The optimsimplex Package

Sébastien Bihorel

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optimsimplex is a R port of a module originally developed for Scilab version 5.2.1 by Michael Baudin (INRIA - DIGITEO). Information about this software can be found at www.scilab.org. The following documentation as well as the content of the functions .Rd files are adaptations of the documentation provided with the original Scilab optimsimplex module.

1 Overview

1.1 Description

The goal of this package is to provide a building block for optimization algorithms based on a simplex. The **optimisimplex** package may be used in the following optimization methods:

- the simplex method Spendley et al.,
- the method of Nelder and Mead,
- the Box's algorithm for constrained optimization,
- the multi-dimensional search by Torczon,
- etc ...

This set of commands allows to manage a simplex made of $k \ge n+1$ points in a n-dimensional space. This component is the building block for a class of direct search optimization methods such as the Nelder-Mead algorithm or Torczon's Multi-Dimensionnal Search.

A simplex is designed as a collection of $k \ge n+1$ vertices. Each vertex is made of a point and a function value at that point.

The simplex can be created with various shapes. It can be configured and quieried at will. The simplex can also be reflected or shrinked. The simplex gradient can be computed with a order 1 forward formula and with a order 2 centered formula.

The optimsimplex.new function allows to create a simplex. If vertices coordinates are given, there are registered in the simplex. If a function is provided, it is evaluated at each vertex. Several functions allow to create a simplex with special shapes and methods, including axes-by-axes (optimsimplex.axes), regular (optimsimplex.spendley), randomized bounds simplex with arbitrary nbve vertices (optimsimplex.randbounds) and an heuristical small variation around a given point (optimsimplex.pfeffer).

In the functions provided in this package, simplices and vertices are, depending on the functions either input or output arguments. The following general principle have been used to manage the storing of the coordinates of the points.

- The vertices are stored row by row, while the coordinates are stored column by column. This implies the following rules.
- The coordinates of a vertex are stored in a row vector, i.e. a $1 \times n$ matrix where n is the dimension of the space.
- The function values are stored in a column vector, i.e. a *nbve* x 1 matrix where *nbve* is the number of vertices.

1.2 Computation of function value at the given vertices

Most functions in the **optimsimplex** package accept a **fun** argument, which corresponds to the function to be evaluated at the given vertices. The function is expected to have the following input and output arguments:

```
myfunction <- function(x, this){
    ...
    return(list(f=f,this=this))
}</pre>
```

where x is a row vector, f is the function value, and this an optional user-defined data passed to the function. If data is provided, it is passed to the callback function both as an input and output argument. data may be used if the function uses some additionnal parameters. It is returned as an output parameter because the function may modify the data while computing the function value. This feature may be used, for example, to count the number of times that the function has been called.

2 Examples

2.1 Creating a simplex given vertex coordinates

In the following example, one creates a simplex with known vertices coordinates and queries the new object. The function values at the vertices are unset.

```
> coords \leftarrow matrix(c(0, 1, 0, 0, 0, 1), ncol = 2)
> tmp <- optimsimplex.new(coords = coords)</pre>
> s1 <- tmp$newobj
> s1
$verbose
[1] 0
$x
      [,1] [,2]
[1,]
         0
               0
[2,]
         1
               0
[3,]
         0
               1
$n
[1] 2
```

```
$fv
     [,1]
$nbve
[1] 3
attr(,"type")
[1] "T_SIMPLEX"
> optimsimplex.getallx(s1)
     [,1] [,2]
[1,]
              0
        0
[2,]
        1
              0
[3,]
        0
              1
> optimsimplex.getn(s1)
[1] 2
> optimsimplex.getnbve(s1)
[1] 3
```

