# Processing Ecological Data in R with the mefa Package

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#### Abstract

mefa is an R package for multivariate data handling in ecology and biogeography. It provides object classes to represent the data coded by samples, taxa and segments (i.e., subpopulations, repeated measures). It supports easy processing of the data along with relational data tables for samples and taxa. An object of class 'mefa' is a project specific compendium of the dataset and can be easily used in further analyses. Methods are provided for extraction, aggregation, conversion, plotting, summary and reporting of 'mefa' objects. Reports can be generated in plain text or LATEX format. This paper presents worked examples on a variety of ecological analyses.

This vignette is based on the manuscript: Péter Sólymos, 2009, Processing Ecological Data in R With the mefa Package. *Journal of Statistical Software* 29(8), 1–28. http://www.jstatsoft.org/v29/i08/; processed with mefa 3.1-3 in R version 2.10.0 beta (2009-10-12 r50045) on October 13, 2009.

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## 1. Introduction

Fortunately, many packages are available for the analysis of ecological data in R (R Development Core Team 2008), e.g., the **ade4** (Thioulouse and Dray 2007), **labdsv** (Roberts 2007) and **vegan** (Oksanen *et~al.* 2008) packages among other more standard statistical packages e.g., **MASS** (Venables and Ripley 2002) and **stats** (R Development Core Team 2008). These, however, often require the multivariate data in the form of a matrix or data frame.

Extensive ecological data sets (with observations of multiple taxa at multiple locations) are not stored in crosstabulated format because most biodiversity data sets are sparse with matrix fill often lower than 30 percent. The conversion between data formats of biodiversity databases and ecological packages might require substantial work. Of course there are many possibilities for general data manipulation in R (Spector 2008). The **Hmisc** (Harrell Jr 2008), **reshape** (Wickham 2007), **simba** (Jurasinski 2007) and **labdsv** (Roberts 2007) packages contain functions for converting ecological data in database formats into crosstabulated data matrices, and vice versa.

When the problems are more complex (e.g., a survey spanning across multiple spatial or temporal scales), results are stored in several related data tables. Most multivariate methods require a matrix, whereas response modeling usually require data frame as input. The simultaneous manipulation and checking of the community data matrix and related data frames

can be time consuming with the standard tools.

The aim of the **mefa** R package is to provide standardized computational environment for specialist work in ecology and biogeography by bridging the gap between the data and the analysis, and reducing the time spent with data preprocessing. It provides object classes and methods for convenient manipulation of related data tables and can be used for generating reports in plain text or LATEX format.

The package name **mefa** is a short for *metafaunistics* indicating that data processing is a critical step prior to data analysis. The *faunistics* part refers to the study of the fauna of some territory or area, while the *meta* part refers to the procedures (data processing and analysis) beyond the data collection part of the scientific endeavor. Of course, the package intends to be more general than covering only faunistics. It can be useful when dealing with almost all kinds of organisms that can be counted or measured, including microorganisms, fungi and plants as well.

Compared to previous versions (< 2.0; Sólymos 2008), the package has been extensively rewritten to enhance efficiency and speed, and with a focus on methods, but the data model remained the same. A stable version of the package is available under the terms of the General Public License from the Comprehensive R Archive Network (CRAN, http://CRAN. R-project.org/package=mefa), developmental version is available at the R-Forge (http://mefa.R-Forge.R-project.org/).

In this paper I outline the motivation and the general idea behind the package, and I describe the structure of the object classes. A real-world data set is used to demonstrate the methods in the package and the use of objects in further data analysis.

# 2. Example dataset

The "Dolina 2007" survey was aimed to discover the soil and litter dwelling macroinvertebrates (land snails, and terrestrial isopods) with special respect to microhabitat characteristics. We have surveyed dolines (sinkholes, karstic depressions) at the Alsó-hegy plateau of the Aggtelek National Park, North Hungary, August, 2007. These dolines were mainly covered by hornbeam and beech, and were 0.5–2 hectares in extent. The dolines contained keystone habitat elements i.e., large pieces of coarse woody debris and different rock formations.

We collected invertebrates from four different microhabitats (<u>L</u>itter, live <u>W</u>ood, <u>D</u>ead wood as an equivalent for coarse woody debris, and  $\underline{R}$ ock<sup>1</sup>) with at least three replicates per microhabitat per doline. We collected 1 L of litter per replicate ("quadrat" method for short) and employed a time restricted search ("time" method, five minutes per replicate) in a 1 m radius around the litter sample location. Litter samples were taken from the bottom of live trees, dead trees and rocks (Kemencei et al. 2008; Vilisics et al. 2008).

Here I will use the data of land snails from the first dolina only, that is provided with the package (dataset dol.count). Samples are named after the microhabitat, the applied method and a number for replication. Snails were identified to species and categorized according to extent of shell decay. Four letter short names were used to refer to species. Live animals and fresh shells constituted the "fresh" group. Whitened, decayed and broken shells constituted

<sup>&</sup>lt;sup>1</sup>Underlined letters indicate the notation used for first characters of sample names. Second characters stand for sampling methods, and thirds are the replicate numbers. The first quadrat and timed samples from the rock microhabitat are RQ1 and RT1, respectively.

the "broken" group. Shell decay stages formed the segments in the data set for further analyses.

A data frame containing microsite characteristics of the samples and the applied methods is provided in the dataset dol.samp. Characteristics (nomenclature, taxonomy, adult shell dimension) of the snail species are in the dataset dol.taxa and are based on (Kerney et~al. 1983). The full dataset along with the code showing how it was extracted from the full dataset is available on the Dataverse Network (Sólymos and Kemencei 2008).

## 3. Motivation

Load the package and the example data set (showing only the first 16 rows out of 297)<sup>2</sup>:

```
R> library("mefa")
```

mefa 3.1-3 2009-10-12

R> data("dol.count")

R> head(dol.count, 16)

	samp	taxa	${\tt count}$	segm
1	LQ1	aacu	1	fresh
2	LQ1	amin	1	broken
3	LQ1	amin	2	fresh
4	LQ1	dper	1	broken
5	LQ1	ffau	1	broken
6	LQ1	рруд	13	fresh
7	LQ1	рруд	15	broken
8	LT1	zero.pseudo	0	zero.pseudo
9	LQ2	aacu	1	fresh
10	LQ2	amin	1	broken
11	LQ2	dper	1	fresh
12	LQ2	рруд	5	fresh
13	LQ2	рруд	8	broken
14	LQ2	pvic	1	broken
15	LT2	amin	1	fresh
16	LT2	pvic	1	broken

This is a typical format for biodiversity datasets, where the samp column represents the observational units (samples). In planned ecological field experiments and surveys these units are expected to be comparable in terms of sampling effort. However, when data came from unplanned field observations, samples are often not comparable but refer to an observation, or set of individuals collected from a given location, by a given person in a given time.

