# The Statistical Sleuth in R: Chapter 5

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January 23, 2019

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### 1 Introduction

This document is intended to help describe how to undertake analyses introduced as examples in the Third Edition of the *Statistical Sleuth* (2013) by Fred Ramsey and Dan Schafer. More information about the book can be found at http://www.proaxis.com/~panorama/home.htm. This file as well as the associated knitr reproducible analysis source file can be found at http://www.math.smith.edu/~nhorton/sleuth3.

This work leverages initiatives undertaken by Project MOSAIC (http://www.mosaic-web.org), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the mosaic package, which was written to simplify the use of R for introductory statistics courses. A short summary of the R needed to teach introductory statistics can be found in the mosaic package vignette (http://cran.r-project.org/web/packages/mosaic/vignettes/MinimalR.pdf).

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To use a package within R, it must be installed (one time), and loaded (each session). The package can be installed using the following command:

```
> install.packages('mosaic') # note the quotation marks
```

Once this is installed, it can be loaded by running the command:

```
> require(mosaic)
```

This needs to be done once per session.

In addition the data files for the *Sleuth* case studies can be accessed by installing the **Sleuth3** package.

```
> install.packages('Sleuth3') # note the quotation marks
```

```
> require(Sleuth3)
```

We also set some options to improve legibility of graphs and output.

```
> trellis.par.set(theme=col.mosaic()) # get a better color scheme
> options(digits=3)
```

The specific goal of this document is to demonstrate how to calculate the quantities described in Chapter 5: Comparisons Among Several Samples using R.

# 2 Diet and lifespan

Does restricting the diet of female mice lead to increased lifespan? This is the question addressed in case study 5.1 in the *Sleuth*.

#### 2.1 Summary statistics and graphical display

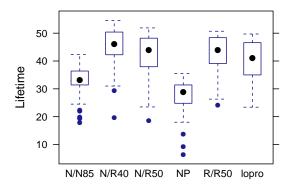
We begin by reading the data and summarizing the variables.

```
> summary(case0501)
    Lifetime
                   Diet
Min. : 6.4
                N/N85:57
 1st Qu.:31.8
                N/R40:60
Median:39.5
                N/R50:71
 Mean
        :38.8
                NP :49
 3rd Qu.:46.9
                R/R50:56
 Max.
        :54.6
                lopro:56
> favstats(Lifetime ~ Diet, data=case0501)
```

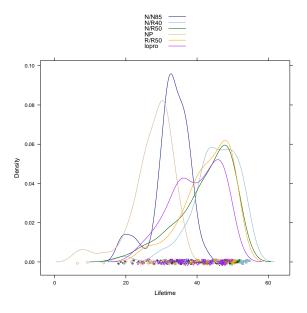
```
Diet
       min
               Q1 median
                           Q3 max mean
                                           sd n missing
1 N/N85 17.9 31.4
                    33.1 36.4 42.3 32.7 5.13 57
2 N/R40 19.6 42.3
                    46.0 50.3 54.6 45.1 6.70 60
                                                       0
3 N/R50 18.6 38.0
                    43.9 48.2 51.9 42.3 7.77 71
                                                       0
         6.4 24.8
                    28.9 31.4 35.5 27.4 6.13 49
     NP
                                                       0
5 R/R50 24.2 39.2
                    44.0 48.3 50.7 42.9 6.68 56
                                                       0
6 lopro 23.4 35.0
                    41.0 46.4 49.7 39.7 6.99 56
                                                       0
```

There were a total of 349 female mice. These mice were randomly assigned to one of 6 diets. Their lifetimes were then recorded, as shown in Display 5.2 (page 115 of the *Sleuth*).

```
> bwplot(Lifetime ~ Diet, data=case0501) # Display 5.1
```



> densityplot(~ Lifetime, groups=Diet, auto.key=TRUE, data=case0501)



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#### 2.2 One-way ANOVA

First we fit the one way analysis of variance (ANOVA) model, using all of the groups.

There is a strong statistically significant difference between the diets.

By default, the use of the linear model (regression) function displays the pairwise differences between the first group and each of the other groups. Note that the overall test of the model is the same.

```
> summary(lm(Lifetime ~ Diet, data=case0501))
Call:
lm(formula = Lifetime ~ Diet, data = case0501)
Residuals:
   Min 1Q Median 3Q
                                 Max
-25.517 -3.386 0.814 5.183 10.014
Coefficients:
          Estimate Std. Error t value Pr(>|t|)
(Intercept) 32.691 0.885 36.96 < 2e-16
DietN/R40
           12.425
                      1.235 10.06 < 2e-16
DietN/R50
            9.606
                      1.188 8.09 1.1e-14
                      1.301 -4.07 5.9e-05
DietNP
            -5.289
DietR/R50
           10.194
                      1.257
                              8.11 8.9e-15
Dietlopro
             6.994
                        1.257
                                5.57 5.2e-08
Residual standard error: 6.68 on 343 degrees of freedom
Multiple R-squared: 0.454, Adjusted R-squared: 0.446
F-statistic: 57.1 on 5 and 343 DF, p-value: <2e-16
```

The reference group is NP, followed by N/N85, lopro, N/R50, R/R50, N/R40.