2.2 Creating a simplex with randomized bounds

In the following example, one creates a simplex with in the 2D domain c(-5, 5)^2, with c(-1.2, 1.0) as the first vertex. One uses the randomized bounds method to generate a simplex with 5 vertices. The function takes an additionnal argument this, which counts the number of times the function is called. After the creation of the simplex, the value of this\$nb is 5, which is the expected result because there is one function call by vertex.

```
> rosenbrock <- function(x) {
+          y <- 100 * (x[2] - x[1]^2)^2 + (1 - x[1])^2
+ }
> mycostf <- function(x, this) {
+          y <- rosenbrock(x)
+          this$nb <- this$nb + 1
+          return(list(f = y, this = this))
+ }
> mystuff <- list(nb = 0)
> tmp <- optimsimplex.randbounds(x0 = c(-1.2, 1), fun = mycostf,
+          boundsmin = c(-5, -5), boundsmax = c(5, 5), nbve = 5,
+          data = mystuff)
> tmp$newobj

$verbose
[1] 0
```

```
$x
           [,1]
                       [,2]
[1,] -1.2000000
                 1.0000000
[2,] -0.1385933
                 4.2248806
[3,] -0.9727057
                 4.7231851
[4,] 4.0621714
                 0.4300012
[5,] 0.3623036 -4.9178620
$n
[1] 2
$fv
          [,1]
        24.200
[1,]
[2,]
      1770.064
[3,]
     1430.486
[4,] 25837.836
[5,]
      2549.774
$nbve
[1] 5
attr(,"type")
[1] "T_SIMPLEX"
> tmp$data
$nb
[1] 5
> cat(sprintf("Function evaluations: %d\n", tmp$data$nb))
Function evaluations: 5
```

3 Initial simplex strategies

In this section, we analyse the various initial simplex which are provided in this component.

It is known that direct search methods based on simplex designs are very sensitive to the initial simplex. This is why the current component provides various ways to create such an initial simplex.

The first historical simplex-based algorithm is the one presented in "Sequential Application of Simplex Designs in Optimisation and Evolutionary Operation" by W. Spendley, G. R. Hext and F. R. Himsworth. The "spendley" simplex creates the regular simplex which is presented in the paper [9].

The "randbounds" simplex is due to M.J. Box in "A New Method of Constrained Optimization and a Comparison With Other Methods" [7].

Pfeffer's method is an heuristic which is presented in "Global Optimization Of Lennard-Jones Atomic Clusters" by E. Fan [4]. It is due to L. Pfeffer at Stanford and it is used in the fminsearch function from the **neldermead** package.

4 References

The functions distributed in **optimsimplex** are also based upon the following bibliography: [5], [3], [6], [8], [1], and [2].

- [1] A. Burmen and J. Puhan and T. Tuma. Grid Restrained Nelder-Mead Algorithm. *Computational Optimization and Applications*, 34(3):359–375, July 2006.
- [2] C.J. Price and I.D. Coope and D. Byatt. A Convergent Variant of The Nelder-Mead algorithm. Journal of Optimization Theory and Applications, 113(1):5–19, April 2002.
- [3] C.T. Kelley. Iterative Methods for Optimization. SIAM Frontiers in Applied Mathematics, Philadelphia, PA, 1999.
- [4] E. Fan. Global Optimization Of Lennard-Jones Atomic Clusters. Master's thesis, McMaster University, February 2002.
- [5] J.A. Nelder and R. Mead. A Simplex Method for Function Minimization. *The Computer Journal*, 7(4):308–313, 1965.
- [6] Lixing Han and Michael Neumann. Effect of Dimensionality on the Nelder-Mead Simplex Method. Optimization methods and software, 21(1):1–16, 2006.
- [7] M.J. Box. A New Method of Constrained Optimization and a Comparison With Other Methods. *The Computer Journal*, 1(8):42–52, 1965.
- [8] V.J. Torczon. Multi-Directional Search: A Direct Search Algorithm for Parallel Machines. PhD thesis, Rice University, Houston, TX, 1989.
- [9] W. Spendley and G.R. Hext and F.R. Himsworth. Sequential Application of Simplex Designs in Optimisation and Evolutionary Operation. *Technometrics*, 4:441–461, 1962.