The taxa column refers to the taxonomic identity of the individuals found in a given sample. The taxonomic resolution might vary due to expert knowledge and development stage of the

<sup>&</sup>lt;sup>2</sup>The package demo (demo(mefa, package = "mefa")) and vignette (vignette("mefa", package = "mefa")) can help to go through the procedures presented in this paper.

individuals. When an actual sample did not contain individuals, it is convenient to refer to this situation by a pseudo-species (here, it is named as "zero.pseudo") indicating that 0 individuals were found in the sample coded as LT1 (first replicate from the litter microhabitat collected by timed search).

The count column contains the outcome of the field experiment, the number of individuals of a given taxa (i.e., a species) that were found in a given sample. It is zero when the sample contained no individuals. This notation is only necessary, if we are interested in zero samples (i.e., indication of very low abundances). Functions in the package accept non-integer values, too.

The segm column is used to distinguish segments (subpopulations) within individuals of the same species (nested into samples and species). Here we use "fresh" and "broken" segments to classify individuals based on shell decay. Other common examples for such segments are when distinguishing between males and females, different life stages or age classes. But it can also be used to identify subsets of the data, e.g., in case of a repeated measures experiment, when samples are nested within subsequent sampling period. As an example, data from museum collections can be used in this way to describe data accumulation trends through time (Sólymos and Fehér 2008).

This format is ideal for the storage of the data but not adequate for data analysis. Prior to analysis, we have to crosstabulate the data to get a matrix filled with numeric values and with rows as samples and columns as taxa. Besides the functions table (in package base, for factors; R Development Core Team 2008), there are some other functions in R to do this. For two-way crosstabulation of such data, there is the function cast in the reshape package (Wickham 2007), the mama function in the simba package (Jurasinski 2007) based on the reshape function, and the matrify function in the labdsv package (Roberts 2007).

Complications may arise, however, when we are dealing with three-way crosstabulation of the data (see xtabs in package stats, with formula interface; R Development Core Team 2008) and complex data structures, like the results of a hierarchical sampling design. We have to aggregate the samples into higher level units or the taxa into taxonomic or functional groups. And we might want to extract a subset of the crosstabulated data along with subsetted tables for samples and taxa at the same time. The way to do it with the mefa package is shown in the next sections.

# 4. Object classes

The structure of the above data set with the four column is basically the prototype of an object of class 'stcs'. This is the primary format for database style data sets in the **mefa** package. The four letter acronym comes from the first letters of the column names ( $\underline{s}$  amples,  $\underline{t}$  axa,  $\underline{c}$  ounts,  $\underline{s}$  egments). To convert our example into an 'stcs' object we do:

```
R> x1 <- stcs(dol.count)
R> str(x1)

Classes 'stcs' and 'data.frame': 297 obs. of 4 variables:
$ samp : Factor w/ 24 levels "DQ1","DQ2","DQ3",..: 1 1 1 1 1 1 1 2 2 2 ...
$ taxa : Factor w/ 29 levels "aacu","amin",..: 2 2 9 11 14 28 28 2 2 3 ...
$ count: num 2 2 2 2 1 2 7 1 3 1 ...
```

```
$ segm : Factor w/ 3 levels "fresh","broken",..: 1 2 1 1 1 2 1 2 1 2 ...
- attr(*, "call")= language stcs(dframe = dol.count)
- attr(*, "expand")= logi FALSE
- attr(*, "zero.count")= logi TRUE
- attr(*, "zero.pseudo")= chr "zero.pseudo"

R> unique(x1$count)

[1] 2 1 7 3 13 4 5 15 8 10 16 17 25 0 6 9 19 12 22 26
```

The object inherits from the data frame class, thus methods available for data frames apply for 'stcs' objects as well. But there are four additional attributes. The call attribute is the function call. The expand attribute refers to the count column. If the count values are all ones (except for empty samples), then each row represent one individual, and the expand attribute is TRUE. We can achieve this by the expand argument in the function call:

```
R> x2 <- stcs(dol.count, expand = TRUE)
R > str(x2)
Classes 'stcs' and 'data.frame':
                                         732 obs. of 4 variables:
 $ samp : Factor w/ 24 levels "DQ1", "DQ2", "DQ3", ...: 1 1 1 1 1 1 1 1 1 1 ...
 $ taxa : Factor w/ 29 levels "aacu", "amin",...: 2 2 2 2 9 9 11 11 14 28 ...
 $ count: num 1 1 1 1 1 1 1 1 1 1 ...
 $ segm : Factor w/ 3 levels "fresh","broken",..: 1 1 2 2 1 1 1 1 1 1 ...
 - attr(*, "call") = language stcs(dframe = dol.count, expand = TRUE)
 - attr(*, "expand")= logi TRUE
 - attr(*, "zero.count")= logi TRUE
 - attr(*, "zero.pseudo")= chr "zero.pseudo"
R> sum(x2$count)
[1] 731
R> unique(x2$count)
[1] 1 0
```

As an effect, the data frame is expanded and the count column contain 1 and 0 values. As we see, now the result contains 732 rows instead of 297. The 732 is the sum of the counts (one row for each count) plus one row for the empty sample. This expansion can be done with any data frame by the inflate function of the package. If values are non-integers, this cannot be applied.

The zero.count attribute refers to the presence or absence of empty samples in the data set. If empty samples are present, taxa and segment indices of the corresponding rows are set to the value stored in the zero.pseudo attribute. This can be set by the zero.pseudo argument in the function call. Count values of this pseudo species should be 0, the segment

value is indifferent (but it can be set as the second element of a character vector supplied as the zero.pseudo argument).

