# Exchange Rate Regime Analysis for the Indian Rupee

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#### Abstract

We investigate the Indian exchange rate regime starting from 1993 when trading in the Indian rupee began up to the end of 2007. This reproduces the analysis from Zeileis, Shah, and Patnaik (2010) which includes a more detailed discussion.

## 1 Analysis

Exchange rate regime analysis is based on a linear regression model for cross-currency returns. A large data set derived from exchange rates available online from the US Federal Reserve at http://www.federalreserve.gov/releases/h10/Hist/ is provided in the FXRatesCHF data set in fxregime.

```
> library("fxregime")
> data("FXRatesCHF", package = "fxregime")
```

It is a "zoo" series containing 25 daily time series from 1971-01-04 to 2010-02-12. The columns correspond to the prices for various currencies (in ISO 4217 format) with respect to CHF as the unit currency.

India is an expanding economy with a currency that has been receiving increased interest over the last years. India is in the process of evolving away from a closed economy towards a greater integration with the world on both the current account and the capital account. This has brought considerable stress upon the pegged exchange rate regime. Therefore, we try to track the evolution of the INR exchange rate regime since trading in the INR began in about 1993 up to the end of 2007. The currency basket employed consists of the most important floating currencies (USD, JPY, EUR, GBP). Because EUR can only be used for the time after its introduction as official euro-zone currency in 1999, we employ the exchange rates of the German mark (DEM, the most important currency in the EUR zone) adjusted to EUR rates. The combined returns are denoted DUR below in FXRatesCHF:

```
> inr <- fxreturns("INR", frequency = "weekly",
+ start = as.Date("1993-04-01"), end = as.Date("2008-01-04"),
+ other = c("USD", "JPY", "DUR", "GBP"), data = FXRatesCHF)</pre>
```

Weekly rather than daily returns are employed to reduce the noise in the data and alleviate the computational burden of the dating algorithm of order  $O(n^2)$ .

Using the full sample, we establish a single exchange rate regression only to show that there is not a single stable regime and to gain some exploratory insights from the associated fluctuation process.

```
> inr_lm <- fxlm(INR ~ USD + JPY + DUR + GBP, data = inr)</pre>
```

As we do not expect to be able to draw valid conclusions from the coefficients of a single regression, we do not report the coefficients and rather move on directly to assessing its stability using the associated empirical fluctuation process.

```
> inr_efp <- gefp(inr_lm, fit = NULL)
> plot(inr_efp, aggregate = FALSE, ylim = c(-1.85, 1.85))
```

Its visualization in Figure 1 shows that there is significant instability because two processes (intercept and variance) exceed their 5% level boundaries. More formally, the corresponding double maximum can be performed by

```
M-fluctuation test

data: inr_efp
f(efp) = 1.7242, p-value = 0.03099
```

> sctest(inr\_efp)

This p value is not very small because there seem to be several changes in various parameters. A more suitable test in such a situation would be the Nyblom–Hansen test

However, the multivariate fluctuation process is interesting as a visualization of the changes in the different parameters. The process for the variance  $\sigma^2$  has the most distinctive shape revealing at least four different regimes: at first, a variance that is lower than the overall average (and hence a decreasing process), then a much larger variance (up to the boundary crossing), a much smaller variance again and finally a period where the variance is roughly the full-sample average. Other interesting processes are the intercept and maybe the USD and DUR. The latter two are not significant but have some peaks revealing a decrease and increase, respectively, in the corresponding coefficients.

To capture this exploratory assessment in a formal way, a dating procedure is conducted for  $1, \ldots, 10$  breaks and a minimal segment size of 20 observations.

```
> inr_reg <- fxregimes(INR ~ USD + JPY + DUR + GBP,
+ data = inr, h = 20, breaks = 10)</pre>
```

# M-fluctuation test (Intercept) DUR ī GBP ī ī (Variance) JΡY Ţ 2005 1995 2000 1995 2000 2005 Time Time

Figure 1: Historical fluctuation process for INR exchange rate regime.

