A Package for Matrix Powers in R,

with Some Edifying Material on R

Norm Matloff and Jack Norman University of California at Davis

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Bay Area R Users Group, August 12, 2014

these slides:

heather.cs.ucdavis.edu/matpow/BARUGmatpow.pdf



Material on R

Norm Matloff and Jack Norman University of California at

Davis

e-mail: matloff@cs.ucdavis.edu R/stat blog: matloff.wordpress.com Edifying Material on R

and Jack Norman University of California at Davis

Goals of this talk:

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 Show how useful matrix powers can be in in data science, especially for parallel computation

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- Show how useful matrix powers can be in in data science, especially for parallel computation
- Present a small R package that facilitates matrix power computation, including parallel approaches.
- Demonstrate a trick useful for accommodating varied data types.

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# Why Matrix Powers?

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Why are matrix powers so important in data science?

Various apps (see below).

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  - R has tons of ways of doing parallel matrix multiplication.
  - "Pretty Good Parallelism": If can obtain fairly good speedup very conveniently, we may not pursue optimal solutions.

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# Examples of Apps

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e-mail: matloff@cs.ucdavis.edu R/stat blog: matloff.wordpress.com Matrix powers have various applications, e.g.:

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determination of graph connectivity
 For adjacency matrix A, the graph is connected if and only if

for some k > 0,  $\tilde{A}^k > 0$  elementwise

where  $\tilde{A}$  is A with all 1s on the diagonal. Moreover, the elements of  $\tilde{A}^k$  can give you the distance from each i to each j.

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Exploit the fact that  $\lim_{n\to\infty} P(X_n = j|X_0 = i) = \pi_j$ . It implies that for transition matrix P,  $\pi$  vector is approximately

Could also adapt the graph-connect method to determine periodicity of a finite chain.

• (principal) eigenvector computation

e-mail: matloff@cs.ucdavis.edu R/stat blog: matloff.wordpress.com (principal) eigenvector computation

For "most" square matrices A and initial guess vectors x,

$$\frac{A^k x}{||A^k x||}$$

converges to the principal eigenvector of A. So, set an initial x, then iterate  $x \leftarrow Ax/\|Ax\|$ .

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• computation of generalized matrix inverse Iterate  $B \leftarrow B(2I - AB)$ , starting with B a small multiple of A'.

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#### R Package: matpow

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matpow <- function(m, k=NULL, squaring=FALSE,
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## Powers by Squaring

• Say you want to find  $M^8$ .

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- In call to matpow(), set squaring = TRUE.

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## Sharing Data

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> | <- list(x=3,y=8)
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function(|st) {
    |$x[1] <- 88
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### R Environments

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#### Contents of **ev**:

- the matrix m
- the target exponent k
- i, the current iteration number
- **stop**; TRUE means stop iterations
- squaring
- etc.
- app-specific data

e-mail: matloff@cs.ucdavis.edu R/stat blog: matloff.wordpress.com The Key Role of Callbacks

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## The Key Role of Callbacks

Our goal is to provide a convenient general framework for diverse applications of matrix powers.

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• **Example:** Graph connectivity and distance computation.

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Example Callback: Graph Connectivity

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# Example Callback: Graph Connectivity

```
matpow(m, k, callback=cgraph, mindist=TRUE)
cgraph <-
   function(ev,cbinit=FALSE,mindist=FALSE) {
   if (cbinit) {
      ev$dists <- ev$m
      return()
   if (all(ev\$prd > 0)) {
      ev$stop <- TRUE
      (mindist) {
      tmp \leftarrow ev\$prd > 0
      ev\$dists[tmp \& ev\$dists == 0] <- ev\$i+1
```

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e-mail: matloff@cs.ucdavis.edu R/stat blog: matloff.wordpress.com Use of eval()

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## Use of eval()

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$$c[,] <- a[,] \% \% b[,]$$

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We want to be able to handle other matrix multiplication types too, including user-defined ones.

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We want to be able to handle other matrix multiplication types too, including user-defined ones. How?

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## R's eval() function

```
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```

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```
> x <- 28
> s <- "x <- 16"
> eval(parse(text=s))
> x
[1] 16
```

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```
> x <- 28
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So, we can embed the different types of matrix multiplication in strings!

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#### Recall form of call:

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 $\label{eq:matpow} \begin{subarray}{ll} matpow &<- & function (m, k=NULL, squaring=FALSE, genmulcmd=NULL, dup=NULL, callback=NULL, . . . ) & \\ \end{subarray}$ 

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```

```
 \begin{array}{lll} \mbox{genmulcmd.gputools} & < & \mbox{function}(a,b,c) \\ \mbox{paste}(c," & < & \mbox{gpuMatMult}(",a,",",b,")") \end{array}
```

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\label{eq:matpow} $$ \leftarrow $ function(m, k=NULL, squaring=FALSE, genmulcmd=NULL, dup=NULL, callback=NULL, \dots) $$ \{ E.g. $$
```

```
genmulcmd.gputools <- function(a,b,c)
   paste(c," <- gpuMatMult(",a,",",b,")")
So matpow() code can be general, e.g.
eval(parse(text=ev$genmulcmd(m,p1,p2))</pre>
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$$eval(parse(text=ev\$genmulcmd(m,p1,p2))$$

The function **genmulcmd()** is either sensed by matrix class or specified by user.

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## Parallel Operation

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- Example: If you have configured R to use OpenBLAS, your multiplications will use all the cores.

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- The matpow() function handles whatever type of multiplication you give. So, if you give it a parallel multiplication, you compute matrix powers in parallel!
- Example: If you have configured R to use OpenBLAS, your multiplications will use all the cores.
- Example: GPU, say with gputools.

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e-mail: matloff@cs.ucdavis.edu R/stat blog: matloff.wordpress.com Brief Timing Experiment with gputools

## Brief Timing Experiment with gputools

Modest hardware: Intel Core i7-2600K CPU, 3.40GHz, GeForce GTX 550 T

A Package for Matrix Powers in R,

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k	CPU	GPU
2	6.134	1.836
3	12.626	0.620
4	18.981	0.930
5	25.222	1.235

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- About 20X speedup due to GPU.
- Lots of overhead in the case k = 2.

Material on R

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- Same for cluster use: The genmulcmd() function should be written to leave the powers at the cluster nodes.
   Actually, should have each node maintain a chunk of rows of the current power.

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#### Conclusions

• Matrix powers have lots of uses.

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Location of the code and these slides: http://heather.cs.ucdavis.edu/matpow/