## Appendix C: Demonstration of selected features

#### James T. Thorson

```
library(dsem)
library(ggplot2)
library(reshape)
library(gridExtra)
library(phylopath)
```

dsem is an R package for fitting dynamic structural equation models (DSEMs) with a simple user-interface and generic specification of simultaneous and lagged effects that could be either recursive or non-recursive in structure. We here highlight a few features in particular.

#### Comparison with dynamic linear models

We first demonstrate that dsem gives identical results to dynlm for a well-known econometric model, the Klein-1 model.

```
data(KleinI, package="AER")
TS = ts(data.frame(KleinI, "time"=time(KleinI) - 1931))
fm_cons <- dynlm(consumption ~ cprofits + L(cprofits) + I(pwage + gwage), data = TS)</pre>
fm_inv <- dynlm(invest ~ cprofits + L(cprofits) + capital, data = TS)</pre>
fm_pwage <- dynlm(pwage ~ gnp + L(gnp) + time, data = TS)</pre>
# dsem
sem = "
 # Link, lag, param_name
  cprofits -> consumption, 0, a1
  cprofits -> consumption, 1, a2
  pwage -> consumption, 0, a3
  gwage -> consumption, 0, a3
  cprofits -> invest, 0, b1
  cprofits -> invest, 1, b2
  capital -> invest, 0, b3
  gnp -> pwage, 0, c2
 gnp -> pwage, 1, c3
  time -> pwage, 0, c1
tsdata = TS[,c("time","gnp","pwage","cprofits",'consumption',
               "gwage", "invest", "capital")]
fit = dsem( sem=sem,
```

```
tsdata = tsdata,
            estimate_delta0 = TRUE.
            control = dsem control(
              quiet = TRUE,
             newton_loops = 0) )
#> 1 regions found.
#> Using 1 threads
#> 1 regions found.
#> Using 1 threads
# Compile
m1 = rbind( summary(fm_cons)$coef[-1,],
            summary(fm_inv)$coef[-1,],
            summary(fm_pwage)$coef[-1,])[,1:2]
m2 = summary(fit$sdrep)[1:9,]
m = rbind(
  data.frame("var"=rownames(m1),m1,"method"="OLS","eq"=rep(c("C","I","Wp"),each=3)),
  data.frame("var"=rownames(m1),m2,"method"="GMRF","eq"=rep(c("C","I","Wp"),each=3))
)
m = cbind(m, "lower"=m$Estimate-m$Std..Error, "upper"=m$Estimate+m$Std..Error)
# qqplot estimates
longform = melt( as.data.frame(KleinI) )
  longform$year = rep( time(KleinI), 9 )
ggplot( data=longform, aes(x=year, y=value) ) +
  facet_grid( rows=vars(variable), scales="free" ) +
  geom_line( )
ggplot(data=m, aes(x=interaction(var,eq), y=Estimate, color=method)) +
  geom_point( position=position_dodge(0.9) ) +
  geom_errorbar( aes(ymax=as.numeric(upper),ymin=as.numeric(lower)),
                 width=0.25, position=position_dodge(0.9)) #
p3 = plot( as_fitted_DAG(fit) ) +
     expand_limits(x = c(-0.2,1))
p4 = plot( as_fitted_DAG(fit, lag=1), text_size=4) +
     expand_limits(x = c(-0.2,1), y = c(-0.2,0))
grid.arrange( arrangeGrob(p3, p4, nrow=2) )
```

Results show that both packages provide (almost) identical estimates and standard errors.

