Using asremlPlus, in conjunction with asreml, to do the analysis of a wheat experiment that includes choosing a local spatial variation model using AICs

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This vignette shows how to use asremlPlus (Brien, 2023), in conjunction with asreml (Butler et al., 2023), to select the terms to be included in a mixed model for an experiment that involves spatial variation by comparing of information criteria . It also illustrates diagnostic checking and prediction production and presentation for this experiment. Here, asremlPlus and asreml are packages for the R Statistical Computing environment (R Core Team, 2023).

It is divided into the following main sections:

- 1. Set up the initial model for this experiment
- 2. Compare a series of information criteria to select a linear mixed model for the data
- 3. Diagnostic checking using residual plots and variofaces
- 4. Prediction production and presentation

1. Set up the initial model for this experiment

```
library(asrem1, quietly=TRUE)

## Offline License checked out Thu Aug 24 10:11:56 2023

## Loading ASRem1-R version 4.2

library(asrem1Plus)
suppressMessages(library(qqplotr, quietly=TRUE))
options(width = 100)
```

Get data available in asremlPlus

The data are from a 1976 spring wheat experiment and are taken from Gilmour et al. (1995). An analysis is presented in the asreml manual by Butler et al. (2023, Section 7.6), although they suggest that it is a barley experiment.

```
data(Wheat.dat)
```

Add row and column covariates for the spatial modelling

```
cRow <- cRow - mean(unique(cRow))
})</pre>
```

Fit an initial model - Row and column random

In the following, an initial model is fitted that has the terms that would be included for a balanced lattice. In addition, a term WithinColPairs has been included to allow for extraneous variation arising between pairs of adjacent lanes.

Intialize a model sequence by loading the current fit into an asrtests object

In creating the asrtests object, IClikelihood is set to full so that the full Restricted Maximum Likelihood (full REML) of Verbyla, 2019 is incorporated into the tests.summary of the asrtests object.

Check for and remove any boundary terms and print a summary of the fit in the asrtests object

```
current.asrt <- rmboundary(current.asrt)</pre>
print(current.asrt)
##
##
## #### Summary of the fitted variance parameters
##
##
                component std.error z.ratio bound %ch
## Row
                 5943.898
                           3815.514 1.557824
                                                  P 0.0
                12380.527
                           6323.542 1.957847
                                                  P 0.3
## Row:Column!R 20477.280 2896.642 7.069316
                                                  P 0.0
##
##
## #### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
##
                  Df denDF
                             F.inc
                                        Pr
                   1 14.9 1390.00 0.0000
## (Intercept)
## Rep
                   5 25.3
                               6.04 0.0008
## WithinColPairs 1 10.4
                               0.49 0.4998
                              4.71 0.0000
## Variety
                  24 104.8
```

```
##
## #### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
## terms DF denDF p AIC BIC action
## 1 Initial model 31 3 NA 1720.891 1823.253 Starting model
```

The test.summary output shows that no changes have been made to the model loaded using as.asrtests. The pseudo-anova table shows that Varieties are highly significant (p < 0.001)

2. Compare a series of information criteria to select a linear mixed model for the data

In this section, models are compared using Akaike Information Criterion (AICs) based on the full REML.

Check the need for the term for within Column pairs (a post hoc factor)

```
current.asrt <- changeModelOnIC(current.asrt, dropFixed = "WithinColPairs",</pre>
                                 label = "Try dropping withinColPairs", IClikelihood = "full")
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, :
## Log-likelihood not converged
print(current.asrt)
##
##
##
         Summary of the fitted variance parameters
  ####
##
##
                component std.error z.ratio bound %ch
## Row
                 5941.153
                           3813.586 1.557891
                11165.335
                           5583.267 1.999785
                                                      0
## Row:Column!R 20472.402 2895.582 7.070219
                                                      0
##
##
## ####
        Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
  Response: yield
##
##
               Df denDF
                          F.inc
                   15.3 1466.00 0e+00
##
  (Intercept)
                1
## Rep
                5 26.7
                           6.11 7e-04
               24 105.3
                           4.73 0e+00
## Variety
##
##
## ####
        Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
                           terms DF denDF p
##
                                                      AIC
                                                                  BIC
                                                                              action
```

