# Various GLGM examples

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This vignette is a bunch of examples, its primary purpose is to test the glgm function.

## The data

```
library("geostatsp")
## Loading required package: Matrix
## Loading required package: terra
## terra 1.7.55
##
## Attaching package: 'terra'
## The following object is masked from 'package:knitr':
##
##
       spin
data('swissRain')
swissRain = unwrap(swissRain)
swissAltitude = unwrap(swissAltitude)
swissBorder = unwrap(swissBorder)
swissRain$lograin = log(swissRain$rain)
swissAltitudeCrop = mask(swissAltitude,swissBorder)
   number of cells... smaller is faster but less interesting
if(!exists('fact')) fact = 1
fact
## [1] 1
(Ncell = round(25*fact))
```

#### ## [1] 25 model with standard formula swissFit = glgm( formula = lograin~ CHE\_alt, data = swissRain, grid = Ncell, buffer = 10\*1000, covariates=swissAltitudeCrop, family="gaussian", prior = list( sd=c(1,0.5),sd0bs = 1,range=c(500000, 0.5)), control.inla = list(strategy='gaussian') ) parameters if(length(swissFit\$parameters)) { knitr::kable(swissFit\$parameters\$summary[,c(1,3,5)], digits=3) } else { print("INLA was not run, install the INLA package to see results") } $\overline{0.02}$ 5quant 0.975quant mean 2.2681.583 2.912 (Intercept) CHE alt 0.0000.0000.000range/1000 182.243 517.500 59.490 sdNugget 0.3090.1810.4920.7043.595 1.562 $\operatorname{sd}$ Exceedance probabilities if(length(swissFit\$parameters)) { swissExc = excProb( x=swissFit, random=TRUE, threshold=0) } if(length(swissFit\$parameters)) {

plot(swissExc, breaks = c(0, 0.2, 0.8, 0.95, 1.00001),

col=c('green','yellow','orange','red'))

plot(swissBorder, add=TRUE)

```
swissExcP = excProb(
    swissFit$inla$marginals.predict, 3,
      template=swissFit$raster)
  plot(swissExcP, breaks = c(0, 0.2, 0.8, 0.95, 1.00001),
    col=c('green','yellow','orange','red'))
  plot(swissBorder, add=TRUE)
  matplot(
    swissFit$parameters$sd$posterior[,'x'],
    swissFit$parameters$sd$posterior[,c('y','prior')],
    lty=1, col=c('black','red'), type='l',
    xlab='sd', ylab='dens', xlim = c(0,5))
  matplot(
    swissFit$parameters$range$posterior[,'x'],
    swissFit$parameters$range$posterior[,c('y','prior')],
    lty=1, col=c('black','red'), type='l',
    xlab='range', ylab='dens')
  }
   non-parametric elevation effect
altSeq = exp(seq(
    log(100), log(5000),
    by = log(2)/5)
altMat = cbind(altSeq[-length(altSeq)], altSeq[-1], seq(1,length(altSeq)-1))
swissAltCut = classify(
  swissAltitudeCrop,
  altMat
)
names(swissAltCut) = 'bqrnt'
  swissFitNp = glgm(
    formula = lograin ~ f(bqrnt, model = 'rw2', scale.model=TRUE,
      values = 1:length(altSeq),
      prior = 'pc.prec', param = c(0.1, 0.01)),
    data=swissRain,
    grid = Ncell,
    covariates=swissAltCut,
    family="gaussian", buffer=20000,
    prior=list(
      sd=c(u = 0.5, alpha = 0.1),
```

