Package 'partitions'

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Type Package
Title Additive Partitions of Integers
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Depends R (>= $3.6.0$)
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Imports gmp, polynom, sets, eddington, mathjaxr
Description Additive partitions of integers. Enumerates the partitions, unequal partitions, and restricted partitions of an integer; the three corresponding partition functions are also given. Set partitions and now compositions are included.
Suggests testthat
License GPL
<pre>URL https://github.com/RobinHankin/partitions</pre>
BugReports https://github.com/RobinHankin/partitions/issues
RdMacros mathjaxr
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partitions-package Integer partitions

Description

Routines to enumerate all partitions of an integer; includes restricted and unequal partitions.

Details

This package comprises eight functions: P(), Q(), R(), and S() give the number of partitions, unequal partitions, restricted partitions, and block partitions of an integer.

Functions parts(), diffparts(), restrictedparts(), and blockparts() enumerate these partitions.

Function conjugate() gives the conjugate of a partition and function durfee() gives the size of the Durfee square.

NB the emphasis in this package is terse, efficient C code. This means that there is a minimum of argument checking. For example, function conjugate() assumes that the partition is in standard form (ie nonincreasing); supplying a vector in nonstandard form will result in garbage being returned silently. Note that a block partition is not necessarily in standard form.

Author(s)

Robin K. S. Hankin

References

- G. E. Andrews 1998 The Theory of Partitions, Cambridge University Press
- M. Abramowitz and I. A. Stegun 1965. Handbook of Mathematical Functions, New York: Dover
- G. H. Hardy and E. M. Wright 1985 *An introduction to the theory of numbers*, Clarendon Press: Oxford (fifth edition)
- R. K. S. Hankin 2006. "Additive integer partitions in R". *Journal of Statistical Software*, Volume 16, code snippet 1
- R. K. S. Hankin 2007. "Urn sampling without replacement: enumerative combinatorics in R". *Journal of Statistical Software*, Volume 17, code snippet 1
- R. K. S. Hankin 2007. "Set partitions in R". *Journal of Statistical Software*, Volume 23, code snippet 2

```
parts(5)
diffparts(9)
restrictedparts(15,10)
P(10,give=TRUE)
Q(10,give=TRUE)
R(5,10)
```

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as.matrix.partition

Coerce partitions to matrices and vice versa

Description

Coercion to and from partitions

Usage

```
## S3 method for class 'partition' as.matrix(x, ...) as.partition(x, ...)
```

Arguments

x Object to be coerced... Further arguments

Author(s)

Robin K. S. Hankin

Examples

```
as.matrix(parts(5))
```

bin

Sundry binary functionality

Description

Utilities to convert things to binary

Usage

```
tobin(n, len, check=TRUE)
todec(bin)
comptobin(comp, check=TRUE)
bintocomp(bin, use.C=TRUE, check=TRUE)
```

Arguments

n	Integer, to be converted to binary by function tobin()
len	Length of the binary vector returned by function tobin()
bin	Binary: a vector of 0s and 1s
comp	A composition
check	Boolean, with default TRUE meaning to perform various checks
use.C	Boolean, with default TRUE meaning to use C

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Details

These functions are not really intended for the end user; they are used in nextcomposition().

- Function tobin() converts integer n to a binary string of length len
- Function todec() converts a binary string to decimal, so todec(tobin(n,i))==n, provided i is big enough
- Function comptobin() converts a composition to binary
- Function bintocomp() converts a binary string to a composition

Author(s)

Robin K. S. Hankin

References

Wikipedia contributors, 2020. "Composition (combinatorics) — Wikipedia, The Free Encyclopedia", $https://en.wikipedia.org/w/index.php?title=Composition_(combinatorics)&oldid=944285378$

Examples

```
tobin(10,5)
todec(tobin(10,5))
comptobin(c(1,1,4))
bintocomp(c(1,1,0,0,1,1,1,1))
```

conjugate

Conjugate partitions and Durfee squares

Description

Given a partition, provide its conjugate or Durfee square

Usage

```
conjugate(x, sorted = TRUE)
durfee(x, sorted = TRUE)
```

Arguments

x Either a vector describing a partition or a matrix whose columns are partitions.

sorted

A logical indicating whether the data is already in standard form. That is to say, are the data within each colum sorted in decreasing order?

conjugate 5

Details

Conjugation is described in Andrews, and (eg) Hardy and Wright.

The *conjugate* of a partition may be calculated by taking its Ferrers diagram and considering the partition defined by columns instead of rows. This may be visualised by flipping the Ferrers diagram about the leading diagonal.

