 Combined test of common and rare variants

It is possible that both common and rare variants are associated with phenotypes. To test for combined effects of common and rare variants, SKAT_CommonRare function can be used. The detailed description of the combined test can be found in the following reference:

Ionita-Laza, I., Lee, S., Makarov, V., Buxbaum, J. Lin, X. (2013). Sequence kernel association tests for the combined effect of rare and common variants. *AJHG*, 92(6):841-53.

```
> # Combined sum test (SKAT-C and Burden-C)
>
> SKAT_CommonRare(Z, obj)$p.value

[1] 0.2238025
> SKAT_CommonRare(Z, obj, r.corr.rare=1, r.corr.common=1)$p.value

[1] 0.1546374
> # Adaptive test (SKAT-A and Burden-A)
> SKAT_CommonRare(Z, obj, method="A")$p.value

[1] 0.4372293
> SKAT_CommonRare(Z, obj, r.corr.rare=1, r.corr.common=1, method="A")$p.value

[1] 0.1548059
```

2.4 Impute missing genotypes.

If there are missing genotypes, SKAT automatically imputes them based on Hardy-Weinberg equilibrium. You can choose from "bestguess", "fixed" or "random". The "bestguess" imputes missing genotypes as most likely values (0,1,2), the "fixed" imputes missing genotypes by assigning the mean genotype value (2p, p is the MAF) and the "random" imputes missing genotypes by generating binomial(2,p) random variables. The default imputation method for the SKAT function is "fixed" and for the SKATBinary function is "bestguess".

```
> # Assign missing
> Z1<-Z
> Z1[1,1:3]<-NA
> # bestguess imputation
> SKAT(Z1,obj,impute.method = "bestguess")$p.value

[1] 0.1401991
> # fixed imputation
> SKAT(Z1,obj,impute.method = "fixed")$p.value

[1] 0.1401982
> # random imputation
> SKAT(Z1,obj,impute.method = "random")$p.value

[1] 0.1401991
>
```

2.5 Resampling

SKAT package provides functions to carry out resampling method to compute empirical p-values and to control for family wise error rate. Two different resampling methods are implemented. "bootstrap" conducts a parametric bootstrap to resample residuals from H_0 with adjusting for covariates. When there is no covariate, "bootstrap" is equivalent to the permutation. "perturbation" perturbs the residuals by multiplying standard normal random variables. The default method is "bootstrap". From ver 0.7, we do not provide the "perturbation" method.

```
> Get_Resampling_Pvalue(re) # get resampling p-value
$p.value
[1] 0.1463707

$is_smaller
[1] FALSE
> detach(SKAT.example)
```

When there are many genes/SNP sets to test, resampling methods can be used to control family-wise error rate. Examples are provided in the next section.

2.6 Adjust for kinship

If related individuals exist in your data, you need to adjust for kinship. SKAT_NULL_emmaX function uses linear mixed model (EMMAX) to estimate the variance component, which will be subsequently used to adjust for kinship. For the kinship adjustment, SKAT_NULL_emmaX function should be used instead of SKAT_Null_Model.

```
> data(SKAT.fam.example)
> attach(SKAT.fam.example)
> # K: kinship matrix
> obj<-SKAT_NULL_emmaX(y ~ X, K=K)
> SKAT(Z, obj)$p.value

[1] 0.2123192
> # SKAT-0
> SKAT(Z, obj, method="SKATO")$p.value

[1] 0.352943
> detach(SKAT.fam.example)
```

2.7 X chromosome test

Since male has only one copy of X-chromosome, special care is needed to test for associations in X-chromosome. We have developed a method to test for X-chromosome in region based rare variant test with and without X-inactivation. To use it, you need to use SKAT_Null_Model_ChrX to fit the null model and SKAT_ChrX for association tests. Detailed description of association tests in X-chromosome can be found in the following reference:

Ma, C., Boehnke, M., Lee, S., the GoT2D Investigators (2015) Evaluating the Calibration and Power of Three Gene-based Association Tests of Rare Variants for the X Chromosome, *Genetic Epidemiology*, 39 (7): 499-508.

For Y chromosome, you can use the same null model function for X with Model.Y=TRUE. The p-value can be calculated with SKAT_ChrY function. The following example use the same genotype matrix previously used to show how these functions can be used.

3 Plink Binary format files

> detach(SKAT.example.ChrX)

>

For the genome-wide data analysis, plink binary format files can be used in SKAT. To use plink files, plink bed, bim and fam files, and your own setid file that contains information of SNP sets are needed. Example files can be found on the SKAT/MetaSKAT google group page.

```
> # Create the MW File
> File.Bed<-"./Example1.bed"</pre>
> File.Bim<-"./Example1.bim"</pre>
> File.Fam<-"./Example1.fam"</pre>
> File.SetID<-"./Example1.SetID"
> File.SSD<-"./Example1.SSD"
> File.Info<-"./Example1.SSD.info"</pre>
> # To use binary ped files, you have to generate SSD file first.
> # If you already have a SSD file, you do not need to call this function.
> Generate_SSD_SetID(File.Bed, File.Bim, File.Fam, File.SetID, File.SSD, File.Info)
Check duplicated SNPs in each SNP set
No duplicate
1000 Samples, 10 Sets, 984 Total SNPs
[1] "SSD and Info files are created!"
   Now you can open SSD and Info file and run SKAT.
> FAM<-Read_Plink_FAM(File.Fam, Is.binary=FALSE)
> y<-FAM$Phenotype
> # To use a SSD file, please open it first. After finishing using it, you must close it.
> SSD.INFO<-Open_SSD(File.SSD, File.Info)
1000 Samples, 10 Sets, 984 Total SNPs
Open the SSD file
> # Number of samples
> SSD.INFO$nSample
[1] 1000
> # Number of Sets
> SSD.INFO$nSets
[1] 10
> obj<-SKAT_Null_Model(y ~ 1, out_type="C")</pre>
> out<-SKAT.SSD.All(SSD.INFO, obj)
> out
$results
              P.value N.Marker.All N.Marker.Test
     SetID
1 GENE_01 0.77747880
                                 94
                                                94
2 GENE_02 0.06245208
                                 84
                                               84
```

108

108

3 GENE_03 0.38416582

4	GENE_04	0.46179268	101	101
5	GENE_05	0.18548863	103	103
6	GENE_06	0.93255760	94	94
7	GENE_07	0.18897220	104	104
8	GENE_08	0.73081683	96	96
9	GENE_09	0.67366458	100	100
10	GENE_10	0.40310682	100	100

P.value.Resampling NULL

\$OUT.snp.mac

\$OUT.snp.mac\$GENE_01

SNP0056	SNP0083	SNP0035	SNP0027	SNP0037	SNP0011	SNP0071	SNP0033	SNP0025	SNP0088
217	219	188	214	192	183	193	186	195	214
SNP0014	SNP0036	SNP0074	SNP0017	SNP0016	SNP0022	SNP0087	SNP0094	SNP0057	SNP0028
180	197	200	199	191	204	217	221	199	202
SNP0058	SNP0054	SNP0031	SNP0046	SNP0062	SNP0082	SNP0012	SNP0093	SNP0050	SNP0068
226	210	202	180	204	221	214	204	189	190
SNP0021	SNP0085	SNP0089	SNP0001	SNP0052	SNP0066	SNP0090	SNP0092	SNP0061	SNP0029
190	226	199	226	203	186	179	193	172	212
SNP0042	SNP0026	SNP0002	SNP0013	SNP0043	SNP0044	SNP0080	SNP0059	SNP0048	SNP0077
191	219	206	191	205	192	211	200	199	200
SNP0049	SNP0039	SNP0067	SNP0076	SNP0003	SNP0018	SNP0040	SNP0079	SNP0009	SNP0024
200	217	198	230	193	180	199	209	186	179
SNP0070	SNP0084	SNP0055	SNP0007	SNP0015	SNP0064	SNP0065	SNP0075	SNP0086	SNP0023
197	210	218	209	190	191	187	211	183	193
SNP0010	SNP0019	SNP0081	SNP0008	SNP0004	SNP0072	SNP0047	SNP0078	SNP0006	SNP0060
203	199	191	188	207	205	187	213	205	218
SNP0032	SNP0030	SNP0005	SNP0053	SNP0069	SNP0034	SNP0041	SNP0073	SNP0091	SNP0051
209	183	195	204	184	212	181	195	197	226
SNP0020	SNP0063	SNP0045	SNP0038						
217	191	228	206						

\$OUT.snp.mac\$GENE_02

SNP0167 SNP0165 SNP0172 SNP0124 SNP0115 SNP0112 SNP0174 SNP0121 SNP0103 SNP0116 SNP0141 SNP0133 SNP0134 SNP0149 SNP0099 SNP0161 SNP0095 SNP0169 SNP0164 SNP0097 SNP0143 SNP0148 SNP0114 SNP0173 SNP0160 SNP0136 SNP0108 SNP0109 SNP0105 SNP0118 SNP0150 SNP0153 SNP0126 SNP0162 SNP0119 SNP0111 SNP0129 SNP0142 SNP0145 SNP0132 SNP0177 SNP0163 SNP0107 SNP0100 SNP0154 SNP0178 SNP0146 SNP0101 SNP0144 SNP0171

	SNP0139	SNP0098							SNP0156
221	210	196	218	217	199	213	213	203	178
SNP0166	SNP0120	SNP0117	SNP0151	SNP0127	SNP0104	SNP0152	SNP0157	SNP0175	SNP0138
196	197	210	208	180	202	196	191	189	200
SNP0106	SNP0130	SNP0176	SNP0168	SNP0135	SNP0158	SNP0170	SNP0102	SNP0128	SNP0159
203	208	209	211	199	191	190	194	188	197
SNP0122	SNP0123	SNP0155	SNP0125						
166	200	239	203						
\$OUT.snr	o.mac\$GE1	VF. 03							
_		SNP0199	SNP0266	SNP0195	SNP0186	SNP0220	SNP0256	SNP0236	SNP0214
219	197	220	196	183	212	202	206	214	195
		SNP0224							
186	207	221	198	183	211	214	196	200	189
		SNP0267							
205	213	231	234	185	205	199	216	213	197
		SNP0245							
202	207	206	187	220	181	195	171	207	194
		SNP0283							
192	200	188	194	212	198	190	203	185	195
		SNP0278							
193	176	211	177	203	187	199	199	195	170
SNP0183	SNP0180	SNP0194	SNP0189	SNP0212	SNP0228	SNP0202	SNP0215	SNP0261	SNP0274
186	197	212	193	200	200	220	188	179	209
SNP0223	SNP0282	SNP0239	SNP0271	SNP0227	SNP0246	SNP0285	SNP0198	SNP0217	SNP0213
214	202	193	183	193	202	217	214	188	201
SNP0184	SNP0187	SNP0193	SNP0253	SNP0251	SNP0185	SNP0201	SNP0182	SNP0258	SNP0281
170	200	183	216	196	212	186	210	202	190
SNP0234	SNP0216	SNP0211	SNP0191	SNP0192	SNP0260	SNP0221	SNP0257	SNP0181	SNP0252
184	190	208	217	207	219	199	216	193	213
SNP0243	SNP0208	SNP0259	SNP0268	SNP0203	SNP0248	SNP0231	SNP0263		
188	195	198	191	210	198	183	220		
\$OUT.sn	o.mac\$GE	NE 04							
_		SNP0387	SNP0346	SNP0348	SNP0332	SNP0313	SNP0288	SNP0309	SNP0329
206	207	223	194	191	207	203	190	212	218
		SNP0320							
194	202	188	200	214	188	206	199	203	187
		SNP0370							
214	218	207	204	201	208	206	194	208	214
		SNP0330							
209	199	197	217	212	214	202	210	191	195
		SNP0350							
184	215	157	200	217	209	169	217	239	208
SNP0315	SNP0359	SNP0307	SNP0371	SNP0310	SNP0366	SNP0386	SNP0379	SNP0378	SNP0372