We can also compare results using the Laplace approximation against those obtained via numerical integration of random effects using MCMC. In this example, MCMC results in somewhat higher estimates of exogenous variance parameters (presumably because those follow a chi-squared distribution with positive skewness), but otherwise the two produce similar estimates.

```
library(tmbstan)

# MCMC for both fixed and random effects
mcmc = tmbstan( fit$obj, init="last.par.best" )
summary_mcmc = summary(mcmc)
```

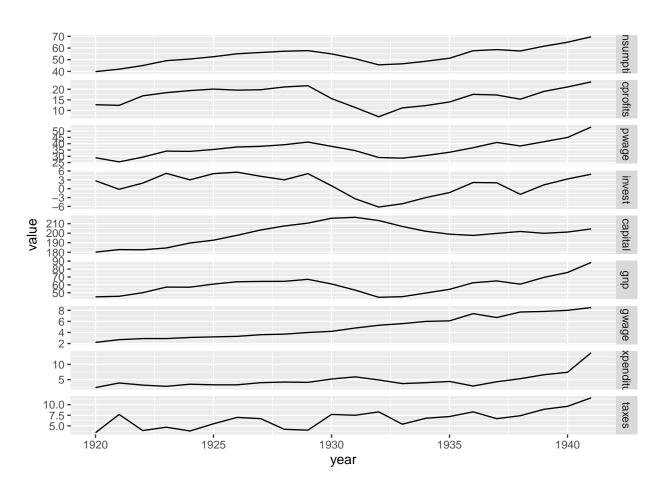


Figure 1: Econometric variables fitted to demonstrate dynamic structural equation modelling

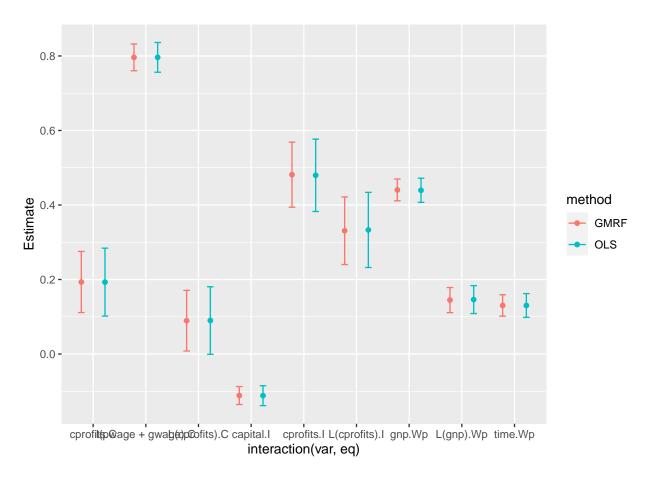
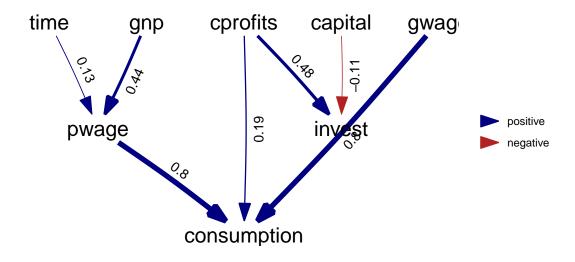


Figure 2: Comparison of package dsem and package dynlm when fitting a dynamic structural equation model to econometric data



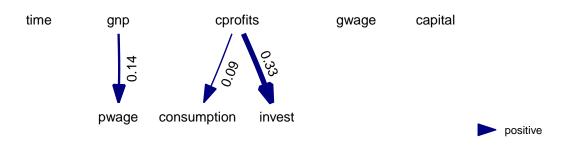


Figure 3: Estimated structural model among econometric variables  $\,$ 

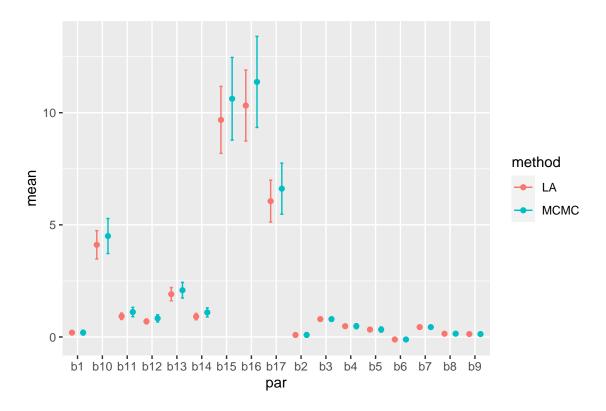


Figure 4: Comparison of Laplace approximation and Markov chain Monte Carlo estimates when fitting an econometric example using dynamic structural equation models

#### Comparison with vector autoregressive models

We next demonstrate that dsem gives similar results to a vector autoregressive (VAR) model. To do so, we analyze population abundance of wolf and moose populations on Isle Royale from 1959 to 2019, downloaded from their website (Vucetich, JA and Peterson RO. 2012. The population biology of Isle Royale wolves and moose: an overview. URL: www.isleroyalewolf.org).