Empty samples can be dropped by the drop.zero = TRUE argument (some multivariate methods, i.e., dissimilarity or diversity indices, are not defined for empty samples):

Now the  ${\tt zero.count}$  attribute is FALSE and the  ${\tt zero.pseudo}$  attribute is "not.defined" as

The number of columns in the input data frame may vary from two to four. If two columns are provided, it is assumed that the first column contains sample, while the second taxa names. If three columns are provided, the first two are treated as sample and taxa names, while the third is treated as count if numeric, and segment if character or factor. If four columns are provided, those are assumed to be in the samples, taxa, counts, segments order.

To crosstabulate the data of a 'stcs' object, use:

```
R > m1 < - mefa(x1)
R> m1
An object of class 'mefa' containing
 $ xtab: 731 individuals of 28 taxa in 24 samples,
 $ segm: 2 (non-nested) segments:
         fresh, broken,
 $ samp: table for samples not provided,
 $ taxa: table for taxa not provided.
R> m1$xtab["LT1", ]
aacu amin apur bbip bcan ccer clam cort ctri dbre dper druf eful estr ffau
                       0
                                       0
                                                 0
                            0
                                 0
                                            0
hobv iiso mbor mobs odol ogla pinc ppyg pvic tuni vcos vicr vidi
                       0
                            0
                                 0
                                     0
                                            0
```

The mefa function returns an object of class 'mefa'. The print method for the 'mefa' objects returns basic information on the dimensions of the data. The \$xtab list element contains the crosstabulated data. The pseudo species has been removed, thus the row for sample LT1 is empty. Row and column ordering follows the original internal coding of factors in the 'stcs' object. The \$segm is a list with length equal to the number of segments, and contains the matrices for each segment, with dimensions and names being the same as for \$xtab:

```
R> str(m1$xtab)
num [1:24, 1:28] 0 0 0 0 0 0 1 1 0 0 ...
- attr(*, "dimnames")=List of 2
..$ samp: chr [1:24] "DQ1" "DQ2" "DQ3" "DT1" ...
..$ taxa: chr [1:28] "aacu" "amin" "apur" "bbip" ...

R> str(m1$segm)
List of 2
$ fresh : num [1:24, 1:28] 0 0 0 0 0 0 1 1 0 0 ...
..- attr(*, "dimnames")=List of 2
....$ samp: chr [1:24] "DQ1" "DQ2" "DQ3" "DT1" ...
....$ taxa: chr [1:28] "aacu" "amin" "apur" "bbip" ...
$ broken: num [1:24, 1:28] 0 0 0 0 0 0 0 0 0 ...
..- attr(*, "dimnames")=List of 2
....$ samp: chr [1:24] "DQ1" "DQ2" "DQ3" "DT1" ...
```

....\$ taxa: chr [1:28] "aacu" "amin" "apur" "bbip" ...

If segments represent e.g., successive sampling periods (years, decades) the use of the nested = TRUE argument can be convenient to inspect the data accumulation over time. In this case, values in subsequent segments are added up and segment names indicate this also:

If the input object for the mefa function is a matrix or data frame, segments cannot be specified directly. Segments can, however, be defined indirectly through a 'mefa'—'stcs'—'mefa' loop by the melt method (discussed in the examples later).

Besides the crosstabulated data, we also have a data frame for the samples. Here are the covariates for the 24 samples (microhabitat type and sampling method):

```
R> data("dol.samp")
R> str(dol.samp)

'data.frame': 24 obs. of 2 variables:
$ microhab: Factor w/ 4 levels "dead.wood","litter",..: 2 2 2 2 2 1 1 1 1..
$ method : Factor w/ 2 levels "time","quadrat": 2 2 1 2 1 2 1 2 1...
```

And we also have a table containing variables related to the species (three factors, one numeric, note that size is based on average adult shell dimension and taken from the literature):

```
R> data("dol.taxa")
R> str(dol.taxa)

'data.frame': 121 obs. of 4 variables:
$ species: Factor w/ 121 levels "Acanthinula aculeata",..: 3 2 81 82 16 1..
$ author : Factor w/ 65 levels "(Alder, 1830)",..: 26 53 42 19 44 47 31 1..
$ familia: Factor w/ 21 levels "Aciculidae","Bradybaenidae",..: 1 1 14 14..
$ size : num 3.4 5.5 16 16 2.2 2.3 17 8 12 7.5 ...
```

These two tables, or either only one of them can easily be combined with the crosstabulation:

```
R > mefa(x1, samp = dol.samp)
R > mefa(x1, taxa = dol.taxa)
R> m2 <- mefa(x1, samp = dol.samp, taxa = dol.taxa)
R> m2
R> str(m2$xtab)
R> str(m2$samp)
R> str(m2$taxa)
An object of class 'mefa' containing
 $ xtab: 731 individuals of 28 taxa in 24 samples,
 $ segm: 2 (non-nested) segments:
         fresh, broken,
 $ samp: table for samples provided (2 variables),
 $ taxa: table for taxa not provided.
An object of class 'mefa' containing
 $ xtab: 731 individuals of 28 taxa in 24 samples,
 $ segm: 2 (non-nested) segments:
```

```
fresh, broken,
$ samp: table for samples not provided,
$ taxa: table for taxa provided (4 variables).
An object of class 'mefa' containing
$ xtab: 731 individuals of 28 taxa in 24 samples,
$ segm: 2 (non-nested) segments:
        fresh, broken,
$ samp: table for samples provided (2 variables),
$ taxa: table for taxa provided (4 variables).
num [1:24, 1:28] 0 0 0 0 0 0 1 1 0 0 ...
- attr(*, "dimnames")=List of 2
  ..$ samp: chr [1:24] "DQ1" "DQ2" "DQ3" "DT1" ...
  ..$ taxa: chr [1:28] "aacu" "amin" "apur" "bbip" ...
'data.frame':
                     24 obs. of 2 variables:
$ microhab: Factor w/ 4 levels "dead.wood","litter",..: 1 1 1 1 1 2 2 2..
$ method : Factor w/ 2 levels "time", "quadrat": 2 2 2 1 1 1 2 2 2 1 ...
                     28 obs. of 4 variables:
'data.frame':
$ species: Factor w/ 121 levels "Acanthinula aculeata",..: 1 4 6 10 14 35...
$ author : Factor w/ 65 levels "(Alder, 1830)",..: 42 57 1 41 27 49 41 38...
$ familia: Factor w/ 21 levels "Aciculidae", "Bradybaenidae",...: 18 21 21 ...
          : num 2 9 5 18 18 18 17 13 2.3 NA ...
```

The tables are subsetted and ordered according to the row and column names in the crosstabulation. If names do not match, an error message is produced. This can be the case e.g., if the input object for the mefa function is a matrix without row or column names. It is not necessary to have names, only if tables for samples and taxa are provided.

