The `germinationmetrics` Package: A Brief Introduction

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2022-08-28

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Contents

Overview

The package `germinationmetrics` is a collection of functions which implements various methods for describing the time-course of germination in terms of single-value germination indices as well as fitted curves.

The goal of this vignette is to introduce the users to these functions and get started in describing sequentially recorded germination count data. This document assumes a basic knowledge of `R` programming language.

Installation

The package can be installed using the following functions:

```
# Install from CRAN
install.packages('germinationmetrics', dependencies=TRUE)

# Install development version from Github
devtools::install_github("aravind-j/germinationmetrics")
```

Then the package can be loaded using the function

```
library(germinationmetrics)
```

```
Welcome to germinationmetrics version 0.1.7


# To know how to use this package type:
  browseVignettes(package = 'germinationmetrics')
  for the package vignette.

# To know whats new in this version type:
  news(package='germinationmetrics')
  for the NEWS file.

# To cite the methods in the package type:
  citation(package='germinationmetrics')

# To suppress this message use:
  suppressPackageStartupMessages(library(germinationmetrics))
--------------------------------------------------------------------------------
```

Version History

The current version of the package is 0.1.7. The previous versions are as follows.

Table 1. Version history of `germinationmetrics` R package.

Version	Date
0.1.0	2018-04-17
0.1.1	2018-07-26
0.1.1.1	2018-10-16
0.1.2	2018-10-31
0.1.3	2019-01-19
0.1.4	2020-06-16
0.1.5	2021-02-17

To know detailed history of changes use `news(package='germinationmetrics')`.

Germination count data

Typically in a germination test, the germination count data of a fixed number of seeds is recorded at regular intervals for a definite period of time or until all the seeds have germinated. These germination count data can be either partial or cumulative (Table 2).

**Table 2 :** A typical germination count data.

intervals	counts	cumulative.counts
1	0	0
2	0	0
3	0	0
4	0	0
5	4	4
6	17	21
7	10	31
8	7	38
9	1	39
10	0	39
11	1	40
12	0	40
13	0	40
14	0	40

The time-course of germination can be plotted as follows.

```r
data <- data.frame(intervals = 1:14,
                   counts = c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0))

# Partial germination counts
x <- data$counts
# Cumulative germination counts
y <- cumsum(x)
# Time intervals of observations
int <- data$intervals

plot(int, cumsum(x))
```

3
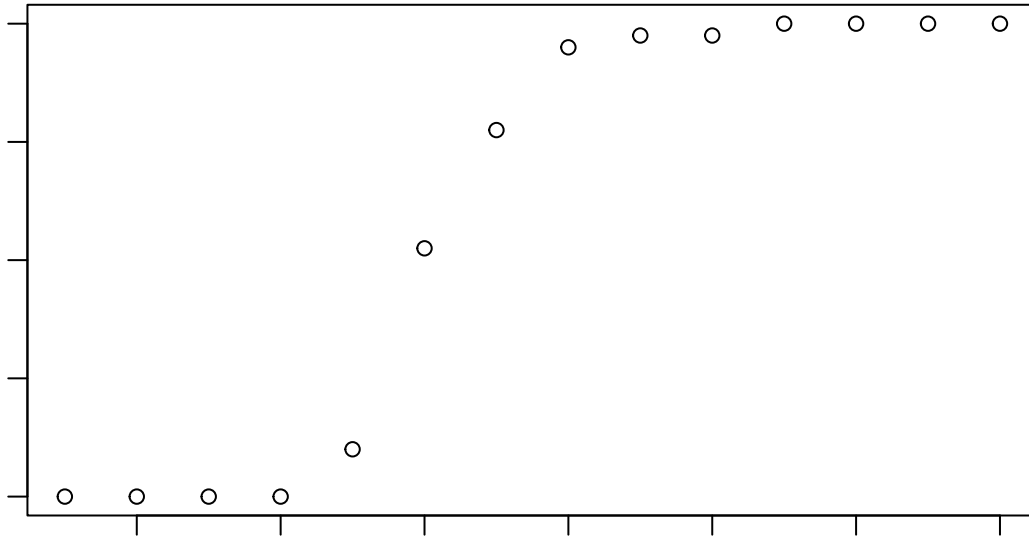
Single-value germination indices

The details about the single-value germination indices implemented in `germinationmetrics` are described in Table 3.

Table 3 : Single-value germination indices implemented in `germinationmetrics`.

Germination index	Function	Details	Unit	Measures	Reference
Germination percentage or Final germination percentage or Germinability (GP)	`GermPercent`	It is computed as follows. $$GP = \frac{N_g}{N_t} \times 100$$ Where, N_g is the number of germinated seeds and N_t is the total number of seeds.	Percentage (%)	Germination capacity	ISTA (2015)
Peak germination percentage (PGP)	`PeakGermPercent`	It is computed as follows. $$PGP = \frac{N_{max}}{N_t} \times 100$$ Where, N_{max} is the maximum number of seeds germinated per interval.	Percentage (%)	Germination capacity	Vallance (1950); Roh et al. (2004)
Time for the first germination or Germination time lag (t_0)	`FirstGermTime`	It is the time for first germination to occur (e.g. First day of germination). $$t_0 = \min\{T_i : N_i \neq 0\}$$ Where, T_i is the time from the start of the experiment to the ith interval and N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval)	time	Germination time	Edwards (1932); Czabator (1962); Goloff and Bazzaz (1975); Labouriau (1983a); Ranal (1999); Quintanilla et al. (2000)
Time for the last germination (t_g)	`LastGermTime`	It is the time for last germination to occur (e.g. Last day of germination) $$t_g = \max\{T_i : N_i \neq 0\}$$ Where, T_i is the time from the start of the experiment to the ith interval and N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval)	time	Germination time	Edwards (1932)
Time spread of germination or Germination distribution	`TimeSpreadGerm`	It is the difference between time for last germination (t_g) and time for first germination (t_0). $$Time\,spread\,of\,germination = t_g - t_0$$	time	Germination time	Al-Mudaris (1998); Schrader and Graves (2000); Kader (2005)
Peak period of germination or Modal time of germination (t_{peak})	`PeakGermTime`	It is the time in which highest frequency of germinated seeds are observed and need not be unique. $$t_{peak} = \{T_i : N_i = N_{max}\}$$ Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval) and N_{max} is the maximum number of seeds germinated per interval.	time	Germination time	Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Median germination time (t_{50}) (Coolbear)	`t50`	It is the time to reach 50% of final/maximum germination. With argument `method` specified as `"coolbear"`, it is computed as follows. $$t_{50} = T_i + \frac{(\frac{N+1}{2} - N_i)(T_j - T_i)}{N_j - N_i}$$ Where, t_{50} is the median germination time, N is the final number of germinated seeds, and N_i and N_j are the total number of seeds germinated in adjacent counts at time T_i and T_j respectively, when $N_i < \frac{N+1}{2} < N_j$.	time	Germination time	Coolbear et al. (1984)
Median germination time (t_{50}) (Farooq)	`t50`	With argument `method` specified as `"farooq"`, it is computed as follows. $$t_{50} = T_i + \frac{(\frac{N}{2} - N_i)(T_j - T_i)}{N_j - N_i}$$ Where, t_{50} is the median germination time, N is the final number of germinated seeds, and N_i and N_j are the total number of seeds germinated in adjacent counts at time T_i and T_j respectively, when $N_i < \frac{N}{2} < N_j$.	time	Germination time	Farooq et al. (2005)
Mean germination time or Mean length of incubation time ($\overline{T}$) or Germination resistance (GR) or Sprouting index (SI) or Emergence index (EI)	`MeanGermTime`	It is the average length of time required for maximum germination of a seed lot and is estimated according to the following formula. $$\overline{T} = \frac{\sum_{i=1}^{k} N_i T_i}{\sum_{i=1}^{k} N_i}$$ Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals. It is the inverse of mean germination rate ($\overline{V}$). $$\overline{T} = \frac{1}{\overline{V}}$$	time	Germination time	Edmond and Drapala (1958); Czabator (1962); Smith and Millet (1964); Gordon (1969); Gordon (1971); Mock and Eberhart (1972); Ellis and Roberts (1980) Labouriau (1983a); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Variance of germination time (s_T^2)	`VarGermTime`	It is computed according to the following formula. $$s_T^2 = \frac{\sum_{i=1}^{k} N_i (T_i - \overline{T})^2}{\sum_{i=1}^{k} N_i - 1}$$ Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.	time^{-1}	Germination time	Labouriau ([1983a](#)); Ranal and Santana ([2006](#))
Standard error of germination time $(s_{\overline{T}})$	`SEGermTime`	It signifies the accuracy of the calculation of the mean germination time. It is estimated according to the following formula: $$s_{\overline{T}} = \sqrt{\frac{s_T^2}{\sum_{i=1}^{k} N_i}}$$ Where, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval) and k is the total number of time intervals.	time	Germination time	Labouriau ([1983a](#)); Ranal and Santana ([2006](#))
Mean germination rate $(\overline{V})$	`MeanGermRate`	It is computed according to the following formula: $$\overline{V} = \frac{\sum_{i=1}^{k} N_i}{\sum_{i=1}^{k} N_i T_i}$$ Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals. It is the inverse of mean germination time $(\overline{T})$. $$\overline{V} = \frac{1}{\overline{T}}$$	time^{-1}	Germination rate	Labouriau and Valadares ([1976](#)); Labouriau ([1983b](#)); Ranal and Santana ([2006](#))

Germination index	Function	Details	Unit	Measures	Reference
Coefficient of velocity of germination (CVG) or Coefficient of rate of germination (CRG) or Kotowski's coefficient of velocity	`CVG`	It is estimated according to the following formula. $$CVG = \frac{\sum_{i=1}^{k} N_i}{\sum_{i=1}^{k} N_i T_i} \times 100$$ $$CVG = \overline{V} \times 100$$ Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.	% time^{-1}	Germination rate	Kotowski ([1926](#)), Nichols and Heydecker ([1968](#)); Bewley and Black ([1994](#)); Labouriau ([1983b](#)); Scott et al. ([1984](#))
Variance of germination rate (s_V^2)	`VarGermRate`	It is calculated according to the following formula. $$s_V^2 = \overline{V}^4 \times s_T^2$$ Where, s_T^2 is the variance of germination time.	time^{-2}	Germination rate	Labouriau ([1983b](#)); Ranal and Santana ([2006](#))
Standard error of germination rate ($s_{\overline{V}}$)	`SEGermRate`	It is estimated according to the following formula. $$s_{\overline{V}} = \sqrt{\frac{s_V^2}{\sum_{i=1}^{k} N_i}}$$ Where, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.	time^{-1}	Germination rate	Labouriau ([1983b](#)); Ranal and Santana ([2006](#))
Germination rate as the reciprocal of the median time (v_{50})	`GermRateRecip`	It is the reciprocal of the median germination time (t_{50}). $$v_{50} = \frac{1}{t_{50}}$$	time^{-1}	Germination rate	Went ([1957](#)); Labouriau ([1983b](#)); Ranal and Santana ([2006](#))
Speed of germination or Germination rate Index or index of velocity of germination or Emergence rate index (Allan, Vogel and Peterson; Erbach; Hsu and Nelson) or Germination index (AOSA)	`GermSpeed`	It is the rate of germination in terms of the total number of seeds that germinate in a time interval. It is estimated as follows. $$S = \sum_{i=1}^{k} \frac{N_i}{T_i}$$ Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals. Instead of germination counts, germination percentages may also be used for computation of speed of germination.	% time^{-1} or count time^{-1}	Mixed	Throneberry and Smith ([1955](#)); Maguire ([1962](#)); Allan et al. ([1962](#)); Kendrick and Frankland ([1969](#)); Bouton et al. ([1976](#)); Erbach ([1982](#)); AOSA ([1983](#)); Khandakar and Bradbeer ([1983](#)); Hsu and Nelson ([1986](#)); Bradbeer ([1988](#)); Wardle et al. ([1991](#))

Germination index	Function	Details	Unit	Measures	Reference
Speed of accumulated germination	GermSpeedAccumulate	It is the rate of germination in terms of the accumulated/cumulative total number of seeds that germinate in a time interval. It is estimated as follows. $$S_{accumulated} = \sum_{i=1}^{k} \frac{\sum_{j=1}^{i} N_j}{T_i}$$ Where, T_i is the time from the start of the experiment to the ith interval, $\sum_{j=1}^{i} N_j$ is the cumuative/accumulated number of seeds germinated in the ith interval, and k is the total number of time intervals. Instead of germination counts, germination percentages may also be used for computation of speed of germination.	% time⁻¹ or count time⁻¹	Mixed	Bradbeer (1988); Wardle et al. (1991); Haugland and Brandsaeter (1996); Santana and Ranal (2004)
Corrected germination rate index	GermSpeedCorrected	It is computed as follows. $$S_{corrected} = \frac{S}{FGP}$$ Where, S is the germination speed computed with germination percentage instead of counts and FGP is the final germination percentage or germinability.	time⁻¹	Mixed	Evetts and Burnside (1972)
Weighted germination percentage (WGP)	WeightGermPercent	It is estimated as follows. $$WGP = \frac{\sum_{i=1}^{k}(k - i + 1)N_i}{k \times N} \times 100$$ Where, N_i is the number of seeds that germinated in the time interval i (not cumulative, but partial count), N is the total number of seeds tested, and k is the total number of time intervals.	Percentage (%)	Mixed	Reddy et al. (1985); Reddy (1978)
Mean germination percentage per unit time ($\overline{GP}$)	MeanGermPercent	It is estimated as follows. $$\overline{GP} = \frac{GP}{T_k}$$ Where, GP is the final germination percentage, T_k is the time at the kth time interval, and k is the total number of time intervals required for final germination.	% time⁻¹	Mixed	Czabator (1962)
Number of seeds germinated per unit time $\overline{N}$	MeanGermNumber	It is estimated as follows. $$\overline{N} = \frac{N_g}{T_k}$$ Where, N_g is the number of germinated seeds at the end of the germination test, T_k is the time at the kth time interval, and k is the total number of time intervals required for final germination.	count time⁻¹	Mixed	Khamassi et al. (2013)

Germination index	Function	Details	Unit	Measures	Reference
Timson's index [$\sum 10$ (Ten summation), $\sum 5$ or $\sum 20$] or Germination energy index (GEI)	`TimsonsIndex`	It is the progressive total of cumulative germination percentage recorded at specific intervals for a set period of time and is estimated in terms of cumulative germination percentage (G_i) as follows. $$\Sigma k = \sum_{i=1}^{k} G_i$$ Where, G_i is the cumulative germination percentage in time interval i, and k is the total number of time intervals. It also estimated in terms of partial germination percentage as follows. $$\Sigma k = \sum_{i=1}^{k} g_i(k-j)$$ Where, g_i is the germination (not cumulative, but partial germination) in time interval i (i varying from 0 to k), k is the total number of time intervals, and $j = i - 1$.	Percentage (%)	Mixed	Grose and Zimmer (1958); Timson (1965); Lyon and Coffelt (1966); Chaudhary and Ghildyal (1970); Negm and Smith (1978); Brown and Mayer (1988); Baskin and Baskin (1998); Goodchild and Walker (1971)
Modified Timson's index (Σk_{mod}) (Labouriau)	`TimsonsIndex`	It is estimated as Timson's index Σk divided by the sum of partial germination percentages. $$\Sigma k_{mod} = \frac{\Sigma k}{\sum_{i=1}^{k} g_i}$$	no unit	Mixed	Ranal and Santana (2006)
Modified Timson's index (Σk_{mod}) (Khan and Unger)	`TimsonsIndex`	It is estimated as Timson's index (Σk) divided by the total time period of germination (T_k). $$\Sigma k_{mod} = \frac{\Sigma k}{T_k}$$	% time^{-1}	Mixed	Khan and Ungar (1984)
George's index (GR)	`GermRateGeorge`	It is estimated as follows. $$GR = \sum_{i=1}^{k} N_i K_i$$ Where N_i is the number of seeds germinated by ith interval and K_i is the number of intervals(eg. days) until the end of the test, and and k is the total number of time intervals.	count time	Mixed	George (1961); Tucker and Wright (1965); Nichols and Heydecker (1968)

