# **Haplo Stats**

(version 1.3.1)

Statistical Methods for Haplotypes When Linkage Phase is Ambiguous

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### 1 Brief Description

Haplo Stats is a suite of S-PLUS/R routines for the analysis of indirectly measured haplotypes. The statistical methods assume that all subjects are unrelated and that haplotypes are ambiguous (due to unknown linkage phase of the genetic markers), while also allowing for missing alleles.

The primary functions in Haplo Stats are:

- haplo.em: for the estimation of haplotype frequencies and posterior probabilities of haplotype pairs for a subject, conditional on the observed marker data
- haplo.glm: glm's for the regression of a trait on haplotypes, with the option of including covariates and interactions
- haplo.score: score statistics to test associations between haplotypes and a variety of traits, including binary, ordinal, quantitative, and Poisson.

Some new features and updates are as follows:

- haplo.design is new function that creates a model matrix with desired haplotype effects
- seqhap is a new function that performs three tests for assocation of a binary trait over a set of bi-allelic loci
- haplo.score now allows additive, dominant, or recessive effects of haplotypes on a trait
- geno1to2 is a new function converting a genotype matrix from one-column (minor allele count) to two-columns per locus

# 2 Operating System and Installation

Haplo Stats version 1.3.1 is written for both S-PLUS (version 8.0.1) and R (version 2.4.1) for Unix. It has been placed on the Comprehensive R Archive Network (CRAN), and is made available on other systems through CRAN. Installation procedures for S-PLUS and R systems will vary; the Unix installations are explained in the *README.haplo.stats* text file, located at the top level of the *haplo.stats* directory. The procedures for running analyses are the same for S-PLUS and R, following instructions in this document.

# 3 Getting Started

After installing the Haplo Stats package, the routines are available by starting an S-PLUS or R session and loading the package. If *haplo.stats* is installed for global use, load the library as done below. If installed as a local library, specify its location in the *lib.loc* parameter as shown in comments(##).

#### > library(haplo.stats)

For users who are new to the S-PLUS or R environments, note the following basic concepts. In the following examples, a user enters the indented text following the prompt ">", and the output results follow. Later, when executing a function in the session, the general syntax will appear like 'myresult <- myfunction(x)' where the results of myfunction, operating on x, are saved in myresult. A user may view the contents of myresult, or make use of the contents in a calculation. The examples provided in this document provide enough tools for a typical haplotype analysis. More information can be found within the function help files, viewed here for haplo.em.

#### > help(haplo.em)

### 3.1 Example Data

The haplo.stats library contains an example data set, (hla.demo), with 11 loci from the HLA region on chromosome 6, with covariates, qualitative, and quantitative responses. Within /haplo.stats/data/hla.demo.tab the data is stored in tab-delimited format. Typically data stored in this format can be read in using read.table(). The hla.demo data is already available in S-PLUS. Below, we load the data in R using data() and view the names of the columns. Then to make the columns of hla.demo accessible without typing it each time, we attach it to the current session.

### > data(hla.demo)

### > names(hla.demo)

```
"resp"
                  "resp.cat"
                              "male"
                                           "age"
                                                       "DPB.a1"
                  "DPA.a1"
 [6] "DPB.a2"
                              "DPA.a2"
                                           "DMA.a1"
                                                       "DMA.a2"
[11] "DMB.a1"
                  "DMB.a2"
                              "TAP1.a1"
                                           "TAP1.a2"
                                                       "TAP2.a1"
                                           "DQA.a1"
[16] "TAP2.a2"
                  "DQB.a1"
                              "DQB.a2"
                                                       "DOA.a2"
[21] "DRB.a1"
                  "DRB.a2"
                              "B.a1"
                                           "B.a2"
                                                       "A.a1"
[26] "A.a2"
```

### > attach(hla.demo)

The column names of hla.demo are shown above. They are defined as follows:

- resp: quantitative antibody response to measles vaccination
- resp.cat: a factor with levels "low", "normal", "high", for categorical antibody response
- male: gender code with 1="male", 0="female"

• age: age (in months) at immunization

The remaining columns are genotypes for 11 HLA loci, with a prefix name (e.g., "DQB") and a suffix for each of two alleles (".a1" and ".a2"). The variables in *hla.demo* can be accessed by typing *hla.demo*\$ before their names, such as *hla.demo*\$resp. Alternatively, it is easier for these examples to attach *hla.demo*, (as shown above with attach()) so the variables can be accessed by simply typing their names.

### 3.2 Creating a Genotype Matrix

Many of the functions require a matrix of genotypes, denoted below as geno. This matrix is arranged such that each locus has a pair of adjacent columns of alleles, and the order of columns corresponds to the order of loci on a chromosome. If there are K loci, then the number of columns of geno is 2K. Rows represent the alleles for each subject. For example, if there are three loci, in the order A-B-C, then the 6 columns of geno would be arranged as A.a1, A.a2, B.a1, B.a2, C.a1, C.a2. For illustration, three of the loci in hla.demo will be used to demonstrate some of the functions. Create a separate data frame for 3 of the loci, and call this geno. Then create a vector of labels for the loci.

```
> geno <- hla.demo[, c(17, 18, 21:24)]
> label <- c("DQB", "DRB", "B")</pre>
```

The *hla.demo* data already had alleles in two columns for each locus. For many SNP datasets, the data is in a one column format, giving the count of the minor allele. To assist in converting this format to two columns, a function named *geno1to2* has been added to the package. See its help file for more details.

#### 3.3 Preview Missing Data: summaryGeno

Before performing a haplotype analysis, the user will want to assess missing genotype data to determine the completeness of the data. If many genotypes are missing, the functions may take a long time to compute results, or even run out of memory. For these reasons, the user may want to remove some of the subjects with a lot of missing data. This step can be guided by using the *summaryGeno* function, which checks for missing allele information and counts the number of potential haplotype pairs that are consistent with the observed data (see the Appendix for a description of this counting scheme).

The codes for missing alleles are defined by the parameter *miss.val*, a vector to define all possible missing value codes. Below, the result is saved in *geno.desc*, which is a data frame, so individual rows may be printed. Here we show the results for subjects 1-10, 80-85, and 135-140, some of which have missing alleles.

```
> geno.desc <- summaryGeno(geno, miss.val = c(0,
+ NA))
> print(geno.desc[c(1:10, 80:85, 135:140), ])
```

|     | loc | miss-0 | loc | miss-1 | loc | miss-2 | num_enum_rows |
|-----|-----|--------|-----|--------|-----|--------|---------------|
| 1   |     | 3      |     | 0      |     | 0      | 4             |
| 2   |     | 3      |     | 0      |     | 0      | 4             |
| 3   |     | 3      |     | 0      |     | 0      | 4             |
| 4   |     | 3      |     | 0      |     | 0      | 2             |
| 5   |     | 3      |     | 0      |     | 0      | 4             |
| 6   |     | 3      |     | 0      |     | 0      | 2             |
| 7   |     | 3      |     | 0      |     | 0      | 4             |
| 8   |     | 3      |     | 0      |     | 0      | 2             |
| 9   |     | 3      |     | 0      |     | 0      | 2             |
| 10  |     | 3      |     | 0      |     | 0      | 1             |
| 80  |     | 3      |     | 0      |     | 0      | 4             |
| 81  |     | 2      |     | 0      |     | 1      | 1800          |
| 82  |     | 3      |     | 0      |     | 0      | 2             |
| 83  |     | 3      |     | 0      |     | 0      | 1             |
| 84  |     | 3      |     | 0      |     | 0      | 2             |
| 85  |     | 3      |     | 0      |     | 0      | 4             |
| 135 |     | 3      |     | 0      |     | 0      | 4             |
| 136 |     | 3      |     | 0      |     | 0      | 2             |
| 137 |     | 1      |     | 0      |     | 2      | 129600        |
| 138 |     | 3      |     | 0      |     | 0      | 4             |
| 139 |     | 3      |     | 0      |     | 0      | 4             |
| 140 |     | 3      |     | 0      |     | 0      | 4             |

The columns with 'loc miss-' illustrate the number of loci missing either 0, 1, or 2 alleles, and the last column, num\_enum\_rows, illustrates the number of haplotype pairs that are consistent with the observed data. In the example above, subjects indexed by rows 81 and 137 have missing alleles. Subject #81 has one locus missing two alleles, while subject #137 has two loci missing two alleles. As indicated by num\_enum\_rows, subject #81 has 1,800 potential haplotype pairs, while subject #137 has nearly 130,000.

The 130,000 haplotype pairs is considered a large number, but haplo.em, haplo.score, and haplo.glm complete in roughly 3-6 minutes (depending on system limits or control parameter settings). If person #137 were removed, the methods would take less than half that time. It is preferred to keep people if they provide information to the analysis, given that run time and memory usage are not overwhelming.

When a person has no genotype information, they do not provide information to any of the methods in *haplo.stats*. Furthermore, they cause a much longer run time. Below, using the *table* function on the third column of *geno.desc* summarizes how many people are missing two alleles at any at of the three loci. If there were people missing two alleles at all three loci, they should be removed. The second command below shows how to make an index of which people to remove from *hla.demo* because they are missing all their alleles.

### 3.4 Random Numbers and Setting Seed

Random numbers are used in several of the functions (e.g., to determine random starting frequencies within haplo.em, and to compute permutation p-values in haplo.score). Random numbers can be controlled when trying to reproduce calculations involving random numbers. Random numbers in S-PLUS and R are controlled by the seed values stored in a vector called .Random.seed. This vector can be set using set.seed() before any function which uses random numbers (i.e., haplo.em, haplo.score, haplo.score.slide, haplo.glm, haplo.group, haplo.cc) to make results reproducible. Section 6.6.2 shows one example of setting the seed for haplo.glm. We illustrate setting the seed below.

```
> seed <- c(17, 53, 1, 40, 37, 0, 62, 56, 5, 52,
+ 12, 1)
> set.seed(seed)
```

# 4 Haplotype Frequency Estimation: haplo.em

### 4.1 Algorithm

For genetic markers measured on unrelated subjects, with linkage phase unknown, haplo.em computes maximum likelihood estimates of haplotype probabilities. Because there may be more than one pair of haplotypes that are consistent with the observed marker phenotypes, posterior probabilities of haplotype pairs for each subject are also computed. Unlike the usual EM which attempts to enumerate all possible haplotype pairs before iterating over the EM steps, our progressive insertion algorithm progressively inserts batches of loci into haplotypes of growing lengths, runs the EM steps, trims off pairs of haplotypes per subject when the posterior probability of the pair is below a specified threshold, and then continues these insertion, EM, and trimming steps until all loci are inserted into the haplotype. The user can choose the batch size. If the batch size is chosen to be all loci, and the threshold for trimming is set to 0, then this reduces to the usual EM algorithm. The basis of this progressive insertion algorithm is from the "snphap" software by David Clayton[4]. Although some of the features and control parameters of haplo.em are modeled after snphap, there are substantial differences, such as extension to allow for more than two alleles per locus, and some other nuances on how the algorithm is implemented.

