# Analyzing data

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#### Where are we so far?

- 1. Introduction: vignette("gc01\_gcplyr")
- 2. Importing and reshaping data: vignette("gc02\_import\_reshape")
- 3. Incorporating experimental designs: vignette("gc03\_incorporate\_designs")
- 4. Pre-processing and plotting your data: vignette("gc04\_preprocess\_plot")
- 5. Processing your data: vignette("gc05\_process")
- 6. Analyzing your data: vignette("gc06\_analyze")
- 7. Dealing with noise: vignette("gc07\_noise")
- 8. Statistics, merging other data, and other resources: vignette("gc08\_conclusion")
- 9. Working with multiple plates: vignette("gc09\_multiple\_plates")

So far, we've imported and transformed our measures, combined them with our design information, preprocessed, processed, and plotted our data. Now we're going to analyze our data by summarizing our growth curves into a number of metrics.

If you haven't already, load the necessary packages.

```
library(gcplyr)
library(dplyr)
library(ggplot2)
```

```
# This code was previously explained
# Here we're re-running it so it's available for us to work with
example_tidydata <- trans_wide_to_tidy(example_widedata_noiseless,</pre>
                                        id cols = "Time")
ex_dat_mrg <- merge_dfs(example_tidydata, example_design_tidy)</pre>
#> Joining, by = "Well"
ex_dat_mrg$Well <-</pre>
  factor(ex dat mrg$Well,
         levels = paste(rep(LETTERS[1:8], each = 12), 1:12, sep = ""))
ex_dat_mrg$Time <- ex_dat_mrg$Time/3600 #Convert time to hours
ex_dat_mrg <-
  mutate(group_by(ex_dat_mrg, Well, Bacteria_strain, Phage),
         deriv = calc_deriv(x = Time, y = Measurements),
         deriv_percap5 = calc_deriv(x = Time, y = Measurements,
                                         percapita = TRUE, blank = 0,
                                         window_width_n = 5, trans_y = "log"),
         doub_time = doubling_time(y = deriv_percap5))
sample_wells <- c("A1", "F1", "F10", "E11")</pre>
# Drop unneeded columns (optional, but makes things cleaner)
ex_dat_mrg <- dplyr::select(ex_dat_mrg,</pre>
                             Time, Well, Measurements, Bacteria_strain, Phage,
                             deriv, deriv_percap5)
```

### Analyzing data with summarize

Ultimately, analyzing growth curves requires summarizing the entire time series of data by some metric or metrics. gcplyr makes it easy to calculate a number of metrics of interest, which I've grouped below into categories:

#### Most common metrics

- the lag time
- the maximum cellular growth rate (i.e. minimum doubling time)
- the maximum density (e.g. carrying capacity)
- the area under the curve

#### Growth

- the initial density
- the lag time
- the time to reach some density
- the time to reach some growth rate
- the maximum per-capita growth rate (i.e. minimum doubling time)

#### Saturation

- the mid-point time or inflection point
- the maximum density (e.g. carrying capacity)

#### Total growth

• the area under the curve

#### Diauxic growth

- the density and time when a diauxic shift occurs
- the maximum per-capita growth rate during diauxie

#### Growth with antagonists (e.g. phages)

- the peak bacterial density before a decline (e.g. from phage predation)
- the extinction time (e.g. from phage predation)

The following sections show how you can use gcplyr functions to calculate these metrics.

But first, we need to familiarize ourselves with one more dplyr function: summarize. Why? Because the upcoming gcplyr analysis functions *must* be used *within* dplyr::summarize. If you're already familiar with dplyr's summarize, feel free to skip the primer in the next section. If you're not familiar yet, don't worry! Continue to the next section, where I provide a primer that will teach you all you need to know on using summarize with gcplyr functions.

### Another brief primer on dplyr: summarize

Here we're going to focus on the summarize function from dplyr, which must be used with the group\_by function we covered in our first primer: A brief primer on dplyr. summarize carries out user-specified calculations on each group in a grouped data.frame independently, producing a new data.frame where each group is now just a single row.

For growth curves, this means we will:

- 1. group\_by our data so that every well is a group
- 2. summarize each well into one or several metrics

As before, to use group\_by we simply pass the data.frame to be grouped, and the names of the columns we want to group by. Since summarize will drop columns that the data aren't grouped by and that aren't summarized, we will typically want to list all of our design columns for group\_by, along with the plate name and well. Again, make sure you're not grouping by Time, Measurements, or anything else that varies within a well, since if you do dplyr will group timepoints within a well separately.

Then, we run summarize. summarize works much like mutate did, where we specify:

- 1. the name of the variable we want results saved to
- 2. the function that calculates the summarized results

Just like mutate, if we want additional summary metrics, we simply add them to the summarize. However, unlike mutate, summarize functions return just a single value for each group.

As you'll see throughout the rest of this article, we'll be using group\_by and summarize to calculate our metrics of interest. If you want to learn more, dplyr has extensive documentation and examples of its own online, but this primer and the coming example should be sufficient to analyze data with gcplyr.

### Plotting summarized metrics

Once you've calculated your summarized metrics, you should plot them on the original data to make sure everything matches what you expect. We can plot summarized values right on top of our original data:

- density or rate metrics can be plotted as a horizontal line with geom\_hline
- time metrics can be plotted as a vertical line with geom\_vline
- pairs of metrics that correspond to both density/rate and time can be plotted as a point with geom\_point

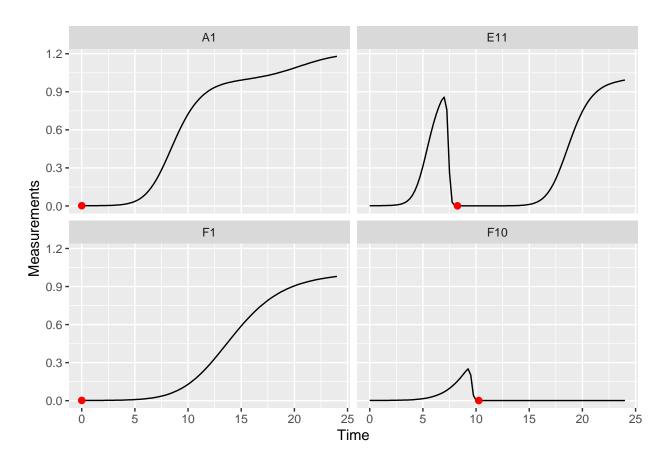
You'll see examples of these plots throughout this article.