100	016	101	010	100	177	101	100	105	005
190	216	194	219	199	177	191	192	195	205
		SNP0293							
191	211	192	211	205	201	203	211	193	197
		SNP0291							
213	190	188	200	212	208	198	198	211	187
		SNP0322							
216	191	196	222	196	209	207	211	190	201
SNP0294	SNP0296	SNP0361	SNP0325		SNP0374		SNP0342	SNP0368	SNP0365
190	193	186	192	166	190	223	194	222	184
SNP0316									
214									
_	o.mac\$GE1								
SNP0460		SNP0404							SNP0416
184	214	199	213	171	183	189	220	197	174
SNP0400	SNP0469	SNP0408	SNP0473	SNP0424	SNP0401	SNP0392	SNP0422	SNP0468	SNP0395
183	197	220	197	216	202	177	216	207	211
SNP0476	SNP0488	SNP0486	SNP0435	SNP0458	SNP0467	SNP0449	SNP0480	SNP0478	SNP0394
182	178	198	215	182	182	210	206	199	205
SNP0442	SNP0456	SNP0447	SNP0421	SNP0444	SNP0405	SNP0414	SNP0413	SNP0475	SNP0477
222	213	212	202	205	185	212	201	225	218
SNP0450	SNP0423	SNP0452	SNP0426	SNP0403	SNP0490	SNP0402	SNP0437	SNP0445	SNP0465
207	205	177	211	213	195	193	240	194	188
SNP0430	SNP0393	SNP0481	SNP0484	SNP0439	SNP0454	SNP0389	SNP0390	SNP0459	SNP0487
183	199	174	188	208	196	208	203	187	196
SNP0470	SNP0399	SNP0428	SNP0427	SNP0472	SNP0455	SNP0397	SNP0391	SNP0453	SNP0398
188	197	203	199	195	193	216	192	197	201
SNP0417	SNP0479	SNP0446	SNP0388	SNP0407	SNP0412	SNP0431	SNP0415	SNP0441	SNP0461
202	199	198	199	207	189	201	180	206	177
SNP0418	SNP0420	SNP0438	SNP0482	SNP0396	SNP0406	SNP0483	SNP0432	SNP0451	SNP0425
190	222	197	205	169	177	202	196	201	207
SNP0436	SNP0443	SNP0464	SNP0471	SNP0433	SNP0434	SNP0485	SNP0463	SNP0489	SNP0457
181	193	208	215	201	219	196	195	211	181
SNP0440	SNP0448	SNP0411							
214		204							
\$OUT.snp	o.mac\$GE1	NE_06							
SNP0543	SNP0534	SNP0517	SNP0518	SNP0525	SNP0568	SNP0550	SNP0554	SNP0523	SNP0542
219	186	216	197	197	200	192	215	190	199
SNP0520	SNP0503	SNP0493	SNP0533	SNP0569	SNP0504	SNP0576	SNP0580	SNP0527	SNP0577
200	198	171	200	179	223	218	215	209	203
SNP0541	SNP0522	SNP0582	SNP0571	SNP0501	SNP0524	SNP0574	SNP0573	SNP0544	SNP0532
201	206	188			185			196	225
		SNP0512							
195	177				209				187
								- · -	

	SNP0537								
199	205	178	202	173	227	218	221	223	184
	SNP0552								
200	202	193	194	177	196	209	198	180	189
SNP0553	SNP0562							SNP0578	SNP0570
213	179	197	191	209	187	195	225	219	221
SNP0581	SNP0496	SNP0548	SNP0575	SNP0540	SNP0545	SNP0530	SNP0538	SNP0559	SNP0497
213	209	193	205	193	173	183	189	208	202
SNP0557	SNP0563	SNP0511	SNP0495	SNP0583	SNP0536	SNP0516	SNP0528	SNP0509	SNP0561
201	189	199	214	201	218	200	192	221	213
SNP0492	SNP0567	SNP0506	SNP0556						
202	211	183	185						
_	p.mac\$GE1								
SNP0609	SNP0649	SNP0667	SNP0685	SNP0661	SNP0597	SNP0598	SNP0623	SNP0636	SNP0603
187	185	219	201	191	212	211	207	229	205
SNP0659	SNP0657	SNP0684	SNP0616	SNP0630	SNP0629	SNP0612	SNP0677	SNP0652	SNP0672
211	211	182	192	186	193	207	200	208	222
SNP0621	SNP0670	SNP0643	SNP0619	SNP0644	SNP0686	SNP0618	SNP0655	SNP0656	SNP0653
216	215	214	187	216	224	188	197	191	203
SNP0683	SNP0663	SNP0640	SNP0592	SNP0679	SNP0658	SNP0611	SNP0676	SNP0617	SNP0634
229	203	218	201	147	202	195	211	209	208
SNP0673	SNP0660	SNP0607	SNP0678	SNP0681	SNP0606	SNP0589	SNP0591	SNP0641	SNP0613
188	193	193	216	176	209	199	198	205	194
SNP0586	SNP0687	SNP0669	SNP0594	SNP0604	SNP0666	SNP0688	SNP0671	SNP0648	SNP0608
205	202	192	206	181	190	204	180	193	201
SNP0664	SNP0626	SNP0651	SNP0602	SNP0615	SNP0674	SNP0642	SNP0628	SNP0662	SNP0668
193	198	198	194	205	211	201	206	194	181
SNP0627	SNP0588	SNP0624	SNP0625	SNP0639	SNP0599	SNP0635	SNP0593	SNP0596	SNP0645
213	194	213	228	190	196	186	215	213	180
SNP0675	SNP0631	SNP0682	SNP0620	SNP0633	SNP0587	SNP0610	SNP0600	SNP0632	SNP0595
199	192	187	209	205	225	196	214	196	199
SNP0680	SNP0638	SNP0665	SNP0637	SNP0622	SNP0647	SNP0654	SNP0601	SNP0585	SNP0646
192	167	217	204	205	202	207	210	210	190
SNP0650	SNP0614	SNP0605	SNP0590						
185	211	195	179						
\$OUT.snj	p.mac\$GE1	NE_08							
SNP0740	SNP0720	SNP0738	SNP0733	SNP0779	SNP0732	SNP0778	SNP0703	SNP0756	SNP0705
194	195	200	196	214	209	201	200	190	194
SNP0727	SNP0734	SNP0765	SNP0772	SNP0699	SNP0775	SNP0741	SNP0763	SNP0749	SNP0715
233	205	219	191	189	201	186	198	231	184
SNP0725	SNP0755	SNP0707	SNP0747	SNP0702	SNP0748	SNP0714	SNP0777	SNP0771	SNP0726
189	179	175	199	206	193	197	189	191	212
SNP0773	SNP0697	SNP0696	SNP0766	SNP0708	SNP0695	SNP0711	SNP0761	SNP0746	SNP0729

198	207	205	185	211	191	189	206	221	182
SNP0781	SNP0710	SNP0722	SNP0742	SNP0753	SNP0689	SNP0735	SNP0730	SNP0731	SNP0768
201	202	188	200	200	199	192	234	213	200
SNP0762	SNP0784	SNP0706	SNP0744	SNP0757	SNP0776	SNP0760	SNP0724	SNP0751	SNP0691
195	208	181	188	207	198	196	197	193	178
SNP0752	SNP0750	SNP0721	SNP0704	SNP0701	SNP0713	SNP0780	SNP0743	SNP0770	SNP0718
188	185	188	213	199	195	212	182	212	221
SNP0782	SNP0774	SNP0737	SNP0745	SNP0769	SNP0723	SNP0693	SNP0716	SNP0758	SNP0694
175	233	218	191	225	216	201	214	181	195
SNP0764	SNP0767	SNP0719	SNP0739	SNP0754	SNP0783	SNP0700	SNP0759	SNP0717	SNP0728
217	194	201	193	201	225	197	194	181	191
SNP0736	SNP0690	SNP0712	SNP0692	SNP0698	SNP0709				
217	223	200	217	191	221				
\$OUT.snp	o.mac\$GE1	VE_09							
SNP0795	SNP0859	SNP0845	SNP0816	SNP0829	SNP0881	SNP0830	SNP0811	SNP0807	SNP0853
190	183	182	197	205	202	212	193	195	194
SNP0841	SNP0796	SNP0880	SNP0854	SNP0821	SNP0797	SNP0882	SNP0843	SNP0828	SNP0789
193	219	198	203	182	228	185	217	193	207
SNP0856	SNP0884	SNP0812	SNP0799	SNP0825	SNP0850	SNP0805	SNP0877	SNP0804	SNP0864
188	217	196	207	203	189	215	211	201	194
SNP0842	SNP0871	SNP0790	SNP0806	SNP0863	SNP0793	SNP0846	SNP0849	SNP0873	SNP0823
202	179	212	175	207	215	186	198	199	191
SNP0792	SNP0831	SNP0866	SNP0858	SNP0847	SNP0860	SNP0791	SNP0824	SNP0787	SNP0819
192	210	215	217	208	193	187	202	190	197
SNP0839	SNP0813	SNP0803	SNP0874	SNP0876	SNP0851	SNP0794	SNP0814	SNP0827	SNP0788
211	201	194	224	216	204	194	212	181	205
SNP0837	SNP0832	SNP0879	SNP0817	SNP0852	SNP0815	SNP0802	SNP0857	SNP0875	SNP0818
198	186	213	225	214	203	211	194	171	207
SNP0809	SNP0835	SNP0800	SNP0878	SNP0801	SNP0786	SNP0870	SNP0868	SNP0844	SNP0855
187	185	192	231	187	232	204	204	203	193
SNP0848	SNP0798	SNP0869	SNP0822	SNP0872	SNP0867	SNP0808	SNP0861	SNP0838	SNP0883
175	195	196	188	230	212	191	201	196	183
SNP0826	SNP0836	SNP0785	SNP0834	SNP0820	SNP0833	SNP0865	SNP0840	SNP0862	SNP0810
193	207	203	209	213	226	193	194	220	201
\$OUT.snp	o.mac\$GE1	VE_10							
SNP088	5 SNP090	08 SNP09	957 SNP	0937 SNI	20886 SI	NP0940	SNP0922	SNP0980	
199.3927	7 191.532	23 206.06	306 224.3	3461 190	.0407 209	5.8527 20	07.4522	187.6892	
SNP0910	SNP093	38 SNP09	975 SNP	0965 SNI	P0889 SI	NP0929	SNP0953	SNP0921	
176.5893	3 205.25	78 181.08	365 205.6	5738 184	.7390 210	0.7396 1	95.5645	189.1348	
SNP0916	SNP090	04 SNPOS	915 SNP	0913 SNI	20949 SI	NP0890	SNP0933	SNP0969	
219.7583	1 214.35	79 200.00	000 217.3	3038 188	.3182 194	4.7262 2	14.3579	223.2323	
SNP0934	SNP096	SO SNPOS	956 SNP	0963 SNI	20895 SI	NP0950	SNP0962	SNP0923	