3 NA 1720.891308 1823.25291 Starting model

Initial model 31

1

```
## 2 Try dropping withinColPairs -1 0 NA -2.281894 -5.29253 Swapped
```

It is clear in the call to changeModelOnIC that the model is being changed by dropping the withinColPairs term, which could also be achieved using update.asreml. However, an asremlPlus model-changing function operates on an asrtests object, that includes an asreml object, and, except for changeTerms.asrtests, results in an asrtests object that may contain the changed model or the supplied model depending on the results of hypothesis tests or comparisons of information criteria. In addition, the result of the test or comparison will be added to a test.summary data.frame stored in the new asrtests object and, if the model was changed, the wald.tab in the new asrtests object will have been updated for the new model.

In this case, as can be seen from the summary of current.asrt after the call, the model without withinColPairs had a smaller AIC and so now the model stored in current.asrt does not include withinColPAirs. The wald.tab has been updated for the new model.

Choose a model for local spatial variation from several potential models

This example has been analyzed using a model for the local spatial variation based on a separable a separable autocorrelation process of order one (Butler et al., 2023). The need for this model can be assessed using the function addSpatialModelOnIC from asremlPlus that uses a forward selection strategy for fitting a correlation model (see output below). For this function, the spatial model to be fitted, the centred covariates for the two dimensions of the grid, and the factors corresponding to the covariates must be specified. Also, checkboundaryonly is set to TRUE so that no terms are removed until the final model has been fitted and IClikelihood is set to full so that the likelihood will be based on the full REML. Because the model that incorporates the spatial model has a smaller AIC, it is the model returned in spatial.ar1.asrt.

The print of spatial.ar1.asrt shows that an ar1 model for Row was tried first and was found to reduce the AIC by 11.898 and so became the current model. Next a model that incorporates an ar1 function for Column was similarly tried and became the current model. Then an appraisal of the need for a nugget term was made by comparing the fits with the residual variance unfixed and fixed at one. The model with the unfixed residual variance was chosen and is the model to be returned. The nugget term represents non-spatial variance, such as measurement error.

```
spatial.ar1.asrt <- addSpatialModelOnIC(current.asrt, spatial.model = "corr",</pre>
                                        row.covar = "cRow", col.covar = "cColumn",
                                        row.factor = "Row", col.factor = "Column",
                                        checkboundaryonly = TRUE, IClikelihood = "full")
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, :
## Log-likelihood not converged
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, :
## Log-likelihood not converged
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in infoCriteria.asreml(asreml.obj, IClikelihood = ic.lik, bound.exclusions = bound.exclusion
## Warning in rmboundary.asrtests(as.asrtests(asreml.obj, wald.tab, test.summary, : In analysing yield,
##
                 but not removed because checkboundaryonly = TRUE:
## Column
## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, IClikelihood = ic.lik, : The following b
```

Warning in infoCriteria.asreml(asrtests.obj\$asreml.obj, IClikelihood = ic.lik, : The following bound

