Primitive array operations in the gRbase package

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>	library(gRbase)	

1 Introduction

This note describes some operations on arrays in R. These operations have been implemented to facilitate implementation of graphical models and Bayesian networks in R.

1.1 Arrays in R

The documentation of R states the following about arrays:

An array in R can have one, two or more dimensions. It is simply a vector which is stored with additional attributes giving the dimensions (attribute "dim") and optionally names for those dimensions (attribute "dimnames").

A two-dimensional array is the same thing as a matrix.

One-dimensional arrays often look like vectors, but may be handled differently by some functions.

Hence the defining characteristic of an array is that it is a vector with a dim attribute. For example

```
> ## 1-dimensional array
> ##
> x1 <- 1:8
> dim(x1) < -8
> x1
[1] 1 2 3 4 5 6 7 8
> is.array(x1)
[1] TRUE
> is.matrix(x1)
[1] FALSE
> ## 2-dimensional array (matrix)
> ##
> x2 <- 1:8
> dim(x2) <- c(2,4)
> x2
     [,1] [,2] [,3] [,4]
    1 3 5 7
[2,]
> is.array(x2)
[1] TRUE
> is.matrix(x2)
[1] TRUE
> ## 3-dimensional array
> ##
> x3 <- array(1:8, dim=c(2,2,2))
> x3
, , 1
     [,1] [,2]
[1,] 1 3
[2,]
       2
, , 2
     [,1] [,2]
[1,]
      5 7
[2,]
       6
> is.array(x3)
[1] TRUE
> is.matrix(x3)
[1] FALSE
```

1.2 Terminology

Consider a set $\Delta = \{\delta_1, \dots, \delta_K\}$ of $|\Delta| = K$ factors where the factor δ_k has levels I_k . The cross product $I = I_1 \times \dots \times I_K$ defines an array where $i = (i_1, \dots, i_K) \in I$ is a cell. It is the convention

here that the first factor varies fastest. To each cell $i \in I$ there is often a value f(i).

As shown above, an array is implemented as a vector x of length L = |I|, that is $x \equiv (f(i), i \in I)$. In practice x is indexed by an entry e as x[e] for $e = 1, \ldots, L$.

The factor levels (I_1, \ldots, I_K) are denoted flevels in the code below. As an example we take the following:

```
> flevels <- c(2,3,2,4)
```

2 cell2entry() and entry2cell()

The map from a cell to the corresponding entry is provided by cell2entry(). The reverse operation, going from an entry to a cell (which is much less needed) is provided by entry2cell().

```
> cell2entry(c(1,1,1,1), flevels)
[1] 1
> entry2cell(1, flevels)
[1] 1 1 1 1
> cell2entry(c(2,1,2,1), flevels)
[1] 8
> entry2cell(8, flevels)
[1] 2 1 2 1
```

3 nextCell() and nextCellMarg()

Given a cell, say i = (1, 1, 2, 1) we often want to find the next cell in the table following the convention that the first factor varies fastest, that is (2, 1, 2, 1). This is provided by nextCell(). Notice the result of finding the next cell to the final cell.

```
> nextCell(c(1,1,2,1), flevels)

[1] 2 1 2 1

> nextCell(c(2,3,2,4), flevels)

NULL
```

Given $A \subset \Delta$ and a cell $i_A \in I_A$ consider the cells $I(i_A) = \{j \in I | j_A = i_A\}$. For example, the cells satisfying that factor 2 is at level 1. Given such a cell, say (2,1,1,2) we often want to find the next cell also satisfying this constraint following the convention that the first factor varies fastest, that is (1,1,2,2). This is provided by nextCellMarg().

```
> nextCellMarg(c(1,3,2,1), margset=c(2,3), flevels)

[1] 2 3 2 1

> nextCellMarg(c(2,3,2,1), margset=c(2,3), flevels)

[1] 1 3 2 2
```

4 margcell2entry()

Given $A \subset \Delta$ and a cell $i_A \in I_A$. This cell defines a slice of the original array, namely the cells $I(i_A) = \{j \in I | j_A = i_A\}$. We often want to find the entries in x for the cells $I(i_A)$. This is provided by margcell2entry(). To be specific, we may want the entries for the cells (*, 1, 2, *) or (2, 2, *, *):

```
> margcell2entry(margcell=c(1,2), margset=c(2,3), flevels)
[1] 7 8 19 20 31 32 43 44
> margcell2entry(margcell=c(2,2), margset=c(1,2), flevels)
[1] 4 10 16 22 28 34 40 46
```

5 Factorial grids

Using the operations above we can obtain the combinations of the factors as a matrix:

```
> ff <- factgrid(flevels)
> head(ff)
     [,1] [,2] [,3] [,4]
[1,]
       1
           1
                 1
[2,]
        2
             1
                  1
[3,]
       1
             2
[4,]
             2
        2
                  1
                     1
[5,]
        1
             3
                  1
[6,]
                  1
> tail(ff)
      [,1] [,2] [,3] [,4]
[43,]
                   2
       1
             1
                        4
                   2
                        4
[44,]
        2
              1
              2
                 2
[45,]
        1
                        4
        2
              2
                 2
                        4
[46,]
[47,]
              3
[48,]
> ff <- factgrid(flevels, margcell=c(1,2), margset=c(2,3))</pre>
> ff
     [,1] [,2] [,3] [,4]
[1,]
       1
             1
                  2
                       1
[2,]
        2
                  2
                       1
             1
[3,]
        1
             1
                  2
                       2
        2
                  2
                       2
[4,]
             1
[5,]
        1
             1
                  2
                       3
[6,]
        2
                  2
                      3
[7,]
        1
             1
                  2
                       4
[8,]
```