### 4.2 Example Usage

Use haplo.em on geno for the 3 loci defined above, then view the results stored in save.em. In this example we show just a quick glance of the output by using the option nlines=10, which prints only the first 10 haplotypes of the full results. (The nlines parameter has been employed in some of the print methods in the Haplo Stats package to shorten the lengthy results for this user guide. In practice, it is best to exclude this parameter so that the default will print all results.)

```
> save.em <- haplo.em(geno = geno, locus.label = label,</pre>
    miss.val = c(0, NA))
> print(save.em, nlines = 10)
______
                  Haplotypes
______
  DOB DRB
         B hap.freq
   21
       1
         8
           0.00232
1
2
   21
       2
         7
           0.00227
3
   21
       2 18
           0.00227
4
   21
       3
         8
           0.10408
5
   21
       3 18
           0.00229
6
   21
       3 35
           0.00570
7
   21
       3 44
           0.00378
8
   21
       3 45
           0.00227
9
   21
       3 49
           0.00227
10
   21
       3 57
           0.00227
______
                   Details
_____
lnlike = -1847.675
lr stat for no LD =
               632.8897 , df = 125 , p-val =
```

#### Explanation of Results

The haplotypes and their estimated frequencies are listed, as well as a few details. The lr stat for no LD is the likelihood ratio statistic contrasting the lnlike for the estimated haplotype frequencies versus the lnlike assuming that alleles from all loci are in linkage equilibrium. Trimming by the progressive insertion algorithm can invalidate the lr stat and the degrees of freedom (df).

### 4.3 Summary Method

The summary on save.em shows the list of haplotypes per subject, and their posterior probabilities:

#### > summary(save.em, nlines = 7)

Subjects: Haplotype Codes and Posterior
Probabilities

| <br> | <br> |  |
|------|------|--|

|   | subj.id | hap1code | hap2code | posterior |
|---|---------|----------|----------|-----------|
| 1 | 1       | 78       | 58       | 1.00000   |
| 2 | 2       | 13       | 143      | 0.12532   |
| 3 | 2       | 138      | 17       | 0.87468   |
| 4 | 3       | 25       | 168      | 1.00000   |
| 5 | 4       | 13       | 39       | 0.28621   |
| 6 | 4       | 17       | 38       | 0.71379   |
| 7 | 5       | 94       | 55       | 1.00000   |

Number of haplotype pairs: max vs used

| X |        | 1   | 2  | 3 | 72 | 135 |
|---|--------|-----|----|---|----|-----|
|   | 1      | 18  | 0  | 0 | 0  | 0   |
|   | 2      | 50  | 4  | 0 | 0  | 0   |
|   | 4      | 116 | 29 | 1 | 0  | 0   |
|   | 1800   | 0   | 0  | 0 | 1  | 0   |
|   | 129600 | 0   | 0  | 0 | 0  | 1   |

### Explanation of Results

The first part of the summary output lists the subject id (row number of input geno matrix), the codes for the haplotypes of each pair, and the posterior probabilities of the haplotype pairs. The second part gives a table of the maximum number of pairs of haplotypes per subject, versus the number of pairs used in the final posterior probabilities. The haplotype codes remove the clutter of illustrating all the alleles of the haplotypes, but may not be as informative as the actual haplotypes themselves. To see the actual haplotypes, use the show.haplo=TRUE option:

#### 

```
13
              2
                        21
                                     7
                                              7
                                                         62
                                                                      2
                                              7
                                                                      7
              2
                        62
                                     2
138
                                                         21
25
              3
                        31
                                     1
                                             27
                                                         63
                                                                     13
              4
                                     7
                        21
                                              7
                                                                      7
13.1
                                                         31
              4
                        21
                                     7
                                                         31
                                                                      7
17
                                             44
              5
                                     8
94
                        42
                                             55
                                                         31
                                                                     11
      hap2.B posterior
                  1.00000
78
           61
13
           44
                  0.12532
138
           44
                  0.87468
25
           62
                  1.00000
13.1
           44
                  0.28621
17
            7
                  0.71379
94
           51
                  1.00000
```

\_\_\_\_\_\_

| Number | of | haplotype | pairs: | max v | s used |  |
|--------|----|-----------|--------|-------|--------|--|
|--------|----|-----------|--------|-------|--------|--|

\_\_\_\_\_\_

| X |        | 1   | 2  | 3 | 72 | 135 |
|---|--------|-----|----|---|----|-----|
|   | 1      | 18  | 0  | 0 | 0  | 0   |
|   | 2      | 50  | 4  | 0 | 0  | 0   |
|   | 4      | 116 | 29 | 1 | 0  | 0   |
|   | 1800   | 0   | 0  | 0 | 1  | 0   |
|   | 129600 | 0   | 0  | 0 | 0  | 7   |

### 4.4 Control Parameters for haplo.em

An additional argument can be passed to haplo.em, called "control". This is a list of parameters that control the EM algorithm based on progressive insertion of loci. The default values are set by a function called haplo.em.control (see the help(haplo.em.control) for a complete description). Although the user can accept the default values, there are times when control parameters may need to be adjusted. For example, for small sample sizes and many possible haplotypes, finding the global maximum of the log-likelihood can be difficult. The algorithm uses multiple attempts to maximize the log-likelihood, starting each attempt with random starting values. If the results from haplo.em, haplo.score, or haplo.glm change when rerunning the analyses, this may be due to different maximizations of the log-likelihood. To avoid this, the user can increase the number of attempts (n.try) to maximize the log-likelihood, increase the batch size (insert.batch.size), or decrease the trimming threshold for posterior probabilities (min.posterior). These parameters are defined below:

• insert.batch.size: Number of loci to be inserted in a single batch.

- min.posterior: Minimum posterior probability of haplotype pair, conditional on observed marker genotypes. Posteriors below this minimum value will have their pair of haplotypes "trimmed" off the list of possible pairs.
- max.iter: Maximum number of iterations allowed for the EM algorithm before it stops and prints an error.
- n.try: Number of times to try to maximize the *lnlike* by the EM algorithm. The first try will use, as initial starting values for the posteriors, either equal values or uniform random variables, as determined by *random.start*. All subsequent tries will use uniform random values as initial starting values for the posterior probabilities.

The example below illustrates the syntax for setting the number of tries to 20, and the batch size to 2.

```
> save.em <- haplo.em(geno = geno, locus.label = label,
+ miss.val = c(0, NA), control = haplo.em.control(n.try = 20,
+ insert.batch.size = 2))</pre>
```

### 4.5 Haplotype Frequencies by Group Subsets

To compute the haplotype frequencies for each level of a grouping variable, use the function haplo.group. The following example illustrates the use of a binomial response based on resp.cat, y.bin, that splits the subjects into two groups.

```
> y.bin <- 1 * (resp.cat == "low")
> group.bin <- haplo.group(y.bin, geno, locus.label = label,
+ miss.val = 0)
> print(group.bin, nlines = 15)

Counts per Grouping Variable Value

group
0 1
157 63

Haplotype Frequencies By Group

DQB DRB B Total y.bin.0 y.bin.1
1 21 1 8 0.00232 0.00335 NA
```

```
8 0.00181 0.00318
                                        NA
2
    21
         10
3
    21
         13
             8
               0.00274
                                        NA
          2
            18 0.00227 0.00318
4
    21
                                        NA
5
          2
               0.00227 0.00318
    21
                                        NA
6
          3 18 0.00229 0.00637
    2.1
                                        NA
7
    21
          3 35 0.00570 0.00639
                                        NA
8
    21
          3 44 0.00378 0.00333
                                  0.01587
9
    21
            45 0.00227
                              NA
                                        NA
            49 0.00227
10
    21
                              NA
                                        NA
    21
          3 57 0.00227
11
                              NA
                                        NA
12
    21
          3
            70 0.00227
                              NA
                                        NA
             8 0.10408 0.06974 0.19048
13
    21
          3
    21
            62 0.00455 0.00637
14
    21
            13 0.01072
15
                              NA 0.02381
```

### Explanation of Results

The group.bin object can be very large, depending on the number of possible haplotypes, so only a portion of the output is illustrated above (limited again by nlines). The first section gives a short summary of how many subjects appear in each of the groups. The second section is a table with the following columns:

- The first column gives row numbers.
- The next columns (3 in this example) illustrate the alleles of the haplotypes.
- Total are the estimated haplotype frequencies for the entire data set.
- The last columns are the estimated haplotype frequencies for the subjects in the levels of the group variable (y.bin=0 and y.bin=1 in this example). Note that some haplotype frequencies have an "NA", which occurs when the haplotypes do not occur in the subgroups.

# 5 Haplotype Score Tests: haplo.score

The function haplo.score is used to compute score statistics to test associations between haplotypes and a wide variety of traits, including binary, ordinal, quantitative, and Poisson. This function provides several different global and haplotype-specific tests for association and allows for adjustment for non-genetic covariates. A new feature is that haplotype effects can be specified as additive, dominant, or recessive. This method also has an option to compute permutation p-values, which may be needed for sparse data when distribution assumptions may not be met. Details on the background and theory of the score statistics can be found in Schaid et al.[10].

### 5.1 Quantitative Trait Analysis

First, assess a haplotype association with a quantitative trait in hla.demo called resp. To tell haplo.score the trait is quantitative, specify the parameter trait.type="gaussian" (a reminder that a gaussian distribution is assumed for the distribution of the error terms). The other arguments, all set to default values, are explained in the help file. Note that rare haplotypes can result in unstable variance estimates, and hence unreliable test statistics for rare haplotypes. We restrict the analysis to get scores for haplotypes with a minimum sample count using min.count=5. For more explanation on handling rare haplotypes, see section 5.5. Below is an example of running haplo.score with a quantitative trait, then viewing the results using the print method (again, output shortened by nlines).

```
> score.gaus.add <- haplo.score(resp, geno, trait.type = "gaussian",
     haplo.effect = "additive", min.count = 5,
     locus.label = label, simulate = FALSE)
> print(score.gaus.add, nlines = 10)
             Haplotype Effect Model: additive
   _____
                 Global Score Statistics
  ______
global-stat = 30.6353, df = 18, p-val = 0.03171
                Haplotype-specific Scores
      DQB DRB B Hap-Freq Hap-Score p-val
 [1,] 21
         3
             8
                0.10408
                        -2.39631
                                0.01656
 [2,] 31
          4
             44 0.02849
                        -2.24273
                                0.02491
 [3,] 51
         1
             44 0.01731
                        -0.99357
                                0.32043
 [4,163
             44 0.01606
                        -0.84453
                                0.39837
          13
 [5,] 63
          2
             7
                0.01333
                        -0.50736
                                0.6119
 [6,] 32
             60 0.0306
         4
                        -0.46606
                                0.64118
 [7,] 21
         7
             44 0.02332
                        -0.41942
                                0.67491
 [8,162
         2
             44 0.01367
                        -0.26221
                                0.79316
 [9,] 62
         2
             18 0.01545
                        -0.21493
                                 0.82982
 [10,] 51
         1
             27 0.01505
                        0.01539
                                 0.98772
```

### **Explanation of Results**

First, the model effect chosen by haplo effect is printed across the top. The section Global Score Statistics shows results for testing an overall association between haplotypes and the response. The global-stat has an asymptotic  $\chi^2$  distribution, with degrees of freedom (df) and p-value as indicated. Next, Haplotype-specific scores are given in a table format. The column descriptions are as follows:

- The first column gives row numbers.
- The next columns (3 in this example) illustrate the alleles of the haplotypes.
- Hap-Freq is the estimated frequency of the haplotype in the pool of all subjects.
- *Hap-Score* is the score for the haplotype, the results are sorted by this value. Note, the score statistic should not be interpreted as a measure of the haplotype effect.
- p-val is the asymptotic  $\chi_1^2$  p-value, calculated from the square of the score statistic.