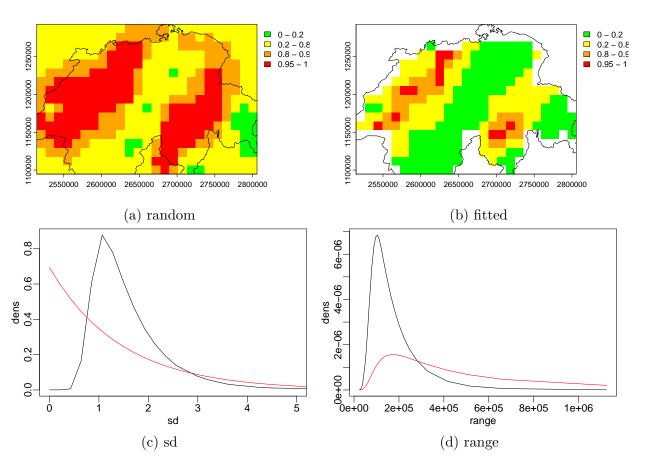


Figure 1: Swiss rain as in help file

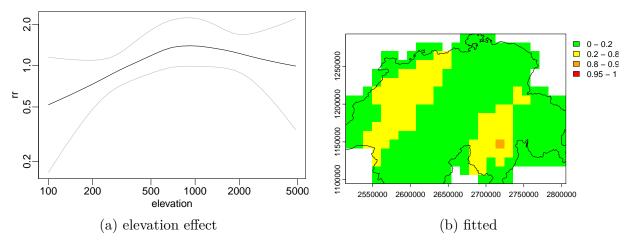


Figure 2: Swiss rain elevation rw2

```
range=c(50000,500000),
      sd0bs = c(u=1, alpha=0.4)),
    control.inla=list(strategy='gaussian')
  )
if(length(swissFitNp$parameters)) {
  knitr::kable(swissFitNp$parameters$summary, digits=3)
  matplot(
    altSeq,
    exp(swissFitNp$inla$summary.random$bqrnt[,
      c('0.025quant', '0.975quant', '0.5quant')]),
    log='xy',
    xlab ='elevation', ylab='rr',
  type='l',
    lty = 1,
    col=c('grey','grey','black')
  swissExcP = excProb(swissFitNp$inla$marginals.predict,
    3, template=swissFitNp$raster)
  plot(swissExcP, breaks = c(0, 0.2, 0.8, 0.95, 1.00001),
    col=c('green','yellow','orange','red'))
  plot(swissBorder, add=TRUE)
}
   intercept only, named response variable. legacy priors
swissFit = glgm("lograin", swissRain, Ncell,
    covariates=swissAltitude, family="gaussian", buffer=20000,
    priorCI=list(sd=c(0.2, 2), range=c(50000,500000), sd0bs = 2),
```

```
control.inla=list(strategy='gaussian')
)
if(length(swissFit$parameters))
    knitr::kable(swissFit$parameters$summary[,c(1, 3:5, 8)], digits=4)
```

	mean	0.025quant	0.5quant	0.975quant	meanExp
(Intercept)	2.4737	1.6863	2.5056	3.0943	12.5294
CHE alt	-0.0001	-0.0004	-0.0001	0.0002	1.0128
range/1000	107.7380	41.6976	91.5685	274.0698	NA
$\overline{\mathrm{sdNugget}}$	0.3229	0.1947	0.3043	0.5177	NA
sd	0.9541	0.5784	0.8936	1.5705	NA

intercept only, add a covariate just to confuse glgm.

}

```
swissFit = glgm(
    formula=lograin~1,
    data=swissRain,
    grid=Ncell,
    covariates=swissAltitude,
    family="gaussian", buffer=20000,
    priorCI=list(sd=c(0.2, 2), range=c(50000,500000)),
    control.inla=list(strategy= 'gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma", param=c(.1, .1))))
  )
  if(length(swissFit$parameters)) {
  knitr::kable(swissFit$parameters$summary[,c(1, 3:5, 8)], digits=3)
  swissExc = excProb(
    swissFit$inla$marginals.random$space, 0,
    template=swissFit$raster)
  plot(swissExc, breaks = c(0, 0.2, 0.8, 0.95, 1.00001),
    col=c('green','yellow','orange','red'))
  plot(swissBorder, add=TRUE)
    matplot(
    swissFit$parameters$range$posterior[,'x'],
    swissFit$parameters$range$posterior[,c('y','prior')],
    lty=1, col=c('black','red'), type='l',
    xlab='range', ylab='dens')
   covariates are in data
newdat = swissRain
newdat$elev = extract(swissAltitude, swissRain, ID=FALSE)
```

