Causal Mediation Analysis Using R^{*}

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Abstract

Causal mediation analysis is widely used across many disciplines to investigate possible causal mechanisms. Such an analysis allows researchers to explore various causal pathways, going beyond the estimation of simple causal effects. Recently, Imai, Keele, and Yamamoto (2010c) and Imai, Keele, and Tingley (2010b) developed general algorithms to estimate causal mediation effects with the variety of data types that are often encountered in practice. The new algorithms can estimate causal mediation effects for linear and nonlinear relationships, with parametric and nonparametric models, with continuous and discrete mediators, and various types of outcome variables. In this paper, we show how to implement these algorithms in the statistical computing language R. Our easy-to-use software, mediation, takes advantage of the object-oriented programming nature of the R language and allows researchers to estimate causal mediation effects in a straightforward manner. Finally, mediation also implements sensitivity analyses which can be used to formally assess the robustness of findings to the potential violations of the key identifying assumption. After describing the basic structure of the software, we illustrate its use with several empirical examples.

^{*}This paper is an updated version of the tutorial for package **mediation** which was previously published in an edited volume: Imai et~al. (2010a). The description is based on version 3.0 of **mediation** and included as the package's vignette. Financial support from the National Science Foundation (SES-0752050) is acknowledged.

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1 Introduction

Causal mediation analysis is important for quantitative social science research because it allows researchers to identify possible causal mechanisms, thereby going beyond the simple estimation of causal effects. As social scientists, we are often interested in empirically testing a theoretical explanation of a particular causal phenomenon. This is the primary goal of causal mediation analysis. Thus, causal mediation analysis has a potential to overcome the common criticism of quantitative social science research that it only provides a black-box view of causality.

Recently, Imai, Keele, and Yamamoto (2010c) and Imai, Keele, and Tingley (2010b) developed general algorithms for the estimation of causal mediation effects with a wide variety of data that are often encountered in practice. The new algorithms can estimate causal mediation effects for linear and nonlinear relationships, with parametric and nonparametric models, with continuous and discrete mediators, and various types of outcome variables. Imai et~al. (2010c,~b) also develop sensitivity analyses which can be used to formally assess the robustness of findings to the potential violations of the key identifying assumption. In this paper, we describe the easy-to-use software, mediation, which allows researchers to conduct causal mediation analysis within the statistical computing language R (R Development Core Team 2009). We illustrate the use of the software with some of the empirical examples presented in Imai et~al. (2010b).

Installation and Updating. Before we begin, we explain how to install and update the software. First, researchers need to install **R** which is available freely at the Comprehensive R Archive Network (http://cran.r-project.org). Next, open **R** and then type the following at the prompt,

```
R> install.packages("mediation")
```

Once **mediation** is installed, the following command will load the package,

R> library("mediation")

Finally, to update **mediation** to its latest version, try the following command,

R> update.packages("mediation")

2 New Features in Version 3.0

This section describes the recent update (version 3.0) to the mediation package. Readers may wish to skip this section and come back later if they are not already familiar with previous versions of the package.

We implemented many new features in version 3.0, along with numerous small changes to the internal code for efficiency improvement. The user-level changes from the previous version include:

More model types have been added to the main mediation analysis function mediate. In
addition to the models already implemented in the previous version, the mediate function
can now be used for ordered response models fitted via the polr function, quantile regressions
for mediators fitted via the qr function in package quantreg, and the tobit model for censored

outcome variables fitted via the vglm function in package VGAM. These models have not been made available for sensitivity analysis via medsens, however.

- Continuous treatment variables can now be used with the mediate function via the treat.value and control.value arguments. The estimated average causal mediation effects (ACME) and average direct effects (ADE) will be equal to the effects of changing treatment from control.value to treat.value while holding the appropriate treatment status constant at either of these two values. This functionality, however, has not been implemented for the medsens function yet.
- The sensitivity analysis via medsens can now be conducted with respect to the average direct effects. Users can choose from "indirect", "direct" or "both" using the effect.type argument. The summary and plot methods are also added for these cases.
- A plot method function for mediate objects is now included, so that the results of mediation analysis using mediate can be easily graphically summarized. When the input includes treatment-mediator interaction and the effect estimates therefore differ between the treatment and control conditions, the user can choose which set of estimates to plot by setting the treatment argument to "treated", "control", or "both".
- The summary output for mediate objects has been updated to include additional information and not to include unnecessary information (e.g. separate estimates for $\bar{\delta}(0)$ and $\bar{\delta}(1)$ when they are equal).
- The output of the mediate function now by default includes the entire sets of simulation draws (d0.sims, z0.sims, etc.) in addition to their means and quantiles. This can be disabled by setting the long argument to FALSE.
- The mediate function can now run even when different data frames are used for the mediator model (model.m) and outcome model (model.y). This is done by internally refitting both models using a combined data frame created via merge. As a result, observations which contain missing values for either model will be automatically listwise discarded. This feature is by default disabled and can be enabled by setting the dropobs option to TRUE.
- Confidence intervals can now be calculated using heteroskedasticity-consistent standard errors for some parametric models (e.g. lm, glm). This feature is controlled by the new robustSE argument of the mediate function. The standard errors are obtained via the vcovHC function in package sandwich and users may also pass options for vcovHC to use different types of robust standard errors. However, these standard errors are currently not carried through for sensitivity analysis; the output of medsens will not be based on robust standard errors regardless of the robustSE argument.
- Users no longer need to manually indicate whether their models include a treatment-mediator interaction. The old INT argument is therefore deprecated (but still accepted with a warning).

- Sampling weights can now be used for the mediate and medsens functions via the weights arguments in the input mediator and outcome models. The estimated quantities will thus be weighted averages when the mediator and outcome models are fitted with a non-NULL weights argument. This will be useful if, for example, data come from a complex survey.
- We have added a new function mediations to easily conduct multiple causal mediation analyses for different treatment-mediator-outcome combinations. Both summary and plot methods have also been added for this function. The function is intended for exploratory analyses only and users are cautioned against its potential abuse. See Section 5 for more discussion.

3 The Software

In this section, we give an overview of the software by describing its design and architecture. To avoid the duplication, we do not provide the details of the methods that are implemented by **mediation** and the assumptions that underline them. Readers are encouraged to read Imai $et^{\tilde{a}}$ al. (2010c, \tilde{b}) for more information about the methodology implemented in **mediation**.