Essentially, conjugate() carries out R idiom rev(cumsum(table(factor(a[a>0],levels=max(a):1)))), but faster.

The "Durfee square" of a partition is defined on page 281 of Hardy and Wright. It is the largest square of nodes contained in the partition's Ferrers graph. Function durfee() returns the length of the side of the Durfee square, which Andrews denotes $d(\lambda)$. It is equivalent to R idiom function(a){sum(a>=1:length) but faster.

Value

Returns either a partition in standard form, or a matrix whose columns are partitions in standard form.

Note

If argument x is not non-increasing, you must use the sorted = FALSE flag. Otherwise, these functions will not work and will silently return garbage. Caveat emptor! (output from blockparts() is not necessarily non-increasing)

Author(s)

Robin K. S. Hankin

```
parts(5)
conjugate(parts(5))

restrictedparts(6,4)
conjugate(restrictedparts(6,4))

durfee(10:1)

# A parition in nonstandard form --- use `sorted = FALSE`
x <- parts(5)[sample(5),]
durfee(x, sorted = FALSE)
conjugate(x, sorted = FALSE)

# Suppose one wanted partitions of 8 with no part larger than 3:
conjugate(restrictedparts(8,3))

# (restrictedparts(8,3) splits 8 into at most 3 parts;
# so no part of the conjugate partition is larger than 3).</pre>
```

6 nextpart

nextpart	Next partition	

Description

Given a partition, return the "next" one; or determine whether it is the last one.

Usage

```
nextpart(part, check=TRUE)
islastpart(part)
firstpart(n)
 nextdiffpart(part, check=TRUE)
islastdiffpart(part)
firstdiffpart(n)
 nextrestrictedpart(part, check=TRUE)
islastrestrictedpart(part)
firstrestrictedpart(n, m, include.zero=TRUE)
 nextblockpart(part, f, n=sum(part), include.fewer=FALSE, check=TRUE)
firstblockpart(
                   f, n=NULL
                                , include.fewer=FALSE)
 nextcomposition(comp, restricted, include.zero=TRUE, check=TRUE)
islastcomposition(comp, restricted, include.zero=TRUE)
                              , include.zero=TRUE)
firstcomposition(n,
                     m=NULL
```

Arguments

part,comp A partition or composition

check Boolean, with default TRUE meaning to carry out various safety checks; the next() functions use C calls which might crash the session with some inputs

f, n, include.fewer, m, include.zero

Other arguments as per the vectorized version

restricted In function nextcomposition() and islastcomposition(), Boolean, with TRUE meaning to consider compositions of fixed length [eg, to iterate through the columns of compositions(6,3)], and FALSE meaning to consider compositions of any length [eg to iterate through the columns of compositions(6)]

Details

These functions are intended to enumerate partitions one at a time, eliminating the need to store a huge matrix. This is useful for optimization over large domains and makes it possible to investigate larger partitions than is possible with the vectorized codes.

The idea is to use a first...() function to generate the first partition, then iterate using a next...() function, stopping when the islast...() function returns TRUE.

An example is given below, in which the "scrabble" problem is solved; note the small size of the sample space. More examples are given in the tests/aab.R file.

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Note

Functions nextpart() and nextdiffpart() require a vector of the right length: they require and return a partition padded with zeros. Functions nextrestrictedpart() and nextblockpart() work with partitions of the specified length. Function nextcomposition() truncates any zeros at the end of the composition. This behaviour is inherited from the C code.

In functions nextcomposition() and firstcomposition(), argument include.zero is ignored if restricted is FALSE.

I must say that the performance of these functions is terrible; they are much much slower than their vectorized equivalents. The magnitude of the difference is much larger than I expected. Heigh ho. Frankly you would better off working directly in C.

Author(s)

Robin K. S. Hankin

See Also

parts

Examples

```
# Do the optimization in scrabble vignette, one partition at a time:
# (but with a smaller letter bag)
scrabble <- c(a=9 , b=2 , c=2 , d=4 , e=12 , f=2 , g=3)

f <- function(a){prod(choose(scrabble,a))/choose(sum(scrabble),7)}
bestsofar <- 0
a <- firstblockpart(scrabble,7)
while(!islastpart(a)){
    jj <- f(a)
    if(jj>bestsofar){
        bestsofar <- jj
        bestpart <- a
    }
    a <- nextblockpart(a,scrabble)
}</pre>
```

 $Number\ of\ partitions\ of\ an\ integer$

Description

Given an integer, P() returns the number of additive partitions, Q() returns the number of unequal partitions, and R() returns the number of restricted partitions. Function S() returns the number of block partitions.