# Initial density

If you want to identify the initial density of your bacteria, it will often be sufficient to use min\_gc (this works just like R's built-in min, but with better default settings for growth curve analyses with summarize).

We can also save the time when this minimum occurs using the which\_min\_gc function. which\_min\_gc returns the *index* of the minimum value, so then we can get the Time value at that index and save it to a column titled min\_time. (which\_min\_gc and extr\_val work just like R's built-in which.min and [, but with better default settings for growth curve analyses with summarize)

```
ex_dat_mrg_sum <-
  summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
            min dens = min gc(Measurements, na.rm = TRUE),
            min_time = extr_val(Time, which_min_gc(Measurements)))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 5
#> # Groups: Bacteria_strain, Phage [6]
   Bacteria_strain Phage
                                  Well min_dens min_time
                                  \langle fct \rangle
   <chr>
#>
                     <chr>
                                           <dbl>
                                                    <dbl>
#> 1 Strain 1
                     No Phage
                                  A1
                                           0.002
                                                     0
#> 2 Strain 1
                     Phage Added A7
                                           0.001
                                                     9.75
#> 3 Strain 10
                     No Phage
                                           0.002
                                  B4
                                                     0
#> 4 Strain 10
                     Phage Added B10
                                           0.001
                                                    11
#> 5 Strain 11
                     No Phage
                                 B5
                                           0.002
                                                     0
#> 6 Strain 11
                     Phage Added B11
                                           0.001
                                                     6
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% sample_wells),
       aes(x = Time, y = Measurements)) +
 geom_line() +
  facet_wrap(~Well) +
  geom_point(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
             aes(x = min_time, y = min_dens),
             size = 2, color = "red")
```



In some cases (e.g. growing with phages), bacteria may later drop to a lower density than they started in the growth curve. In this case, we want the first *local* minima of the Measurements data, rather than the global minima:

```
ex_dat_mrg_sum <-
  summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
           min_dens = first_minima(y = Measurements, x = Time, return = "y"),
           min_time = first_minima(y = Measurements, x = Time, return = "x"))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 5
#> # Groups: Bacteria_strain, Phage [6]
   Bacteria_strain Phage
                                 Well min_dens min_time
#>
    \langle chr \rangle
                  <chr>
                                 <fct> <dbl> <dbl>
#> 1 Strain 1
                    No Phage
                                A1
                                          0.002
#> 2 Strain 1
                    Phage Added A7
                                         0.002
                                                       0
#> 3 Strain 10
                    No Phage
                                B4
                                         0.002
                                                       0
#> 4 Strain 10
                    Phage Added B10
                                         0.002
                                                       0
#> 5 Strain 11
                    No Phage
                                B5
                                          0.002
                                                       0
#> 6 Strain 11
                    Phage Added B11
                                          0.002
                                                       0
```

Note that you can tune the sensitivity of first\_minima to different heights and widths of peaks and valleys using the window\_width, window\_width\_n, and window\_height arguments. You should check that first\_minima is working with your data by plotting it, although the default sensitivity works much of the time.

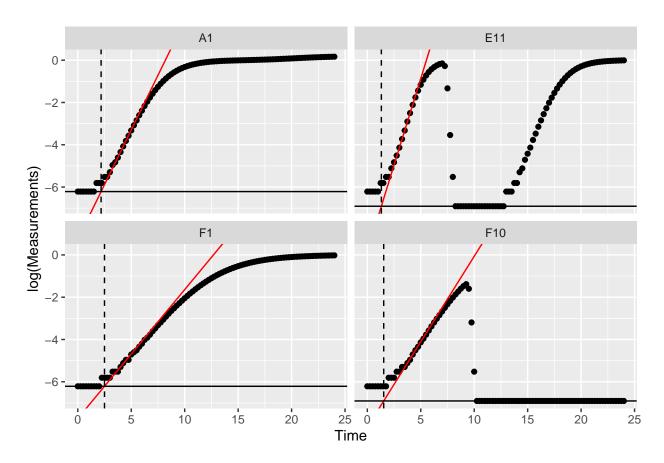
### Lag time

Bacteria often have a period of time before they reach their maximum growth rate. If you would like to quantify this lag time, you can use the lag\_time function. lag\_time needs the x and y values, as well as the (per-capita) derivative. It will find the maximum derivative, then project the tangent line with that slope back until it crosses the starting density.

Below, I calculate lag time. So that you can see a visualization of what this tangent-line calculation does, I also calculate the max\_percap\_time, max\_percap\_dens, and min\_dens, but you don't have to do that.

