momentuHMM: R package for analysis of telemetry data using generalized multivariate hidden Markov models of animal movement

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RUNNING HEAD: R package momentuHMM

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Summary

- 1. Discrete-time hidden Markov models (HMMs) have become an immensely popular tool for inferring latent animal behaviors from telemetry data, largely because they are relatively fast and easy to implement when data streams are observed without error and at regular time intervals. While movement HMMs typically rely solely on location data, auxiliary biotelemetry and environmental data are powerful and readily-available resources for incorporating much more behavioral realism and inferring ecological relationships that would otherwise be difficult or impossible to infer from location data alone. However, there is a paucity of generalized user-friendly software available for implementing (multivariate) HMMs of animal movement. Furthermore, location measurement error, temporal irregularity, and other forms of missing data are often pervasive in telemetry studies (particularly in marine systems).
- 2. Here we introduce an open-source R package, momentuHMM, that addresses many of the deficiencies in existing software. Features for multivariate HMMs in momentuHMM include: 1) tools for data pre-processing and visualization; 2) user-specified probability distributions for an unlimited number of data streams, such as those based on location (e.g., step length, turning angle) and auxiliary biotelemetry data (e.g., from pressure, conductivity, heart rate, or motion sensors); 3) user-specified design matrices and constraints for covariate modelling of state transition probability and probability distribution parameters using linear model formulas familiar to most R users; 4) multiple imputation methods that account for observation error attributable to measurement error and temporally-irregular or missing data; 5) seamless integration of spatio-temporal environmental covariate data (e.g., wind direction, forest cover, sea ice concentration) using rasters; 6) incorporation of "activity center" effects on parameters (e.g., areas associated with attractive or repulsive forces); 7) circular-circular regression models for angular probability distributions; 8) cosinor and spline regression formulas for cyclical (e.g., daily, seasonal) and other complicated patterns; and 9) data simulation capabilities for power analyses and assessing model performance, including simulation of location data subject to temporal irregularity and/or measurement error.
- **3.** After providing a brief introduction to (multivariate) HMMs for telemetry data, we demonstrate some of the capabilities of momentuHMM using real-world examples. This brief tutorial includes workflows for data formatting, model specification, model fitting, and diagnostics.

4. While many of the features of momentuHMM were motivated by animal movement data, the package can be used for analyzing any type of data that is amenable to (multivariate) HMMs. Practitioners interested in additional features for momentuHMM are encouraged to contact the authors.

Key-words biologging, biotelemetry, crawl, moveHMM, state-space model, state-switching

1 Introduction

Discrete-time hidden Markov models (HMMs) have become immensely popular for the analysis of animal telemetry data (e.g. Morales et al. 2004; Jonsen et al. 2005; Langrock et al. 2012; McClintock et al. 2012). In short, an HMM is a time series model composed of a (possibly multivariate) observation process $(\mathbf{Z}_1, \ldots, \mathbf{Z}_T)$, in which each data stream is generated by N state-dependent probability distributions, and where the unobservable (hidden) state sequence $(S_t \in \{1, \ldots, N\}, t = 1, \ldots, T)$ is assumed to be a Markov chain. The state sequence of the Markov chain is governed by (typically first-order) state transition probabilities, $\gamma_{ij}^{(t)} = \Pr(S_{t+1} = j \mid S_t = i)$ for $i, j = 1, \ldots, N$, and an initial distribution $\delta^{(0)}$. The likelihood of an HMM can be succinctly expressed using the forward algorithm:

$$\mathcal{L} = \boldsymbol{\delta}^{(0)} \boldsymbol{\Gamma}^{(1)} \mathbf{P}(\mathbf{z}_1) \boldsymbol{\Gamma}^{(2)} \mathbf{P}(\mathbf{z}_2) \boldsymbol{\Gamma}^{(3)} \cdots \boldsymbol{\Gamma}^{(T-1)} \mathbf{P}(\mathbf{z}_{T-1}) \boldsymbol{\Gamma}^{(T)} \mathbf{P}(\mathbf{z}_T) \mathbf{1}^N$$
(1)

where $\mathbf{\Gamma}^{(t)} = \left(\gamma_{ij}^{(t)}\right)$ is the $N \times N$ transition probability matrix, $\mathbf{P}(\mathbf{z}_t) = \operatorname{diag}(p_1(\mathbf{z}_t), \dots, p_N(\mathbf{z}_t))$, $p_s(\mathbf{z}_t)$ is the conditional probability density of \mathbf{Z}_t given $S_t = s$, and $\mathbf{1}^N$ is a N-vector of ones (for a thorough introduction to HMMs see Zucchini *et al.* 2016).

One of the most common discrete-time animal movement HMMs for telemetry location data is composed of two data streams, step length and turning angle (or bearing), which are calculated for each of the T time steps from the temporally-regular observations of an animal's position, (x_t, y_t) , for t = 1, ..., T + 1 (e.g. Morales $et \ al. \ 2004$; Langrock $et \ al. \ 2012$; McClintock $et \ al. \ 2012$). Step length (l_t) is typically calculated as the Euclidean distance between the locations (x_t, y_t) and (x_{t+1}, y_{t+1}) , while turning angle (ϕ_t) is calculated as the change in bearing $(b_t = \tan 2(y_{t+1} - y_t, x_{t+1} - x_t))$ between the intervals [t-1,t] and [t,t+1] (e.g. $\phi_t = 0$ if $b_{t-1} = b_t$). For this HMM composed of 2 data streams, $\mathbf{z}_t = (l_t, \phi_t)$, and, conditional on the latent state S_t , independent prob-

ability distributions are typically assumed for each stream, e.g., $p_s(\mathbf{z}_t) = p_s(l_t)p_s(\phi_t)$. Some common probability distributions for the step length data stream are the gamma or Weibull distributions, while the wrapped Cauchy or von Mises distributions are often employed for turning angle or bearing.

While HMMs for animal movement based solely on location data are somewhat limited in the number and type of biologically-meaningful movement behavior states they are able to accurately identify, advances in biologging technology are now allowing the collection of valuable auxiliary biotelemetry data (e.g., dive activity, accelerometer, heart rate, stomach temperature), which, when combined with location data, allow for multivariate HMMs that can incorporate much more behavioral realism and facilitate inferences about complex ecological relationships that would otherwise be difficult or impossible to infer from location data alone (e.g. McClintock et al. 2013; DeRuiter et al. 2017; McClintock et al. 2017). Multivariate HMMs that utilize both location and auxiliary biotelemetry data can facilitate the identification of additional states that go beyond the N=2 state approaches that are most frequently used by practitioners. For example, the most widely used 2-state HMMs for animal movement include "encamped" (or "foraging") and "exploratory" (or "transit") states characterized by area-restrictedsearch-type movements (shorter step lengths with little to no directional persistence) and migratory-type movements (longer step lengths with high directional persistence), respectively (Morales et al. 2004; Jonsen et al. 2005). However, very different behaviors can exhibit similar horizontal trajectories. For example, for herbivores such as North American elk (Morales et al. 2004) or central-place foragers such as harbour seals (Mc-Clintock et al. 2013), the horizontal trajectories of "resting" and "foraging" movements can be very difficult to distinguish. Standard 2-state HMMs based solely on horizontal trajectory will tend to lump these behaviors together, and this could have unintended consequences if, for example, one intends to use the estimated state sequences to identify foraging habitat. In order to tweeze apart distinct behaviors with similar horizontal trajectories, additional states can be informed by auxiliary information (such as mandible accelerometer or dive data), incorporated as additional data stream(s) in a multivariate HMM.

When data streams are observed without error and at regular time intervals, a major advantage of HMMs is the relatively fast and efficient maximization of the likelihood using the forward algorithm (Eq. 1). However, location measurement error is rarely

non-existent in animal-borne telemetry studies and depends on both the device and the system under study. For example, GPS errors are typically less than 50m, but Argos errors can exceed 10km (e.g. Costa et al. 2010). An extreme case of missing data can arise when location data are obtained with little or no temporal regularity, as in many marine mammal telemetry studies (e.g. Jonsen et al. 2005), such that few (if any) observations align with the regular time steps required by discrete-time HMMs. When explicitly accounting for uncertainty attributable to location measurement error, temporally-irregular observations, or other forms of missing data, one must typically fit (multivariate) HMMs using computationally-intensive (and often time-consuming) model fitting techniques such as Markov chain Monte Carlo (Jonsen et al. 2005; McClintock et al. 2012). However, complex analyses requiring novel statistical methods and custom model-fitting algorithms are not practical for many practitioners.