#### 2.3 Pairwise comparisons

Next we used contrasts for the results on page 122, Display 5.7, and part (a) on page 115:

#### The results for (b) on page 115-116:

#### The results for (c) on page 116:

```
> # N/R40 vs N/R50 (c)
> fit.contrast(lm(Lifetime ~ Diet, data=case0501), "Diet", c(0, -1, 1, 0, 0, 0), conf.int=0.95
                       Estimate Std. Error t value Pr(>|t|) lower CI
Diet c=( 0 -1 1 0 0 0 ) -2.82
                                  1.17 -2.41 0.0166 -5.12
                      upper CI
Diet c=( 0 -1 1 0 0 0 ) -0.516
attr(,"class")
[1] "fit_contrast"
> # N/N85 vs N/R40
> fit.contrast(lm(Lifetime ~ Diet, data=case0501), "Diet", c(-1, 1, 0, 0, 0, 0), conf.int=0.95
                       Estimate Std. Error t value Pr(>|t|) lower CI
Diet c=( -1 1 0 0 0 0 )
                                     1.24 10.1 4.96e-21
                         12.4
                       upper CI
Diet c=( -1 1 0 0 0 0 ) 14.9
attr(,"class")
[1] "fit_contrast"
```

The results for (d) on page 116:

The results for (e) on page 116:

Another way of viewing these results is through a model table, which displays the differences between the grand mean and the group means.

Another way of calculating the above results is done with the following code:

```
> mean(Lifetime ~ Diet, data=case0501)-mean(~ Lifetime, data=case0501)

N/N85  N/R40  N/R50  NP  R/R50  lopro
-6.106  6.320  3.500 -11.395  4.089  0.889
```

#### 2.4 Other analyses

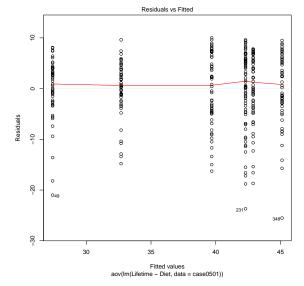
We will next demonstrate how to calculate the quantities on 121 (Display 5.6).

Note that the pooled standard deviation reported in chapter 5 is not the same as the root MSE from the ANOVA. For the rest of this document we will use the ANOVA estimate of the root mean squared error.

## 2.5 Residual analysis and diagnostics

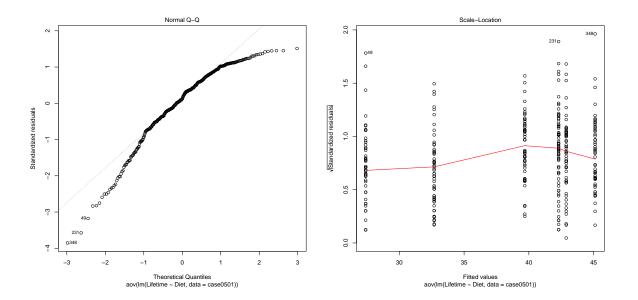
The residuals versus fitted graph does not demonstrate dramatic lack of fit (though some of the mice had very small residuals). The following figure is akin to Display 5.14 (page 132).

```
> aov1 = aov(lm(Lifetime ~ Diet, data=case0501))
> plot(aov1, which=1)
```



The quantile plot of the residuals indicates that the normality assumption may be violated.

```
> plot(aov1, which=2)
> plot(aov1, which=3)
```



# 3 Spock Conspiracy Trial

Did Dr. Benjamin Spock have a fair trial? More specifically, were women underrepresented on his jury pool? This is the question considered in case study 5.2 in the *Sleuth*.

### 3.1 Summary statistics and graphical display

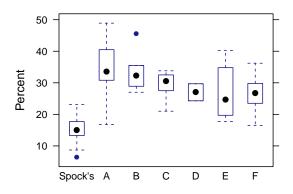
We begin by reading the data and summarizing the variables.

```
> case0502 = transform(case0502, Judge = factor(Judge, levels = c("Spock's", "A", "B", "C", "D
> summary(case0502)
    Percent
                    Judge
        : 6.4
                Spock's:9
1st Qu.:19.9
                Α
                        :5
Median:27.5
                        :6
                В
Mean
        :26.6
                С
                        :9
 3rd Qu.:32.4
                        :2
                D
                Ε
                        :6
 Max.
        :48.9
                F
                        :9
> case0502$Judge = with(case0502, as.factor(Judge))
> favstats(Percent ~ Judge, data=case0502)
    Judge min
                 Q1 median
                              Q3 max mean
                                              sd n missing
```

