Computing Cumulative Incidence Functions with the etmCIF Function, with a view Towards Pregnancy Applications

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1 Introduction

This paper documents the use of the etmCIF function to compute the cumulative incidence function (CIF) in pregnancy data.

2 Data Example

The data set abortion, included in the **etm** package will be used to illustrate the computation of the CIFs. We first load the **etm** package and the data set.

- > require(etm)
- > data(abortion)

Briefly, the data set contains information on 1186 pregnant women collected prospectively by the Teratology Information Service of Berlin, Germany (Meister and Schaefer, 2008). Among these pregnant women, 173 were exposed therapeutically to coumarin derivatives, a class of orally active anticoagulant, and 1013 women served as controls. Coumarin derivatives are suspected to increase the number of spontaneous abortions. Competing events are elective abortion (ETOP) and life birth.

Below is an excerpt of the data set

> head(abortion)

	id	entry	exit	group	cause
1	1	6	37	0	2
2	2	9	40	0	2
3	3	29	40	0	2
4	4	32	41	0	2
5	5	11	39	0	2
6	6	10	39	0	2

id is the individual number, entry is the gestational age at which the women entered the study, exit is the gestational age at the end of pregnancy, group is

the group membership (0 for controls and 1 for the women exposed to coumarin derivatives) and cause is the cause of end of pregnancy (1 for induced abortion, 2 for life birth and 3 for spontaneous abortion.)

3 Computing and plotting the CIFs

3.1 The etmCIF function

The CIFs are computed using the etmCIF function. It is a wrapper around the etm function, meant to facilitate the computation of the CIFs. etmCIF takes as arguments

- formula: A formula consisting of a Surv object on the left of a operator, and the group covariate on the right. A Surv object is for example created this way: Surv(entry, exit, cause != 0). We need to specify the entry time (entry), the gestational age at end of pregnancy (exit), and an event indicator (cause != 0). The latter means that any value different from 0 in cause will be considered as an event which is the case in our example, as we don't have censoring.
- data: A data set in which to interpret the terms of the formula. In our case, it will be abortion.
- etype: Competing risks event indicator. When the status indicator is 1 (or TRUE) in the formula, etype describes the type of event, otherwise, for censored observation, the value of etype is ignored.
- failcode: Indicates the failure type of interest. Default is one. This option is only interesting for some features of the plot function.

3.2 Estimation and display of the CIFs

```
We know compute the CIFs
```

```
CIF 2
        43 0.79905931 0.022186468
                                       924
CIF 3
        43 0.16078139 0.021326113
                                        69
 group = 1
      time
                   Ρ
                           se(P) n.event
        42 0.2851118 0.04249308
                                      38
CIF 1
        42 0.3525651 0.04213898
                                      92
CIF 3
        42 0.3623231 0.04947340
                                      43
```

Above is the display provided by the print function. It gives, at the last event time, the probabilities (P) standard errors (se(P)), and the total number of events (n.event) for the three possible pregnancy outcomes and for both groups.

More information is provided by the summary function.

> s.cif.ab <- summary(cif.abortion)</pre>

The function returns a list of data frames that contain probabilities, variances, pointwise confidence intervals, number at risk and number of events for each event times. the print function displays this information for some selected event times.

> s.cif.ab

group=0

CIF 1

Р	time	var	lower	upper	n.risk	n.event
0.00000000	4	0.000000e+00	0.00000000	0.0000000	18	0
0.03895488	13	8.444048e-05	0.02448808	0.06169378	645	1
0.04015931	23	8.570657e-05	0.02551262	0.06293875	819	0
0.04015931	33	8.570657e-05	0.02551262	0.06293875	885	0
0.04015931	39	8.570657e-05	0.02551262	0.06293875	716	0
0.04015931	43	8.570657e-05	0.02551262	0.06293875	6	0