In those cases, when the tables for samples and taxa do not contain rows for all the crosstabulated ones, the xtab.fixed = FALSE argument can be useful. This results in a 'mefa' object containing samples and taxa that are common in the names (natural join based on intersect of dimnames):

```
$ segm: 2 (non-nested) segments:
        fresh, broken,
$ samp: table for samples provided (2 variables),
$ taxa: table for taxa provided (4 variables).
num [1:19, 1:9] 4 4 3 1 2 3 0 3 7 13 ...
- attr(*, "dimnames")=List of 2
  ..$ samp: chr [1:19] "DQ1" "DQ2" "DQ3" "DT1" ...
  ..$ taxa: chr [1:9] "amin" "apur" "estr" "ffau" ...
'data.frame':
                    19 obs. of 2 variables:
$ microhab: Factor w/ 4 levels "dead.wood","litter",..: 1 1 1 1 1 2 4 4..
$ method : Factor w/ 2 levels "time","quadrat": 2 2 2 1 1 1 1 2 2 2 ...
                    9 obs. of 4 variables:
'data.frame':
$ species: Factor w/ 121 levels "Acanthinula aculeata",..: 4 6 48 24 51 5...
$ author : Factor w/ 65 levels "(Alder, 1830)",..: 57 1 13 48 42 55 42 53...
$ familia: Factor w/ 21 levels "Aciculidae", "Bradybaenidae",...: 21 21 12 ...
$ size
          : num 9 5 18 20 15 11 16 15.5 8
```

As we see, the count data matrix is also subsetted, according to the related tables of samples and taxa.

An object of class 'mefa' is a list of length five. The first element is the function call (\$call), second is a matrix with the cross tabulated data (\$xtab). These two are always present, the remaining three depend on the availability of data and the aims of the study. The third element contains a list of matrices for segments (\$segm), the fourth and fifth contain data frames with data for samples (\$samp) and taxa (\$taxa), respectively. The general structure of an object of class 'mefa' follows a relational data model, where dimnames attributes of the main count data matrix, the segment data matrices and the samples/taxa data tables for the rows and columns are identical. The print method for the 'mefa' objects shows the names of these elements to help memorizing the notation. Figure 1 depicting the object structure can be called as:

R> mefalogo()

# 5. S3 methods

#### 5.1. Summary and graphical display

Dimensions and dimension names can be retrieved by the dim and dimnames methods:

```
R > dim(m2)
```

[1] 24 28 2

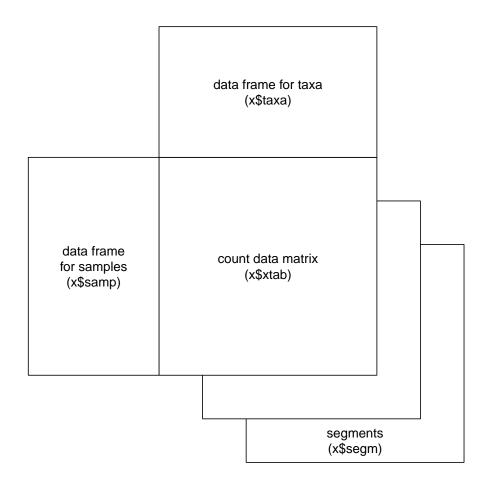


Figure 1: Representation of the relational data model in an object of class 'mefa'.

# R> dimnames(m2)

R> summary(m2)

```
$samp
  [1] "DQ1" "DQ2" "DQ3" "DT1" "DT2" "DT3" "LQ1" "LQ2" "LQ3" "LT1" "LT2" "LT3"
[13] "RQ1" "RQ2" "RQ3" "RT1" "RT2" "RT3" "WQ1" "WQ2" "WQ3" "WT1" "WT2" "WT3"

$taxa
  [1] "aacu" "amin" "apur" "bbip" "bcan" "ccer" "clam" "cort" "ctri" "dbre"
[11] "dper" "druf" "eful" "estr" "ffau" "hobv" "iiso" "mbor" "mobs" "odol"
[21] "ogla" "pinc" "ppyg" "pvic" "tuni" "vcos" "vicr" "vidi"

$segm
[1] "fresh" "broken"
To get a summary of the data, use the summary method:
```

#### Call:

```
mefa(xtab = x1, samp = dol.samp, taxa = dol.taxa)
```

	Summary
Total sum	731
Matrix fill (%)	26
Number of samples	24
Number of taxa	28
Number of segments	2

#### Segments (non-nested):

fresh, broken

```
s.rich s.abu t.occ t.abu
        0.000 0.00
Min.
                     1.000
                              1.00
1st Qu.
         5.000 9.75
                      2.000
                              4.00
Median
         7.000 20.50
                     4.500
                            10.50
Mean
         7.333 30.46 6.286 26.11
3rd Qu. 10.000 44.75 10.000 27.75
        16.000 97.00 23.000 245.00
Max.
```

This returns basic characteristics of the data matrix. There are observations of 731 land snail individuals in the object and  $26^{\circ}\%$  of the matrix cells are non zero. There is also a list with segment levels, and summaries of the marginal tables derived from the count data matrix. Four vectors are based on marginal tables, the number of taxa (species) and individuals in the samples (s.rich and s.abu), and the number of occupied samples and individuals per species (t.occ and t.abu). The characteristics shown in the summary can be extracted according to their names:

#### R> names(summary(m2))

```
[1] "s.rich" "s.abu" "t.occ" "t.abu" "ntot" [6] "mfill" "nsamp" "ntaxa" "nsegm" "segment" [11] "call" "nested" "drop.zero" "xtab.fixed"
```

For example to return species richness values for the samples, or matrix fill, use:

## R> summary(m2)\$s.rich

```
DQ1 DQ2 DQ3 DT1 DT2 DT3 LQ1 LQ2 LQ3 LT1 LT2 LT3 RQ1 RQ2 RQ3 RT1 RT2 RT3 WQ1
                          5
                                           2
  5
      7
                 10
                      5
                              5
                                  7
                                      0
                                               5 10
                                                      16
                                                         13 11
WQ2 WQ3 WT1 WT2 WT3
 10
      8
          5
              4
```