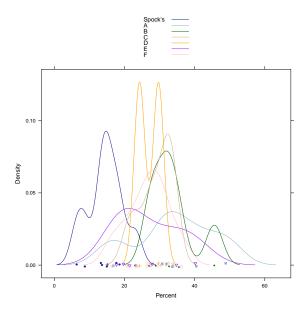
```
1 Spock's 6.4 13.3
                       15.0 17.7 23.1 14.6
                                            5.04 9
                                                           0
2
        A 16.8 30.8
                       33.6 40.5 48.9 34.1 11.94 5
                                                           0
3
        B 27.0 29.7
                       32.4 34.8 45.6 33.6
                                             6.58 6
                                                           0
4
        C 21.0 27.5
                       30.5 32.5 33.8 29.1
                                                           0
                                             4.59 9
5
        D 24.3 25.7
                       27.0 28.3 29.7 27.0
                                             3.82 2
                                                           0
6
        E 17.7 20.1
                       24.7 33.1 40.2 27.0
                                                           0
                                             9.01 6
        F 16.5 23.5
                       26.7 29.8 36.2 26.8
                                            5.97 9
                                                           0
```

There were a total of 46 venires. They compared Spock's judge with 6 other judges. The precent of women within each venire was recorded as shown in Display 5.4 (page 117 of the *Sleuth*).

```
> bwplot(Percent ~ Judge, data=case0502) # Display 5.5 (page 118)
```



> densityplot(~ Percent, groups=Judge, auto.key=TRUE, data=case0502)



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#### 3.2 One-way ANOVA

First we fit the one way analysis of variance (ANOVA) model, with all of the groups. These results are summarized on page 118 and shown in Display 5.10 (page 127).

By default, the use of the linear model (regression) function displays the pairwise differences between the first group and each of the other groups. Note that the overall test of the model is the same.

```
> summary(lm(Percent ~ Judge, data=case0502))
Call:
lm(formula = Percent ~ Judge, data = case0502)
Residuals:
  Min 1Q Median 3Q Max
-17.32 -4.37 -0.25 3.32 14.78
Coefficients:
          Estimate Std. Error t value Pr(>|t|)
(Intercept) 14.62 2.30 6.34 1.7e-07
                      3.86 5.06 1.1e-05
            19.50
JudgeA
                      3.64 5.21 6.4e-06
JudgeB
            18.99
                     3.26 4.44 7.2e-05
            14.48
JudgeC
                      5.41 2.29 0.0275
JudgeD
            12.38
JudgeE
             12.34
                       3.64
                               3.39
                                   0.0016
             12.18
                        3.26 3.74 0.0006
JudgeF
Residual standard error: 6.91 on 39 degrees of freedom
Multiple R-squared: 0.508, Adjusted R-squared: 0.433
F-statistic: 6.72 on 6 and 39 DF, p-value: 6.1e-05
```

```
> model.tables(aov(lm(Percent ~ Judge, data=case0502)))
Tables of effects
```

```
Judge
Spock's A B C D E F
-11.96 7.537 7.034 2.517 0.4174 0.3841 0.2174
rep 9.00 5.000 6.000 9.000 2.0000 6.0000 9.0000
```

Then we can fit the one way analysis of variance F-test of whether the mean percentage is the same for judges A-F (page 118).

#### 3.3 Additional analyses

Now we will demonstrate how to fit the reduced model comparing Spock's judge to a combination of the other judges. First we create a 2 level version of the grouping variable.

```
> case0502$twoJudge = as.character(case0502$Judge)
> case0502$twoJudge[case0502$Judge!="Spock's"] = "notspock"
> tally(twoJudge ~ Judge, format="count", data=case0502)

Judge
twoJudge Spock's A B C D E F
Spock's 9 0 0 0 0 0 0
notspock 0 5 6 9 2 6 9
```

Recall that the book calculates the extra sum of squares as (2,190.90 - 1864.45)/(44-39)) / (1864.45 / 39) = 1.37, with df 5 and 39. P(F > 1.366) = 0.26 (page 130). Below are the calculations for the results found on page 128.

```
> numdf1 = aov1["Residuals", "Df"]; numdf1 # Within

[1] 39
> ss1 = aov1["Residuals", "Sum Sq"]; ss1 # Within

[1] 1864
> aov2 = anova(lm(Percent ~ as.factor(twoJudge), data=case0502)); aov2
```

```
Analysis of Variance Table
Response: Percent
                   Df Sum Sq Mean Sq F value Pr(>F)
as.factor(twoJudge) 1 1601
                                1601 32.1 1e-06
Residuals
                   44
                        2191
                                  50
> df2 = aov2["Residuals", "Df"]; df2 # Spock and others
Γ1 ] 44
> ss2 = aov2["Residuals", "Sum Sq"]; ss2 # Spock and others
[1] 2191
> Fstat = ((ss2 - ss1)/(df2 - numdf1)) / (ss1 / numdf1); Fstat
[1] 1.37
> 1-pf(Fstat, length(levels(case0502$Judge))-2, numdf1)
[1] 0.258
```

We can also compare the two models using ANOVA (Display 5.12, page 130).

There are some other ways to compare whether the other judges differ from Dr. Spock's judge in their female composition using contrasts.

#### 3.3.1 Kruskal-Wallis Nonparametric Analysis of Variance

For the results of the Kruskal-Wallis test on page 136 we can use the following code:

```
> kruskal.test(Percent ~ Judge, data=case0502)

Kruskal-Wallis rank sum test

data: Percent by Judge
Kruskal-Wallis chi-squared = 20, df = 6, p-value = 0.001
```