While statisticians have been applying HMMs to telemetry data for decades, R (R Core Team 2016) packages such as bsam (Jonsen et al. 2005), moveHMM (Michelot et al. 2016), and swim (Whoriskey et al. 2017) have recently helped make these models of animal movement behavior more accessible to the practitioners that are actually conducting telemetry studies. These advances represent important steps toward making HMMs of animal movement more accessible, but the models that can currently be implemented using existing software remain limited in many key respects. For example, existing HMM software for animal movement is limited to two data streams based solely on location data (e.g. step length and turning angle), and while moveHMM allows for a user-specified number of latent behavioral states (bsam and swim are limited to N=2 states), it is typically difficult to identify >2 biologically-meaningful behavior states from only 2 data streams (e.g. Morales et al. 2004; Beyer et al. 2013; McClintock et al. 2014). Both moveHMM and swim are designed for temporally-regular (or linearly-interpolated) location data with negligible measurement error, but the realities of animal-borne telemetry often yield temporally-irregular location data subject to error (particularly in aquatic environments). Other notable deficiencies of existing software include limited abilities to incorporate spatio-temporal environmental or individual covariates on parameters, biased (or directed) movements in response to attractive or repulsive forces (e.g. McClintock et al. 2012; Langrock et al. 2014), cyclical (e.g. daily, seasonal) and other more complicated behavioral patterns, or constraints on parameters.

To address these defeciencies in existing software, we introduce a new user-friendly R package, momentuHMM (Maximum likelihood analysis Of animal MovemENT behavior Using multivariate Hidden Markov Models), intended for practitioners wishing to implement more flexible and realistic (multivariate) HMM analyses of animal movement while accounting for common challenges associated with telemetry data. Features for multivariate HMM analyses in momentuHMM include: 1) tools for data pre-processing and visualization; 2) user-specified probability distributions for an unlimited number of data streams and latent behavior states; 3) user-specified design matrices and constraints for covariate modelling of state transition probability and probability distribution parameters using linear model formulas familiar to most R users; 4) multiple imputation methods that account for observation error attributable to measurement error and temporally-irregular or missing data (Hooten et al. 2017; McClintock 2017); 5) seamless integration of spatio-temporal environmental covariate data (e.g., wind direction, forest cover, sea ice concentration) using the raster package (Hijmans 2016b); 6) incorporation of "activity center" effects (e.g., areas associated with attractive or repulsive forces); 7) circular-circular regression models for angular probability distributions (Duchesne et al. 2015); 8) cosinor (e.g. Cornelissen 2014) and spline regression formulas for cyclical and other complicated behavioral patterns; and 9) data simulation capabilities for power analyses and assessing model performance, including simulation of location data subject to temporal irregularity and/or measurement error.

In the following tutorial, we demonstrate some of the capabilities of momentuHMM using real-world examples, including an example of periodic cycles in African elephant movement, a 3-state ("resting", "foraging", "transit") northern fur seal example incorporating auxiliary dive activity data (McClintock et al. 2014), a loggerhead turtle example relating "foraging" and "transit" movements to ocean surface currents, and a 5-state grey seal example incorporating biased movements toward haul-out and foraging locations (McClintock et al. 2012). This brief tutorial includes workflows for data formatting, model specification, model fitting, and diagnostics. While many of the features of momentuHMM were motivated by animal movement data, the package can be used for analyzing any type of data that is amenable to (multivariate) HMMs. Additional information, including help files, data, examples, and package usage is available by downloading the momentuHMM package from CRAN (cran.r-project.org) or Github (github.com/bmcclintock/momentuHMM). This article describes momentuHMM version

Table 1. Workhorse functions for the R package momentuHMM.

Function	Description		
crawlMerge	Merge crawlWrap output with additional data streams or covariates		
crawlWrap	Fit crawl models and predict temporally-regular locations		
fitHMM	Fit a (multivariate) HMM to the data		
MIfitHMM	Fit (multivariate) HMMs to multiple imputation data		
MIpool	Pool momentuHMM model results across multiple imputations		
plot.crwData	Plot crawlWrap output		
plot.miSum	Plot summaries of multiple imputation momentuHMM models		
<pre>plot.momentuHMM</pre>	Plot summaries of momentuHMM models		
plot.momentuHMMData	Plot summaries of selected data streams and covariates		
plotPR	Plot time series, qq-plots and sample ACFs of pseudo-residuals		
plotSat	Plot locations on satellite image		
${ t plotSpatialCov}$	Plot locations on raster image		
plotStates	Plot the (Viterbi-)decoded states and state probabilities		
${ t prepData}$	Pre-process data streams and covariates		
pseudoRes	Calculate pseudo-residuals for momentuHMM models		
simData	Simulate movement data using a (multivariate) HMM		
stateProbs	State probabilities for each time step		
viterbi	Most likely state sequence (using the Viterbi algorithm)		

1.0.1.

2 momentuHMM overview

Before delving into some of the finer details, we will first provide an overview of the main features and functions of the package. While space is limited in this tutorial, further details on implementation can be found in the package's documentation and vignette. The workhorse functions of momentuHMM are listed in Table 1. Usage of several of these functions (e.g. fitHMM, prepData, simData) is deliberately very similar to equivalent functions in moveHMM (Michelot et al. 2016), but the momentuHMM arguments for these functions have been generalized and expanded to accommodate a more flexible framework for data pre-processing, model specification, parameterization, and simulation. Rusers already familiar with moveHMM will therefore likely find it easy to immediately begin using momentuHMM.

One of the key features of momentuHMM is the ability to specify an unlimited number of HMM data streams from a broad range of commonly used probability distributions. Any of the parameters of the probability distributions used for the observed data can be modelled as a function of environmental and individual covariates using link functions (Table 2). For any given "natural scale" (or "real scale") probability distribution parameter θ , all of the link functions (g) in momentuHMM are of the general form $g(\theta) = \mathbf{X}_{\theta} \boldsymbol{\beta}_{\theta}$, where \mathbf{X}_{θ} is the $T \times k$ design matrix (composed of k covariates) and $\boldsymbol{\beta}_{\theta}$ is the correponding k-vector of "working scale" (or "beta scale") parameters for θ . For example, suppose step length is assumed to have a gamma distribution, $l_t \mid S_t = s \sim \text{gamma}(\mu_s, \sigma_s)$. In momentuHMM, the natural scale parameters for the gamma distribution are the (state-dependent) step length mean $(\mu_s > 0)$ and standard deviation $(\sigma_s > 0)$. Because both of these parameters must be positive, the log link function is a natural choice for modelling these parameters as a function of covariates, e.g., $\log(\boldsymbol{\mu}) = \mathbf{X}_{\mu} \boldsymbol{\beta}_{\mu}$.

The state transition probabilities can also be modelled as functions of covariates, using a multinomial logit link, as described e.g. by Michelot *et al.* (2016).

2.1 Data preparation and visualization

For temporally-regular location data with negligible measurement error, the prepData function is used to create a momentuHMMData object that can be used for data visualization and further analysis. The arguments for prepData include:

- data A data frame with T+1 rows including optionally a field 'ID' (identifiers for different individuals), coordinates from which step length ('step') and turning angle ('angle') data streams are to be calculated, any additional data streams, and any covariates identified in the covNames and angleCovs arguments. Altervatively, data can be a crwData object returned by crawlWrap.
- type Coordinate type; 'UTM' if easting-northing or 'LL' if longitude-latitude.
- coordNames Names of the two coordinate columns in data. If coordNames=NULL then step lengths, turning angles, and any location-based covariates (i.e., those specified by spatialCovs, centers, and angleCovs) are not calculated.
- covNames Character vector indicating the names of any covariates in data. Any variables in data (other than "ID") that are not identified in covNames or angleCovs are assumed to be data streams.

Table 2. Data stream (z) probability distributions, natural parameters, and default link functions for covariate modelling. Probability distributions with positive support can be zero-inflated (with additional zero-mass parameters), while the beta distribution can be zero- and one-inflated (with additional one-mass parameters). If user-specified bounds are provided, then custom link functions are used instead of the defaults (see package documentation for further details). If circular-circular regression is specified for the mean of angular distributions ("vm" and "wrpcauchy"), then the link function described in Duchesne et al. (2015) is used. Users seeking additional probability distributions are encouraged to contact the authors.

Distribution	Support	Parameters	Link function
Beta ("beta")	$z_t \in (0,1)$	$\mathtt{shape1} > 0$	log
		$\mathtt{shape2} > 0$	log
		$\texttt{zero-mass} \in (0,1)$	logit
		$\mathtt{one\text{-}mass} \in (0,1)$	logit
Exponential ("exp")	$z_t > 0$	$\mathtt{rate} > 0$	\log
		$\texttt{zero-mass} \in (0,1)$	logit
Gamma ("gamma")	$z_t > 0$	$\mathtt{mean} > 0$	\log
		$\operatorname{sd} > 0$	\log
		$\texttt{zero-mass} \in (0,1)$	logit
Log normal ("lnorm")	$z_t > 0$	$\texttt{location} \in {\rm I\!R}$	identity
		$\mathtt{scale} > 0$	log
		$\texttt{zero-mass} \in (0,1)$	logit
Poisson ("pois")	$z_t \in \{0, 1, \ldots\}$		\log
Von Mises ("vm")	$z_t \in (-\pi, \pi]$	$\mathtt{mean} \in (-\pi,\pi]$	$ an(\mathtt{mean}/2)$
		${\tt concentration} > 0$	log
Weibull ("weibull")	$z_t > 0$	$\mathtt{shape} > 0$	\log
		$\mathtt{scale} > 0$	log
		$\texttt{zero-mass} \in (0,1)$	logit
Wrapped Cauchy ("wrpcauchy")	$z_t \in (-\pi, \pi]$	$\mathtt{mean} \in (-\pi,\pi]$	$\tan(\mathtt{mean}/2)$
		$\mathtt{concentration} \in (0,1)$	logit

- spatialCovs List of Raster-class objects (Hijmans 2016b) containing spatiotemporally referenced covariates. Covariates specified by spatialCovs are extracted from the raster layer(s) based on the location data. Raster stacks may also be included, in which case the appropriate z values (e.g. time, date) must also be included in data.
- centers 2-column matrix providing the coordinates for any activity centers (e.g., potential centers of attraction or repulsion) from which distance and angle covariates will be calculated based on the location data and returned in the momentuHMMData object.
- angleCovs Character vector indicating the names of any circular-circular regression angular covariates in data or spatialCovs that need conversion from standard direction (in radians relative to the x-axis) to turning angle (relative to previous movement direction).