Ρ

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Usage

```
P(n, give = FALSE)
Q(n, give = FALSE)
R(m, n, include.zero = FALSE)
S(f, n = NULL, include.fewer = FALSE)
```

Arguments

n	Integer whose partition number is desired. In function S(), the default of NULL means to return the number of partitions of any size
m	In function R(), the order of the decomposition
give	Boolean, with default FALSE meaning to return just $P(n)$ or $Q(n)$ and TRUE meaning to return $P(1:n)$ or $Q(1:n)$ (this option takes no extra computation)
include.zero	In restrictedparts(), Boolean with default FALSE meaning to count only partitions of n into $exactly\ m$ parts; and TRUE meaning to include partitions of n into $at\ most\ m$ parts (because parts of zero are included)
include.fewer	In function blockparts(), Boolean with default FALSE meaning to return partitions into <i>exactly</i> n and TRUE meaning to return partitions into <i>at most</i> n
f	In function S(), the stack vector

Details

Functions P() and Q() use Euler's recursion formula. Function R() enumerates the partitions using Hindenburg's method (see Andrews) and counts them until the recursion bottoms out.

Function S() finds the coefficient of x^n in the generating function $\prod_{i=1}^L \sum_{j=0}^{f_i} x^j$, where L is the length of f, using the **polynom** package.

All these functions return a double.

Note

Functions P() and Q() use unsigned long long integers, a type which is system-dependent. For me, P() works for n equal to or less than 416, and Q() works for n less than or equal to 792. YMMV; none of the methods test for overflow, so use with care!

Author(s)

Robin K. S. Hankin; S() is due to an anonymous JSS referee

```
P(10,give=TRUE)
Q(10,give=TRUE)
R(10,20,include.zero=FALSE)
R(10,20,include.zero=TRUE)
S(1:4,5)
```

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parts Enumerate the partitions of an integer	
--	--

Description

Given an integer, return a matrix whose columns enumerate various partitions.

Function parts() returns the unrestricted partitions; function diffparts() returns the unequal partitions; function restrictedparts() returns the restricted partitions; function blockparts() returns the partitions subject to specified maxima; and function compositions() returns all compositions of the argument.

Usage

```
parts(n)
diffparts(n)
restrictedparts(n, m, include.zero=TRUE, decreasing=TRUE)
blockparts(f, n=NULL, include.fewer=FALSE)
compositions(n, m=NULL, include.zero=TRUE)
multiset(v,n=length(v))
mset(v)
```

Arguments

n	Integer to be partitioned. In function blockparts(), the default of NULL means to return all partitions of any size
m	In functions $\ensuremath{restrictedparts}$ () and $\ensuremath{compositions}$ (), the order of the partition
include.zero	In functions restrictedparts() and compositions(), Boolean with default FALSE meaning to include only partitions of n into exactly m parts; and TRUE meaning to include partitions of n into at most m parts (because zero parts are included)
include.fewer	In function blockparts(), Boolean with default FALSE meaning to return vectors whose sum is $\it exactly$ n and TRUE meaning to return partitions whose sum is $\it at most$ n
decreasing	In restrictedparts(), Boolean with default TRUE meaning to return partitions whose parts are in decreasing order and FALSE meaning to return partitions in lexicographical order, as appearing in Hindenburg's algorithm. Note that setting to decreasing to FALSE has the effect of making conjugate() return garbage
f	In function blockparts(), a vector of strictly positive integers that gives the maximal number of blocks; see details
V	In function multiset(), an integer vector representing a multiset. Argument n is the size of the sample to be taken

Details

• Function parts() uses the algorithm in Andrews. Function diffparts() uses a very similar algorithm that I have not seen elsewhere. These functions behave strangely if given an argument of zero.

10 parts

• Function restrictedparts() uses the algorithm in Andrews, originally due to Hindenburg. For partitions into at most m parts, the same Hindenburg's algorithm is used but with a start vector of c(rep(0,m-1),n).

If m > n, the partitions are padded with zeros.

• Function blockparts() enumerates the compositions of an integer subject to a maximum criterion: given vector $y = (y_1, \ldots, y_n)$ all sets of $a = (a_1, \ldots, a_n)$ satisfying $\sum_{i=1}^p a_i = n$ subject to $0 \le a_i \le y_i$ for all i are given in lexicographical order. If argument y includes zero elements, these are treated consistently (ie a position with zero capacity).