Germination index	Function	Details	Unit	Measures	Reference
Germination Index (GI) (Melville)	`GermIndex`	It is estimated as follows. $$GI = \sum_{i=1}^{k} \frac{|(T_k - T_i)\,N_i|}{N_t}$$ Where, T_i is the time from the start of the experiment to the ith interval (day for the example), N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), N_t is the total number of seeds used in the test, and k is the total number of time intervals.	time	Mixed	Melville et al. (1980)
Germination Index (GI_{mod}) (Melville; Santana and Ranal)	`GermIndex`	It is estimated as follows. $$GI_{mod} = \sum_{i=1}^{k} \frac{|(T_k - T_i)\,N_i|}{N_g}$$ Where, T_i is the time from the start of the experiment to the ith interval (day for the example), N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), N_g is the total number of germinated seeds at the end of the test, and k is the total number of time intervals.	time	Mixed	Melville et al. (1980); Santana and Ranal (2004); Ranal and Santana (2006)
Emergence Rate Index (ERI) or Germination Rate Index (Shmueli and Goldberg)	`EmergenceRateIndex`	It is estimated as follows. $$ERI = \sum_{i=i_0}^{k-1} N_i(k-i)$$ Where, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), i_0 is the time interval when emergence/germination started, and k is the total number of time intervals.	count	Mixed	Shmueli and Goldberg (1971)
Modified Emergence Rate Index (ERI_{mod}) or Modified Germination Rate Index (Shmueli and Goldberg; Santana and Ranal)	`EmergenceRateIndex`	It is estimated by dividing Emergence rate index (ERI) by total number of emerged seedlings (or germinated seeds). $$ERI_{mod} = \frac{\sum_{i=i_0}^{k-1} N_i(k-i)}{N_g} = \frac{ERI}{N_g}$$ Where, N_g is the total number of germinated seeds at the end of the test, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), i_0 is the time interval when emergence/germination started, and k is the total number of time intervals.	no unit	Mixed	Shmueli and Goldberg (1971); Santana and Ranal (2004); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Emergence Rate Index (ERI) or Germination Rate Index (Bilbro & Wanjura)	EmergenceRateIndex	It is the estimated as follows. $$ERI = \frac{\sum_{i=1}^{k} N_i}{\overline{T}} = \frac{N_g}{\overline{T}}$$ Where, N_g is the total number of germinated seeds at the end of the test, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and $\overline{T}$ is the mean germination time or mean emergence time.	count time^{-1}	Mixed	Bilbro and Wanjura ([1982](#))
Emergence Rate Index (ERI) or Germination Rate Index (Fakorede)	EmergenceRateIndex	It is estimated as follows. $$ERI = \frac{\overline{T}}{FGP/100}$$ Where, $\overline{T}$ is the Mean germination time and FGP is the final germination time.	time count^{-1}	Mixed	Fakorede and Ayoola ([1980](#)); Fakorede and Ojo ([1981](#)); Fakorede and Agbana ([1983](#))
Peak value(PV) (Czabator) or Emergence Energy (EE)	PeakValue	It is the accumulated number of seeds germinated at the point on the germination curve at which the rate of germination starts to decrease. It is computed as the maximum quotient obtained by dividing successive cumulative germination values by the relevant incubation time. $$PV = \max\left(\frac{G_1}{T_1}, \frac{G_2}{T_2}, \cdots \frac{G_k}{T_k}\right)$$ Where, T_i is the time from the start of the experiment to the ith interval, G_i is the cumulative germination percentage in the ith time interval, and k is the total number of time intervals.	% time^{-1}	Mixed	Czabator ([1962](#)); Bonner ([1967](#))
Germination value (GV) (Czabator)	GermValue	It is computed as follows. $$GV = PV \times MDG$$ Where, PV is the peak value and MDG is the mean daily germination percentage from the onset of germination. It can also be computed for other time intervals of successive germination counts, by replacing MDG with the mean germination percentage per unit time ($\overline{GP}$). GV value can be modified (GV_{mod}), to consider the entire duration from the beginning of the test instead of just from the onset of germination.	%^{2} time^{-2}	Mixed	Czabator ([1962](#)); Brown and Mayer ([1988](#))

Germination index	Function	Details	Unit	Measures	Reference
Germination value (GV) (Diavanshir and Pourbiek)	`GermValue`	It is computed as follows. $$GV = \frac{\sum DGS}{N} \times GP \times c$$ Where, DGS is the daily germination speed computed by dividing cumulative germination percentage by the number of days since the since the onset of germination, N is the frequency or number of DGS calculated during the test, GP is the germination percentage expressed over 100, and c is a constant. The value of c is decided on the basis of average daily speed of germination ($\frac{\sum DGS}{N}$). If it is less than 10, then c value of 10 can be used and if it is more than 10, then value of 7 or 8 can be used for c. GV value can be modified (GV_{mod}), to consider the entire duration from the beginning of the test instead of just from the onset of germination.	$\%^2$ time^{-1}	Mixed	Djavanshir and Pourbeik (1976); Brown and Mayer (1988)
Coefficient of uniformity of germination (CUG)	`CUGerm`	It is computed as follows. $$CUG = \frac{\sum_{i=1}^{k} N_i}{\sum_{i=1}^{k} (\overline{T} - T_i)^2 N_i}$$ Where, $\overline{T}$ is the the mean germination time, T_i is the time from the start of the experiment to the ith interval (day for the example), N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.	time^{-2}	Germination unifromity	Heydecker (1972); Bewley and Black (1994)
Coefficient of variation of the germination time (CV_T)	`CVGermTime`	It is estimated as follows. $$CV_T = \sqrt{\frac{s_T^2}{\overline{T}}}$$ Where, s_T^2 is the variance of germination time and $\overline{T}$ is the mean germination time.	no unit	Germination unifromity	Gomes (1960); Ranal and Santana (2006)
Synchronization index ($\overline{E}$) or Uncertainty of the germination process (U) or informational entropy (H)	`GermUncertainty`	It is estimated as follows. $$\overline{E} = -\sum_{i=1}^{k} f_i \log_2 f_i$$ Where, f_i is the relative frequency of germination ($f_i = \frac{N_i}{\sum_{i=1}^{k} N_i}$), N_i is the number of seeds germinated on the ith time interval, and k is the total number of time intervals.	bit	Germination synchrony	Shannon (1948); Labouriau and Valadares (1976); Labouriau (1983b)

Germination index	Function	Details	Unit	Measures	Reference
Synchrony of germination (Z index)	`GermSynchrony`	It is computed as follows. $$Z = \frac{\sum_{i=1}^{k} C_{N_i,2}}{C_{\Sigma N_i,2}}$$ Where, $C_{N_i,2}$ is the partial combination of the two germinated seeds from among N_i, the number of seeds germinated on the ith time interval (estimated as $C_{N_i,2} = \frac{N_i(N_i-1)}{2}$), and $C_{\Sigma N_i,2}$ is the partial combination of the two germinated seeds from among the total number of seeds germinated at the final count, assuming that all seeds that germinated did so simultaneously.	no unit	Germination synchrony	Primack (1985); Ranal and Santana (2006)

Examples

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
z <- c(0, 0, 0, 0, 11, 11, 9, 7, 1, 0, 1, 0, 0, 0)
int <- 1:length(x)

# From partial germination counts
#-------------------------------------------------------------------------
GermPercent(germ.counts = x, total.seeds = 50)
```

GermPercent()

```
[1] 80
```

```
PeakGermPercent(germ.counts = x, intervals = int, total.seeds = 50)
```

```
[1] 34
```

```
# For multiple peak germination times
PeakGermPercent(germ.counts = z, intervals = int, total.seeds = 50)
```

```
Warning in PeakGermPercent(germ.counts = z, intervals = int, total.seeds = 50):
Multiple peak germination times exist.
```

```
[1] 22
```

```
# From cumulative germination counts
#-------------------------------------------------------------------------
GermPercent(germ.counts = y, total.seeds = 50, partial = FALSE)
```

```
[1] 80
```

```
PeakGermPercent(germ.counts = y, intervals = int, total.seeds = 50,
                partial = FALSE)
```

```
[1] 34
```

```
# For multiple peak germination times
PeakGermPercent(germ.counts = cumsum(z), intervals = int, total.seeds = 50,
                partial = FALSE)
```

```
Warning in PeakGermPercent(germ.counts = cumsum(z), intervals = int, total.seeds
= 50, : Multiple peak germination times exist.
```

```
[1] 22
```

```
# From number of germinated seeds
#-------------------------------------------------------------------------
GermPercent(germinated.seeds = 40, total.seeds = 50)
```

```
[1] 80
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
z <- c(0, 0, 0, 0, 11, 11, 9, 7, 1, 0, 1, 0, 0, 0)
int <- 1:length(x)
```

```
# From partial germination counts
#-------------------------------------------------------------------------------
FirstGermTime(germ.counts = x, intervals = int)
```

FirstGermTime(), LastGermTime(), PeakGermTime(), TimeSpreadGerm()

```
[1] 5
LastGermTime(germ.counts = x, intervals = int)
```

```
[1] 11
TimeSpreadGerm(germ.counts = x, intervals = int)
```

```
[1] 6
PeakGermTime(germ.counts = x, intervals = int)
```

```
[1] 6
# For multiple peak germination times
PeakGermTime(germ.counts = z, intervals = int)
```

```
Warning in PeakGermTime(germ.counts = z, intervals = int): Multiple peak
germination times exist.
```

```
[1] 5 6
# From cumulative germination counts
#-------------------------------------------------------------------------------
FirstGermTime(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 5
LastGermTime(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 11
TimeSpreadGerm(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 6
PeakGermTime(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 6
# For multiple peak germination time
PeakGermTime(germ.counts = cumsum(z), intervals = int, partial = FALSE)
```

```
Warning in PeakGermTime(germ.counts = cumsum(z), intervals = int, partial =
FALSE): Multiple peak germination times exist.
```

```
[1] 5 6
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-------------------------------------------------------------------------------
t50(germ.counts = x, intervals = int, method = "coolbear")
```

```r
t50()
```

```
[1] 5.970588
```

```r
t50(germ.counts = x, intervals = int, method = "farooq")
```

```
[1] 5.941176
```

```r
# From cumulative germination counts
#-----------------------------------------------------------------------------
t50(germ.counts = y, intervals = int, partial = FALSE, method = "coolbear")
```

```
[1] 5.970588
```

```r
t50(germ.counts = y, intervals = int, partial = FALSE, method = "farooq")
```

```
[1] 5.941176
```

```r
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-----------------------------------------------------------------------------
MeanGermTime(germ.counts = x, intervals = int)
```

```r
MeanGermTime(), VarGermTime(), SEGermTime(), CVGermTime()
```

```
[1] 6.7
```

```r
VarGermTime(germ.counts = x, intervals = int)
```

```
[1] 1.446154
```

```r
SEGermTime(germ.counts = x, intervals = int)
```

```
[1] 0.1901416
```

```r
CVGermTime(germ.counts = x, intervals = int)
```

```
[1] 0.1794868
```

```r
# From cumulative germination counts
#-----------------------------------------------------------------------------
MeanGermTime(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 6.7
```

```r
VarGermTime(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 19.04012
```

```r
SEGermTime(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 0.2394781
```

```r
CVGermTime(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 0.6512685
```

```r
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#------------------------------------------------------------------------------
MeanGermRate(germ.counts = x, intervals = int)
```

```
MeanGermRate(), CVG(), VarGermRate(), SEGermRate(), GermRateRecip()
```

```
[1] 0.1492537
```

```r
CVG(germ.counts = x, intervals = int)
```

```
[1] 14.92537
```

```r
VarGermRate(germ.counts = x, intervals = int)
```

```
[1] 0.0007176543
```

```r
SEGermRate(germ.counts = x, intervals = int)
```

```
[1] 0.004235724
```

```r
GermRateRecip(germ.counts = x, intervals = int, method = "coolbear")
```

```
[1] 0.1674877
```

```r
GermRateRecip(germ.counts = x, intervals = int, method = "farooq")
```

```
[1] 0.1683168
```

```r
# From cumulative germination counts
#------------------------------------------------------------------------------
MeanGermRate(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 0.1492537
```

```r
CVG(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 14.92537
```

```r
VarGermRate(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 0.009448666
```

```r
SEGermRate(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 0.005334776
```

```r
GermRateRecip(germ.counts = y, intervals = int,
              method = "coolbear", partial = FALSE)
```

```
[1] 0.1674877
```

```r
GermRateRecip(germ.counts = y, intervals = int,
              method = "farooq", partial = FALSE)
```

```
[1] 0.1683168
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-------------------------------------------------------------------------
GermSpeed(germ.counts = x, intervals = int)
```

GermSpeed(), GermSpeedAccumulated(), GermSpeedCorrected()

```
[1] 6.138925
```

```
GermSpeedAccumulated(germ.counts = x, intervals = int)
```

```
[1] 34.61567
```

```
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                   method = "normal")
```

```
[1] 0.1534731
```

```
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                   method = "accumulated")
```

```
[1] 0.8653917
```

```
# From partial germination counts (with percentages instead of counts)
#-------------------------------------------------------------------------
GermSpeed(germ.counts = x, intervals = int,
          percent = TRUE, total.seeds = 50)
```

```
[1] 12.27785
```

```
GermSpeedAccumulated(germ.counts = x, intervals = int,
                     percent = TRUE, total.seeds = 50)
```

```
[1] 69.23134
```

```
# From cumulative germination counts
#-------------------------------------------------------------------------
GermSpeed(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 6.138925
```

```
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 34.61567
```

```
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "normal")
```

```
[1] 0.1534731
```

```
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "accumulated")
```

```
[1] 0.8653917
```

```
# From cumulative germination counts (with percentages instead of counts)
#-------------------------------------------------------------------------
```

```
GermSpeed(germ.counts = y, intervals = int, partial = FALSE,
          percent = TRUE, total.seeds = 50)
```

```
[1] 12.27785
```

```
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE,
                     percent = TRUE, total.seeds = 50)
```

```
[1] 69.23134
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-----------------------------------------------------------------------------
WeightGermPercent(germ.counts = x, total.seeds = 50, intervals = int)
```

WeightGermPercent()

```
[1] 47.42857
```

```
# From cumulative germination counts
#-----------------------------------------------------------------------------
WeightGermPercent(germ.counts = y, total.seeds = 50, intervals = int,
                  partial = FALSE)
```

```
[1] 47.42857
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-----------------------------------------------------------------------------
MeanGermPercent(germ.counts = x, total.seeds = 50, intervals = int)
```

MeanGermPercent(), MeanGermNumber()

```
[1] 5.714286
```

```
MeanGermNumber(germ.counts = x, intervals = int)
```

```
[1] 2.857143
```

```
# From cumulative germination counts
#-----------------------------------------------------------------------------
MeanGermPercent(germ.counts = y, total.seeds = 50, intervals = int, partial = FALSE)
```

```
[1] 5.714286
```

```
MeanGermNumber(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 2.857143
```

```
# From number of germinated seeds
#------------------------------------------------------------------------------
MeanGermPercent(germinated.seeds = 40, total.seeds = 50, intervals = int)
```

```
[1] 5.714286
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#------------------------------------------------------------------------------
# Wihout max specified
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50)
```

TimsonsIndex(), GermRateGeorge()

```
[1] 664
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            modification = "none")
```

```
[1] 664
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            modification = "labouriau")
```

```
[1] 8.3
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            modification = "khanungar")
```

```
[1] 47.42857
```

```
GermRateGeorge(germ.counts = x, intervals = int)
```

```
[1] 332
```

```
# With max specified
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50, max = 10)
```

```
[1] 344
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            max = 10, modification = "none")
```

```
[1] 344
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            max = 10, modification = "labouriau")
```

```
[1] 4.410256
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            max = 10, modification = "khanungar")
```

```
[1] 24.57143
```

```
GermRateGeorge(germ.counts = x, intervals = int, max = 10)
```

```
[1] 172
```
```
GermRateGeorge(germ.counts = x, intervals = int, max = 14)
```
```
[1] 332
```
```
# From cumulative germination counts
#-------------------------------------------------------------------------------
# Wihout max specified
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50)
```
```
[1] 664
```
```
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             modification = "none")
```
```
[1] 664
```
```
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             modification = "labouriau")
```
```
[1] 8.3
```
```
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             modification = "khanungar")
```
```
[1] 47.42857
```
```
GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,)
```
```
[1] 332
```
```
# With max specified
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50, max = 10)
```
```
[1] 344
```
```
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             max = 10, modification = "none")
```
```
[1] 344
```
```
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             max = 10, modification = "labouriau")
```
```
[1] 4.410256
```
```
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             max = 10, modification = "khanungar")
```
```
[1] 24.57143
```
```
GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,
               max = 10)
```