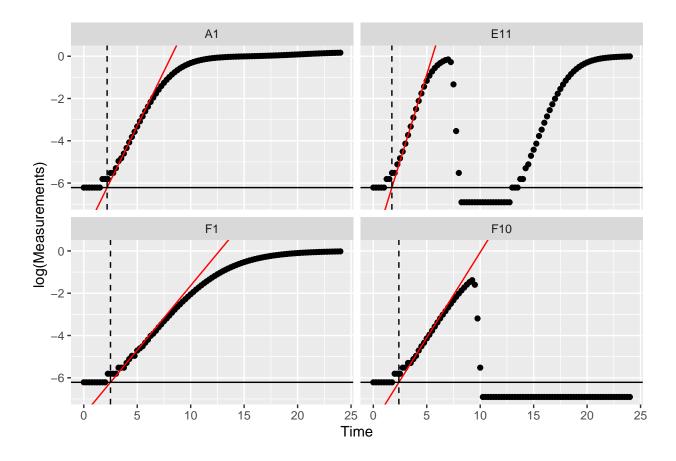
```
ex_dat_mrg_sum <-
 summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
           lag_time = lag_time(y = Measurements, x = Time,
                              deriv = deriv_percap5),
           max_percap = max_gc(deriv_percap5),
           max_percap_time = Time[which_max_gc(deriv_percap5)],
           max_percap_dens = Measurements[which_max_gc(deriv_percap5)],
           min_dens = min_gc(Measurements))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 8
#> # Groups: Bacteria_strain, Phage [6]
#>
  Bacteria strain Phage
                             Well lag_time max_percap max_percap_time max_pe~1 min_d~2
                                                          <dbl> <dbl>
    <chr>
                              <fct> <dbl> <dbl>
                    <chr>
```

```
#> 1 Strain 1
                     No Phage
                                  A1
                                            2.18
                                                        1.03
                                                                        4.25
                                                                                 0.017
                                                                                         0.002
#> 2 Strain 1
                     Phage Added A7
                                            1.51
                                                        1.03
                                                                        4.25
                                                                                 0.017
                                                                                         0.001
#> 3 Strain 10
                     No Phage
                                            1.78
                                                        1.59
                                                                        3.5
                                                                                 0.031
                                                                                         0.002
                                  B4
                     Phage Added B10
#> 4 Strain 10
                                                        1.59
                                                                                 0.031
                                            1.34
                                                                        3.5
                                                                                         0.001
                                                                        3.5
#> 5 Strain 11
                     No Phage
                                                        1.65
                                                                                 0.041
                                                                                         0.002
                                  B5
                                            1.67
#> 6 Strain 11
                     Phage Added B11
                                            1.24
                                                        1.65
                                                                        3.5
                                                                                 0.041
                                                                                         0.001
#> # ... with abbreviated variable names 1: max_percap_dens, 2: min_dens
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% sample_wells),
       aes(x = Time, y = log(Measurements))) +
  geom_point() +
  facet_wrap(~Well) +
  geom_abline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
              color = "red",
              aes(slope = max_percap,
                  intercept = log(max_percap_dens) - max_percap*max_percap_time)) +
  geom_vline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
             aes(xintercept = lag_time), lty = 2) +
  geom_hline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
             aes(yintercept = log(min_dens)))
```



Notice how in some of the wells the minimum density value isn't the *initial* density? We can fix that by overriding the default minimum density calculation with first\_minima via the y0 argument of lag\_time.

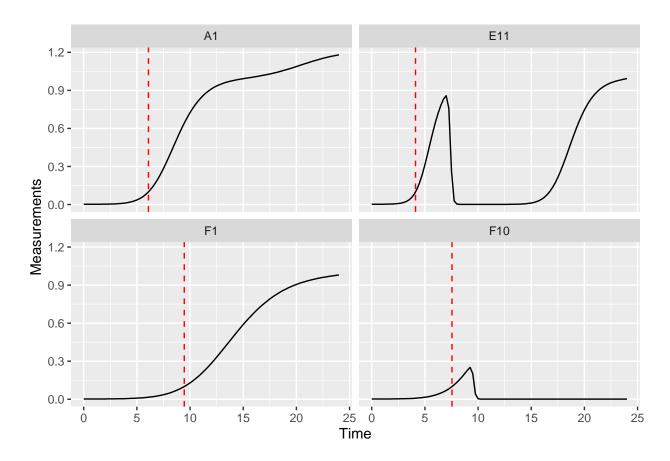
```
ex_dat_mrg_sum <-
 summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
           min dens = first minima(Measurements, return = "y"),
           lag_time = lag_time(y = Measurements, x = Time,
                              deriv = deriv_percap5, y0 = min_dens),
           max_percap = max_gc(deriv_percap5),
           max_percap_time = Time[which_max_gc(deriv_percap5)],
           max_percap_dens = Measurements[which_max_gc(deriv_percap5)])
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 8
#> # Groups: Bacteria_strain, Phage [6]
#> Bacteria_strain Phage
                              Well min_dens lag_time max_percap max_percap_time max_p~1
#> <chr>
              <chr>
                                      <dbl> <dbl> <dbl>
                              <fct>
                                                                         <dbl>
                                                                                 <db1>
                                                                         4.25
#> 1 Strain 1
                 No Phage A1
                                       0.002
                                               2.18
                                                          1.03
                                                                                 0.017
#> 2 Strain 1
                  Phage Added A7
                                       0.002
                                               2.18
                                                          1.03
                                                                          4.25
                                                                                 0.017
#> 3 Strain 10
                   No Phage B4
                                       0.002
                                                1.78
                                                          1.59
                                                                          3.5
                                                                                 0.031
#> 4 Strain 10
                                               1.78
                                                          1.59
                                                                         3.5
                                                                                 0.031
                   Phage Added B10
                                      0.002
#> 5 Strain 11
                   No Phage
                             B5
                                      0.002
                                               1.67
                                                          1.65
                                                                         3.5
                                                                                 0.041
                  Phage Added B11
                                     0.002 1.67
                                                          1.65
#> 6 Strain 11
                                                                         3.5
                                                                                 0.041
#> # ... with abbreviated variable name 1: max percap dens
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% sample_wells),
      aes(x = Time, y = log(Measurements))) +
 geom point() +
 facet_wrap(~Well) +
 geom_abline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
             color = "red",
             aes(slope = max_percap,
                intercept = log(max_percap_dens) - max_percap*max_percap_time)) +
 geom_vline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
            aes(xintercept = lag_time), lty = 2) +
 geom_hline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
            aes(yintercept = log(min_dens)))
```



### Time to reach threshold density

If you want to quantify how long it takes bacteria to reach some threshold density, you can use the first\_above function. In this example, we'll use a Measurements value of 0.1 as our threshold.

```
ex_dat_mrg_sum <-
  summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
            above_01 = first_above(y = Measurements, x = Time,
                                    threshold = 0.1, return = "x"))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 4
#> # Groups:
              Bacteria_strain, Phage [6]
     Bacteria_strain Phage
                                  Well above_01
#>
#>
     <chr>>
                      <chr>
                                  \langle fct \rangle
                                            <db1>
#> 1 Strain 1
                      No Phage
                                  A1
                                             6.09
#> 2 Strain 1
                                             6.09
                      Phage Added A7
#> 3 Strain 10
                      No Phage
                                  B4
                                             4.25
#> 4 Strain 10
                      Phage Added B10
                                             4.25
#> 5 Strain 11
                      No Phage
                                  B5
                                             4.04
#> 6 Strain 11
                      Phage Added B11
                                             4.04
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% sample_wells),
```