Column

```
## Column
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, :
## Log-likelihood not converged
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration
## Warning in infoCriteria.asreml(asreml.obj, IClikelihood = ic.lik, bound.exclusions = bound.exclusion
## Column, Row:Column!R
## Warning in rmboundary.asrtests(as.asrtests(asreml.obj, wald.tab, test.summary, : In analysing yield,
                 but not removed because checkboundaryonly = TRUE:
## Column
## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, IClikelihood = ic.lik, : The following b
## Column, Row:Column!R
spatial.ar1.asrt <- rmboundary(spatial.ar1.asrt)</pre>
infoCriteria(list(nonspatial = current.asrt$asreml.obj,
                  ar1 = spatial.ar1.asrt$asreml.obj))
##
              fixedDF varDF NBound
                                                  BIC
                                        AIC
                                                         loglik
## nonspatial
                    0
                          3
                                 0 1409.023 1417.386 -701.5117
                    0
                          5
                                 0 1353.762 1367.700 -671.8811
print(spatial.ar1.asrt)
##
## #### Summary of the fitted variance parameters
##
##
                            component
                                         std.error
                                                      z.ratio bound %ch
                         2.198199e+03 8.220214e+03 0.2674138
                                                                  P 0.1
## R.ow
## Row:Column
                         5.182611e+04 3.379376e+04 1.5336001
                                                                  P 0.0
## Row:Column!Row!cor
                         7.121385e-01 9.571021e-02 7.4405696
                                                                  U 0.0
## Row:Column!Column!cor 8.599836e-01 1.104248e-01 7.7879542
                                                                  U 0.0
                         4.821195e+03 1.717266e+03 2.8074825
## Row:Column!R
                                                                  P 0.0
##
##
## #### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
##
               Df denDF
                          F.inc
## (Intercept)
               1
                    1.8 194.600 0.0076
                5 21.8
                          0.559 0.7303
## Rep
## Variety
               24 74.3 10.560 0.0000
##
##
## #### Sequence of model investigations
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##
                           terms DF denDF p
                                                      AIC
                                                                  BIC
                                                                              action
## 1
                                        3 NA 1720.891308 1823.252908 Starting model
                   Initial model 31
```

```
## 2 Try dropping withinColPairs -1
                                          O NA
                                                  -2.281894
                                                              -5.292530
                                                                                 Swapped
## 3
                                    0
                                          2 NA
                                                -11.897888
                                                                                 Swapped
                     Try ar1(Row)
                                                              -5.876617
                  Try ar1(Column)
                                                 -55.397582
## 4
                                          O NA
                                                             -55.397582
                                                                                 Swapped
## 5 Try fixed residual variance
                                   0
                                                   1.809461
                                                              -1.201174
                                                                               Unswapped
                                         -1 NA
## 6
                           Column
                                         NA NA
                                                                                Boundary
```

However, the spatial models that are available in asremlPlus also include those based on two-dimensional tensor-product natural cubic smoothing splines (TPNCSS), as described by Verbyla et al. (2018), and on two-dimensional tensor-product P-splines (TPPS), as described by Rodriguez-Alvarez et al. (2018) and Piepho, Boer and Williams (2022). The P-splines have been implemented using functions from the R package TPSbits authored by Sue Welham (2022)

The asremlPlus function chooseSpatialModelOnIC allows one to select the best model from amongst these spatial correlation models using the AIC. The four models from which it selects are (i) a separable autocorrelation model on both row and column dimensions (corr), (ii) a two-dimensional tensor-product natural cubic smoothing spline (TPNCSS), (ii) a two-dimensional tensor-product cubic P-spline with second-difference penalties (TPPCS), and (iii) a tensor-product two-dimensional linear P-spline with first-difference penalties (TPP1LS). By default all four are fitted and compared, but the trySpatial argument can be used to specify a subset of them.

The call to chooseSpatialModelOnIC, in addition to the arguments specifying covariates and factors, has further arguments: (i) dropRowTerm and dropColTerm that are needed in fitting P-splines, if overall Row and Column terms have been fitted in the supplied model, because the code also automatically includes these terms, (ii) rotateX and ngridangles so that a grid of angles of every five degrees between 0 and 90 in both directions is explored for rotating the eigenvectors of the penalty matrix for the linear component of the P-splines (requiring $(18+1)^2=361$ re-analyses), (iii) an asreml.option argument to specify that the grp method be used in fitting the P-spline terms, this being required for rotateX set to TRUE, and (iv) return.asrts to specify which asrtests objects are to be returned. Here we specify all so that asrtests objects for the fits for all four spatial models will be returned. In this case, neither the checkboundaryonly nor the IClikelihood arguments were set because their defaults for chooseSpatialModelOnIC are appropriate.

```
: Spline design points closer than .000900 have been merged
          : Spline design points closer than .001400 have been merged
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## Notice
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          : Spline design points closer than .000900 have been merged
          : Spline design points closer than .000900 have been merged
```

- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 0 time 3.29 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 1 time 6.68 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 2 time 9.91 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 3 time 13.3 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 4 time 16.72 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 5 time 20.08 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 6 time 23.41 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 7 time 26.77 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 8 time 30.16 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 9 time 33.41 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 10 time 36.69 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 11 time 40.13 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 12 time 43.35 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 13 time 46.63 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 14 time 49.91 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 15 time 53.4 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 16 time 56.68 seconds
- ## Terms with zero df listed in attribute 'zerodf' of the wald table.
- ## sc 17 time 59.94 seconds

```
## Terms with zero df listed in attribute 'zerodf' of the wald table.
## Terms with zero df listed in attribute 'zerodf' of the wald table.
## Terms with zero df listed in attribute 'zerodf' of the wald table.
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## Terms with zero df listed in attribute 'zerodf' of the wald table.
## Terms with zero df listed in attribute 'zerodf' of the wald table.
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## Terms with zero df listed in attribute 'zerodf' of the wald table.
## Terms with zero df listed in attribute 'zerodf' of the wald table.
## Terms with zero df listed in attribute 'zerodf' of the wald table.
## Terms with zero df listed in attribute 'zerodf' of the wald table.
## sc 18 time 63.35 seconds
##
##
## #### Optimal thetas: 15, 90
##
## Notice : Spline design points closer than .000900 have been merged
## Terms with zero df listed in attribute 'zerodf' of the wald table.
## Notice : Spline design points closer than .000900 have been merged
## Terms with zero df listed in attribute 'zerodf' of the wald table.
## Notice : Spline design points closer than .000900 have been merged
## Terms with zero df listed in attribute 'zerodf' of the wald table.
## Notice : Spline design points closer than .000900 have been merged
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## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .000900 have been merged
```

Output the results

```
print(spatial.asrts$spatial.IC)
## fixedDF varDF AIC BIC loglik
```

```
## nonspatial
                   30
                          3 1718.609 1817.960 -826.3047
## corr
                   30
                          5 1651.314 1756.686 -790.6570
## TPNCSS
                   33
                          6 1639.489 1756.904 -780.7445
## TPPCS
                   32
                          6 1645.033 1759.437 -784.5164
## TPP1LS
                   30
                          3 1708.443 1807.794 -821.2215
print(spatial.asrts$best.spatial.mod)
## [1] "TPNCSS"
print(spatial.asrts$asrts$TPNCSS)
##
##
## #### Summary of the fitted variance parameters
##
##
                           component std.error z.ratio bound %ch
## spl(cRow):cColumn
                            523.2004 372.8016 1.403429
## dev(cRow)
                           7664.0211 4442.0646 1.725329
                                                                 0
## spl(cColumn)
                          13338.7348 9236.0511 1.444203
                                                                 0
## spl(cColumn):cRow
                            366.7707 322.7484 1.136399
                                                                 0
## spl(cRow):spl(cColumn) 3630.2187 2186.1497 1.660554
                                                             Ρ
                                                                 0
## Row:Column!R
                           7658.0113 1312.2026 5.835998
                                                                 0
##
##
## #### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
                           F.inc
##
                Df denDF
## (Intercept)
                1
                     6.8 2645.00 0.0000
                 5
                           20.45 0.0000
## Rep
                   41.3
## Variety
                24
                   86.5
                           10.15 0.0000
                     7.0
                           0.07 0.7954
## cRow
                 1
                           20.30 0.0001
## cColumn
                 1
                    30.1
## cRow:cColumn 1 64.3
                           22.00 0.0000
##
##
## #### Sequence of model investigations
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
                           terms DF denDF p
##
                                                                BIC
                                                                             action
                                                     AIC
## 1
                   Initial model 31
                                        3 NA 1720.891308 1823.25291 Starting model
## 2 Try dropping withinColPairs -1
                                                                            Swapped
                                        O NA
                                               -2.281894
                                                           -5.29253
          Try tensor NCS splines 3
                                        3 NA -79.120426 -61.05661
                                                                            Swapped
## 4
                    dev(cColumn) 1
                                       NA NA 1639.488959 1756.90374
                                                                           Boundary
                       spl(cRow) 1
                                       NA NA 1639.489011 1756.90379
                                                                           Boundary
printFormulae(spatial.asrts$asrts$TPNCSS$asreml.obj)
##
##
```