### 5.2 Ordinal Trait Analysis

To create an ordinal trait, here we convert resp.cat (described above) to numeric values, y.ord (with levels 1, 2, 3). For haplo.score, use y.ord as the response variable, and set the parameter trait.type = "ordinal".

DQB DRB B Hap-Freq Hap-Score p-val

```
[1,] 32
             62 0.02349 -2.17133
                                    0.02991
[2,] 21
         3
                0.10408
                         -1.34661
                                    0.17811
[3,] 32
             7
                0.01678
                        -1.09487
         4
                                    0.27357
[4,] 62
         2
                0.05098
                         -0.96874
             7
                                    0.33268
         7
             44 0.02332
                         -0.83747
                                    0.40233
[5,] 21
[6,] 63
         13
             7
                0.01655 -0.80787
                                    0.41917
[7,] 21
                0.01246
                         -0.63316
                                    0.52663
```

### Warning for Ordinal Traits

When analyzing an ordinal trait with adjustment for covariates (using the x.adj option), the software requires the libraries Design and Hmisc, distributed by Frank Harrell [6]. If the user does not have these libraries installed, then it will not be possible to use the x.adj option. However, the unadjusted scores for an ordinal trait (using the default option x.adj=NA) do not require these libraries. Check the list of your local libraries in the list shown from entering library() in your prompt.

### 5.3 Binary Trait Analysis

Let us assume that "low" responders are of primary interest, so we create a binary trait that has values of 1 when resp.cat is "low", and 0 otherwise. Then in haplo.score specify the parameter trait.type="binomial".

```
DQB DRB B
                  Hap-Freq Hap-Score p-val
 [1,] 62
           2
               7
                   0.05098
                             -2.19387
                                        0.02824
 [2,] 51
           1
                  0.03018
                             -1.58421
                                        0.11315
               35
 [3,] 63
           13
               7
                   0.01655
                             -1.56008
                                        0.11874
           7
               7
 [4,] 21
                   0.01246
                             -1.47495
                                        0.14023
 [5,] 32
           4
               7
                   0.01678
                             -1.00091
                                        0.31687
 [6,] 32
           4
                  0.02349
                             -0.6799
                                        0.49657
 [7,] 51
                   0.01505
                             -0.66509
                                        0.50599
           1
 [8,] 31
           11
               35 0.01754
                             -0.5838
                                        0.55936
 [9,] 31
           11
               51 0.01137
                             -0.43721
                                        0.66196
               44 0.01731
[10,] 51
           1
                             0.00826
                                        0.99341
```

### 5.4 Plots and Haplotype Labels

A convenient way to view results from haplo.score is a plot of the haplotype frequencies (Hap-Freq) versus the haplotype score statistics (Hap-Score). This plot, and the syntax for creating it, are shown in Figure 1.

Some points on the plot may be of interest. To identify individual points on the plot, use locator.haplo(score.gaus), which is similar to locator(). Use the mouse to select points on the plot. After points are chosen, click on the middle mouse button, and the points are labeled with their haplotype labels. Note, in constructing Figure 1, we had to define which points to label, and then assign labels in the same way as done within the locator.haplo function.

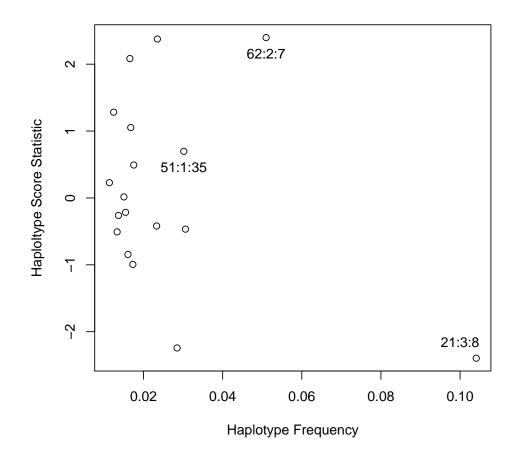


Figure 1: Haplotype Statistics: Score vs. Frequency, Quantitative Response

### 5.5 Skipping Rare Haplotypes

For the quantitative trait analyses, the *skip.haplo* and *min.count* parameters control which rare haplotypes are pooled into a common group. The *min.count* parameter is a recent addition to *haplo.score*, yet it does the same task as *skip.haplo* and is the same idea as *haplo.min.count* used in *haplo.glm.control* for *haplo.glm*. As a guideline, you may wish to set *min.count* to calculate scores for haplotypes with expected haplotype counts of 5 or greater in the sample. We concentrate on this expected count because it adjusts to the size of the input data. If N is the number of subjects and f the haplotype frequency, then the expected haplotype count is  $count = 2 \times N \times f$ . So you can choose  $skip.haplo = \frac{count}{2 \times N}$ . In the following example we try a different cut-off than before, min.count=10, which corresponds to skip.haplo of  $10 \div (2 \times 220) = .045$ . In the output, notice the global statistic and its p-value change because of the fewer haplotypes, while the haplotype-specific scores do not change.

```
> score.gaus.min10 <- haplo.score(resp, geno, trait.type = "gaussian",</pre>
     x.adj = NA, min.count = 10, locus.label = label,
     miss.val = 0, simulate = FALSE)
> print(score.gaus.min10)
              Haplotype Effect Model: additive
 ------
                 Global Score Statistics
global-stat = 20.66451, df = 7, p-val = 0.0043
                Haplotype-specific Scores
     DQB DRB B
               Hap-Freq Hap-Score p-val
[1,] 21
         3
                0.10408 -2.39631
                                 0.01656
[2,] 31
             44 0.02849
                        -2.24273
         4
                                 0.02491
 [3,] 32
         4
             60 0.0306
                        -0.46606
                                  0.64118
 [4,] 21
         7
             44 0.02332 -0.41942
                                 0.67491
 [5,] 51
         1
             35 0.03018 0.69696
                                  0.48583
[6,] 32
             62 0.02349 2.37619
                                  0.01749
 [7,] 62
             7 0.05098
                       2.39795
                                  0.01649
```

### 5.6 Haplotype Scores, Adjusted for Covariates

To adjust for covariates in *haplo.score*, first set up a matrix of covariates from the example data. For example, use a column for male (1 if male; 0 if female), and a second column for age. Then pass the matrix to *haplo.score* using parameter *x.adj*. The results change, though not by much in this example.

```
> x.ma <- cbind(male, age)</pre>
 score.gaus.adj <- haplo.score(resp, geno, trait.type = "gaussian",
     x.adj = x.ma, min.count = 5, locus.label = label,
     miss.val = 0, simulate = FALSE)
> print(score.gaus.adj, nlines = 10)
              Haplotype Effect Model: additive
 ______
                  Global Score Statistics
global-stat = 31.02908, df = 18, p-val = 0.02857
                 Haplotype-specific Scores
                Hap-Freq Hap-Score p-val
      DOB DRB B
  [1,] 21
                 0.10408
                          -2.4097
                                   0.01597
  [2,] 31
              44 0.02849
                         -2.25293
                                  0.02426
  [3,] 51
              44 0.01731
                         -0.98763 0.32333
          1
              44 0.01606
                         -0.83952 0.40118
  [4,] 63
          13
  [5,] 63
          2
              7
                 0.01333
                         -0.48483
                                  0.6278
  [6,] 32
          4
              60 0.0306
                          -0.46476
                                   0.64211
  [7,] 21
          7
              44 0.02332
                         -0.41249
                                   0.67998
  [8,] 62
          2
                          -0.26443
                                   0.79145
              44 0.01367
  [9,] 62
          2
              18 0.01545
                          -0.20425
                                   0.83816
 [10,] 51
              27 0.01505
          1
                          0.02243
                                   0.9821
```

#### 5.7 Haplotype Model Effect (NEW)

A recent addition to *haplo.score* is the ability to select non-additive effects to score haplotypes. The possible effects for haplotypes are additive, dominant, and recessive. Under recessive effects, fewer

haplotypes may be scored, because subjects are required to be homozygous for haplotypes. Furthermore, there would have to be min.count such persons in the sample to have the recessive effect scored. Therefore, a recessive model should only be used on samples with common haplotypes. In the example below with the gaussian response, set the haplotype effect to dominant using parameter haplo.effect = "dominant". Notice the results change slightly compared to the score.gaus.add results above.

```
> score.gaus.dom <- haplo.score(resp, geno, trait.type = "gaussian",
     x.adj = NA, min.count = 5, haplo.effect = "dominant",
     locus.label = label, miss.val = 0, simulate = FALSE)
> print(score.gaus.dom, nlines = 10)
             Haplotype Effect Model: dominant
 -----
 _____
                 Global Score Statistics
global-stat = 29.56133, df = 18, p-val = 0.04194
                Haplotype-specific Scores
      DQB DRB B
               Hap-Freq Hap-Score p-val
 [1,] 21
         3
                0.10408
                        -2.23872
                                 0.02517
 [2,] 31
             44 0.02849
                        -2.13233
                                0.03298
 [3,] 51
             44 0.01731
                        -0.99357
                                0.32043
          1
             44 0.01606
 [4,] 63
         13
                        -0.84453
                                0.39837
 [5,] 63
         2
             7
                0.01333
                       -0.50736
                                0.6119
 [6,] 32
         4
             60 0.0306
                        -0.46606
                                0.64118
 [7,] 21
         7
             44 0.02332
                        -0.41942
                                0.67491
 [8,] 62
          2
             44 0.01367
                        -0.26221
                                0.79316
 [9,] 62
          2
             18 0.01545
                        -0.21493
                                0.82982
 [10,] 51
             27 0.01505
         1
                        0.01539
                                 0.98772
```

### 5.8 Simulation p-values

When simulate=TRUE, haplo.score gives simulated p-values. Simulated haplotype score statistics are the re-calculated score statistics from a permuted re-ordering of the trait and covariates and the original ordering of the genotype matrix. The simulated p-value for the global score statistic

(Global sim. p-val) is the number of times the simulated global score statistic exceeds the observed, divided by the total number of simulations. Likewise, simulated p-value for the maximum score statistic (Max-stat sim. p-val) is the number of times the simulated maximum haplotype score statistic exceeds the observed maximum score statistic, divided by the total number of simulations. The maximum score statistic is the maximum of the square of the haplotype-specific score statistics, which has an unknown distribution, so its significance can only be given by the simulated p-value. Intuitively, if only one or two haplotypes are associated with the trait, the maximum score statistic should have greater power to detect association than the global statistic.

The score.sim.control function manages control parameters for simulations. The haplo.score function employs the simulation p-value precision criteria of Besag and Clifford[1]. These criteria ensure that the simulated p-values for both the global and the maximum score statistics are precise for small p-values. The algorithm performs a user-defined minimum number of permutations (min.sim) to guarantee sufficient precision for the simulated p-values for score statistics of individual haplotypes. Permutations beyond this minimum are then conducted until the sample standard errors for simulated p-values for both the global-stat and max-stat score statistics are less than a threshold (p.threshold \* p-value). The default value for  $p.threshold = \frac{1}{4}$  provides a two-sided 95% confidence interval for the p-value with a width that is approximately as wide as the p-value itself. Effectively, simulations are more precise for smaller p-values. The following example illustrates computation of simulation p-values with min.sim = 1000.