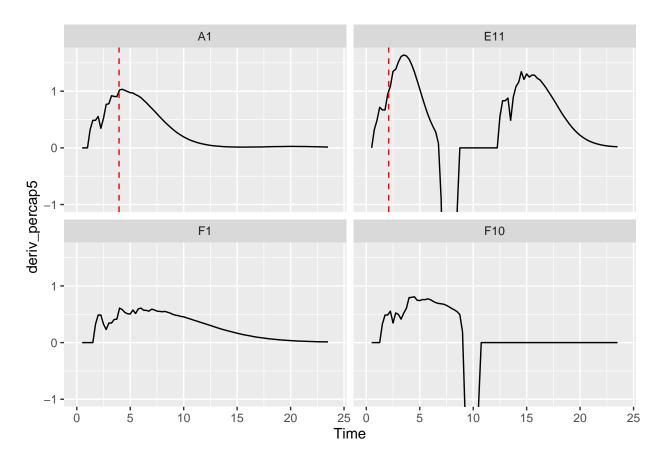


# Time to reach threshold growth rate

If you want to quantify how long it takes bacteria to reach some threshold per-capita growth rate, you can use the first\_above function. In this example, we'll use a per-capita derivative of 1 as our threshold.

```
ex_dat_mrg_sum <-
  summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
            percap_above_1 = first_above(y = deriv_percap5, x = Time,
                                   threshold = 1, return = "x"))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 4
#> # Groups: Bacteria_strain, Phage [6]
    Bacteria strain Phage
                                 Well
                                      percap_above_1
     <chr>
                                 <fct>
                                                 <dbl>
                     <chr>
#> 1 Strain 1
                     No Phage
                                 A1
                                                  3.95
```

```
#> 2 Strain 1
                     Phage Added A7
                                                  3.95
#> 3 Strain 10
                     No Phage
                                                  2.28
                                  B4
#> 4 Strain 10
                     Phage Added B10
                                                  2.28
                     No Phage
#> 5 Strain 11
                                  B5
                                                  2.11
#> 6 Strain 11
                     Phage Added B11
                                                  2.11
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% sample_wells),
       aes(x = Time, y = deriv_percap5)) +
  geom_line() +
  facet_wrap(~Well) +
  geom_vline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
             aes(xintercept = percap_above_1), lty = 2, color = "red") +
  coord_cartesian(ylim = c(-1, NA))
#> Warning: Removed 4 rows containing missing values (`geom_line()`).
#> Warning: Removed 2 rows containing missing values (`geom_vline()`).
```



# Maximum growth rate and minimum doubling time

If you want to calculate the bacterial maximum growth rate (i.e. the minimum doubling time), it will often be sufficient to use max\_gc on the per-capita derivatives we calculated in vignette("gc05\_process"). (max\_gc works just like R's built-in max, but with better default settings for growth curve analyses with summarize).

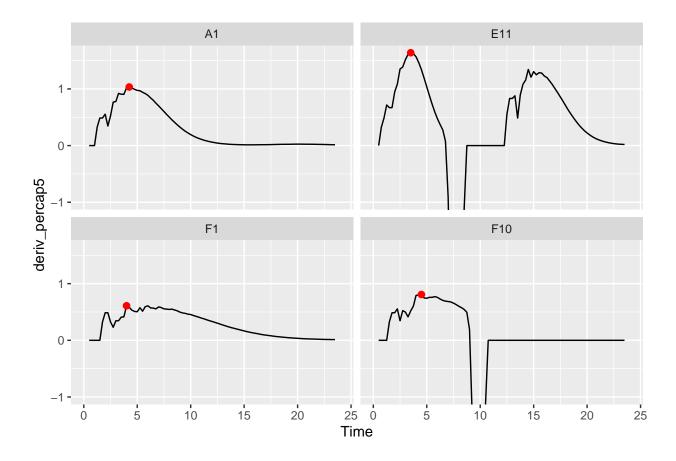
We can also save the time when this maximum occurs using the which\_max\_gc function. which\_max\_gc returns the *index* of the maximum value, so then we can get the Time value at that index and save it to a

column titled max\_percap\_time. (which\_max\_gc and extr\_val work just like R's built-in which.max and [, but with better default settings for growth curve analyses with summarize)

If you would like the equivalent minimum doubling time, you can simply calculate the maximum growth rate as above and then convert that into the equivalent minimum doubling time using the doubling\_time function.

It is important to note that gcplyr calculates the maximum realized growth rate during your growth curve. This is distinct from the intrinsic growth rate (the maximum possible growth rate), although the two will be quite similar if you started your growth curves at sufficiently low densities (see: Ghenu et al., 2024. Challenges and pitfalls of inferring microbial growth rates from lab cultures. Frontiers in Ecology and Evolution.)

```
ex dat mrg sum <-
  summarize(group by(ex dat mrg, Bacteria strain, Phage, Well),
           max percap = max gc(deriv percap5, na.rm = TRUE),
           max_percap_time = extr_val(Time, which_max_gc(deriv_percap5)),
            doub_time = doubling_time(y = max_percap))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex dat mrg sum)
#> # A tibble: 6 x 6
#> # Groups: Bacteria_strain, Phage [6]
#> Bacteria_strain Phage
                                 Well max_percap max_percap_time doub_time
   \langle chr \rangle
                    <chr>
#>
                                 <fct>
                                            <dbl>
                                                             <db1>
                                                                       \langle db l \rangle
#> 1 Strain 1
                    No Phage
                                                                       0.670
                                 A1
                                             1.03
                                                             4.25
#> 2 Strain 1
                   Phage Added A7
                                             1.03
                                                             4.25
                                                                       0.670
#> 3 Strain 10
                    No Phage
                                B4
                                             1.59
                                                             3.5
                                                                       0.436
#> 4 Strain 10
                     Phage Added B10
                                             1.59
                                                             3.5
                                                                       0.436
#> 5 Strain 11
                     No Phage
                                 B5
                                             1.65
                                                             3.5
                                                                       0.421
#> 6 Strain 11
                     Phage Added B11
                                             1.65
                                                             3.5
                                                                       0.421
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% sample_wells),
       aes(x = Time, y = deriv_percap5)) +
  geom line() +
  facet_wrap(~Well) +
  geom point(data = dplyr::filter(ex dat mrg sum, Well %in% sample wells),
             aes(x = max_percap_time, y = max_percap),
             size = 2, color = "red") +
  coord_cartesian(ylim = c(-1, NA))
#> Warning: Removed 4 rows containing missing values (`qeom_line()`).
```