CIF 2

P	time	var	lower	upper	n.risk	n.event
0.00000000	4	0.000000e+00	0.000000000	0.0000000	18	0
0.00000000	13	0.000000e+00	0.000000000	0.0000000	645	0
0.00000000	23	0.000000e+00	0.000000000	0.0000000	819	0
0.01354288	33	1.216141e-05	0.008169604	0.02241009	885	6
0.32201590	39	2.469805e-04	0.292313907	0.35391574	716	165
0.79905931	43	4.922394e-04	0.753968839	0.84061317	6	6

CIF 3

P time var lower upper n.risk n.event 0.0000000 4 0.000000000 0.0000000 0.0000000 18 0

0.1504675	13	0.0004551293	0.1135970	0.1979013	645	1
0.1570366	23	0.0004553237	0.1199469	0.2041947	819	0
0.1599039	33	0.0004549788	0.1227389	0.2069247	885	0
0.1607814	39	0.0004548031	0.1235965	0.2077571	716	0
0.1607814	43	0.0004548031	0.1235965	0.2077571	6	0

group=1

CIF 1

P	time	var	lower	upper	${\tt n.risk}$	n.event
0.0000000	4	0.000000000	0.0000000	0.0000000	8	0
0.2604775	12	0.001785362	0.1879526	0.3542503	94	5
0.2811533	21	0.001802770	0.2074197	0.3742279	93	1
0.2851118	32	0.001805662	0.2111650	0.3780568	90	0
0.2851118	38	0.001805662	0.2111650	0.3780568	71	0
0.2851118	42	0.001805662	0.2111650	0.3780568	6	0

CIF 2

P	time	var	lower	upper	n.risk	n.event
0.00000000	4	0.000000e+00	0.000000000	0.00000000	8	0
0.00000000	12	0.000000e+00	0.000000000	0.00000000	94	0
0.00000000	21	0.000000e+00	0.000000000	0.00000000	93	0
0.01541036	32	6.016217e-05	0.005730041	0.04110307	90	1
0.13034947	38	5.576254e-04	0.090999609	0.18489993	71	12
0.35256510	42	1.775693e-03	0.276882073	0.44177471	6	6

CIF 3

P	time	var	lower	upper	n.risk	n.event
0.0000000	4	0.00000000	0.0000000	0.0000000	8	0
0.3143493	12	0.002571501	0.2266494	0.4254211	94	1
0.3507019	21	0.002482739	0.2627692	0.4576195	93	0
0.3584918	32	0.002459261	0.2706266	0.4644770	90	0
0.3584918	38	0.002459261	0.2706266	0.4644770	71	0
0.3623231	42	0.002447617	0.2744987	0.4678544	6	0

3.3 Plotting the CIFs

Interest lies in the CIFs of spontaneous abortion. We display them using the plot function, which by default, plots only the CIFs for the event of interest, i.e., the one specified in failcode.

> plot(cif.abortion)

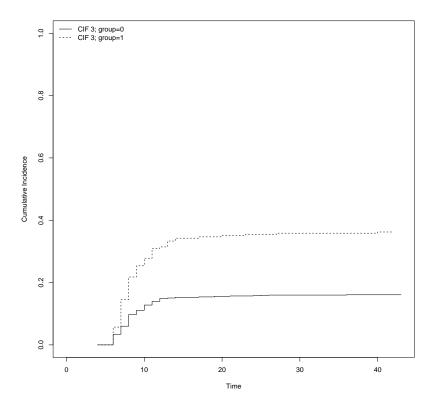


Figure 1: CIFs of spontaneous abortion for the controls (solid line) and the exposed (dashed line), using the default settings of the plot function.

We now add confidence intervals taken at week 27, plus a bit of customisation.

```
> plot(cif.abortion, curvlab = c("Control", "Exposed"), ylim = c(0, 0.6),
+ ci.type = "bars", pos.ci = 27, col = c(1, 2), ci.lwd = 6,
+ lwd = 2, lty = 1, cex = 1.3)
```

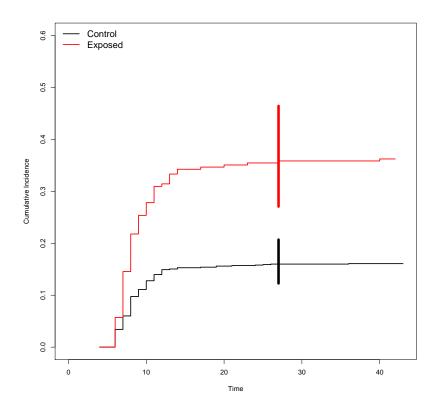


Figure 2: CIFs of spontaneous abortion for the controls (black) and the exposed (red), along with pointwise confidence intervals taken at week 27.