Summary plots of the momentuHMMData object returned by prepData can be created for any data stream or covariate using the generic plot function.

If location data are temporally-irregular or subject to measurement error, then they are not suitable for prepData. In this case, momentuHMM can be used to perform a 2-stage multiple imputation approach (McClintock 2017). We discuss this pragmatic approach to incorporating uncertainty attributable to observation error and temporal irreglarity into multivariate HMM analyses in section 2.3.

2.2 HMM specification and fitting

Once a momentuHMMData object has been created using prepData, then the data are ready to be passed to the generalized multivariate HMM-fitting function fitHMM. There are many different options for specifying HMMs using fitHMM, so here we will only focus on several of the most important and useful features (further details of all fitHMM arguments are in the package documentation). The bare essentials of fitHMM include the arguments:

- data A momentuHMMData object
- nbStates Number of latent states (N)

- dist A named list indicating the probability distributions of the data streams.
- estAngleMean An optional named list indicating whether or not to estimate the angle mean for data streams with angular distributions (e.g. turning angle). If not estimated (the default), the angle mean is fixed to 0.
- formula Regression formula for the transition probability covariates
- stationary Logical indicating whether or not the initial distribution is considered equal to the stationary distribution (must be FALSE if formula includes covariates)
- Par0 A named list containing vectors of starting values for the state-dependent probability distribution parameters of each data stream

These seven arguments are all that are needed in order to fit the HMMs currently supported in moveHMM (Michelot et al. 2016). For example, here is how the analysis of 15 "wild haggis" tracks described in Michelot et al. (2016) would be implemented using momentuHMM:

```
> library(momentuHMM)
> ### Load raw data
> rawHaggis<-read.csv("rawHaggises.csv")</pre>
> ### Process data
> processedHaggis<-prepData(data=rawHaggis,covNames=c("slope","temp"))</pre>
> ### Fit HMM
> # initial step distribution natural scale parameters
> stepPar0 <- c(1,5,0.5,3) # (mu_1,mu_2,sd_1,sd_2)
> # initial angle distribution natural scale parameters
> anglePar0 < c(0,0,1,8) # (mean_1,mean_2,concentration_1,concentration_2)
> fitHaggis <- fitHMM(data = processedHaggis, nbStates = 2,</pre>
                      dist = list(step = "gamma", angle = "vm"),
                      Par0 = list(step = stepPar0, angle = anglePar0),
                       formula = ~ slope + I(slope^2),
                       estAngleMean = list(angle=TRUE))
+
```

Note that many of the arguments in fitHMM are lists, with each element of the list corresponding to a data stream. The list names provided in dist, ParO, and estAngleMean (e.g. 'step' and 'angle') must therefore have a corresponding column in data with the same name. Additional data streams can be added to the model by simply adding the additional elements to these list arguments (see example in section 3.2).

As seen above, the formula argument can include many of the functions and operators commonly used to construct terms in R linear model formulas (e.g. a*b, a:b, cos(a)). Unique to momentuHMM, the formula argument can also be used to specify transition probability matrix models that incorporate cyclical patterns (using the cosinor special function; see example in section 3.1), splines for explaining other more complicated patterns (e.g., bs and ns functions in the R base package splines), and factor variables (e.g., formula=~ID for individual-level effects). By default the formula argument applies to all state transition probabilities, but the special functions state and betaCol allow for state- and parameter-specific formulas to be specified (see example in section 3.4). Specific state transition probabilities can also be fixed to zero (or any other value) using the fixPar argument, which can be useful for incorporating more behavioral realism. For example, fixPar can be used to prohibit or enforce switching from one particular state to another (possibly as a function of spatio-temporal covariates).

Similar to the formula argument for state transition probability modelling, it is through the DM argument of fitHMM that models are specified for the state-dependent probability distribution parameters for each data stream. DM is a list argument containing an element for each data stream, but each element itself is also a list specifying the design matrix formulas for each parameter. For example, the following fits the exact same wild haggis model as above, but employs a user-specified (intercept-only) design matrix for the step length data stream:

Note that when DM is specified for a data stream, the initial parameter values (ParO) for that data stream now correspond to columns of the resulting design matrix and must be on the working scale instead of the natural scale. In this case, because the log link is used for the natural parameters of the gamma distribution, ParO\$step was specified on the log scale. The functions getParO and getParDM are designed to assist users

in the specification of design matrices and corresponding initial values on the working scale for any given model (see package documentation for further details). DM formulas are just as flexible as the formula argument and, in addition to common linear model formula functions and operators, can also include cyclical cosinor models, splines, factor variables, and state-specific probability distribution parameter formulas (see examples in sections 3.3 and 3.4). As with the state transition probabilities, working parameters for probability distributions can also be fixed to user-specified values using the fixPar argument.

Specification of design matrices using DM is not limited to formulas. Alternatively, "pseudo-design" matrices can be specified, using an R matrix with rows corresponding to the natural parameters and columns corresponding to the working parameters. The elements in the matrix may be numeric or character strings containing model formula terms (see examples in sections 3.2 and 3.4). Using a pseudo-design matrix for step length, the following is yet another way to implement the exact same wild haggis model:

(note that column and rownames for pseudo-design matrices are not required but can be useful). Pseudo-design matrices allow for the sharing of common working parameters (such as intercept terms) among natural scale parameters, and this can be used to constrain natural scale parameters (e.g., $\mu_1 \leq \mu_2$) when used in tandem with the cons argument. This is particularly useful for preventing state label switching when repeatedly fitting the same HMM using multiple imputation methods (see section 2.3).

Another noteworthy fitHMM argument, circular AngleMean, is a list argument that enables users to specify circular-circular regression models for the mean (μ) parameter

of angular distributions, such as the wrapped Cauchy and von Mises, instead of circular-linear models based on the tangent link function (Table 2). When circularAngleMean is specified as TRUE for any given angular data stream (e.g. turning angle), then a special link function based on Duchesne *et al.* (2015) is used:

$$\boldsymbol{\mu} = \operatorname{atan2}(\sin(\mathbf{X}_{\mu})\boldsymbol{\beta}_{\mu}, 1 + \cos(\mathbf{X}_{\mu})\boldsymbol{\beta}_{\mu}), \tag{2}$$

where \mathbf{X}_{μ} is a $T \times k$ matrix composed of the turning angles between k angular covariates (e.g., wind direction, sea surface currents) and the bearing of movement during the previous time step, i.e., each element

$$x_{t,i} = \operatorname{atan2}(\sin(r_{t,i} - b_{t-1}), \cos(r_{t,i} - b_{t-1}))$$
(3)

for angular covariate $r_{t,i}$ and $i=1,\ldots,k$ (note that prepData calculates \mathbf{X}_{μ} based on the angleCovs or centers arguments so users need not bother). Because this link function is designed for turning angles, a turning angle of 0 is provided as the reference angle (hence the "1+" preceding the cosine term in Eq. 2). Thus as a trade-off between biased and correlated movements, the working parameters ($\boldsymbol{\beta}_{\mu}$) for the expected turning angle at time t weight the attractive (or repulsive) strengths of the angular covariates relative to directional persistence. When all $\boldsymbol{\beta}_{\mu}=0$, the model reduces to a correlated random walk, but an increasingly biased random walk results as $\boldsymbol{\beta}_{\mu}$ gets larger (or smaller). Many interesting hypotheses about animal movement can be addressed using circular-circular regression on movement direction, including the effects of wind, sea surface currents (see example in section 3.3), and centers of attraction or repulsion (see example in section 3.4)

2.3 Multiple imputation

When location data are temporally-irregular or subject to measurement error, then they are not suitable for standard maximum-likelihood HMM analyses based on the forward algorithm (Eq. 1). In this case, momentuHMM can be used to perform the 2-stage multiple imputation approach of McClintock (2017). The basic concept is to first employ a single-state (i.e., N=1) movement model that is relatively easy to fit but can accommodate location measurement error and temporally-irregular or missing observations (e.g. Johnson et al. 2008). The second stage involves repeatedly fitting

the desired HMM to m temporally-regular realizations of the position process drawn from the model output of the first stage. Data streams or covariates that are dependent on location (e.g., step length, turning angle, habitat type, snow depth, sea surface temperature) will of course vary among the m realizations of the position process, and the pooled inferences across the HMM analyses therefore reflect location uncertainty.

