An Example of mi Usage

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There are several steps in an analysis of missing data. Initially, users must get their data into R. There are several ways to do so, including the read.table, read.csv, read.fwf functions plus several functions in the foreign package. All of these functions will generate a data.frame, which is a bit like a spreadsheet of data. http://cran.r-project.org/doc/manuals/R-data.html for more information.

```
options(width = 65)
suppressMessages(library(mi))
data(nlsyV, package = "mi")
```

From there, the first step is to convert the data.frame to a missing_data.frame, which is an enhanced version of a data.frame that includes metadata about the variables that is essential in a missing data context.

```
mdf <- missing_data.frame(nlsyV)</pre>
```

```
## NOTE: In the following pairs of variables, the missingness pattern of the first is a subset of the s
## Please verify whether they are in fact logically distinct variables.
## [,1] [,2]
## [1,] "b.marr" "income"
```

The missing_data.frame constructor function creates a missing_data.frame called mdf, which in turn contains seven missing_variables, one for each column of the nlsyV dataset.

The most important aspect of a missing_variable is its class, such as continuous, binary, and count among many others (see the table in the Slots section of the help page for missing_variable-class. The missing_data.frame constructor function will try to guess the appropriate class for each missing_variable, but rarely will it correspond perfectly to the user's intent. Thus, it is very important to call the show method on a missing_data.frame to see the initial guesses

```
show(mdf) # momrace is guessed to be ordered
```

```
## Object of class missing_data.frame with 400 observations on 7 variables
##
## There are 20 missing data patterns
## Append '@patterns' to this missing_data.frame to access the corresponding pattern for every observat
##
##
                            type missing method model
## ppvtr.36
                     continuous
                                      75
                                            ppd linear
## first
                                       0
                                           <NA>
                                                  <NA>
                         binary
## b.marr
                                      12
                         binary
                                            ppd logit
## income
                     continuous
                                      82
                                            ppd linear
## momage
                     continuous
                                       0
                                           <NA>
                                                   <NA>
```

ppd ologit

ppd ologit

40

117

ordered-categorical

momrace ordered-categorical

momed

##

```
##
                             link transformation
                  family
                                      standardize
## ppvtr.36
                gaussian identity
## first
                    <NA>
                              <NA>
                                              <NA>
                                              <NA>
## b.marr
               binomial
                            logit
## income
                gaussian identity
                                      standardize
                                      standardize
## momage
                    <NA>
                              <NA>
## momed
            multinomial
                            logit
                                              <NA>
                                              <NA>
## momrace
            multinomial
                            logit
```

and to modify them, if necessary, using the change function, which can be used to change many things about amissing_variable, so see its help page for more details. In the example below, we change the class of the *momrace* (race of the mother) variable from the initial guess of ordered-categorical to a more appropriate unordered-categorical and change the income nonnegative-continuous.

```
mdf <- change(mdf, y = c("income", "momrace"), what = "type",</pre>
                     to = c("non", "un"))
## NOTE: In the following pairs of variables, the missingness pattern of the first is a subset of the s
    Please verify whether they are in fact logically distinct variables.
        [,1]
## [1,] "b.marr" "income"
show(mdf)
## Object of class missing_data.frame with 400 observations on 7 variables
## There are 20 missing data patterns
##
## Append '@patterns' to this missing_data.frame to access the corresponding pattern for every observat
##
##
                                     type missing method model
                                                75
                                                      ppd linear
## ppvtr.36
                               continuous
## first
                                   binary
                                                0
                                                     <NA>
                                                            <NA>
## b.marr
                                                12
                                   binary
                                                      ppd logit
                                                      ppd linear
## income
                  nonnegative-continuous
                                                82
## income:is_zero
                                   binary
                                                82
                                                      ppd
                                                           logit
## momage
                               continuous
                                                0
                                                     <NA>
                                                            <NA>
                      ordered-categorical
## momed
                                                40
                                                      ppd ologit
## momrace
                   unordered-categorical
                                                      ppd mlogit
                                               117
##
##
                        family
                                   link transformation
## ppvtr.36
                      gaussian identity
                                            standardize
                          <NA>
                                                   <NA>
## first
                                   <NA>
```