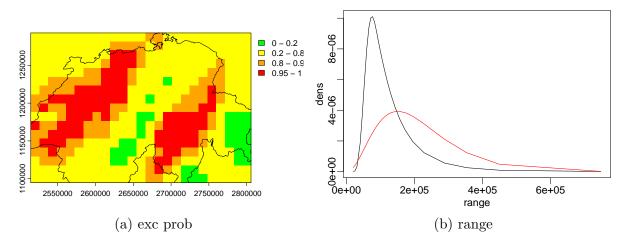


Figure 3: Swiss intercept only

```
swissLandType = unwrap(swissLandType)
  swissFit = glgm(lograin~ elev + land,
    newdat, Ncell,
    covariates=list(land=swissLandType),
    family="gaussian", buffer=40000,
    priorCI=list(sd=c(0.2, 2), range=c(50000,500000)),
    control.inla = list(strategy='gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma",
          param=c(.1, .1))))
  )
  if(length(swissFit$parameters)) {
  knitr::kable(swissFit$parameters$summary, digits=3)
  plot(swissFit$raster[['predict.mean']])
   plot(swissBorder, add=TRUE)
    matplot(
    swissFit$parameters$range$posterior[,'x'],
    swissFit$parameters$range$posterior[,c('y','prior')],
    lty=1, col=c('black','red'), type='l',
    xlab='range', ylab='dens')
}
   formula, named list elements
swissFit = glgm(lograin~ elev,
    swissRain, Ncell,
    covariates=list(elev=swissAltitude),
    family="gaussian", buffer=20000,
    priorCI=list(sd=c(0.2, 2), range=c(50000,500000)),
```

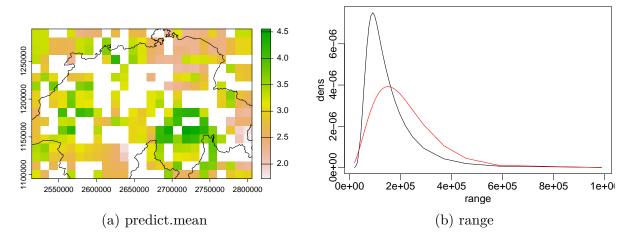


Figure 4: covaraites in data

```
control.mode=list(theta=c(1.9,0.15,2.6),restart=TRUE),
    control.inla = list(strategy='gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma",
          param=c(.1, .1))))
 )
if(length(swissFit$parameters))
    swissFitparameterssummary[,c(1,3,5)]
##
                                0.025quant
                                             0.975quant
                        mean
                2.455538e+00 1.6627584590 3.085039e+00
## (Intercept)
## elev
               -9.695412e-05 -0.0004013502 2.068248e-04
## range/1000
                1.296197e+02 42.5925140996 3.700202e+02
## sdNugget
                3.438354e-01 0.2148894824 5.235268e-01
## sd
                1.029996e+00 0.5698945076 1.908126e+00
  categorical covariates
swissFit = glgm(
    formula = lograin ~ elev + factor(land),
    data = swissRain, grid = Ncell,
    covariates=list(elev=swissAltitude,land=swissLandType),
    family="gaussian", buffer=20000,
    prior=list(sd=c(0.2, 0.5), range=c(100000,0.5)),
    control.inla=list(strategy='gaussian'),
    control.family=list(hyper=list(
      prec=list(prior="loggamma",
          param=c(.1, .1))))
if(length(swissFit$parameters)) {
 knitr::kable(swissFit$parameters$summary[,c(1,3,5)], digits=3)
```

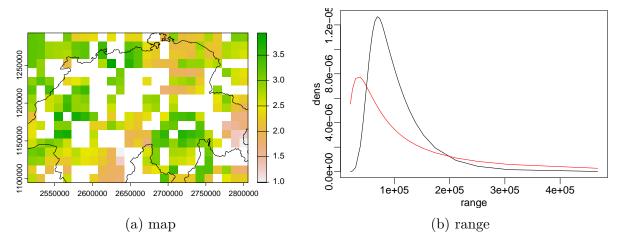


Figure 5: categorical covariates

```
plot(swissFit$raster[['predict.mean']])
   plot(swissBorder, add=TRUE)
    matplot(
    swissFit$parameters$range$posterior[,'x'],
    swissFit$parameters$range$posterior[,c('y','prior')],
    lty=1, col=c('black','red'), type='l',
    xlab='range', ylab='dens')
}
   put some missing values in covaritates also dont put factor() in formula
temp = values(swissAltitude)
temp[seq(10000, 12000)] = NA
values(swissAltitude) = temp
swissFitMissing = glgm(rain ~ elev + land,swissRain, Ncell,
    covariates=list(elev=swissAltitude,land=swissLandType),
    family="gaussian", buffer=20000,
    prior=list(sd=c(0.2, 0.5), range=c(100000,0.5)),
    control.inla = list(strategy='gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma",
          param=c(.1, .1))))
)
if(length(swissFitMissing$parameters))
      knitr::kable(swissFitMissing$parameters$summary[,1:5], digits=3)
```