When the figure is to be in black and white, or when the confidence intervals are not as separated as in this example, it might be a good idea to shift slightly one of the bar representing the confidence interval, so that the two bars don't overlap. This might be done manipulating the pos.ci argument:

```
> plot(cif.abortion, curvlab = c("Control", "Exposed"), ylim = c(0, 0.6),
+ ci.type = "bars", pos.ci = c(27, 28), col = c(1, 1), ci.lwd = 6,
+ lwd = 2, lty = c(2, 1), cex = 1.3)
```

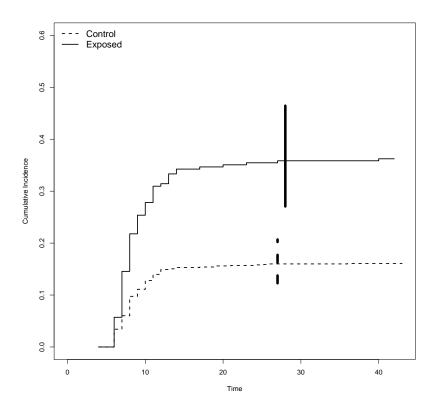


Figure 3: CIFs of spontaneous abortion for the controls (dashed line) and the exposed (solid line), along with pointwise confidence intervals.

Pointwise confidence intervals can also be plotted for the whole follow-up period.

```
> plot(cif.abortion, curvlab = c("Control", "Exposed"), ylim = c(0, 0.5), + ci.type = "pointwise", col = c(1, 2), lwd = 2, lty = 1, cex = 1.3)
```

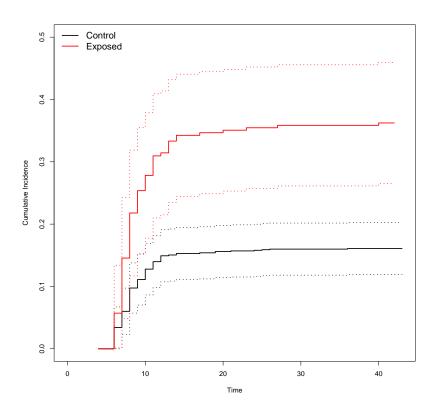


Figure 4: Same as the last pictures, except for the confidence intervals, that are displayed for the whole follow-up period.

CIFs for other pregnancy outcomes can also be plotted using the which.cif arguments. For instance, for plotting the CIFs of ETOP and life birth on the same graph, we specify which.cif = c(1, 2) in the call to plot.

```
> plot(cif.abortion, which.cif = c(1, 2), ylim = c(0, 0.8), lwd = 2,
+ col = c(1, 1, 2, 2), lty = c(1, 2, 1, 2), legend = FALSE)
> legend(0, 0.8, c("Control", "Exposed"), col = c(1, 2), lty = 1,
+ bty = "n", lwd = 2)
> legend(0, 0.7, c("ETOP", "Life Birth"), col = 1, lty = c(1, 2),
+ bty = "n", lwd = 2)
```

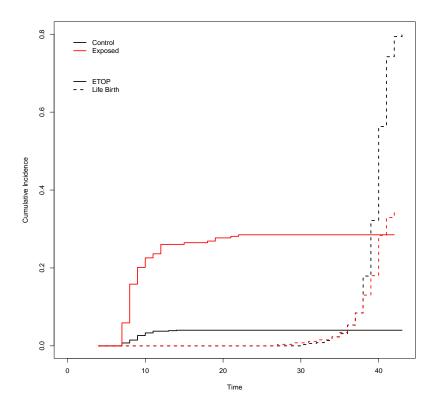


Figure 5: CIFs of ETOP (solid lines) and life birth (dashed lines) for the exposed, in red, and the controls, in black.