This dataset was previously analyzed by in Chapter 14 of the User Manual for the R-package MARSS (Holmes, E. E., M. D. Scheuerell, and E. J. Ward (2023) Analysis of multivariate time-series using the MARSS package. Version 3.11.8. NOAA Fisheries, Northwest Fisheries Science Center, 2725 Montlake Blvd E., Seattle, WA 98112, DOI: 10.5281/zenodo.5781847).

Here, we compare fits using dsem with dynlm, as well as a vector autoregressive model package vars, and finally with MARSS.

```
data(isle royale)
data = ts( log(isle_royale[,2:3]), start=1959)
sem = "
  # Link, lag, param_name
 wolves -> wolves, 1, arW
 moose -> wolves, 1, MtoW
 wolves -> moose, 1, WtoM
 moose -> moose, 1, arM
# initial first without delta0 (to improve starting values)
fit0 = dsem( sem = sem,
             tsdata = data,
             estimate_delta0 = FALSE,
             control = dsem_control(
               quiet = TRUE,
               getsd = FALSE) )
\#> Warning in nlminb(start = out\$opt\$par, objective = obj\$fn, <math>qradient = obj\$qr, : NA/NaN function eval
# Refit with delta0
fit = dsem( sem = sem,
            tsdata = data,
            estimate delta0 = TRUE,
            control = dsem_control( quiet=TRUE,
                                     parameters = fit0$obj$env$parList()) )
# dynlm
fm_wolf = dynlm( wolves ~ 1 + L(wolves) + L(moose), data=data )
fm_moose = dynlm( moose ~ 1 + L(wolves) + L(moose), data=data )
# MARSS
library(MARSS)
z.royale.dat <- t(scale(data.frame(data),center=TRUE,scale=FALSE))</pre>
royale.model.1 <- list(
  Z = "identity",
  B = "unconstrained",
  Q = "diagonal and unequal",
  R = "zero",
  U = "zero"
kem.1 <- MARSS(z.royale.dat, model = royale.model.1)</pre>
#> Success! abstol and log-log tests passed at 16 iterations.
#> Alert: conv.test.slope.tol is 0.5.
#> Test with smaller values (<0.1) to ensure convergence.
#>
#> MARSS fit is
#> Estimation method: kem
```

```
#> Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
#> Estimation converged in 16 iterations.
#> Log-likelihood: -3.21765
#> AIC: 22.4353 AICc: 23.70964
#>
#>
                         Estimate
#> B. (1,1)
                           0.8669
#> B. (2,1)
                          -0.1240
#> B. (1,2)
                          0.1417
\#>B.(2,2)
                           0.8176
#> Q.(X.wolves, X.wolves) 0.1341
#> Q.(X.moose, X.moose)
                         0.0284
#> x0.X.wolves
                          0.2324
#> x0.X.moose
                          -0.6476
\#> Initial states (x0) defined at t=0
#> Standard errors have not been calculated.
#> Use MARSSparamCIs to compute CIs and bias estimates.
SE <- MARSSparamCIs( kem.1 )</pre>
# Using VAR package
library(vars)
var = VAR( data, type="const" )
### Compile
m1 = rbind( summary(fm_wolf)$coef[-1,], summary(fm_moose)$coef[-1,])[,1:2]
m2 = summary(fit$sdrep)[1:4,]
#m2 = cbind( "Estimate"=fit$opt$par, "Std. Error"=fit$sdrep$par.fixed )[1:4,]
m3 = cbind(SE\$parMean[c(1,3,2,4)], SE\$par.se\$B[c(1,3,2,4)])
colnames(m3) = colnames(m2)
m4 = rbind( summary(var$varresult$wolves)$coef[-3,], summary(var$varresult$moose)$coef[-3,])[,1:2]
# Bundle
m = rbind(
 data.frame("var"=rownames(m1), m1, "method"="dynlm", "eq"=rep(c("Wolf", "Moose"), each=2)),
 data.frame("var"=rownames(m1), m2, "method"="dsem", "eq"=rep(c("Wolf", "Moose"), each=2)),
 data.frame("var"=rownames(m1), m3, "method"="MARSS", "eq"=rep(c("Wolf", "Moose"), each=2)),
 data.frame("var"=rownames(m1), m4, "method"="vars", "eq"=rep(c("Wolf", "Moose"), each=2))
#knitr::kable( m1, digits=3)
#knitr::kable( m2, digits=3)
m = cbind(m, "lower"=m$Estimate-m$Std..Error, "upper"=m$Estimate+m$Std..Error)
\# ggplot estimates ... interaction(x,y) causes an error sometimes
library(ggplot2)
library(ggpubr)
library(ggraph)
longform = reshape( isle_royale, idvar = "year", direction="long", varying=list(2:3), v.names="abundanc")
p1 = ggplot( data=longform, aes(x=year, y=abundance) ) +
 facet_grid( rows=vars(species), scales="free" ) +
  geom_point( )
```