-----

Haplotype-specific Scores

\_\_\_\_\_

```
DQB DRB B
                  Hap-Freq Hap-Score p-val
                                                sim p-val
 [1,] 62
           2
               7
                  0.05098
                            -2.19387
                                       0.02824 0.03519
 [2,] 51
                            -1.58421
           1
               35
                  0.03018
                                       0.11315 0.13863
               7
                            -1.56008
                                       0.11874 0.19177
 [3,] 63
           13
                  0.01655
 [4,]
      21
           7
               7
                  0.01246
                            -1.47495
                                       0.14023 0.15588
 [5,] 32
           4
               7
                  0.01678
                            -1.00091
                                       0.31687 0.26882
 [6,] 32
           4
                  0.02349
                            -0.6799
                                       0.49657 0.47467
 [7,] 51
           1
                  0.01505
                            -0.66509
                                       0.50599 0.64286
 [8,] 31
           11
               35 0.01754
                            -0.5838
                                       0.55936 0.6506
 [9,] 31
                  0.01137
                            -0.43721
                                       0.66196 0.91872
           11
               51
[10,] 51
           1
               44 0.01731
                            0.00826
                                       0.99341 1
                            0.03181
[11,] 32
           4
               60 0.0306
                                       0.97462 0.94968
[12,] 62
           2
               44 0.01367
                            0.16582
                                       0.8683
                                                0.91872
[13,] 63
           13
               44 0.01606
                            0.22059
                                       0.82541 0.73962
[14,] 63
           2
                  0.01333
                            0.2982
                                       0.76555 0.77164
[15,] 62
           2
               18 0.01545
                            0.78854
                                       0.43038 0.6608
[16,] 21
           7
               44 0.02332
                            0.84562
                                       0.39776 0.3962
[17,] 31
           4
               44
                  0.02849
                            2.50767
                                       0.01215 0.01196
[18,] 21
                  0.10408
                            3.77763
                                       0.00016 0.00035
```

## 6 Regression Models: haplo.glm

The haplo.glm function computes the regression of a trait on haplotypes, and possibly other covariates and their interactions with haplotypes. Although this function is based on a generalized linear model, only two types of traits are currently supported: 1) quantitative traits with a normal (gaussian) distribution and identity link, and 2) binomial traits with a logit-link function. The effects of haplotypes on the link function can be modeled as either additive, dominant (heterozygotes and homozygotes for a particular haplotype assumed to have equivalent effects), or recessive (homozygotes of a particular haplotype considered to have an alternative effect on the trait). The basis of the algorithm is a two-step iteration process; the posterior probabilities of pairs of haplotypes per subject are used as weights to update the regression coefficients, and the regression coefficients are used to update the haplotype posterior probabilities. See Lake et al.[7] for details.

### **6.1** Preparing the data frame for haplo.glm

A critical distinction between haplo.glm and all other functions in Haplo Stats is that the definition of the regression model follows the S-PLUS/R formula standard (see lm or glm). So, a data.frame must be defined, and this object must contain the trait, a special kind of genotype matrix (geno.glm for this example) that contains the genotypes of the marker loci, and optionally other covariates and weights. The key features of this data.frame are in how we set up a genotype matrix specific for use in haplo.glm. We prepare geno.glm using setupGeno, which handles character, numeric, or factor alleles, and keeps the columns of the genotype matrix as a single unit when inserting into (and extracting from) a data.frame. The setupGeno function also recodes alleles to integer values (the initial allele codes become an attribute of the returned object), and returns a model.matrix, which can then be included in a data.frame. In the example below we prepare geno.glm, then create a data.frame object (my.data) for use in haplo.glm.

```
> geno <- hla.demo[, c(17, 18, 21:24)]
> geno.glm <- setupGeno(geno, miss.val = c(0, NA),
+ locus.label = label)
> y.bin <- 1 * (resp.cat == "low")
> my.data <- data.frame(geno.glm, age = age, male = male,
+ y = resp, y.bin = y.bin)</pre>
```

### 6.2 Handling Rare Haplotypes

The issue of deciding which haplotypes to use for association is critical in *haplo.glm*. The haplotypes chosen to be modeled in *haplo.glm* are chosen similar to *haplo.score*, by a minimum frequency or a minimum expected count in the sample. The default for choosing a cut-off is the same for setting *skip.haplo* and *min.count* in *haplo.score*, as described in section 5.5.

The default minimum frequency cut-off in haplo.glm is based on a minimum expected count of 5. Two control parameters set in haplo.glm.control may be used to control this setting: haplo.freq.min may be set to a selected minimum haplotype frequency; haplo.min.count may be set to select the cut-off for minimum expected haplotype count in the sample.

### 6.3 Regression for a Quantitative Trait

The following illustrates how to fit a regression of a quantitative trait y on the haplotypes estimated from the geno.glm matrix, and the covariate male. For na.action, we use na.geno.keep, which allows missing values in the genotype matrix, but removes a subject with missing values (NA) in either the response or covariate. The setupGeno function recoded alleles to numeric values in geno.glm numbered starting with 1, but we can preserve the original allele values by setting the allele.lev parameter to be the unique.alleles attribute from geno.glm.

```
> fit.gaus <- haplo.glm(y ~ male + geno.glm, family = gaussian,
+ data = my.data, na.action = "na.geno.keep",</pre>
```

- + locus.label = label, allele.lev = attributes(geno.glm)\$unique.alleles,
- + control = haplo.glm.control(haplo.min.count = 5))
- > print(fit.gaus)

### Call:

haplo.glm(formula = y ~ male + geno.glm,
 family = gaussian, data = my.data, na.action = "na.geno.keep",
 locus.label = label, allele.lev = attributes(geno.glm)\$unique.alleles,
 control = haplo.glm.control(haplo.min.count = 5))

#### Coefficients:

|                          | coef    | se    | t.stat  | pval    |
|--------------------------|---------|-------|---------|---------|
| (Intercept)              | 0.9918  | 0.349 | 2.8393  | 0.00499 |
| male                     | 0.1281  | 0.161 | 0.7962  | 0.42684 |
| geno.glm.13              | 1.1208  | 0.539 | 2.0791  | 0.03889 |
| geno.glm.17              | 0.2713  | 0.441 | 0.6155  | 0.53895 |
| geno.glm.34              | -0.2573 | 0.347 | -0.7408 | 0.45970 |
| geno.glm.50              | 0.7687  | 0.485 | 1.5846  | 0.11463 |
| geno.glm.55              | 0.4538  | 0.566 | 0.8018  | 0.42364 |
| geno.glm.69              | 1.1080  | 0.552 | 2.0057  | 0.04624 |
| geno.glm.77              | 0.2336  | 0.355 | 0.6572  | 0.51178 |
| geno.glm.78              | 1.2370  | 0.387 | 3.1928  | 0.00164 |
| geno.glm.99              | 0.4800  | 0.501 | 0.9573  | 0.33957 |
| geno.glm.100             | 0.6125  | 0.375 | 1.6342  | 0.10378 |
| geno.glm.102             | -0.1097 | 0.447 | -0.2453 | 0.80650 |
| geno.glm.138             | 0.9849  | 0.305 | 3.2342  | 0.00143 |
| geno.glm.140             | 0.4224  | 0.482 | 0.8756  | 0.38228 |
| geno.glm.143             | 0.0215  | 0.500 | 0.0430  | 0.96571 |
| geno.glm.155             | 0.3706  | 0.522 | 0.7104  | 0.47830 |
| geno.glm.162             | 1.3679  | 0.472 | 2.8974  | 0.00418 |
| geno.glm.165             | 0.1172  | 0.460 | 0.2550  | 0.79896 |
| <pre>geno.glm.rare</pre> | 0.3936  | 0.189 | 2.0837  | 0.03846 |

### Haplotypes:

|             | DQB | DRB | B  | hap.freq |
|-------------|-----|-----|----|----------|
| geno.glm.13 | 21  | 7   | 7  | 0.0124   |
| geno.glm.17 | 21  | 7   | 44 | 0.0229   |
| geno.glm.34 | 31  | 4   | 44 | 0.0286   |
| geno.glm.50 | 31  | 11  | 35 | 0.0170   |
| geno.glm.55 | 31  | 11  | 51 | 0.0114   |
| geno.glm.69 | 32  | 4   | 7  | 0.0150   |

```
geno.glm.77
                 32
                       4 60
                               0.0319
geno.glm.78
                 32
                       4
                         62
                               0.0239
geno.glm.99
                 51
                       1 27
                               0.0150
geno.glm.100
                       1
                               0.0300
                 51
                         35
geno.glm.102
                 51
                               0.0176
                       1
                         44
                       2
geno.glm.138
                 62
                          7
                               0.0510
geno.glm.140
                 62
                       2
                         18
                               0.0154
geno.glm.143
                 62
                       2
                         44
                               0.0141
                       2
geno.glm.155
                          7
                               0.0136
                 63
geno.glm.162
                 63
                          7
                               0.0161
                     13
geno.glm.165
                 63
                     13 44
                               0.0165
geno.glm.rare
                               0.5434
haplo.base
                 21
                       3
                          8
                               0.1041
```

### **Explanation of Results**

The above table for Coefficients lists the estimated regression coefficient (coef), its standard error (se), the corresponding t-statistic (t.stat), and p-value (pval). The labels for haplotype coefficients are a concatenation of the name of the genotype matrix (geno.glm) and unique haplotype codes assigned within haplo.glm. The haplotypes corresponding to these haplotype codes are listed in the Haplotypes table, along with the estimates of the haplotype frequencies (hap.freq). The rare haplotypes, those with expected counts less than haplo.min.count=5 (equivalent to having frequencies less than haplo.freq.min = 0.01136 in the above example), are pooled into a single category labeled geno.glm.rare. The haplotype chosen as the baseline category for the design matrix (most frequent haplotype is the default) is labeled as haplo.base; more information on the baseline may be found in section 6.6.2.