```
[1] 172
```

```r
GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,
               max = 14)
```

```
[1] 332
```

```r
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-----------------------------------------------------------------------------
GermIndex(germ.counts = x, intervals = int, total.seeds = 50)
```

```r
GermIndex()
```

```
[1] 5.84
```

```r
GermIndex(germ.counts = x, intervals = int, total.seeds = 50,
          modification = "none")
```

```
[1] 5.84
```

```r
GermIndex(germ.counts = x, intervals = int, total.seeds = 50,
          modification = "santanaranal")
```

```
[1] 7.3
```

```r
# From cumulative germination counts
#-----------------------------------------------------------------------------
GermIndex(germ.counts = y, intervals = int, partial = FALSE,
          total.seeds = 50)
```

```
[1] 5.84
```

```r
GermIndex(germ.counts = y, intervals = int, partial = FALSE,
          total.seeds = 50,
          modification = "none")
```

```
[1] 5.84
```

```r
GermIndex(germ.counts = y, intervals = int, partial = FALSE,
          total.seeds = 50,
          modification = "santanaranal")
```

```
[1] 7.3
```

```r
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-----------------------------------------------------------------------------
EmergenceRateIndex(germ.counts = x, intervals = int)
```

```r
EmergenceRateIndex()
```

```
[1] 292
```
```
EmergenceRateIndex(germ.counts = x, intervals = int,
                   method = "shmueligoldberg")
```

```
[1] 292
```
```
EmergenceRateIndex(germ.counts = x, intervals = int,
                   method = "sgsantanaranal")
```

```
[1] 7.3
```
```
EmergenceRateIndex(germ.counts = x, intervals = int,
                   method = "bilbrowanjura")
```

```
[1] 5.970149
```
```
EmergenceRateIndex(germ.counts = x, intervals = int,
                   total.seeds = 50, method = "fakorede")
```

```
[1] 8.375
```
```
# From cumulative germination counts
#-------------------------------------------------------------------------------
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,)
```

```
[1] 292
```
```
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   method = "shmueligoldberg")
```

```
[1] 292
```
```
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   method = "sgsantanaranal")
```

```
[1] 7.3
```
```
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   method = "bilbrowanjura")
```

```
[1] 5.970149
```
```
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   total.seeds = 50, method = "fakorede")
```

```
[1] 8.375
```

```
x <- c(0, 0, 34, 40, 21, 10, 4, 5, 3, 5, 8, 7, 7, 6, 6, 4, 0, 2, 0, 2)
y <- c(0, 0, 34, 74, 95, 105, 109, 114, 117, 122, 130, 137, 144, 150,
       156, 160, 160, 162, 162, 164)
int <- 1:length(x)
total.seeds = 200

# From partial germination counts
#-------------------------------------------------------------------------------
PeakValue(germ.counts = x, intervals = int, total.seeds = 200)
```

PeakValue(), GermValue()

```
[1] 9.5
```

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
          method = "czabator")
```

```
$`Germination Value`
[1] 38.95
```

```
[[2]]
   germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent
3           34         3                     34                    17.0
4           40         4                     74                    37.0
5           21         5                     95                    47.5
6           10         6                    105                    52.5
7            4         7                    109                    54.5
8            5         8                    114                    57.0
9            3         9                    117                    58.5
10           5        10                    122                    61.0
11           8        11                    130                    65.0
12           7        12                    137                    68.5
13           7        13                    144                    72.0
14           6        14                    150                    75.0
15           6        15                    156                    78.0
16           4        16                    160                    80.0
17           0        17                    160                    80.0
18           2        18                    162                    81.0
19           0        19                    162                    81.0
20           2        20                    164                    82.0
        DGS
3  5.666667
4  9.250000
5  9.500000
6  8.750000
7  7.785714
8  7.125000
9  6.500000
10 6.100000
11 5.909091
12 5.708333
13 5.538462
14 5.357143
15 5.200000
16 5.000000
17 4.705882
18 4.500000
19 4.263158
20 4.100000
```

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
          method = "dp", k = 10)
```

```
$`Germination Value`
[1] 53.36595
```

```
[[2]]
```

```
   germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent
3           34         3                     34                    17.0
4           40         4                     74                    37.0
5           21         5                     95                    47.5
6           10         6                    105                    52.5
7            4         7                    109                    54.5
8            5         8                    114                    57.0
9            3         9                    117                    58.5
10           5        10                    122                    61.0
11           8        11                    130                    65.0
12           7        12                    137                    68.5
13           7        13                    144                    72.0
14           6        14                    150                    75.0
15           6        15                    156                    78.0
16           4        16                    160                    80.0
17           0        17                    160                    80.0
18           2        18                    162                    81.0
19           0        19                    162                    81.0
20           2        20                    164                    82.0
        DGS SumDGSbyN         GV
3  5.666667  5.666667  9.633333
4  9.250000  7.458333 27.595833
5  9.500000  8.138889 38.659722
6  8.750000  8.291667 43.531250
7  7.785714  8.190476 44.638095
8  7.125000  8.012897 45.673512
9  6.500000  7.796769 45.611097
10 6.100000  7.584673 46.266503
11 5.909091  7.398497 48.090230
12 5.708333  7.229481 49.521942
13 5.538462  7.075752 50.945411
14 5.357143  6.932534 51.994006
15 5.200000  6.799262 53.034246
16 5.000000  6.670744 53.365948
17 4.705882  6.539753 52.318022
18 4.500000  6.412268 51.939373
19 4.263158  6.285850 50.915385
20 4.100000  6.164414 50.548194


$testend
[1] 16
```

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
          method = "czabator", from.onset = FALSE)
```

```
$`Germination Value`
[1] 38.95


[[2]]
   germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent
1            0         1                      0                     0.0
2            0         2                      0                     0.0
3           34         3                     34                    17.0
4           40         4                     74                    37.0
5           21         5                     95                    47.5
```

6	10	6	105	52.5
7	4	7	109	54.5
8	5	8	114	57.0
9	3	9	117	58.5
10	5	10	122	61.0
11	8	11	130	65.0
12	7	12	137	68.5
13	7	13	144	72.0
14	6	14	150	75.0
15	6	15	156	78.0
16	4	16	160	80.0
17	0	17	160	80.0
18	2	18	162	81.0
19	0	19	162	81.0
20	2	20	164	82.0

```
        DGS
1   0.000000
2   0.000000
3   5.666667
4   9.250000
5   9.500000
6   8.750000
7   7.785714
8   7.125000
9   6.500000
10  6.100000
11  5.909091
12  5.708333
13  5.538462
14  5.357143
15  5.200000
16  5.000000
17  4.705882
18  4.500000
19  4.263158
20  4.100000
```

```r
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
          method = "dp", k = 10, from.onset = FALSE)
```

```
$`Germination Value`
[1] 46.6952


[[2]]
   germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent
1            0         1                      0                     0.0
2            0         2                      0                     0.0
3           34         3                     34                    17.0
4           40         4                     74                    37.0
5           21         5                     95                    47.5
6           10         6                    105                    52.5
7            4         7                    109                    54.5
8            5         8                    114                    57.0
9            3         9                    117                    58.5
10           5        10                    122                    61.0
```

```
11               8        11                      130                    65.0
12               7        12                      137                    68.5
13               7        13                      144                    72.0
14               6        14                      150                    75.0
15               6        15                      156                    78.0
16               4        16                      160                    80.0
17               0        17                      160                    80.0
18               2        18                      162                    81.0
19               0        19                      162                    81.0
20               2        20                      164                    82.0
        DGS SumDGSbyN        GV
1   0.000000  0.000000  0.000000
2   0.000000  0.000000  0.000000
3   5.666667  1.888889  3.211111
4   9.250000  3.729167 13.797917
5   9.500000  4.883333 23.195833
6   8.750000  5.527778 29.020833
7   7.785714  5.850340 31.884354
8   7.125000  6.009673 34.255134
9   6.500000  6.064153 35.475298
10 6.100000  6.067738 37.013202
11 5.909091  6.053316 39.346552
12 5.708333  6.024567 41.268285
13 5.538462  5.987174 43.107655
14 5.357143  5.942172 44.566291
15 5.200000  5.892694 45.963013
16 5.000000  5.836901 46.695205
17 4.705882  5.770370 46.162961
18 4.500000  5.699794 46.168331
19 4.263158  5.624182 45.555871
20 4.100000  5.547972 45.493374


$testend
[1] 16
```

```
# From cumulative germination counts
#-------------------------------------------------------------------------------
PeakValue(germ.counts = y, interval = int, total.seeds = 200,
          partial = FALSE)
```

```
[1] 9.5
```

```
GermValue(germ.counts = y, intervals = int, total.seeds = 200,
          partial = FALSE, method = "czabator")
```

```
$`Germination Value`
[1] 38.95


[[2]]
   germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent
3           34         3                     34                    17.0
4           40         4                     74                    37.0
5           21         5                     95                    47.5
6           10         6                    105                    52.5
7            4         7                    109                    54.5
```

8	5	8	114	57.0
9	3	9	117	58.5
10	5	10	122	61.0
11	8	11	130	65.0
12	7	12	137	68.5
13	7	13	144	72.0
14	6	14	150	75.0
15	6	15	156	78.0
16	4	16	160	80.0
17	0	17	160	80.0
18	2	18	162	81.0
19	0	19	162	81.0
20	2	20	164	82.0

```
        DGS
3   5.666667
4   9.250000
5   9.500000
6   8.750000
7   7.785714
8   7.125000
9   6.500000
10  6.100000
11  5.909091
12  5.708333
13  5.538462
14  5.357143
15  5.200000
16  5.000000
17  4.705882
18  4.500000
19  4.263158
20  4.100000
```

```r
GermValue(germ.counts = y, intervals = int, total.seeds = 200,
          partial = FALSE, method = "dp", k = 10)
```

```
$`Germination Value`
[1] 53.36595


[[2]]
   germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent
3           34         3                     34                    17.0
4           40         4                     74                    37.0
5           21         5                     95                    47.5
6           10         6                    105                    52.5
7            4         7                    109                    54.5
8            5         8                    114                    57.0
9            3         9                    117                    58.5
10           5        10                    122                    61.0
11           8        11                    130                    65.0
12           7        12                    137                    68.5
13           7        13                    144                    72.0
14           6        14                    150                    75.0
15           6        15                    156                    78.0
16           4        16                    160                    80.0
```

```
17               0        17              160                  80.0
18               2        18              162                  81.0
19               0        19              162                  81.0
20               2        20              164                  82.0
        DGS SumDGSbyN        GV
3   5.666667  5.666667  9.633333
4   9.250000  7.458333 27.595833
5   9.500000  8.138889 38.659722
6   8.750000  8.291667 43.531250
7   7.785714  8.190476 44.638095
8   7.125000  8.012897 45.673512
9   6.500000  7.796769 45.611097
10  6.100000  7.584673 46.266503
11  5.909091  7.398497 48.090230
12  5.708333  7.229481 49.521942
13  5.538462  7.075752 50.945411
14  5.357143  6.932534 51.994006
15  5.200000  6.799262 53.034246
16  5.000000  6.670744 53.365948
17  4.705882  6.539753 52.318022
18  4.500000  6.412268 51.939373
19  4.263158  6.285850 50.915385
20  4.100000  6.164414 50.548194


$testend
[1] 16
```

```
GermValue(germ.counts = y, intervals = int, total.seeds = 200,
          partial = FALSE, method = "czabator", from.onset = FALSE)
```

```
$`Germination Value`
[1] 38.95


[[2]]
   germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent
1            0         1                      0                     0.0
2            0         2                      0                     0.0
3           34         3                     34                    17.0
4           40         4                     74                    37.0
5           21         5                     95                    47.5
6           10         6                    105                    52.5
7            4         7                    109                    54.5
8            5         8                    114                    57.0
9            3         9                    117                    58.5
10           5        10                    122                    61.0
11           8        11                    130                    65.0
12           7        12                    137                    68.5
13           7        13                    144                    72.0
14           6        14                    150                    75.0
15           6        15                    156                    78.0
16           4        16                    160                    80.0
17           0        17                    160                    80.0
18           2        18                    162                    81.0
19           0        19                    162                    81.0
20           2        20                    164                    82.0
```

```
          DGS
1   0.000000
2   0.000000
3   5.666667
4   9.250000
5   9.500000
6   8.750000
7   7.785714
8   7.125000
9   6.500000
10  6.100000
11  5.909091
12  5.708333
13  5.538462
14  5.357143
15  5.200000
16  5.000000
17  4.705882
18  4.500000
19  4.263158
20  4.100000
```

```
GermValue(germ.counts = y, intervals = int, total.seeds = 200,
          partial = FALSE, method = "dp", k = 10, from.onset = FALSE)
```

```
$`Germination Value`
[1] 46.6952


[[2]]
   germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent
1            0         1                      0                     0.0
2            0         2                      0                     0.0
3           34         3                     34                    17.0
4           40         4                     74                    37.0
5           21         5                     95                    47.5
6           10         6                    105                    52.5
7            4         7                    109                    54.5
8            5         8                    114                    57.0
9            3         9                    117                    58.5
10           5        10                    122                    61.0
11           8        11                    130                    65.0
12           7        12                    137                    68.5
13           7        13                    144                    72.0
14           6        14                    150                    75.0
15           6        15                    156                    78.0
16           4        16                    160                    80.0
17           0        17                    160                    80.0
18           2        18                    162                    81.0
19           0        19                    162                    81.0
20           2        20                    164                    82.0
        DGS SumDGSbyN        GV
1  0.000000  0.000000  0.000000
2  0.000000  0.000000  0.000000
3  5.666667  1.888889  3.211111
4  9.250000  3.729167 13.797917
```

```
5  9.500000  4.883333 23.195833
6  8.750000  5.527778 29.020833
7  7.785714  5.850340 31.884354
8  7.125000  6.009673 34.255134
9  6.500000  6.064153 35.475298
10 6.100000  6.067738 37.013202
11 5.909091  6.053316 39.346552
12 5.708333  6.024567 41.268285
13 5.538462  5.987174 43.107655
14 5.357143  5.942172 44.566291
15 5.200000  5.892694 45.963013
16 5.000000  5.836901 46.695205
17 4.705882  5.770370 46.162961
18 4.500000  5.699794 46.168331
19 4.263158  5.624182 45.555871
20 4.100000  5.547972 45.493374

$testend
[1] 16
```

```r
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#----------------------------------------------------------------------------
CUGerm(germ.counts = x, intervals = int)
```

CUGerm()

```
[1] 0.7092199
```

```r
# From cumulative germination counts
#----------------------------------------------------------------------------
CUGerm(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 0.05267935
```

```r
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#----------------------------------------------------------------------------
GermSynchrony(germ.counts = x, intervals = int)
```

GermSynchrony(), GermUncertainty()

```
[1] 0.2666667
```

```r
GermUncertainty(germ.counts = x, intervals = int)
```

```
[1] 2.062987
```

```
# From cumulative germination counts
#-------------------------------------------------------------------------------
GermSynchrony(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 0.2666667
```

```
GermUncertainty(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 2.062987
```

Non-linear regression analysis

Several mathematical functions have been used to fit the cumulative germination count data and describe the germination process by non-linear regression analysis. They include functions such as Richard's, Weibull, logistic, log-logistic, gaussian, four-parameter hill function etc. Currently `germinationmetrics` implements the four-parameter hill function to fit the count data and computed various associated metrics.

Four-parameter hill function

The four-parameter hill function defined as follows (El-Kassaby et al., 2008).

$$f(x) = y = y_0 + \frac{ax^b}{x^b + c^b}$$

Where, y is the cumulative germination percentage at time x, y_0 is the intercept on the y axis, a is the asymptote, b is a mathematical parameter controlling the shape and steepness of the germination curve and c is the "half-maximal activation level".

The details of various parameters that are computed from this function are given in Table 4.

Table 4 Germination parameters estimated from the four-parameter hill function.