	mean	sd	0.025quant	0.5quant	0.975quant	
(Intercept)	27.182	3.251	20.782	27.186	33.560	
elev	-0.005	0.003	-0.011	-0.005	0.002	
landMixed forests	-4.249	3.257	-10.638	-4.253	2.166	
landGrasslands	-3.329	4.903	-12.950	-3.333	6.319	
landCroplands	-9.535	4.215	-17.803	-9.540	-1.236	
landUrban and built-up	-8.064	5.482	-18.821	-8.070	2.727	
landEvergreen needleleaf forest	-11.996	6.274	-24.303	-12.004	0.357	
landWater bodies	-15.819	8.052	-31.602	-15.832	0.043	
landDeciduous needleleaf forest	-8.982	8.016	-24.706	-8.992	6.796	
landDeciduous broadleaf forest	8.307	8.012	-7.440	8.309	24.046	
landOpen shrublands	-11.585	11.040	-33.226	-11.601	10.150	
landPermanent Wetlands	-21.610	10.884	-42.914	-21.637	-0.149	
range/1000	205.922	266.637	23.521	127.127	883.397	
$\operatorname{sdNugget}$	11.646	-2.956	9.608	11.217	13.097	
sd	0.009	0.000	0.004	0.008	0.020	
• 1 1 6 1						

covariates in data, factors

```
newdat = swissRain
newdat$landOrig = extract(swissLandType, swissRain, ID=FALSE)
newdat$landRel = relevel(newdat$landOrig, 'Mixed forests')
swissFit = glgm(
    formula = lograin~ elev + landOrig,
    data=newdat,
    covariates=list(elev = swissAltitude),
    grid=squareRaster(swissRain,Ncell),
    family="gaussian", buffer=0,
    prior=list(sd=c(0.2, 0.5), range=c(100000,0.5)),
    control.inla = list(strategy='gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma",
          param=c(.1, .1))))
)
swissFitR = glgm(
    formula = lograin~ elev + landRel,
    data=newdat,
    grid=squareRaster(swissRain,Ncell),
    covariates=list(elev = swissAltitude, landRel = swissLandType),
    family="gaussian", buffer=0,
    prior=list(sd=c(0.2, 0.5), range=c(100000,0.5)),
    control.inla = list(strategy='gaussian'),
    control.family=list(hyper=list(prec=list(prior="loggamma",
          param=c(.1, .1))))
 )
```

### levels(newdat\$landOrig)

```
##
    [1] "Water bodies"
                                              "Evergreen needleleaf forest"
##
    [3] "Evergreen broadleaf forest"
                                              "Deciduous needleleaf forest"
##
    [5] "Deciduous broadleaf forest"
                                              "Mixed forests"
    [7] "Closed shrublands"
##
                                              "Open shrublands"
    [9] "Woody savannas"
                                              "Savannas"
##
## [11] "Grasslands"
                                              "Permanent Wetlands"
## [13] "Croplands"
                                              "Urban and built-up"
## [15] "Cropland/natural vegetation mosaic"
                                              "Snow and ice"
## [17] "Barren or sparsely vegetated"
levels(newdat$landRel)
    [1] "Mixed forests"
                                              "Water bodies"
##
##
    [3] "Evergreen needleleaf forest"
                                              "Evergreen broadleaf forest"
##
    [5] "Deciduous needleleaf forest"
                                              "Deciduous broadleaf forest"
                                              "Open shrublands"
    [7] "Closed shrublands"
                                              "Savannas"
    [9] "Woody savannas"
## [11] "Grasslands"
                                              "Permanent Wetlands"
## [13] "Croplands"
                                              "Urban and built-up"
## [15] "Cropland/natural vegetation mosaic" "Snow and ice"
## [17] "Barren or sparsely vegetated"
if(length(swissFit$parameters)) {
    levels(swissFit$inla$.args$data$landOrig)
    levels(swissFitR$inla$.args$data$landRel)
  }
    [1] "Cropland/natural vegetation mosaic" "Mixed forests"
##
##
    [3] "Grasslands"
                                              "Croplands"
##
    [5] "Urban and built-up"
                                              "Evergreen needleleaf forest"
    [7] "Water bodies"
                                              "Deciduous needleleaf forest"
##
    [9] "Deciduous broadleaf forest"
                                              "Open shrublands"
## [11] "Permanent Wetlands"
if(length(swissFit$parameters)) {
    knitr::kable(swissFit$parameters$summary[,c(1,3,5)], digits=3)
    knitr::kable(swissFitR$parameters$summary[,c(1,3,5)], digits=3)
}
```