### 6.4 Fitting Haplotype x Covariate Interactions

Interactions are fit by the standard S-language model syntax, using a '\*' in the model formula to indicate main effects and interactions. Some other formula constructs are not supported, so use the formula parameter with caution. Below is an example of modeling the interaction of *male* and the haplotypes. Because more terms will be estimated in this case, we limit how many haplotypes will be included by increasing *haplo.min.count* to 10.

```
> fit.inter <- haplo.glm(formula = y ~ male * geno.glm,
+ family = gaussian, data = my.data, na.action = "na.geno.keep",
+ locus.label = label, allele.lev = attributes(geno.glm)$unique.alleles,
+ control = haplo.glm.control(haplo.min.count = 10))
> print(fit.inter)
Call:
haplo.glm(formula = y ~ male * geno.glm,
```

```
family = gaussian, data = my.data, na.action = "na.geno.keep",
locus.label = label, allele.lev = attributes(geno.glm)$unique.alleles,
control = haplo.glm.control(haplo.min.count = 10))
```

#### Coefficients:

|                    | coef    | se    | t.stat  | pval    |
|--------------------|---------|-------|---------|---------|
| (Intercept)        | 0.9754  | 0.523 | 1.8661  | 0.06347 |
| male               | 0.2581  | 0.674 | 0.3832  | 0.70201 |
| geno.glm.17        | 0.1444  | 0.545 | 0.2648  | 0.79144 |
| geno.glm.34        | -0.1716 | 0.668 | -0.2570 | 0.79744 |
| geno.glm.77        | 0.8052  | 0.650 | 1.2398  | 0.21649 |
| geno.glm.78        | 0.4956  | 0.566 | 0.8760  | 0.38208 |
| geno.glm.100       | 0.5231  | 0.481 | 1.0883  | 0.27776 |
| geno.glm.138       | 1.1570  | 0.423 | 2.7337  | 0.00681 |
| geno.glm.rare      | 0.4555  | 0.287 | 1.5859  | 0.11432 |
| male:geno.glm.17   | 0.5087  | 0.875 | 0.5812  | 0.56176 |
| male:geno.glm.34   | -0.2814 | 0.786 | -0.3581 | 0.72063 |
| male:geno.glm.77   | -0.9008 | 0.791 | -1.1386 | 0.25618 |
| male:geno.glm.78   | 1.2638  | 0.771 | 1.6385  | 0.10287 |
| male:geno.glm.100  | 0.0507  | 0.775 | 0.0655  | 0.94785 |
| male:geno.glm.138  | -0.4459 | 0.619 | -0.7203 | 0.47218 |
| male:geno.glm.rare | -0.0979 | 0.372 | -0.2631 | 0.79272 |

### Haplotypes:

|                          | DQB | DRB | B  | hap.freq |
|--------------------------|-----|-----|----|----------|
| geno.glm.17              | 21  | 7   | 44 | 0.0235   |
| geno.glm.34              | 31  | 4   | 44 | 0.0285   |
| geno.glm.77              | 32  | 4   | 60 | 0.0306   |
| geno.glm.78              | 32  | 4   | 62 | 0.0241   |
| geno.glm.100             | 51  | 1   | 35 | 0.0301   |
| geno.glm.138             | 62  | 2   | 7  | 0.0505   |
| <pre>geno.glm.rare</pre> | *   | *   | *  | 0.7086   |
| haplo.base               | 21  | 3   | 8  | 0.1041   |
|                          |     |     |    |          |

### **Explanation of Results**

The listed results are as explained under section 6.3. The main difference is that the interaction coefficients are labeled as a concatenation of the covariate (*male* in this example) and the name of the haplotype, as described above. In addition, estimates may differ because the model has changed.

### 6.5 Regression for a Binomial Trait

Next we illustrate the fitting of a binomial trait with the same genotype matrix and covariate.

```
> fit.bin <- haplo.glm(y.bin ~ male + geno.glm,</pre>
      family = binomial, data = my.data, na.action = "na.geno.keep",
      locus.label = label, allele.lev = attributes(geno.glm)$unique.alleles,
      control = haplo.glm.control(haplo.min.count = 10))
> print(fit.bin)
   Call:
 haplo.glm(formula = y.bin ~ male + geno.glm,
     family = binomial, data = my.data, na.action = "na.geno.keep",
     locus.label = label, allele.lev = attributes(geno.glm)$unique.alleles,
     control = haplo.glm.control(haplo.min.count = 10))
 Coefficients:
                 coef
                          se t.stat
                                        pval
                             2.361 0.019137
 (Intercept)
                1.546 0.655
 male
               -0.480 0.331 -1.452 0.148055
               -0.723 0.801 -0.902 0.367986
 geno.glm.17
 geno.glm.34
                0.364 0.680 0.536 0.592782
 geno.glm.77
               -0.988 0.733 -1.349 0.178829
 geno.glm.78
               -1.409 0.854 -1.650 0.100519
               -2.591 1.128 -2.297 0.022594
 geno.glm.100
 geno.glm.138
               -2.716 0.852 -3.186 0.001661
 geno.glm.rare -1.261 0.354 -3.565 0.000451
 Haplotypes:
               DQB DRB
                        B hap.freq
                             0.0230
 geno.glm.17
                21
                     7 44
 geno.glm.34
                31
                      4 44
                             0.0284
 geno.glm.77
                32
                     4 60
                             0.0306
 geno.glm.78
                32
                     4 62
                             0.0235
 geno.glm.100
                      1 35
                51
                             0.0298
 geno.glm.138
                62
                      2
                         7
                             0.0518
 geno.glm.rare
                             0.7088
 haplo.base
                21
                     3
                        8
                             0.1041
```

#### Explanation of Results

The underlying methods for haplo.glm are based on a prospective likelihood. Normally, this

type of likelihood works well for case-control studies with standard covariates. For ambiguous haplotypes, however, one needs to be careful when interpreting the results from fitting haplo.glm to case-control data. Because cases are over-sampled, relative to the population prevalence (or incidence, for incident cases), haplotypes associated with disease will be over-represented in the case sample, and so estimates of haplotype frequencies will be biased. Positively associated haplotypes will have haplotype frequency estimates that are higher than the population haplotype frequency. To avoid this problem, one can weight each subject. The weights for the cases should be the population prevalence, and the weights for controls should be 1 (assuming the disease is rare in the population, and controls are representative of the general population). See Stram et al.[11] for background on using weights, and see the help file for haplo.glm for how to implement weights.

The estimated regression coefficients for case-control studies can be biased by either a large amount of haplotype ambiguity and mis-specified weights, or by departures from Hardy-Weinberg Equilibrium of the haplotypes in the pool of cases and controls. Generally, the bias is small, but tends to be towards the null of no association. See Stram et al. [11] and Epstein and Satten [5] for further details.

#### 6.5.1 Caution on Rare Haplotypes with Binomial Response

If a rare haplotype occurs only in cases or only in controls, the fitted values would go to 0 or 1, where R or S-PLUS would issue a warning. Also, the coefficient estimate for that haplotype would go to positive or negative infinity, If the default *haplo.min.count=5* were used above, this warning would appear. To keep this from occuring, increase the minimum count or minimum frequency.

### 6.6 Control Parameters

Additional parameters are handled using *control*, which is a list of parameters providing additional functionality in *haplo.glm*. This list is set up by the function *haplo.glm.control*. See the help file (*help(haplo.glm.control*)) for a full list of control parameters, with details of their usage. Some of the options are described here.

#### **6.6.1** Controlling Genetic Models: haplo.effect

The haplo effect control parameter for haplo glm instructs whether the haplotype effects are fit as additive, dominant, or recessive. That is, haplo effect determines whether the covariate (x) coding of haplotypes follows the values in Table 1 for each effect type. Heterozygous means a subject has one copy of a particular haplotype, and homozygous means a subject has two copies of a particular haplotype.

**Table 1:** Coding haplotype covariates in a model matrix

| Hap - Pair   | additive | dominant | recessive |
|--------------|----------|----------|-----------|
| Heterozygous | 1        | 1        | 0         |
| Homozygous   | 2        | 1        | 1         |

Note that in a recessive model, the haplotype effects are estimated only from subjects who are homozygous for a haplotype. Some of the haplotypes which meet the *haplo.freq.min* and *haplo.count.min* cut-offs may occur as homozygous in only a few of the subjects. As stated in 5.7, recessive models should be used when the region has common haplotypes.

The default haplo effect is additive, whereas the example below illustrates the fit of a dominant effect of haplotypes for the gaussian trait with the gender covariate.

#### Coefficients:

```
se t.stat
                 coef
                                       pval
               1.6493 0.373
                             4.416 1.61e-05
(Intercept)
               0.0797 0.157
                             0.507 6.13e-01
male
geno.glm.17
              -0.0604 0.423 -0.143 8.87e-01
              -0.6650 0.364 -1.827 6.91e-02
geno.glm.34
geno.glm.77
              -0.0734 0.347 -0.212 8.33e-01
geno.glm.78
               0.8537 0.364
                            2.344 2.00e-02
geno.glm.100
               0.2470 0.346 0.715 4.76e-01
geno.glm.138
               0.6729 0.282
                            2.389 1.78e-02
geno.glm.rare
               0.1120 0.340 0.329 7.42e-01
```

#### Haplotypes:

DQB DRB B hap.freq

```
geno.glm.17
                21
                      7 44
                              0.0230
geno.glm.34
                31
                      4 44
                              0.0286
geno.glm.77
                              0.0302
                32
                      4 60
geno.glm.78
                              0.0239
                32
                      4 62
geno.glm.100
                      1 35
                              0.0300
                51
geno.glm.138
                62
                      2
                         7
                              0.0502
geno.glm.rare
                              0.7100
haplo.base
                21
                      3
                         8
                              0.1041
```

### 6.6.2 Selecting the Baseline Haplotype

coef

The haplotype chosen for the baseline in the model is the one with the highest frequency. Sometimes the most frequent haplotype may be an at-risk haplotype, and so the measure of its effect is desired. To specify a more appropriate haplotype as the baseline in the binomial example, choose from the list of other common haplotypes, fit.bin\$haplo.common. To specify an alternative baseline, such as haplotype 77, use the control parameter haplo.base and haplotype code, as in the example below.

```
> fit.bin$haplo.common
 [1]
          34 77
                 78 100 138
> fit.bin$haplo.freq.init[fit.bin$haplo.common]
 [1] 0.02332031 0.02848720 0.03060053 0.02349463 0.03018431
 [6] 0.05097906
> fit.bin.base77 <- haplo.glm(y.bin ~ male + geno.glm,</pre>
      family = binomial, data = my.data, na.action = "na.geno.keep",
      locus.label = label, allele.lev = attributes(geno.glm)$unique.alleles,
      control = haplo.glm.control(haplo.base = 77,
          haplo.min.count = 8))
> print(fit.bin.base77)
   Call:
 haplo.glm(formula = y.bin ~ male + geno.glm,
     family = binomial, data = my.data, na.action = "na.geno.keep",
     locus.label = label, allele.lev = attributes(geno.glm)$unique.alleles,
     control = haplo.glm.control(haplo.base = 77,
         haplo.min.count = 8))
 Coefficients:
```

pval

se t.stat

```
(Intercept)
               -0.431 1.359 -0.317 0.7513
               -0.480 0.331 -1.452 0.1481
male
geno.glm.4
                0.988 0.733
                              1.349 0.1788
geno.glm.17
                0.266 1.025
                              0.259 0.7958
geno.glm.34
                1.353 0.922
                              1.466 0.1440
geno.glm.78
               -0.421 1.043 -0.404 0.6870
geno.glm.100
               -1.602 1.301 -1.232 0.2194
geno.glm.138
               -1.727 1.032 -1.674 0.0957
geno.glm.rare -0.273 0.683 -0.399 0.6904
Haplotypes:
               DQB DRB
                         B hap.freq
geno.glm.4
                21
                     3
                         8
                             0.1041
geno.glm.17
                21
                     7
                             0.0230
                       44
geno.glm.34
                             0.0284
                31
                     4
                       44
geno.glm.78
                32
                     4
                             0.0235
                       62
geno.glm.100
                51
                     1 35
                             0.0298
geno.glm.138
                     2
                             0.0518
                62
                         7
geno.glm.rare
                             0.7088
haplo.base
                     4 60
                             0.0306
                32
```

### **Explanation of Results**

The above model has the same haplotypes as *fit.bin*, except haplotype 4, the old baseline, now has an effect estimate while haplotype 77 is the new baseline. Due to randomness in the starting values of the haplotype frequency estimation, different runs of *haplo.glm* may result in a different set of haplotypes meeting the minimum counts requirement for being modeled. Therefore, once you have arrived at a suitable model, and you wish to modify it by changing baseline and/or effects, you can make results consistent by controlling the randomness using *set.seed*, as described in section 3.4. In this document, we use the same seed before making *fit.bin* and *fit.bin.base*77.