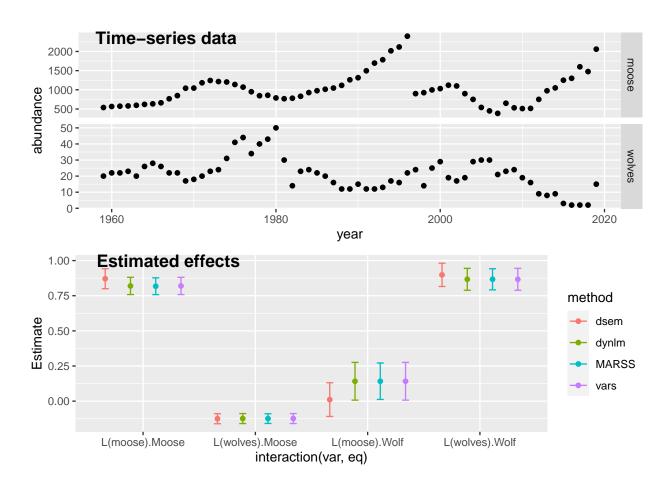


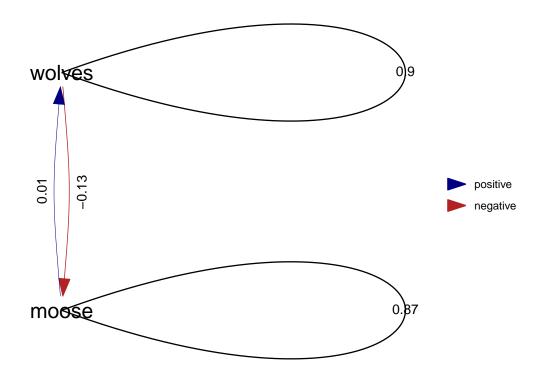
Figure 5: Time-series observations (top panel) and a comparison of estimated structural linkages (bottom panel) among alternative software for fitting a cross-lagged model for wolves and moose in Isle Royale

```
plot( as_fitted_DAG(fit, lag=1), rotation=0 ) +
    geom_edge_loop( aes( label=round(weight,2), direction=0)) + #arrow=arrow(), , angle_calc="along",
    expand_limits(x = c(-0.1,0) )
```

Results again show that dsem can estimate parameters for a vector autoregressive model (VAM), and it exactly matches results from vars, using dynlm, or using MARSS.

#### Multi-causal ecosystem synthesis

We next replicate an analysis involving climate, forage fishes, stomach contents, and recruitment of a predatory fish.