5 Network of optimsimplex functions

The network of functions provided in **optimsimplex** is illustrated in the network map given in the **neldermead** package.

6 Help on optimsimplex functions

Description

The goal of this package is to provide a building block for optimization algorithms based on a simplex. The **optimisimplex** package may be used in the following optimization methods:

- the simplex method of Spendley et al.,
- the method of Nelder and Mead,
- the Box's algorithm for constrained optimization,
- the multi-dimensional search by Torczon,
- etc ...

Features The following is a list of features currently provided:

- Manage various simplex initializations
 - initial simplex given by user,
 - initial simplex computed with a length and along the coordinate axes,
 - initial regular simplex computed with Spendley et al. formula,
 - initial simplex computed by a small perturbation around the initial guess point,
 - initial simplex computed from randomized bounds.
- sort the vertices by increasing function values,
- compute the standard deviation of the function values in the simplex,
- compute the simplex gradient with forward or centered differences,
- shrink the simplex toward the best vertex,
- etc...

Details

Package: optimsimplex
Type: Package
Version: 1.0
Date: 2010-05-01
License: CeCILL-2
LazyLoad: yes

See vignette('optimsimplex',package='optimsimplex') for more information.

Author(s)

Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

Function evaluations $Computation \ of \ Function \ Value(s)$

Description

These functions compute the value of the function at the vertices points stored in the current simplex object and stored them back into the simplex object. optimsimplex.computefv determines how many vertices are stored in the simplex object and delegates the calculation of the function values to optimsimplex.compsomefv.

Usage

```
optimsimplex.computefv(this = NULL, fun = NULL, data = NULL)
optimsimplex.compsomefv(this = NULL, fun = NULL, indices = NULL, data = NULL)
```

Arguments

this

The current simplex object, containing the nbve x n matrix of vertice coordinates (i.e. x element), where n is the dimension of the space and nbve the number of vertices.

fun

The function to compute at vertices. The function is expected to have the following input and output arguments:

```
myfunction <- function(x, this){
...
return(list(f=f,this=this))
}</pre>
```

where x is a row vector and this a user-defined data, i.e. the data argument.

data

A user-defined data passed to the function. If data is provided, it is passed to the callback function both as an input and output argument. data may be used if the function uses some additionnal parameters. It is returned as an output parameter because the function may modify the data while computing the function value. This feature may be used, for example, to count the number of times that the function has been called.

indices

A vector of increasing integers from 1 to nove.

Value

optimsimplex.computefv and optimsimplex.compsomefv return a list with the following elements:

this The updated simplex object.

data The updated user-defined data.

Author(s)

```
Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)
```

See Also

```
optimsimplex.new
```

optimsimplex.destroy Erase Simplex Object

Description

This function erases the coordinates of the vertices (x) and the function values (fv) in a simplex object

Usage

```
optimsimplex.destroy(this = NULL)
```

Arguments

this

A simplex object.

Value

Return an updated simplex object for which the content of the x and fv elements were set to NULL.

Author(s)

```
Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)
```

See Also

```
optimsimplex.new
```

Description

```
The functions extract the content to various elements of a simplex object:

optimsimplex.getall Get all the coordinates and the function values of all the vertices.

optimsimplex.getallfv Get all the function values of all the vertices.

optimsimplex.getallx Get all the coordinates of all the vertices.

optimsimplex.getfv Get the function value at a given index.

optimsimplex.getn Get the dimension of the space of the simplex.

optimsimplex.getnbve Get the number of vertices of the simplex.

optimsimplex.getve Get the vertex at a given index in the current simplex.
```

optimsimplex.getx Get the coordinates of the vertex at a given index in the current simplex.