3.1 The Overview

The methods implemented via **mediation** rely on the following identification result obtained under the sequential ignorability assumption of Imai et $\tilde{a}l$. (2010c),

$$\bar{\delta}(t) = \int \int \mathbb{E}(Y_i \mid M_i = m, T_i = t, X_i = x) \left\{ dF_{M_i \mid T_i = 1, X_i = x}(m) - dF_{M_i \mid T_i = 0, X_i = x}(m) \right\} dF_{X_i}(x), \tag{1}$$

$$\bar{\zeta}(t) = \int \int \left\{ \mathbb{E}(Y_i \mid M_i = m, T_i = 1, X_i = x) - \mathbb{E}(Y_i \mid M_i = m, T_i = 0, X_i = x) \right\} dF_{M_i \mid T_i = t, X_i = x}(m) dF_{X_i}(x), \tag{2}$$

where $\bar{\delta}(t)$ and $\bar{\zeta}(t)$ are the average causal mediation and average (natural) direct effects, respectively, and (Y_i, M_i, T_i, X_i) represents the observed outcome, mediator, treatment, and pre-treatment covariates. The sequential ignorability assumption states that the observed mediator status is as if randomly assigned conditional on the randomized treatment variable and the pre-treatment covariates. Causal mediation analysis under this assumption requires two statistical models; one for the mediator $f(M_i \mid T_i, X_i)$ and the other for the outcome variable $f(Y_i \mid T_i, M_i, X_i)$. (Note that we use the empirical distribution of X_i to approximate F_{X_i} .) Once these models are chosen and fitted by researchers, then **mediation** will compute the estimated causal mediation and other relevant estimates using the algorithms proposed in Imai et^*al . (2010b). The algorithms also produce uncertainty estimates such as standard errors and confidence intervals, based on either a nonparametric bootstrap procedure (for parametric or nonparametric models) or a quasi-Bayesian Monte Carlo approximation (for parametric models).

Figure 1 graphically illustrates the three steps required for a mediation analysis. The first step is to fit the mediator and outcome models using, for example, regression models with the usual 1m or glm functions. In the second step, the analysts takes the output objects from these models, which in Figure 1 we call model.m and model.y, and use them as inputs for the main function, mediate.

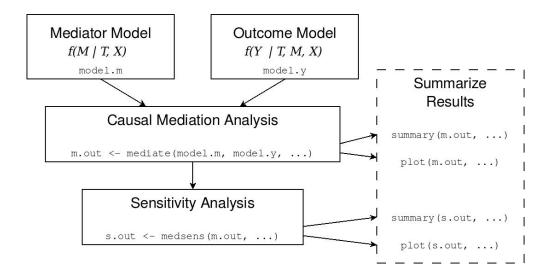


Figure 1: The Diagram Illustrating the Use of the Software **mediation**. Users first fit the mediator and outcome models. Then, the function **mediate** conducts causal mediation analysis while **medsens** implements sensitivity analysis. The functions **summary** and **plot** help users interpret the results of these analyses.

This function then estimates the causal mediation effects, direct effects, and total effect along with their uncertainty estimates. Finally, sensitivity analysis can be conducted via the function medsens which takes the output of mediate as an input. For these outputs, there are both summary and plot methods to display numerical and graphical summaries of the analyses, respectively.

3.2 Estimation of the Causal Mediation Effects

Estimation of the causal mediation effects is based on Algorithms 1 and 2 of Imai et al. (2010b). These are general algorithms in that they can be applied to any parametric (Algorithm 1 or 2) or semi/nonparametric models (Algorithm 2) for the mediator and outcome variables. Here, we briefly describe how these algorithms have been implemented in **mediation** by taking advantage of the object-oriented nature of **R** programming language.

Algorithm^{*}1 for Parametric Models. We begin by explaining how to implement Algorithm^{*}1 of Imai et al. (2010b) for standard parametric models. First, analysts fit parametric models for the mediator and outcome variables. That is, we model the observed mediator M_i given the treatment T_i and pre-treatment covariates X_i . Similarly, we model the observed outcome Y_i given the treatment, mediator, and pre-treatment covariates. For example, to implement the Baron-Kenny procedure in **mediation**, linear models are fitted for both the mediator and outcome models using the 1m command.

The model objects from these two parametric models form the inputs for the mediate function. The user must also supply the names for the mediator and outcome variables along with how many simulations should be used for inference, and whether the mediator variable interacts with the treatment variable in the outcome model. Given these model objects, the estimation proceeds by simulating the model parameters based on their approximate asymptotic distribution (i.e., the multivariate normal distribution with the mean equal to the parameter estimates and the variance equal to the asymptotic variance estimate), and then computing causal mediation effects of interest for each parameter draw (e.g., using equations (1) and (2) for average causal mediation and (natural) direct effects, respectively). This method of inference can be viewed as an approximation to the Bayesian posterior distribution due to the Bernstein-Von Mises Theorem (King et al. 2000). The advantage of this procedure is that it is relatively computationally efficient (when compared to Algorithm 2).

We take advantage of the object-oriented nature of **R** programming language at several steps in the function mediate. For example, the functions like coef and vcov are useful for extracting the point and uncertainty estimates from the model objects to form the multivariate normal distribution from which the parameter draws are sampled. In addition, the computation of the estimated causal mediation effects of interest requires the prediction of the mediator values under different treatment regimes as well as the prediction of the outcome values under different treatment and mediator values. This can be done by using model.frame to set the treatment and/or mediator values to specific levels while keeping the values of the other variables unchanged. We then use the model.matrix and matrix multiplication with the distribution of simulated parameters to compute the mediation and direct effects. The main advantage of this approach is that it is applicable to a wide range of parametric models and allows us to avoid coding a completely separate function for different models.

Algorithm² for Non/Semiparametric Inference. The disadvantage of Algorithm¹ is that it cannot be easily applied to non/semiparametric models. For such models, Algorithm², which is based on nonparametric bootstrap, can be used although it is more computationally intensive. Algorithm² may also be used for the usual parametric models which may be useful since mediation effects are known to have skewed distributions (e.g., Mackinnon et al. 2004; Preacher and Hayes 2008). Specifically, in Algorithm², we resample the observed data with replacement. Then, for each of bootstrapped samples, we fit both the outcome and mediator models and compute the quantities of interest. As before, the computation requires the prediction of the mediator values under different treatment regimes as well as the prediction of the outcome values under different treatment and mediator values. To take advantage of the object-oriented nature of the R language, Algorithm² relies on the predict function to compute these predictions, while we again manipulate the treatment and mediator status using the model.frame function. This process is repeated a large number of times and returns a bootstrap distribution of the mediation, direct, and total effects. We use the percentiles of the bootstrap distribution for confidence intervals. Thus, Algorithm² allows analysts to estimate mediation effects with more flexible model specifications or to estimate mediation effects for quantiles of the distribution.

3.3 Sensitivity Analysis

Causal mediation analysis relies on the sequential ignorability assumption that cannot be directly verified with the observed data. The assumption implies that the treatment is ignorable given

the observed pre-treatment confounders and that the mediator is ignorable given the observed treatment and the observed pre-treatment covariates. In order to probe the plausibility of such a key identification assumption, analysts must perform a sensitivity analysis (Rosenbaum 2002). Unfortunately, it is difficult to construct a sensitivity analysis that is generally applicable to any parametric or nonparametric model. Thus, Imai et al. (2010c, b) develop sensitivity analyses for commonly used parametric models, which we implement in **mediation**.