	mean	0.025quant	0.975quant
(Intercept)	3.155	2.642	3.648
elev	-0.001	-0.001	0.000
landRelMixed forests	-0.186	-0.466	0.092
landRelGrasslands	-0.059	-0.479	0.359
landRelCroplands	-0.387	-0.735	-0.048
landRelUrban and built-up	-0.685	-1.265	-0.101
landRelEvergreen needleleaf forest	-0.597	-1.192	-0.026
landRelWater bodies	-0.997	-1.746	-0.247
landRelDeciduous needleleaf forest	-0.594	-1.314	0.122
landRelDeciduous broadleaf forest	0.329	-0.354	1.039
landRelOpen shrublands	-0.133	-1.235	0.974
landRelPermanent Wetlands	-2.635	-3.651	-1.624
range/1000	112.471	42.916	269.761
$\operatorname{sdNugget}$	0.353	0.230	0.493
sd	0.809	0.465	1.391

covariates are in data, interactions

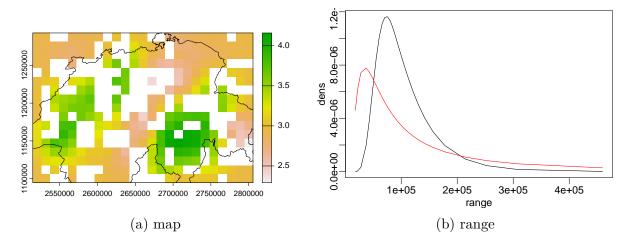


Figure 6: interactions

	mean	0.025quant	0.975quant
(Intercept)	2.937	2.446	3.417
elev:landCropland/natural vegetation mosaic	0.000	-0.001	0.000
elev:landMixed forests	-0.001	-0.001	0.000
elev:landGrasslands	0.000	-0.001	0.000
elev:landCroplands	-0.001	-0.002	0.000
elev:landUrban and built-up	-0.001	-0.002	0.000
elev:landEvergreen needleleaf forest	-0.001	-0.001	-0.001
elev:landWater bodies	-0.002	-0.004	0.000
elev:landDeciduous needleleaf forest	-0.001	-0.001	0.000
elev:landDeciduous broadleaf forest	0.000	-0.001	0.001
elev:landOpen shrublands	-0.001	-0.001	0.000
elev:landPermanent Wetlands	-0.010	-0.013	-0.006
range/1000	107.855	42.659	252.902
sdNugget	0.347	0.230	0.477
sd	0.772	0.450	1.314

```
if(length(swissFit$parameters)) {
   plot(swissFit$raster[['predict.mean']])
     plot(swissBorder, add=TRUE)

   matplot(
     swissFit$parameters$range$posterior[,'x'],
     swissFit$parameters$range$posterior[,c('y','prior')],
     lty=1, col=c('black','red'), type='l',
     xlab='range', ylab='dens')
}

categorical tests
data('loaloa')
```

```
loaloa = unwrap(loaloa)
 ltLoa = unwrap(ltLoa)
 elevationLoa = unwrap(elevationLoa)
 eviLoa = unwrap(eviLoa)
 rcl = rbind(
    # wedlands and mixed forests to forest
    c(5,2),c(11,2),
# savannas to woody savannas
    c(9,8),
    # croplands and urban changed to crop/natural mosaid
    c(12,14),c(13,14))
ltLoaR = classify(ltLoa, rcl)
levels(ltLoaR) = levels(ltLoa)
elevationLoa = elevationLoa - 750
elevLow = min(elevationLoa, 0)
elevHigh = max(elevationLoa, 0)
eviLoa2 = (eviLoa - 1e7)/1e6
covList = list(elLow = elevLow, elHigh = elevHigh,
    land = ltLoaR, evi=eviLoa2)
loaFit = glgm(
    y ~ 1 + land + evi + elHigh + elLow +
      f(villageID, prior = 'pc.prec', param = c(log(2), 0.5),
      model="iid"),
    loaloa,
   Ncell,
    covariates=covList,
    family="binomial", Ntrials = loaloa$N,
    shape=2, buffer=25000,
    prior = list(
      sd=log(2),
     range = 100*1000),
    control.inla = list(strategy='gaussian')
    )
if(length(loaFit$parameters)) {
 knitr::kable(loaFit$par$summary[,c(1,3,5)], digits=3)
}
```

