A one-minute introduction to the gRain package

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1 Introduction

The gRain package implements propagation in [gra]phical [i]ndependence [n]etworks (hereafter abbreviated grain). Such networks are also known as probabilistic networks and Bayesian networks. More information about the package might be available from the webpage http://gbi.agrsci.dk/~sorenh/R/gRainweb.

2 A worked example: chest clinic

This section reviews the chest clinic example of Lauritzen and Spiegelhalter (1988) (illustrated in Figure 1) and shows one way of specifying the model in gRain. Lauritzen and Spiegelhalter (1988) motivate the chest clinic example as follows:

"Shortness—of—breath (dyspnoea) may be due to tuberculosis, lung cancer or bronchitis, or none of them, or more than one of them. A recent visit to Asia increases the chances of tuberculosis, while smoking is known to be a risk factor for both lung cancer and bronchitis. The results of a single chest X—ray do not discriminate between lung cancer and tuberculosis, as neither does the presence or absence of dyspnoea."

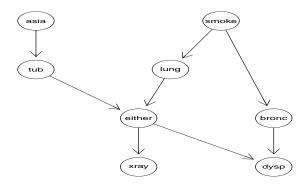


Figure 1: Chest clinic example from LS.

2.1 Building a grain

A Bayesian network is a special case of graphical independence networks. In this section we outline how to build a Bayesian network. The starting point is a probability distribution factorising according to a DAG with nodes V. Each node $v \in V$ has a set pa(v) of parents and each node $v \in V$ has a finite set of states. A joint distribution over the variables V can be given as

$$p(V) = \prod_{v \in V} p(v|pa(v)) \tag{1}$$

where p(v|pa(v)) is a function defined on (v, pa(v)). This function satisfies that $\sum_{v^*} p(v = v^*|pa(v)) = 1$, i.e. that for each configuration of the parents pa(v), the sum over the levels of v equals one. Hence p(v|pa(v)) becomes the conditional distribution of v given pa(v). In practice p(v|pa(v)) is specified as a table called a conditional probability table or a CPT for short. Thus, a Bayesian network can be regarded as a complex stochastic model built up by putting together simple components (conditional probability distributions).

Thus the DAG in Figure 1 dictates a factorization of the joint probability function as $\frac{1}{2}$

$$p(V) = p(\alpha)p(\sigma)p(\tau|\alpha)p(\lambda|\sigma)p(\beta|\sigma)p(\epsilon|\tau,\lambda)p(\delta|\epsilon,\beta)p(\xi|\epsilon). \tag{2}$$

In (2) we have $\alpha =$ asia, $\sigma =$ smoker, $\tau =$ tuberculosis, $\lambda =$ lung cancer, $\beta =$ bronchitis, $\epsilon =$ either tuberculosis or lung cancer, $\delta =$ dyspnoea and $\xi =$ xray. Note that ϵ is a logical variable which is true if either τ or λ are true and false otherwise.

2.2 Queries to grains

Suppose we are given the finding (evidence) that a set of variables $E \subset V$ have a specific value e^* . For example that a person has recently visited Asia and suffers from dyspnoea, i.e. $\alpha = \text{yes}$ and $\delta = \text{yes}$.

With this finding, we are often interested in the conditional distribution $p(v|E=e^*)$ for some of the variables $v \in V \setminus E$ or in $p(U|E=e^*)$ for a set $U \subset V \setminus E$.

In the chest clinic example, interest might be in $p(\lambda|e^*)$, $p(\tau|e^*)$ and $p(\beta|e^*)$, or possibly in the joint (conditional) distribution $p(\lambda, \tau, \beta|e^*)$.

Interest might also be in calculating the probability of a specific event, e.g. the probability of seeing a specific finding, i.e. $p(E = e^*)$.

3 A one-minute version of gRain

A simple way of specifying the model for the chest clinic example is as follows.

1. Specify conditional probability tables (with values as given in Lauritzen and Spiegelhalter (1988)):

2. Create the grain from the conditional probability tables:

```
> plist <- compileCPT(list(a, t.a, s, l.s, b.s, e.lt, x.e, d.be))
> plist

CPTspec with probabilities:
  P( asia )
  P( tub | asia )
  P( smoke )
  P( lung | smoke )
  P( bronc | smoke )
  P( either | lung tub )
  P( xray | either )
  P( dysp | bronc either )
```

```
> in1 <- grain(plist)</pre>
  > in1
  Independence network: Compiled: FALSE Propagated: FALSE
   Nodes: chr [1:8] "asia" "tub" "smoke" "lung" "bronc" "either" "xray" ...
3. The grain can be queried to give marginal probabilities:
  > querygrain(in1,nodes=c("lung","bronc"), type="marginal")
  $lung
  lung
    yes
           no
  0.055 0.945
  $bronc
  bronc
   yes
  0.45 0.55
  Likewise, a joint distribution can be obtained.
  > querygrain(in1,nodes=c("lung","bronc"), type="joint")
       bronc
  lung
           yes
    yes 0.0315 0.0235
    no 0.4185 0.5265
4. Findings can be entered as:
  > in12 <- setFinding(in1,nodes=c("asia","dysp"),states=c("yes","yes"))</pre>
5. The grain can be queried again:
  > querygrain(in12,nodes=c("lung","bronc"))
  $lung
  lung
          yes
  0.09952515 0.90047485
  $bronc
  bronc
         yes
                    no
  0.8114021 0.1885979
  > querygrain(in12,nodes=c("lung","bronc"), type="joint")
```

```
bronc
  lung
                yes
    yes 0.06298076 0.03654439
    no 0.74842132 0.15205354
6. Zero probabilities
  Consider setting the finding
  > in13 <- setFinding(in1,nodes=c("either","tub"),states=c("no","yes"))</pre>
  Under the model, this finding has zero probability;
  > pFinding(in13)
  [1] 0
  Therefore, all conditional probabilities are (under the model) undefined;
  > querygrain(in13,nodes=c("lung","bronc"), type="joint")
        bronc
  lung yes no
    yes NaN NaN
    no NaN NaN
```

References

Steffen Lilholt Lauritzen and David Spiegelhalter. Local computations with probabilities on graphical structures and their application to expert systems. J. Roy. Stat. Soc. Ser. B, 50(2):157–224, 1988.