The Baron-Kenny Procedure. Imai et~al. (2010c) develop a sensitivity analysis for the Baron-Kenny procedure and Imai et~al. (2010b) generalize it to the linear structural equation model (LSEM) with an interaction term. This general model is given by,

$$M_i = \alpha_2 + \beta_2 T_i + \xi_2^\top X_i + \epsilon_{i2}, \tag{3}$$

$$Y_i = \alpha_3 + \beta_3 T_i + \gamma M_i + \kappa T_i M_i + \xi_3^{\top} X_i + \epsilon_{i3}, \tag{4}$$

where the sensitivity parameter is the correlation between ϵ_{i2} and ϵ_{i3} , which we denote by ρ . Under sequential ignorability, ρ is equal to zero and thus the magnitude of this correlation coefficient represents the departure from the ignorability assumption (about the mediator). Note that the treatment is assumed to be ignorable as it would be the case in randomized experiments where the treatment is randomized but the mediator is not. Theorem 2 of Imai et al. (2010b) shows how the average causal mediation effects change as a function of ρ .

To obtain the confidence intervals for the sensitivity analysis, we apply the following iterative algorithm to equations (3) and (4) for a fixed value of ρ . At the tth iteration, given the current values of the coefficients, i.e., $\theta^{(t)} = (\alpha_2^{(t)}, \beta_2^{(t)}, \xi_2^{(t)}, \alpha_3^{(t)}, \beta_3^{(t)}, \xi_3^{(t)}, \gamma^{(t)}, \kappa^{(t)})$, and a given error correlation ρ , we compute the variance-covariance matrix of $(\epsilon_{i2}, \epsilon_{i3})$, which is denoted by $\Sigma^{(t)}$. The matrix is computed by setting $\sigma_j^{(t)^2} = \|\hat{\epsilon}_j^{(t)}\|^2/(n-L_j)$ and $\sigma_{23}^{(t)} = \rho \sigma_2^{(t)} \sigma_3^{(t)}$, where $\hat{\epsilon}_j^{(t)}$ is the residual vector and L_j is the number of coefficients for the mediator model (j=2) and the outcome model (j=3) at the tth iteration. We then update the parameters via generalized least squares, i.e.,

$$\theta^{(t+1)} = \{ V^{\top} (\Sigma^{(t)^{-1}} \otimes I_n) V \}^{-1} V^{\top} (\Sigma^{(t)^{-1}} \otimes I_n) W$$

where $V = \begin{bmatrix} \mathbf{1} & T & X & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{1} & T & M & TM & X \end{bmatrix}, W = \begin{bmatrix} M \\ Y \end{bmatrix}, T = (T_1, \dots, T_n)^\top, M = (M_1, \dots, M_n)^\top,$ and $Y = (Y_1, \dots, Y_n)^\top$ are column vectors of length n, and $X = (X_1, \dots, X_n)^\top$ are the $(n \times K)$ matrix of observed pre-treatment covariates, and \otimes represents the Kronecker product. We typically use equation-by-equation least squares estimates as the starting values of θ and iterate these two steps until convergence. This is essentially an application of the iterative feasible generalized least square (FGLS) algorithm of the seemingly unrelated regression (Zellner 1962), and thus the asymptotic variance of $\hat{\theta}$ is given by $\operatorname{Var}(\hat{\theta}) = \{V^\top (\Sigma^{-1} \otimes I_n)V\}^{-1}$. Then, for a given value of ρ , the asymptotic variance of the estimated average causal mediation effects is found, for example, by the Delta method and the confidence intervals can be constructed.

The Binary Outcome Case. The sensitivity analysis for binary outcomes parallels the case when both the mediator and outcome are continuous. Here, we assume that the model for the

outcome is a probit regression. Using a probit regression for the outcome allows us to assume the error terms are jointly normal with a possibly non-zero correlation ρ . Imai $et^{\sim}al$. (2010b) derive the average causal mediation effects as a function of ρ and a set of parameters that are identifiable due to randomization of the treatment. This lets us use ρ as a sensitivity parameter in the same way as in the Baron-Kenny procedure. For the calculation of confidence intervals, we rely on the quasi-Bayesian approach of Algorithm 1 by approximating the posterior distribution with the sampling distribution of the maximum likelihood estimates.

The Binary Mediator Case. Finally, a similar sensitivity analysis can also be conducted in a situation where the mediator variable is dichotomous and the outcome is continuous. In this case, we assume that the mediator can be modeled as a probit regression where the error term is independently and identically distributed as standard normal distribution. A linear normal regression with error variance equal to σ_3^2 is used to model the continuous outcome variable. We further assume that the two error terms jointly follow a bivariate normal distribution with mean zero and covariance $\rho\sigma_3$. Then, as in the other two cases, we use the correlation between the two error terms ρ as the sensitivity parameter. Imai $et\tilde{\ \ }al.$ (2010b) show that under this setup, the causal mediation effects can be expressed as a function of the model parameters that can be consistently estimated given a fixed value of ρ . Uncertainty estimates are computed based on the quasi-Bayesian approach, as in the binary outcome case. The results can be graphically summarized via the plot function in a manner similar to the other two cases.

Alternative Interpretations Based on R^2 The main advantage of using ρ as a sensitivity parameter is its simplicity. However, applied researchers may find it difficult to interpret the magnitude of this correlation coefficient. To overcome this limitation, Imai et^*al . (2010c) proposed alternative interpretations of ρ based on the coefficients of determination or R^2 and Imai et^*al . (2010b) extended them to the binary mediator and binary outcome cases. In that formulation, it is assumed that there exists a common unobserved pre-treament confounder in both mediator and outcome models. Applied researchers are then required to specify whether the coefficients of this unobserved confounder in the two models have the same sign or not; i.e., $sgn(\lambda_2\lambda_3) = 1$ or -1 where λ_2 and λ_3 are the coefficients in the mediator and outcome models, respectively. Once this information is provided, the average causal mediation effect can be expressed as the function of "the proportions of original variances explained by the unobserved confounder" where the original variances refer to the variances of the mediator and the outcome (or the variance of latent variable in the case of binary dependent variable). This allows researchers to quantify how large the unobserved confounder must be (relative to the observed pre-treatment covariates in the model) in order for the original conclusions to be reversed.