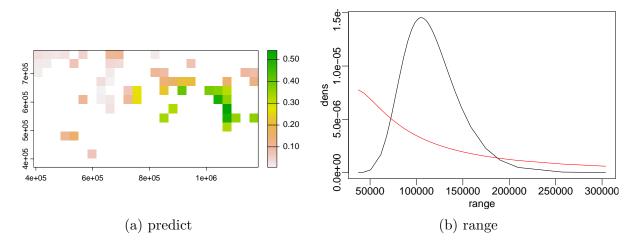


Figure 7: categorical

	mean	0.025quant	0.975quant
(Intercept)	-5.272	-7.157	-3.391
landWoody Savannas	-0.157	-0.659	0.338
landCropland/Natural Vegetation Mosaics	0.136	-0.290	0.562
evi	0.115	0.068	0.163
elHigh	-0.003	-0.005	-0.002
elLow	0.003	0.001	0.004
range/1000	116.997	67.822	189.945
sd	0.693	0.438	1.033
sd villageID	0.651	0.527	0.746

```
if(length(loaFit$parameters)) {
    plot(loaFit$raster[['predict.exp']])

matplot(
        loaFit$parameters$range$posterior[,'x'],
        loaFit$parameters$range$posterior[,c('y','prior')],
        lty=1, col=c('black','red'), type='l',
        xlab='range', ylab='dens')
}

prior for observation standard deviation

swissFit = glgm( formula="lograin",data=swissRain, grid=Ncell,
        covariates=swissAltitude, family="gaussian", buffer=20000,
        prior=list(sd=0.5, range=200000, sd0bs=1),
        control.inla = list(strategy='gaussian')
)
```

## no data checks

```
a model with little data, posterior should be same as prior
data2 = vect(cbind(c(1,0), c(0,1)),
    atts=data.frame(y=c(0,0), offset=c(-50,-50), x=c(-1,1)),
    crs = '+proj=merc')
resNoData = res = glgm(
  data=data2, grid=Ncell,
    formula=y~1 + x+offset(offset),
    prior = list(sd=0.5, range=0.1),
    family="poisson",
    buffer=0.5,
    control.fixed=list(
      mean.intercept=0, prec.intercept=1,
      mean=0, prec=4),
    control.mode = list(theta = c(0.651, 1.61), restart=TRUE),
    control.inla = list(strategy='gaussian')
  )
if(length(res$parameters)) {
# beta
  plot(res$inla$marginals.fixed[['x']], col='blue', type='l',
    xlab='beta',lwd=3)
  xseq = res$inla$marginals.fixed[['x']][,'x']
  lines(xseq, dnorm(xseq, 0, 1/2),col='red',lty=2,lwd=3)
  legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))
# sd
    matplot(
      res$parameters$sd$posterior[,'x'],
      res$parameters$sd$posterior[,c('y','prior')],
      xlim = c(0, 4),
      type='l', col=c('red','blue'),xlab='sd',lwd=3, ylab='dens')
    legend("topright", col=c("blue", "red"), lty=1, legend=c("prior", "post'r"))
# range
    matplot(
      res$parameters$range$posterior[,'x'],
      res$parameters$range$posterior[,c('y','prior')],
      xlim = c(0, 1.5),
      type='1', col=c('red','blue'),xlab='range',lwd=3, ylab='dens')
```