176.1134 208.9249 196.1577 181.4516 180.4435 200.4028 186.6126 196.5552

```
SNP0914 SNP0959 SNP0897 SNP0971 SNP0968
                                            SNP0954
                                                     SNP0958
                                                              SNP0902
189.0799 207.7393 192.1132 179.9798 202.2245 195.9596 184.2105 198.5816
 SNP0935 SNP0899 SNP0926 SNP0943 SNP0976
                                            SNP0955
                                                     SNP0946
                                                              SNP0978
184.4758 205.0761 190.3323 194.5838 218.1448 204.6606 203.2520 202.4291
 SNP0917 SNP0901 SNP0907 SNP0909 SNP0948
                                            SNP0939
                                                     SNP0906
178.6075 228.6002 192.3464 194.7262 204.6371 183.7563 201.6211 201.4099
 SNP0894 SNP0936 SNP0920 SNP0984 SNP0981
                                            SNP0931
                                                     SNP0928
                                                              SNP0912
210.1010 203.6290 212.1212 227.4549 198.5816 185.4103 196.3746 226.3959
 SNP0952 SNP0924 SNP0919 SNP0925 SNP0930
                                            SNP0941
                                                     SNP0974
                                                              SNP0903
200.8155 229.5248 187.3112 208.4592 183.5700 212.4874 171.3710 191.1021
 SNP0972 SNP0905 SNP0979 SNP0982 SNP0932 SNP0942
                                                     SNP0973
                                                              SNP0892
185.2971 212.5506 200.4028 184.6620 198.9848 200.2022 195.5420 195.9799
 SNP0898 SNP0966 SNP0911 SNP0970 SNP0918 SNP0967
                                                     SNP0951
200.2012 213.7097 201.0050 218.5297 198.1800 184.4758 201.0101 207.8708
 SNP0947 SNP0944 SNP0891 SNP0961 SNP0887 SNP0927
                                                     SNP0896
210.8981 177.8894 191.7255 170.7071 206.8618 223.9108 207.8708 205.8527
SNP0888 SNP0900 SNP0893 SNP0983
208.4592 188.8889 224.9240 202.2245
```

```
attr(,"class")
[1] "SKAT_SSD_ALL"
```

> out

> File.Cov<-"./Example1.Cov"

If you have a plink covariate file, Read_Plink_FAM_Cov function can be used to read both FAM and covariate files.

```
> FAM_Cov<-Read_Plink_FAM_Cov(File.Fam, File.Cov, Is.binary=FALSE)
> # First 5 rows
> FAM_Cov[1:5,]
     FID IID PID MID Sex Phenotype
                                            X1 X2
1 FID454
                       1 0.679793 1.0297614
               0
                   0
2 FID977
               0
                        1 0.836566 0.1846235
3 FID462
               0
                   0
                       1 -0.408388 -0.6141158
4 FID958
           1
               0
                   0
                        1 -0.522305 -2.0226759
5 FID668
                        1 -0.328300 -0.8213776 0
               0
> # Run with covariates
> X1 = FAM_Cov$X1
> X2 = FAM_Cov$X2
> y<-FAM_Cov$Phenotype
> obj<-SKAT_Null_Model(y ~ X1 + X2, out_type="C")</pre>
> out<-SKAT.SSD.All(SSD.INFO, obj)
```

\$results

	${\tt SetID}$	P.value	N.Marker.All	${\tt N.Marker.Test}$
1	GENE_01	0.77771227	94	94
2	GENE_02	0.06157071	84	84
3	GENE_03	0.39818504	108	108
4	GENE_04	0.46548442	101	101
5	GENE_05	0.18981516	103	103
6	GENE_06	0.94073952	94	94
7	GENE_07	0.18779019	104	104
8	GENE_08	0.74559501	96	96
9	GENE_09	0.66573796	100	100
10	GENE_10	0.40204308	100	100

\$P.value.Resampling
NULL

\$OUT.snp.mac

\$OUT.snp.mac\$GENE_01

SNP0056 SNP0083 SNP0035 SNP0027 SNP0037 SNP0011 SNP0071 SNP0033 SNP0025 SNP0088 SNP0014 SNP0036 SNP0074 SNP0017 SNP0016 SNP0022 SNP0087 SNP0094 SNP0057 SNP0028 SNP0058 SNP0054 SNP0031 SNP0046 SNP0062 SNP0082 SNP0012 SNP0093 SNP0050 SNP0068 SNP0021 SNP0085 SNP0089 SNP0001 SNP0052 SNP0066 SNP0090 SNP0092 SNP0061 SNP0029 SNP0042 SNP0026 SNP0002 SNP0013 SNP0043 SNP0044 SNP0080 SNP0059 SNP0048 SNP0077 SNP0049 SNP0039 SNP0067 SNP0076 SNP0003 SNP0018 SNP0040 SNP0079 SNP0009 SNP0024 SNP0070 SNP0084 SNP0055 SNP0007 SNP0015 SNP0064 SNP0065 SNP0075 SNP0086 SNP0023 SNP0010 SNP0019 SNP0081 SNP0008 SNP0004 SNP0072 SNP0047 SNP0078 SNP0006 SNP0060 SNP0032 SNP0030 SNP0005 SNP0053 SNP0069 SNP0034 SNP0041 SNP0073 SNP0091 SNP0051 SNP0020 SNP0063 SNP0045 SNP0038

\$OUT.snp.mac\$GENE_02

SNP0167 SNP0165 SNP0172 SNP0124 SNP0115 SNP0112 SNP0174 SNP0121 SNP0103 SNP0116 SNP0141 SNP0133 SNP0134 SNP0149 SNP0099 SNP0161 SNP0095 SNP0169 SNP0164 SNP0097 SNP0143 SNP0148 SNP0114 SNP0173 SNP0160 SNP0136 SNP0108 SNP0109 SNP0105 SNP0118

194	208	225	208	206	209	206	208	182	193
		SNP0126		206					
201	183	169	219	200		186	200	216	
					218				198
		SNP0107							
207	215	206	209	212	187	199	213	193	229
		SNP0098							
221	210	196	218	217	199	213	213	203	178
		SNP0117							
196	197	210	208	180	202	196	191	189	200
		SNP0176							SNP0159
203	208	209	211	199	191	190	194	188	197
SNP0122	SNP0123	SNP0155	SNP0125						
166	200	239	203						
ቀ ር፲፹ ~~~	-	TE OO							
-	o.mac\$GEl	NE_03 SNP0199	CMDOOSS	CMDO10E	CMDO106	CMDOOOO	CMDOOE	CMDOOSE	CMDO014
219	197	220	196	183	212	202	206	214	195
		SNP0224							
186	207	221	198	183	211	214	196	200	189
		SNP0267							
205	213	231	234	185	205	199	216	213	197
		SNP0245							
202	207	206	187	220	181	195	171	207	194
SNP0262	SNP0244	SNP0283	SNP0240	SNP0218	SNP0235		SNP0247	SNP0242	SNP0197
192	200	188	194	212	198	190	203	185	195
SNP0210	SNP0255	SNP0278	SNP0219	SNP0276	SNP0190	SNP0277	SNP0200	SNP0179	SNP0229
193	176	211	177	203	187	199	199	195	170
SNP0183	SNP0180	SNP0194	SNP0189	SNP0212	SNP0228	SNP0202	SNP0215	SNP0261	SNP0274
186	197	212	193	200	200	220	188	179	209
SNP0223	SNP0282	SNP0239	SNP0271	SNP0227	SNP0246	SNP0285	SNP0198	SNP0217	SNP0213
214	202	193	183	193	202	217	214	188	201
SNP0184	SNP0187	SNP0193	SNP0253	SNP0251	SNP0185	SNP0201	SNP0182	SNP0258	SNP0281
170	200	183	216	196	212	186	210	202	190
SNP0234	SNP0216	SNP0211	SNP0191	SNP0192	SNP0260	SNP0221	SNP0257	SNP0181	SNP0252
184	190	208	217	207	219	199	216	193	213
SNP0243	SNP0208	SNP0259	SNP0268	SNP0203	SNP0248	SNP0231	SNP0263		
188	195	198	191	210	198	183	220		
\$OUT.sn	p.mac\$GE	NE_04							
SNP0303	SNP0362	SNP0387	SNP0346	SNP0348	SNP0332	SNP0313	SNP0288	SNP0309	SNP0329
206	207	223	194	191	207	203	190	212	218
SNP0377	SNP0300	SNP0320	SNP0347	SNP0290	SNP0344	SNP0319	SNP0343	SNP0339	SNP0304
194	202	188	200	214	188	206	199	203	187
SNP0356	SNP0340	SNP0370	SNP0327	SNP0351	SNP0335	SNP0314	SNP0380	SNP0336	SNP0333
214	218	207	204	201	208	206	194	208	214

SNP0306	SNP0334	SNP0330	SNP0373	SNP0297	SNP0305	SNP0341	SNP0357	SNP0317	SNP0302
209	199	197	217	212	214	202	210	191	195
SNP0299	SNP0367	SNP0350	SNP0354	SNP0324	SNP0352	SNP0382	SNP0383	SNP0301	SNP0295
184	215	157	200	217	209	169	217	239	208
SNP0315	SNP0359	SNP0307	SNP0371	SNP0310	SNP0366	SNP0386	SNP0379	SNP0378	SNP0372
190	216	194	219	199	177	191	192	195	205
SNP0321	SNP0385	SNP0293	SNP0376	SNP0363	SNP0308	SNP0318	SNP0323	SNP0287	SNP0381
191	211	192	211	205	201	203	211	193	197
SNP0364	SNP0328	SNP0291	SNP0349	SNP0289	SNP0337	SNP0353	SNP0345	SNP0375	SNP0311
213	190	188	200	212	208	198	198	211	187
SNP0326	SNP0358	SNP0322	SNP0292	SNP0298	SNP0369	SNP0360	SNP0355	SNP0338	SNP0384
216	191	196	222	196	209	207	211	190	201
SNP0294	SNP0296	SNP0361	SNP0325	SNP0312	SNP0374	SNP0331	SNP0342	SNP0368	SNP0365
190	193	186	192	166	190	223	194	222	184
SNP0316									
214									
	p.mac\$GEI								
		SNP0404							
184	214	199	213	171	183	189	220	197	174
		SNP0408							
183	197	220	197	216	202	177	216	207	211
		SNP0486							
182	178	198	215	182	182	210	206	199	205
		SNP0447							
222	213	212	202	205	185	212	201	225	218
207		SNP0452 177							
	205	SNP0481	211	213	195	193	240	194	188
183	199	174	188	208	196	208	203	187	196
	SNP0399						203 SNP0391		
188	197	203	199	195	193	216	192	197	201
		SNP0446							
202	199	198	199	207	189	201	180	206	177
		SNP0438							
190	222	197		169	177	202		201	207
		SNP0464							
181	193	208	215	201	219	196	195	211	181
	SNP0448								
214		204							
211	201	201							
\$OUT.sn	o.mac\$GE	NE_06							
SNP0543	SNP0534	SNP0517	SNP0518	SNP0525	SNP0568	SNP0550	SNP0554	SNP0523	SNP0542
219	186	216	197	197	200	192	215	190	199
SNP0520	SNP0503	SNP0493	SNP0533	SNP0569	SNP0504	SNP0576	SNP0580	SNP0527	SNP0577