Sensitivity Analyses with Respect to the Average Direct Effects. In addition to the above procedures for the average causal mediation effects, an analogous sensitivity analysis can also be conducted for the average direct effects using the medsens function. This is possible because it can be shown that the average direct effects are also expressed as a function of ρ in any of the above three cases. First, when both the mediator and outcome variables are continuous and modelled

	Outcome Model Types						
$Mediator\ Model\ Types$	Linear	GLM	Ordered	Censored	Quantile	Semiparametric	
Linear (lm)	√	✓	√*	✓	✓	√ *	
GLM (probit etc. via glm)	\checkmark	\checkmark	√ *	\checkmark	\checkmark	√ *	
Ordered (polr)	\checkmark	\checkmark	√ *	\checkmark	\checkmark	√ *	
Censored (tobit via vglm)	-	-	-	-	-	-	
Quantile (rq)	√ *	√ *	√ *	√ *	√ *	√ *	
Semiparametric (gam)	√ *	√ *	√ *	√ *	√ *	√ *	

Table 1: The Types of Models That Can be Handled by mediate for the Estimation of Causal Mediation Effects. Stars (*) indicate the model combinations that can only be estimated using the nonparametric bootstrap (i.e. with boot = TRUE).

using linear structural equations, the iterative FGLS algorithm given above can be used to estimate the model coefficients and both the point and interval estimates of the average direct effects can be obtained using the formulas given by Imai et al. (2010c, Section 4.1) and Imai et al. (2010b, p.314 and Appendix A). Second, when the mediator is binary and modelled using the probit regression, the average direct effect is given by $\bar{\zeta}(t) = \beta_3 + \kappa \mathbb{E}\{\Phi(\alpha_2 + \beta_2 t + \xi_2^\top X_i)\}$ using the same notation as Imai et al. (2010b, footnote 12), where all of the parameters, $(\alpha_2, \beta_2, \xi_2, \beta_3, \kappa)$, are identified and consistently estimated using the same procedure. Finally, for the binary outcome case, the average direct effect is identified given a value of ρ and expressed as $\bar{\zeta}(t) = \mathbb{E}\{\Phi(\alpha_1 + \beta_1 t + \xi_1^\top X_i + \beta_3(1 - t)/\sqrt{\gamma^2\sigma_2^2 + 2\gamma\rho\sigma_2 + 1}) - \Phi(\alpha_1 + \beta_1 t + \xi_1^\top X_i - \beta_3 t/\sqrt{\gamma^2\sigma_2^2 + 2\gamma\rho\sigma_2 + 1})\}$, which can be estimated via the same procedure as described in Appendix H of Imai et al. (2010b). The medsens function uses these procedures for sensitivity analyses for the average direct effects.

3.4 Current Limitations

Our software, **mediation**, is quite flexible and can handle many of the model types that researchers are likely to use in practice. Table 1 categorizes the types of the mediator and outcome models and lists whether **mediation** can produce the point and uncertainty estimates of causal mediation effects. For example, while **mediation** can estimate average causal mediation effects for censored outcomes with the tobit model, it has not yet been extended to cases involving censored mediators. In addition, **mediate** can be used with common generalized linear models (GLMs) such as binary logit and probit, Poisson and gamma regression models, but it cannot be used with binomial mediator models with multiple trials.

In each situation handled by **mediation**, it is possible to have an interaction term between treatment status and the mediator variable, in which case the estimated quantities of interest will be reported separately for the treatment and control groups.

Our software provides a convenient way to probe the sensitivity of results to potential violations of the ignorability assumption for certain model types. The sensitivity analysis requires the specific derivations for each combination of models, making it difficult to develop a general sensitivity analysis method. As summarized in Table 2, mediation can handle several cases that are likely

	Outcome Model Types		
Mediator Model Types	Linear	Binary Probit	
Linear	✓	✓	
Binary Probit	\checkmark	-	

Table 2: The Types of Models That Can Be Handled by medsens for Sensitivity Analysis.

to be encountered by applied researchers in practice. When the mediator is continuous, then sensitivity analysis can be conducted with continuous and binary outcome variables. In addition, when the mediator is binary, sensitivity analysis is available for continuous outcome variables. For sensitivity analyses that combine binary or continuous mediators and outcomes, analysts must use a probit regression model with a linear regression model. It should be noted that unlike the estimation of causal mediation effects, sensitivity analysis with treatment/mediator interactions can only be done for the continuous outcome/continuous mediator and continuous outcome/binary mediator cases. In the future, we hope to expand the range of models that are available for sensitivity analysis.

4 Examples

Next, we provide several examples to illustrate the use of **mediation** for the estimation of causal mediation effects and sensitivity analysis. The data used is available as part of the package so that readers can replicate the results reported below. We demonstrate the variety of models that can be used for the outcome and mediating variables.

Before presenting our examples, we load the **mediation** library and the example data set included with the library.

```
R> library("mediation")
mediation: R Package for Causal Mediation Analysis
Version: 3.0
R> data("jobs")
```

This dataset is from the Job Search Intervention Study (JOBS II) (Vinokur and Schul 1997). In the JOBS II field experiment, 1,801 unemployed workers received a pre-screening questionnaire and were then randomly assigned to treatment and control groups. Those in the treatment group participated in job-skills workshops. Those in the control condition received a booklet describing job-search tips. In follow-up interviews, two key outcome variables were measured; a continuous measure of depressive symptoms based on the Hopkins Symptom Checklist (depress2), and a binary variable representing whether the respondent had become employed (work1). In the JOBS II data, a continuous measure of job-search self-efficacy represents a key mediating variable (job_seek). In addition to the outcome and mediators, the JOBS II data also include the following list of baseline covariates that were measured prior to the administration of the treatment: pre-treatment level of depression (depress1), education (educ), income, race (nonwhite),

marital status (marital), age, sex, previous occupation (occp), and the level of economic hardship (econ_hard).

4.1 Estimation of Causal Mediation Effects

The Baron-Kenny Procedure. We start with an example when both the mediator and the outcome are continuous. In this instance, the results from either algorithm will return point estimates essentially identical to the usual Baron and Kenny procedure though the quasi-Bayesian or nonparametric bootstrap approximation is used. Using the JOBS II data, we first estimate two linear regressions for both the mediator and the outcome using the lm function.

These two model objects, model.m and model.y, become the arguments for the mediate function. When different data frames are used for these two models, the mediate function internally refits them using a merged dataset if the dropobs argument is set to TRUE; otherwise an error message is returned.

In the first call to mediate below, we specify boot = TRUE to call the nonparametric bootstrap with 1000 resamples (sims = 1000). When this option is set to FALSE in the second call, inference proceeds via the quasi-Bayesian Monte Carlo approximation using Algorithm~1 rather than Algorithm~2. In this case, heteroskedasticity-robust standard errors can be used for the calculation of confidence intervals for some types of models by setting the robustSE argument to TRUE. Finally, we must also specify the variable names for the treatment indicator and the mediator variable using treat and mediator, respectively.

The objects from a call to mediate, i.e., out.1 and out.2 above, are lists of class "mediate" which contain several different quantities from the analysis. For example, out.1\$d0 returns the point estimate for the average causal mediation effect based on Algorithm~1. The help file contains a full list of values that are contained in mediate objects.

The summary function prints out the results of the analysis in tabular form:

```
R> summary(out.2)
```

Causal Mediation Analysis

Quasi-Bayesian Confidence Intervals

Mediation Effect: -0.01375 95 % CI -0.031812 0.003299

Direct Effect: -0.03873 95 % CI -0.11938 0.04668 Total Effect: -0.05247 95 % CI -0.13431 0.03150

Proportion of Total Effect via Mediation: 0.2028 95 % CI -1.383 1.934

Sample Size Used: 899

The output from the summary function displays the estimates for the average causal mediation effect, direct effect, total effect, and proportion of total effect mediated. The first column displays the quantity of interest, the second column displays the point estimate, and the other columns present the confidence intervals at the level specified by the conf.level argument which defaults to 0.95. The number of observations used for the estimation is then displayed at the bottom. In this case, we find that job search self-efficacy mediated the effect of the treatment on depression in the negative direction. This effect, however, was small with a point estimate of -.014 and the 95% confidence interval (-.032, -.003) barely covers 0.