Usage

```
optimsimplex.getall(this = NULL)
optimsimplex.getallfv(this = NULL)
optimsimplex.getallx(this = NULL)
optimsimplex.getfv(this = NULL, ive = NULL)
optimsimplex.getn(this = NULL)
optimsimplex.getnbve(this = NULL)
optimsimplex.getve(this = NULL, ive = NULL)
optimsimplex.getx(this = NULL, ive = NULL)
```

Arguments

this A simplex object. ive Vertex index.

Value

optimsimplex.getall Return a nove x n+1 matrix, where n is the dimension of the space, nove is the number of vertices and with the following content:

- simplex[k,1] is the function value of the vertex k, with k = 1 to nove,
- simplex[k,2:(n+1)] is the coordinates of the vertex k, with k=1 to nove.

optimsimplex.getallfv Return a row vector of function values, which k $\hat{}$ th element is the function value for the vertex k, with k = 1 to nove.

optimsimplex.getallx Return a nove x n matrix of vertice coordinates; any given vertex is expected to be stored at row k, with k = 1 to nove.

```
optimsimplex.getfv Return a numeric scalar.
```

optimsimplex.getn Return a numeric scalar.

optimsimplex.getnbve Return a numeric scalar.

optimsimplex.getve Return a list with a 'type' attribute set to 'T_VERTEX' and with the following elements:

- **n** The dimension of the space of the simplex.
- x The coordinates of the vertex at index ive.
- fv The value of the function at index ive.

optimsimplex.getx Return a row vector, representing the coordinates of the vertex at index

Author(s)

```
Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)
```

See Also

```
optimsimplex.new
```

Simplex gradient

Simplex Gradient

Description

optimsimplex.gradientfv determines the simplex gradient of the function which is computed by the secondary functions optimsimplex.gradcenter and optimsimplex.gradforward.

Usage

```
optimsimplex.gradientfv(this = NULL, fun = NULL, method = "forward",
                        data = NULL)
optimsimplex.gradcenter(this = NULL, fun = NULL, data = NULL)
optimsimplex.gradforward(this = NULL)
```

Arguments

this An simplex object

The function to compute at vertices. The function is expected to have the fun

following input and output arguments:

```
myfunction <- function(x, this){}
return(list(f=f,this=this))
```

where x is a row vector and this a user-defined data, i.e. the data argument.

method

The method used to compute the simplex gradient. Two methods are available:

'forward' and 'centered'. The 'forward' method uses the current simplex to compute the gradient (using optimsimplex.dirmat and optimsimplex.deltafv). The 'centered' method creates an intermediate simplex and computes the average.

data

A user-defined data passed to the function. If data is provided, it is passed to the callback function both as an input and output argument. data may be used if the function uses some additionnal parameters. It is returned as an output parameter because the function may modify the data while computing the function value. This feature may be used, for example, to count the number of times that the function has been called.

Value

optimsimplex.gradientfv returns a list with the following elements:

 ${\bf g}$ A column vector of function gradient (with length ${\tt this\$n}).$

data The updated user-defined data.

optimsimplex.gradcenter returns a list with the following elements:

g A column vector of function gradient (with length this\$n).

data The updated user-defined data.

optimsimplex.gradforward returns a column vector of function gradient (with length this\$n).

Author(s)

 $\label{eq:author} \mbox{Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)}$

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

optimsimplex.new, optimsimplex.dirmat, optimsimplex.deltafv

optimsimplex.log

Optimsimplex Logging

Description

This function prints a message to screen (or log file).

Usage

```
optimsimplex.log(this = NULL, msg = NULL)
```

Arguments

this An simplex object.

msg A message to print.

Value

Do not return any value but print msg to screen if the verbose in this is set to 1.