Formulae from asreml object

```
##
## fixed: yield ~ Rep + Variety + cRow + cColumn + cRow:cColumn
## random: ~ spl(cColumn) + dev(cRow) + spl(cRow):cColumn + spl(cColumn):cRow + spl(cRow):spl(cColumn)
## residual: ~ Row:Column
```

The output shows that the TPNCSS model has the lowest AIC and so is selected as the best model. The model fitted for the TPNCSS model has been printed using printFormulae.asreml. The fitted model includes the term dev(cRow) that is equivalent to a random Row term and measures the deviations of the Row trend from a linear trend, the spl(cRow) term having been dropped because it was estimated to be zero. The Wald F-statistic for Variety is now 10.15 with 86.5 denominator degrees of freedom, as compared to 10.56 and 74.3 for the correlation model and 4.71 and 104.8 for the initial nonspatial model.

3. Diagnosting checking using residual plots and variofaces

Get current fitted asreml object and update to include standardized residuals

```
current.asr <- spatial.asrts$asrts$TPNCSS$asreml.obj
current.asr <- update(current.asr, aom=TRUE)

## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
Wheat.dat$res <- residuals(current.asr, type = "stdCond")
Wheat.dat$fit <- fitted(current.asr)</pre>
```

Do diagnostic checking

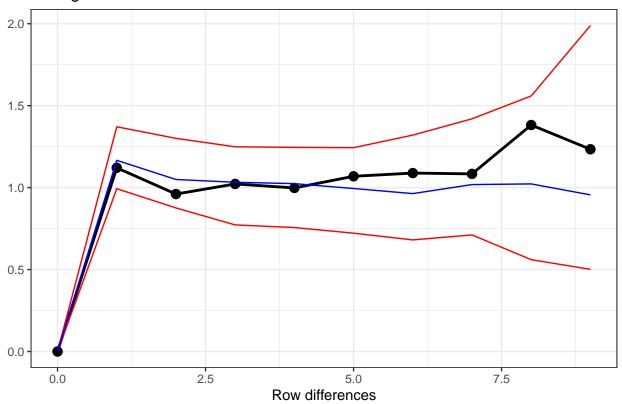
Do residuals-versus-fitted values plot

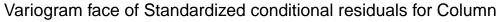
fit

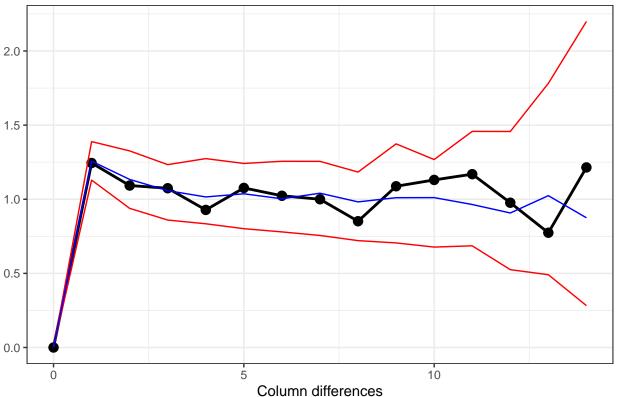
Plot variofaces

Notice : Spline design points closer than .001400 have been merged ## Notice : Spline design points closer than .000900 have been merged

Variogram face of Standardized conditional residuals for Row







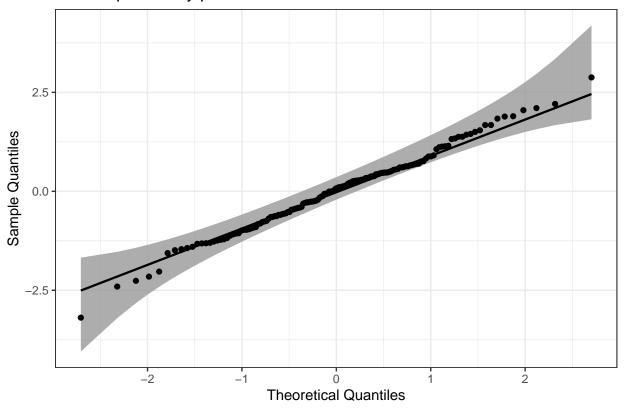
The variofaces are the lag 1 plots of the sample semivariogram with simulated confidence envelopes (Stefanova et al., 2009).