3.4 Some More Features

Competing event names For those who don't like using plain numbers for naming the competing events or the group allocation, it is of course possible to give more informative names, either as factors or character vectors. For instance, we define a new group variable that takes value 'control' or 'exposed', and we give more informative names for the pregnancy outcomes.

```
> abortion$status <- with(abortion, ifelse(cause == 2, "life birth",
                           ifelse(cause == 1, "ETOP", "spontaneous abortion")))
> abortion$status <- factor(abortion$status)</pre>
> abortion$treat <- with(abortion, ifelse(group == 0, "control", "exposed"))
> abortion$treat <- factor(abortion$treat)</pre>
   We can compute the CIFs as before, taking care of changing the failcode
argument.
> new.cif <- etmCIF(Surv(entry, exit, status != 0) ~ treat, abortion,
                    etype = status, failcode = "spontaneous abortion")
> new.cif
Call: etmCIF(formula = Surv(entry, exit, status != 0) ~ treat, data = abortion,
    etype = status, failcode = "spontaneous abortion")
Covariate: treat
        levels: control exposed
 treat = control
                          time
                                                se(P) n.event
CIF ETOP
                            43 0.04015931 0.009257784
                                                            20
CIF life birth
                            43 0.79905931 0.022186468
                                                           924
CIF spontaneous abortion
                           43 0.16078139 0.021326113
                                                            69
 treat = exposed
                                       Ρ
                                              se(P) n.event
                          time
CIF ETOP
                            42 0.2851118 0.04249308
                                                          38
CIF life birth
                           42 0.3525651 0.04213898
                                                          92
                           42 0.3623231 0.04947340
CIF spontaneous abortion
                                                          43
```

The summary and plot functions will work as before, except for a more informative outcome from scratch.

Taking advantage of the miscellaneous functions defined for etm objects The etmCIF function uses the more general etm machinery for computing the CIFs. Thus the returned etmCIF object is for part a list of etm objects (one for each covariate level). It is therefore relatively easy to use the methods defined for etm on etmCIF objects.

An example would be to use the trprob function to extract the CIF of spontaneous abortion for the controls. This function takes as arguments an etm object, the transition we are interested in, in the form "from to" (the state a patient comes from is automatically defined as being 0 in etmCIF), and possibly some time points. Using new.cif from the example above:

```
> trprob(new.cif[[1]], "O spontaneous abortion", c(1, 10, 27))
```

[1] 0.0000000 0.1278037 0.1599039

We applied the trprob function to the etm object for the controls (which is in the first item of the output, for the exposed in the second). The transition of interest is from 0 to spontaneous abortion, and we want the CIF at weeks 1, 10 and 27 (just put nothing if you want the CIF for all time points).

Another example would be to use the lines function to add a CIF to an existing plot. The following code snippet adds the CIF of ETOP for the exposed to Figure 3. That's the tr.choice arguments that defines which CIF to pick. It works in the same way as in the trprob function.

> lines(cif.abortion[[2]], tr.choice = "0 1", col = 2, lwd = 2)

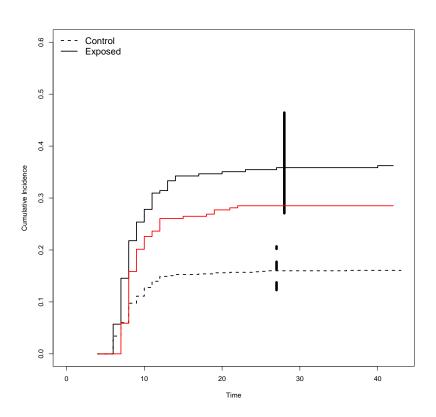


Figure 6: Figure 3 along with the CIF of ETOP for the exposed in red.

References

Meister, R. and Schaefer, C. (2008). Statistical methods for estimating the probability of spontaneous abortion in observational studies—analyzing pregnancies exposed to coumarin derivatives. *Reproductive Toxicology*, 26(1):31–35.