Author(s)

```
Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)
```

See Also

```
optimsimplex.new
```

optimsimplex.new

Creates a Simplex Object

Description

optimsimplex.new creates a simplex list object which contains, among other elements, a matrix of vertices and a vector of function values calculated at those vertices. The object is actually created by a secondary function based upon the value of the method argument:

```
NULL -> optimsimplex.coords
'axes' -> optimsimplex.axes
'pfeffer' -> optimsimplex.pfeffer
'randbounds' -> optimsimplex.randbounds
'spendley' -> optimsimplex.spendley
'oriented' -> optimsimplex.oriented
```

Usage

Arguments

coords The matrix of point estimate coordinates in the simplex. The coords matrix

is expected to be a nbve x n matrix, where n is the dimension of the space and nbve is the number of vertices in the simplex, with nbve>= n+1. Only used

if method is set to NULL.

fun The function to compute at vertices. The function is expected to have the

following input and output arguments:

```
myfunction <- function(x, this){
...
return(list(f=f,this=this))
}</pre>
```

where x is a row vector and this a user-defined data, i.e. the data argument.

data A user-defined data passed to the function. If data is provided, it is passed

to the callback function both as an input and output argument. data may be used if the function uses some additionnal parameters. It is returned as an output parameter because the function may modify the data while computing the function value. This feature may be used, for example, to count the number

of times that the function has been called.

method The method used to create the new optimsimplex object, either 'axes', 'pfeffer',

'randbounds', 'spendley' or 'oriented'.

The initial point estimates, as a row vector of length n.

1en The dimension of the simplex. If length is a value, that unique length is used

in all directions. If length is a vector with n values, each length is used with the corresponding direction. Only used if method is set to 'axes' or 'spendley'.

deltausual The absolute delta for non-zero values. Only used if method is set to 'pfeffer'.

deltazero The absolute delta for zero values. Only used if method is set to 'pfeffer'.

boundsmin A vector of minimum bounds. Only used if method is set to 'randbounds'.

boundsmax A vector of maximum bounds. Only used if method is set to 'randbounds'.

nbve The total number of vertices in the simplex. Only used if method is set to

'randbounds'.

simplex0 The initial simplex. Only used if method is set to 'oriented'.

Details

All arguments of optimsimplex.new are optional. If no input is provided, the new simplex object is empty.

If method is NULL, the new simplex object is created by optimsimplex.coords. If coords is NULL, the simplex object is empty; otherwise, coords is used as the initial vertice coordinates in the new simplex.

If method is set to 'axes', the new simplex object is created by optimsimplex.axes. The initial vertice coordinates are stored in a nove x n matrix built as follows:

[1] | x0[1] x0[n] | len[1] ... 0

If method is set to 'pfeffer', the new simplex object is created by optimsimplex.pfeffer using the Pfeffer's method, i.e. a relative delta for non-zero values and an absolute delta for zero values

If method is set to 'randbounds', the new simplex object is created by optimsimplex.randbounds. The initial vertice coordinates are stored in a nbve x n matrix consisting of the initial point estimates (on the first row) and a (nbve-1) x n matrix of randomly sampled numbers between the specified the bounds. The number of vertices nbve in the simplex is arbitrary.

If method is set to 'spendley', the new simplex object is created by optimsimplex.spendley using the Spendely's method, i.e. a regular simplex made of nove = n+1 vertices.

If method is set to 'oriented', the new simplex object is created by optimsimplex.oriented in sorted order. The new simplex has the same sigma-length of the base simplex, but is "oriented" depending on the function value. The created simplex may be used, as Kelley suggests, for a restart of Nelder-Mead algorithm.

Value

Return a list with the following elements:

newobj A list with a 'type' attribute set to 'T_SIMPLEX' and with the following elements:

verbose The verbose option, controlling the amount of messages. Set to 0.

- \mathbf{x} The coordinates of the vertices, with size nove \mathbf{x} n.
- **n** The dimension of the space.

fv The values of the function at given vertices. It is a column matrix of length nove.

nbve The number of vertices.

data The updated data input argument.