<NA>

<NA>

<NA>

<NA>

logshift

standardize

Once all of the missing_variables are set appropriately, it is useful to get a sense of the raw data, which can be accomplished by looking at the summary, image, and / or hist of a missing_data.frame

```
summary(mdf)
```

b.marr

income

momage

momrace

momed

income:is zero

```
## ppvtr.36 first b.marr
## Min. : 41.00 Min. :0.000 Min. :0.0000
```

binomial

binomial

multinomial

multinomial

< NA >

gaussian identity

logit

logit

<NA>

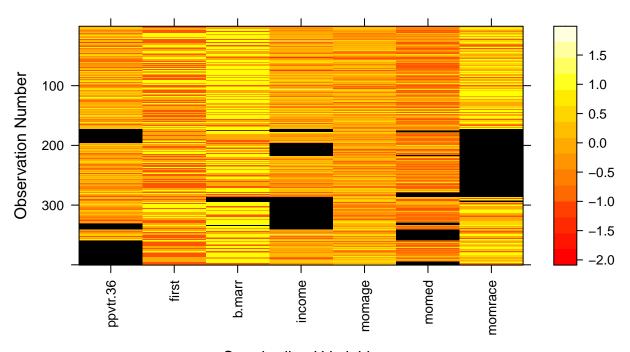
logit

logit

```
1st Qu.: 74.00
                      1st Qu.:0.000
                                        1st Qu.:0.0000
    Median : 87.00
                      Median :0.000
                                       Median :1.0000
##
           : 85.94
                              :0.435
                                               :0.7062
##
                      Mean
                                        Mean
    3rd Qu.: 99.00
                      3rd Qu.:1.000
                                        3rd Qu.:1.0000
##
            :132.00
##
    Max.
                      Max.
                              :1.000
                                        Max.
                                               :1.0000
##
    NA's
            :75
                                        NA's
                                               :12
##
        income
                           momage
                                             momed
                                                          momrace
##
                   0
                               :16.00
    Min.
           :
                       Min.
                                         Min.
                                                :1.000
                                                          1
                                                              : 55
##
    1st Qu.:
                8590
                       1st Qu.:22.00
                                         1st Qu.:1.000
                                                          2
                                                              : 80
##
    Median :
               17906
                       Median :24.00
                                         Median :2.000
                                                              :148
    Mean
               32041
                       Mean
                               :23.75
                                         Mean
                                                :2.042
                                                          NA's:117
    3rd Qu.:
               31228
                       3rd Qu.:26.00
                                         3rd Qu.:3.000
##
##
            :1057448
                               :32.00
                                                :4.000
    Max.
                       Max.
                                         Max.
    NA's
                                         NA's
                                                :40
##
            :82
```

image(mdf)

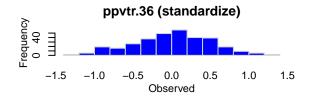
Dark represents missing data

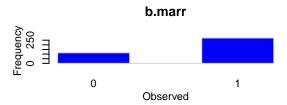


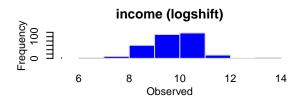
Standardized Variable

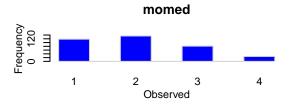
Clustered by missingness

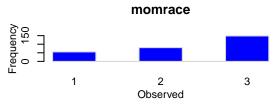
hist(mdf)











Next we

use the mi function to do the actual imputation, which has several extra arguments that, for example, govern how many independent chains to utilize, how many iterations to conduct, and the maximum amount of time the user is willing to wait for all the iterations of all the chains to finish. The imputation step can be quite time consuming, particularly if there are many missing_variables and if many of them are categorical. One important way in which the computation time can be reduced is by imputing in parallel, which is highly recommended and is implemented in the mi function by default on non-Windows machines. If users encounter problems running mi with parallel processing, the problems are likely due to the machine exceeding available RAM. Sequential processing can be used instead for mi by using the parallel=FALSE option.

```
rm(nlsyV)  # good to remove large unnecessary objects to save RAM
options(mc.cores = 2)
imputations <- mi(mdf, n.iter = 30, n.chains = 4, max.minutes = 20)
show(imputations)</pre>
```

Object of class mi with 4 chains, each with 30 iterations.