### Mid-point time or inflection point

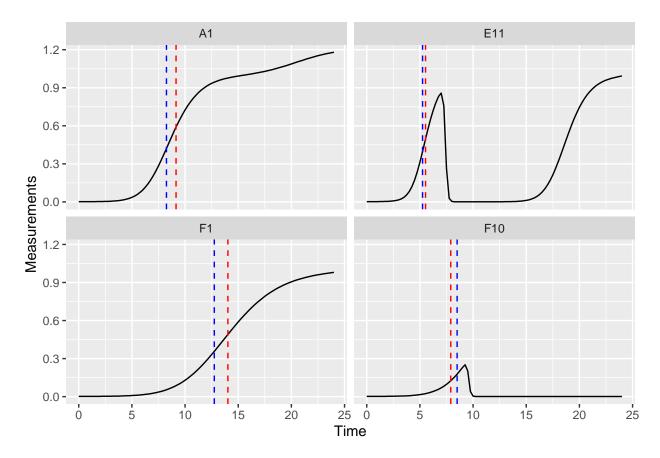
If you want to find the mid-point or inflection point of bacterial growth, there are two different approaches:

- 1. Mid-point: find the point when the density first reaches half the maximum density.
- 2. Inflection point: find the point when the derivative is at a maximum.

In growth curve analysis approaches using fitting of a symmetric function (e.g. when other R packages fit a logistic function to data), these two points will be equivalent. However, since gcplyr does model-free analyses, we do not assume symmetry, and so the points may be very similar or very different.

For the mid-point, we use the first\_above function, with the threshold equal to the maximum bacterial density divided by 2. For the inflection point, we find the time when the deriv was at a maximum using which\_max\_gc (which\_max\_gc and extr\_val work just like R's built-in which.max and [, but with better default settings for growth curve analyses with summarize).

```
#> # A tibble: 6 x 5
#> # Groups:
               Bacteria_strain, Phage [6]
     Bacteria strain Phage
                                  Well mid_point infl_point
#>
     <chr>
                      <chr>
                                  \langle fct \rangle
                                             <db1>
                                                         <db1>
#> 1 Strain 1
                      No Phage
                                  A1
                                              9.15
                                                         8.25
#> 2 Strain 1
                      Phage Added A7
                                              7.29
                                                         8.25
#> 3 Strain 10
                      No Phage
                                  B4
                                              6.06
                                                         5.5
                                                         5.5
#> 4 Strain 10
                      Phage Added B10
                                              5.67
#> 5 Strain 11
                      No Phage
                                  B5
                                              5.71
                                                         5
                                                         5
#> 6 Strain 11
                      Phage Added B11
                                             16.7
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% sample_wells),
       aes(x = Time, y = Measurements)) +
  geom_line() +
  facet_wrap(~Well) +
  geom_vline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
             aes(xintercept = mid_point), lty = 2, color = "red") +
  geom_vline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
             aes(xintercept = infl_point), lty = 2, color = "blue")
```



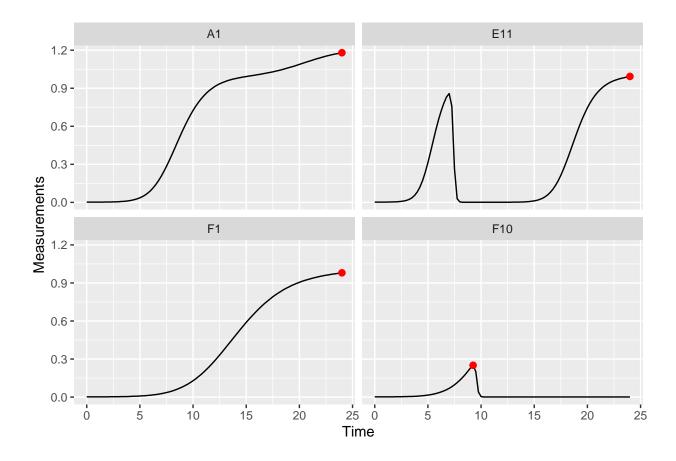
# Maximum density

The maximum bacterial density can be a measure of bacterial growth yield/efficiency. If your bacteria plateau in density, the maximum density can also be a measure of bacterial carrying capacity. If you want

to quantify the maximum bacterial density, we can use max\_gc to get the global maxima of Measurements (max\_gc, which\_max\_gc, and extr\_val work just like R's built-in max, which.max, and [, but with better default settings for growth curve analyses with summarize).

See Peak bacterial density for identifying *local* maxima of Measurements (e.g. if you wanted the first peak in Well E11 shown below).

```
ex_dat_mrg_sum <-
 summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
           max_dens = max_gc(Measurements, na.rm = TRUE),
           max_time = extr_val(Time, which_max_gc(Measurements)))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex dat mrg sum)
#> # A tibble: 6 x 5
#> # Groups: Bacteria_strain, Phage [6]
                            Well max_dens max_time
#> Bacteria_strain Phage
                                <fct>
#>
   < chr >
                  <chr>
                                        <dbl>
                                                 <dbl>
#> 1 Strain 1
                   No Phage A1
                                        1.18
                                                 24
#> 2 Strain 1
                   Phage Added A7
                                        0.499
                                                 8.75
#> 3 Strain 10
                    No Phage
                               B4
                                        1.21
                                                 23.8
#> 4 Strain 10
                    Phage Added B10
                                        0.962
                                                 8.5
#> 5 Strain 11
                    No Phage
                                                 19.5
                               B5
                                        1.21
#> 6 Strain 11
                    Phage Added B11
                                        1.03
                                                 24
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% sample_wells),
      aes(x = Time, y = Measurements)) +
 geom_line() +
 facet_wrap(~Well) +
 geom_point(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
            aes(x = max time, y = max dens),
            size = 2, color = "red")
```