#### R> summary(m2)\$mfill

## [1] 0.2619048

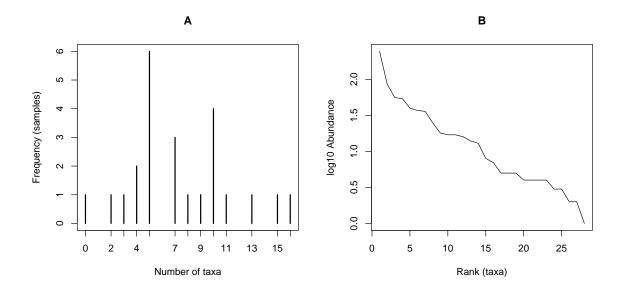


Figure 2: Plotting an object of class 'mefa': barcharts for species richness (A), and ranked log abundances for species (B).

To get summaries for the linked data tables, use e.g., summary(m2\$samp) or summary(m2\$taxa). The first four characteristics of the samples and taxa can be plotted as barchart (type = "bar"; Figure~2A) or ranked in decreasing order (type = "rank"; Figure~2B) by the plot method. Values can be log transformed (trafo = "log"; Figure~2B) or normalized by their maxima (trafo = "ratio"). Here, only two cases are shown (when the second argument is 1 and 4):

```
R> plot(m2, 1, main = "A")
R> plot(m2, 4, type = "rank", trafo = "log", main = "B")
```

The boxplot method is provided to retreive these statistics for each segment (Figure 3). Again, only two cases are shown (when the second argument is 2 and 3 to complement the previous figure):

```
R> boxplot(m2, 2, main = "A")
R> boxplot(m2, 3, main = "B")
```

The melt method refers to the conversion of a 'mefa' object into an 'stcs' representation. The generic function is defined here, but can be found in the reshape package as well (transforming between wide and long formatted data), which also contains methods for data frames, arrays, matrices, tables and lists. The method for 'mefa' objects is defined in the mefa package. Use the sampling method column in the samples table for segments (m2\$samp\$method), and make an object of class 'stcs' as follows:

```
R> molten <- melt(m2, "method")
R> str(molten)
```

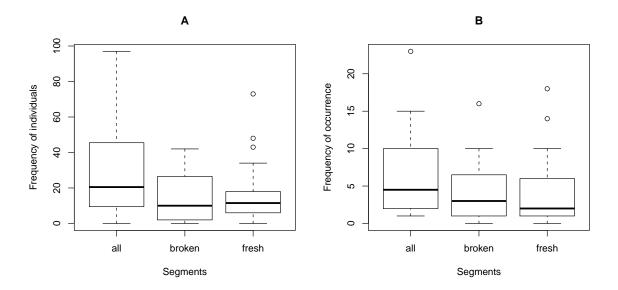


Figure 3: Boxplots to depict differences among segments in abundances for samples (A), frequency of occurrences for taxa (B).

Then make an object of class 'mefa' using the samples and taxa tables, because those have not changed, only the segments (instead of shell decay stage, now it refers to sampling methods, see segment names in the following example):

This kind of melting—refreezing can be useful, if e.g., segments were not defined in the original 'stcs' object, or the 'mefa' object was based on a matrix or data frame (without segments).

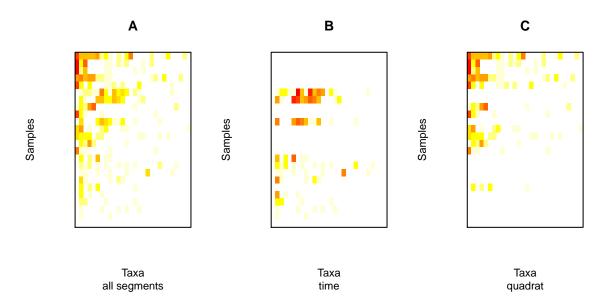


Figure 4: Levelplot representation of an object of class 'mefa'. Intensity of red coloring refers to increasing log abundances in the cells of the main data matrix (A) and the segments for the time restricted search (B), and the quadrat (C) methods.

In this way, we can create segmented representations based on groups of samples (e.g., spatial units, repeated measures) or groups of taxa (e.g., taxonomic or functional groups) to more easily explore their differences.

Here we used melting—refreezing to explore the effects of sampling methods (note, originally shell decay stages were used as segments, and not sampling methods). We can visualize the relationship by the <code>image</code> method. This method creates a grid of colored rectangles with colors corresponding to the values in count data table. Segments can be specified as well. The rows and the columns are ordered according to their sums, being the top-left corner with the highest values. Transformations (log, order-scaled values based on quantiles, presence-absence) are also available to best represent the data in the plot. Figure 4 shows differences between the sampling methods compared to the main data matrix.

Methods for objects of class 'stcs' (summary, plot, boxplot, image) are also provided for convenience, but those merely use the crostabulated results to do the same job as the respective method for the 'mefa' objects. Other methods for 'stcs' objects rely on methods for data frames (e.g., print, str, dim, dimnames).

#### 5.2. Extraction and aggregation

If we want to analyze only a subset of the data, the extraction of the 'mefa' objects can be done via square brackets and by indexing the samples, taxa and segments to extract. Indexing can be numeric, or can refer to dimnames:

```
R> ex1 <- m2[1:20, 11:15, "fresh"]
R> dim(ex1)

[1] 20 5 1

R> dim(ex1$samp)

[1] 20 2

R> dim(ex1$taxa)

[1] 5 4
```

As a result, the count data and the samples/taxa tables were subsetted in the same step. If negative numeric values are given, the respective parts of the object are omitted, e.g., the first element in the second dimension can be excluded by m2[, -1]. Unused factor levels in the \$samp and \$taxa tables can be dropped by the argument drop = TRUE:

The data set can be easily aggregated if we want to calculate statistics, e.g., species richness, on different levels of the sampling hierarchy (like in additive diversity partitioning; Lande 1996; Crist et~al. 2003). Aggregation can be done by internal vectors, when the name of the variable refers to a column in the samples or taxa tables. If external vectors (that are not part of the 'mefa' object) are used, the current implementation require a class attribute (e.g., "factor") to be recognized as an external object. Now we create a factor with levels "large" and "small" for snail species with adult body size larger or equal to, or smaller than 5 millimeters, respectively<sup>3</sup>. Then, aggregate the object according to the internal "microhab" (microhabitat type) variable for samples and this external body size factor for taxa:

<sup>&</sup>lt;sup>3</sup>We treat semislugs with NA values as small sized species.

