Crash Introduction to markovchain R package

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2018-06-29

Intro

- ▶ The markovchain package (Spedicato 2017) will be introduced.
- ► The package is intended to provide S4 classes to perform probabilistic and statistical analysis of Discrete Time Markov Chains (DTMC). See (Brémaud 1999) for a theoretical review of the mathematics underlying the DTMC models.
- The vignette will show: how to load the package and create a DTMC, how to manage a DTMC, how to perform basic probabilistic analysis, how to fit a DTMC.

- ▶ The package is on Cran since Summer 2013.
- ▶ It requires a recent version of R (>=3.0). Since version 0.2
- parts of code have been moved to Rcpp (Eddelbuettel 2013). ▶ The package won a slot in Google Summer of Code 2015 for

optimizing internals and expanding functionalities.

First moves into the markovchain package

Loading the package

► The package is loaded using

```
#load the package
library(markovchain)
```

Creating a DTMC

a 0.0 0.5 0.5 ## b 0.5 0.0 0.5

▶ DTMC can be easily create following standard S4 classes syntax. The show method displays it.

```
## MarkovChain A
## A 3 - dimensional discrete Markov Chain defined by the
## a, b, c
## The transition matrix (by rows) is defined as follows
## a b c
```

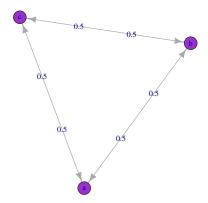
▶ Otherwise, it can also be created directly coercing a matrix.

```
dtmcA2<-as(tmA, "markovchain") #using coerce from matrix
states(dtmcA2) #note default names assigned to states</pre>
```

[1] "s1" "s2" "s3"

▶ It is also possible to display a DTMC, using igraph package (Csardi and Nepusz 2006) capabilities

plot(dtmcA)



Probabilistic analysis

The basic

- It is possible to access transition probabilities and to perform basic operations.
- ▶ Similarly, it is possible to access the conditional distribution of states, $Pr(X_{t+1}|X_t=s)$

```
dtmcA[2,3] #using [ method
```

```
## [1] 0.5
```

```
## [1] 0.5
```

▶ It is possible to simulate states distribution after n-steps

```
initialState<-c(0,1,0)
steps<-4
finalState<-initialState*dtmcA^steps #using power operator
finalState</pre>
```

```
## a b c
## [1,] 0.3125 0.375 0.3125
```

As well as steady states distribution

```
steadyStates(dtmcA) #S4 method
```

```
## a b c
## [1,] 0.3333333 0.3333333 0.3333333
```

Advanced

► We use an example found on Mathematica Web page, (Wolfram Research 2013)

 $E \leftarrow matrix(0, nrow = 4, ncol = 4)$

```
E[1, 2] <- 1;E[2, 1] <- 1/3; E[2, 3] <- 2/3

E[3,2] <- 1/4; E[3, 4] <- 3/4; E[4, 3] <- 1

mcMathematica <- new("markovchain", states = c("a", "b", "c

transitionMatrix = E, name = "Mathemats
```

The summary method shows the proprieties of the DTCM

summary(mcMathematica)

```
## Mathematica Markov chain that is composed by:
## Closed classes:
## a b c d
## Recurrent classes:
## {a,b,c,d}
## Transient classes:
## NONE
## The Markov chain is irreducible
## The absorbing states are: NONE
```

Estimation and simulation

The package permits to fit a DTMC estimating the transition matrix from a sequence of data. - createSequenceMatrix returns a function showing previous vs actual states from the pairs in a given sequence.

```
#using Alofi rainfall dataset
data(rain)
```

```
mysequence<-rain$rain
createSequenceMatrix(mysequence)</pre>
```

```
## 0 1-5 6+
## 0 362 126 60
## 1-5 136 90 68
## 6+ 50 79 124
```

markovchainFit function allows to obtain the estimated transition matric and the confidence levels (using elliptic MLE hyphotesis).

```
myFit<-markovchainFit(data=mysequence,confidencelevel = .9</pre>
myFit
```

```
## $estimate
## MI.F. Fit.
    A 3 - dimensional discrete Markov Chain defined by the
```

0, 1-5, 6+## ## 1-5 6+

The transition matrix (by rows) is defined as follows ## 0 0.6605839 0.2299270 0.1094891

1-5 0.4625850 0.3061224 0.2312925

6+ 0.1976285 0.3122530 0.4901186

##

##

\$standardError

6+

► See the vignettes for further fitting methods as well as for functionalities targeted on non - homogeneous Markov chains.

```
alofiMc<-myFit$estimate
alofiMc</pre>
```

1-5 0.4625850 0.3061224 0.2312925 ## 6+ 0.1976285 0.3122530 0.4901186

```
## MLE Fit
## A 3 - dimensional discrete Markov Chain defined by the
## 0, 1-5, 6+
## The transition matrix (by rows) is defined as follows
## 0 1-5 6+
## 0 0.6605839 0.2299270 0.1094891
```

Bibliography I

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