Author(s)

Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References

"A Simplex Method for Function Minimization", Nelder, J. A. and Mead, R. The Computer Journal, January, 1965, 308-313

"Sequential Application of Simplex Designs in Optimisation and Evolutionary Operation", W. Spendley, G. R. Hext, F. R. Himsworth, Technometrics, Vol. 4, No. 4 (Nov., 1962), pp. 441-461, Section 3.1

"A New Method of Constrained Optimization and a Comparison With Other Methods", M. J. Box, The Computer Journal 1965 8(1):42-52, 1965 by British Computer Society

"Detection and Remediation of Stagnation in the Nelder-Mead Algorithm Using a Sufficient Decrease Condition", SIAM J. on Optimization, Kelley C.T., 1999

"Multi-Directional Search: A Direct Search Algorithm for Parallel Machines", by E. Boyd, Kenneth W. Kennedy, Richard A. Tapia, Virginia Joanne Torczon, Virginia Joanne Torczon, 1989, Phd Thesis, Rice University

"Grid Restrained Nelder-Mead Algorithm", Arpad Burmen, Janez Puhan, Tadej Tuma, Computational Optimization and Applications, Volume 34, Issue 3 (July 2006), Pages: 359 - 375

"A convergent variant of the Nelder-Mead algorithm", C. J. Price, I. D. Coope, D. Byatt, Journal of Optimization Theory and Applications, Volume 113, Issue 1 (April 2002), Pages: 5 - 19,

"Global Optimization Of Lennard-Jones Atomic Clusters", Ellen Fan, Thesis, February 26, 2002, McMaster University

Examples

optimsimplex-package R port of the Scilab optimsimplex module

Description

The goal of this package is to provide a building block for optimization algorithms based on a simplex. The **optimismplex** package may be used in the following optimization methods:

- $\bullet\,$ the simplex method of Spendley et al.,
- the method of Nelder and Mead,
- the Box's algorithm for constrained optimization,
- the multi-dimensional search by Torczon,
- etc ...

Features The following is a list of features currently provided:

- Manage various simplex initializations
 - initial simplex given by user,
 - initial simplex computed with a length and along the coordinate axes,
 - initial regular simplex computed with Spendley et al. formula,

- initial simplex computed by a small perturbation around the initial guess point,
- initial simplex computed from randomized bounds.
- sort the vertices by increasing function values,
- compute the standard deviation of the function values in the simplex,
- compute the simplex gradient with forward or centered differences,
- shrink the simplex toward the best vertex,
- etc...

Details

Package: optimsimplex Type: Package Version: 1.0

Date: 2010-05-01 License: CeCILL-2

LazyLoad: yes

See vignette('optimsimplex',package='optimsimplex') for more information.

Author(s)

Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

optimsimplex.print

Simplex Formatting and Display

Description

optimsimplex.tostring formats the coordinates and function values in a character vector. optimsimplex.print displays to screen the content of the current simplex with dimensions, coordinates and function values. This function calls optimsimplex.tostring to format the content of the simplex.

Usage

```
optimsimplex.print(this = NULL)
optimsimplex.tostring(this = NULL)
```

Arguments

this

A simplex object.

Value

optimsimplex.tostring returns a vector of character string of length nove, where nove is the number of vertices.

optimsimplex.print does not return any value but print to screen (or log file) the content of the current simplex.

Author(s)

```
Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)
```

See Also

```
optimsimplex.new
```

Examples

```
opt <- optimsimplex.new(method='axes',x0=1:5)$newobj
optimsimplex.tostring(opt)
optimsimplex.print(opt)</pre>
```

```
optimsimplex.reflect Simplex Reflection
```

Description

This function returns a new simplex by reflection of the current simplex with respect to the first vertex in the simplex. This move is used in the centered simplex gradient.

Usage

```
optimsimplex.reflect(this = NULL, fun = NULL, data = NULL)
```

Arguments

this fun

An simplex object.