Germination parameters	Details	Unit	Measures
y intercept (y_0)	The intercept on the y axis.		
Asymptote (a)	It is the maximum cumulative germination percentage, which is equivalent to germination capacity.	%	Germination capacity
Shape and steepness (b)	Mathematical parameter controlling the shape and steepness of the germination curve. The larger the b, the steeper the rise toward the asymptote a, and the shorter the time between germination onset and maximum germination.		Germination rate
Half-maximal activation level (c)	Time required for 50% of viable seeds to germinate.	time	Germination time
lag	It is the time at germination onset and is computed by solving four-parameter hill function after setting y to 0 as follows. $$lag = b\sqrt{\frac{-y_0 c^b}{a + y_0}}$$	time	Germination time
D_{lag-50}	The duration between the time at germination onset (lag) and that at 50% germination (c).	time	Germination time

Germination parameters	Details	Unit	Measures
$t_{50_{total}}$	Time required for 50% of total seeds to germinate.	time	Germination time
$t_{50_{germinated}}$	Time required for 50% of viable/germinated seeds to germinate	time	Germination time
$t_{x_{total}}$	Time required for $x\%$ of total seeds to germinate.	time	Germination time
$t_{x_{germinated}}$	Time required for $x\%$ of viable/germinated seeds to germinate	time	Germination time
Uniformity ($U_{t_{max}-t_{min}}$)	It is the time interval between the percentages of viable seeds specified in the arguments `umin` and `umin` to germinate.	time	Germination time
Time at maximum germination rate ($TMGR$)	The partial derivative of the four-parameter hill function gives the instantaneous rate of germination (s) as follows. $$s = \frac{\partial y}{\partial x} = \frac{abc^b x^{b-1}}{(c^b + x^b)^2}$$ From this function for instantaneous rate of germination, $TMGR$ can be estimated as follows. $$TMGR = b\sqrt{\frac{c^b(b-1)}{b+1}}$$ It represents the point in time when the instantaneous rate of germination starts to decline.	time	Germination time
Area under the curve (AUC)	It is obtained by integration of the fitted curve between time 0 and time specified in the argument `tmax`.		Mixed
MGT	Calculated by integration of the fitted curve and proper normalisation.	time	Germination time
Skewness	It is computed as follows. $$\frac{MGT}{t_{50_{germinated}}}$$		

Examples

```r
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)
total.seeds = 50

# From partial germination counts
#----------------------------------------------------------------------------
FourPHFfit(germ.counts = x, intervals = int, total.seeds = 50, tmax = 20)
```

FourPHFfit()

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```
$data
   gp csgp intervals
1   0    0         1
2   0    0         2
3   0    0         3
4   0    0         4
5   8    8         5
6  34   42         6
7  20   62         7
8  14   76         8
9   2   78         9
10  0   78        10
11  2   80        11
12  0   80        12
13  0   80        13
14  0   80        14


$Parameters
  term   estimate   std.error  statistic      p.value
1    a  80.000000  1.24158595   64.43372 1.973240e-14
2    b   9.881947  0.70779379   13.96162 6.952322e-08
3    c   6.034954  0.04952654  121.85294 3.399385e-17
4   y0   0.000000  0.91607007    0.00000 1.000000e+00


$Fit
     sigma isConv       finTol     logLik      AIC      BIC deviance df.residual
1 1.769385   TRUE 1.490116e-08 -25.49868 60.99736 64.19265 31.30723          10
  nobs
1   14


$a
[1] 80


$b
[1] 9.881947


$c
[1] 6.034954


$y0
[1] 0


$lag
[1] 0


$Dlag50
[1] 6.034954


$t50.total
[1] 6.355122


$txp.total
       10        60
4.956266 6.744598
```

```
$t50.Germinated
[1] 6.034954

$txp.Germinated
       10        60
4.831809 6.287724

$Uniformity
          90           10 uniformity
   7.537688     4.831809    2.705880

$TMGR
[1] 5.912195

$AUC
[1] 1108.975

$MGT
[1] 6.632252

$Skewness
[1] 1.098973

$msg
[1] "#1. Relative error in the sum of squares is at most `ftol'. "

$isConv
[1] TRUE

attr(,"class")
[1] "FourPHFfit" "list"
```

```r
# From cumulative germination counts
#-----------------------------------------------------------------------------
FourPHFfit(germ.counts = y, intervals = int, total.seeds = 50, tmax = 20,
partial = FALSE)
```

```
$data
    gp csgp intervals
1    0    0         1
2    0    0         2
3    0    0         3
4    0    0         4
5    8    8         5
6   34   42         6
7   20   62         7
8   14   76         8
9    2   78         9
10   0   78        10
11   2   80        11
12   0   80        12
13   0   80        13
14   0   80        14
```

```
$Parameters
  term   estimate std.error statistic      p.value
1    a 80.000000 1.2415867  64.43368 1.973252e-14
2    b  9.881927 0.7077918  13.96163 6.952270e-08
3    c  6.034953 0.0495266 121.85275 3.399437e-17
4   y0  0.000000 0.9160705   0.00000 1.000000e+00

$Fit
     sigma isConv      finTol    logLik      AIC      BIC deviance df.residual
1 1.769385   TRUE 1.490116e-08 -25.49868 60.99736 64.19265 31.30723          10
  nobs
1   14

$a
[1] 80

$b
[1] 9.881927

$c
[1] 6.034953

$y0
[1] 0

$lag
[1] 0

$Dlag50
[1] 6.034953

$t50.total
[1] 6.355121

$txp.total
      10       60
4.956263 6.744599

$t50.Germinated
[1] 6.034953

$txp.Germinated
      10       60
4.831806 6.287723

$Uniformity
       90       10 uniformity
  7.537691 4.831806   2.705885

$TMGR
[1] 5.912194

$AUC
[1] 1108.976
```

```
$MGT
[1] 6.632252

$Skewness
[1] 1.098973

$msg
[1] "#1. Relative error in the sum of squares is at most `ftol'. "

$isConv
[1] TRUE

attr(,"class")
[1] "FourPHFfit" "list"
```

```r
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)
total.seeds = 50

# From partial germination counts
#-------------------------------------------------------------------------------
fit1 <- FourPHFfit(germ.counts = x, intervals = int,
                   total.seeds = 50, tmax = 20)

# From cumulative germination counts
#-------------------------------------------------------------------------------
fit2 <- FourPHFfit(germ.counts = y, intervals = int,
                   total.seeds = 50, tmax = 20, partial = FALSE)

# Default plots
plot(fit1)
```
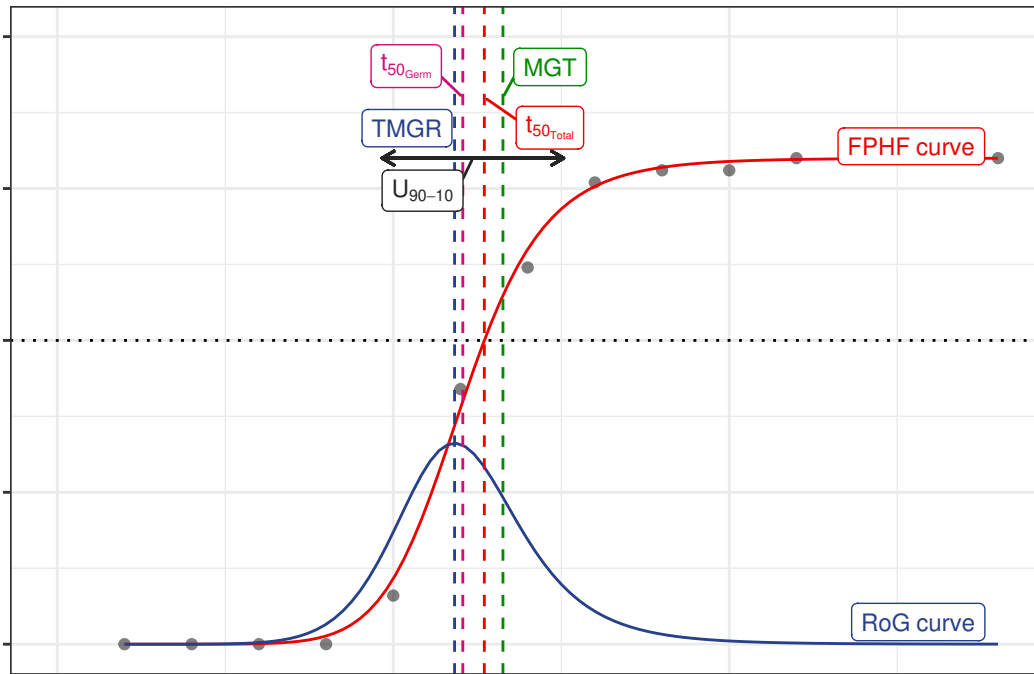
```
plot(fit2)
```
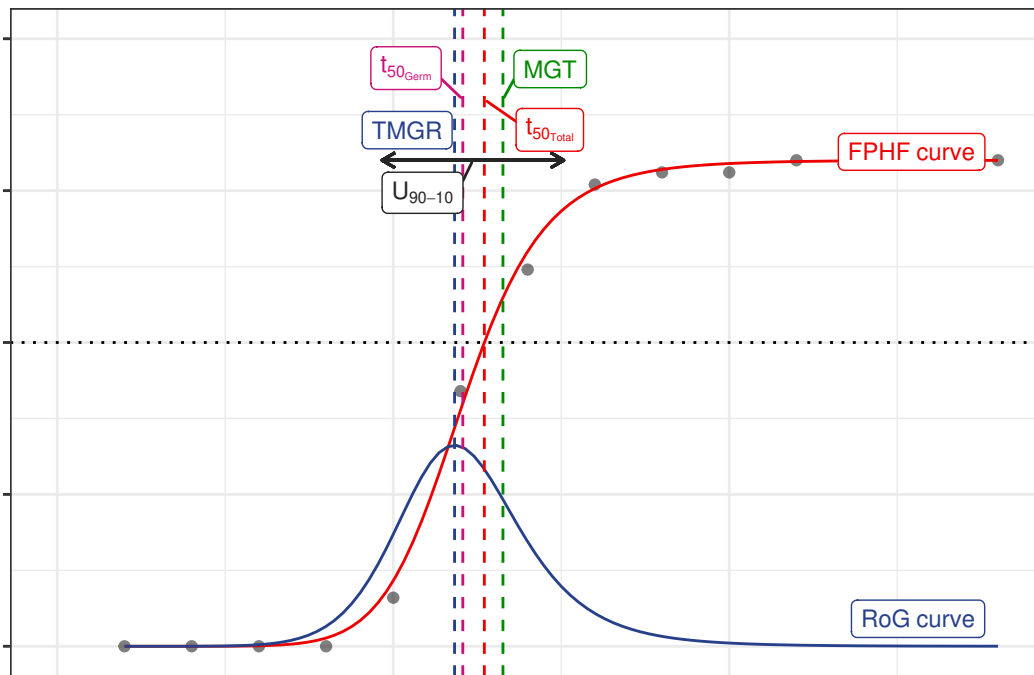


```
# No labels
plot(fit1, plotlabels = FALSE)
```
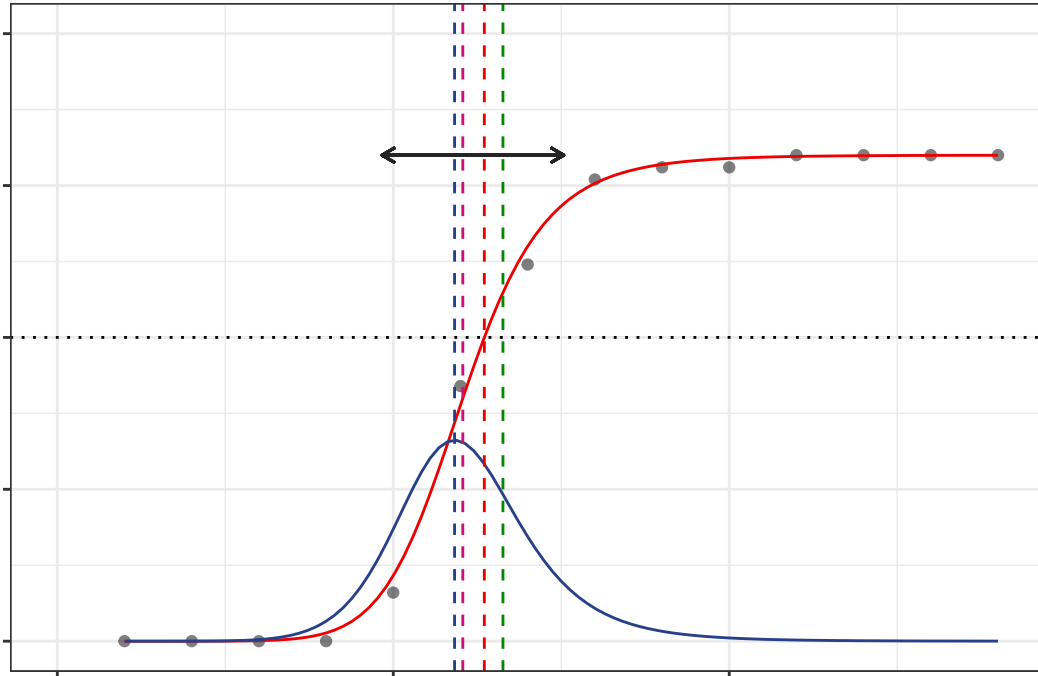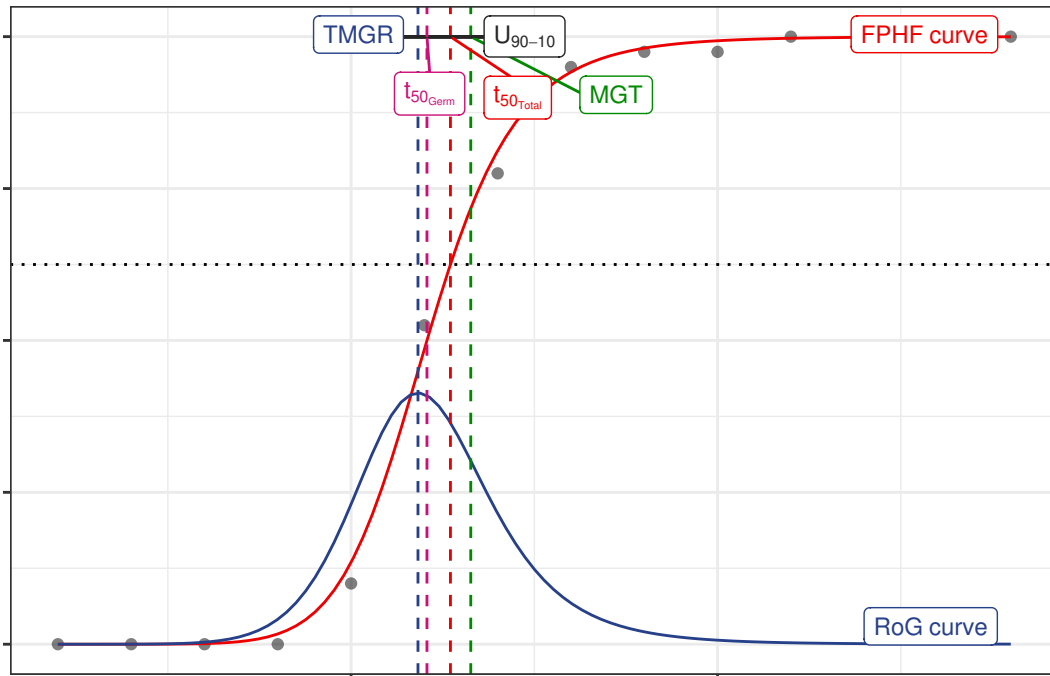
```
plot(fit2, plotlabels = FALSE)
```
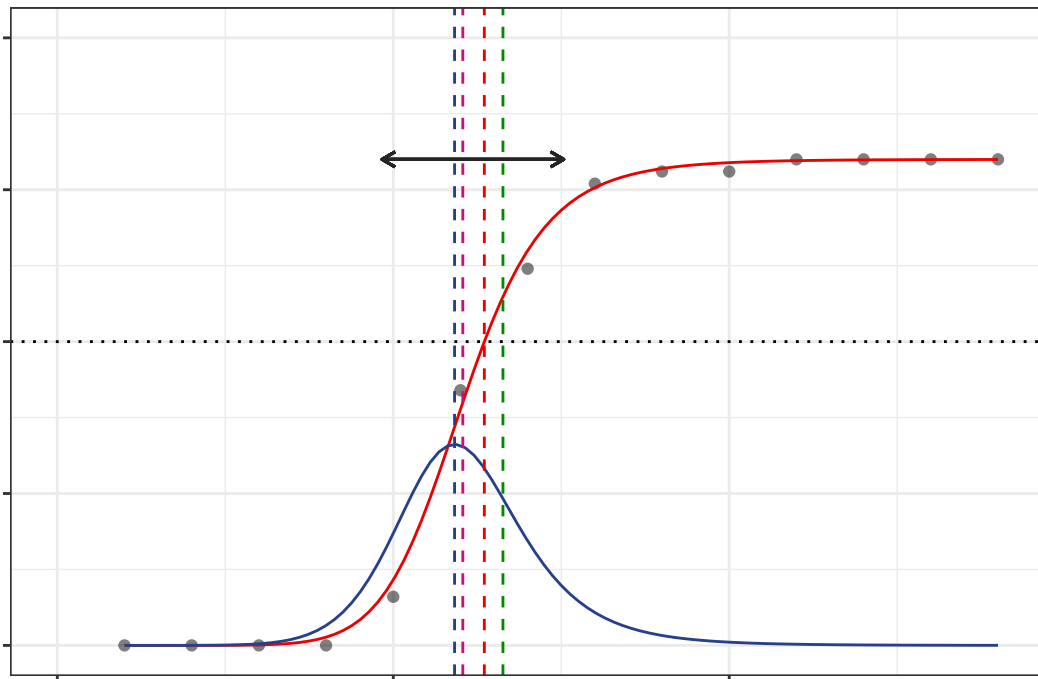