These results can be graphically presented by using the plot function:

```
R> plot(out.2)
```

The output is shown in Figure 2. The standard arguments for plot, such as titles (main, xlab, etc.) and line widths (lwd), can be used and behave as expected.

The Baron-Kenny Procedure with the Interaction Term. Analysts can also allow the causal mediation effect to vary with treatment status. Here, the model for the outcome must be altered by including an interaction term between the treatment indicator, treat, and the mediator variable, job_seek:

Causal Mediation Analysis

Quasi-Bayesian Confidence Intervals

```
Mediation Effect_0: -0.01899 95 % CI -0.045271 0.003649 Mediation Effect_1: -0.01203 95 % CI -0.029640 0.002195 Direct Effect_0: -0.03596 95 % CI -0.1187 0.0426 Direct Effect_1: -0.02899 95 % CI -0.10879 0.05082 Total Effect: -0.04799 95 % CI -0.13495 0.03154
```

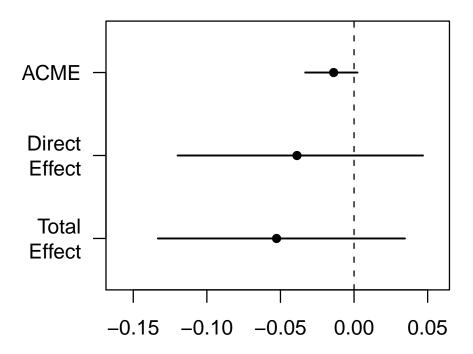


Figure 2: Graphical Summary of Causal Mediation Analysis.

```
Proportion of Total Effect via Mediation_0: 0.2912 95 % CI -3.386 2.707

Proportion of Total Effect via Mediation_1: 0.1823 95 % CI -1.994 2.018

Mediation Effect (Average): -0.01551 95 % CI -0.035757 0.003138

Direct Effect (Average): -0.03248 95 % CI -0.1129 0.0464

Proportion of Total Effect via Mediation (Average): 0.2381 95 % CI -2.867 2.443
```

Sample Size Used: 899

Again using the summary function provides a table of the results. Now estimates for the mediation effects, direct effects and proportion of total effect mediated correspond to the levels of the treatment and are printed as such in the tabular summary. In this case, the mediation effect under the treatment condition, listed as Mediation Effect_1 is estimated to be -.012 while the mediation effect under the control condition, Mediation Effect_0, is -.019. The bottom of the table shows the overall summary of these quantities averaged over the two treatment levels, as well as the number of data points.

When using the plot function on a mediate object with interactions, one can select which treatment condition to plot the estimated effects for by specifying the treatment argument. The

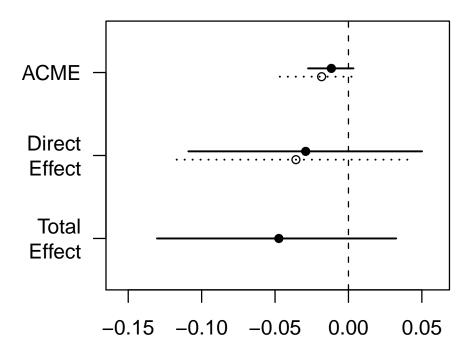


Figure 3: Causal Mediation Analysis with Interaction between Treatment and Mediator.

default is to plot both estimates, which is equivalent to setting treatment to "both":

```
R> plot(out.3, treatment = "both")
```

The resulting plot is in Figure 3.

Use of Non/Semi-parametric Regression. The flexibility of mediation becomes readily apparent when we move beyond standard linear regression models. For example, we might suspect that the mediator has a nonlinear effect on the outcome. Generalized Additive Models (GAMs) allow analysts to use splines for flexible nonlinear fits. This presents no difficulties for the mediate function. We model the mediator as before, but we alter the outcome model using the gam function from the mgcv library.

In this case we fit a Generalized Additive Model for the outcome variable, but allow the effect of the job_seek variable to be non-linear and determined by the data. This is done by using the s notation which allows the fit between the mediator and the outcome to be modeled with a spline. Using the spline for the fit allows the estimate for the mediator on the outcome to be a series of piecewise polynomial regression fits. This semiparametric regression model is a more general version of nonparametric regression models such as lowess. The model above allows the estimate to vary across the range of the predictor variable. Here, we specify the model with a cubic basis function (bs = "cr") for the smoothing spline and leave the smoothing selection to be done at the program defaults which is generalized cross-validation. Fully understanding how to fit such models is beyond the scope here. Interested readers should consult Wood (2006) for full technical details and Keele (2008) provides coverage of these models from a social science perspective.

The call to mediate with a gam fit remains unchanged except that when the outcome model is a semiparametric regression only the nonparametric bootstrap is valid for calculating uncertainty estimates, i.e., boot = TRUE.

The model for the mediator can be modeled with the gam function as well. The gam function also allows analysts to include interactions; thus analysts can still allow the mediation effects to vary with treatment status. This simply requires altering the model specification by using the by option in the gam function and using two separate indicator variables for treatment status. To fit this model we need one variable that indicates whether the observation was in the treatment group and a second variable that indicates whether the observation was in the control group. To allow the mediation effect to vary with treatment status, the call to gam takes the following form:

In this case, we must also alter the options in the mediate function by providing the variable name for the control group indicator using the control option.

Causal Mediation Analysis

Confidence Intervals Based on Nonparametric Bootstrap

```
Mediation Effect_0: -0.02254 95 % CI -0.051956 0.004447
Mediation Effect_1: -0.0171 95 % CI -0.038895 0.002281
Direct Effect_0: -0.009742 95 % CI -0.09718 0.07924
```

Direct Effect_1: -0.004302 95 % CI -0.08926 0.08285

Total Effect: -0.02684 95 % CI -0.11932 0.06449

Proportion of Total Effect via Mediation_0: 0.3892 95 % CI -4.411 9.161

Proportion of Total Effect via Mediation_1: 0.2768 95 % CI -3.614 6.960

Mediation Effect (Average): -0.01982 95 % CI -0.045831 0.003105

Direct Effect (Average): -0.007022 95 % CI -0.09207 0.08178

Proportion of Total Effect via Mediation (Average): 0.3398 95 % CI -3.870 8.105

Sample Size Used: 899

Quantile Causal Mediation Effects. Researchers might also be interested in modeling mediation effects for quantiles of the outcome. Quantile regression allows for a convenient way to model the quantiles of the outcome distribution while adjusting for a variety of covariates (Koenker 2008). For example, a researcher might be interested in the 0.5 quantile (i.e., median) of the distribution. This also presents no difficulties for the mediate function. Again for these models, uncertainty estimates are calculated using the nonparametric bootstrap. To use quantile regression, we use the rq function in package quantreg and model the median of the outcome, though other quantiles are also permissible. Analysts can also relax the no-interaction assumption for the quantile regression models as well. Below we estimate the mediator with a standard linear regression, while for the outcome we use rq to model the median.