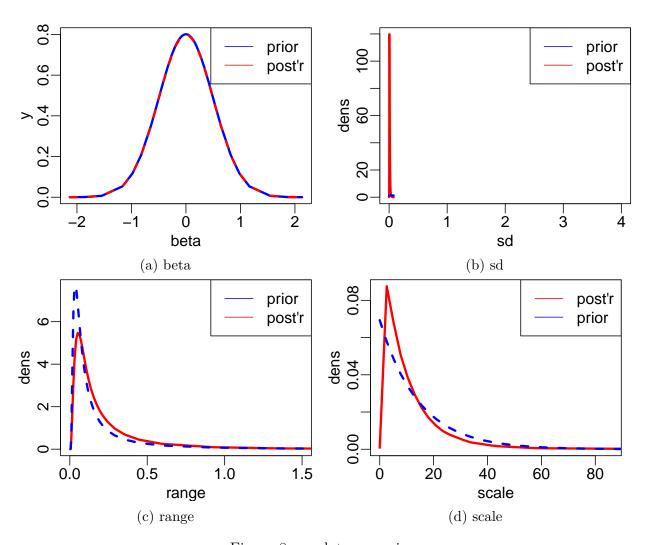


Figure 8: no data, pc priors

```
legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))

    matplot(
    res$parameters$scale$posterior[,'x'],
    res$parameters$scale$posterior[,c('y','prior')],
    xlim = c(0, 2/res$parameters$summary['range','0.025quant']),
    ylim = c(0, 10^(-3)), xlim = c(0,1000),
    type='l', col=c('red','blue'),xlab='scale',lwd=3, ylab='dens')
    legend("topright", col=c("red","blue"),lty=1,legend=c("post'r","prior"))}

resQuantile = res = glgm(
    data=data2,
    grid=25,
    formula=y~1 + x+offset(offset),
```

```
prior = list(
      sd=c(lower=0.2, upper=2),
      range=c(lower=0.02, upper=0.5)),
    family="poisson", buffer=1,
    control.fixed=list(
      mean.intercept=0, prec.intercept=1,
      mean=0, prec=4),
    control.inla = list(strategy='gaussian')
  )
if(length(res$parameters)) {
# beta
  plot(res$inla$marginals.fixed[['x']], col='blue', type='l',
    xlab='beta',lwd=3)
  xseq = res$inla$marginals.fixed[['x']][,'x']
  lines(xseq, dnorm(xseq, 0, 1/2),col='red',lty=2,lwd=3)
  legend("topright", col=c("blue","red"),lty=1,legend=c("prior","post'r"))
# sd
    matplot(
      res$parameters$sd$posterior[,'x'],
      res$parameters$sd$posterior[,c('y','prior')],
      xlim = c(0, 4),
      type='l', col=c('red','blue'),xlab='sd',lwd=3, ylab='dens')
    legend("topright", col=c("blue", "red"), lty=1, legend=c("prior", "post'r"))
# range
    matplot(
      res$parameters$range$posterior[,'x'],
      res$parameters$range$posterior[,c('y','prior')],
      xlim = c(0, 1.2*res$parameters$summary['range','0.975quant']),
#
       xlim = c(0, 1), ylim = c(0,5),
      type='l', col=c('red','blue'),xlab='range',lwd=3, ylab='dens')
    legend("topright", col=c("red","blue"),lty=1,legend=c("post'r","prior"))
# scale
    matplot(
      res$parameters$scale$posterior[,'x'],
      res$parameters$scale$posterior[,c('y','prior')],
      xlim = c(0, 2/res$parameters$summary['range','0.025quant']),
       ylim = c(0, 10^{(-3)}), xlim = c(0, 1000),
#
      type='1', col=c('red','blue'),xlab='scale',lwd=3, ylab='dens')
    legend("topright", col=c("red","blue"),lty=1,legend=c("post'r","prior"))
}
```