#### Area under the curve

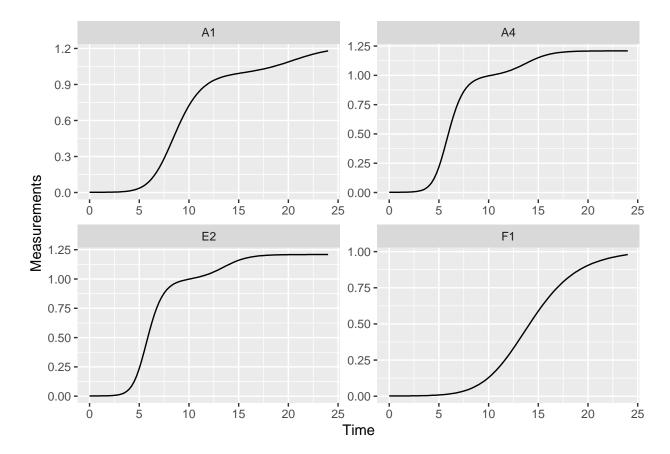
The area under the curve is a common metric of total bacterial growth, for instance in the presence of antagonists like antibiotics or phages. If you want to calculate the area under the curve, you can use the gcplyr function auc. Simply specify Time as the x and Measurements as the y data whose area-under-the-curve you want to calculate.

```
ex_dat_mrg_sum <-
  summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
             auc = auc(x = Time, y = Measurements))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 4
#> # Groups:
                Bacteria_strain, Phage [6]
#>
     Bacteria_strain Phage
                                    Well
                                            auc
#>
     <chr>
                       <chr>
                                    \langle fct \rangle \langle dbl \rangle
#> 1 Strain 1
                                          15.9
                      No Phage
                                    A1
#> 2 Strain 1
                      Phage Added A7
                                           1.07
#> 3 Strain 10
                      No Phage
                                    B4
                                          20.4
#> 4 Strain 10
                      Phage Added B10
                                           6.15
#> 5 Strain 11
                      No Phage
                                    B5
                                          20.9
#> 6 Strain 11
                      Phage Added B11
                                           7.77
```

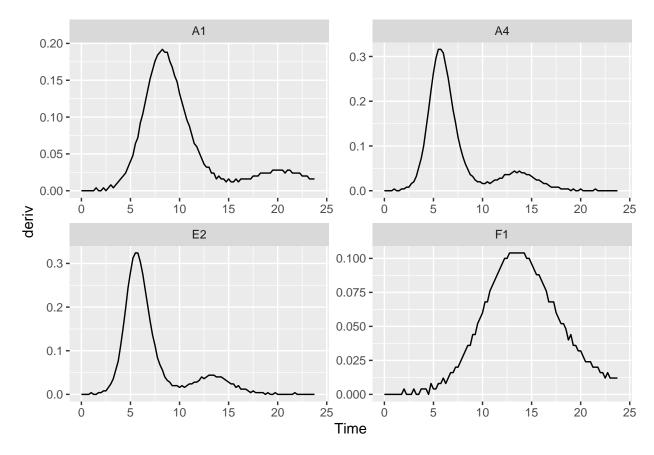
#### Diauxic shifts

Bacteria frequently exhibit a second, slower, burst of growth after their first period of rapid growth. This is common in growth curves and is called *diauxic growth*.

If we plot the data from some of our example data wells with no phage added, we'll see this pattern repeatedly:



We can identify the time when bacteria switch from their first period of rapid growth to their second period by finding a minima in the derivative values. Specifically, we want to identify the second minima (the first minima will occur at the beginning of the growth curve, when bacteria are just starting to grow). Let's look at some of the derivative values to see this.

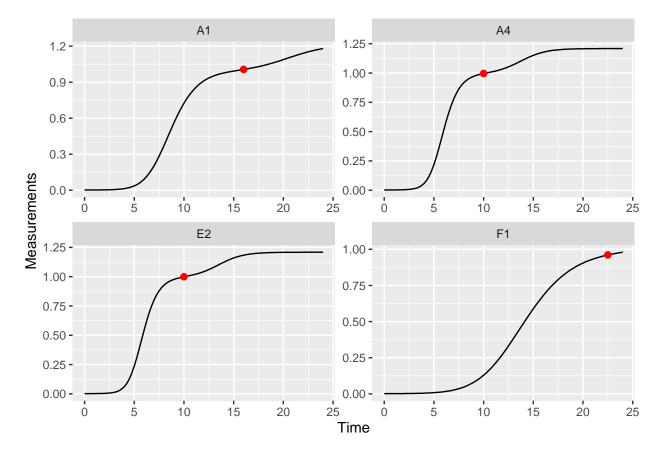


We can use the gcplyr function find\_local\_extrema to find that minima. Specify deriv as the y data and Time as the x data, and that we want find\_local\_extrema to return the x values associated with local minima. It will return a vector of those x values, and we're going to save just the second one.