# 7 Extended Applications

The following functions are designed to wrap the functionality of the major functions in Haplo Stats into other useful applications.

### 7.1 Combine Score and Group Results: haplo.score.merge

When analyzing a qualitative trait, such as binary, it can be helpful to align the results from haplo.score with haplo.group. To do so, use the function haplo.score.merge, as illustrated in the following example:

```
> merge.bin <- haplo.score.merge(score.bin, group.bin)</pre>
> print(merge.bin, nlines = 10)
         Haplotype Scores, p-values, and Frequencies
                             By Group
                             p.val Hap.Freq y.bin.0 y.bin.1
    DQB DRB
              B Hap.Score
 1
     62
          2
              7
                 -2.19387 0.02824
                                    0.05098 0.06789 0.01587
 2
     51
          1 35
                 -1.58421 0.11315
                                    0.03018 0.03754 0.00907
 3
     63
         13
              7
                 -1.56008 0.11874
                                    0.01655 0.02176
                                                           NA
              7
 4
     21
          7
                 -1.47495 0.14023
                                    0.01246 0.01969
                                                           NA
 5
              7
     32
           4
                 -1.00091 0.31687
                                    0.01678 0.02628 0.00794
 6
     32
           4 62
                 -0.67990 0.49657
                                    0.02349 0.01911
                                                           NA
 7
     51
          1 27
                 -0.66509 0.50599
                                    0.01505 0.01855 0.00907
 8
     31
         11 35
                 -0.58380 0.55936
                                     0.01754 0.01982 0.01587
                 -0.43721 0.66196
                                     0.01137 0.01321
 9
     31
         11 51
                  0.00826 0.99341
                                    0.01731 0.01595 0.00000
 10
     51
           1 44
```

### **Explanation of Results**

The first column is a row index, the next columns (3 in this example) illustrate the haplotype, the Hap.Score column is the score statistic and p.val the corresponding  $\chi^2$  p-value. Hap.Freq is the haplotype frequency for the total sample, and the remaining columns are the estimated haplotype frequencies for each of the group levels (y.bin in this example). The default print method only prints results for haplotypes appearing in the haplo.score output. To view all haplotypes, use the print option all.haps=TRUE, which prints all haplotypes from the haplo.group output. The output is ordered by the score statistic, but the order.by parameter can specify ordering by haplotypes or by haplotype frequencyies.

### 7.2 Case-Control Haplotype Analysis: haplo.cc

It is possible to combine the results of haplo.score, haplo.group, and haplo.glm for case-control data, all performed within haplo.cc. The function performs a score test and a glm on the same haplotypes. Haplotypes used in the analysis have an expected count at least as large as haplo.min.count, which is explained in section 6.2.

Below, we execute *haplo.cc*, view a print-out of the results, then look at the names of the objects stored within the *cc.hla* result.

```
> y.bin <- 1 * (hla.demo$resp.cat == "low")
> cc.hla <- haplo.cc(y = y.bin, geno = geno, haplo.min.count = 8,</pre>
```

+ locus.label = label, control = haplo.glm.control(em.c = haplo.em.control(
> print(cc.hla, nlines = 25, digits = 2)

-----

Global Score Statistics

-----

global-stat = 27, df = 7, p-val = 0.00029

\_\_\_\_\_

#### Counts for Cases and Controls

-----

control case 157 63

Haplotype Scores, p-values, Hap-Frequencies (hf), and Odds Ratios (95% CI)

\_\_\_\_\_ DQB DRB B Hap-Score p-val pool.hf control.hf case.hf 2 7 -2.166 0.03030 0.0504 0.0679 0.0159 147 62 1 35 -1.583 0.11340 0.0302 99 51 0.0376 0.0088 4 62 -0.680 0.49660 0.0235 77 32 0.0191 NA76 4 60 0.029 0.97683 0.0306 32 0.0315 0.0397 15 7 44 1.090 0.27568 0.0219 21 0.0175 0.0476 49 31 4 44 2.514 0.01193 0.0285 0.0145 0.0635 10 21 3 8 3.778 0.00016 0.1040 0.0697 0.1897 1 21 1 8 NANA 0.0023 0.0033 NA2 21 10 8 NANA 0.0018 0.0032 NA3 21 13 8 NANA 0.0027 NANA4 2 18 NA 0.0023 0.0032 21 NANA5 2 7 21 NANA 0.0023 0.0032 NA 6 21 3 18 NA 0.0046 0.0064 NANA7 21 3 35 NANA 0.0057 0.0064 NA8 21 3 44 NANA 0.0038 0.0033 0.0166 9 3 70 NA 0.0023 21 NANANA11 21 4 14 NANA 0.0045 0.0064 NA12 21 4 62 NANA 0.0045 0.0064 NA13 21 7 13 NA 0.0108 NA 0.0238 NANA 0.0079 14 21 7 35 NANA 0.0023 16 21 7 45 NANA 0.0023 0.0032 NA

```
17
     21
             50
                         NA
                                  NA
                                       0.0045
                                                    0.0032
                                                             0.0079
      21
           7
             57
18
                         NA
                                  NA
                                       0.0045
                                                         NA
                                                                  NA
19
      21
           7
             62
                                       0.0077
                                                    0.0074
                         NA
                                  NA
                                                                  NA
20
     21
           7
               7
                                  NA
                                       0.0142
                                                    0.0197
                                                                  NA
                         NA
    glm.eff OR.lower
                           OR OR.upper
         Eff
                 0.014 0.075
                                    0.39
147
         Eff
99
                 0.010 0.092
                                    0.81
                 0.049 0.259
77
         Eff
                                    1.37
76
         Eff
                 0.082 0.338
                                    1.40
         Eff
15
                 0.133 0.639
                                    3.07
49
         Eff
                 0.362 1.386
                                    5.31
                    NA 1.000
10
        Base
                                      NA
1
           R
                 0.147 0.293
                                    0.58
2
                 0.147 0.293
                                    0.58
           R
3
                 0.147 0.293
           R
                                    0.58
4
           R
                 0.147 0.293
                                    0.58
5
           R
                 0.147 0.293
                                    0.58
6
           R
                 0.147 0.293
                                    0.58
7
           R
                 0.147 0.293
                                    0.58
8
                 0.147 0.293
                                    0.58
           R
9
           R
                 0.147 0.293
                                    0.58
           R
                 0.147 0.293
                                    0.58
11
12
           R
                 0.147 0.293
                                    0.58
13
           R
                 0.147 0.293
                                    0.58
14
           R
                 0.147 0.293
                                    0.58
16
           R
                 0.147 0.293
                                    0.58
17
           R
                 0.147 0.293
                                    0.58
18
           R
                 0.147 0.293
                                    0.58
19
           R
                 0.147 0.293
                                    0.58
20
           R
                 0.147 0.293
                                    0.58
```

### > names(cc.hla)

### **Explanation of Results**

First, from the names function we see that *cc.hla* also contains *score.lst* and *fit.lst*, which are the *haplo.score* and *haplo.glm* objects, respectively. For the printed results of *haplo.cc*, first are the global statistics from *haplo.score*, followed by cell counts for cases and controls. The last portion of the output is a data frame containing combined results for individual haplotypes:

- Hap-Score: haplotype score statistic
- p-val: haplotype score statistic p-value
- sim p-val: (if simulations performed) simulated p-value for the haplotype score statistic
- pool.hf: haplotype frequency for the pooled sample
- control.hf: haplotype frequencies for the control sample only
- case.hf: haplotype frequencies for the case sample only
- glm.eff: one of three ways the haplotype appeared in the glm model: Eff: modeled as an effect; Base: part of the baseline; and R: a rare haplotype, included in the effect of pooled rare haplotypes
- OR.lower: Odds Ratio confidence interval lower limit
- **OR:** Odds Ratio for each effect in the model
- OR.upper: Odds Ratio confidence interval upper limit

Significance levels are indicated by the p-values for the score statistics, and the odds ratio (OR) confidence intervals for the haplotype effects. Note that the Odds Ratios are effect sizes of haplotypes, assuming haplotype effects are multiplicative. Since this last table has many columns, lines are wrapped in the output in this manual. You can align wrapped lines by the haplotype code which appears on the far left. Alternatively, instruct the print function to only print digits significant digits, and set the width settings for output in your session using the options() function.

### 7.3 Score Tests on Sub-Haplotypes: haplo.score.slide

To evaluate the association of sub-haplotypes (subsets of alleles from the full haplotype) with a trait, the user can evaluate a "window" of alleles by *haplo.score*, and slide this window across the entire haplotype. This procedure is implemented by the function *haplo.score.slide*. To illustrate this method, we use all 11 loci in the demo data, *hla.demo*.

First, make the geno matrix and the locus labels for the 11 loci. Then use *haplo.score.slide* for a window of 3 loci (*n.slide=3*), which will slide along the haplotype for all 9 contiguous subsets of size 3, using the previously defined gaussian trait resp.

|   | start.loc | score.global.p | <pre>global.p.sim</pre> | max.p.sim |
|---|-----------|----------------|-------------------------|-----------|
| 1 | 1         | 0.215498       | NA                      | NA        |
| 2 | 2         | 0.093664       | NA                      | NA        |
| 3 | 3         | 0.390424       | NA                      | NA        |
| 4 | 4         | 0.487713       | NA                      | NA        |
| 5 | 5         | 0.137468       | NA                      | NA        |
| 6 | 6         | 0.149241       | NA                      | NA        |
| 7 | 7         | 0.110008       | NA                      | NA        |
| 8 | 8         | 0.009963       | NA                      | NA        |
| 9 | 9         | 0.029047       | NA                      | NA        |

#### **Explanation of Results**

The first column is the row index of the nine calls to haplo.score, the second column is the number of the starting locus of the sub-haplotype, the third column is the global score statistic p-value for each call. The last two columns are the simulated p-values for the global and maximum score statistics, respectively. If you specify simulate = TRUE in the function call, the simulated p-values would be present.

#### 7.3.1 Plot Results from haplo.score.slide

The results from haplo.score.slide can be easily viewed in a plot shown in Figure 2 below. The x-axis has tick marks for each locus, and the y-axis is the  $-log_{10}(pval)$ . To select which p-value to plot, use the parameter pval, with choices "global", "global.sim", and "max.sim" corresponding to p-values described above. If the simulated p-values were not computed, the default is to plot the global p-values. For each p-value, a horizontal line is drawn at the height of  $-log_{10}(pval)$  across the loci over which it was calculated. For example, the p-value score.global.p = 0.009963 for loci 8-10 is plotted as a horizontal line at y = 2.002 spanning the  $8^{th}$ ,  $9^{th}$ , and  $10^{th}$  x-axis tick marks.