There are three primary functions (MIfitHMM, MIpool, and crawlWrap) for performing multiple imputation HMM analyses in momentuHMM, and all rely on parallel processing to speed up computations. crawlWrap is a wrapper function for fitting the continuous-time correlated random walk (CTCRW) model of Johnson et al. (2008) to one or more tracks (subject to location measurement error and/or temporal irregularity) and then predicting temporally-regular tracks of the user's choosing (e.g. 15 min, hourly, daily) based on the CTCRW model output. crawlWrap returns a crwData object that can be used to draw m realization of the position process within the MIfitHMM function. MIfitHMM is essentially a wrapper function for fitHMM that repeatedly fits the same user-specified HMM to m imputed data sets and stores the output from each of the m model fits. If a crwData object is provided, then MIfitHMM will first draw m imputations based on the crwData output and then fit the specified HMM to each imputed data set. If users wish to use a movement model other than the CTCRW to account for measurement error and temporal irregularity (e.g. Calabrese et al. 2016; Gurarie et al. 2017), or if other observation error processes (e.g. missing data) are to be accounted for in the imputation step, MIfitHMM can also be used for analysis of a list of m momentuHMMData objects that were imputed by the user. Based on the m model fits, the MIpool function calculates pooled estimates, standard errors, and confidence intervals for the working scale parameters, natural scale parameters (based on transformations of the pooled working parameters and mean or user-specified values for any covariates), state sequences, state probabilities, and activity budgets (i.e. the proportion of the T times step assigned to each state) using standard multiple imputation formulae (Rubin & Schenker 1986; McClintock 2017). MIpool can be called separately or within MIfitHMM (using the poolEstimates argument), and the function returns a miSum object containing the pooled output across all imputations. See sections 3.2, 3.3, and 3.4 for example HMM analyses that use multiple imputation to account for location measurement error and temporally irregularity.

2.4 Model visualization and diagnostics

The generic plot functions for momentuHMM models (plot.momentuHMM and plot.miSum) plot the data stream histograms along with their corresponding estimated probability distributions, the estimated natural parameters and state transition probabilities as a function of any covariates included in the model, and the tracks of all individuals (color-coded by the most likely state sequence). By default, the probability distributions are plotted based on the means of any covariate values, but user-specified covariate values for the plots can be provided using the covs argument. When the argument plotCI=TRUE, then confidence intervals for the natural parameters and state transition probabilities are also plotted. Confidence intervals are calculated from the working parameter estimates based on the delta method and finite-difference approximations of the first derivative for the transformation using the numDeriv::grad function (Gilbert & Varadhan 2016). For multiple imputation analyses (plot.miSum), all plots are based on the pooled parameter estimates and the means of any covariates (if not provided by the covs argument) across each imputation. Using the argument errorEllipse, plot.miSum will include estimated location error ellipses in the plots of individual tracks. The functions plotSat, plotSpatialCov, and plotStates (Table 1) provide further methods for visualizing model results.

Diagnostic tools include the calculation and plotting of pseudo-residuals (Zucchini et al. 2016) using the pseudoRes and plotPR functions, respectively. Akaike's Information Criterion can be calculated for one or more models using the AIC.momentuHMM function.

2.5 Simulation

The function simData can be used to simulate multivariate HMM data from scratch or based on the estimated parameters of existing momentuHMM or miSum models. The simData arguments are very similar to those used for model specification in fitHMM (e.g., dist, DM) and data preparation in prepData (e.g., spatialCovs, centers), but they include additional arguments, lambda and errorEllipse, for simulating location data subject to temporal irregularity and measurement error, respectively. The spatialCovs argument allows for rasters of spatio-temporal covariate values to be utilized in simulation models, while the centers argument allows activity centers to be incorporated.

Thus simData can be used to simulate more ecologically-realistic tracks (potentially subject to observation error) that can be useful for study design, power analyses, and assessing model performance.

3 Examples

We will now demonstrate some of the capabilities of momentuHMM using real telemetry data. These examples are intended for demonstration purposes only, and we do not claim these example analyses represent improvements relative to previous or alternative analyses for these data sets. While only some of the key workflow elements are included here, complete R code and further details for these analyses are available in the "vignettes" source directory.

3.1 African elephant

As our first example, we use an African elephant (*Loxodonta africana*) bull track described in Wall *et al.* (2014) and publicly available from the movebank.org data repository.

We can load the data from the URL (this requires an Internet connection):

The data set contains two tracks; for this analysis, we only consider the first one. In addition to hourly locations, the tag also collected external temperature data. We subset the data frame to keep only the relevant rows and columns:

```
> # select and rename relevant columns
> rawData <- rawData[,c(11,3,4,5,6)]
> colnames(rawData) <- c("ID","time","lon","lat","temp")
> # only keep first track
> rawData <- subset(rawData,ID==unique(ID)[1])</pre>
```

The data now has the following columns:

```
> head(rawData)
```

```
ID
                                             lon
                                  time
                                                      lat temp
1 Salif Keita 2008-03-22 17:00:00.000 -2.160167 15.65350
                                                            38
2 Salif Keita 2008-03-22 18:00:00.000 -2.160075 15.65452
                                                            35
3 Salif Keita 2008-03-22 19:00:00.000 -2.159902 15.65451
                                                            32
4 Salif Keita 2008-03-22 20:00:00.000 -2.159435 15.65489
                                                            30
5 Salif Keita 2008-03-22 21:00:00.000 -2.158113 15.65512
                                                            29
6 Salif Keita 2008-03-22 22:00:00.000 -2.157848 15.65461
                                                            28
```

Location measurement error is negligible for these terrestrial GPS data, although about 1% of the hourly observations collected between 22 March 2008 and 30 September 2010 are missing. Instead of simply ignoring these missing data, we can employ crawlWrap to predict the missing locations based on the CTCRW model of Johnson et al. (2008) prior to conducting our HMM analysis.

To use crawlWrap, we convert times from factors to POSIX, and project the observed locations to UTM coordinates:

Then, we call crawlWrap to fit a CTCRW model and predict hourly locations:

```
> # initial parameters for crawl fit

> inits <- list(a = c(rawData$x[1],0,rawData$y[1],0),

+ P = diag(c(5000^2, 10*3600^2, 5000^2, 10*3600^2)))

> # fit crawl model

> crwOut <- crawlWrap(obsData=rawData, timeStep="hour", initial.state=inits,

+ theta=c(4,-10), fixPar=c(NA,NA))
```

Here the desired time step is specified by the timeStep argument, and the initial.state, theta, and fixPar arguments are the same as for crawl::crwMLE (Johnson 2017). For the choice of initial parameters in crawlWrap, we refer the reader to the documentation of the package crawl, in particular crawl::crwMLE and crawl::crwPredict. We now have a complete set of temporally-regular location data.

Autocorrelation function (ACF) estimates suggest there are 24-hour cycles in the step length data, and this presents an opporunity to demonstrate the use of the cosinor function for incorporating cyclical behavior in model parameters using momentuHMM. We create a momentuHMMData object, and the 24-hour cosinor model covariate:

```
> # create momentuHMMData object from crwData object
> elephantData <- prepData(data=crwOut, covNames="temp")
> # add cosinor covariate based on hour of day
> elephantData$hour <- as.integer(strftime(elephantData$time, format = "%H", tz="GMT")</pre>
```

As seen here, the function prepData can also be used for pre-processing the best predicted track data from crawlWrap output. The 24-hour cosinor covariate ("hour") is simply a set of integers (0, 1, ..., 23) indicating the hour of day for each observation. The ACF plot of the step lengths, shown in Figure 1, was obtained with:

```
> acf(elephantData$step[!is.na(elephantData$step)],lag.max=300)
```

Our aim is to fit a 2-state HMM to the elephant track that includes temperature effects on the turning angle concentration parameters and cycling temperature effects (with a 24-hour periodicity) on the step length and state transition probability parameters. Complex models such as this can require many parameters, and it can be challenging to choose good starting parameter values for the optimization. Here, we take an incremental approach, starting from a simpler model with no covariates. In momentuhm, the function getParO extracts initial parameters from a fitted (nested) HMM, given arguments for the more complex model.

For the covariate-free 2-state model, six initial parameters need to be chosen: for each state, the mean and standard deviation of the gamma distribution of step lengths, and the concentration of the wrapped Cauchy distribution of turning angles. Looking at the histograms of the step lengths and the turning angles (e.g. output by plot(elephantData)) is often useful to choose good starting parameter values.

To ensure convergence, we could also use the argument retryFits to specify the number of attempts to minimize the negative log-likelihood based on random perturbations of the parameter estimates at the current minimum.

We can build on complexity, by including the temperature and time of day as covariates in the state transition probabilities. We use the function getPar0 to extract the new starting parameter values.

The special function cosinor(hour, period = 24) internally creates the cosinor model covariates, $\cos(2\pi \times hour/period)$ and $\sin(2\pi \times hour/period)$, and includes both terms (plus interactions with "temp") in the fitted model.

Finally, we can fit the more complex model, including the effect of temperature and time of day on the parameters of the state-dependent distributions of steps and angles.