Causal Mediation Analysis

Confidence Intervals Based on Nonparametric Bootstrap

Mediation Effect: -0.01424 95 % CI -0.031317 0.002109

Direct Effect: -0.04165 95 % CI -0.12413 0.03538

Total Effect: -0.05589 95 % CI -0.14305 0.02377

Proportion of Total Effect via Mediation: 0.2042 95 % CI -2.003 2.707

Sample Size Used: 899

where the summary command gives the estimated median causal mediation effect along with the estimates for the other quantities of interest.

It is also possible to estimate mediation effects for quantiles of the outcome other than the median. This is done simply by specifying a different outcome quantile in the quantile regression model. For example, if the 10th percentile of the outcome were of interest, then the user can change tau option,

Furthermore, it is straightforward to loop over a set of quantiles and graph the mediation effects for a range of quantiles, as done in Imai et~al.~(2010b).

Discrete Mediator and Outcome Data. Often analysts use measures for the mediator and outcome that are discrete. For standard methods, this has presented a number of complications requiring individually tailored techniques. The **mediation** software, however, can handle a number of different discrete data types using the general algorithms developed in Imai et al. (2010b). For example, one outcome of interest in the JOBS II study is a binary indicator (work1) for whether the subject became employed after the training sessions. To estimate the mediation effect, we simply use a probit regression instead of a linear regression for the outcome and then call mediate as before,

Quasi-Bayesian Confidence Intervals

Causal Mediation Analysis

```
Mediation Effect_0: 0.003290 95 % CI -0.0009537 0.0098747

Mediation Effect_1: 0.003538 95 % CI -0.001052 0.010728

Direct Effect_0: 0.05514 95 % CI -0.006427 0.113568

Direct Effect_1: 0.05538 95 % CI -0.006487 0.114191

Total Effect: 0.05867 95 % CI -0.003816 0.117091
```

```
Proportion of Total Effect via Mediation_0: 0.0455 95 % CI -0.0768 0.4070

Proportion of Total Effect via Mediation_1: 0.05042 95 % CI -0.0777 0.4110

Mediation Effect (Average): 0.003414 95 % CI -0.001003 0.010269

Direct Effect (Average): 0.05526 95 % CI -0.006457 0.113879

Proportion of Total Effect via Mediation (Average): 0.04802 95 % CI -0.07725 0.41005
```

Sample Size Used: 899

In the table printed by the summary function, the estimated average causal mediation effect along with the quasi-Bayesian confidence interval are printed on the first line followed by the direct and total effects, and the proportion of the total effect due to mediation. Even though the outcome model does not include an interaction term between the treatment and mediator, the estimated effects slightly differ between the treatment and control conditions. This difference, however, is solely due to the nonlinearity in the outcome model and should be extremely small. It is also possible to use a logit model for the outcome instead of a probit model. However, we recommend the use of a probit model because our implementation of the sensitivity analysis below requires a probit model for analytical tractability.

The mediator can also be binary or ordered measures as well. This simply requires modeling the mediator with either a probit or ordered probit model. For demonstration purposes, the jobs data contains two variables, job_dich and job_disc, which are recoded versions of job_seek. The first measure is simply the continuous scale divided at the median into a binary variable. The second measure, job_disc, recodes the continuous scale into a discrete four point scale. We emphasize that this is for demonstration purposes only, and analysts in general should not recode continuous measures into discrete measures. Estimating mediation effects with a binary mediator is quite similar to the case above with a binary outcome. We simply now use a probit model for the mediator and a linear regression for the outcome,

In this example we include the interaction term between the treatment and mediator to allow the effect of the mediator to vary with treatment status. The user now calls mediate and can use either the quasi-Bayesian approximation or nonparametric bootstrap.

Causal Mediation Analysis

Quasi-Bayesian Confidence Intervals

```
Mediation Effect_0: -0.01823 95 % CI -0.038944 -0.002616

Mediation Effect_1: -0.02040 95 % CI -0.038965 -0.003155

Direct Effect_0: -0.02823 95 % CI -0.10786 0.05154

Direct Effect_1: -0.03039 95 % CI -0.11164 0.04764

Total Effect: -0.04863 95 % CI -0.13146 0.02839

Proportion of Total Effect via Mediation_0: 0.2782 95 % CI -3.055 3.325

Proportion of Total Effect via Mediation_1: 0.3162 95 % CI -3.443 3.628

Mediation Effect (Average): -0.01932 95 % CI -0.037878 -0.003201

Direct Effect (Average): -0.02931 95 % CI -0.11052 0.04807

Proportion of Total Effect via Mediation (Average): 0.301 95 % CI -3.016 3.477
```

Sample Size Used: 899

In the table, we see that Mediation Effect_0 is the mediation effect under the control condition, while Mediation Effect_1 is the mediation effect under the treatment condition. The same notation applies to the direct effects. As the reader can see, the output also indicates which algorithm is used for the 95% confidence intervals.

When the mediator is an ordered variable, we switch to an ordered probit model for the mediator. In **R**, the polr function in the MASS library provides this functionality. Thus, we fit the outcome and mediator models below,

The reader should note that in the call to polr the Hess = TRUE should be specified to compute the asymptotic variance covariance matrix for the estimated model coefficients in the quasi-Bayesian approximation. Otherwise, the Hessian of the log-likelihood will be recalculated within the mediate call.

Once we have estimated these two models, analysis proceeds as before,

Causal Mediation Analysis

Quasi-Bayesian Confidence Intervals

Mediation Effect: -0.01048 95 % CI -0.03188 0.01008

Direct Effect: -0.03311 95 % CI -0.10759 0.04848

Total Effect: -0.04360 95 % CI -0.12376 0.03895

Proportion of Total Effect via Mediation: 0.1726 95 % CI -2.752 2.077

Sample Size Used: 899

Again, for any of these data types, analysts can relax the no-interaction assumption as before by including the interaction between treatment and the mediator variable in the outcome model.

4.2 Sensitivity Analysis

Once analysts have estimated mediation effects, they should explore how robust their finding is to the ignorability assumption, whenever possible. The medsens function allows analysts to conduct sensitivity analyses for mediation effects as well as direct effects. In this section we provide a demonstration of these functionalities. Currently, mediation can conduct sensitivity analyses when both mediator and outcome are continuous and modelled with the lm function, as well as when either mediator or outcome (but not both) is binary and modelled using a binary probit regression via glm.