VIATIOO	Description
Method	Description evaluates if an object is of class 'stcs'.
	coerces to class 'stcs'.
•	does the same as summary for 'mefa' objects, just for convenience.
olot	does the same as plot for 'mefa' objects, just for convenience.
ooxplot	does the same as boxplot for 'mefa' objects, just for convenience.
image	does the same as image for 'mefa' objects, just for convenience.
is.mefa	evaluates if an object is of class 'mefa'.
as.mefa	coerces to class 'mefa'.
orint	print basic characteristics of the object.
summary	print basic summaries on the data.
olot	graphical display of basic summaries of the data based on the main
	data matrix.
ooxplot	graphical display of basic summaries of the data based on data ma-
1	trices for segments.
image	graphical display of the values in the main data matrix or data matrix
	for a segment.
aggragata	aggregate (sum) the values in the matrices (main data and segments).
	extract an object (data matrices and relational data frames) based
L	,
<b>3</b> .	on indexing for rows (samples) columns (taxa) and segments.
	convert an object of class 'mefa' into an object of class 'stcs'.
-	writes data from an object of class 'mefa' into a file.
dim	return dimension of the 'mefa' object.
dimnames	return names for rows (samples) columns (taxa) and segments in the
	'mefa' object.
	s.stcs as.stcs summary plot mage s.mefa as.mefa print summary plot mage

Table 1: Description of methods provided for the object classes.

# R> lapply(m4\$segm, t)

## \$time

	dead.wood	litter	live.wood	rock
large	32	12	16	118
small	5	0	1	3

#### \$quadrat

	dead.wood	litter	live.wood	rock
large	21	21	64	92
small	45	112	98	91

From these results it is clear, that the proportion of size categories differs among sampling methods and microhabitats. We will further analyze this in the next chapters.

The methods provided for the object classes in the **mefa** package are reviewed in Table~1.

## 5.3. Writing reports

If the count data as the result of a field experiment are given, along with information about the sampling locations, making a report is easy with the report method. This writes a text file into the specified or the working directory. Contents of this text file can be further used e.g., by copy-pasting it into a word processor. But it is more straightforward to use the tex = TRUE argument to write a formatted LATEX file and use the LATEX function input to include the results into the main document. A sample document on how to use the function in a Sweave document (Leisch 2002) can be viewed by calling mefadocs ("SampleReport").

Now we write the dataset into a file after extracting the ten randomly selected species only, retaining all samples and both segments:

```
R> set.seed(1234)
R> m5 <- m2[ , sample(1:dim(m2)[2], 10)]
R> report(m5, "report.tex", tex = TRUE, segment = TRUE,
+ taxa.name = 1, author.name = 2, drop.redundant = 1)
```

The meaning of the arguments used is: use the m5 'mefa' object to write a report into the file "report.tex" by using LATEX formatting. Use segments. Taxa names are in the first, author names are in the second column of the taxa table. We also want that implicitly all columns in the sample table should be used in the same order as before, to generate sample information (this can be specified by the samp.var argument not used here). Redundant levels of these sample information are dropped here (see help page ?report.mefa for further details). The result is shown in Figure 5 with appropriate LATEX formatting. The formatting rules can be modified via the tex.control argument.

# 6. Data analysis

#### 6.1. Single taxon response modeling

Coefficients:

Here we use the data of the land snail species Aegopinella minor ("amin") and the samples data table to investigate the effect of microhabitat and sampling method on the abundance of this species. The response is the "amin" column of the m2\$xtab matrix, for the data argument of the Poisson GLM, we simply provide the m2\$samp table:

```
R> mod.amin <- glm(m2$xtab[, "amin"] ~ ., data = m2$samp, family = poisson)
R> summary(mod.amin)

Call:
glm(formula = m2$xtab[, "amin"] ~ ., family = poisson, data = m2$samp)

Deviance Residuals:
    Min    1Q    Median    3Q    Max
-1.8037    -0.8167    -0.2117    0.3163    2.4082
```

```
Acanthinula aculeata (O. F. Muller, 1774)
litter, quadrat (fresh: 2). rock, quadrat (broken: 2).
Balea biplicata (Montagu, 1803)
dead.wood, time (fresh: 1, broken: 1). litter, quadrat (broken: 1). live.wood: time (fresh: 2,
broken: 3); quadrat (broken: 1). rock: time (fresh: 2, broken: 3); quadrat (fresh: 6, broken: 5).
Bulgarica cana (Held, 1836)
dead.wood, time (broken: 1). live.wood, quadrat (broken: 1). rock, time (broken: 1).
Chilostoma faustinum (Rossmassler, 1835)
litter, quadrat (broken: 1). live.wood: time (broken: 2); quadrat (fresh: 1, broken: 1). rock:
time (fresh: 1, broken: 5); quadrat (fresh: 6, broken: 19).
Daudebardia brevipes (Draparnaud, 1805)
rock, quadrat (fresh: 3, broken: 1).
Euomphalia strigella (Draparnaud, 1801)
dead.wood: time (fresh: 1); quadrat (broken: 2). live.wood: time (broken: 3); quadrat
(broken: 1). rock: time (fresh: 3); quadrat (fresh: 1, broken: 3).
Helicodonta obvoluta (O. F. Muller, 1774)
dead.wood: time (broken: 3); quadrat (fresh: 7, broken: 1). rock: time (fresh: 12, broken: 1);
quadrat (fresh: 4, broken: 9).
Isognomostoma isognomostomos (Schroter, 1784)
live.wood, quadrat (fresh: 2). rock, time (fresh: 1, broken: 14).
Oxychilus glaber (Rossmassler, 1838)
rock, quadrat (fresh: 2, broken: 2).
Vallonia costata (O. F. Muller, 1774)
rock, quadrat (fresh: 2).
```

Figure 5: Report generated from a 'mefa' object by the report method.