Each chain is the evolution of an object of missing_data.frame class with 400 observations on 7 vari

The next step is very important and essentially verifies whether enough iterations were conducted. We want the mean of each completed variable to be roughly the same for each of the 4 chains.

```
round(mipply(imputations, mean, to.matrix = TRUE), 3)
```

```
##
                      chain:1 chain:2 chain:3 chain:4
## ppvtr.36
                        0.007
                                 0.001
                                        -0.009
                                                  0.012
## first
                        1.435
                                 1.435
                                          1.435
                                                  1.435
## b.marr
                        1.685
                                 1.685
                                         1.685
                                                  1.685
                                         9.542
## income
                        9.553
                                 9.462
                                                  9.562
                                         0.000
## momage
                        0.000
                                 0.000
                                                  0.000
                        2.047
## momed
                                 2.020
                                          2.047
                                                  2.067
## momrace
                        2.277
                                 2.255
                                         2.285
                                                  2.275
## missing_ppvtr.36
                        0.188
                                 0.188
                                         0.188
                                                  0.188
## missing_b.marr
                        0.030
                                 0.030
                                         0.030
                                                  0.030
```

```
## missing_income 0.205 0.205 0.205 0.205
## missing_momed 0.100 0.100 0.100 0.100
## missing_momrace 0.292 0.292 0.292 0.292
```

Rhats(imputations)

##	mean_ppvtr.36	${\tt mean_b.marr}$	${\tt mean_income}$	${\tt mean_momed}$
##	0.9963562	0.9864222	1.0247337	1.0097897
##	mean_momrace	sd_ppvtr.36	sd_b.marr	sd_income
##	1.0489513	0.9914262	0.9864756	1.0514557
##	sd_{momed}	sd_momrace		
##	0.9931345	0.9924724		

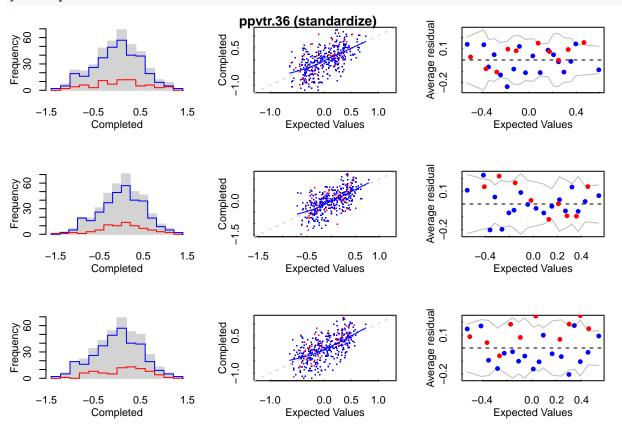
If so — and when it does in the example depends on the pseudo-random number seed — we can procede to diagnosing other problems. For the sake of example, we continue our 4 chains for another 5 iterations by calling

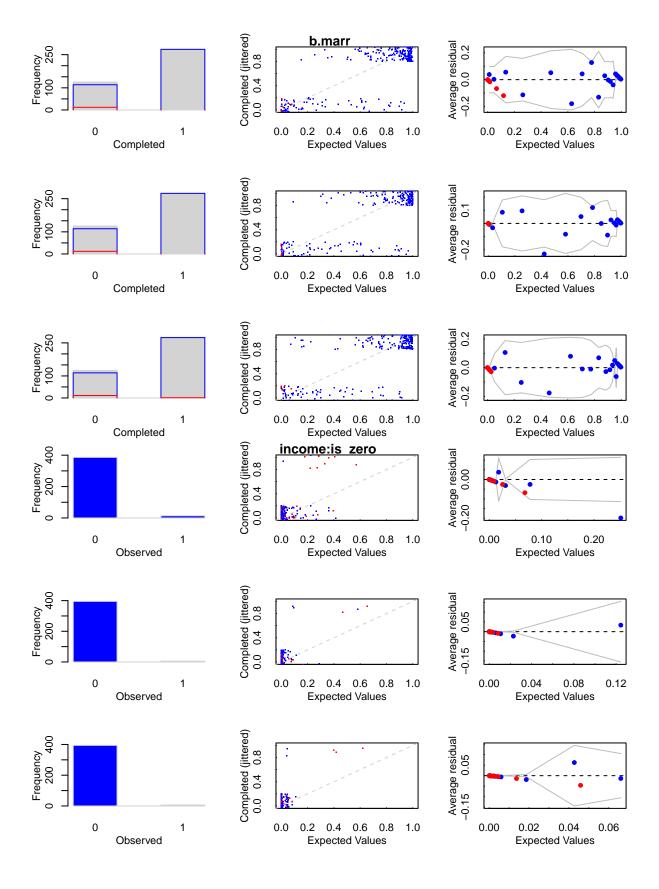
```
imputations <- mi(imputations, n.iter = 5)</pre>
```