The above model m3 identified a state of slow undirected movement ("encamped"), and a state of faster and more directed movement ("exploratory") (Figure 1). For a fitted model, the function viterbi computes the most likely state sequence:

```
> # decode most likely state sequence
> states <- viterbi(m3)</pre>
```

```
> # derive percentage of time spent in each state
> table(states)/nrow(elephantData)
```

Here, about 74% of the steps were attributed to the "encamped" state, and 26% were attributed to the "exploratory" state.

We can use AIC(m1,m2,m3) to compare the three fitted models in terms of AIC; here, m3 is overwhelmingly supported by the AIC when compared to alternative models with fewer covariates.

The model can be visualized with the generic function plot, which was used for the plots shown in Figure 2, and the decoded track in Figure 1.

```
> plot(m3, plotCI = TRUE, covs = data.frame(hour=12))
```

Interestingly, this model suggests step lengths and directional persistence for the "encamped" state decreased as temperature increased, step lengths for both states tended to decrease in the late evening and early morning, and transition probabilities from the "encamped" to "exploratory" state decreased as temperature increased (Figure 2).

Model fit can be assessed using the pseudo-residuals, with the functions pseudoRes and plotPR. The residual ACF plot shown in Figure 1 was produced by:

```
> # compute pseudo-residuals for the steps and the angles
> pr <- pseudoRes(m3)
> # plot the ACF of step pseudo-residuals
> acf(pr$stepRes[!is.na(pr$stepRes)],lag.max = 300)
```

Autocorrelation function plots of the pseudo-residuals indicate this model explained much of the periodicity in step length, although there does still appear to be some room for improvement.

3.2 Northern fur seal

In our second example, we use the northern fur seal (Callorhinus ursinus) example from McClintock et al. (2014) to demonstrate the use of additional data streams for distinguishing behaviors with similar horizontal trajectories in a multivariate HMM. The data consist of 241 temporally-irregular Fastloc GPS locations obtained during a foraging trip of a nursing female near the Pribilof Islands of Alaska, USA, from 10-17 October 2007. The tag included time-depth recording capabilities, and the dive activity data were summarized as the number of foraging dives over T = 228 temporally-regular 1 hr time

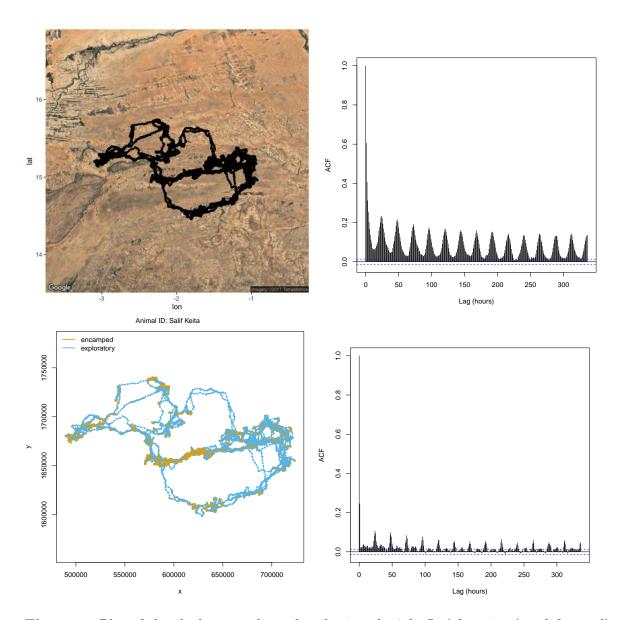


Figure 1. Plot of the elephant track produced using the 'plotSat' function (top-left panel), autocorrelation function (ACF) plot of the corresponding step length data (top-right panel), plot of the Viterbi-decoded state sequence for the 2-state ("encamped" and "exploratory") model generated using the generic 'plot' function (bottom-left panel), and the step length pseudo-residual ACF plot for this model using the 'plotPR' function (bottom-right panel).

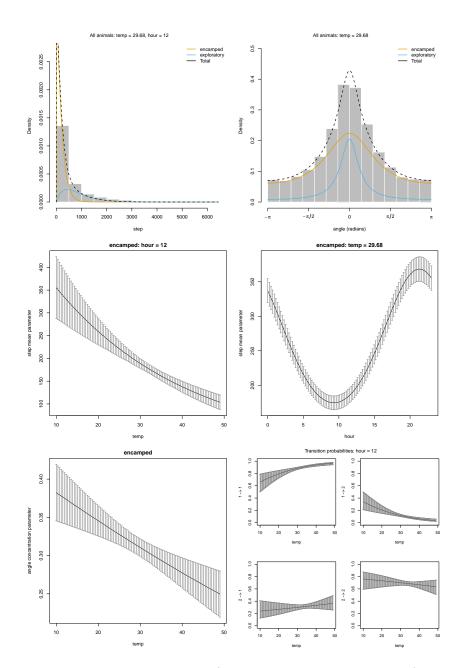


Figure 2. Selected plots for the 2-state ("encamped" and "exploratory") African elephant example generated using the generic 'plot' function. Top panels present histograms of the step length (top-left) and turning angle (top-right) data along with the estimated state-dependent probability distributions based on the mean temperature (temp = 29.7 degrees celsius) at 12:00 GMT (hour = 12). Middle panels present estimates (and 95% confidence intervals) for the step length mean parameter of the "encamped" state as a function of temperature and hour of day. Bottom-left panel presents estimates for the turning angle concentration parameter of the "encamped" state as a function of temperature. Bottom-right panel presents estimated state transition probabilities (1 = "encampled", 2 = "exploratory") as a function of temperature at 12:00 GMT.

steps. To fit the Z=3 state (1="resting", 2="foraging", 3="transit") of McClintock et al. (2014) using momentuHMM, we first used crawlWrap to predict temporally-regular locations at 1 hr time steps assuming a bivariate normal measurement error model and merged the results with the foraging dive data using the crawlMerge function. Then multiple imputation was used to account for location measurement error by repeatedly fitting the HMM to nSims realizations of the position process using MIfitHMM:

Here we specified a gamma distribution for step length ('step'), wrapped Cauchy distribution for turning angle ('angle'), and Poisson distribution for the number of foraging dives ('dive'). The function getParDM was used to organize the starting values for the data stream working parameters (Par0) in the correct format based on DM, cons, and estimates of the natural parameters (Par) from McClintock et al. (2014). The DM and cons arguments were specified to avoid label switching among the nSims imputed data model fits and enforce similar state-dependent probability distribution constraints as McClintock et al. (2014), e.g., constraining the Poisson rate parameters such that the "foraging" state tends to have higher numbers of foraging dives than the "transit" state ($\lambda_2 > \lambda_3$). To prohibit foraging dives for the "resting" state, we used the fixPar argument to effectively fix the Poisson rate parameter to zero on the natural scale (i.e. $\lambda_1 \approx 0$). To help deal with the problem of convergence to local maxima, the retryFits argument allows users to specify the number of times to attempt to re-fit each model using random perturbations of the parameter estimates as the starting values for optimization.

The results are very similar to those of the discrete-time model of McClintock *et al.* (2014), with periods of foraging often followed by resting (Figure 3). The "activity

budgets" (i.e. the proportion of time steps allocated to each state) calculated by MIpool based on the estimated state sequences for each imputation were 0.3 (95% CI: 0.22-0.39) for "resting", 0.29 (95% CI: 0.22-0.36) for "foraging", and 0.41 (95% CI: 0.32-0.52) for "transit".

3.3 Loggerhead turtle

For our third example, we demonstrate how to model movement direction and step length as a function of angular covariates using hitherto unpublished loggerhead turtle (Caretta caretta) data for a captive-raised juvenile released in 2012 on the coast of North Carolina, USA. The data consist of 165 temporally-irregular Argos locations subject to measurement error and rasters of daily ocean surface currents collected between 20 November and 19 December 2012. Assuming a gamma distribution for step length (l_t) and a wrapped Cauchy distribution for turning angle (ϕ_t) , we model the mean step length parameter (μ_t^l) as a function of ocean surface current speed (w_t) and direction (r_t) relative to the bearing of movement (b_t) :

$$\mu_t^l = \exp(\beta_0^l + \beta_1^l w_t \cos(b_t - r_t)), \tag{4}$$

and the turning angle mean parameter (μ_t^{ϕ}) as a trade-off between short-term directional persistence and bias in the direction of ocean surface currents using the circular-circular regression link function:

$$\mu_t^{\phi} = \operatorname{atan2}(\sin(d_t)\beta^{\phi}, 1 + \cos(d_t)\beta^{\phi}), \tag{5}$$

where $d_t = \text{atan2}(\sin(r_t - b_{t-1}), \cos(r_t - b_{t-1})).$

We wish to fit a 2-state HMM to the turtle data, with a "foraging" state unaffected by currents and a "transit" state potentially influenced by ocean surface currents as in Eqs. 4 and 5. We used crawlWrap to predict T=350 temporally-regular locations at 2 hr time steps assuming a bivariate normal measurement error model that accounts for the Argos location quality class (i.e. 3,2,1,0,A,B) of each observation. We then again used multiple imputation to account for location uncertainty by repeatedly fitting the HMM to nSims realizations of the position process using MIfithm. We first draw nSims realizations of the position process and extract the corresponding spatial covariates from the raster bricks for ocean surface current speed ("speedBrick") and direction