```
# Only the FPHF curve
plot(fit1, rog = FALSE, t50.total = FALSE, t50.germ = FALSE,
     tmgr = FALSE, mgt = FALSE, uniformity = FALSE)
```
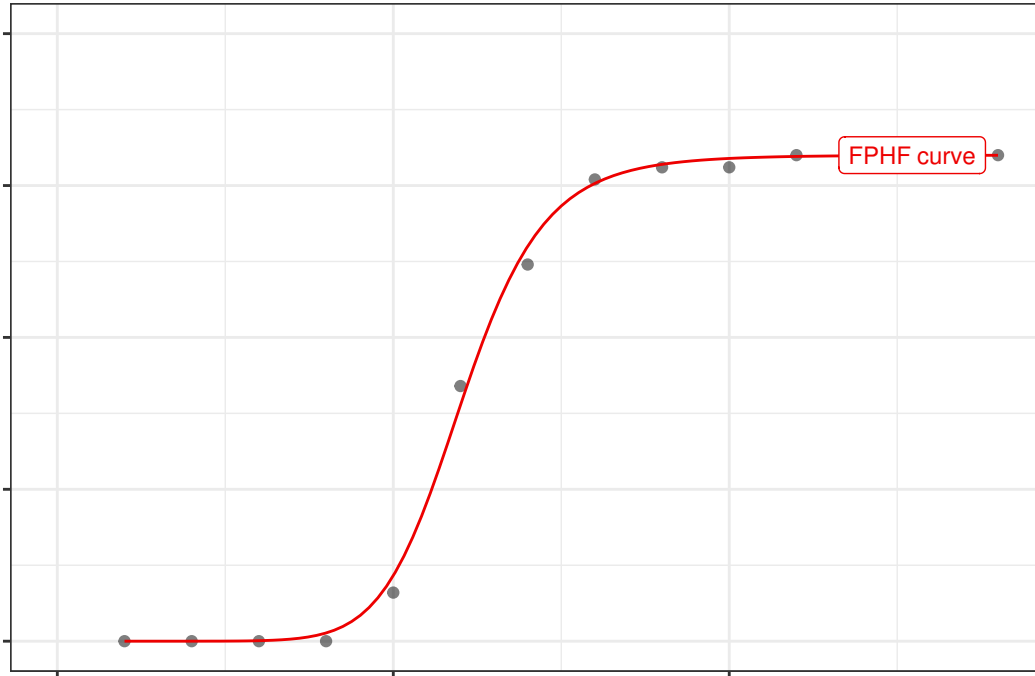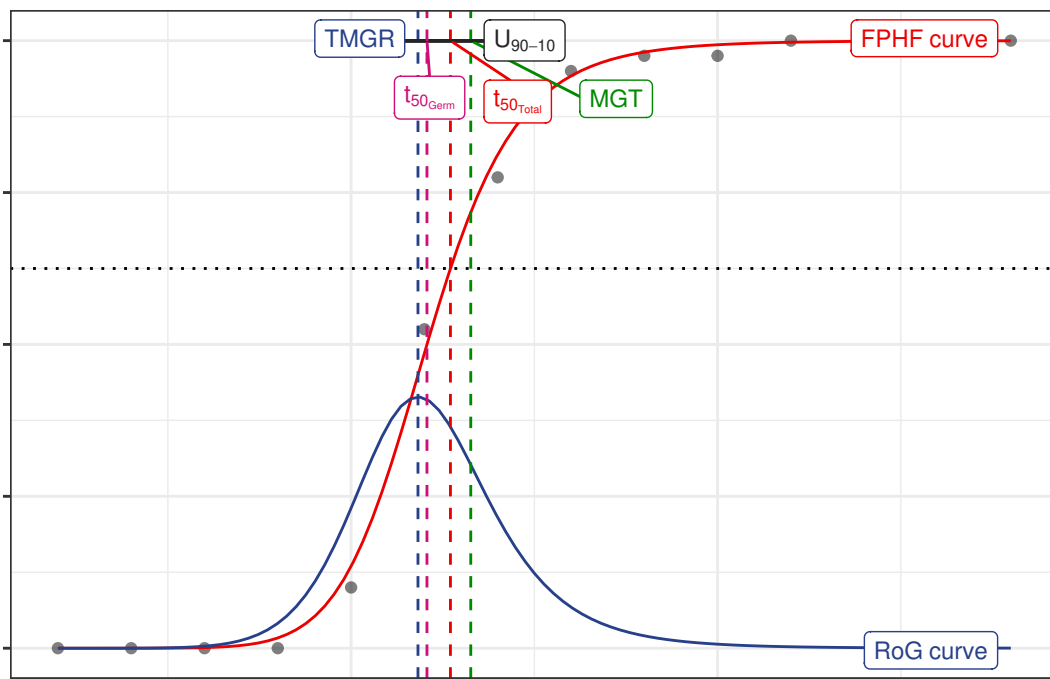
```
plot(fit2, rog = FALSE, t50.total = FALSE, t50.germ = FALSE,
     tmgr = FALSE, mgt = FALSE, uniformity = FALSE)
```
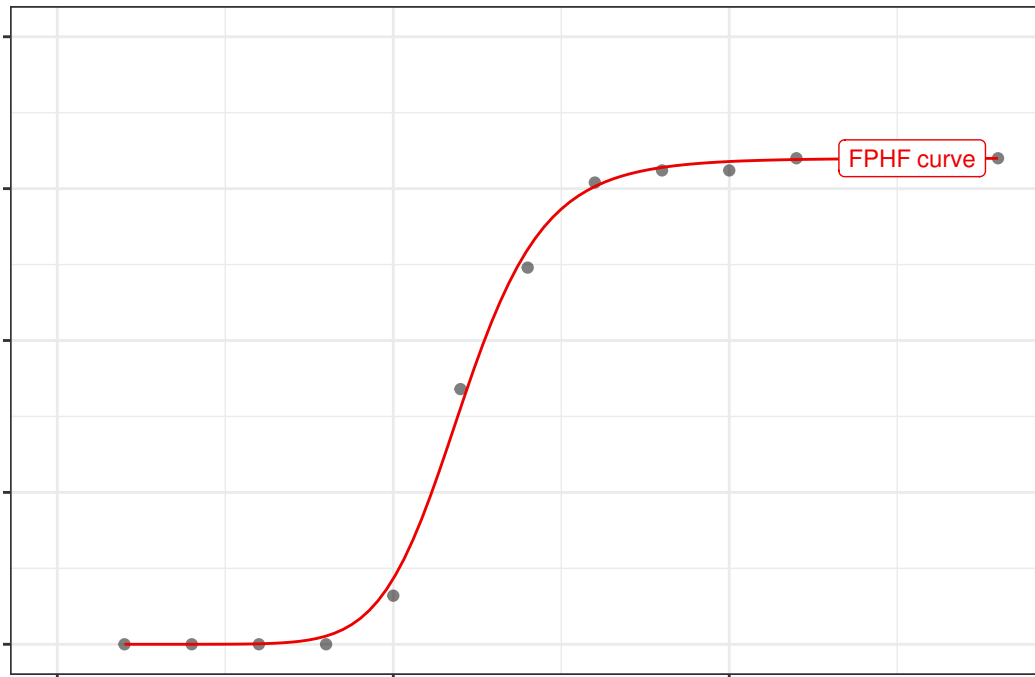


```
# Without y axis limits adjustment
plot(fit1, limits = FALSE)
```

```
plot(fit2, limits = FALSE)
```


Wrapper functions

Wrapper functions `germination.indices()` and `FourPHFfit.bulk()` are available in the package for computing results for multiple samples in batch from a data frame of germination counts recorded at specific time intervals.

`germination.indices()` This wrapper function can be used to compute several germination indices simultaneously for multiple samples in batch.

```
data(gcdata)

counts.per.intervals <- c("Day01", "Day02", "Day03", "Day04", "Day05",
                          "Day06", "Day07", "Day08", "Day09", "Day10",
                          "Day11", "Day12", "Day13", "Day14")
germination.indices(gcdata, total.seeds.col = "Total Seeds",
                    counts.intervals.cols = counts.per.intervals,
                    intervals = 1:14, partial = TRUE, max.int = 5)
```

	Genotype	Rep	Day01	Day02	Day03	Day04	Day05	Day06	Day07	Day08	Day09	Day10
1	G1	1	0	0	0	0	4	17	10	7	1	0
2	G2	1	0	0	0	1	3	15	13	6	2	1
3	G3	1	0	0	0	2	3	18	9	8	2	1
4	G4	1	0	0	0	0	4	19	12	6	2	1
5	G5	1	0	0	0	0	5	20	12	8	1	0
6	G1	2	0	0	0	0	3	21	11	7	1	1
7	G2	2	0	0	0	0	4	18	11	7	1	0
8	G3	2	0	0	0	1	3	14	12	6	2	1
9	G4	2	0	0	0	1	3	19	10	8	1	1
10	G5	2	0	0	0	0	4	18	13	6	2	1
11	G1	3	0	0	0	0	5	21	11	8	1	0
12	G2	3	0	0	0	0	3	20	10	7	1	1
13	G3	3	0	0	0	0	4	19	12	8	1	1
14	G4	3	0	0	0	0	3	21	11	6	1	0
15	G5	3	0	0	0	0	4	17	10	8	1	1

	Day11	Day12	Day13	Day14	Total Seeds	GermPercent	PeakGermPercent
1	1	0	0	0	50	80.00000	34.00000
2	0	1	0	0	51	82.35294	29.41176
3	1	1	0	0	48	93.75000	37.50000
4	1	1	0	0	51	90.19608	37.25490
5	0	1	1	0	50	96.00000	40.00000
6	1	1	0	0	49	93.87755	42.85714
7	1	0	0	0	48	87.50000	37.50000
8	0	1	0	0	47	85.10638	29.78723
9	1	1	0	0	52	86.53846	36.53846
10	0	1	0	0	50	90.00000	36.00000
11	0	1	1	0	51	94.11765	41.17647
12	1	1	0	0	51	86.27451	39.21569
13	0	1	1	0	49	95.91837	38.77551
14	1	1	0	0	48	91.66667	43.75000
15	1	0	0	0	48	87.50000	35.41667

	FirstGermTime	LastGermTime	PeakGermTime	TimeSpreadGerm	t50_Coolbear
1	5	11	6	6	5.970588
2	4	12	6	8	6.192308
3	4	12	6	8	6.000000
4	5	12	6	7	6.041667
5	5	13	6	8	5.975000
6	5	12	6	7	5.976190
7	5	11	6	6	5.972222
8	4	12	6	8	6.208333
9	4	12	6	8	6.000000
10	5	12	6	7	6.076923
11	5	13	6	8	5.928571
12	5	12	6	7	5.975000