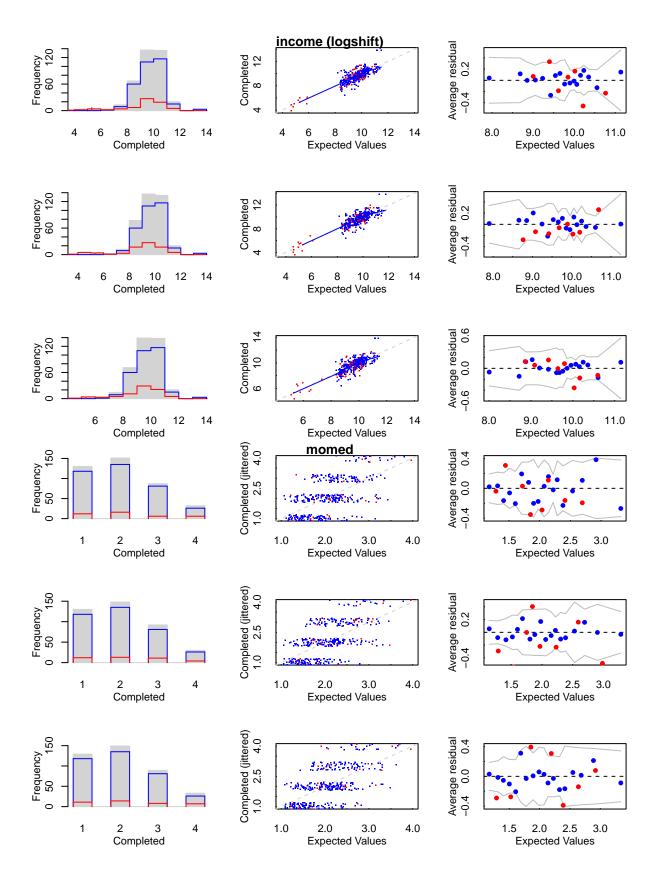
to illustrate that this process can be continued until convergence is reached.

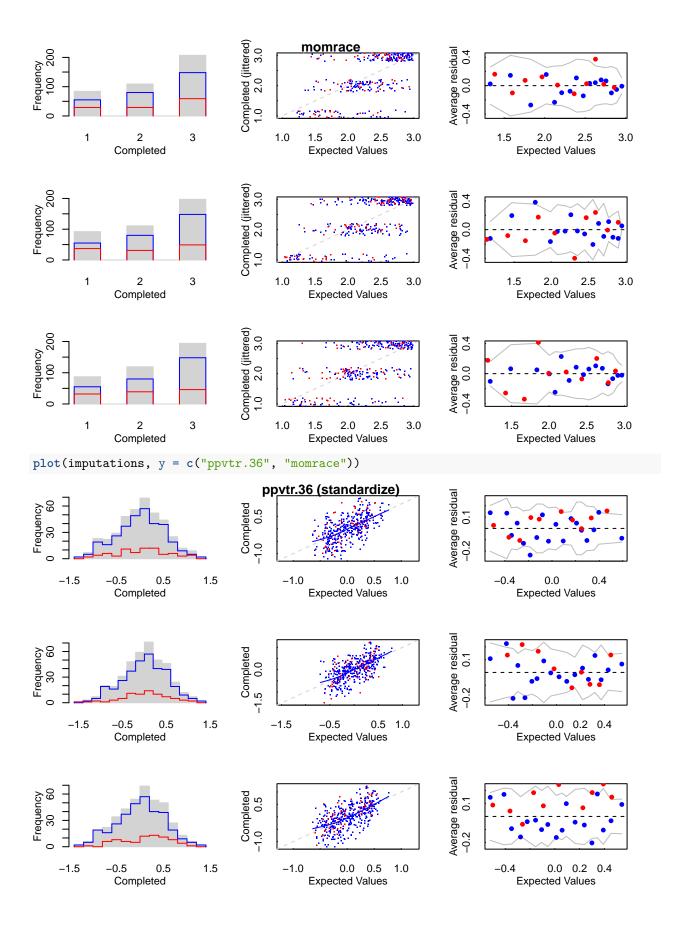
Next, the plot of an object produced by mi displays, for all missing_variables (or some subset thereof), a histogram of the observed, imputed, and completed data, a comparison of the completed data to the fitted values implied by the model for the completed data, and a plot of the associated binned residuals. There will be one set of plots on a page for the first three chains, so that the user can get some sense of the sampling variability of the imputations. The hist function yields the same histograms as plot, but groups the histograms for all variables (within a chain) on the same plot. The imagefunction gives a sense of the missingness patterns in the data.