200	198	171	200	170	വാ	010	215	209	203
		171		179	223	218	SNP0573		
201	206	188	191	200	185	192	206	196	225
							SNP0531		
195	177	199	215	205	209	188	206	172	187
							SNP0491		
199	205	178	202	173	227	218	221	223	184
							SNP0565		
200	202	193	194	177	196	209	198	180	189
							SNP0513		
213	179	197	191	209	187	195	225	219	221
							SNP0538		
213	209	193	205	193	173	183	189	208	202
							SNP0528		
201	189	199	214	201	218	200	192	221	213
		SNP0506		201	210	200	132	221	210
202	211	183	185						
202	211	100	100						
\$OUT snr	o.mac\$GE1	VF. 07							
-	•		SNP0685	SNP0661	SNP0597	SNP0598	SNP0623	SNP0636	SNP0603
187	185	219	201	191	212	211	207	229	205
							SNP0677		
211	211	182	192	186	193	207	200	208	222
SNP0621							SNP0655		SNP0653
216	215	214	187	216	224	188	197	191	203
SNP0683	SNP0663						SNP0676		SNP0634
229	203	218	201	147	202	195	211	209	208
SNP0673	SNP0660	SNP0607	SNP0678	SNP0681			SNP0591	SNP0641	SNP0613
188	193	193	216	176	209	199	198	205	194
SNP0586	SNP0687	SNP0669	SNP0594	SNP0604	SNP0666	SNP0688	SNP0671	SNP0648	SNP0608
205	202	192	206	181	190	204	180	193	201
SNP0664	SNP0626	SNP0651	SNP0602	SNP0615	SNP0674	SNP0642	SNP0628	SNP0662	SNP0668
193	198	198	194	205	211	201	206	194	181
SNP0627	SNP0588	SNP0624	SNP0625	SNP0639	SNP0599	SNP0635	SNP0593	SNP0596	SNP0645
213	194	213	228	190	196	186	215	213	180
SNP0675	SNP0631	SNP0682	SNP0620	SNP0633	SNP0587	SNP0610	SNP0600	SNP0632	SNP0595
199	192	187	209	205	225	196	214	196	199
SNP0680	SNP0638	SNP0665	SNP0637	SNP0622	SNP0647	SNP0654	SNP0601	SNP0585	SNP0646
192	167	217	204	205	202	207	210	210	190
SNP0650	SNP0614	SNP0605	SNP0590						
185	211	195	179						
\$OUT.snp	o.mac\$GE1	NE_08							
SNP0740	SNP0720	SNP0738	SNP0733	SNP0779	SNP0732	SNP0778	SNP0703	SNP0756	SNP0705
194	195	200	196	214	209	201	200	190	194

SNP0727 SNP0734 SNP0765 SNP0772 SNP0699 SNP0775 SNP0741 SNP0763 SNP0749 SNP0715 SNP0725 SNP0755 SNP0707 SNP0747 SNP0702 SNP0748 SNP0714 SNP0777 SNP0771 SNP0726 SNP0773 SNP0697 SNP0696 SNP0766 SNP0708 SNP0695 SNP0711 SNP0761 SNP0746 SNP0729 SNP0781 SNP0710 SNP0722 SNP0742 SNP0753 SNP0689 SNP0735 SNP0730 SNP0731 SNP0768 SNP0762 SNP0784 SNP0706 SNP0744 SNP0757 SNP0776 SNP0760 SNP0724 SNP0751 SNP0691 SNP0752 SNP0750 SNP0721 SNP0704 SNP0701 SNP0713 SNP0780 SNP0743 SNP0770 SNP0718 SNP0782 SNP0774 SNP0737 SNP0745 SNP0769 SNP0723 SNP0693 SNP0716 SNP0758 SNP0694 SNP0764 SNP0767 SNP0719 SNP0739 SNP0754 SNP0783 SNP0700 SNP0759 SNP0717 SNP0728 SNP0736 SNP0690 SNP0712 SNP0692 SNP0698 SNP0709 \$OUT.snp.mac\$GENE_09 SNP0795 SNP0859 SNP0845 SNP0816 SNP0829 SNP0881 SNP0830 SNP0811 SNP0807 SNP0853 SNP0841 SNP0796 SNP0880 SNP0854 SNP0821 SNP0797 SNP0882 SNP0843 SNP0828 SNP0789 SNP0856 SNP0884 SNP0812 SNP0799 SNP0825 SNP0850 SNP0805 SNP0877 SNP0804 SNP0864 SNP0842 SNP0871 SNP0790 SNP0806 SNP0863 SNP0793 SNP0846 SNP0849 SNP0873 SNP0823 SNP0792 SNP0831 SNP0866 SNP0858 SNP0847 SNP0860 SNP0791 SNP0824 SNP0787 SNP0819 SNP0839 SNP0813 SNP0803 SNP0874 SNP0876 SNP0851 SNP0794 SNP0814 SNP0827 SNP0788 SNP0837 SNP0832 SNP0879 SNP0817 SNP0852 SNP0815 SNP0802 SNP0857 SNP0875 SNP0818 SNP0809 SNP0835 SNP0800 SNP0878 SNP0801 SNP0786 SNP0870 SNP0868 SNP0844 SNP0855 SNP0848 SNP0798 SNP0869 SNP0822 SNP0872 SNP0867 SNP0808 SNP0861 SNP0838 SNP0883 SNP0826 SNP0836 SNP0785 SNP0834 SNP0820 SNP0833 SNP0865 SNP0840 SNP0862 SNP0810

\$OUT.snp.mac\$GENE_10

SNP0885 SNP0908 SNP0957 SNP0937 SNP0886 SNP0940 SNP0922 SNP0980 199.3927 191.5323 206.0606 224.3461 190.0407 205.8527 207.4522 187.6892 SNP0910 SNP0938 SNP0975 SNP0965 SNP0889 SNP0929 SNP0953 SNP0921

```
176.5893 205.2578 181.0865 205.6738 184.7390 210.7396 195.5645 189.1348
 SNP0916 SNP0904 SNP0915 SNP0913 SNP0949 SNP0890
                                                    SNP0933 SNP0969
219.7581 214.3579 200.0000 217.3038 188.3182 194.7262 214.3579 223.2323
                                            SNP0950
 SNP0934 SNP0960 SNP0956 SNP0963 SNP0895
                                                     SNP0962
                                                              SNP0923
176.1134 208.9249 196.1577 181.4516 180.4435 200.4028 186.6126 196.5552
 SNP0914 SNP0959 SNP0897 SNP0971
                                   SNP0968
                                            SNP0954
                                                     SNP0958
189.0799 207.7393 192.1132 179.9798 202.2245 195.9596 184.2105 198.5816
 SNP0935 SNP0899 SNP0926 SNP0943 SNP0976 SNP0955
                                                     SNP0946
                                                              SNP0978
184.4758 205.0761 190.3323 194.5838 218.1448 204.6606 203.2520 202.4291
 SNP0917 SNP0901 SNP0907 SNP0909 SNP0948
                                            SNP0939
                                                     SNP0906
                                                              SNP0977
178.6075 228.6002 192.3464 194.7262 204.6371 183.7563 201.6211 201.4099
 SNP0894 SNP0936 SNP0920 SNP0984 SNP0981
                                            SNP0931
                                                     SNP0928
                                                              SNP0912
210.1010 203.6290 212.1212 227.4549 198.5816 185.4103 196.3746 226.3959
 SNP0952 SNP0924 SNP0919 SNP0925
                                   SNP0930
                                            SNP0941
                                                     SNP0974
                                                              SNP0903
200.8155 229.5248 187.3112 208.4592 183.5700 212.4874 171.3710 191.1021
 SNP0972 SNP0905 SNP0979 SNP0982 SNP0932 SNP0942
                                                     SNP0973
                                                             SNP0892
185.2971 212.5506 200.4028 184.6620 198.9848 200.2022 195.5420 195.9799
 SNP0898 SNP0966 SNP0911 SNP0970 SNP0918
                                            SNP0967
                                                     SNP0951
                                                              SNP0964
200.2012 213.7097 201.0050 218.5297 198.1800 184.4758 201.0101 207.8708
SNP0947 SNP0944 SNP0891 SNP0961 SNP0887
                                            SNP0927
                                                     SNP0896
210.8981 177.8894 191.7255 170.7071 206.8618 223.9108 207.8708 205.8527
 SNP0888 SNP0900 SNP0893 SNP0983
208.4592 188.8889 224.9240 202.2245
```

```
attr(,"class")
[1] "SKAT_SSD_ALL"
```

To use custom weight, you need to make a weight file and read it using "Read_SNP_WeightFile" function. The weight file should have two columns, SNP ID and weight values. The output object of "Read_SNP_WeightFile" can be used as a parameter in SKAT.SSD functions

```
> # Custom weight
```

- > # File: Example1_Weight.txt
- > obj.SNPWeight<-Read_SNP_WeightFile("./Example1_Weight.txt")
- > out<-SKAT.SSD.All(SSD.INFO, obj, obj.SNPWeight=obj.SNPWeight)

> out

\$results

	${\tt SetID}$	P.value	N.Marker.All	N.Marker.Test
1	GENE_01	0.58647860	94	94
2	GENE_02	0.03286684	84	84
3	GENE_03	0.25752493	108	108
4	GENE_04	0.18486050	101	101
5	GENE 05	0 43670123	103	103

6	GENE_06	0.98039703	94	94
7	GENE_07	0.12460640	104	104
8	GENE_08	0.78814493	96	96
9	GENE_09	0.80206141	100	100
10	GENE_10	0.34070404	100	100

\$P.value.Resampling NULL

\$OUT.snp.mac

\$OUT.snp.mac\$GENE_01

SNP0056	SNP0083	SNP0035	SNP0027	SNP0037	SNP0011	SNP0071	SNP0033	SNP0025	SNP0088
217	219	188	214	192	183	193	186	195	214
SNP0014	SNP0036	SNP0074	SNP0017	SNP0016	SNP0022	SNP0087	SNP0094	SNP0057	SNP0028
180	197	200	199	191	204	217	221	199	202
SNP0058	SNP0054	SNP0031	SNP0046	SNP0062	SNP0082	SNP0012	SNP0093	SNP0050	SNP0068
226	210	202	180	204	221	214	204	189	190
SNP0021	SNP0085	SNP0089	SNP0001	SNP0052	SNP0066	SNP0090	SNP0092	SNP0061	SNP0029
190	226	199	226	203	186	179	193	172	212
SNP0042	SNP0026	SNP0002	SNP0013	SNP0043	SNP0044	SNP0080	SNP0059	SNP0048	SNP0077
191	219	206	191	205	192	211	200	199	200
SNP0049	SNP0039	SNP0067	SNP0076	SNP0003	SNP0018	SNP0040	SNP0079	SNP0009	SNP0024
200	217	198	230	193	180	199	209	186	179
SNP0070	SNP0084	SNP0055	SNP0007	SNP0015	SNP0064	SNP0065	SNP0075	SNP0086	SNP0023
197	210	218	209	190	191	187	211	183	193
SNP0010	SNP0019	SNP0081	SNP0008	SNP0004	SNP0072	SNP0047	SNP0078	SNP0006	SNP0060
203	199	191	188	207	205	187	213	205	218
SNP0032	SNP0030	SNP0005	SNP0053	SNP0069	SNP0034	SNP0041	SNP0073	SNP0091	SNP0051
209	183	195	204	184	212	181	195	197	226
SNP0020	SNP0063	SNP0045	SNP0038						
017	101	വാഠ	206						