 $\label{lem:coss-lagged} \ \, \text{Interactions between wolves and moose in Isle Royale}$ 

```
data(bering_sea)
Z = ts( bering_sea )
family = rep('fixed', ncol(bering_sea))
# Specify model
sem = "
  # Link, lag, param_name
 log seaice -> log CP, 0, seaice to CP
 log_CP -> log_Cfall, 0, CP_to_Cfall
 log_CP -> log_Esummer, 0, CP_to_E
  log_PercentEuph -> log_RperS, 0, Seuph_to_RperS
  log_PercentCop -> log_RperS, 0, Scop_to_RperS
  log Esummer -> log PercentEuph, 0, Esummer to Suph
  log_Cfall -> log_PercentCop, 0, Cfall_to_Scop
  log_SSB -> log_RperS, 0, SSB_to_RperS
  log_seaice -> log_seaice, 1, AR1, 0.001
  log_CP -> log_CP, 1, AR2, 0.001
  log_Cspring -> log_Cspring, 1, AR3, 0.001
  log_Cfall -> log_Cfall, 1, AR4, 0.001
  log_Esummer -> log_Esummer, 1, AR5, 0.001
 log_SSB -> log_SSB, 1, AR6, 0.001
 log_RperS -> log_RperS, 1, AR7, 0.001
 log_PercentEuph -> log_PercentEuph, 1, AR8, 0.001
 log_PercentCop -> log_PercentCop, 1, AR9, 0.001
# Fit
fit = dsem( sem = sem,
           tsdata = Z,
            family = family,
            control = dsem_control(use_REML=FALSE, quiet=TRUE) )
#> Warning in nlminb(start = out$opt$par, objective = obj$fn, gradient = obj$gr, : NA/NaN function eval
\#> Warning in nlminb(start = out\$opt\$par, objective = obj\$fn, gradient = obj\$gr, : NA/NaN function eval
ParHat = fit$obj$env$parList()
# summary( fit )
# Timeseries plot
oldpar <- par(no.readonly = TRUE)</pre>
par( mfcol=c(3,3), mar=c(2,2,2,0), mgp=c(2,0.5,0), tck=-0.02 )
for(i in 1:ncol(bering_sea)){
  tmp = bering_sea[,i,drop=FALSE]
  tmp = cbind( tmp, "PSEM"=ParHat$x_tj[,i] )
  SD = as.list(fit$sdrep,what="Std.")$x_tj[,i]
  tmp = cbind(tmp, outer(tmp[,2],c(1,1)) +
               outer(ifelse(is.na(SD),0,SD),c(-1,1)) )
  plot( x=rownames(bering_sea), y=tmp[,1], ylim=range(tmp,na.rm=TRUE),
        type="p", main=colnames(bering_sea)[i], pch=20, cex=2 )
  lines( x=rownames(bering_sea), y=tmp[,2], type="1", lwd=2,
         col="blue", lty="solid" )
  polygon( x=c(rownames(bering_sea),rev(rownames(bering_sea))),
```

```
y=c(tmp[,3],rev(tmp[,4])), col=rgb(0,0,1,0.2), border=NA)}
```

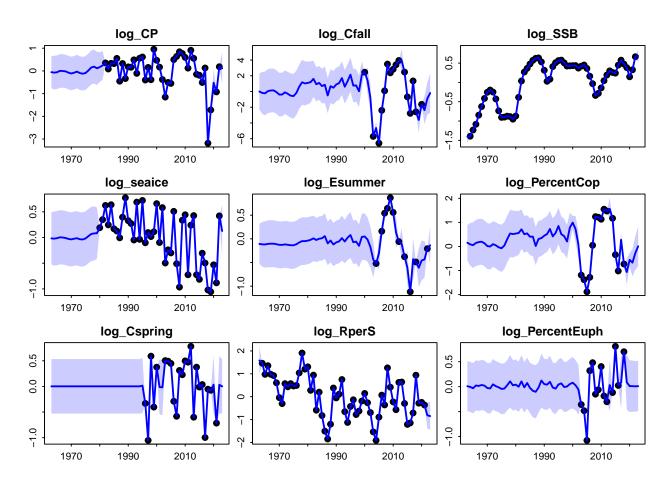


Figure 7: Time-series observations (dots) and estimates (blue lines and shading) for variables affecting recruitment for Alaska pollock in the eastern Bering Sea