The function to compute at vertices. The function is expected to have the following input and output arguments:

```
myfunction <- function(x, this){
...
return(list(f=f,this=this))
}</pre>
```

data

where x is a row vector and this a user-defined data, i.e. the data argument. A user-defined data passed to the function. If data is provided, it is passed to the callback function both as an input and output argument. data may be

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used if the function uses some additionnal parameters. It is returned as an output parameter because the function may modify the data while computing the function value. This feature may be used, for example, to count the number of times that the function has been called.

Value

Return a list with the following elements:

r The reflected simplex object.

data The updated user-defined data.

Author(s)

```
Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)
```

See Also

```
optimsimplex.new
```

Set functions

Optimsimplex Set Function Class

Description

The functions assign content to various elements of a simplex object:

```
optimsimplex.setall Set all the coordinates and the function values of all the vertices.
```

optimsimplex.setallfv Set all the function values of all the vertices.

optimsimplex.setallx Set all the coordinates of all the vertices.

optimsimplex.setfv Set the function value at a givenindex.

optimsimplex.setn Set the dimension of the space of the simplex.

optimsimplex.setnbve Set the number of vertices of the simplex.

optimsimplex.setve Set the coordinates of the vertex and the function values at a given index in the current simplex.

optimsimplex.setx Set the coordinates of the vertex at a given index in the current simplex.

Usage

```
optimsimplex.setall(this = NULL, simplex = NULL)
optimsimplex.setallfv(this = NULL, fv = NULL)
optimsimplex.setallx(this = NULL, x = NULL)
optimsimplex.setfv(this = NULL, ive = NULL, fv = NULL)
optimsimplex.setn(this = NULL, n = NULL)
optimsimplex.setnbve(this = NULL, nbve = NULL)
optimsimplex.setve(this = NULL, ive = NULL, fv = NULL, x = NULL)
optimsimplex.setx(this = NULL, ive = NULL, x = NULL)
```

Arguments

fv

х

| this | A simplex object. |
|------|-------------------|
|------|-------------------|

The simplex to set. It is expected to be a nove x n+1 matrix where n is the simplex

dimension of the space, nove is the number of vertices and with the following content:

• simplex[k,1] is the function value of the vertex k, with k = 1 to nove,

• simplex[k,2:(n+1)] is the coordinates of the vertex k, with k=1 to

A row vector of function values; fv[k] is expected to be the function value for

the vertex k, with k = 1 to nove. For optimsimplex.setfv, fv is expected to

be a numerical scalar.

The nbve x n matrix of vertice coordinates; the vertex is expected to be

stored in x[k,1:n], with k = 1 to nove. For optimsimplex.setve and

optimsimplex.setx, x is expected to be a row matrix.

ive Vertex index.

n The dimension of the space of the simplex.

nbve The number of vertices of the simplex.

Value

Return a updated simplex object this.

Author(s)

Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

optimsimplex.new

Simplex Shrink optimsimplex.shrink

Description

This function shrinks the simplex with given coefficient sigma and returns an updated simplex. The shrink is performed with respect to the first point in the simplex.

Usage

```
optimsimplex.shrink(this = NULL, fun = NULL, sigma = 0.5, data = NULL)
```

Arguments

this An simplex object

fun The function to compute at vertices. The function is expected to have the

following input and output arguments:

```
\begin{array}{l} {\rm myfunction} < - \; {\rm function}(x, \; {\rm this}) \{\\ \dots \\ {\rm return}({\rm list}(f = f, {\rm this} = {\rm this}))\\ \} \end{array}
```

where x is a row vector and this a user-defined data, i.e. the data.

sigma

The shrinkage coefficient. The default value is 0.5.

data

A user-defined data passed to the function. If data is provided, it is passed to the callback function both as an input and output argument. data may be used if the function uses some additionnal parameters. It is returned as an output parameter because the function may modify the data while computing the function value. This feature may be used, for example, to count the number of times that the function has been called.