At the same time, we're also going to save the density where the diauxic shift occurs. First, we'll use find\_local\_extrema again, but this time to save the *index* where the diauxic shift occurs to a column titled diauxie\_idx. Then, we can get the Measurements value at that index. (Note that it wouldn't work to just specify return = "y", because the y values in this case are the deriv values). (extr\_val works just like R's built-in [, but with better default settings for growth curve analyses with summarize).

```
ex_dat_mrg_sum <-
  summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
    diauxie_time = find_local_extrema(x = Time, y = deriv, return = "x",
                                    return_maxima = FALSE, return_minima = TRUE,
                                    window_width_n = 39)[2],
    diauxie_idx = find_local_extrema(x = Time, y = deriv, return = "index",
                                    return_maxima = FALSE, return_minima = TRUE,
                                    window_width_n = 39)[2],
    diauxie_dens = extr_val(Measurements, diauxie_idx))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 6
               Bacteria_strain, Phage [6]
#> # Groups:
                                  Well
     Bacteria_strain Phage
                                        diauxie_time diauxie_idx diauxie_dens
     <chr>
                                  <fct>
                                                <db1>
                                                            \langle int \rangle
                                                                          <db1>
#>
                      <chr>
#> 1 Strain 1
                     No Phage
                                  A1
                                                16
                                                                          1.01
```

```
#> 2 Strain 1
                     Phage Added A7
                                                                         0.379
#> 3 Strain 10
                     No Phage
                                  B4
                                                9.75
                                                               40
                                                                         0.999
#> 4 Strain 10
                     Phage Added B10
                                                9.25
                                                               38
                                                                         0.682
                     No Phage
#> 5 Strain 11
                                  B5
                                                9.5
                                                               39
                                                                         1.01
#> 6 Strain 11
                     Phage Added B11
                                                5.5
                                                               23
                                                                         0.346
# Plot data with a point at the moment of diauxic shift
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% nophage_wells),
       aes(x = Time, y = Measurements)) +
  geom_line() +
  facet_wrap(~Well, scales = "free") +
  geom_point(data = dplyr::filter(ex_dat_mrg_sum, Well %in% nophage_wells),
             aes(x = diauxie_time, y = diauxie_dens),
             size = 2, color = "red")
```



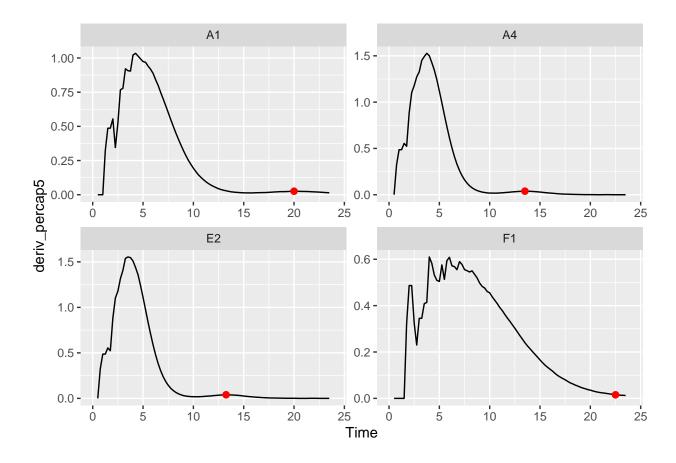
If needed, you can tune the sensitivity of find\_local\_extrema to different heights and widths of peaks and valleys using the window\_width, window\_width\_n, and window\_height arguments.

## Growth rate during diauxie

In the previous section we identified when bacteria shifted into their second period of rapid growth ('diauxic growth'). If you want to find out what the peak per-capita growth rate was during that second burst, we'll have to use max on the subset of data after the diauxic shift identified by find\_local\_extrema

Just as we did in the previous section, we'll use find\_local\_extrema to save the time when the diauxic shift occurs. Then, we'll find the maximum of the per-capita derivative after that shift occurs. Finally, we'll find the time when that post-diauxie maximum growth rate occurs. Note that we're using max\_gc and which\_max\_gc, which work just like R's built-in max and which.max, but with better default settings for growth curve analyses with summarize.

```
ex_dat_mrg_sum <-
  summarize(
    group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
   diauxie_time =
      find_local_extrema(x = Time, y = deriv, return = "x",
                         return_maxima = FALSE, return_minima = TRUE,
                         window width n = 39)[2],
   diauxie_percap = max_gc(deriv_percap5[Time >= diauxie_time]),
   diauxie percap time =
      extr_val(Time[Time >= diauxie_time],
               which_max_gc(deriv_percap5[Time >= diauxie_time]))
 )
#> `summarise()` has grouped output by 'Bacteria strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 6
#> # Groups: Bacteria_strain, Phage [6]
   Bacteria_strain Phage
                                 Well diauxie_time diauxie_percap_diauxie_percap_time
    <chr>
#>
                    <chr>
                                 <fct>
                                              <dbl>
                                                             <dbl>
                                                                                  <db1>
#> 1 Strain 1
                    No Phage
                                              16
                                                            0.0257
                                                                                  20
                                 A1
#> 2 Strain 1
                    Phage Added A7
                                              9
                                                            0.832
                                                                                  19.8
#> 3 Strain 10
                     No Phage
                                 B4
                                               9.75
                                                            0.0398
                                                                                  13.2
#> 4 Strain 10
                    Phage Added B10
                                               9.25
                                                                                  17.8
                                                            1.24
#> 5 Strain 11
                     No Phage
                                 B5
                                               9.5
                                                            0.0438
                                                                                  12.2
#> 6 Strain 11
                    Phage Added B11
                                                                                  12.8
                                               5.5
                                                            1.43
# Plot data with a point at the moment of peak diauxic growth rate
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% nophage_wells),
       aes(x = Time, y = deriv_percap5)) +
  geom line() +
  facet wrap(~Well, scales = "free") +
  geom_point(data = dplyr::filter(ex_dat_mrg_sum, Well %in% nophage_wells),
             aes(x = diauxie_percap_time, y = diauxie_percap),
             size = 2, color = "red")
#> Warning: Removed 4 rows containing missing values (`geom_line()`).
```



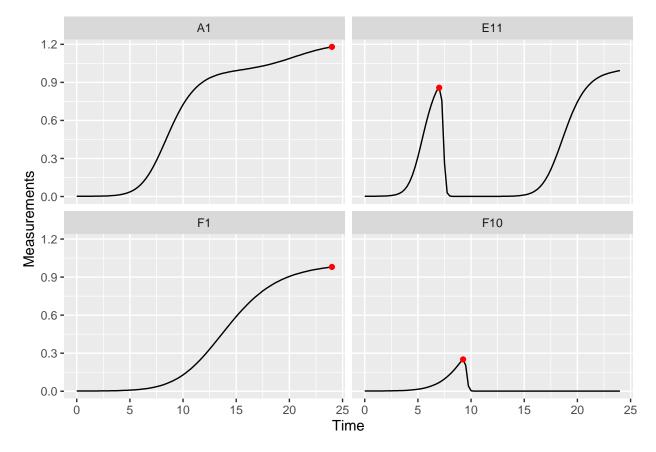
## Peak bacterial density

We previously found the global maximum in bacterial density using the simple max\_gc and which\_max\_gc functions. The first *local* maxima can also be of interest. This is especially true when bacteria are grown with phages, where their first peak density can act as a proxy measure for their susceptibility to the phage. If you're interested in finding the first local maxima in bacterial density, you can use the gcplyr function first\_maxima.