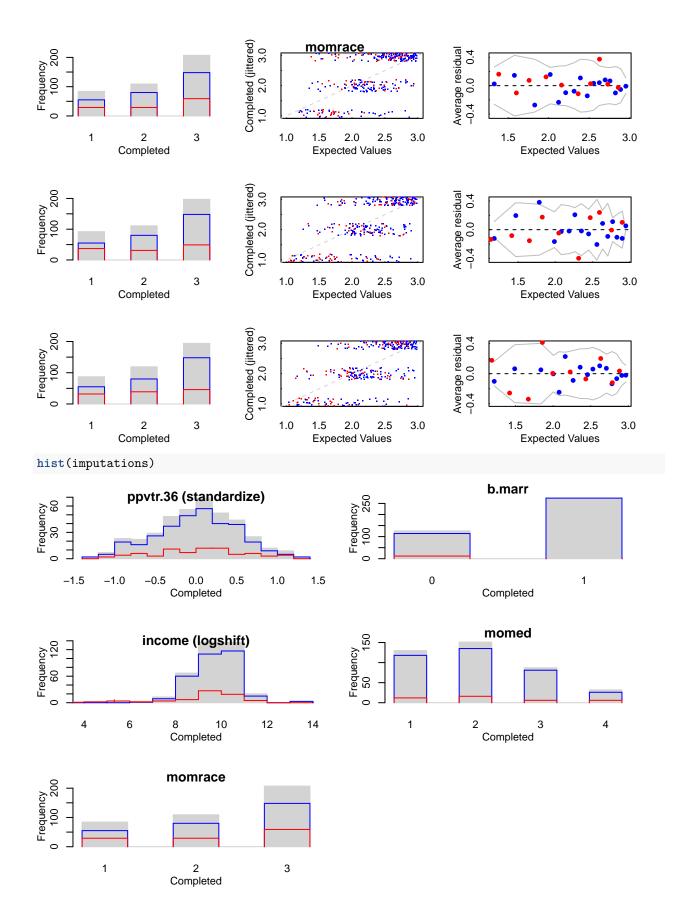
plot(imputations)