# > plot(score.slide.gaus, las = 2)

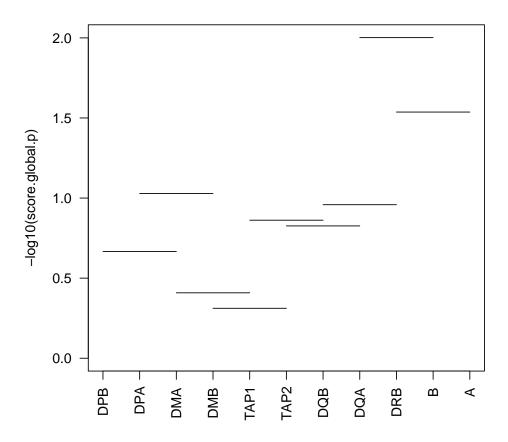


Figure 2: Global p-values for sub-haplotypes; Gaussian Response

#### 7.4 Scanning Haplotypes Within a Fixed-Width Window: haplo.scan

Another method to search for a candidate locus within a genome region is haplo.scan, an implementation of the method proposed in Cheng et al. 2005 [3]. This method searches for a region for which the haplotypes have the strongest association with a binary trait by sliding a window of fixed width over each marker locus, and then scans over all haplotype lengths within each window. This latter step, scanning over all possible haplotype lengths within a window, distinguishes haplo.scan from haplo.score.slide (which considers only the maximum haplotype length within a window). To account for unknown linkage phase, the function haplo.em is called prior to scanning, to create a list of haplotype pairs and posterior probabilities. To illustrate the scanning of window, consider a 10-locus dataset. When placing a window of width 3 over locus 5, the possible haplotype lengths that contain locus 5 are three (loci 3-4-5, 4-5-6, and 5-6-7), two (loci 4-5 and 5-6) and one (locus 5). For each of these loci subsets a score statistic is computed, which is based on the difference between the mean vector of haplotype counts for cases and that for controls. The maximum of these score statistics, over all possible haplotype lengths within a window, is the locus-specific test statistic, or the locus scan statistic. The global test statistic is the maximum over all computed score statistics. To compute p-values, the case/control status is randomly permuted. Below we run haplo.scan on the 11-locus HLA dataset with a binary response and a window width of 3, but first we use the results of summary Geno to choose subjects with less than 50,000 haplotype pairs to speed calculations with all 11 polymorphic loci with many missing alleles.

```
> geno.11 <- hla.demo[, -c(1:4)]</pre>
 y.bin <- 1 * (hla.demo$resp.cat == "low")</pre>
 hla.summary <- summaryGeno(geno.11, miss.val = c(0, miss.val)
      NA))
 many.haps <- (1:length(y.bin))[hla.summary[, 4] >
      50000]
 geno.scan <- geno.11[-many.haps, ]</pre>
> y.scan <- y.bin[-many.haps]</pre>
 scan.hla <- haplo.scan(y.scan, geno.scan, width = 3,</pre>
      sim.control = score.sim.control(min.sim = 100,
          max.sim = 100), em.control = haplo.em.control())
> print(scan.hla)
   Call:
 haplo.scan(y = y.scan, geno = geno.scan,
     width = 3, em.control = haplo.em.control(),
     sim.control = score.sim.control(min.sim = 100,
         max.sim = 100))
```

Locus Scan-statistic Simulated P-values

\_\_\_\_\_\_

```
loc-1 loc-2 loc-3 loc-4 loc-5 loc-6 loc-7 loc-8 sim.p-val 0.03 0.02 0.03 0.01 0.01 0.03 0.01 0.01 loc-9 loc-10 loc-11 sim.p-val 0.01 0.01 0.01
```

Loci with max scan statistic: 2

Max-Stat Simulated Global p-value: 0.02

Number of Simulations: 100

### **Explanation of Results**

In the output we report the simulated p-values for each locus test statistic. Additionally, we report the loci (or locus) which provided the maximum observed test statistic, and the *Max-Stat Simulated Global p-value* is the simulated p-value for that maximum statistic. We print the number of simulations, because they are performed until p-value precision criteria are met, as described in section 5.8. We would typically allow simulations to run under default parameters rather than limiting to 100 by the control parameters.

## 7.5 Sequential Haplotype Scan Methods: seqhap (NEW)

Another approach for choosing loci for haplotype associations is by seqhap, as described in Yu and Schaid, 2007 [13]. The seqhap method performs three tests for association of a binary trait over a set of bi-allelic loci. When evaluating each locus, loci close to it are added in a sequential manner based on the Mantel-Haenszel test [9]. For each marker locus, three tests are provided:

- single locus, the traditional single-locus  $\chi_1^2$  test of association,
- sequential haplotype, based on a haplotype test for sequentially chosen loci,
- sequential summary, based on the sum of a series of conditional  $\chi^2$  statistics.

All three tests are assessed for significance with permutation p-values, in addition to the asymptotic p-value. The point-wise p-value for a statistic at a locus is the fraction of times that the statistic for the permuted data is larger than that for the observed data. The regional p-value is the chance of observing a permuted test statistic, maximized over a region, that is greater than that for the observed data.

Below is an example usage of seqhap on data with case-control response for a chromosome region. Set up the binary response, y, with 0=control, 1=case, a genotype matrix with two columns per locus, and a vector of chromosome positions. In S-PLUS, example data is available in seqhap.dat and chromosome positions seqhap.pos. In R, these objects must be loaded using data(). Run seqhap with 1000 permutations (n.sim=1000), and default settings for threshold parameters.

```
> data(seqhap.dat)
> data(seqhap.pos)
> y <- seqhap.dat$disease
> geno <- seqhap.dat[, -1]</pre>
> pos <- seqhap.pos$pos</pre>
> seqhap.out <- seqhap(y = y, geno = geno, pos = pos,</pre>
    n.sim = 1000, r2.threshold = 0.95, mh.threshold = 3.84,
    miss.val = c(0, NA))
> print(seqhap.out)
______
             Single-locus Chi-square Test
______
Regional permuted P-value based on single-locus test is 0.134
      chi.stat perm.point.p asym.point.p
                   0.299
loc-1 1.22062
                            0.26924
loc-2 1.35462
                   0.234
                            0.24447
loc-3 5.20288
                   0.022
                           0.02255
loc-4 3.36348
                   0.062
                            0.06666
loc-5 3.55263
                   0.067
                            0.05945
loc-6 0.39263
                   0.553
                           0.53092
loc-7 5.54913
                   0.024
                           0.01849
loc-8 3.74740
                   0.062
                           0.05289
loc-9 0.03602
                   0.824
                            0.84947
loc-10 1.99552
                   0.158
                            0.15777
______
                  Sequential Scan
______
Loci Combined in Sequential Analysis
seq-loc-1 1
seq-loc-2 2 3 4 5
seq-loc-3 3 4 5
seq-loc-4 4 3
seq-loc-5 5
seq-loc-6 6 7
seq-loc-7 7
seq-loc-8 8
seq-loc-9 9
seq-loc-10 10
```

Sequential Haplotype Test

| Regional | permuted | P-value  | based   | on   | sequential  | haplotype | test | is | 0.015 |
|----------|----------|----------|---------|------|-------------|-----------|------|----|-------|
|          | han ata  | at df na | rm noir | nt r | n agam noin | - n       |      |    |       |

|            | nap.stat | аI | perm.point.p | asym.point.p |
|------------|----------|----|--------------|--------------|
| seq-loc-1  | 1.22062  | 1  | 0.333        | 0.26924      |
| seq-loc-2  | 24.15359 | 12 | 0.024        | 0.01938      |
| seq-loc-3  | 19.77899 | 6  | 0.006        | 0.00303      |
| seq-loc-4  | 14.95667 | 3  | 0.002        | 0.00185      |
| seq-loc-5  | 3.55263  | 1  | 0.100        | 0.05945      |
| seq-loc-6  | 5.45808  | 2  | 0.114        | 0.06528      |
| seq-loc-7  | 5.54913  | 1  | 0.048        | 0.01849      |
| seq-loc-8  | 3.74740  | 1  | 0.119        | 0.05289      |
| seq-loc-9  | 0.03602  | 1  | 0.848        | 0.84947      |
| seq-loc-10 | 1.99552  | 1  | 0.208        | 0.15777      |

Sequential Summary Test

-----

| Regional p | ermuted P- | -va] | lue based on :          | sequential | summary | test | is | 0.003 |
|------------|------------|------|-------------------------|------------|---------|------|----|-------|
|            | sum.stat   | df   | <pre>perm.point.p</pre> | asym.point | .p      |      |    |       |
| seq-loc-1  | 1.22062    | 1    | 0.333                   | 0.269      | 924     |      |    |       |
| seq-loc-2  | 21.15624   | 4    | 0.000                   | 0.000      | 029     |      |    |       |

| seq-loc-2  | 21.15624 | 4 | 0.000 | 0.00029 |
|------------|----------|---|-------|---------|
| seq-loc-3  | 18.65425 | 3 | 0.000 | 0.00032 |
| seq-loc-4  | 14.62017 | 2 | 0.004 | 0.00067 |
| seq-loc-5  | 3.55263  | 1 | 0.105 | 0.05945 |
| seq-loc-6  | 5.43926  | 2 | 0.115 | 0.06590 |
| seq-loc-7  | 5.54913  | 1 | 0.048 | 0.01849 |
| seq-loc-8  | 3.74740  | 1 | 0.120 | 0.05289 |
| seq-loc-9  | 0.03602  | 1 | 0.848 | 0.84947 |
| seq-loc-10 | 1.99552  | 1 | 0.208 | 0.15777 |

# **Explanation of Results**

For the printed results, the first section (Single-locus Chi-square Test) shows a table with columns for single-locus tests. The table includes test statistics, permuted p-values, and asymptotic p-values based on a  $\chi_1^2$  distribution. The second section (Sequential Scan) shows which loci are combined for association. In this example, the table shows the first locus is not combined with other loci,

whereas the second locus is combined with loci 3, 4, and 5. The third section (Sequential Haplotype Test), shows the test statistics for the sequential haplotype method with degrees of freedom and permuted and asymptotic p-values. The fourth section (Sequential Summary Test) shows similar information for the sequential summary tests.

#### 7.5.1 Plot Results from seqhap

The results from seqhap can be viewed in a useful plot shown in Figure 3. The plot is similar to the plot for haplo.score.slide results, with the x-axis having tick marks for all loci and the y-axis is the -log10() of p-value for the tests performed. For the sequential result for each locus, a horizontal line at the height of -log10(p-value) is drawn across the loci combined. The start locus is indicated by a filled triangle and other loci combined with the start locus are indicated by an asterisk or circle. The choices for pval include "hap" (sequential haplotype asymptotic p-value), "hap.sim" (sequential haplotype simulated p-value), "sum" (sequential summary asymptotic p-value), and "sum.sim" (sequential summary simulated p-value). The other parameter option is single, indicating whether to plot a line for the single-locus tests.

```
> plot(seqhap.out, pval = "hap", single = TRUE,
+ las = 2)
```

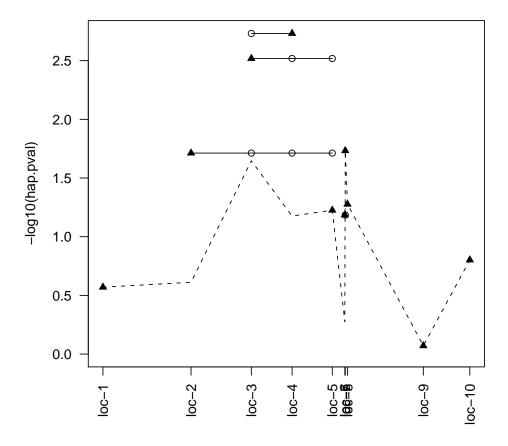


Figure 3: Plot p-values for sequential haplotype scan and single-locus tests

# 7.6 Creating Haplotype Effect Columns: haplo.design (NEW)

In some instances, the desired model for haplotype effects is not possible with the methods given in haplo.glm. Examples include modeling just one haplotype effect, or modeling an interaction of haplotypes from different chromosomes, or analyzing censored data. To circumvent these limitations, we provide a function called haplo.design, which will set up an expected haplotype design matrix from a haplo.em object, to create columns that can be used to model haplotype effects in other modeling functions.