### par(oldpar)

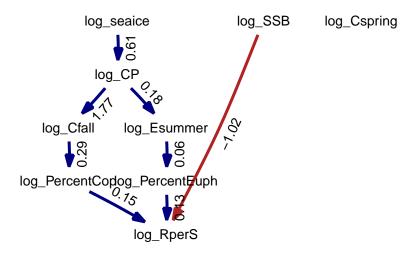
These results are further discussed in the paper describing dsem.

#### Site-replicated trophic cascade

Finally, we replicate an analysis involving a trophic cascade involving sea stars predators, sea urchin consumers, and kelp producers.

```
data(sea_otter)
Z = ts(sea_otter[,-1])
# Specify model
sem = "
  Pycno_CANNERY_DC -> log_Urchins_CANNERY_DC, 0, x2
  log_Urchins_CANNERY_DC -> log_Kelp_CANNERY_DC, 0, x3
  log_Otter_Count_CANNERY_DC -> log_Kelp_CANNERY_DC, 0, x4
  Pycno_CANNERY_UC -> log_Urchins_CANNERY_UC, 0, x2
  log_Urchins_CANNERY_UC -> log_Kelp_CANNERY_UC, 0, x3
  log_Otter_Count_CANNERY_UC -> log_Kelp_CANNERY_UC, 0, x4
  Pycno_HOPKINS_DC -> log_Urchins_HOPKINS_DC, 0, x2
  log_Urchins_HOPKINS_DC -> log_Kelp_HOPKINS_DC, 0, x3
  log_Otter_Count_HOPKINS_DC -> log_Kelp_HOPKINS_DC, 0, x4
  Pycno_HOPKINS_UC -> log_Urchins_HOPKINS_UC, 0, x2
  log_Urchins_HOPKINS_UC -> log_Kelp_HOPKINS_UC, 0, x3
  log_Otter_Count_HOPKINS_UC -> log_Kelp_HOPKINS_UC, 0, x4
  Pycno_LOVERS_DC -> log_Urchins_LOVERS_DC, 0, x2
  log_Urchins_LOVERS_DC -> log_Kelp_LOVERS_DC, 0, x3
  log_Otter_Count_LOVERS_DC -> log_Kelp_LOVERS_DC, 0, x4
  Pycno_LOVERS_UC -> log_Urchins_LOVERS_UC, 0, x2
  log Urchins LOVERS UC -> log Kelp LOVERS UC, 0, x3
  log_Otter_Count_LOVERS_UC -> log_Kelp_LOVERS_UC, 0, x4
  Pycno MACABEE DC -> log Urchins MACABEE DC, 0, x2
  log Urchins MACABEE DC -> log Kelp MACABEE DC, 0, x3
  log_Otter_Count_MACABEE_DC -> log_Kelp_MACABEE_DC, 0, x4
  Pycno_MACABEE_UC -> log_Urchins_MACABEE_UC, 0, x2
```