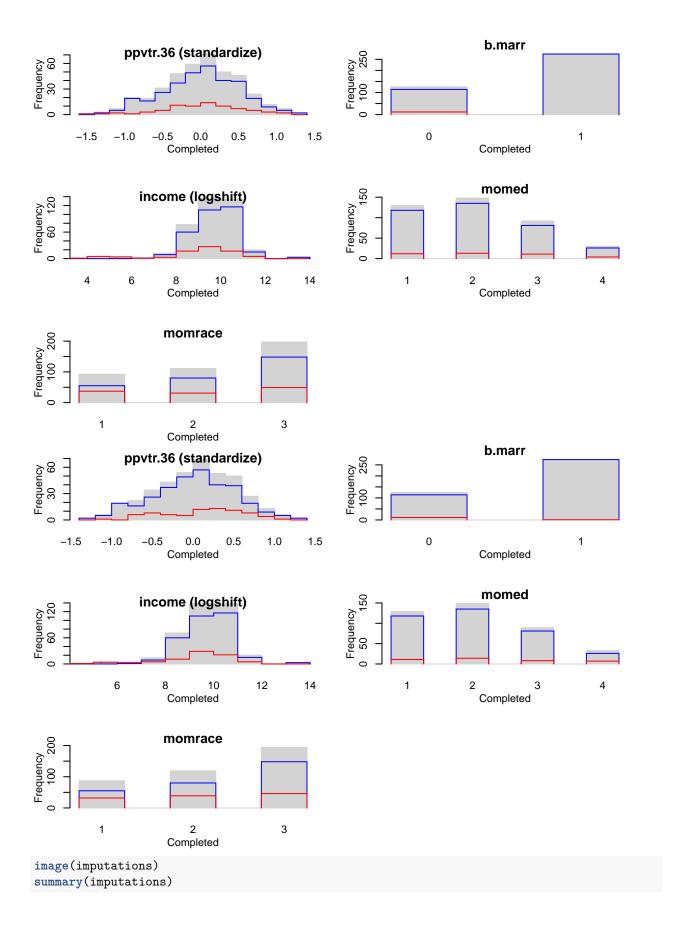






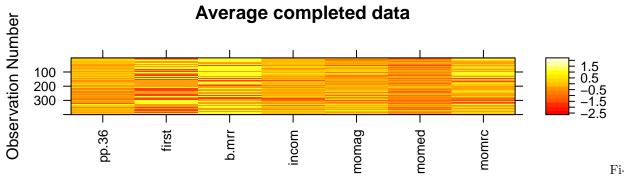






```
## $ppvtr.36
## $ppvtr.36$is_missing
## missing
## FALSE TRUE
##
     325
           75
##
## $ppvtr.36$imputed
       Min. 1st Qu.
                      Median
                                 Mean 3rd Qu.
## -1.48248 -0.30522 0.09308 0.05732 0.38357 1.46177
##
## $ppvtr.36$observed
       Min. 1st Qu.
                      Median
                                 Mean 3rd Qu.
                                                   Max.
## -1.20189 -0.31924 0.02848 0.00000 0.34944 1.23210
##
##
## $first
## $first$is_missing
## [1] "all values observed"
## $first$observed
##
##
   1 2
## 226 174
##
##
## $b.marr
## $b.marr$crosstab
##
##
       observed imputed
##
     0
           456
                     47
##
     1
           1096
                      1
##
##
## $income
## $income$is_missing
## missing
## FALSE TRUE
##
     318
           82
##
## $income$imputed
     Min. 1st Qu. Median
                            Mean 3rd Qu.
     3.205 8.064
                    9.318
                            8.800 10.049 11.985
##
## $income$observed
     Min. 1st Qu. Median
                             Mean 3rd Qu.
##
     5.323
           9.079
                    9.804
                            9.699 10.358 13.872
##
##
## $momage
## $momage$is_missing
## [1] "all values observed"
##
## $momage$observed
##
       Min. 1st Qu.
                      Median
                                 Mean 3rd Qu.
```

```
## -1.21377 -0.27468 0.03835 0.00000 0.35137 1.29046
##
##
## $momed
##
   $momed$crosstab
##
##
        observed imputed
              472
##
      1
##
      2
              540
                          58
              324
                         35
##
      3
##
              104
                          21
##
##
##
   $momrace
##
   $momrace$crosstab
##
##
        observed imputed
##
      1
              220
                        128
##
      2
              320
                        133
      3
              592
##
                        207
                                           Original data
Observation Number
      100
      200
     300
                 pp.36
                            first
                                       b.mrr
                                                   incom
                                                                                    momrc
                                                              nomag
                                                                         momed
```



nally, we pool over $\mathtt{m}=5$ imputed datasets – pulled from across the 4 chains – in order to estimate a descriptive linear regression of test scores (ppvtr.36) at 36 months on a variety of demographic variables pertaining to the mother of the child.

```
## bayesglm(formula = ppvtr.36 ~ first + b.marr + income + momage +
## momed + momrace, data = imputations, m = 5)
```

```
##
               coef.est coef.se
## (Intercept) 79.59
                         8.91
                3.98
                         1.93
## first1
## b.marr1
                5.35
                         2.61
## income
                0.00
                         0.00
## momage
               -0.02
                         0.37
## momed.L
               10.77
                         2.62
## momed.Q
                0.40
                         2.98
## momed.C
                0.19
                         2.07
## momrace2
               -6.67
                         3.30
## momrace3
               11.45
                         2.71
## n = 390, k = 10
## residual deviance = 91558.0, null deviance = 140303.1 (difference = 48745.1)
## overdispersion parameter = 234.8
## residual sd is sqrt(overdispersion) = 15.32
```

The rest is optional and only necessary if you want to perform some operation that is not supported by the **mi** package, perhaps outside of R. Here we create a list of **data.frames**, which can be saved to the hard disk and / or exported in a variety of formats with the **foreign** package. Imputed data can be exported to Stata by using the **mi2stata** function instead of **complete**.

```
dfs <- complete(imputations, m = 2)</pre>
```