The function haplo.design first creates a design marix for all pairs of haplotypes over all subjects, and then uses the posterior probabilities to create a weighted average contribution for each subject, so that the number of rows of the final design matrix is equal to the number of subjects. This is sometimes called the expectation-substitution method, as proposed by Zaykin et al. 2002 [14], and using this haplotype design matrix in a regression model is asymptotically equivalent to the score statistics from haplo.score (Xie and Stram 2005 [12]). Although this provides much flexibility, by using the design matrix in any type of regression model, the estimated regression parameters can be biased toward zero (see Lin and Zeng, 2006 [8] for concerns about the expectation-substitution method).

In the first example below, using default parameters, the returned data.frame contains a column for each haplotype that meets a minimum count in the sample *min.count*. The columns are named by the code they are assigned in *haplo.em*.

# > hap.effect.frame <- haplo.design(save.em)</pre>

> names(hap.effect.frame)

```
[1] "hap.4" "hap.13" "hap.17" "hap.34" "hap.50" [6] "hap.55" "hap.69" "hap.77" "hap.78" "hap.99" [11] "hap.100" "hap.102" "hap.138" "hap.140" "hap.143" [16] "hap.155" "hap.162" "hap.165"
```

#### > hap.effect.frame[1:10, 1:8]

|    | hap.4 | hap.13    | hap.17    | hap.34 | hap.50 | hap.55 | hap.69 |
|----|-------|-----------|-----------|--------|--------|--------|--------|
| 1  | 0     | 0.0000000 | 0.0000000 | 0      | 0      | 0      | 0      |
| 2  | 0     | 0.1253234 | 0.8746766 | 0      | 0      | 0      | 0      |
| 3  | 0     | 0.0000000 | 0.0000000 | 0      | 0      | 0      | 0      |
| 4  | 0     | 0.2862131 | 0.7137869 | 0      | 0      | 0      | 0      |
| 5  | 0     | 0.0000000 | 0.0000000 | 0      | 0      | 1      | 0      |
| 6  | 1     | 0.0000000 | 1.0000000 | 0      | 0      | 0      | 0      |
| 7  | 0     | 0.0000000 | 0.0000000 | 0      | 0      | 0      | 0      |
| 8  | 0     | 0.0000000 | 0.0000000 | 0      | 0      | 0      | 0      |
| 9  | 0     | 0.0000000 | 0.0000000 | 0      | 0      | 0      | 0      |
| 10 | 0     | 0.0000000 | 0.0000000 | 0      | 0      | 0      | 0      |

```
hap.77
1
           0
2
           0
3
           0
4
           0
5
           0
6
           0
7
           0
8
           0
9
           0
           0
10
```

Additionally, *haplo.design* gives the user flexibility to make a more specific design matrix with the following parameters:

- hapcodes: codes assigned in the haplo.em object, the only haplotypes to be made into effects
- haplo.effect: the coding of haplotypes as additive, dominant, or recessive
- haplo.base: code for the baseline haplotype
- min.count: minimum haplotype count

This second example below creates columns for specific haplotype codes that were most interesting in *score.gaus.add*, haplotypes with alleles 21-3-8 and 62-2-7, corresponding to codes 4 and 138 in *haplo.em*, respectively. Assume we want to test their individual effects when they are coded with *haplo.effect="dominant"*.

```
> hap4.hap138.frame <- haplo.design(save.em, hapcodes = c(4,</pre>
      138), haplo.effect = "dominant")
> hap4.hap138.frame[1:10, ]
    hap.4
            hap.138
 1
        0 0.0000000
 2
        0 0.8746766
 3
        0 0.0000000
 4
        0 0.0000000
 5
        0 0.0000000
 6
        1 0.0000000
 7
        0 1.0000000
 8
        0 0.0000000
 9
        0 0.1358697
        0 0.0000000
 10
```

```
> dat.glm <- data.frame(resp, male, age, hap.4 = hap4.hap138.frame$hap.4,</pre>
     hap.138 = hap4.hap138.frame$hap.138)
> glm.hap4.hap138 <- glm(resp ~ male + age + hap.4 +</pre>
     hap.138, family = "gaussian", data = dat.glm)
> summary(glm.hap4.hap138)
Call:
 glm(formula = resp ~ male + age + hap.4 + hap.138, family = "gaussian",
    data = dat.glm)
 Deviance Residuals:
    Min
              10
                 Median
                          3Q
                                      Max
 -2.3261 -1.0749 -0.0656 1.0448
                                   2.3904
 Coefficients:
            Estimate Std. Error t value Pr(>|t|)
 (Intercept) 1.913834 0.229577 8.336 9.1e-15 ***
           0.048588 0.155290 0.313 0.7547
 male
           -0.002651 0.011695 -0.227 0.8209
 age
 hap.4
           -0.405530 0.195857 -2.071 0.0396 *
 hap.138
           Signif. codes: 0 ,***, 0.001 ,**, 0.01 ,*, 0.05 ,., 0.1 , , 1
 (Dispersion parameter for gaussian family taken to be 1.318277)
    Null deviance: 297.01 on 219 degrees of freedom
 Residual deviance: 283.43 on 215 degrees of freedom
 AIC: 692.07
```

Number of Fisher Scoring iterations: 2

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## **Appendix**

# A Counting Haplotype Pairs When Marker Phenotypes Have Missing Alleles

The following describes the process for counting the number of haplotype pairs that are consistent with a subject's observed marker phenotypes, allowing for some loci with missing data. Note that we refer to marker phenotypes, but our algorithm is oriented towards typical markers that have a one-to-one correspondence with their genotypes. We first describe how to count when none of the loci have missing alleles, and then generalize to allow loci to have either one or two missing alleles. When there are no missing alleles, note that homozygous loci are not ambiguous with respect to the underlying haplotypes, because at these loci the underlying haplotypes will not differ if we interchange alleles between haplotypes. In contrast, heterozygous loci are ambiguous, because we do not know the haplotype origin of the distinguishable alleles (i.e., unknown linkage phase). However, if there is only one heterozygous locus, then it doesn't matter if we interchange alleles, because the pair of haplotypes will be the same. In this situation, if parental origin of alleles were known, then interchanging alleles would switch parental origin of haplotypes, but not the composition of the haplotypes. Hence, ambiguity arises only when there are at least two heterozygous loci. For each heterozygous locus beyond the first one, the number of possible haplotypes increases by a factor of 2, because we interchange the two alleles at each heterozygous locus to create all possible pairs of haplotypes. Hence, the number of possible haplotype pairs can be expressed as  $2^x$ , where x = H - 1, if H (the number of heterozygous loci) is at least 2, otherwise x=0.

Now consider a locus with missing alleles. The possible alleles at a given locus are considered to be those that are actually observed in the data. Let  $a_i$  denote the number of distinguishable alleles at the locus. To count the number of underlying haplotypes that are consistent with the observed and missing marker data, we need to enumerate all possible genotypes for the loci with missing data, and consider whether the imputed genotypes are heterozygous or homozygous.

To develop our method, first consider how to count the number of genotypes at a locus, say the  $i^{th}$  locus, when either one or two alleles are missing. This locus could have either a homozygous or heterozygous genotype, and both possibilities must be considered for our counting method. If the locus is considered as homozygous, and there is one allele missing, then there is only one possible genotype; if there are two alleles missing, then there are  $a_i$  possible genotypes. A function to perform this counting for homozygous loci is denoted  $f(a_i)$ . If the locus is considered as heterozygous, and there is one allele missing, then there are  $a_i - 1$  possible genotypes; if there are two alleles missing, then there are  $\frac{a_i(a_i-1)}{2}$  possible genotypes. A function to perform this counting for heterozygous loci is denoted  $g(a_i)$  These functions and counts are summarized in Table A.1.

**Table A.1:** Factors for when a locus having missing allele(s) is counted as homozygous(f()) or heterozygous(g())

| Number of       | Homozygous        | Heterozygous           |
|-----------------|-------------------|------------------------|
| missing alleles | function $f(a_i)$ | function $g(a_i)$      |
| 1               | 1                 | $a_i - 1$              |
| 2               | $a_i$             | $\frac{a_i(a_i-1)}{2}$ |

Now, to use these genotype counting functions to determine the number of possible haplotype pairs, first consider a simple case where only one locus, say the  $i^{th}$  locus, has two missing alleles. Suppose that the phenotype has H heterozygous loci (H is the count of heterozygous loci among those without missing data). We consider whether the locus with missing data is either homozygous or heterozygous, to give the count of possible haplotype pairs as

$$a_i 2^x + \left[ \frac{a_i (a_i - 1)}{2} \right] 2^{x+1} \tag{1}$$

where again x = H - 1 if H is at least 2, otherwise x = 0. This special case can be represented by our more general genotype counting functions as

$$f(a_i) 2^x + g(a_i) 2^{x+1}$$
 (2)

When multiple loci have missing data, we need to sum over all possible combinations of heterozygous and homozygous genotypes for the incomplete loci. The rows of Table A.2 below present these combinations for up to m=3 loci with missing data. Note that as the number of heterozygous loci increases (across the columns of Table A.2), so too does the exponent of 2. To calculate the total number of pairs of haplotypes, given observed and possibly missing genotypes, we need to sum the terms in Table A.2 across the appropriate row. For example, with m=3, there are eight terms to sum over. The general formulation for this counting method can be expressed as

$$TotalPairs = \sum_{j=0}^{m} \sum_{combo} C(combo, j)$$
(3)

where combo is a particular pattern of heterozygous and homozygous loci among the loci with missing values (e.g., for m=3, one combination is the first locus heterozygous and the  $2^{nd}$  and  $3^{rd}$  third as homozygous), and C(combo,j) is the corresponding count for this pattern when there are i loci that are heterozygous (e.g., for m=3 and j=1, as illustrated in Table A.2).

**Table A.2:** Genotype counting terms when m loci have missing alleles, grouped by number of heterozygous loci (out of m)

| m | j = 0 of m              | j = 1  of  m                     | j = 2 of m                  | j = 3  of  m                |
|---|-------------------------|----------------------------------|-----------------------------|-----------------------------|
| 0 | $2^x$                   |                                  |                             |                             |
| 1 | $f(a_1)2^x$             | $g(a_1)2^{x+1}$                  |                             |                             |
| 2 | $f(a_1)f(a_2)2^x$       | $g(a_1)f(a_2)2^{x+1}$            | $g(a_1)g(a_2)2^{x+1}$       |                             |
|   |                         | $f(a_1)g(a_2)2^{x+1}$            |                             |                             |
| 3 | $f(a_1)f(a_2)f(a_3)2^x$ | $g(a_1)f(a_2)f(a_3)2^{x+1}$      | $g(a_1)g(a_2)f(a_3)2^{x+2}$ | $g(a_1)g(a_2)g(a_3)2^{x+2}$ |
|   |                         | $f(a_1)g(a_2)f(a_3)2^{x+1}$      | $g(a_1)f(a_2)g(a_3)2^{x+2}$ |                             |
|   |                         | $\int f(a_1)f(a_2)g(a_3)2^{x+1}$ | $f(a_1)g(a_2)g(a_3)2^{x+2}$ |                             |

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