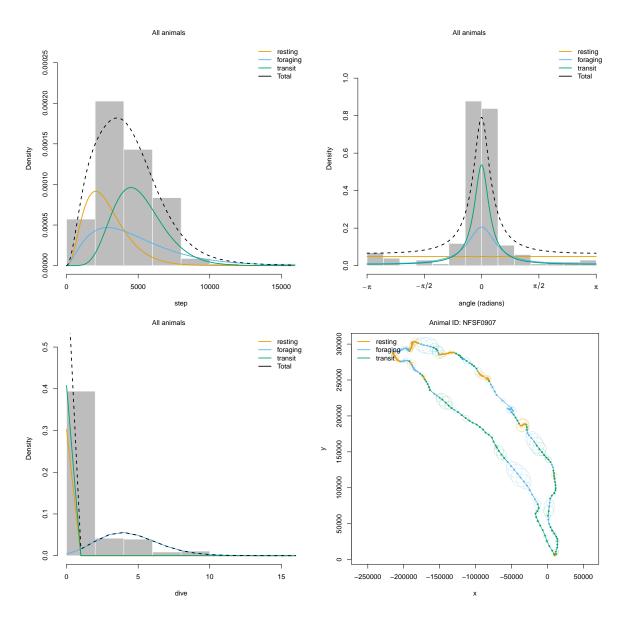


Figure 3. Plots of the northern fur seal example results generated using the generic 'plot' function. The estimated probability distributions for step length (top-left panel), turning angle (top-right panel), and number of foraging dives (bottom-left panel) for the 3-state ("resting", "foraging", and "transit") model are plotted along with histograms of these data streams. The temporally-regular predicted locations (and 95% ellipsoidal confidence bands) and estimated states are plotted in the bottom-right panel. All estimates are pooled across multiple imputations of the position process and thus reflect uncertainty attributable to location measurement error and temporally-irregular observations.

("dirBrick") using MIfitHMM with fit=FALSE:

When the fit argument is FALSE, MIfitHMM returns a list of length nSims composed of momentuHMMData objects (miData). For convenience and ease of interpretation, we manually added an additional covariate ($angle_osc = cos(b_t - r_t)$) to each of the imputed data sets and fitted the 2-state HMM using Eqs. 4 and 5 for state 2 ("transit"):

Note that the state2 special function in DM indicates the covariate formulas are specific to state 2 ("transit") and the circularAngleMean argument indicates that circular-circular regression link function is to be used on the mean turning angle parameter as in Eq. 5.

For the "transit" state, pooled parameter estimates indicated step lengths increased with ocean surface current speed and as the bearing of movement aligned with ocean surface current direction ($\beta_1^l = 0.43,95\%$ CI: 0.1-0.77; Figure 4). The estimated wrapped Cauchy distribution for turning angle had mean angles (μ_t^{ϕ}) biased towards the direction of ocean surface currents for each time step ($\beta^{\phi} = 0.24,95\%$ CI: -0.01-0.5), with concentration parameter $\rho_2^{\phi} = 0.85$ (95% CI: 0.77-0.92) indicating turning angles were concentrated at μ_t^{ϕ} . Thus movement during the "transit" state appears to strongly follow ocean surface currents (mean $angle_osc = 0.87, SD = 0.23$), while movement during the "foraging" state exhibited shorter step lengths ($\mu_1^l = 2996$ m, 95% CI: 1791 – 4202) perpendicular to ocean surface currents (mean $angle_osc = 0.07, SD = 0.26$), with no directional persistence ($\rho_1^{\phi} = 0.03$). The turtle spent 0.53 (95% CI: 0.34–0.71) of the 2 hr time steps in the "foraging" state and 0.47 (95% CI: 0.29–0.66) of time steps in the "transit" state as it travelled northeast along a predominant current until it (presumably) found an attractive foraging patch (Figure 4).

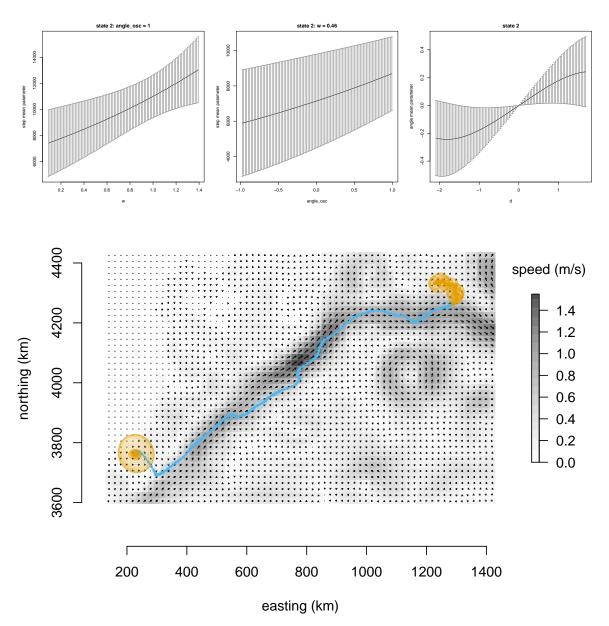


Figure 4. Selected results from the loggerhead turtle example. Top panels include estimates and 95% confidence intervals for the mean step length parameter as a function of ocean surface current speed (w) when ocean surface current direction (r_t) is the same as the bearing (b_t) of movement (i.e. $angle_osc = cos(b_t - r_t) = 1$; top-left panel), mean step length parameter as a function of $angle_osc$ at the mean ocean surface current speed (w = 0.46 m/s; top-middle panel), and mean turning angle parameter as a function of $d_t = atan2(\sin(r_t - b_{t-1}), \cos(r_t - b_{t-1}))$ (top-right panel). Bottom panel plots the pooled track, 95% error ellipse confidence bands, and state (orange = "foraging", blue = "transit") estimates based on multiple imputations of the position process relative to ocean surface current speed (m/s) and direction on 2 December 2012.

3.4 Grey seal

For our next example, we perform a similar analysis of a grey seal (Halichoerus grypus) track that was originally conducted by McClintock et al. (2012) using Bayesian methods and (computationally-intensive) Markov chain Monte Carlo. The data consist of 1045 temporally-irregular Fastloc GPS locations collected in the North Sea between 9 April and 11 August 2008. Because the seal repeatedly visited the same haulout and foraging locations, it provides a nice example for demonstrating how to implement biased movements relative to activity centers using momentuHMM. McClintock et al. (2012) fitted a 5-state model to these data that included three center of attraction states, with movement biased towards two haulout sites ("Abertay" and "Farne Islands") and a foraging area ("Dogger Bank"), and two "exploratory" states ("low speed", "high speed") that were unassociated with an activity center. After using crawlWrap to predict T=1515temporally-regular locations at 2 hr time steps including a bivariate normal measurement error model, we can perform a very similar analysis to McClintock et al. (2012) in momentuHMM by using the centers argument and state-specific functions for the probability distribution parameters. A cluster analysis on the observed locations using the R package dtwclust (Sarda-Espinosa 2017) identified three centroids with coordinates that were nearly identical to the three activity centers ("Abertay", "Farne Islands", and "Dogger Bank") identified by McClintock et al. (2012). We use these coordinates to derive covariates relative to the activity centers when drawing nSims realizations of the position process:

```
> crwSim <- MIfitHMM(crwOut, nSims = 100, fit=FALSE,
+ center = centers)</pre>
```

Specifying the **centers** argument results in the calculation of two covariates for each activity center: the distance (with '.dist' suffix) and angle (with '.angle' suffix) from each location at time t. These covariates can then be used to model parameters as a function of the distance and angle to activity centers for each time step:

```
> angleDM <- list(mean = angleFormula, concentration = distFormula)
> DM <- list(step = stepDM, angle = angleDM)</pre>
```

Similar to McClintock $et\ al.\ (2012)$, we assume a Weibull distribution for step length where both the shape and scale parameter depend on the distance from the location at time t to each activity center. For the activity centers on land ("Abertay" and "Farne"), we allow the (state-dependent) step length parameters to change when the seal is beyond 2500m of the haulout. For the "Dogger" activity center, we allow the parameters to change when the seal is beyond 15000m of this (presumably) foraging area. We thus allow the movement behavior to change within these activity center states upon entering or leaving the viscinity of these sites. We assume a wrapped Cauchy distribution for turning angle with (state-dependent) mean angle derived from the direction to each activity center at time t, and the concentration parameter is modeled similarly to the step length parameters. For the two "exploratory" states, we assumed they are simple random walks unaffected by proximity to activity centers. To complete our model specification, we use the knownStates argument to assign the seal to the corresponding activity center state whenever it was within the 2500m (haulout area) or 15000m (foraging area) thresholds for each imputed data set:

As with the step length and turning angle concentration parameters, the state transition probabilities are also allowed to change as a function of distance to activity centers (as specified by the formula argument). The starting values (ParO and betaO) for each imputation were extracted from a single HMM fitted to the best predicted locations from crawlWrap, and fixPar was used to remove short-term directional persistence (and thus formulate the model as a mixture of biased and simple random walks).