Plot normal quantile plot

The plot is obtained using the ggplot function with extensions available from the qqplotr package (Almeida et al., 2023).

```
ggplot(data = Wheat.dat, mapping = aes(sample = res)) +
   stat_qq_band(bandType = "ts") + stat_qq_line() + stat_qq_point() +
   labs(x = "Theoretical Quantiles", y = "Sample Quantiles",
        title = "Normal probability plot") +
   theme(plot.title = element_text(size = 12, face = "bold")) + theme_bw()
```

Normal probability plot



4. Prediction production and presentation

Get Variety predictions and all pairwise prediction differences and p-values

```
Var.diffs <- predictPlus(classify = "Variety",</pre>
                         asreml.obj=current.asr,
                         error.intervals="halfLeast",
                         wald.tab=current.asrt$wald.tab,
                         sortFactor = "Variety",
                         tables = "predictions")
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
##
##
## #### Predictions for yield from Variety
##
##
## Notes:
## - The predictions are obtained by averaging across the hypertable
     calculated from model terms constructed solely from factors in
##
     the averaging and classify sets.
## - Use 'average' to move ignored factors into the averaging set.
## - spl(cRow) evaluated at average value of 0.00000
## - spl(cColumn) evaluated at average value of 0.00000
## - The simple averaging set: Rep
```

```
##
      Variety predicted.value standard.error upper.halfLeastSignificant.limit
## 1
           10
                      1196.214
                                      64.11316
                                                                          1255.028
## 2
            9
                      1266.442
                                      69.62176
                                                                          1325.255
## 3
           16
                      1268.206
                                      74.01873
                                                                          1327.020
## 4
            1
                                      69.30592
                                                                          1332.608
                      1273.794
## 5
           14
                      1310.806
                                      70.75661
                                                                          1369.620
           23
## 6
                      1329.114
                                      73.70238
                                                                          1387.928
## 7
            11
                      1340.668
                                      75.07426
                                                                          1399.481
## 8
             4
                      1406.408
                                      76.83336
                                                                          1465.222
## 9
             3
                      1408.543
                                      71.85868
                                                                          1467.356
## 10
            7
                                      72.23082
                                                                          1473.284
                      1414.471
## 11
           12
                      1423.303
                                      71.18629
                                                                          1482.117
## 12
            8
                      1445.533
                                      75.37805
                                                                          1504.347
                                      70.31499
## 13
            5
                      1480.687
                                                                          1539.500
## 14
            15
                      1485.249
                                      74.28025
                                                                          1544.063
## 15
           17
                      1495.212
                                      71.09930
                                                                          1554.026
## 16
           21
                      1512.767
                                      72.53109
                                                                          1571.580
## 17
            6
                      1520.841
                                      72.50721
                                                                          1579.654
## 18
           24
                      1563.649
                                      65.33308
                                                                          1622.463
## 19
           18
                      1568.887
                                      71.06200
                                                                          1627.700
## 20
           25
                      1579.929
                                      70.52509
                                                                          1638.743
## 21
            2
                                      74.96623
                                                                          1644.211
                      1585.398
## 22
           22
                      1633.080
                                      71.38265
                                                                          1691.894
## 23
           13
                      1637.119
                                      66.24775
                                                                          1695.932
## 24
           19
                      1651.533
                                      74.93686
                                                                          1710.347
## 25
           20
                      1657.612
                                      68.65452
                                                                          1716.426
##
      lower.halfLeastSignificant.limit est.status
## 1
                                          Estimable
                                1137.400
## 2
                                1207.628
                                          Estimable
## 3
                                1209.393
                                           Estimable
## 4
                                1214.980
                                           Estimable
## 5
                                1251.993
                                           Estimable
## 6
                                1270.300
                                          Estimable
## 7
                                1281.854
                                          Estimable
## 8
                                1347.594
                                          Estimable
## 9
                                1349.729
                                          Estimable
## 10
                                1355.657
                                          Estimable
## 11
                                1364.490
                                          Estimable
## 12
                                1386.720
                                          Estimable
## 13
                                1421.873
                                          Estimable
                                          Estimable
## 14
                                1426.435
## 15
                                1436.399
                                          Estimable
## 16
                                          Estimable
                                1453.953
## 17
                                           Estimable
                                1462.027
## 18
                                          Estimable
                                1504.836
## 19
                                1510.073
                                           Estimable
## 20
                                1521.115
                                          Estimable
## 21
                                1526.584
                                          Estimable
## 22
                                1574.266
                                          Estimable
## 23
                                          Estimable
                                1578.305
## 24
                                1592.719
                                          Estimable
## 25
                                1598.798 Estimable
##
```