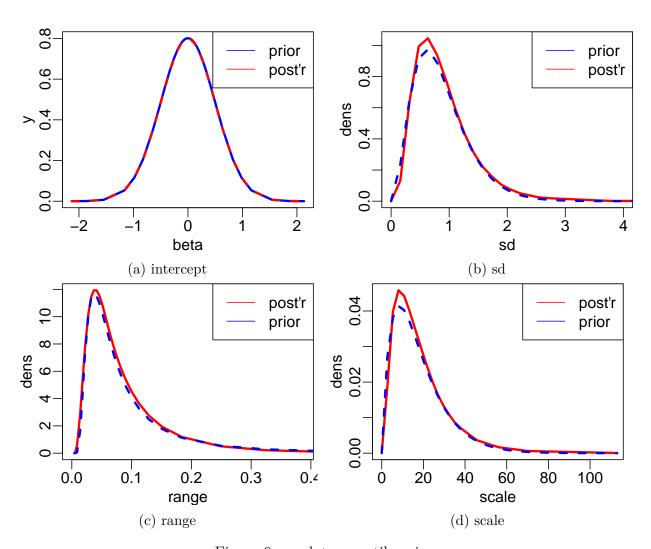


Figure 9: no data quantile priors

No data, legacy priors

```
resLegacy = res = glgm(data=data2,
    grid=20,
    formula=y~1 + x+offset(offset),
    priorCI = list(
        sd=c(lower=0.3,upper=0.5),
        range=c(lower=0.25, upper=0.4)),
    family="poisson",
    buffer=0.5,
    control.fixed=list(
        mean.intercept=0,
        prec.intercept=1,
        mean=0, prec=4),
    control.inla = list(strategy='gaussian'),
    control.mode=list(theta=c(2, 2),restart=TRUE)
```

```
)
if(length(res$parameters)) {
# intercept
  plot(res$inla$marginals.fixed[['(Intercept)']], col='blue', type='l',
    xlab='intercept',lwd=3)
  xseq = res$inla$marginals.fixed[['(Intercept)']][,'x']
  lines(xseq, dnorm(xseq, 0, 1),col='red',lty=2,lwd=3)
  legend("topright", col=c("blue", "red"), lty=1, legend=c("prior", "post'r"))
# beta
  plot(res$inla$marginals.fixed[['x']], col='blue', type='l',
    xlab='beta',lwd=3)
  xseq = res$inla$marginals.fixed[['x']][,'x']
  lines(xseq, dnorm(xseq, 0, 1/2),col='red',lty=2,lwd=3)
  legend("topright", col=c("blue", "red"), lty=1, legend=c("prior", "post'r"))
# sd
    matplot(
      res$parameters$sd$posterior[,'x'],
      res$parameters$sd$posterior[,c('y','prior')],
      type='l', col=c('red','blue'),xlab='sd',lwd=3, ylab='dens')
    legend("topright", col=c("blue", "red"), lty=1, legend=c("prior", "post'r"))
# range
    matplot(
      res$parameters$range$posterior[,'x'],
      res$parameters$range$posterior[,c('y','prior')],
      type='l', col=c('red','blue'),xlab='range',lwd=3, ylab='dens')
    legend("topright", col=c("blue", "red"), lty=1, legend=c("prior", "post'r"))
}
   specifying spatial formula
swissRain$group = 1+rbinom(length(swissRain), 1, 0.5)
theGrid = squareRaster(swissRain, Ncell, buffer=10*1000)
swissFit = glgm(
    formula = rain ~ 1,
    data=swissRain,
    grid=theGrid,
    family="gaussian",
    spaceFormula = ~ f(space, model='matern2d',
      nrow = nrow(theGrid), ncol = ncol(theGrid),
```

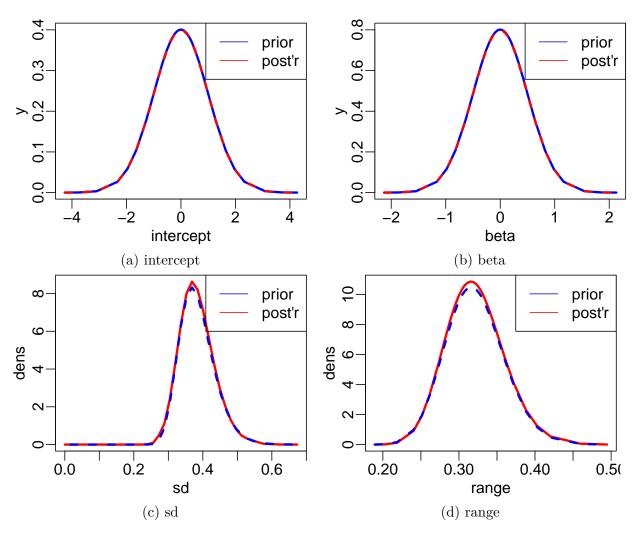


Figure 10: No data, legacy priors

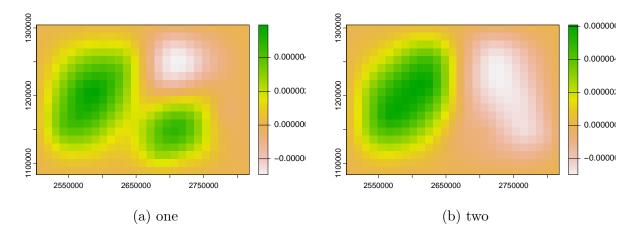


Figure 11: spatial formula provided