Estimated activity budgets for the 5 states of this multiple imputation HMM were 0.28 (0.27 - 0.3) for the "Abertay" haul-out state, 0.12 (0.11 - 0.14) for the "Farne Islands" haul-out state, 0.37 (0.35 - 0.38) for the "Dogger Bank" foraging state, 0.09

(0.03-0.2) for a low-speed "exploratory" state, and 0.14 (0.08-0.23) for a high-speed "exploratory" state. All three activity center states exhibited shorter step lengths and less biased movements when within the viscinity of these targets (Figure 5). Results from this analysis were thus very similar to those of McClintock *et al.* (2012), but this implementation required far less computation time and no custom model-fitting algorithms.

The simData function can be used to simulate tracks from a fitted model:

```
> greySealSim<-simData(model = greySealFits, centers = centers,
+ initialPosition = centers[1,],
+ obsPerAnimal = 1515)</pre>
```

A simulated track is presented along with the fitted track in Figure 6. While potentially useful for study design, power analysis, and prediction, the simData function can also be helpful in assessing goodness of fit by repeatedly drawing simulated data sets from a fitted model and comparing them to observed properties of the data (e.g. Morales et al. 2004).

3.5 Southern elephant seal

Here, we analyse the southern elephant seal (*Mirounga leonina*) data from Michelot et al. (2017) using momentuHMM. The data set consists of 15 tracks, each encompassing (at most) one foraging trip, starting from Kerguelen Island. We want to fit the model described by Michelot et al. (2017), with the four following states:

- 1. outbound trip from the colony to the ice;
- 2. searching;
- 3. foraging;
- 4. inbound trip from the ice to the colony.

The data set has three columns: "ID" (track ID), "x" (longitude), and "y" (latitude):

> head(tracks)

```
ID x y
1 1 70.60946 -49.60737
2 1 70.82908 -50.08287
```

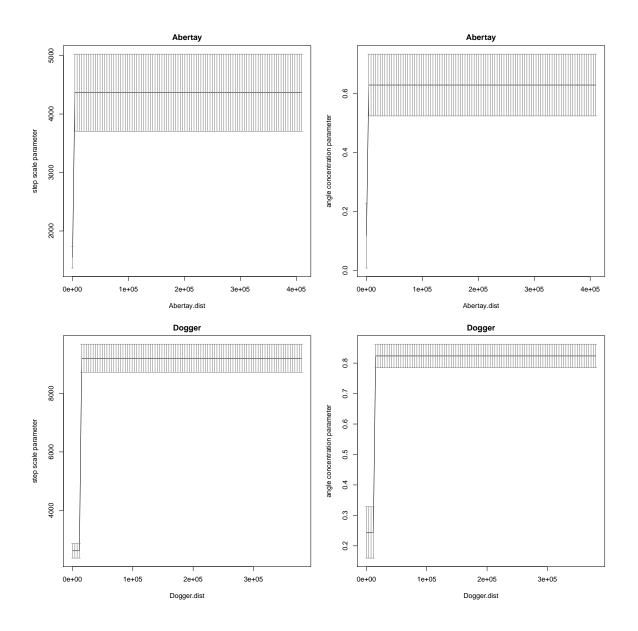
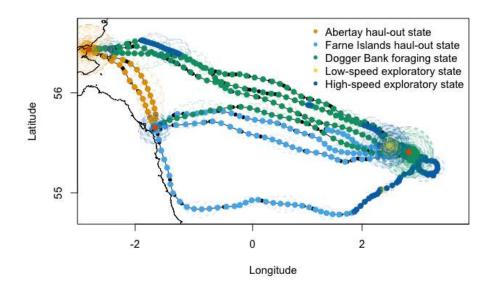


Figure 5. Selected results from the grey seal example. Panels include estimates and 95% confidence intervals for the "Abertay" haul-out state step length scale parameter as a function of distance in meters ('Abertay.dist'; top-left panel), "Abertay" haul-out state turning angle concentration parameter as a function of distance (top-right panel), "Dogger Bank" foraging state step length scale parameter as a function of distance ('Dogger.dist'; bottom-left panel), and the "Dogger Bank" foraging state turning angle concentration parameter as a function of distance (bottom-right panel).



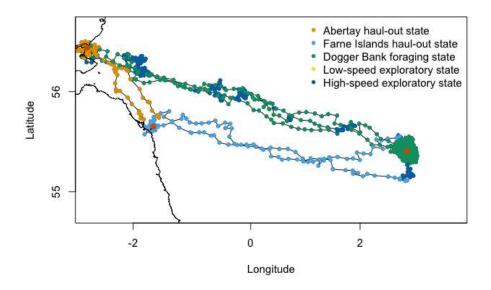


Figure 6. Fitted and simulated tracks from the grey seal example. This seal tended to move in a clockwise fashion between two haul-out locations ("Abertay" and "Farne Islands") and a foraging area ("Dogger Bank") in the North Sea. Top panel plots the pooled track, 95% error ellipse confidence bands, and state estimates based on the 5-state HMM fitted to multiple imputations of the position process. Red points indicate the locations of the three activity centers. Black points indicate the (temporally-irregular) observed locations. Bottom panel presents the locations and states for a track simulated from the fitted model using the 'simData' function.

```
3 1 70.90029 -50.32835
4 1 70.85766 -50.54746
5 1 70.63792 -50.90529
6 1 70.48480 -50.99666
```

From the locations, we use prepData to derive the step lengths and turning angles, as well as the distance and bearing (relative to previous movement direction as in Eq. 3) to the Kerguelen Island colony (with coordinates 70° longitude and -49° latitude):

```
> center <- matrix(c(70,-49),nrow=1,dimnames=list("colony"))
> data <- prepData(data=tracks, type="LL", centers=center)</pre>
```

Note that distances are in kilometers and angles are based on initial bearings (using geosphere::bearing; Hijmans 2016a) when calculated from longitude and latitude coordinates.

3.5.1 Model 1: no covariates

We start by fitting a covariate-free 4-state correlated random walk model, which we will use to extract starting parameter values for more complex models. We use the argument fixPar to fix some transition probabilities to zero, following Michelot $et\ al.$ (2017). We set to NA the columns of unconstrained transition probabilities, and we fix the intercept of the other columns to a large negative number (here -100) to set the corresponding transition probabilities to be virtually zero (i.e. impossible transition). As in Michelot $et\ al.$ (2017), we set transition probabilities from outbound to forage, outbound to inbound, search to outbound, forage to outbound, forage to inbound, inbound to outbound, inbound to search, and inbound to forage to be effectively zero.

3.5.2 Model 2

This model mimics the formulation of Michelot *et al.* (2017). We model the effect of the distance to colony on the transition probability from outbound to search, and of the time since departure on the transition probability from search to inbound.

As before, we constrain the transition probability matrix to prevent some of the transitions (e.g. from forage to inbound, etc.). We define a 3×12 matrix for the beta parameters, in which each column corresponds to a transition $(1 \to 2, 1 \to 3, 1 \to 4, 2 \to 1, \ldots)$, and each row corresponds to a covariate (intercept, distance to center, time since departure). We set to NA the columns of unconstrained transition probabilities, and we again fix the intercept of the other columns to a large negative number (here -100) to set the corresponding transition probabilities to be virtually zero (i.e. impossible transition).

```
> fixbeta <- matrix(c(NA,-100,-100,-100,NA,NA,-100,NA,-100,-100,-100,-100,
                       NA,
                                  0,
                                       0, 0, 0,
                                                   0, 0,
                             0,
                                       O, O, NA,
                                                   0, 0,
+
                        0,
                             0,
                                  0,
                                                           0,
                                                                 0,
                                                                      0,
                                                                           0),
                    nrow=3, byrow=TRUE)
```

Biased random walks are used to model the movement in states 1 and 4, with repulsion away from the colony in the outbound trip, and attraction towards the colony in the inbound trip. For that purpose, we include 'colony.angle' as a covariate on the angle mean of the von Mises distributions for turning angles in states 1 and 4.

```
> angleFormula <- ~ state1(colony.angle) + state4(colony.angle)</pre>
```

To specify the direction of the bias (away from or towards the colony), we fix the parameters linking the mean turning angle to the direction of the colony. In state 1, we

fix the coefficient to a large negative number (e.g. -100) so that the mean direction is away from the colony. In state 4, we fix it to a large positive number (e.g. 100) so that the mean direction is towards the colony. Fixing these parameters to large positive (or negative) values effectively removes the correlated random walk component of Eq. 2 for states 1 and 4. The four other parameters correspond to the angle concentrations and should be estimated (NAs in fixPar).

```
> fixPar <- list(angle=c(-100,100,NA,NA,NA,NA),beta=fixbeta)</pre>
```

Because no covariates are specified for the mean angle of state 2 (searching) and state 3 (foraging), these states are reduced to correlated random walks with a mean turning angle of zero (i.e. atan2(0,1) = 0 as in Eq. 2).