first\_maxima simply requires the y data you want to identify the peak in. Specify Measurements as the y data and Time as the x data, and that we want first\_peak to return the x and y values associated with the peak. We'll save those in columns first\_maxima\_x and first\_maxima\_y, respectively.

```
ex_dat_mrg_sum <-
  summarize(group_by(ex_dat_mrg, Bacteria_strain, Phage, Well),
            first_maxima_x = first_maxima(x = Time, y = Measurements,
                                            return = "x"),
            first_maxima_y = first_maxima(x = Time, y = Measurements,
                                            return = "y"))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 5
#> # Groups:
               Bacteria_strain, Phage [6]
     Bacteria strain Phage
#>
                                  Well first_maxima_x first_maxima_y
     <chr>>
                      <chr>
                                  \langle fct \rangle
                                                   <dbl>
```

```
#> 1 Strain 1
                      No Phage
                                                  24
                                                                  1.18
#> 2 Strain 1
                      Phage Added A7
                                                   8.75
                                                                  0.499
#> 3 Strain 10
                      No Phage
                                                  19.8
                                                                  1.21
                                  B4
                      Phage Added B10
#> 4 Strain 10
                                                   8.5
                                                                  0.962
#> 5 Strain 11
                      No Phage
                                                  19.5
                                                                  1.21
                                  B5
#> 6 Strain 11
                      Phage Added B11
                                                   5.25
                                                                  0.439
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% sample_wells),
       aes(x = Time, y = Measurements)) +
  geom_line() +
  facet_wrap(~Well) +
  geom_point(data = dplyr::filter(ex_dat_mrg_sum, Well %in% sample_wells),
             aes(x = first_maxima_x, y = first_maxima_y),
             color = "red", size = 1.5)
```

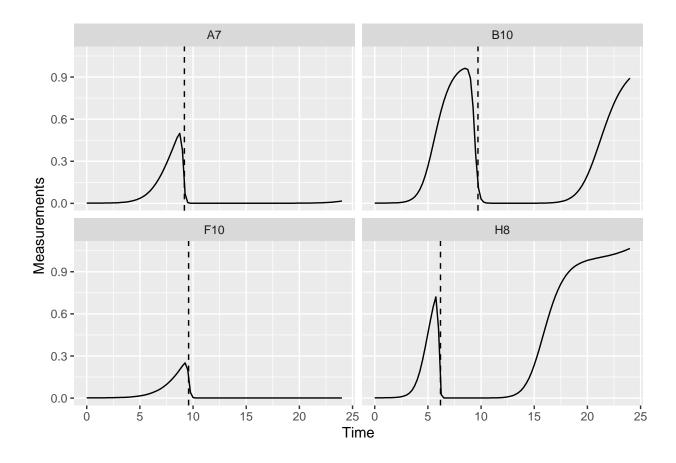


Note that you can tune the sensitivity of first\_maxima to different heights and widths of peaks and valleys using the window\_width, window\_width\_n, and window\_height arguments, although the defaults work much of the time.

### **Extinction time**

The time when bacterial density falls below some threshold can also be of interest. This is especially true when bacteria are grown with phages, where this 'extinction time' can act as a proxy measure for their susceptibility to the phage. If you're interested in finding the extinction time, you can use the gcplyr function first\_below. In this example, we'll use a Measurements value of 0.15 as our threshold.

```
ex_dat_mrg_sum <-
 summarize(
   group by(ex dat mrg, Bacteria strain, Phage, Well),
    extin_time = first_below(x = Time, y = Measurements, threshold = 0.15,
                           return = "x", return endpoints = FALSE))
#> `summarise()` has grouped output by 'Bacteria_strain', 'Phage'. You can override using
#> the `.groups` argument.
head(ex_dat_mrg_sum)
#> # A tibble: 6 x 4
#> # Groups: Bacteria_strain, Phage [6]
#> Bacteria_strain Phage Well extin_time
#> <chr>
               <chr>
                               <fct>
                                         <dbl>
#> 1 Strain 1
                   No Phage A1
                                          NA
                                          9.18
#> 2 Strain 1
                   Phage Added A7
#> 3 Strain 10
                  No Phage B4
                                          NA
#> 4 Strain 10
                   Phage Added B10
                                         9.71
#> 5 Strain 11
                   No Phage B5
                                         NA
#> 6 Strain 11
                    Phage Added B11
                                          5.64
phage_wells <- c("A7", "B10", "F10", "H8")</pre>
ggplot(data = dplyr::filter(ex_dat_mrg, Well %in% phage_wells),
      aes(x = Time, y = Measurements)) +
 geom_line() +
 facet_wrap(~Well) +
  geom_vline(data = dplyr::filter(ex_dat_mrg_sum, Well %in% phage_wells),
            aes(xintercept = extin_time), lty = 2)
```



#### What's next?

Now that you've analyzed your data, you can read about approaches to deal with noise in your growth curve data, or you can read some concluding notes on best practices for running statistics, merging growth curve analyses with other data, and additional resources for analyzing growth curves.

- Introduction: vignette("gc01\_gcplyr")
- 2. Importing and reshaping data: vignette("gc02\_import\_reshape")
- 3. Incorporating experimental designs: vignette("gc03 incorporate designs")
- 4. Pre-processing and plotting your data: vignette("gc04\_preprocess\_plot")
- 5. Processing your data: vignette("gc05\_process")
- 6. Analyzing your data: vignette("gc06\_analyze")
- 7. Dealing with noise: vignette("gc07\_noise")
- 8. Statistics, merging other data, and other resources: vignette("gc08\_conclusion")
- 9. Working with multiple plates: vignette("gc09\_multiple\_plates")