##

```
##
## LSD values
##
## minimum LSD = 109.6008
##
## mean LSD = 117.6273
##
## maximum LSD = 126.3422
##
## (sed range / mean sed = 0.142 )
```

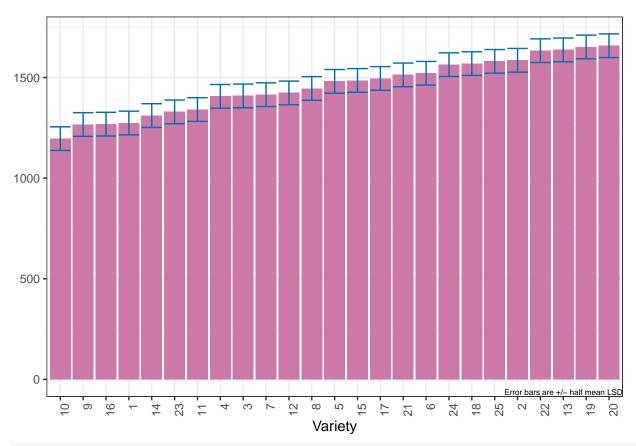
We have set error.intervals to halfLeast so that the limits for each prediction \pm (0.5 LSD) are calculated. When these are plotted overlapping error bars indicate predictions that are not significant, while those that do not overlap are significantly different (Snee, 1981).

Also set was sortFactor, so that the results would be ordered for the values of the predictions for Variety.

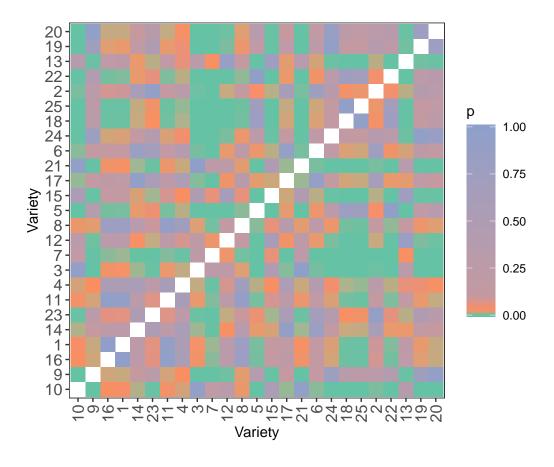
The function predictPlus returns an alldiffs object, a list consisting of the following components:

- predictions: the predictions, their standard errors and error intervals;
- vcov: the variance matrix of the predictions;
- differences: all pairwise differences between the predictions,
- p.differences: p-values for all pairwise differences between the predictions;
- sed: the standard errors of all pairwise differences between the predictions;
- LSD: the mean, minimum and maximum of the LSDs.

Plot the Variety predictions, with halfLSD intervals, and the p-values



plotPvalues(Var.diffs)



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