Value

Return a list with the following elements:

this The updated simplex object.

data The updated user-defined data.

Author(s)

```
Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)
```

See Also

```
optimsimplex.new
```

optimsimplex.utils

Optimsimplex Utility Functions

Description

These functions enable various calculations and checks on the current simplex:

optimsimplex.center Compute the center of the current simplex.

optimsimplex.check Check the consistency of the data in the current simplex.

optimsimplex.deltafv Compute the vector of function value differences with respect to the function value at the first vertex (the lowest).

optimsimplex.deltafvmax Compute the difference of function value between the lowest and the highest vertices. It is expected that the first vertex (this\$x[1,]) is associated with the smallest function value and that the last vertex (this\$x[nbve,]) is associated with the highest function value.

optimsimplex.dirmat Compute the matrix of simplex direction, i.e. the matrix of differences of vertice coordinates with respect to the first vertex.

optimsimplex.fvmean Compute the mean of the function values in the current simplex.

optimsimplex.fvstdev Compute the standard deviation of the function values in the current simplex.

optimsimplex.fvvariance Compute the variance of the function values in the current simplex. optimsimplex.size Determines the size of the simplex.

optimsimplex.sort Sort the simplex by increasing order of function value, so the smallest function is at the first vertex.

optimsimplex.xbar Compute the center of n vertices, by excluding the vertex with index iexcl. The default of iexcl is the number of vertices: in that case, if the simplex is sorted in increasing function value order, the worst vertex is excluded.

Usage

```
optimsimplex.center(this = NULL)
optimsimplex.check(this = NULL)
optimsimplex.deltafv(this = NULL)
optimsimplex.deltafvmax(this = NULL)
optimsimplex.dirmat(this = NULL)
optimsimplex.fvmean(this = NULL)
optimsimplex.fvstdev(this = NULL)
optimsimplex.fvvariance(this = NULL)
optimsimplex.size(this = NULL, method = NULL)
optimsimplex.sort(this = NULL, iexcl = NULL)
```

Arguments

this The current simplex.

method The method to

The method to use to compute the size of the simplex. The available methods are the following:

'sigmaplus' (this is the default) The sigmamplus size is the maximum 2-norm length of the vector from each vertex to the first vertex. It requires one loop over the vertices.

'sigmaminus' The sigmaminus size is the minimum 2-norm length of the vector from each vertex to the first vertex. It requires one loop over the vertices.

'Nash' The 'Nash' size is the sum of the norm of the norm-1 length of the vector from the given vertex to the first vertex. It requires one loop over the vertices.

'diameter' The diameter is the maximum norm-2 length of all the edges of the simplex. It requires 2 nested loops over the vertices.

iexcl The index of the vertex to exclude in center computation.

Value

optimsimplex.center Return a vector of length nove, where nove is the number of vertices in the current simplex.

optimsimplex.check Return an error message if the dimensions of the various elements of the current simplex do not match.

optimsimplex.deltafv Return a column vector of length nbve-1.

optimsimplex.deltafvmax Return a numeric scalar.

optimsimplex.dirmat Return a n x n numeric matrix, where n is the dimension of the space of the simplex.

optimsimplex.fvmean Return a numeric scalar.

optimsimplex.fvstdev Return a numeric scalar.

optimsimplex.fvvariance Return a numeric scalar.

optimsimplex.size Return a numeric scalar.

optimsimplex.sort Return an updated simplex object.

optimsimplex.xbar Return a row vector of length n.

Author(s)

Author of Scilab optimsimplex module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References

"Compact Numerical Methods For Computers - Linear Algebra and Function Minimization", J.C. Nash, 1990, Chapter 14. Direct Search Methods

"Iterative Methods for Optimization", C.T. Kelley, 1999, Chapter 6., section 6.2

See Also

optimsimplex.new

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Version 2.0 dated 2006-09-05.