The Baron-Kenny Procedure. As before, one must first fit models for the mediator and outcome and then pass these model objects through the mediate function:

Once the analyst estimates the mediation effects, the output from the mediate function becomes the argument for medsens, which is the workhorse function. The medsens function recognizes main arguments specified in the mediate function and thus there is no need to specify options such as treat or mediator.

```
R> sens.cont <- medsens(med.cont, rho.by = 0.05)
```

The rho.by option specifies how finely incremented the parameter ρ is for the sensitivity analysis. When ρ is on a coarser grid, this speeds up estimation considerably but comes at the cost of estimating the robustness of the original conclusion only imprecisely.

After running the sensitivity analysis via medsens, the summary function can be used to produce a table with the values of ρ for which the confidence interval contains zero. This allows the analyst to immediately see the approximate range of ρ where the sign of the causal mediation effect is indeterminate. The second section of the table contains the value of ρ for which the mediation effect is exactly zero, which in this application is -0.19. The table also presents coefficients of determination that correspond to the critical value of ρ where the mediation effect is zero. First, $R^*_M^2 R^*_Y^2$ is the product of coefficients of determination which represents the proportion of the previously unexplained variance in the mediator and outcome variables that is explained by an unobservable pretreatment unconfounder. An alternative formulation is in terms of the proportion of the original variance explained by an unobserved confounder, which we denote as $\widetilde{R}_M^2 \widetilde{R}_Y^2$.

R> summary(sens.cont)

Mediation Sensitivity Analysis for Average Causal Mediation Effect

Sensitivity Region

Rho Med. Eff. 95% CI Lower 95% CI Upper R^2_M*R^2_Y* R^2_M~R^2_Y~

[14,] -0.30	0.0064	-0.0025	0.0153	0.0900	0.0588
[15,] -0.25	0.0028	-0.0026	0.0082	0.0625	0.0408
[16,] -0.20	-0.0007	-0.0049	0.0036	0.0400	0.0261
[17,] -0.15	-0.0040	-0.0105	0.0025	0.0225	0.0147

Rho at which ACME = 0: -0.2

 $R^2_M*R^2_Y*$ at which ACME = 0: 0.04

 $R^2_M^2 = 0:0.0261$

The table above presents the estimated mediation effect along with its confidence interval for each value of ρ . The reader can verify that when ρ is equal to zero, the reported mediation effect matches the estimate produced by the **mediate** function. For other values of ρ , the mediation effect is calculated under different levels of unobserved confounding.

The information from the sensitivity analysis can also be summarized graphically using the plot function. First, passing the medsens object to plot and specifying the sens.par option to "rho", i.e.,

R> plot(sens.cont, sens.par = "rho")

produces the left hand side of Figure 4. In the plot, the dashed horizontal line represents the estimated mediation effect under the sequential ignorability assumption, and the solid line represents the mediation effect under various values of ρ . The grey region represents the 95% confidence bands.

Similarly, we can also plot the sensitivity analysis in terms of the coefficients of determination as discussed above. Here we specify sens.par option to "R2". We also need to specify two additional pieces of information. First, r.type option tells the plot function whether to plot $R^*_M R^*_Y$ or $\widetilde{R}_M^2 \widetilde{R}_Y^2$. To plot the former r.type is set to "residual" and to plot the latter r.type is set to "total". Finally, the sign.prod option specifies the sign of the product of the coefficients of the unobserved confounder in the mediator and outcome models. This product indicates whether the unobserved confounder affects both mediator and outcome variables in the same direction ("positive") or different directions ("negative"), thereby reflecting the analyst's expectation about the nature of confounding.

For example, the following command produces the plot representing the sensitivity of estimates with respect to the proportion of the original variances explained by the unobserved confounder when the confounder is hypothesized to affect the mediator and outcome variables in opposite directions.

```
R> plot(sens.cont, sens.par = "R2", r.type = "total", sign.prod = "negative")
```

The resulting plot is shown on the right hand side of Figure 4. Each contour line represents the mediation effect for the corresponding values of \widetilde{R}_M^2 and \widetilde{R}_Y^2 . For example, the 0 contour line corresponds to values of the product $\widetilde{R}_M^2\widetilde{R}_Y^2$ such that the ACME is 0. As reported in the table, even a small proportion of original variance unexplained by the confounder, .02%, produces mediation effects of 0. Accordingly, the right hand side of Figure 4 shows how increases in $\widetilde{R}_M^2\widetilde{R}_Y^2$ (moving from the lower left to upper right) produce positive mediation effects.

For both types of sensitivity plots, the user can specify additional options available in the plot function such as alternative title (main) and axis labels (xlab, ylab) or manipulate common graphical options (e.g., xlim).

Binary Outcome. The medsens function also extends to analyses where the mediator is binary and the outcome is continuous, as well as when the mediator is continuous and the outcome is binary. If either variable is binary, medsens takes an additional argument. For example, recall the binary outcome model estimated earlier:

The call to medsens works as before, with the output from the mediate function passed through medsens.

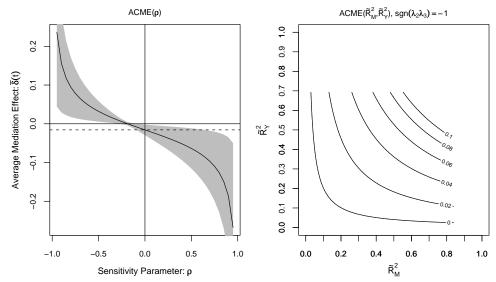


Figure 4: Sensitivity Analysis with Continuous Outcome and Mediator.

```
R> sens.bout <- medsens(med.bout, rho.by = 0.05, sims = 1000)
```

The sims option provides control over the number of Monte Carlo draws used to compute confidence bands. When either the mediator or outcome is binary, the exact values of sensitivity parameters where the mediation effects are zero cannot be analytically obtained as in the fully continuous case (see Imai et al. 2010c, Section 4). Thus, this information is reported based on the signs of the estimated mediation effects under various values of ρ and corresponding coefficients of determination. The usage of the summary function, however, remains identical to the fully continuous case in that the output table contains the estimated mediation effects and the corresponding values of ρ for which the confidence region contains zero.

As in the case with continuous mediator and outcome variables, we can plot the results of the sensitivity analysis. The following code produces Figure 5.

```
R> plot(sens.bout, sens.par = "rho")
R> plot(sens.bout, sens.par = "R2", r.type = "total", sign.prod = "positive")
```

On the left hand side we plot the ACME in terms of ρ , while we plot the ACME in terms of \widetilde{R}_M^2 and \widetilde{R}_Y^2 on the right hand side. In the ρ plot, the dashed line represents the estimated mediation effect under sequential ignorability, and the solid line represents the mediation effect under various values of ρ . The grey region represents the 95% confidence bands. In the \widetilde{R}^2 plot the ACME is plotted against various values of \widetilde{R}_M^2 and \widetilde{R}_Y^2 and is interpreted in the same way as above.