	Estimate	Std. Error	z value	Pr(> z )	
(Intercept)	0.6475	0.2858	2.266	0.02346	*
microhablitter	-0.3483	0.3770	-0.924	0.35559	
microhablive.wood	0.3448	0.3170	1.088	0.27668	
microhabrock	0.6633	0.2985	2.222	0.02630	*
methodquadrat	0.6758	0.2281	2.963	0.00305	**

microhablitter

microhabrock

methodquadrat

microhablive.wood

microhablitter:methodquadrat

microhabrock:methodquadrat

microhablive.wood:methodquadrat

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 49.377 on 23 degrees of freedom

Residual deviance: 28.515 on 19 degrees of freedom

AIC: 106.99
```

Number of Fisher Scoring iterations: 5

The model output indicates that the species was more frequent in dead wood and rock microhabitats than in live wood and litter, further, most of the individuals were collected by the quadrat method.

## 6.2. Modeling the marginal sum as response

The distribution of the number of snails in the samples is skewed and likely overdispersed, thus we use a negative binomial model to analyze the relationship between land snail abundances and sample covariates. The GLM for the negative binomial is implemented in the MASS package (Venables and Ripley 2002). As part of the maximum likelihood fit, a shape parameter (theta) is also estimated in order to model the data as gamma mixture of Poisson distributions. We use the summary method to get the vector of the number of individuals, and the samples table again for covariates using their interaction as well:

```
R> library("MASS")
R> mod.abu <- glm.nb(summary(m2)$s.abu ~ .^2, data = m2$samp)
R> summary(mod.abu)
Call:
glm.nb(formula = summary(m2)$s.abu ~ .^2, data = m2$samp, init.theta = 4.73055585509537,
    link = log)
Deviance Residuals:
                1Q
                      Median
                                     30
                                              Max
                                0.21741
                                          1.70730
-2.40783
         -0.64639 -0.06349
Coefficients:
                                 Estimate Std. Error z value Pr(>|z|)
(Intercept)
                                   2.5123
                                              0.3122
                                                       8.046 8.54e-16 ***
```

0.5013

0.4762

0.4198

0.4279

0.6441

0.6237

0.5812 -0.284

-2.246 0.02469 \*

0.10245

0.17622

0.77643

0.00476 \*\*

0.00457 \*\*

0.00722 \*\*

-1.633

2.823

1.352

2.836

2.687

-1.1260

-0.7777

1.1849

0.5787

1.8267

1.6756

-0.1650

---

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

(Dispersion parameter for Negative Binomial(4.7306) family taken to be 1)

Null deviance: 94.216 on 23 degrees of freedom Residual deviance: 26.815 on 16 degrees of freedom

AIC: 198.21

Number of Fisher Scoring iterations: 1

Theta: 4.73 Std. Err.: 1.71

2 x log-likelihood: -180.214

The abundance of snails in the samples was positively associated with dead wood and rock microhabitats. The interaction of sampling method and microhabitat has proved to be significant, indicating that the collecting efficiency of snails varied among microhabitats. The number of snails collected by the quadrat method was higher for the litter and live wood microhabitats, while in the dead wood microhabitat, the timed search resulted in more snails.

We can take advantage of the segments in the analysis as well. We now investigate, whether the proportion of fresh shells (including living animals) differ among microhabitats and sampling methods. First, we make a two-column matrix with the number of fresh shells per samples and the total number of shells (fresh and broken) collected per samples. Then, assuming that decay status (fresh or broken) of a single shell follows a Bernoulli process, we use this matrix in a binomial GLM (logistic regression) with the number of trials equal to the total number of individuals per sample:

```
R> prop.fr <- cbind(summary(m2[ , , "fresh"])$s.abu, summary(m2)$s.abu)
R> mod.fr <- glm(prop.fr ~ .^2, data = m2$samp, family = binomial)
R> summary(mod.fr)
```

#### Call:

```
glm(formula = prop.fr ~ .^2, family = binomial, data = m2$samp)
```

Deviance Residuals:

```
Min 1Q Median 3Q Max -1.21602 -0.54213 -0.07867 0.30911 2.13176
```

#### Coefficients:

	Estimate	Std.	Error	z value	Pr(> z )
(Intercept)	-0.14518	0.	24141	-0.601	0.547573
microhablitter	-0.03714	0.	49154	-0.076	0.939771
microhablive.wood	-0.49081	0.	47772	-1.027	0.304230

```
-1.09526
                                             0.30840
                                                      -3.551 0.000383 ***
microhabrock
                                 -0.35559
                                             0.31373
                                                      -1.133 0.257036
methodquadrat
microhablitter:methodquadrat
                                 -0.16278
                                             0.55175
                                                      -0.295 0.767977
microhablive.wood:methodquadrat
                                 0.29843
                                             0.53561
                                                       0.557 0.577402
microhabrock:methodquadrat
                                                       3.041 0.002359 **
                                  1.17404
                                             0.38609
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Signif. codes:
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 33.970
                           on 22
                                   degrees of freedom
Residual deviance: 13.825
                           on 15
                                   degrees of freedom
AIC: 117.20
```

Number of Fisher Scoring iterations: 4

It is clear that the proportion of fresh shells is not constant among microhabitats and sampling methods. The proportion was lowest in the rock microhabitats, although the quadrat method resulted more fresh shells from the rock microhabitats than the timed search method (due to the significant microhabitat  $\times$  method interaction).

#### 6.3. Multivariate response modeling

We employ a non-parametric multivariate analysis of variance to assess the effects of covariates on community composition. The method is implemented in the adonis function (McArdle and Anderson 2001; Anderson 2001) of the **vegan** package (Oksanen *et~al.* 2008). The method is based on a distance matrix calculated from the community data by the Bray–Curtis index of dissimilarity, by default. Thus, the input data matrix should not contain rows with zero sum. We have to remove those samples from the count data matrix and the samples table as well. This is most easily done by the as.mefa method with using the argument drop.zero = TRUE:

```
R> library("vegan")
R> m6 <- as.mefa(m2, drop.zero = TRUE)</pre>
R> m6.ado <- adonis(m6$xtab ~ .^2, data = m6$samp, permutations = 100)
R> m6.ado
Call:
adonis(formula = m6$xtab ~ .^2, data = m6$samp, permutations = 100)
                      Df SumsOfSqs
                                     MeanSqs F.Model
                                                           R2
                                                                Pr(>F)
microhab
                 3.00000
                            1.61242
                                     0.53747
                                              2.93142 0.2461 0.009901 **
                                              6.43358 0.1801 0.009901 **
method
                 1.00000
                            1.17959
                                     1.17959
microhab:method 3.00000
                            1.00861
                                     0.33620
                                              1.83368 0.1540 0.009901 **
                                                       0.4198
Residuals
                15.00000
                            2.75025
                                     0.18335
                22.00000
Total
                            6.55087
                                                       1.0000
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The results revealed that  $18^{\circ}\%$  of the total variation in community composition was due to sampling method (see also Figure 4), and  $24.6^{\circ}\%$  was explained by microhabitats. Their interaction was also significant, explaining  $15.4^{\circ}\%$  of the total variation. But the unexplained variance remained relatively high  $(42^{\circ}\%)$ .