```
13           5          13           6           8   6.083333
14           5          12           6           7   5.928571
15           5          11           6           6   6.050000
   t50_Farooq MeanGermTime VarGermTime SEGermTime CVGermTime MeanGermRate
1    5.941176     6.700000    1.446154  0.1901416  0.1794868    0.1492537
2    6.153846     6.857143    2.027875  0.2197333  0.2076717    0.1458333
3    5.972222     6.866667    2.572727  0.2391061  0.2335882    0.1456311
4    6.000000     6.891304    2.187923  0.2180907  0.2146419    0.1451104
5    5.950000     6.812500    2.368351  0.2221275  0.2259002    0.1467890
6    5.952381     6.869565    2.071498  0.2122088  0.2095140    0.1455696
7    5.944444     6.690476    1.389663  0.1818989  0.1761967    0.1494662
8    6.166667     6.875000    2.112179  0.2297923  0.2113940    0.1454545
9    5.973684     6.866667    2.300000  0.2260777  0.2208604    0.1456311
10   6.038462     6.822222    1.831313  0.2017321  0.1983606    0.1465798
11   5.904762     6.791667    2.381206  0.2227295  0.2272072    0.1472393
12   5.950000     6.886364    2.149577  0.2210295  0.2129053    0.1452145
13   6.041667     6.936170    2.539315  0.2324392  0.2297410    0.1441718
14   5.904762     6.772727    1.900634  0.2078370  0.2035568    0.1476510
15   6.000000     6.809524    1.670151  0.1994129  0.1897847    0.1468531
    VarGermRate  SEGermRate      CVG GermRateRecip_Coolbear
1  0.0007176543 0.004235724 14.92537               0.1674877
2  0.0009172090 0.004673148 14.58333               0.1614907
3  0.0011572039 0.005071059 14.56311               0.1666667
4  0.0009701218 0.004592342 14.51104               0.1655172
5  0.0010995627 0.004786184 14.67890               0.1673640
6  0.0009301809 0.004496813 14.55696               0.1673307
7  0.0006935558 0.004063648 14.94662               0.1674419
8  0.0009454531 0.004861721 14.54545               0.1610738
9  0.0010345321 0.004794747 14.56311               0.1666667
10 0.0008453940 0.004334343 14.65798               0.1645570
11 0.0011191581 0.004828643 14.72393               0.1686747
12 0.0009558577 0.004660905 14.52145               0.1673640
13 0.0010970785 0.004831366 14.41718               0.1643836
14 0.0009033254 0.004531018 14.76510               0.1686747
15 0.0007767634 0.004300508 14.68531               0.1652893
   GermRateRecip_Farooq GermSpeed_Count GermSpeed_Percent
1             0.1683168        6.138925          12.27785
2             0.1625000        6.362698          12.47588
3             0.1674419        6.882179          14.33787
4             0.1666667        6.927417          13.58317
5             0.1680672        7.318987          14.63797
6             0.1680000        6.931782          14.14649
7             0.1682243        6.448449          13.43427
8             0.1621622        6.053175          12.87909
9             0.1674009        6.830592          13.13575
10            0.1656051        6.812698          13.62540
11            0.1693548        7.342796          14.39764
12            0.1680672        6.622258          12.98482
13            0.1655172        7.052320          14.39249
14            0.1693548        6.706782          13.97246
15            0.1666667        6.363925          13.25818
   GermSpeedAccumulated_Count GermSpeedAccumulated_Percent
1                    34.61567                     69.23134
2                    35.54058                     69.68741
```

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```
3                       38.29725                        79.78594
4                       38.68453                        75.85202
5                       41.00786                        82.01571
6                       38.77620                        79.13509
7                       36.38546                        75.80304
8                       33.77079                        71.85275
9                       38.11511                        73.29829
10                      38.19527                        76.39054
11                      41.17452                        80.73436
12                      37.00640                        72.56158
13                      39.29399                        80.19182
14                      37.69490                        78.53103
15                      35.69697                        74.36868
   GermSpeedCorrected_Normal GermSpeedCorrected_Accumulated WeightGermPercent
1                  0.1534731                      0.8653917          47.42857
2                  0.1514928                      0.8462043          47.89916
3                  0.1529373                      0.8510501          54.46429
4                  0.1505960                      0.8409680          52.24090
5                  0.1524789                      0.8543303          56.14286
6                  0.1506909                      0.8429608          54.51895
7                  0.1535345                      0.8663205          51.93452
8                  0.1513294                      0.8442698          49.39210
9                  0.1517909                      0.8470024          50.27473
10                 0.1513933                      0.8487837          52.57143
11                 0.1529749                      0.8578026          55.18207
12                 0.1505059                      0.8410547          50.00000
13                 0.1500494                      0.8360424          55.24781
14                 0.1524269                      0.8567022          53.86905
15                 0.1515220                      0.8499278          51.19048
   MeanGermPercent MeanGermNumber TimsonsIndex TimsonsIndex_Labouriau
1         5.714286       2.857143     8.000000                   1.00
2         5.882353       3.000000     9.803922                   1.25
3         6.696429       3.214286    14.583333                   1.40
4         6.442577       3.285714     7.843137                   1.00
5         6.857143       3.428571    10.000000                   1.00
6         6.705539       3.285714     6.122449                   1.00
7         6.250000       3.000000     8.333333                   1.00
8         6.079027       2.857143    10.638298                   1.25
9         6.181319       3.214286     9.615385                   1.25
10        6.428571       3.214286     8.000000                   1.00
11        6.722689       3.428571     9.803922                   1.00
12        6.162465       3.142857     5.882353                   1.00
13        6.851312       3.357143     8.163265                   1.00
14        6.547619       3.142857     6.250000                   1.00
15        6.250000       3.000000     8.333333                   1.00
   TimsonsIndex_KhanUngar GermRateGeorge GermIndex GermIndex_mod
1               0.5714286              4  5.840000      7.300000
2               0.7002801              5  5.882353      7.142857
3               1.0416667              7  6.687500      7.133333
4               0.5602241              4  6.411765      7.108696
5               0.7142857              5  6.900000      7.187500
6               0.4373178              3  6.693878      7.130435
7               0.5952381              4  6.395833      7.309524
8               0.7598784              5  6.063830      7.125000
```

```
9             0.6868132          5  6.173077    7.133333
10            0.5714286          4  6.460000    7.177778
11            0.7002801          5  6.784314    7.208333
12            0.4201681          3  6.137255    7.113636
13            0.5830904          4  6.775510    7.063830
14            0.4464286          3  6.625000    7.227273
15            0.5952381          4  6.291667    7.190476
   EmergenceRateIndex_SG EmergenceRateIndex_SG_mod
1                    292                   7.300000
2                    300                   7.142857
3                    321                   7.133333
4                    327                   7.108696
5                    345                   7.187500
6                    328                   7.130435
7                    307                   7.309524
8                    285                   7.125000
9                    321                   7.133333
10                   323                   7.177778
11                   346                   7.208333
12                   313                   7.113636
13                   332                   7.063830
14                   318                   7.227273
15                   302                   7.190476
   EmergenceRateIndex_BilbroWanjura EmergenceRateIndex_Fakorede PeakValue
1                          5.970149                    8.375000  9.500000
2                          6.125000                    8.326531  9.313725
3                          6.553398                    7.324444 10.416667
4                          6.675079                    7.640359 10.049020
5                          7.045872                    7.096354 11.250000
6                          6.696203                    7.317580 10.714286
7                          6.277580                    7.646259 10.416667
8                          5.818182                    8.078125  9.574468
9                          6.553398                    7.934815  9.855769
10                         6.596091                    7.580247 10.250000
11                         7.067485                    7.216146 11.029412
12                         6.389439                    7.981921  9.803922
13                         6.776074                    7.231326 10.969388
14                         6.496644                    7.388430 10.677083
15                         6.167832                    7.782313 10.156250
   GermValue_Czabator GermValue_DP GermValue_Czabator_mod GermValue_DP_mod
1            54.28571     57.93890               54.28571         39.56076
2            54.78662     52.58713               54.78662         40.99260
3            69.75446     68.62289               69.75446         53.42809
4            64.74158     70.43331               64.74158         48.86825
5            77.14286     80.16914               77.14286         56.23935
6            71.84506     76.51983               71.84506         53.06435
7            65.10417     69.41325               65.10417         47.37690
8            58.20345     56.00669               58.20345         43.67948
9            60.92165     58.13477               60.92165         45.30801
10           65.89286     70.91875               65.89286         49.10820
11           74.14731     77.39782               74.14731         54.27520
12           60.41632     64.44988               60.41632         44.71582
13           75.15470     78.16335               75.15470         54.94192
14           69.90947     74.40140               69.90947         51.41913
```

```
15              63.47656     67.62031                63.47656          46.48043
       CUGerm GermSynchrony GermUncertainty
1  0.7092199     0.2666667        2.062987
2  0.5051546     0.2346109        2.321514
3  0.3975265     0.2242424        2.462012
4  0.4672113     0.2502415        2.279215
5  0.4312184     0.2606383        2.146051
6  0.4934701     0.2792271        2.160545
7  0.7371500     0.2729384        2.040796
8  0.4855842     0.2256410        2.357249
9  0.4446640     0.2494949        2.321080
10 0.5584666     0.2555556        2.187983
11 0.4288905     0.2686170        2.128670
12 0.4760266     0.2737844        2.185245
13 0.4023679     0.2506938        2.241181
14 0.5383760     0.2991543        2.037680
15 0.6133519     0.2497096        2.185028
```

FourPHFfit.bulk()   This wrapper function can be used to fit the four-parameter hill function for multiple samples in batch.

```
data(gcdata)

counts.per.intervals <- c("Day01", "Day02", "Day03", "Day04", "Day05",
                          "Day06", "Day07", "Day08", "Day09", "Day10",
                          "Day11", "Day12", "Day13", "Day14")

FourPHFfit.bulk(gcdata, total.seeds.col = "Total Seeds",
                counts.intervals.cols = counts.per.intervals,
                intervals = 1:14, partial = TRUE,
                fix.y0 = TRUE, fix.a = TRUE, xp = c(10, 60),
                tmax = 20, tries = 3, umax = 90, umin = 10)
```

```
   Genotype Rep Day01 Day02 Day03 Day04 Day05 Day06 Day07 Day08 Day09 Day10
1        G1   1     0     0     0     0     4    17    10     7     1     0
2        G2   1     0     0     0     1     3    15    13     6     2     1
3        G3   1     0     0     0     2     3    18     9     8     2     1
4        G4   1     0     0     0     0     4    19    12     6     2     1
5        G5   1     0     0     0     0     5    20    12     8     1     0
6        G1   2     0     0     0     0     3    21    11     7     1     1
7        G2   2     0     0     0     0     4    18    11     7     1     0
8        G3   2     0     0     0     1     3    14    12     6     2     1
9        G4   2     0     0     0     1     3    19    10     8     1     1
10       G5   2     0     0     0     0     4    18    13     6     2     1
11       G1   3     0     0     0     0     5    21    11     8     1     0
12       G2   3     0     0     0     0     3    20    10     7     1     1
13       G3   3     0     0     0     0     4    19    12     8     1     1
14       G4   3     0     0     0     0     3    21    11     6     1     0
15       G5   3     0     0     0     0     4    17    10     8     1     1
   Day11 Day12 Day13 Day14 Total Seeds        a        b        c y0 lag
1      1     0     0     0          50 80.00000 9.881947 6.034954  0   0
2      0     1     0     0          51 82.35294 9.227667 6.175193  0   0
3      1     1     0     0          48 93.75000 7.793055 6.138110  0   0
4      1     1     0     0          51 90.19608 8.925668 6.125172  0   0
5      0     1     1     0          50 96.00000 9.419194 6.049641  0   0
```

```
6      1    1    0    0          49 93.87755  9.450187 6.097412  0    0
7      1    0    0    0          48 87.50000 10.172466 6.029851  0    0
8      0    1    0    0          47 85.10638  8.940702 6.189774  0    0
9      1    1    0    0          52 86.53846  8.617395 6.125121  0    0
10     0    1    0    0          50 90.00000  9.608849 6.109503  0    0
11     0    1    1    0          51 94.11765  9.400248 6.018759  0    0
12     1    1    0    0          51 86.27451  9.162558 6.108449  0    0
13     0    1    1    0          49 95.91837  8.995233 6.149011  0    0
14     1    1    0    0          48 91.66667 10.391898 6.015907  0    0
15     1    0    0    0          48 87.50000  9.136762 6.121580  0    0
      Dlag50 t50.total t50.Germinated     TMGR      AUC      MGT Skewness
1   6.034954  6.355122       6.034954 5.912195 1108.975 6.632252 1.098973
2   6.175193  6.473490       6.175193 6.031282 1128.559 6.784407 1.098655
3   6.138110  6.244190       6.138110 5.938179 1283.693 6.772742 1.103392
4   6.125172  6.276793       6.125172 5.972686 1239.887 6.739665 1.100323
5   6.049641  6.103433       6.049641 5.914289 1328.328 6.654980 1.100062
6   6.097412  6.182276       6.097412 5.961877 1294.463 6.702470 1.099232
7   6.029851  6.202812       6.029851 5.914057 1213.908 6.622417 1.098272
8   6.189774  6.439510       6.189774 6.036193 1164.346 6.804000 1.099232
9   6.125121  6.352172       6.125121 5.961631 1188.793 6.745241 1.101242
10  6.109503  6.253042       6.109503 5.978115 1240.227 6.711899 1.098600
11  6.018759  6.099434       6.018759 5.883558 1305.200 6.624247 1.100600
12  6.108449  6.326181       6.108449 5.964079 1188.021 6.718636 1.099892
13  6.149011  6.207500       6.149011 5.998270 1316.407 6.762272 1.099733
14  6.015907  6.122385       6.015907 5.905179 1273.386 6.604963 1.097916
15  6.121580  6.317392       6.121580 5.976088 1203.664 6.732267 1.099760
                                                             msg isConv
1  #1. Relative error in the sum of squares is at most `ftol'.   TRUE
2  #1. Relative error in the sum of squares is at most `ftol'.   TRUE
3  #1. Relative error in the sum of squares is at most `ftol'.   TRUE
4  #1. Relative error in the sum of squares is at most `ftol'.   TRUE
5  #1. Relative error in the sum of squares is at most `ftol'.   TRUE
6  #1. Relative error in the sum of squares is at most `ftol'.   TRUE
7  #1. Relative error in the sum of squares is at most `ftol'.   TRUE
8  #1. Relative error in the sum of squares is at most `ftol'.   TRUE
9  #1. Relative error in the sum of squares is at most `ftol'.   TRUE
10 #1. Relative error in the sum of squares is at most `ftol'.   TRUE
11 #1. Relative error in the sum of squares is at most `ftol'.   TRUE
12 #1. Relative error in the sum of squares is at most `ftol'.   TRUE
13 #1. Relative error in the sum of squares is at most `ftol'.   TRUE
14 #1. Relative error in the sum of squares is at most `ftol'.   TRUE
15 #1. Relative error in the sum of squares is at most `ftol'.   TRUE
   txp.total_10 txp.total_60 Uniformity_90 Uniformity_10 Uniformity
1      4.956266     6.744598      7.537688      4.831809   2.705880
2      4.983236     6.872603      7.835407      4.866755   2.968652
3      4.673022     6.608437      8.137340      4.630062   3.507277
4      4.850876     6.614967      7.834806      4.788598   3.046208
5      4.814126     6.386788      7.639025      4.790947   2.848078
6      4.868635     6.477594      7.693458      4.832474   2.860984
7      4.930423     6.510495      7.483642      4.858477   2.625165
8      4.940058     6.823299      7.914162      4.841106   3.073056
9      4.836659     6.733275      7.904040      4.746574   3.157466
10     4.920629     6.566505      7.679176      4.860681   2.818494
11     4.798630     6.391288      7.603603      4.764249   2.839354
```

```
12      4.893597      6.684521      7.763844      4.806015    2.957830
13      4.841310      6.509952      7.850339      4.816395    3.033943
14      4.915143      6.397486      7.432360      4.869401    2.562960
15      4.892505      6.667247      7.785804      4.813086    2.972718
```