#### [1] TRUE

The associated segmented negative log-likelihood (NLL) and LWZ criterion. Both can be visualized via

#### > plot(inr\_reg)

producing Figure 2. NLL is decreasing quickly up to 3 breaks with a kink in the slope afterwards. Similarly, LWZ takes its minimum for 3 breaks, choosing a 4-segment model. The confidence intervals corresponding to the breaks can be obtained by

#### LWZ and Negative Log-Likelihood

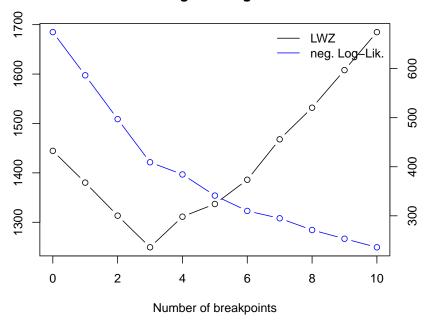


Figure 2: Negative log-likelihood and LWZ information criterion for INR exchange rate regimes.

> confint(inr\_reg, level = 0.9)

Confidence intervals for breakpoints of optimal 4-segment partition:

#### Call:

confint.fxregimes(object = inr\_reg, level = 0.9)

Breakpoints at observation number:

5 % breakpoints 95 % 1 84 100 101 2 280 281 298 3 556 572 574

Corresponding to breakdates:

5 % breakpoints 95 % 1 1994-11-11 1995-03-03 1995-03-10 2 1998-08-14 1998-08-21 1998-12-18 3 2003-11-28 2004-03-19 2004-04-02

showing that the start/end of segments with low variance can be determined more precisely than for segments with high variance.

The parameter estimates for all segments can be queried via

#### > coef(inr\_reg)

```
(Intercept)
                                      USD
                                                  JPY
                                                             DUR.
1993-04-09--1995-03-03 -0.005740591 0.9716100 0.023466575
                                                      0.01126713
1995-03-10--1998-08-21
                     0.161133317 0.9431395 0.066918732 -0.02606616
1998-08-28--2004-03-19
                     0.018610654 0.9933245 0.009763423
                                                      0.09831871
2004-03-26--2008-01-04 -0.057614447 0.7464939 0.125614049 0.43544995
                             GBP (Variance)
1993-04-09--1995-03-03
                     0.020370927 0.02476617
1995-03-10--1998-08-21
                     0.042358762 0.85392476
1998-08-28--2004-03-19 -0.003220436 0.07554646
```