\$OUT.snp.mac\$GENE_02 SNP0167 SNP0165 SNP0172 SNP0124 SNP0115 SNP0112 SNP0174 SNP0121 SNP0103 SNP0116 SNP0141 SNP0133 SNP0134 SNP0149 SNP0099 SNP0161 SNP0095 SNP0169 SNP0164 SNP0097 SNP0143 SNP0148 SNP0114 SNP0173 SNP0160 SNP0136 SNP0108 SNP0109 SNP0105 SNP0118 SNP0150 SNP0153 SNP0126 SNP0162 SNP0119 SNP0111 SNP0129 SNP0142 SNP0145 SNP0132 SNP0177 SNP0163 SNP0107 SNP0100 SNP0154 SNP0178 SNP0146 SNP0101 SNP0144 SNP0171 SNP0140 SNP0139 SNP0098 SNP0110 SNP0147 SNP0131 SNP0137 SNP0113 SNP0096 SNP0156

SNP0166							SNP0157		
196	197	210	208	180	202	196	191	189	200
SNP0106	SNP0130	SNP0176	SNP0168			SNP0170	SNP0102	SNP0128	SNP0159
203	208	209	211	199	191	190	194	188	197
SNP0122	SNP0123	SNP0155	SNP0125						
166	200	239	203						
_	o.mac\$GE1								
SNP0254	SNP0273	SNP0199	SNP0266	SNP0195	SNP0186		SNP0256	SNP0236	SNP0214
219	197	220	196	183	212	202	206	214	195
SNP0196	SNP0225	SNP0224	SNP0270	SNP0188	SNP0209	SNP0204	SNP0264	SNP0233	SNP0279
186	207	221	198	183	211	214	196	200	189
SNP0238	SNP0250	SNP0267	SNP0226	SNP0275	SNP0205	SNP0280	SNP0286	SNP0207	SNP0206
205	213	231	234	185	205	199	216	213	197
SNP0222	SNP0272	SNP0245	SNP0232	SNP0241	SNP0265	SNP0230	SNP0249	SNP0269	SNP0284
202	207	206	187	220	181	195	171	207	194
SNP0262	SNP0244	SNP0283	SNP0240	SNP0218	SNP0235	SNP0237	SNP0247	SNP0242	SNP0197
192	200	188	194	212	198	190	203	185	195
SNP0210	SNP0255	SNP0278	SNP0219	SNP0276	SNP0190	SNP0277	SNP0200	SNP0179	SNP0229
193	176	211	177	203	187	199	199	195	170
SNP0183	SNP0180	SNP0194	SNP0189	SNP0212	SNP0228	SNP0202	SNP0215	SNP0261	SNP0274
186	197	212	193	200	200	220	188	179	209
SNP0223	SNP0282	SNP0239	SNP0271	SNP0227	SNP0246	SNP0285	SNP0198	SNP0217	SNP0213
214	202	193	183	193	202	217	214	188	201
SNP0184	SNP0187	SNP0193	SNP0253	SNP0251	SNP0185	SNP0201	SNP0182	SNP0258	SNP0281
170	200	183	216	196	212	186	210	202	190
SNP0234	SNP0216	SNP0211	SNP0191	SNP0192	SNP0260	SNP0221	SNP0257	SNP0181	SNP0252
184	190	208	217	207	219	199	216	193	213
SNP0243	SNP0208	SNP0259	SNP0268	SNP0203	SNP0248	SNP0231	SNP0263		
188	195	198	191	210	198	183	220		
\$OUT.snp	o.mac\$GE1	VE_04							
SNP0303	SNP0362	SNP0387	SNP0346	SNP0348	SNP0332	SNP0313	SNP0288	SNP0309	SNP0329
206	207	223	194	191	207	203	190	212	218
SNP0377	SNP0300	SNP0320	SNP0347	SNP0290	SNP0344	SNP0319	SNP0343	SNP0339	SNP0304
194	202	188	200	214	188	206	199	203	187
SNP0356	SNP0340	SNP0370	SNP0327	SNP0351	SNP0335	SNP0314	SNP0380	SNP0336	SNP0333
214	218	207	204	201	208	206	194	208	214
SNP0306	SNP0334	SNP0330	SNP0373	SNP0297	SNP0305	SNP0341	SNP0357	SNP0317	SNP0302
209	199	197	217	212	214	202	210	191	195
SNP0299	SNP0367	SNP0350	SNP0354	SNP0324	SNP0352	SNP0382	SNP0383	SNP0301	SNP0295
184	215	157	200	217	209	169	217	239	208
SNP0315	SNP0359	SNP0307	SNP0371	SNP0310	SNP0366	SNP0386	SNP0379	SNP0378	SNP0372
190	216	194	219	199	177	191	192	195	205
SNP0321	SNP0385	SNP0293	SNP0376	SNP0363	SNP0308	SNP0318	SNP0323	SNP0287	SNP0381

191	211	192	211	205	201	203	211	193	197
		SNP0291							
213	190	188	200	212	208	198	198	211	187
		SNP0322							
216	191	196	222	196	209	207	211	190	201
		SNP0361							
190	193	186	192	166	190	223	194	222	184
SNP0316	193	100	192	100	190	223	194	222	104
214									
214									
\$NIT snr	o.mac\$GE1	JF 05							
-	•	SNP0404	SNP0466	SNP0462	SNP0429	SNP0410	SNP0419	SNP0409	SNP0416
184	214	199	213	171	183	189	220	197	174
		SNP0408							
183	197	220	197	216	202	177	216	207	211
		SNP0486							
182	178	198	215	182	182	210	206	199	205
		SNP0447							
222	213	212	202	205	185	212	201	225	218
		SNP0452							
207	205	177	211	213	195	193	240	194	188
		SNP0481							
183	199	174	188	208	196	208	203	187	196
		SNP0428							
188	197	203	199	195	193	216	192	197	201
		SNP0446							
202	199	198	199	207	189	201	180	206	177
		SNP0438							
190	222	197	205	169	177	202	196	201	207
		SNP0464							
181	193	208	215	201	219	196	195	211	181
	SNP0448		210	201	210	100	100		101
214	201	204							
211	201	201							
\$OUT snr	o.mac\$GE1	JF. 06							
-	•	SNP0517	SNP0518	SNP0525	SNP0568	SNP0550	SNP0554	SNP0523	SNP0542
219	186	216			200				199
		SNP0493							
200	198	171			223			209	203
		SNP0582							
201	206	188			185	192		196	225
		SNP0512							
195	177	199			209			172	187
		SNP0526							
199	205				227				184
100	200	1.0	202	1.0	221	210	221	220	101

SNP0547	SNP0552	SNP0508	SNP0535	SNP0515	SNP0529	SNP0539	SNP0565	SNP0584	SNP0546
200	202	193	194	177	196	209	198	180	189
SNP0553	SNP0562	SNP0510	SNP0499	SNP0502	SNP0505	SNP0514	SNP0513	SNP0578	SNP0570
213	179	197	191	209	187	195	225	219	221
SNP0581	SNP0496	SNP0548	SNP0575	SNP0540	SNP0545	SNP0530	SNP0538	SNP0559	SNP0497
213	209	193	205	193	173	183	189	208	202
SNP0557	SNP0563	SNP0511	SNP0495	SNP0583	SNP0536	SNP0516	SNP0528	SNP0509	SNP0561
201	189	199	214	201	218	200	192	221	213
SNP0492	SNP0567	SNP0506	SNP0556						
202	211	183	185						
202	211	100	100						
\$OUT.snp	o.mac\$GE1	NE_07							
SNP0609	SNP0649	SNP0667	SNP0685	SNP0661	SNP0597	SNP0598	SNP0623	SNP0636	SNP0603
187	185	219	201	191	212	211	207	229	205
SNP0659	SNP0657	SNP0684	SNP0616	SNP0630	SNP0629	SNP0612	SNP0677	SNP0652	SNP0672
211	211	182	192	186	193	207	200	208	222
SNP0621	SNP0670	SNP0643	SNP0619	SNP0644		SNP0618	SNP0655	SNP0656	SNP0653
216	215	214	187	216	224	188	197	191	203
		SNP0640				SNP0611			
229	203	218	201	147	202	195	211	209	208
		SNP0607							
188	193	193	216	176	209	199	198	205	194
		SNP0669							
205	202	192	206	181	190	204	180	193	201
		SNP0651							
193	198	198	194	205	211	201	206	194	181
		SNP0624							
213	194	213	228	190	196	186	215	213	180
		SNP0682							
199	192	187	209	205	225	196	214	196	199
		SNP0665							
192	167	217	204	205	202	207	210	210	190
		SNP0605							
185	211	195	179						
\$OUT.snr	o.mac\$GE1	NE_08							
_		SNP0738	SNP0733	SNP0779	SNP0732	SNP0778	SNP0703	SNP0756	SNP0705
194	195	200	196	214	209	201	200	190	194
		SNP0765							
233	205	219	191	189	201	186	198	231	184
		SNP0707							
189	179	175			193				212
		SNP0696							
198	207	205	185	211	191	189	206		182
		SNP0722							
DMI.OLOT	DINLOLIO	DMLOIZZ	DMI_0147	PMI_0199	PML 0009	DML0199	D111_0120	DIMILOLOI	DINT_0100