Multiple fitted curves generated in batch can also be plotted.

```
data(gcdata)

counts.per.intervals <- c("Day01", "Day02", "Day03", "Day04", "Day05",
                          "Day06", "Day07", "Day08", "Day09", "Day10",
                          "Day11", "Day12", "Day13", "Day14")

fits <- FourPHFfit.bulk(gcdata, total.seeds.col = "Total Seeds",
                        counts.intervals.cols = counts.per.intervals,
                        intervals = 1:14, partial = TRUE,
                        fix.y0 = TRUE, fix.a = TRUE, xp = c(10, 60),
                        tmax = 20, tries = 3, umax = 90, umin = 10)

# Plot FPHF curves
plot(fits, group.col = "Genotype")
```
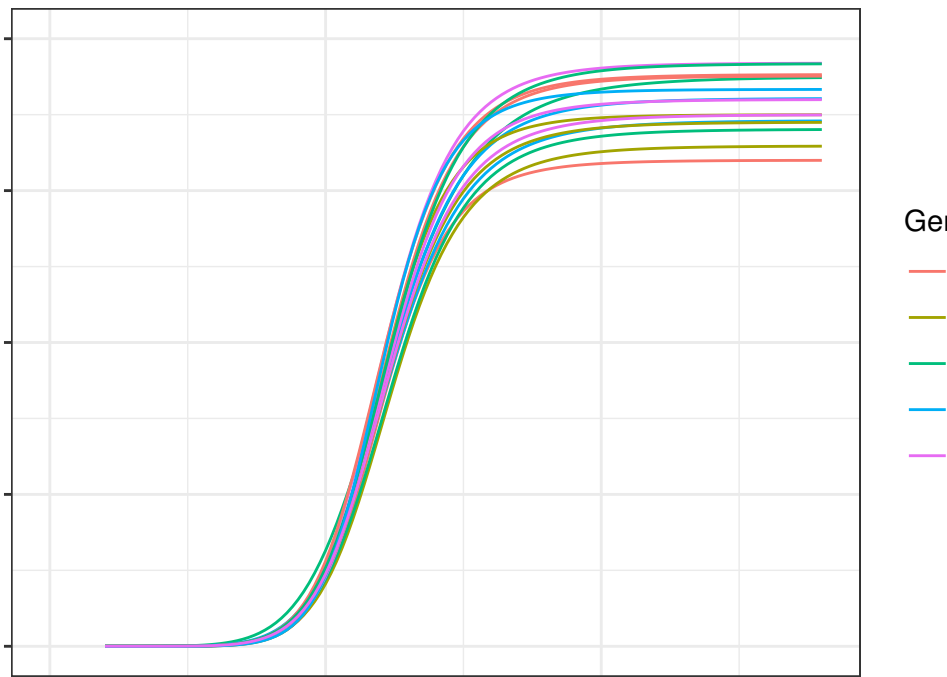


```
# Plot ROG curves
plot(fits, rog = TRUE, group.col = "Genotype")
```
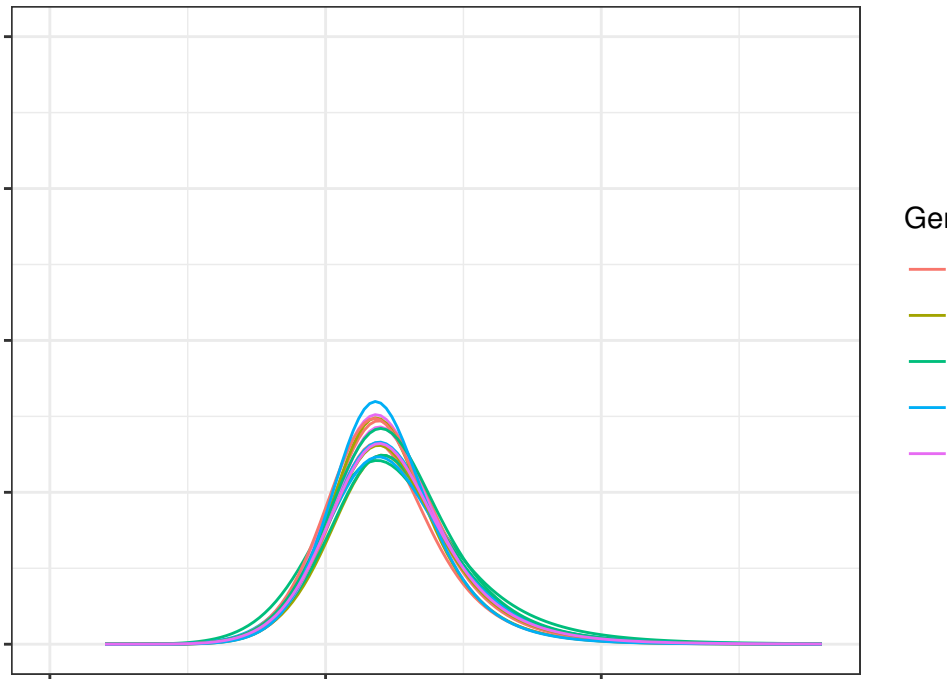
```r
# Plot FPHF curves with points
plot(fits, group.col = "Genotype", show.points = TRUE)
```
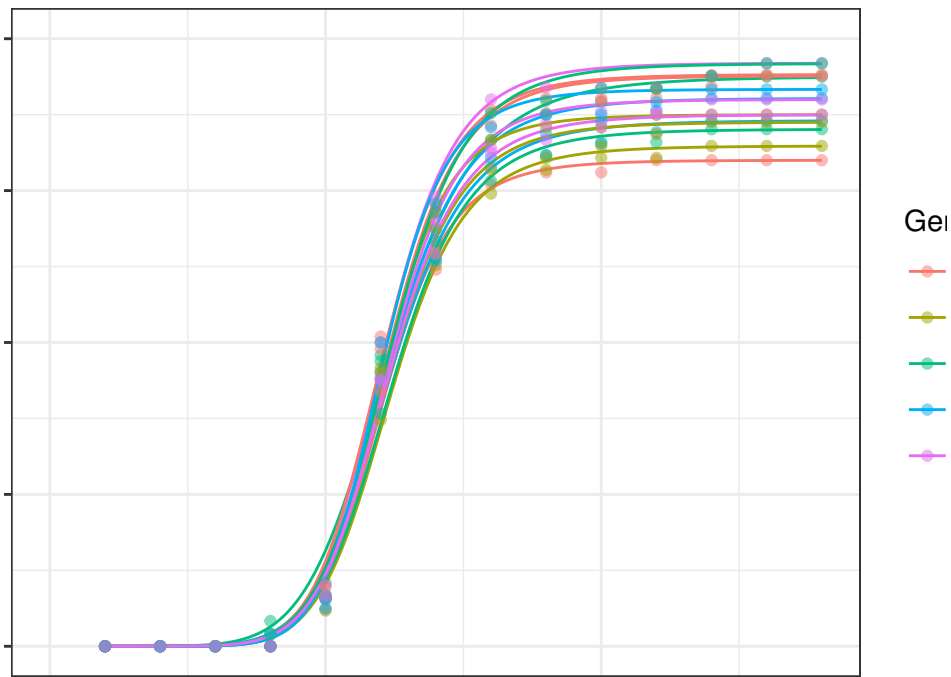


```r
# Plot FPHF curves with annotations
plot(fits, group.col = "Genotype", annotate = "t50.total")
```
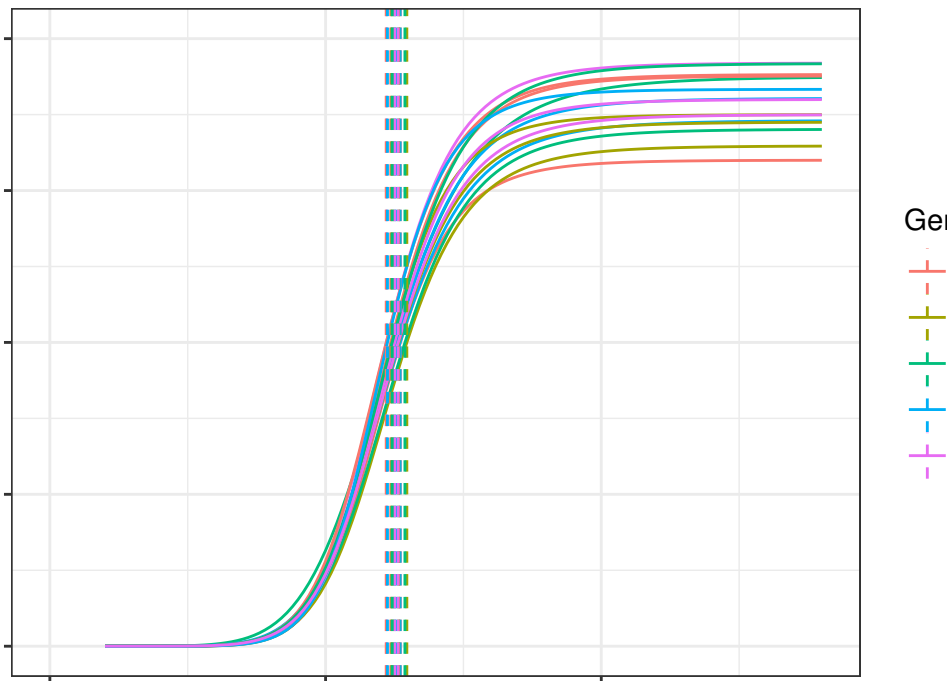
```
plot(fits, group.col = "Genotype", annotate = "t50.germ")
```
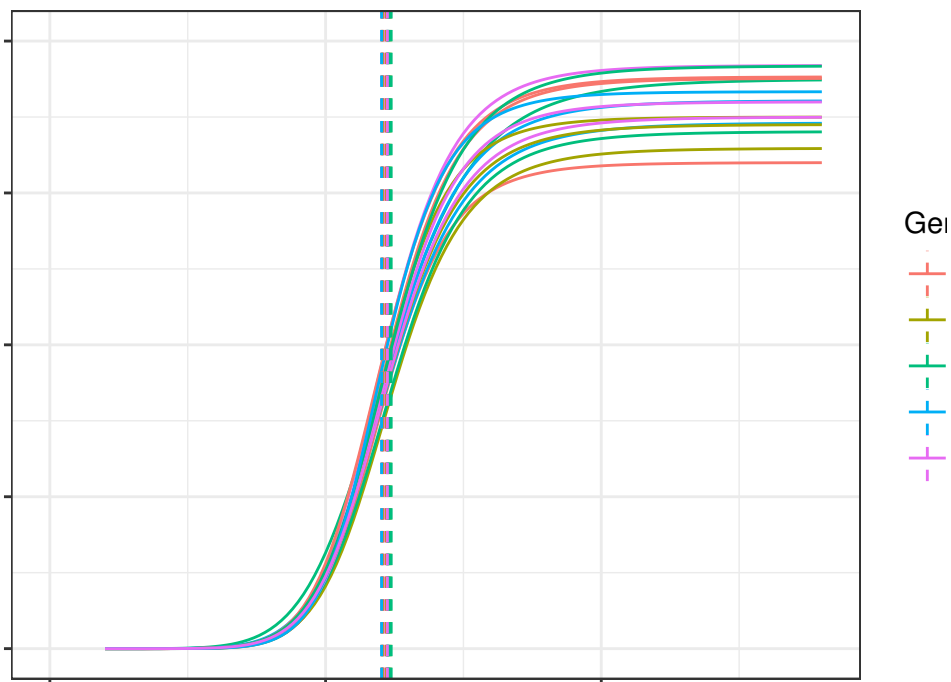


```
plot(fits, group.col = "Genotype", annotate = "tmgr")
```
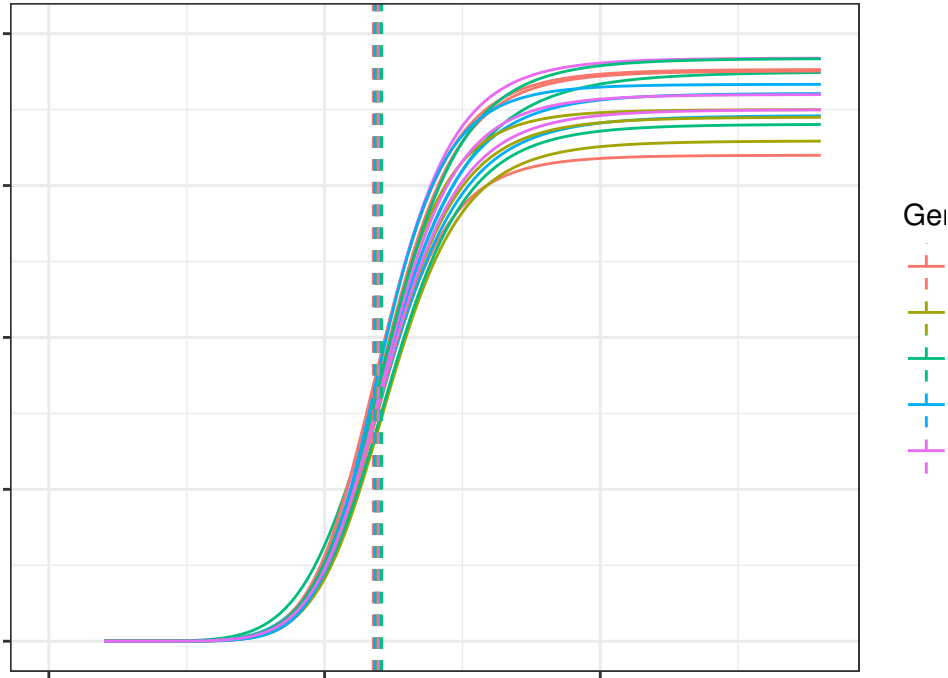
```
plot(fits, group.col = "Genotype", annotate = "mgt")
```
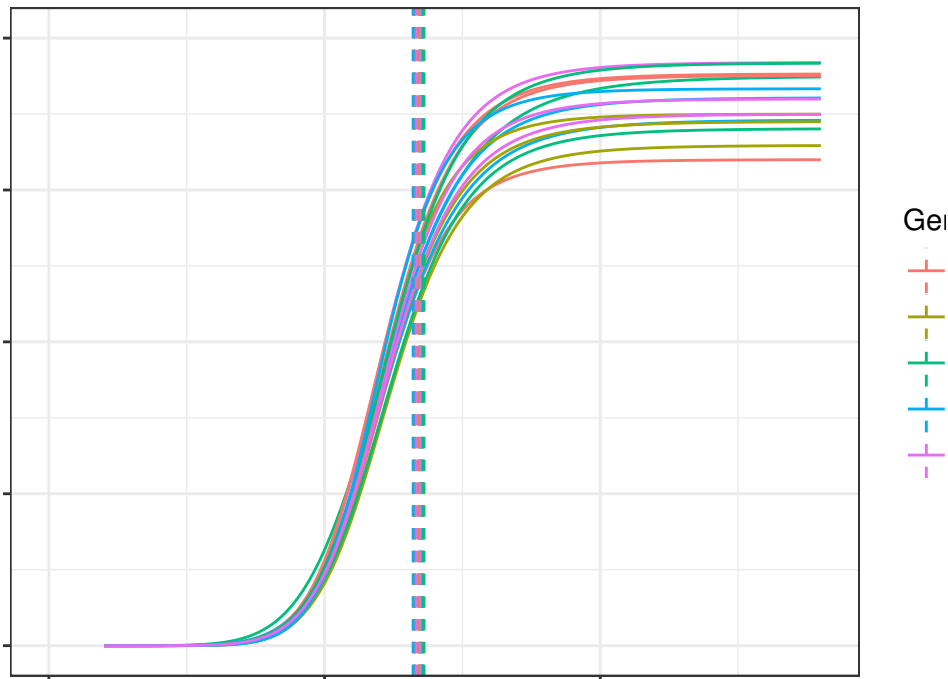


```
plot(fits, group.col = "Genotype", annotate = "uniformity")
```

```
Warning: position_dodge requires non-overlapping x intervals
position_dodge requires non-overlapping x intervals
```
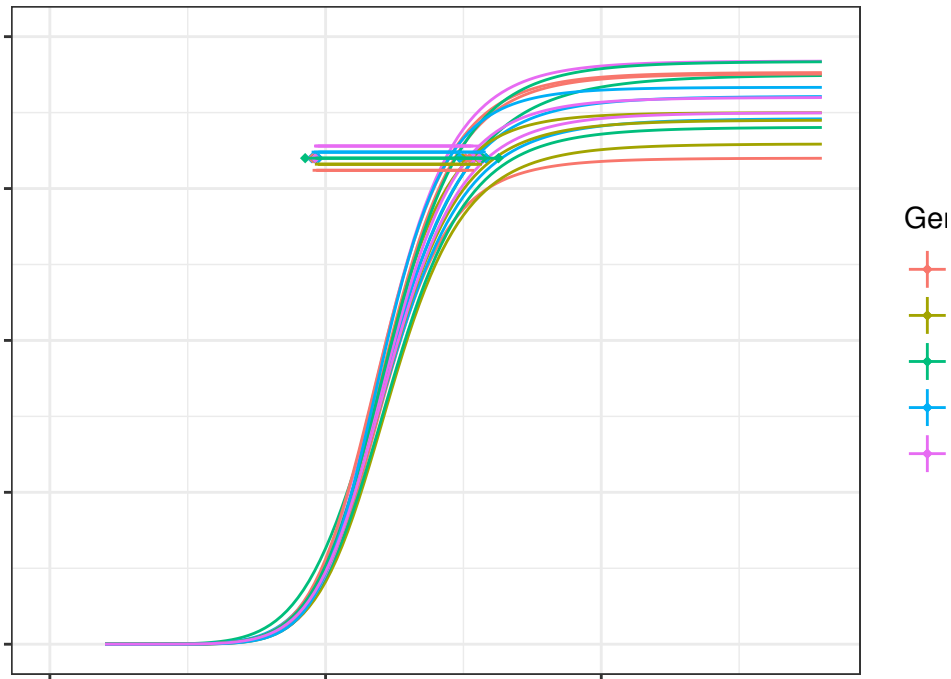
```
# Plot ROG curves with annotations
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "t50.total")
```
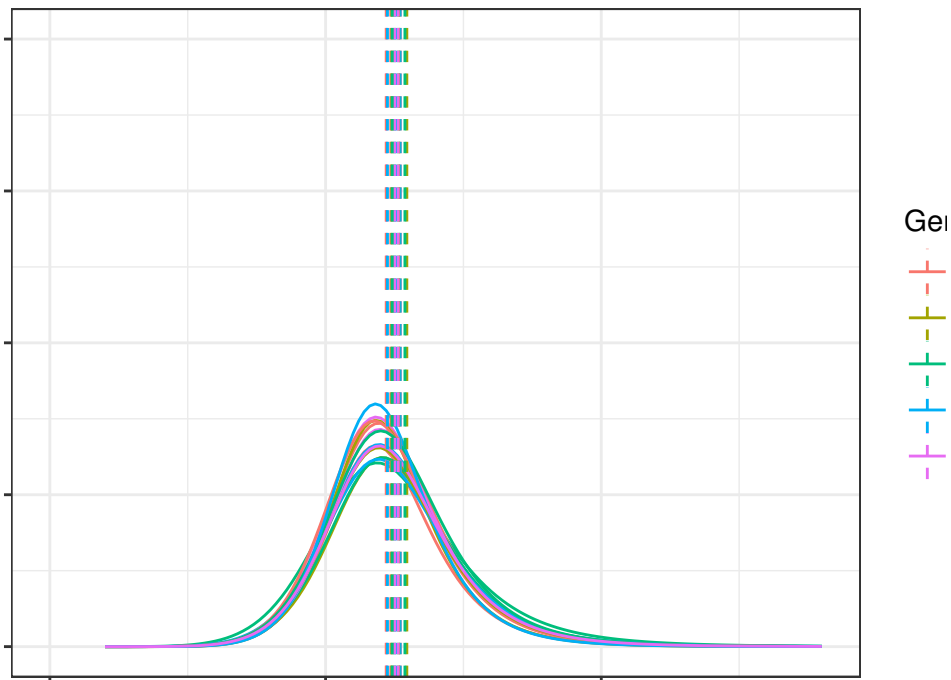


```
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "t50.germ")
```
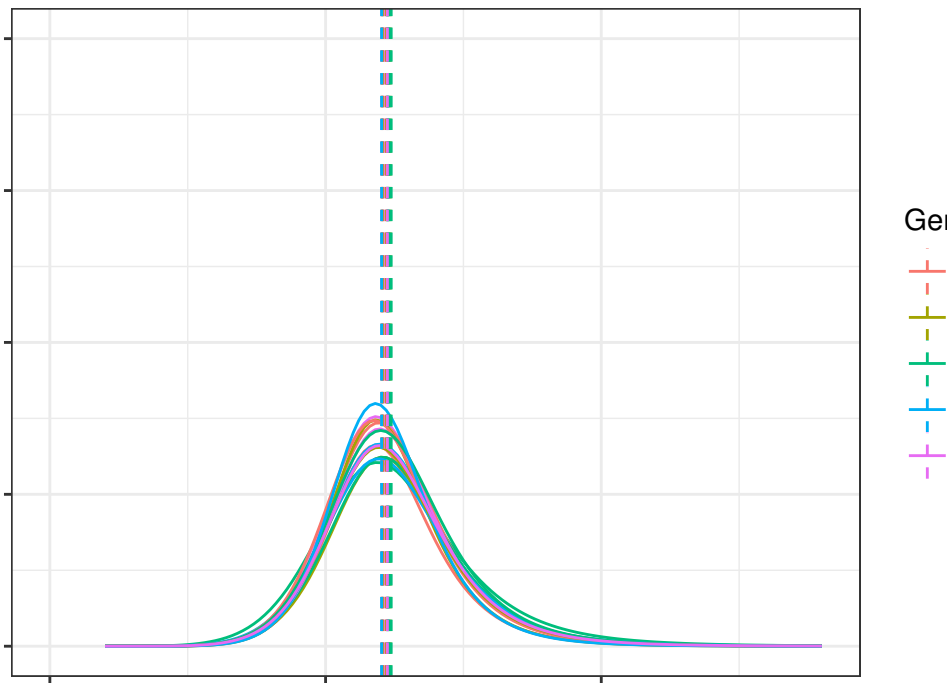
```
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "tmgr")
```
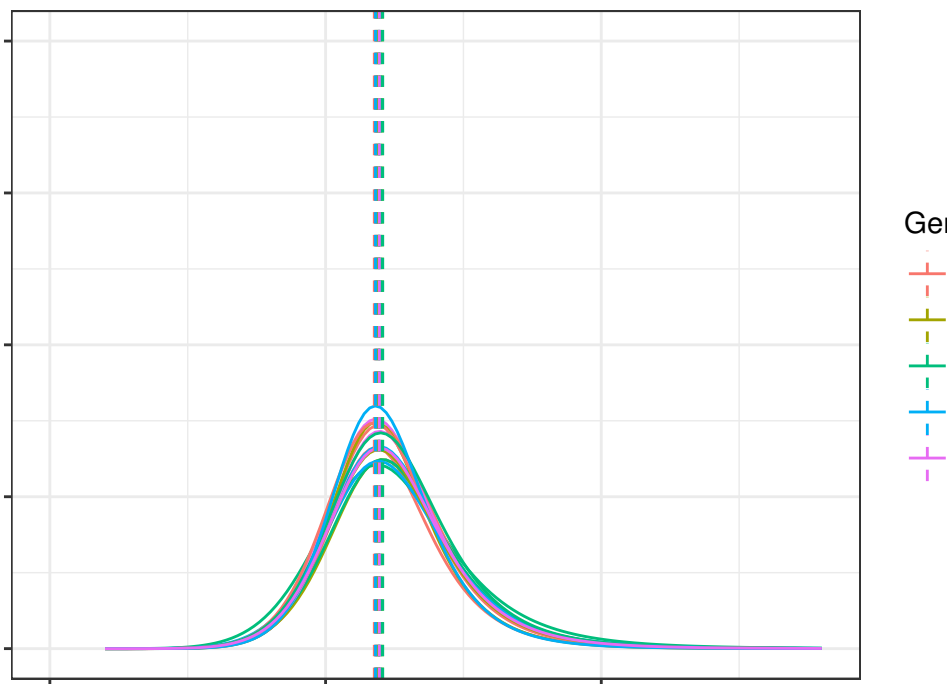


```
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "mgt")
```
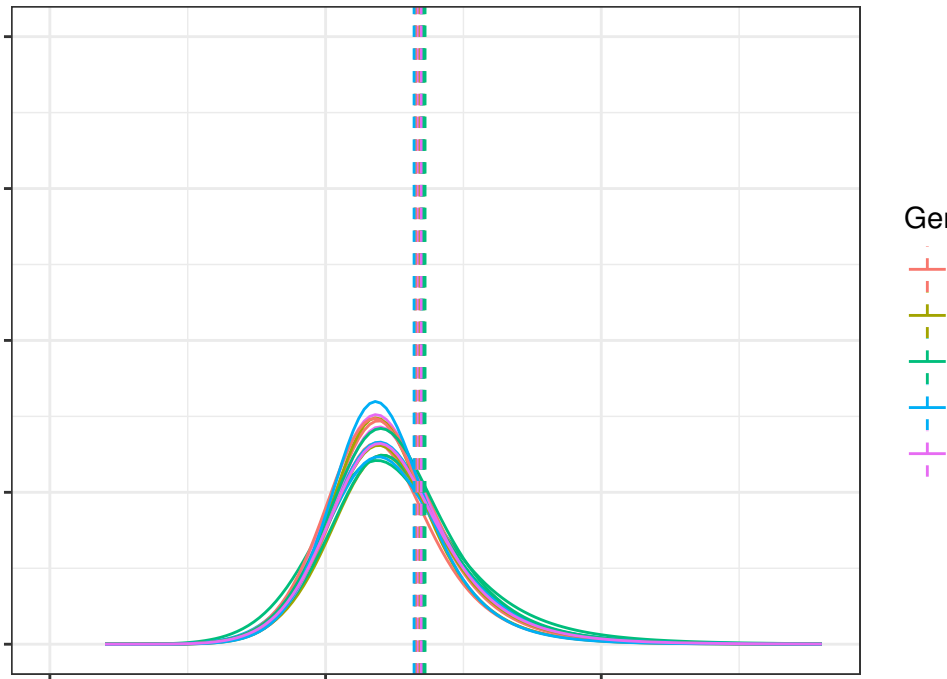
```
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "uniformity")
```

```
Warning: position_dodge requires non-overlapping x intervals
position_dodge requires non-overlapping x intervals
```
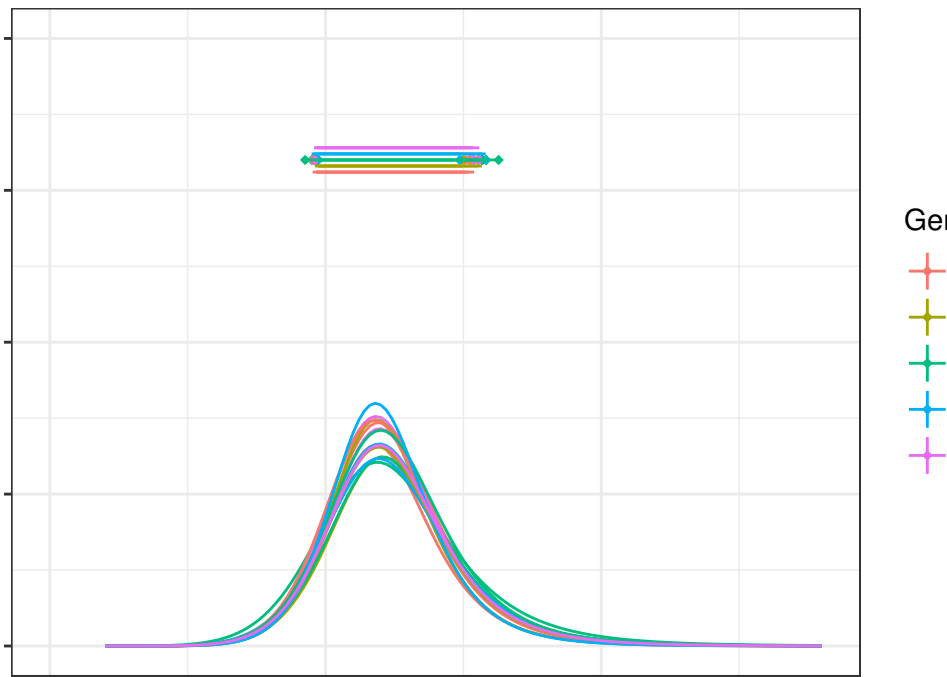


```
# Change colour of curves using ggplot2 options
library(ggplot2)
curvesplot <- plot(fits, group.col = "Genotype")

# 'Dark2' palette from RColorBrewer
curvesplot + scale_colour_brewer(palette = "Dark2")
```
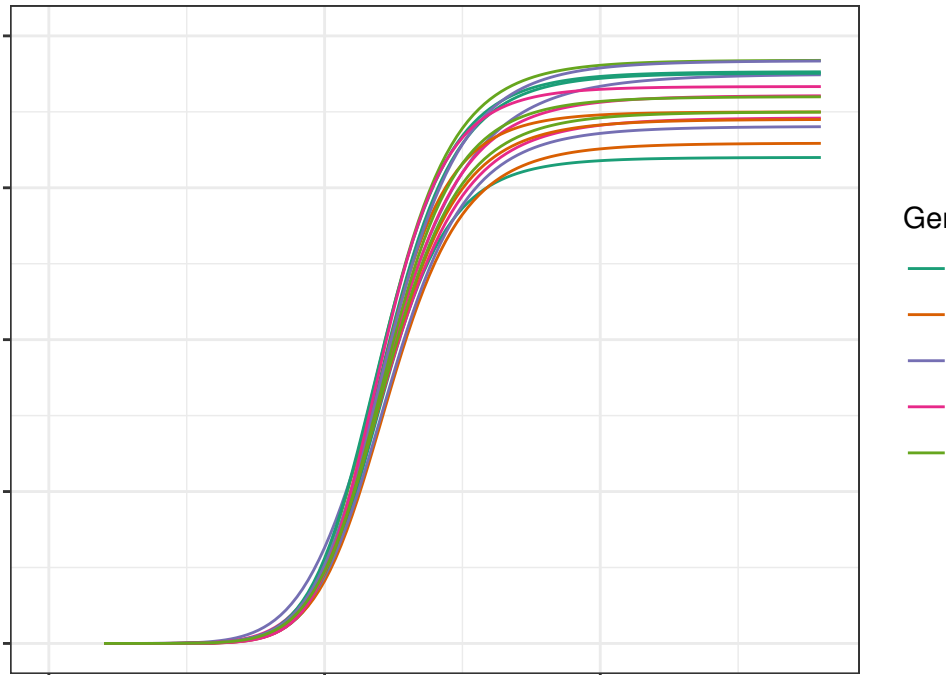
```
# Manual colours
curvesplot +
  scale_colour_manual(values = c("Coral", "Brown", "Blue",
                                 "Aquamarine", "Red"))
```
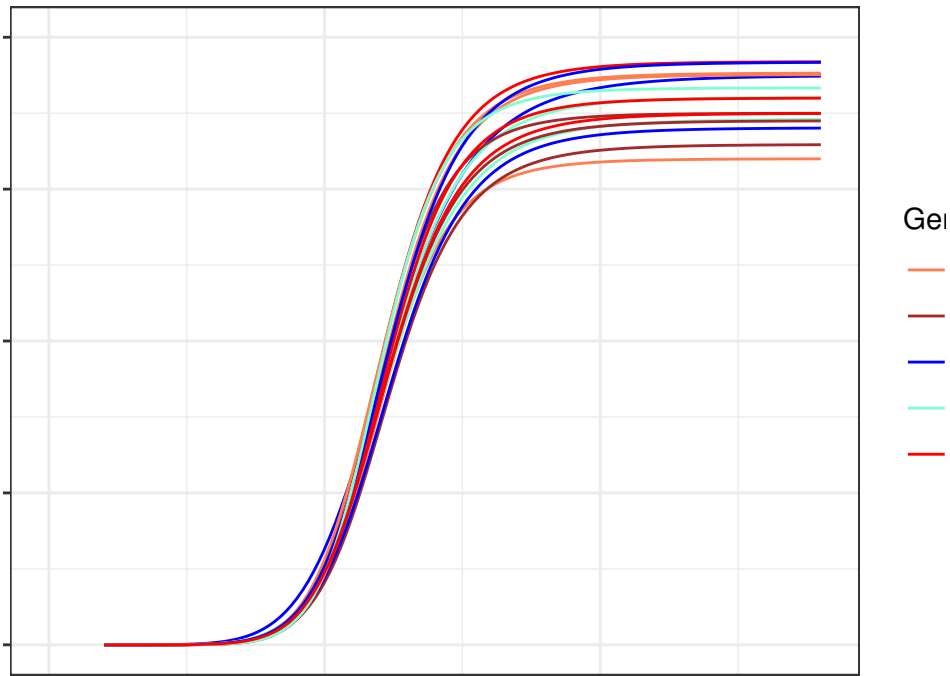