When the outcome is binary, the proportion of the total effect due to mediation can also be calculated as function of the sensitivity parameter ρ . The pr.plot option in the plot command (in conjunction with the sens.par = "rho" option) allows users to plot a summary of the sensitivity analysis for the proportion mediated. For example, the following call would provide a plot of this quantity:

```
R> plot(sens.bout, sens.par = "rho", pr.plot = TRUE)
```

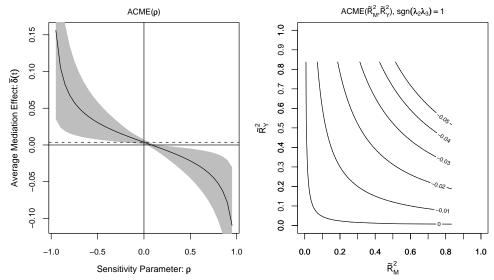


Figure 5: Sensitivity Analysis with Continuous Outcome and Binary Mediator.

Binary Mediator. The final form of sensitivity analysis deals with the case where the outcome variable is continuous but the mediator is binary. For the purpose of illustration, we simply dichotomize the job_seek variable to produce a binary measure job_dich. We fit a probit model for the mediator and linear regression for the outcome variable.

Again we can pass the output of the medsens function through the plot function,

```
R> plot(sens.bmed, sens.par = "rho")
```

producing Figure 6. The plot is interpreted in the same way as the above cases. The user also has the option to plot sensitivity results in terms of the coefficients of determination just as in the case with continuous outcome and mediator variables.

When the mediator variable is binary, the plotted values of the mediation effect and their confidence bands may not be perfectly smooth curves due to simulation errors. This is especially likely when the number of simulations (sims) is set to a small value. In such situations, the user can choose to set the smooth.effect and smooth.ci options to TRUE in the plot function so that the corresponding values become smoothed out via a lowess smoother before being plotted. Although this option often makes the produced graph look nicer, the user should be cautious as the adjustment could affect one's substantive conclusions in a significant way. A recommended alternative is to increase the number of simulations.

$ACME(\rho)$

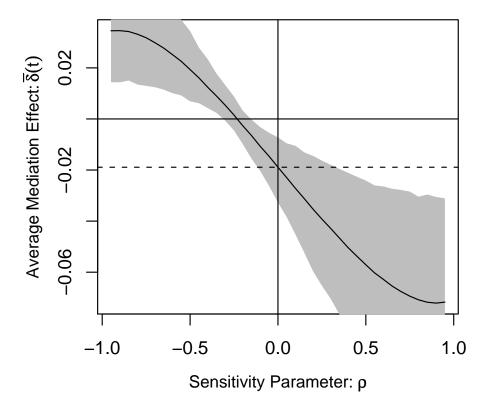


Figure 6: Sensitivity Analysis with Continuous Outcome and Binary Mediator.

5 Multiple Causal Mediation Analyses via mediations

Researchers may face a situation where they want to conduct multiple causal mediation analyses. For example, the researcher may have run several different experiments that had different treatment conditions but had the same mediator and outcome variables. Or, a researcher may measure several different mediating variables in their experiment and wish to estimate causal mediation effects for each of these cases. In these situations the researcher would need to write separate lines of code for the different models. A more efficient way is to loop over the different combinations of interest. The mediations function facilitates this process.

The mediations function can be used to conduct causal mediation analyses over the range of treatment, mediator, and outcome combinations that could be present within a study. For example, if there were two treatment conditions, two measured mediators, and two outcomes, mediations would run eight causal mediation analyses. The results can then be analyzed with the summary and plot functions. If there is only one treatment variable, the user needs only a single data set that contains all mediators and outcomes of interest. If there are multiple treatment variables, then the researcher must first create separate data frames, each with all mediator/outcome variables to be considered, and named using a convention where the name of the data frame object begins with the name of the treatment variable contained within it.

Use of the mediations function is straightforward. First, the user creates vectors of the treatment, mediator, outcome, and covariates names that are to be used. The treatment, mediator, and outcome variables are looped over to produce all possible combinations of mediator and outcome models. The set of covariates is held constant across the models. The different model combinations are then entered into the mediate function.

The user can specify several different options for mediations. First, the type of model to be used for the mediator and outcome equations must be specified. Currently, mediations can handle a variety of different model combinations. Either the mediator or outcome equation can be modeled with linear regression, probit, ordered probit, and quantile regression. The mediations function also handles the case where tobit is used for the outcome. Next, the user must also specify the standard features that are necessary for the mediate function, such as the number of simulations (sims). In addition, if quantile regression or tobit regression is used, the user needs to specify the appropriate parameters, such as the quantiles to be estimated (tau.m, tau.y) and cutpoints (LowerY, UpperY). If the user wishes for estimates to include weights (e.g., survey weights) then the name of the weight variable needs to be passed via the weights argument.

The output of mediations contains a collection of mediate objects. The naming system uses the name of the particular outcome variable, mediator, and treatment, each separated by a dot. For example, if the output of mediations is output and the outcome, mediator and treatment variable names 0, M1 or M2, and T, respectively, then output\$0.M2.T would be the mediate object from using mediator M2.

There are several limitations to the code. First, it works only with a subset of the model types that will be accommodated if mediate is used individually. Second, one cannot specify separate sets of covariates for different treatment/mediator/outcome combinations. Users should use mediate separately for individual models if more flexibility is required in their specific applications.

While mediations is a helpful function, it is also easy to abuse. First, researchers must be aware of the assumptions being made at every step of causal mediation analysis. For example, if there are multiple mediators, a strong assumption must be made for the estimates to be interpreted as causal quantities. One such assumption is that the mediators are not causally related. Second, care must be taken against the risks of multiple testing when a large number of treatment/mediator/outcome combinations are involved. The mediations function simply runs independent mediate processes and does not use any correction procedures for multiple testing, so the confidence intervals may be too narrow. We recommend that the use of this function be limited for exploratory analyses.

An illustration of the mediations function can be found in the Examples section of its help document; see ?mediations or example(mediations).

6 Concluding Remarks

Causal mediation analysis is a key tool for social scientific research. In this paper, we describe our easy-to-use software for causal mediation analysis, **mediation**, that implements the new methods and algorithms introduced by Imai, Keele, and Yamamoto (2010c) and Imai, Keele, and Tingley (2010b). The software provides a flexible, unified approach to causal mediation analysis in various

situations encountered by applied researchers. The object-oriented nature of the **R** programming made it possible for us to implement these algorithms in a fairly general way. In addition to the estimation of causal mediation effects, **mediation** implements formal sensitivity analyses so that researchers can assess the robustness of their findings to the potential violations of the key identifying assumption. This is an important contribution for at least two reasons. First, even in randomized experiments, causal mediation analysis requires an additional assumption that is not directly testable from the observed data. Thus, researchers must evaluate the consequences of potential violations of the assumption via sensitivity analysis. Second, the accumulation of such sensitivity analyses is essential for interpreting the relative degree of robustness across different studies. Thus, the development of easy-to-use software, such as **mediation**, facilitates causal mediation analysis in applied social science research in several critical directions.

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