201	202	188	200	200	199	192	234	213	200		
SNP0762	SNP0784	SNP0706	SNP0744	SNP0757	SNP0776	SNP0760	SNP0724	SNP0751	SNP0691		
195	208	181	188	207	198	196	197	193	178		
SNP0752	SNP0750	SNP0721	SNP0704	SNP0701	SNP0713	SNP0780	SNP0743	SNP0770	SNP0718		
188	185	188	213	199	195	212	182	212	221		
SNP0782	SNP0774	SNP0737	SNP0745	SNP0769	SNP0723	SNP0693	SNP0716	SNP0758	SNP0694		
175	233	218	191	225	216	201	214	181	195		
SNP0764	SNP0767	SNP0719	SNP0739	SNP0754	SNP0783	SNP0700	SNP0759	SNP0717	SNP0728		
217	194	201	193	201	225	197	194	181	191		
SNP0736	SNP0690	SNP0712	SNP0692	SNP0698	SNP0709						
217	223	200	217	191	221						
\$OUT.snp.mac\$GENE_09											
-			SMD0816	CNDUSOO	SMD0881	GMDU83U	QNDOQ11	SNP0807	GMDUSES		
190	183	182	197	205	202	212		195	194		
								SNP0828			
193	219	198	203	182	228	185	217	193	207		
								SNP0804			
188	217	196	207	203	189	215	211	201	194		
								SNP0873			
202	179	212	175	207	215	186	198	199	191		
SNP0792	SNP0831							SNP0787	SNP0819		
192	210	215	217	208	193	187	202	190	197		
SNP0839	SNP0813	SNP0803	SNP0874	SNP0876	SNP0851	SNP0794	SNP0814	SNP0827	SNP0788		
211	201	194	224	216	204	194	212	181	205		
SNP0837	SNP0832	SNP0879	SNP0817	SNP0852	SNP0815	SNP0802	SNP0857	SNP0875	SNP0818		
198	186	213	225	214	203	211	194	171	207		
SNP0809	SNP0835	SNP0800	SNP0878	SNP0801	SNP0786	SNP0870	SNP0868	SNP0844	SNP0855		
187	185	192	231	187	232	204	204	203	193		
SNP0848	SNP0798	SNP0869	SNP0822	SNP0872	SNP0867	SNP0808	SNP0861	SNP0838	SNP0883		
175	195	196	188	230	212	191	201	196	183		
SNP0826	SNP0836	SNP0785	SNP0834	SNP0820	SNP0833	SNP0865	SNP0840	SNP0862	SNP0810		
193	207	203	209	213	226	193	194	220	201		
\$OUT.snr	o.mac\$GE1	JF. 10									
_			957 SNP(0937 SNI	90886 SI	NP0940	SNP0922	SNP0980			
199.3927	7 191.532	23 206.06	606 224.3	3461 190	.0407 209	5.8527 2	07.4522	187.6892			
			975 SNP(
176.5893	3 205.257	78 181.08	365 205.6	5738 184	.7390 210	0.7396 1	95.5645	189.1348			
SNP0916	3 SNP090	04 SNPOS	915 SNP(0913 SNF	90949 SI	NP0890	SNP0933	SNP0969			
219.7581	1 214.357	79 200.00	000 217.3	3038 188	.3182 194	1.7262 2	14.3579	223.2323			
SNP0934	4 SNP096	SO SNPOS	956 SNP(0963 SNI	P0895 SI	NP0950	SNP0962	SNP0923			
176.1134	4 208.924	19 196.19	577 181.4	4516 180.	.4435 200	0.4028 1	86.6126	196.5552			

SNP0914 SNP0959 SNP0897 SNP0971 SNP0968 SNP0954 SNP0958 SNP0902 189.0799 207.7393 192.1132 179.9798 202.2245 195.9596 184.2105 198.5816

```
SNP0935 SNP0899 SNP0926 SNP0943 SNP0976 SNP0955
                                                     SNP0946
                                                              SNP0978
184.4758 205.0761 190.3323 194.5838 218.1448 204.6606 203.2520 202.4291
 SNP0917 SNP0901 SNP0907 SNP0909 SNP0948
                                            SNP0939
                                                     SNP0906
                                                              SNP0977
178.6075 228.6002 192.3464 194.7262 204.6371 183.7563 201.6211 201.4099
 SNP0894 SNP0936 SNP0920 SNP0984 SNP0981 SNP0931
                                                     SNP0928
                                                              SNP0912
210.1010 203.6290 212.1212 227.4549 198.5816 185.4103 196.3746 226.3959
 SNP0952 SNP0924 SNP0919 SNP0925
                                   SNP0930
                                            SNP0941
                                                     SNP0974
200.8155 229.5248 187.3112 208.4592 183.5700 212.4874 171.3710 191.1021
 SNP0972 SNP0905 SNP0979 SNP0982 SNP0932 SNP0942
                                                     SNP0973
                                                             SNP0892
185.2971 212.5506 200.4028 184.6620 198.9848 200.2022 195.5420 195.9799
 SNP0898 SNP0966 SNP0911 SNP0970 SNP0918 SNP0967
                                                     SNP0951
                                                              SNP0964
200.2012 213.7097 201.0050 218.5297 198.1800 184.4758 201.0101 207.8708
SNP0947 SNP0944 SNP0891 SNP0961
                                   SNP0887 SNP0927
                                                     SNP0896
210.8981 177.8894 191.7255 170.7071 206.8618 223.9108 207.8708 205.8527
 SNP0888 SNP0900 SNP0893 SNP0983
208.4592 188.8889 224.9240 202.2245
```

```
attr(,"class")
[1] "SKAT_SSD_ALL"
```

The output object of SKAT.SSD.All has an output dataframe object "results". You can save it using write.table function.

```
> output.df = out$results
> write.table(output.df, file="./save.txt", col.names=TRUE, row.names=FALSE)
>
```

If more than one gene/SNP sets are to be tested, multiple test should be adjusted to control for family-wise error rate. It can be done by the bonferroni correction. If gene/SNP sets are correlated, however, this approach can be conservative. Alternatively, you can directly control family wise error rate (FWER) using the resampling method.

```
> obj<-SKAT_Null_Model(y ~ 1, out_type="C", n.Resampling=1000, type.Resampling="bootstrap")
> out<-SKAT.SSD.All(SSD.INFO, obj)
> # No gene is significant with controling FWER = 0.05
> Resampling_FWER(out,FWER=0.05)
$result
NULL
$n
```

[1] 0

\$ID NULL

```
> # 1 gene is significant with controling FWER = 0.5
> Resampling_FWER(out,FWER=0.5)
$result
             P.value N.Marker.All N.Marker.Test
    SetID
2 GENE_02 0.06245208
                                84
$n
[1] 1
$ID
[1] 2
  "SKAT.SSD.OneSet" or "SKAT.SSD.OneSet SetIndex" functions can be used to test for a single
gene/SNP set. Alternatively, you can obtain a genotype matrix using "Get Genotypes SSD"
function and then run SKAT.
> obj<-SKAT_Null_Model(y ~ 1, out_type="C")
> # test the second gene
> id<-2
> SetID<-SSD.INFO$SetInfo$SetID[id]
> SKAT.SSD.OneSet(SSD.INFO,SetID, obj)$p.value
[1] 0.06245208
> SKAT.SSD.OneSet_SetIndex(SSD.INFO,id, obj)$p.value
[1] 0.06245208
> # test the second gene with the logistic weight.
> Z<-Get_Genotypes_SSD(SSD.INFO, id)
> weights = Get_Logistic_Weights(Z, par1=0.07, par2=150)
> SKAT(Z, obj, weights=weights)$p.value
[1] 0.7227001
>
   SKAT_CommonRare function also can be used with SSD files.
> # test all genes in SSD file
> obj<-SKAT_Null_Model(y ~ X1 + X2, out_type="C")</pre>
> out<-SKAT_CommonRare.SSD.All(SSD.INFO, obj)</pre>
> out
```

φ	1
*regii	ゖたら

	${\tt SetID}$	P.value	Q	N.Marker.All	${\tt N.Marker.Test}$	N.Marker.Rare
1	GENE_01	0.69065787	7793.492	94	94	0
2	GENE_02	0.01627559	10487.653	84	84	0
3	GENE_03	0.57047824	9340.646	108	108	0
4	GENE_04	0.31381746	9743.714	101	101	0
5	GENE_05	0.21088057	10224.331	103	103	0
6	GENE_06	0.91250955	6734.116	94	94	0
7	GENE_07	0.26552996	10193.704	104	104	0
8	GENE_08	0.64072991	8087.342	96	96	0
9	GENE_09	0.65984552	8376.438	100	100	0
10	GENE_10	0.28938130	9502.883	100	100	0

N.Marker.Common

1	94
2	84
3	108
4	101
5	103
6	94
7	104
8	96
9	100
10	100

\$P.value.Resampling
NULL

\$OUT.snp.mac

\$OUT.snp.mac\$GENE_01

SNP0056 SNP0083 SNP0035 SNP0027 SNP0037 SNP0011 SNP0071 SNP0033 SNP0025 SNP0088 SNP0014 SNP0036 SNP0074 SNP0017 SNP0016 SNP0022 SNP0087 SNP0094 SNP0057 SNP0028 SNP0058 SNP0054 SNP0031 SNP0046 SNP0062 SNP0082 SNP0012 SNP0093 SNP0050 SNP0068 SNP0021 SNP0085 SNP0089 SNP0001 SNP0052 SNP0066 SNP0090 SNP0092 SNP0061 SNP0029 SNP0042 SNP0026 SNP0002 SNP0013 SNP0043 SNP0044 SNP0080 SNP0059 SNP0048 SNP0077 SNP0049 SNP0039 SNP0067 SNP0076 SNP0003 SNP0018 SNP0040 SNP0079 SNP0009 SNP0024 SNP0070 SNP0084 SNP0055 SNP0007 SNP0015 SNP0064 SNP0065 SNP0075 SNP0086 SNP0023 SNP0010 SNP0019 SNP0081 SNP0008 SNP0004 SNP0072 SNP0047 SNP0078 SNP0006 SNP0060

SNP0032 209	SNP0030 183	SNP0005 195	SNP0053 204	SNP0069 184	SNP0034 212	SNP0041 181	SNP0073 195	SNP0091 197	SNP0051 226
SNP0020	SNP0063	SNP0045	SNP0038						
217	191	228	206						
\$OUT.snj	o.mac\$GEN	VE_02							
SNP0167	SNP0165	SNP0172	SNP0124	SNP0115	SNP0112	SNP0174	SNP0121	SNP0103	SNP0116
184	197	216	208	198	184	210	173	189	201
SNP0141	SNP0133	SNP0134	SNP0149	SNP0099	SNP0161	SNP0095	SNP0169	SNP0164	SNP0097
221	173	220	203	217	202	200	213	223	201
SNP0143	SNP0148	SNP0114	SNP0173	SNP0160	SNP0136	SNP0108	SNP0109	SNP0105	SNP0118
194	208	225	208	206	209	206	208	182	193
SNP0150	SNP0153	SNP0126	SNP0162	SNP0119	SNP0111	SNP0129	SNP0142	SNP0145	SNP0132
201	183	169	219	200	218	186	200	216	198
SNP0177	SNP0163	SNP0107	SNP0100	SNP0154	SNP0178	SNP0146	SNP0101	SNP0144	SNP0171
207	215	206	209	212	187	199	213	193	229
SNP0140	SNP0139	SNP0098	SNP0110	SNP0147	SNP0131	SNP0137	SNP0113	SNP0096	SNP0156
221	210	196	218	217	199	213	213	203	178
SNP0166	SNP0120	SNP0117	SNP0151	SNP0127	SNP0104	SNP0152	SNP0157	SNP0175	SNP0138
196	197	210	208	180	202	196	191	189	200
SNP0106	SNP0130						SNP0102	SNP0128	SNP0159
203	208	209	211	199	191	190	194	188	197
	SNP0123						-01		
166	200	239	203						
100	200	200	200						
\$OUT.sn:	o.mac\$GEN	IE 03							
_			SNP0266	SNP0195	SNP0186	SNP0220	SNP0256	SNP0236	SNP0214
219	197	220	196	183	212	202	206	214	195
							SNP0264		
186	207	221	198	183	211	214	196	200	189
							SNP0286		
205	213	231	234	185	205	199	216	213	197
							SNP0249		
202	207	206	187		181	195	171	207	194
							SNP0247		
192	200	188				190	203	185	195
							SNP0200		
193	176	211	177	203	187	199	199	195	170
							SNP0215		
186	197	212	193	200	200	220	188	179	209
							SNP0198		
214	202	193	183	193	202	217	214	188	201
							SNP0182		
170	200	183				186		202	190
SNP0234	SNP0216	SNP0211	SNP0191	SNP0192	SNP0260	SNP0221	SNP0257	SNP0181	SNP0252