## Simultaneous effects



## Two-sided p-value

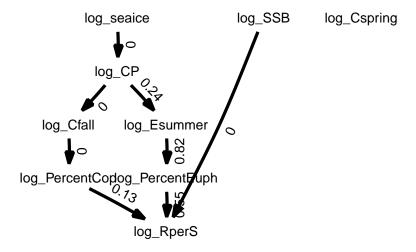


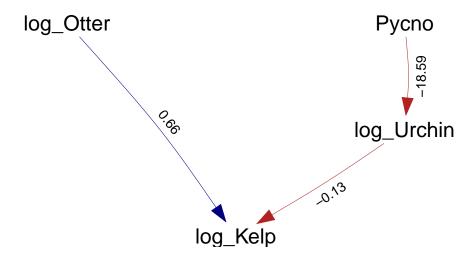
Figure 8: Structural model representing ecosystem linkages affecting recruitment for Alaska pollock in the eastern Bering Sea

```
log_Urchins_MACABEE_UC -> log_Kelp_MACABEE_UC, 0, x3
log_Otter_Count_MACABEE_UC -> log_Kelp_MACABEE_UC, 0, x4
Pycno_OTTER_PT_DC -> log_Urchins_OTTER_PT_DC, 0, x2
log Urchins OTTER PT DC -> log Kelp OTTER PT DC, 0, x3
log_Otter_Count_OTTER_PT_DC -> log_Kelp_OTTER_PT_DC, 0, x4
Pycno_OTTER_PT_UC -> log_Urchins_OTTER_PT_UC, 0, x2
log_Urchins_OTTER_PT_UC -> log_Kelp_OTTER_PT_UC, 0, x3
log_Otter_Count_OTTER_PT_UC -> log_Kelp_OTTER_PT_UC, 0, x4
Pycno_PINOS_CEN -> log_Urchins_PINOS_CEN, 0, x2
log_Urchins_PINOS_CEN -> log_Kelp_PINOS_CEN, 0, x3
log_Otter_Count_PINOS_CEN -> log_Kelp_PINOS_CEN, 0, x4
Pycno_SIREN_CEN -> log_Urchins_SIREN_CEN, 0, x2
log_Urchins_SIREN_CEN -> log_Kelp_SIREN_CEN, 0, x3
log_Otter_Count_SIREN_CEN -> log_Kelp_SIREN_CEN, 0, x4
# AR1
Pycno CANNERY DC -> Pycno CANNERY DC, 1, ar1
log Urchins CANNERY DC -> log Urchins CANNERY DC, 1, ar2
log_Otter_Count_CANNERY_DC -> log_Otter_Count_CANNERY_DC, 1, ar3
log_Kelp_CANNERY_DC -> log_Kelp_CANNERY_DC, 1, ar4
Pycno_CANNERY_UC -> Pycno_CANNERY_UC, 1, ar1
log_Urchins_CANNERY_UC -> log_Urchins_CANNERY_UC, 1, ar2
log_Otter_Count_CANNERY_UC -> log_Otter_Count_CANNERY_UC, 1, ar3
log_Kelp_CANNERY_UC -> log_Kelp_CANNERY_UC, 1, ar4
Pycno_HOPKINS_DC -> Pycno_HOPKINS_DC, 1, ar1
log_Urchins_HOPKINS_DC -> log_Urchins_HOPKINS_DC, 1, ar2
log_Otter_Count_HOPKINS_DC -> log_Otter_Count_HOPKINS_DC, 1, ar3
log_Kelp_HOPKINS_DC -> log_Kelp_HOPKINS_DC, 1, ar4
Pycno_HOPKINS_UC -> Pycno_HOPKINS_UC, 1, ar1
log_Urchins_HOPKINS_UC -> log_Urchins_HOPKINS_UC, 1, ar2
log Otter Count HOPKINS UC -> log Otter Count HOPKINS UC, 1, ar3
log_Kelp_HOPKINS_UC -> log_Kelp_HOPKINS_UC, 1, ar4
Pycno_LOVERS_DC -> Pycno_LOVERS_DC, 1, ar1
log_Urchins_LOVERS_DC -> log_Urchins_LOVERS_DC, 1, ar2
log_Otter_Count_LOVERS_DC -> log_Otter_Count_LOVERS_DC, 1, ar3
log_Kelp_LOVERS_DC -> log_Kelp_LOVERS_DC, 1, ar4
Pycno_LOVERS_UC -> Pycno_LOVERS_UC, 1, ar1
log_Urchins_LOVERS_UC -> log_Urchins_LOVERS_UC, 1, ar2
log_Otter_Count_LOVERS_UC -> log_Otter_Count_LOVERS_UC, 1, ar3
log_Kelp_LOVERS_UC -> log_Kelp_LOVERS_UC, 1, ar4
Pycno_MACABEE_DC -> Pycno_MACABEE_DC, 1, ar1