We can now fit the second model with starting parameter values extracted from the simpler model using getParO. In fitHMM, we use the arguments estAngleMean and circularAngleMean to indicate that the angle mean is to be estimated using circular-circular regression.

Instead of relying entirely on fixPar for parameter constraints, an equivalent model for the transition probabilities could be specified using the special function betaCol in formula:

Here betaCol1(colony.dist) specifies an effect of distance to colony only on the transition from state 1 to state 2 (which corresponds to the first column of the beta

matrix) and betaCol6(time) specifies an effect of time since departure only on the transition from state 2 to state 4 (which corresponds to the sixth column of the beta matrix). When the special function betaCol is used, then fitHMM automatically fixes the appropriate elements in the second ('colony.dist') and third ('time') rows of the beta matrix to zero (without the user needing to do so manually using fixPar). However, note that the first row (corresponding to the intercept terms) must still be manually fixed to achieve the desired constraints on the transition probability matrix.

3.5.3 Model 3

In addition to the covariates included in model 2, we add the effect of distance to colony on the step length and turning angle concentration parameters for states 1 and 4. We specify the following formulas:

```
> distFormula <- ~ state1(colony.dist) + state4(colony.dist)
> stepDM <- list(mean=distFormula, sd=distFormula)
> angleDM <- list(mean=angleFormula, concentration=distFormula)</pre>
```

The initial parameters are extracted from model 2, again using the function getPar0. Instead of fixing the mean direction of movement like in model 2, we estimate it here as a trade-off between short-term directional persistence and bias toward (or away) from the colony (i.e. a biased correlated random walk as in Eq. 2).

```
> # remove fixed angle parameters
> fixPar <- list(beta=fixbeta)</pre>
> # get starting parameters from m2
> Par0 <- getPar0(model=m2, nbStates=4,
                  DM = list(step=stepDM, angle=angleDM),
                   estAngleMean=list(angle=TRUE),
                   circularAngleMean=list(angle=TRUE),
                   formula=formula)
> # the bias is estimated rather than fixed
> Par0$Par$angle[c("mean_1:colony.angle", "mean_4:colony.angle")] <- 0</pre>
> m3 <- fitHMM(data=data, nbStates=4, dist=list(step="gamma",angle="vm"),</pre>
               Par0=list(step=Par0$Par$step, angle=Par0$Par$angle),
               beta0=Par0$beta, fixPar=fixPar, formula=formula,
               DM = list(step=stepDM, angle=angleDM),
               estAngleMean=list(angle=TRUE),
               circularAngleMean=list(angle=TRUE),
               stateNames = stateNames)
```

The three fitted model can be compared with AIC(m1,m2,m3), which overwhelmingly supports model 3. The most likely state sequence is obtained with viterbi(m3). Figure 7 shows a map of the state-decoded track. The estimated circular-circular regression coefficients for the angle means of state 1 (outbound) and state 4 (inbound) were -0.66 (95% CI: -0.82-0.5) and 0.4 (95% CI: 0.32-0.49), respectively, thus indicating biased correlated random walks with repulsion away from the colony during outbound movements and attraction towards the colony during inbound movements. The estimated regressoin coefficients for the step length mean and turning angle concentration parameters for states 1 and 4 suggest that step lengths decreased and turning angles became more concentrated at the mean angle as distance to colony increased (Figure 8)

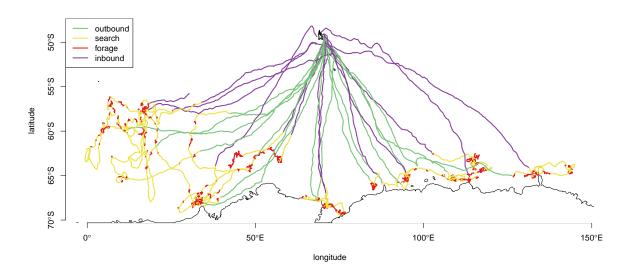


Figure 7. The 15 elephant seal tracks, colored by the most likely state sequence.

4 Discussion

Here we have introduced version 1.0.1 of the R package momentuHMM and demonstrated some of its capabilities for conducting multivariate HMM analyses with animal location, auxiliary biotelemetry, and environmental data. The package allows for fitting (and simulating from) a suite of biased and correlated random walk movement process models (e.g. McClintock *et al.* 2012), can be used for an unlimited number of data streams and

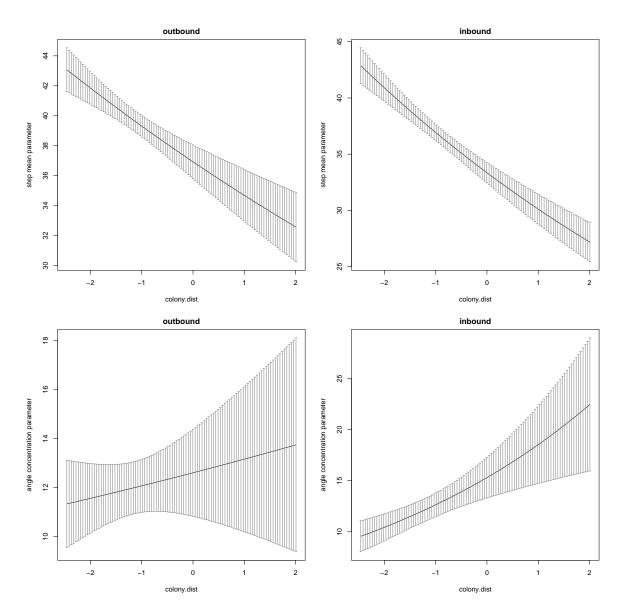


Figure 8. Selected results from the elephant seal example. Panels include estimates and 95% confidence intervals for the "outbound" mean step length parameter (top-left panel), "inbound" mean step length parameter (top-right panel), "outbound" turning angle concentration parameter (bottom-left panel), and "inbound" turning angle concentration parameter (bottom-right panel) as a function of distance to colony ('colony.dist'). Distance to colony has been standardized based on a mean of 2539 km (SD = 1021.3).

latent behavior states, includes multiple imputation methods to account for measurement error, temporal irregularity, and other forms of missing data that would otherwise be prohibitive to maximum likelihood analysis, and integrates seamlessly with rasters to facilitate spatio-temporal covariate modelling. Because the package incorporates biased random walks, it can also be used to implement group dynamic models (e.g. Langrock et al. 2014). The package therefore greatly expands on available software and facilitates the incoporation of more ecological and behavioral realism for hypothesis-driven analyses of animal movement that account for many of the challenges commonly associated with telemetry data. While many of the features of momentuHMM were motivated by animal movement data, we note that the package is not limited to location data and can be used for analyzing any type of data that is amenable to (multivariate) HMMs.

Model fitting in momentuHMM is relatively fast because the forward algorithm (Eq. 1) is coded in C++. Because multiple imputations are completely parallelizable, with sufficient processing power computation times for analyses that account for measurement error, temporal irregularity, or other forms of missing data need not be longer than that required to fit a single HMM. However, computation times will necessarily be slower as the number of states and/or parameters increase. For example, momentuHMM required about 1 hr to fit a single HMM with N=6 states, seven data streams, and T=7414 time steps (McClintock 2017).

As in any maximum likelihood analysis based on numerical optimization, computation times will also depend on the starting values (ParO and betaO). Specifying "good" starting values is arguably the most challenging aspect of model fitting in momentuHMM, particularly for the working scale coefficients when using covariates. The getPar, getParO, and getParDM functions are designed to help with the specification of starting values, and the retryFits argument in crawlWrap, fitHMM, and MIfitHMM will re-optimize based on random perturbations of the parameters to help explore the likelihood surface and diagnose convergence to local maxima. Optimization for the circular-linear regression link function (tan(mean/2); see Table 2) in particular can be prone to local minima, so users are encouraged to explore a range of starting values when fitting these models.

While momentuHMM includes functions for drawing realizations of the position process based on the CTCRW model of Johnson *et al.* (2008), this is but one of many methods for performing the first stage of multiple imputation. Realizations of the po-

sition process from any movement model that accounts for measurement error and/or temporal irregularity (e.g. Calabrese et al. 2016; Gurarie et al. 2017) could be passed to MIfitHMM for HMM-type analyses in the second stage. Multiple imputation methods also need not be limited to these telemetry error scenarios. For example, conventional missing data could also be imputed using standard techniques (Rubin & Schenker 1986), thereby allowing the investigation of non-random mechanisms for missingness that can be problematic if left unaccounted for in HMMs.

There remain many potential avenues for refining and extending the capabilities of momentuHMM. Computation times could likely be improved by further optimizing the R and C++ code for speed. Notable extensions include hidden semi-Markov models and random effects on data stream probability distribution and state transition probability parameters (Zucchini et al. 2016). We would also like to incorporate additional parameters for change-point thresholds and the locations of activity centers instead of requiring that they be pre-specified (and potentially compared using AIC or other model selection criteria) as in grey seal example. Lastly, it is relatively straightforward to add additional probability distributions, and we are pleased to do so upon request. Practitioners interested in additional features for momentuHMM are encouraged to contact the authors.

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