184	190	208	217	207	219	199	216	193	213
SNP0243	SNP0208	SNP0259	SNP0268	SNP0203	SNP0248	SNP0231	SNP0263		
188	195	198	191	210	198	183	220		
\$OUT.snp	o.mac\$GE1	VE_04							
SNP0303	SNP0362	SNP0387	SNP0346	SNP0348	SNP0332	SNP0313	SNP0288	SNP0309	SNP0329
206	207	223	194	191	207	203	190	212	218
SNP0377	SNP0300	SNP0320	SNP0347	SNP0290	SNP0344	SNP0319	SNP0343	SNP0339	SNP0304
194	202	188	200	214	188	206	199	203	187
SNP0356	SNP0340	SNP0370	SNP0327	SNP0351	SNP0335	SNP0314	SNP0380	SNP0336	SNP0333
214	218	207	204	201	208	206	194	208	214
SNP0306	SNP0334	SNP0330	SNP0373	SNP0297	SNP0305	SNP0341	SNP0357	SNP0317	SNP0302
209	199	197	217	212	214	202	210	191	195
SNP0299	SNP0367	SNP0350	SNP0354	SNP0324	SNP0352	SNP0382	SNP0383	SNP0301	SNP0295
184	215	157	200	217	209	169	217	239	208
SNP0315	SNP0359	SNP0307	SNP0371	SNP0310	SNP0366	SNP0386	SNP0379	SNP0378	SNP0372
190	216	194	219	199	177	191	192	195	205
SNP0321	SNP0385	SNP0293	SNP0376	SNP0363	SNP0308	SNP0318	SNP0323	SNP0287	SNP0381
191	211	192	211	205	201	203	211	193	197
SNP0364	SNP0328	SNP0291	SNP0349	SNP0289	SNP0337	SNP0353	SNP0345	SNP0375	SNP0311
213	190	188	200	212	208	198	198	211	187
SNP0326	SNP0358	SNP0322	SNP0292	SNP0298	SNP0369	SNP0360	SNP0355	SNP0338	SNP0384
216	191	196	222	196	209	207	211	190	201
SNP0294	SNP0296	SNP0361	SNP0325	SNP0312	SNP0374	SNP0331	SNP0342	SNP0368	SNP0365
190	193	186	192	166	190	223	194	222	184
SNP0316									
214									
\$OUT.snp	o.mac\$GE1	VE_05							
SNP0460	SNP0474	SNP0404	SNP0466	SNP0462	SNP0429	SNP0410	SNP0419	SNP0409	SNP0416
184	214	199	213	171	183	189	220	197	174
SNP0400	SNP0469	SNP0408	SNP0473	SNP0424	SNP0401	SNP0392	SNP0422	SNP0468	SNP0395
183	197	220	197	216	202	177	216	207	211
SNP0476	SNP0488	SNP0486	SNP0435	SNP0458	SNP0467	SNP0449	SNP0480	SNP0478	SNP0394
182	178	198	215	182	182	210	206	199	205
SNP0442	SNP0456	SNP0447	SNP0421	SNP0444	SNP0405	SNP0414	SNP0413	SNP0475	SNP0477
222	213	212	202	205	185	212	201	225	218
SNP0450	SNP0423	SNP0452	SNP0426	SNP0403	SNP0490	SNP0402	SNP0437	SNP0445	SNP0465
207	205	177	211	213	195	193	240	194	188
SNP0430	SNP0393	SNP0481	SNP0484	SNP0439	SNP0454	SNP0389	SNP0390	SNP0459	SNP0487
183	199	174	188	208	196	208	203	187	196
SNP0470	SNP0399	SNP0428	SNP0427	SNP0472	SNP0455	SNP0397	SNP0391	SNP0453	SNP0398
188	197	203	199	195	193	216	192	197	201
SNP0417	SNP0479	SNP0446	SNP0388	SNP0407	SNP0412	SNP0431	SNP0415	SNP0441	SNP0461
202	199	198	199	207	189	201	180	206	177

	SNP0420								
190	222	197	205	169	177	202	196	201	207
	SNP0443								
181	193	208	215	201	219	196	195	211	181
	SNP0448								
214	201	204							
ΦΩΙΙΤ αna	p.mac\$GEI	IE OG							
_	SNP0534		CMDUE18	GMDUESE	QMD0E68	CMDUEEU	GMDUEE4	GMDUEJS	GMDUE/10
219	186	216	197	197	200	192	215	190	199
	SNP0503								
200	198	171	200	179	223	218	215	209	203
	SNP0522								
201	206	188						196	225
			191	200	185	192	206		
	SNP0521								
195	177	199	215	205	209	188	206	172	187
	SNP0537								
199	205	178	202	173	227	218	221	223	184
	SNP0552								
200	202	193	194	177	196	209	198	180	189
	SNP0562								
213	179	197	191	209	187	195	225	219	221
SNP0581	SNP0496	SNP0548	SNP0575	SNP0540	SNP0545	SNP0530	SNP0538	SNP0559	
213	209	193	205	193	173	183	189	208	202
SNP0557	SNP0563	SNP0511	SNP0495	SNP0583	SNP0536	SNP0516	SNP0528	SNP0509	SNP0561
201	189	199	214	201	218	200	192	221	213
SNP0492	SNP0567	SNP0506	SNP0556						
202	211	183	185						
\$OUT.sn	p.mac\$GEl	VE_07							
-	SNP0649		SNP0685	SNP0661	SNP0597	SNP0598	SNP0623	SNP0636	SNP0603
187	185	219	201	191	212	211	207	229	205
SNP0659	SNP0657	SNP0684							SNP0672
211	211	182	192	186	193	207	200	208	222
	SNP0670					SNP0618	SNP0655	SNP0656	
216	215	214	187					191	203
	SNP0663								
229	203	218	201	147		195	211	209	208
	SNP0660								
188	193	193		176					194
	SNP0687								
205	202	192	206	181		204	180	193	201
	SNP0626								
193	198	198							181
2NP0021	SNP0588	5NPU624	9NL0072	2ML0038	9NL09AA	9NL0032	2NL02A3	9ML02AQ	5NPU645

213	194	213	228	190	196	186	215	213	180
SNP0675	SNP0631	SNP0682							SNP0595
199	192	187	209	205	225	196	214	196	199
SNP0680	SNP0638	SNP0665	SNP0637	SNP0622	SNP0647	SNP0654	SNP0601	SNP0585	SNP0646
192	167	217	204	205	202	207	210	210	190
SNP0650	SNP0614	SNP0605	SNP0590						
185	211	195	179						
\$OUT.snp	o.mac\$GE	NE_08							
SNP0740	SNP0720	SNP0738	SNP0733	SNP0779	SNP0732	SNP0778	SNP0703	SNP0756	SNP0705
194	195	200	196	214	209	201	200	190	194
SNP0727	SNP0734	SNP0765	SNP0772	SNP0699	SNP0775	SNP0741	SNP0763	SNP0749	SNP0715
233	205	219	191	189	201	186	198	231	184
SNP0725	SNP0755	SNP0707	SNP0747	SNP0702	SNP0748	SNP0714	SNP0777	SNP0771	SNP0726
189	179	175	199	206	193	197	189	191	212
SNP0773	SNP0697	SNP0696	SNP0766	SNP0708	SNP0695	SNP0711	SNP0761	SNP0746	SNP0729
198	207	205	185	211	191	189	206	221	182
SNP0781	SNP0710	SNP0722	SNP0742	SNP0753	SNP0689	SNP0735	SNP0730	SNP0731	SNP0768
201	202	188	200	200	199	192	234	213	200
SNP0762	SNP0784	SNP0706	SNP0744	SNP0757	SNP0776	SNP0760	SNP0724	SNP0751	SNP0691
195	208	181	188	207	198	196	197	193	178
SNP0752	SNP0750	SNP0721	SNP0704	SNP0701	SNP0713	SNP0780	SNP0743	SNP0770	SNP0718
188	185	188	213	199	195	212	182	212	221
SNP0782	SNP0774	SNP0737	SNP0745	SNP0769	SNP0723	SNP0693	SNP0716	SNP0758	SNP0694
175	233	218	191	225	216	201	214	181	195
SNP0764	SNP0767	SNP0719	SNP0739	SNP0754	SNP0783	SNP0700	SNP0759	SNP0717	SNP0728
217	194	201	193	201	225	197	194	181	191
SNP0736	SNP0690	SNP0712	SNP0692	SNP0698	SNP0709				
217	223	200	217	191	221				
_	o.mac\$GE								
SNP0795	SNP0859	SNP0845	SNP0816	SNP0829	SNP0881	SNP0830	SNP0811	SNP0807	SNP0853
190	183	182	197	205	202	212	193	195	194
SNP0841	SNP0796	SNP0880	SNP0854	SNP0821	SNP0797	SNP0882	SNP0843	SNP0828	SNP0789
193	219	198	203	182		185			207
SNP0856	SNP0884	SNP0812	SNP0799	SNP0825	SNP0850	SNP0805	SNP0877	SNP0804	SNP0864
188	217	196	207	203	189	215	211	201	194
SNP0842	SNP0871	SNP0790	SNP0806	SNP0863	SNP0793	SNP0846	SNP0849	SNP0873	SNP0823
202	179	212	175	207	215	186	198	199	191
SNP0792	SNP0831	SNP0866	SNP0858	SNP0847	SNP0860	SNP0791	SNP0824	SNP0787	SNP0819
192	210	215	217	208	193	187	202	190	197
SNP0839	SNP0813	SNP0803	SNP0874	SNP0876	SNP0851	SNP0794	SNP0814	SNP0827	SNP0788
211	201	194	224	216	204	194	212	181	205
SNP0837	SNP0832	SNP0879	SNP0817	SNP0852	SNP0815	SNP0802	SNP0857	SNP0875	SNP0818
198	186	213	225	214	203	211	194	171	207

```
SNP0809 SNP0835 SNP0800 SNP0878 SNP0801 SNP0786 SNP0870 SNP0868 SNP0844 SNP0855
    187
            185
                     192
                             231
                                      187
                                              232
                                                       204
                                                               204
                                                                        203
                                                                                 193
SNP0848 SNP0798 SNP0869 SNP0822 SNP0872 SNP0867 SNP0808 SNP0861 SNP0838 SNP0883
    175
            195
                     196
                             188
                                      230
                                              212
                                                       191
                                                               201
                                                                        196
                                                                                 183
SNP0826 SNP0836 SNP0785 SNP0834 SNP0820 SNP0833 SNP0865 SNP0840 SNP0862 SNP0810
    193
            207
                     203
                              209
                                      213
                                              226
                                                       193
                                                                194
                                                                        220
                                                                                 201
```