log_Urchins_MACABEE_DC -> log_Urchins_MACABEE_DC, 1, ar2
log_Otter_Count_MACABEE_DC -> log_Otter_Count_MACABEE_DC, 1, ar3
```

```
log_Kelp_MACABEE_DC -> log_Kelp_MACABEE_DC, 1, ar4
  Pycno MACABEE UC -> Pycno MACABEE UC, 1, ar1
  log Urchins MACABEE UC -> log Urchins MACABEE UC, 1, ar2
  log_Otter_Count_MACABEE_UC -> log_Otter_Count_MACABEE_UC, 1, ar3
  log_Kelp_MACABEE_UC -> log_Kelp_MACABEE_UC, 1, ar4
  Pycno_OTTER_PT_DC -> Pycno_OTTER_PT_DC, 1, ar1
  log_Urchins_OTTER_PT_DC -> log_Urchins_OTTER_PT_DC, 1, ar2
  log_Otter_Count_OTTER_PT_DC -> log_Otter_Count_OTTER_PT_DC, 1, ar3
  log_Kelp_OTTER_PT_DC -> log_Kelp_OTTER_PT_DC, 1, ar4
  Pycno_OTTER_PT_UC -> Pycno_OTTER_PT_UC, 1, ar1
  log_Urchins_OTTER_PT_UC -> log_Urchins_OTTER_PT_UC, 1, ar2
  log_Otter_Count_OTTER_PT_UC -> log_Otter_Count_OTTER_PT_UC, 1, ar3
  log_Kelp_OTTER_PT_UC -> log_Kelp_OTTER_PT_UC, 1, ar4
  Pycno PINOS CEN -> Pycno PINOS CEN, 1, ar1
  log_Urchins_PINOS_CEN -> log_Urchins_PINOS_CEN, 1, ar2
  log_Otter_Count_PINOS_CEN -> log_Otter_Count_PINOS_CEN, 1, ar3
  log Kelp PINOS CEN -> log Kelp PINOS CEN, 1, ar4
  Pycno_SIREN_CEN -> Pycno_SIREN_CEN, 1, ar1
  log_Urchins_SIREN_CEN -> log_Urchins_SIREN_CEN, 1, ar2
  log_Otter_Count_SIREN_CEN -> log_Otter_Count_SIREN_CEN, 1, ar3
  log_Kelp_SIREN_CEN -> log_Kelp_SIREN_CEN, 1, ar4
# Fit model
fit = dsem( sem = sem,
            tsdata = Z,
            control = dsem_control(use_REML=FALSE, quiet=TRUE) )
# summary( fit )
library(phylopath)
library(ggplot2)
library(ggpubr)
get_part = function(x){
  vars = c("log_Kelp","log_Otter","log_Urchin","Pycno")
  index = sapply( vars, FUN=\(y) grep(y,rownames(x$coef))[1] )
  x$coef = x$coef[index,index]
  dimnames(x$coef) = list( vars, vars )
  return(x)
p1 = plot( get_part(as_fitted_DAG(fit)), type="width", show.legend=FALSE)
p1$layers[[1]]$mapping$edge_width = 0.5
p2 = plot( get_part(as_fitted_DAG(fit, what="p_value" )), type="width",
           show.legend=FALSE, colors=c('black', 'black'))
p2$layers[[1]]$mapping$edge_width = 0.1
longform = melt( sea otter[,-1], as.is=TRUE )
\#> Warning in type.convert.default(X[[i]], ...): 'as.is' should be specified by the caller; using TRUE
```

Again, these results are further discussed in the paper describing dsem.

## Simultaneous effects



# Two-sided p-value

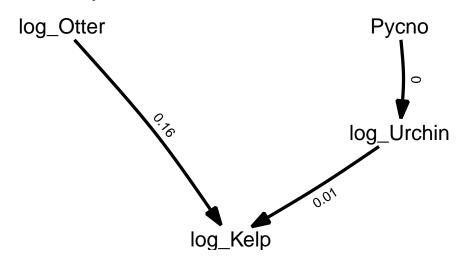


Figure 9: Structural model representing a trophic cascade