The most striking observation from the segmented coefficients is that INR was closely pegged to USD up to 2004-03-19 when it shifted to a basket peg in which USD has still the highest weight but considerably less than before. Furthermore, the changes in  $\sigma$  are remarkable, roughly matching the exploratory observations from the empirical fluctuation process. A more detailed look at the full summaries provided below shows that the first period is a clear and tight USD peg. During that time, pressure to appreciate was blocked by purchases of USD by the central bank. The second period, including the time of the East Asian crisis, saw a highly increased flexibility in the exchange rates. Although the Reserve Bank of India (RBI) made public statements about managing volatility on the currency market, the credibility of these statements were low in the eyes of the market. The third period exposes much tighter pegging again with low volatility, some appreciation and some small (but significant) weight on DUR. In the fourth period after March 2004, India moved away from the tight USD peg to a basket peg involving several currencies with greater flexibility (but smaller than in the second period). In this period, reserves in excess of 20% of GDP were held by the RBI, and a modest pace of reserves accumulation has continued.

```
> inr_rf <- refit(inr_reg)</pre>
> lapply(inr_rf, summary)
$'1993-04-09--1995-03-03'
Call:
fxlm(formula = object$formula, data = window(object$data, start = sbp[i],
    end = ebp[i]))
Residuals:
     Min
                                  3Q
                1Q
                     Median
                                           Max
-0.89169 -0.03021 0.00528
                             0.03859
                                       0.89131
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
```

```
(Intercept) -0.005741 0.016507 -0.348 0.7288
           0.971610 0.017626 55.124 <2e-16 ***
USD
JPY
           0.023467 0.013988 1.678 0.0967 .
           DUR
GBP
           0.020371 0.024284 0.839 0.4037
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Residual standard error: 0.1615 on 95 degrees of freedom
Multiple R-squared: 0.9893,
                              Adjusted R-squared: 0.9889
F-statistic: 2205 on 4 and 95 DF, p-value: < 2.2e-16
$'1995-03-10--1998-08-21'
Call:
fxlm(formula = object$formula, data = window(object$data, start = sbp[i],
   end = ebp[i]))
Residuals:
           1Q Median
                          3Q
                                Max
-4.8702 -0.2943 -0.1225 0.2002 4.5560
Coefficients:
          Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.16113 0.07052 2.285 0.0235 *
USD
           0.94314
                    0.07372 12.794 <2e-16 ***
           JPY
DUR
          -0.02607 0.15530 -0.168 0.8669
          0.04236 0.07980 0.531 0.5962
GBP
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Residual standard error: 0.9371 on 176 degrees of freedom
Multiple R-squared: 0.7289,
                               Adjusted R-squared: 0.7227
F-statistic: 118.3 on 4 and 176 DF, p-value: < 2.2e-16
$'1998-08-28--2004-03-19'
Call:
fxlm(formula = object$formula, data = window(object$data, start = sbp[i],
   end = ebp[i]))
Residuals:
    Min
             1Q
                Median
                             3Q
                                    Max
-0.94397 -0.12781 -0.02506 0.08499 1.11702
```

```
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.018611
                       0.016292
                                  1.142
                                         0.25427
USD
                       0.016092 61.726 < 2e-16 ***
            0.993324
JPY
            0.009763 0.009838
                                  0.992
                                         0.32185
DUR
            0.098319
                       0.033850
                                  2.905
                                         0.00397 **
GBP
           -0.003220
                       0.020529 -0.157 0.87546
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Residual standard error: 0.2772 on 286 degrees of freedom
Multiple R-squared: 0.9688,
                                   Adjusted R-squared:
F-statistic: 2222 on 4 and 286 DF, p-value: < 2.2e-16
$'2004-03-26--2008-01-04'
Call:
fxlm(formula = object$formula, data = window(object$data, start = sbp[i],
    end = ebp[i]))
Residuals:
     Min
              1Q
                   Median
                                3Q
                                        Max
-2.19182 -0.29861 0.01349 0.25854 1.57820
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-0.05761	0.04195	-1.373	0.171227	
USD	0.74649	0.04458	16.746	< 2e-16	***
JPY	0.12561	0.04230	2.970	0.003361	**
DUR	0.43545	0.11588	3.758	0.000227	***
GBP	0.12137	0.05608	2.164	0.031673	*

Signif. codes: 0 '\*\*\* 0.001 '\*\* 0.01 '\* 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.586 on 193 degrees of freedom

Multiple R-squared: 0.8002, Adjusted R-squared: 0.796

F-statistic: 193.2 on 4 and 193 DF, p-value: < 2.2e-16

#### 2 Summary

For the Indian rupee, a 4-segment model is found with a close linkage of INR to USD in the first three periods (with tight/flexible/tight pegging, respectively) before moving to a more flexible basket peg in spring 2004.

The existing literature classifies the INR is a de facto pegged exchange rate to the USD in the

period after April 1993. The results above show the fine structure of this pegged exchange rate; it supplies dates demarcating the four phases of the exchange rate regime; and it finds that by the fourth period, there was a basket peg in operation.

### References

Zeileis A, Shah A, Patnaik I (2010). "Testing, Monitoring, and Dating Structural Changes in Testing, Monitoring, and Dating Structural Changes in Exchange Rate Regimes." Computational Statistics & Data Analysis, 54(6), 1696–1706. doi:10.1016/j.csda.2009.12.005.