We can visualize this relationship by constrained (canonical) correspondence analysis (CCA). For this, use the cca function from the ade4 package (Thioulouse and Dray 2007; Dray and Dufour 2007). We base the analysis only on the matrix of the "fresh" segment (note that here we use it as data frame<sup>4</sup>) and use the samples table for environmental constraints:

```
R> library("ade4")
R> m2.cca <- ade4::cca(data.frame(m2$segm[["fresh"]]), m2$samp, scan = FALSE)
R> plot.pcaiv(m2.cca)
```

The compound results in Figure 6 show environmental variables loadings and correlations (top and middle left), projection of the axes of the taxa analysis into the CCA (lower left), species scores (bottom middle), eigenvalues bar chart (bottom right), and a biplot of site scores superimposed with their predictions by environmental variables (main graph). Most of the species tend to be associated with dead wood and rock microsites, and samples separate well according to sampling method (see middle letters in the main graph).

#### 6.4. Analyzing multiple subsets

The modular structure of the 'mefa' objects enables easy processing of the data in loops. Now we use hierarchical cluster analysis based on multiple subsets of the data to assess the effects of shell decay stages and sampling methods on the community composition. We first make a list with four subsets of the Dolina dataset, referring to combinations of timed search and quadrat method, and fresh and broken shells. We also aggregate the samples over microhabitats:

Then we do the clustering on each elements of the list object m.list using Euclidean distance and Ward's method:

```
R> for (i in 1:4) {
+ tmp <- hclust(dist(m.list[[i]]$xtab), "ward")
+ plot(tmp, main = LETTERS[i], sub = names(m.list)[i], xlab = "")
+ }</pre>
```

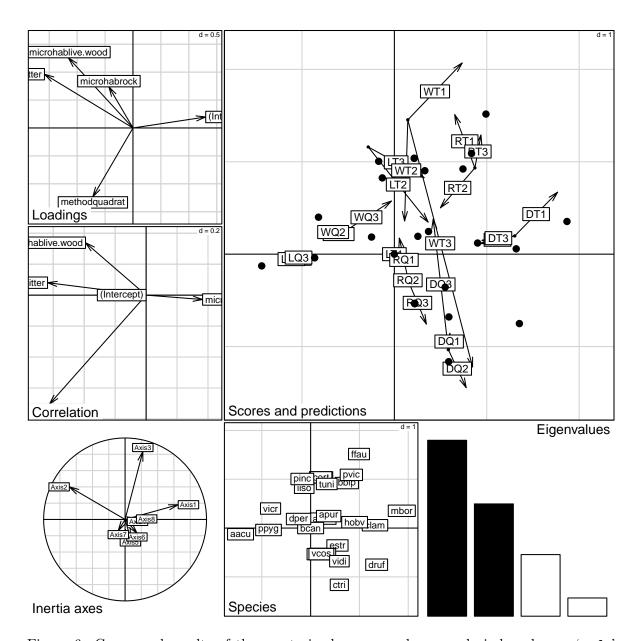


Figure 6: Compound results of the constrained correspondence analysis based on a 'mefa' object.

Figure 7 shows that the dendrograms for the fresh and broken segments of the quadrat method are congruent, while that for the timed search are not. For the fresh shells, the dead wood communities resembled the rock community. While for the broken shells, dead wood communities were more similar to live wood and litter communities than to the rock.

<sup>&</sup>lt;sup>4</sup>We have to use the package name in the call as ade4::cca, and the plot.pcaiv function written in full, because the object class 'cca' is defined in both the vegan and ade4 packages.

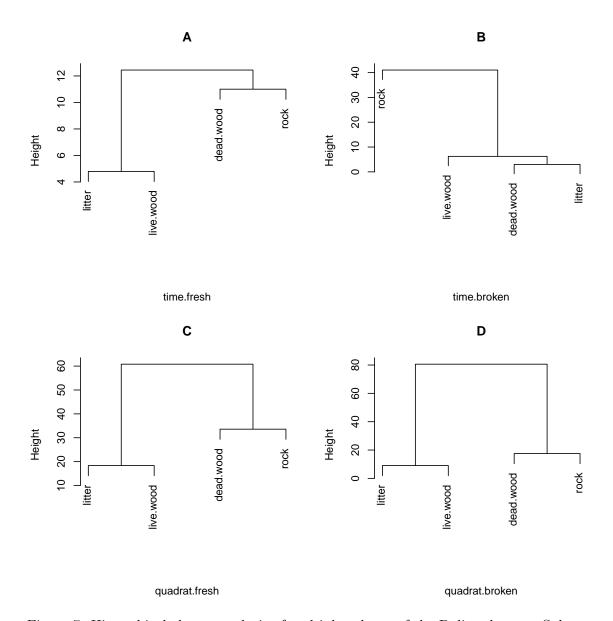


Figure 7: Hierarchical cluster analysis of multiple subsets of the Dolina dataset. Subsets are extracted to represent combinations of shell decay stages (A, C: fresh; B, D: broken) and sampling methods (A–B: timed search; C–D: quadrat method).

# 7. Conclusions

The mefa package provides standardized environment and a and convenient tool for ecologists and biogeographers working on biodiversity data sets in R. The object classes ('stcs' and 'mefa') and S3 methods provide a coherent framework for data preprocessing of structured data sets. Based on 'mefa' objects, reports can be generated in plain text or LATEX format. It was presented how the objects can be directly used in further analyses for a variety of ecological problems.

# 8. Acknowledgments

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