Citing germinationmetrics

To cite the R package 'germinationmetrics' in publications use:

Aravind, J., Vimala Devi, S., Radhamani, J., Jacob, S. R., and
Kalyani Srinivasan (2022). germinationmetrics: Seed Germination
Indices and Curve Fitting. R package version 0.1.7,
https://github.com/aravind-j/germinationmetricshttps://cran.r-project.org/package=germinationmetrics.

A BibTeX entry for LaTeX users is

```
@Manual{,
  title = {germinationmetrics: Seed Germination Indices and Curve Fitting},
  author = {J. Aravind and S. {Vimala Devi} and J. Radhamani and Sherry Rachel Jacob and {Kalyani Sri
  year = {2022},
  note = {R package version 0.1.7},
  note = {https://github.com/aravind-j/germinationmetrics},
  note = {https://cran.r-project.org/package=germinationmetrics},
}
```

This free and open-source software implements academic research by the
authors and co-workers. If you use it, please support the project by
citing the package.

Session Info

```
sessionInfo()
```

```
R Under development (unstable) (2022-08-18 r82725 ucrt)
Platform: x86_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 19044)

Matrix products: default

locale:
[1] LC_COLLATE=C                   LC_CTYPE=English_India.utf8
[3] LC_MONETARY=English_India.utf8 LC_NUMERIC=C
[5] LC_TIME=English_India.utf8

attached base packages:
[1] stats     graphics  grDevices utils     datasets  methods   base

other attached packages:
[1] germinationmetrics_0.1.7 ggplot2_3.3.6

loaded via a namespace (and not attached):
 [1] utf8_1.2.2         generics_0.1.3    tidyr_1.2.0       bitops_1.0-7
 [5] stringi_1.7.8      digest_0.6.29     magrittr_2.0.3    RColorBrewer_1.1-3
 [9] evaluate_0.16      grid_4.3.0        fastmap_1.1.0     plyr_1.8.7
[13] ggrepel_0.9.1      backports_1.4.1   DBI_1.1.3         httr_1.4.4
[17] pander_0.6.5       purrr_0.3.4       fansi_1.0.3       scales_1.2.1
[21] XML_3.99-0.10      Rdpack_2.4        cli_3.3.0         rlang_1.0.4
[25] rbibutils_2.2.9    munsell_0.5.0     withr_2.5.0       yaml_2.3.5
[29] tools_4.3.0        reshape2_1.4.4    minpack.lm_1.2-2  dplyr_1.0.9
[33] colorspace_2.0-3   mathjaxr_1.6-0    curl_4.3.2        broom_1.0.0
[37] assertthat_0.2.1   vctrs_0.4.1       R6_2.5.1          lifecycle_1.0.1
[41] stringr_1.4.1      pkgconfig_2.0.3   pillar_1.8.1      gtable_0.3.0
[45] data.table_1.14.2  glue_1.6.2        Rcpp_1.0.9        highr_0.9
```

```
[49] xfun_0.32        tibble_3.1.8      tidyselect_1.1.2   rstudioapi_0.14
[53] knitr_1.40       farver_2.1.1      htmltools_0.5.3    labeling_0.4.2
[57] rmarkdown_2.16   compiler_4.3.0    RCurl_1.98-1.8
```

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