\$OUT.snp.mac\$GENE_10 SNP0885 SNP0908 SNP0957 SNP0937 SNP0886 SNP0940 SNP0922 SNP0980 199.3927 191.5323 206.0606 224.3461 190.0407 205.8527 207.4522 187.6892 SNP0910 SNP0938 SNP0975 SNP0965 SNP0889 SNP0929 SNP0953 SNP0921 176.5893 205.2578 181.0865 205.6738 184.7390 210.7396 195.5645 189.1348 SNP0916 SNP0904 SNP0915 SNP0913 SNP0949 SNP0890 SNP0933 219.7581 214.3579 200.0000 217.3038 188.3182 194.7262 214.3579 223.2323 SNP0934 SNP0960 SNP0956 SNP0963 SNP0895 SNP0950 SNP0962 176.1134 208.9249 196.1577 181.4516 180.4435 200.4028 186.6126 196.5552 SNP0914 SNP0959 SNP0897 SNP0971 SNP0968 SNP0954 SNP0958 SNP0902 189.0799 207.7393 192.1132 179.9798 202.2245 195.9596 184.2105 198.5816 SNP0935 SNP0899 SNP0926 SNP0943 SNP0976 SNP0955 SNP0946 SNP0978 184.4758 205.0761 190.3323 194.5838 218.1448 204.6606 203.2520 202.4291 SNP0917 SNP0901 SNP0907 SNP0909 SNP0948 SNP0939 SNP0906 178.6075 228.6002 192.3464 194.7262 204.6371 183.7563 201.6211 201.4099 SNP0894 SNP0936 SNP0920 SNP0984 SNP0981 SNP0931 SNP0928 SNP0912 210.1010 203.6290 212.1212 227.4549 198.5816 185.4103 196.3746 226.3959 SNP0952 SNP0924 SNP0919 SNP0925 SNP0930 SNP0941 SNP0974 SNP0903 200.8155 229.5248 187.3112 208.4592 183.5700 212.4874 171.3710 191.1021 SNP0972 SNP0905 SNP0979 SNP0982 SNP0932 SNP0942 SNP0973 185.2971 212.5506 200.4028 184.6620 198.9848 200.2022 195.5420 195.9799 SNP0898 SNP0966 SNP0911 SNP0970 SNP0918 SNP0967 SNP0951 200.2012 213.7097 201.0050 218.5297 198.1800 184.4758 201.0101 207.8708 SNP0947 SNP0944 SNP0891 SNP0961 SNP0887 SNP0927 SNP0896 SNP0945 210.8981 177.8894 191.7255 170.7071 206.8618 223.9108 207.8708 205.8527 SNP0888 SNP0900 SNP0893 SNP0983

attr(,"class")
[1] "SKAT_SSD_ALL"

After finishing to use SSD files, please close them.

208.4592 188.8889 224.9240 202.2245

> Close_SSD()

Close the opened SSD file: /private/var/folders/1n/hmqxyn1x5vz9669g58n65_f40000gn/T/RtmpoeEF0f

3.1 Plink Binary format files: SKATBinary

SKATBinary functions can also be used with plink formatted files. This section shows an example code. Example plink files can be found on the SKAT/MetaSKAT google group page.

```
> # File names
> File.Bed<-"./SKATBinary.example.bed"
> File.Bim<-"./SKATBinary.example.bim"
> File.Fam<-"./SKATBinary.example.fam"
> File.Cov<-"./SKATBinary.example.cov"
> File.SetID<-"./SKATBinary.example.SetID"
> File.SSD<-"./SKATBinary.example.SSD"
> File.Info<-"./SKATBinary.example.SSD.info"
> # Generate SSD file, and read fam and cov files
> # If you already have a SSD file, you do not need to call this function.
> Generate_SSD_SetID(File.Bed, File.Bim, File.Fam, File.SetID, File.SSD, File.Info)
Check duplicated SNPs in each SNP set
No duplicate
2000 Samples, 30 Sets, 340 Total SNPs
[1] "SSD and Info files are created!"
> FAM<-Read_Plink_FAM_Cov(File.Fam, File.Cov, Is.binary=TRUE, cov_header=FALSE)
> # open SSD files
> SSD.INFO<-Open_SSD(File.SSD, File.Info)
2000 Samples, 30 Sets, 340 Total SNPs
Open the SSD file
> # No adjustment is needed
> obj<-SKAT_Null_Model(Phenotype ~ COV1 + COV2, out_type="D", data=FAM, Adjustment=FALSE)
> # SKAT
> out.skat<-SKATBinary.SSD.All(SSD.INFO, obj, method="SKAT")
> # SKAT-0
> out.skato<-SKATBinary.SSD.All(SSD.INFO, obj, method="SKATO")
> # First 5 variant sets, SKAT
> out.skat$results[1:5,]
           P.value N.Marker.All N.Marker.Test MAC m Method.bin
  SetID
                                                                          MAP
1
      1 0.92753378
                             11
                                           11 18 17
                                                              ER 2.512149e-07
2
      2 0.24947578
                              2
                                            2
                                                3 3
                                                             ER 3.544808e-02
                              7
                                            7 19 19
3
      3 0.60706345
                                                             ER 3.312382e-08
      4 0.08566388
                             11
                                           11 19 18
                                                             ER 6.640864e-08
```

18 18

ER 2.721199e-07

5 0.63625247

The effective number of tests and QQ plots can be obtained using the minimum achievable p-values (MAP).

```
> # Effective number of test is smaller than 30 (number of variant sets)
> # Use SKAT results
> Get_EffectiveNumberTest(out.skat$results$MAP, alpha=0.05)

[1] 28
> # QQ plot
> QQPlot_Adj(out.skat$results$P.value, out.skat$results$MAP)
>
```

4 Power/Sample Size calculation.

4.1 Dataset

>

SKAT package provides a haplotype dataset (SKAT.haplotypes) which contains a haplotype matrix of 10,000 haplotypes over 200kb region (Haplotype), and a dataframe with information on each SNP. These haplotypes were simulated using a calibrated coalescent model (cosi) with mimicking linkage disequilibrium structure of European ancestry. If no haplotype data are available, this dataset can be used to compute power/sample size.

```
> data(SKAT.haplotypes)
> names(SKAT.haplotypes)
[1] "Haplotype" "SNPInfo"
> attach(SKAT.haplotypes)
```

4.2 Power/Sample Size calculation

The following example uses the haplotypes in SKAT.haplotypes with the following parameters.

- 1. Subregion length = 3k bp
- 2. Causal percent = 20%
- 3. Negative percent = 20%
- 4. For continuous traits, $\beta = c |log_{10}(MAF)|$ (BetaType = "Log") with $\beta = 2$ at MAF = 10^{-4}
- 5. For binary traits, $log(OR) = c|log_{10}(MAF)|$ (OR.Type = "Log") with OR = 2 at MAF = 10^{-4} , and 50% of samples are cases and 50% of samples are controls

```
> set.seed(500)
> out <<-Power Continuous(Hanlotype SNPInfo$CHROM POS SubReg
```

- > out.c<-Power_Continuous(Haplotype,SNPInfo\$CHROM_POS, SubRegion.Length=5000,
- + Causal.Percent= 20, N.Sim=10, MaxBeta=2, Negative.Percent=20)

```
[1] "10/10"
> out.b<-Power_Logistic(Haplotype,SNPInfo$CHROM_POS, SubRegion.Length=5000,
+ Causal.Percent= 20, N.Sim=10 ,MaxOR=7, Negative.Percent=20)
[1] "10/10"
> out.c
$Power
          0.01
                   0.001
                             1e-06
500 0.6175978 0.4876905 0.2812231
1000 0.8196568 0.6959138 0.4967577
1500 0.9260644 0.8176848 0.6047217
2000 0.9795038 0.9033846 0.6978467
2500 0.9964443 0.9611981 0.7625096
3000 0.9996061 0.9888946 0.8168844
3500 0.9999708 0.9977467 0.8687841
4000 0.9999985 0.9996697 0.9163105
4500 0.9999999 0.9999641 0.9541347
5000 1.0000000 0.9999970 0.9789134
$R.sq
[1] 0.07804945
attr(,"class")
[1] "SKAT_Power"
> out.b
$Power
          0.01
                   0.001
                              1e-06
500 0.3195274 0.1838831 0.03372994
1000 0.5729441 0.3887094 0.15492725
1500 0.7488294 0.5687846 0.25885689
2000 0.8557195 0.7085993 0.37007813
2500 0.9189064 0.8044937 0.48059575
3000 0.9569876 0.8689837 0.58421719
3500 0.9790826 0.9146539 0.67116819
4000 0.9907789 0.9475064 0.73753304
4500 0.9963200 0.9700309 0.78656221
5000 0.9986658 0.9842302 0.82447737
attr(,"class")
[1] "SKAT_Power"
```

> Get_RequiredSampleSize(out.c, Power=0.8)

```
$`alpha = 1.00e-02`
[1] 951.3587

$`alpha = 1.00e-03`
[1] 1427.385

$`alpha = 1.00e-06`
[1] 2844.741

> Get_RequiredSampleSize(out.b, Power=0.8)

$`alpha = 1.00e-02`
[1] 1739.361

$`alpha = 1.00e-03`
[1] 2476.569

$`alpha = 1.00e-06`
[1] 4677.209

>
```

In this example, N.Sim=10 was used to get the result quickly. When you run the power calculation, please increase it to more than 100. When BetaType = "Log" or OR.Type = "Log", the effect size of continuous trait and the log odds ratio of binary traits are $c|log_{10}(MAF)|$, where c is determined by Max_Beta or Max_OR. For example, c = 2/4 = 0.5 when the Max_Beta = 2. In this case, a causal variant with MAF=0.01 has $\beta = 1$. For binary traits, c = log(7)/4 = 0.486 with MAX_OR=7. And thus, a causal variant with MAF=0.01 has log OR = 0.972.

Power_Continuous_R or Power_Logistic_R functions can be used to compute power with with non-zero r.corr (ρ). Since these functions use slightly different method to compute power, power estimates from Power_Continuous_R and Power_Logistic_R can be slightly different from estimates from Power_Continuous and Power_Logistic even when r.corr=0. If you want to computer the power of SKAT-O by estimating the optimal r.corr, please use r.corr=2. The estimated optimal r.corr is

$$r.corr = p_1^2 (2p_2 - 1)^2,$$

where p_1 is the proportion of nonzero β s, and p_2 is the proportion of negative (or positive) β s among the non-zero β s.

```
> set.seed(500)
> out.c<-Power_Continuous_R(Haplotype,SNPInfo$CHROM_POS, SubRegion.Length=5000,
+ Causal.Percent= 20, N.Sim=10, MaxBeta=2,Negative.Percent=20, r.corr=2)
[1] "10/10"
> out.c
```

```
$Power
                   0.001
          0.01
                             1e-06
500 0.6143437 0.4867279 0.2821814
1000 0.8155499 0.6904465 0.4962072
1500 0.9246785 0.8124547 0.5991376
2000 0.9798723 0.9006001 0.6923563
2500 0.9967484 0.9611003 0.7558941
3000 0.9996732 0.9894869 0.8095854
3500 0.9999783 0.9980407 0.8629075
4000 0.9999990 0.9997413 0.9136032
4500 1.0000000 0.9999749 0.9542956
5000 1.0000000 0.9999981 0.9801759
$R.sq
[1] 0.07804945
$r.corr
[1] 0.0144
attr(,"class")
[1] "SKAT_Power"
> Get_RequiredSampleSize(out.c, Power=0.8)
\alpha = 1.00e-02
[1] 961.3582
\alpha = 1.00e-03
[1] 1448.959
\alpha = 1.00e-06
[1] 2910.736
```