If n takes its default value of NULL, then the restriction $\sum_{i=1}^{p} a_i = n$ is relaxed (so that the numbers may sum to anything). Note that these solutions are not necessarily in standard form, so functions durfee() and conjugate() may fail.

• With a single argument, compositions(n) returns all 2^{n-1} ways of partitioning an integer; thus 4+1+1 is distinct from 1+4+1 or 1+1+4.

With two arguments, compositions (n, m) returns all nonnegative solutions to $x_1 + \cdots + x_m = n$.

This function is different from all the others in the package in that it is written in R; it is not clear that C would be any faster.

• Function multiset() returns all ways of ordering a multiset (mset() is a low-level helper function).

```
[1,] 7 6 5 5 4 4 4 3 3 3 3 2 2 2 1
[2,] 0 1 2 1 3 2 1 3 2 2 1 2 2 1 1
[3,] 0 0 0 1 0 1 1 1 2 1 1 2 1 1 1
[4,] 0 0 0 0 0 0 1 0 0 1 1 1 1 1 1
[5,] 0 0 0 0 0 0 0 0 0 1 0 1 1 1
[6,] 0 0 0 0 0 0 0 0 0 0 0 0 1 1
[7,] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1
> P(7)
[1] 15
> diffparts(9)
[1,] 9 8 7 6 6 5 5 4
[2,] 0 1 2 3 2 4 3 3
[3,] 0 0 0 0 1 0 1 2
> Q(9)
[1] 8
> restrictedparts(9,4)
[1,] 9 8 7 6 5 7 6 5 4 5 4 3 6 5 4 4 3 3
[2,] 0 1 2 3 4 1 2 3 4 2 3 3 1 2 3 2 3 2
[3,] 0 0 0 0 0 1 1 1 1 2 2 3 1 1 1 2 2 2
[4,] 0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 1 2
> R(4,9,include.zero=TRUE)
[1] 18
> blockparts(1:4,5)
[1,] 1 1 0 1 1 0 1 0 1 1 0 1 0 0 1 0 1 0 0 1 0 0
[2,] 2 1 2 2 1 2 0 1 2 1 2 0 1 0 1 2 0 1 0 0 1 0
\hbox{\tt [3,] 2 3 3 1 2 2 3 3 0 1 1 2 2 3 0 0 1 1 2 0 0 1}
```

> parts(7)

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```
[4,] 0 0 0 1 1 1 1 1 2 2 2 2 2 2 3 3 3 3 3 4 4 4
> S(1:4,5)
[1] 22
> compositions(5,3)
[1,] 5 4 3 2 1 0 4 3 2 1 0 3 2 1 0 2 1 0 1 0 0
[2,] 0 1 2 3 4 5 0 1 2 3 4 0 1 2 3 0 1 2 0 1 0
[3,] 0 0 0 0 0 0 1 1 1 1 1 2 2 2 2 3 3 3 4 4 5
> S(rep(5,3),5)
[1] 21
> setparts(4)
[1,] 1 1 1 1 2 1 1 1 1 1 1 2 2 2 1
[2,] 1 1 1 2 1 2 1 2 2 1 2 1 1 3 2
[3,] 1 2 1 1 1 2 2 1 3 2 1 3 1 1 3
[4,] 1 1 2 1 1 1 2 2 1 3 3 1 3 1 4
> setparts(c(1,2,2))
[1,] 1 1 1 1 1 1 1 1 1 1 1 3 3 3
[2,] 2 2 3 1 1 1 2 2 3 2 2 3 1 1 1
[3,] 3 2 2 3 2 2 1 1 1 3 2 2 2 1 2
[4,] 2 3 2 2 3 2 3 2 2 1 1 1 2 2 1
[5,] 1 1 1 2 2 3 2 3 2 2 3 2 1 2 2
```

Note

These vectorized functions return a matrix whose columns are the partitions. If this matrix is too large, consider enumerating the partitions individually using the functionality documented in nextpart.Rd.

One commonly encountered idiom is blockparts(rep(n,n),n), which is equivalent to compositions(n,n) [Sloane's A001700].

If you have a minimum number of balls in each block, a construction like

```
x <- c(1,1,2,1)  # min

y <- c(2,3,4,5)  # max

sweep(blockparts(y-x,7-sum(x)),1,x,"+")
```

can be helpful (that is, subtract off the minimum number of balls and add them back again at the end).

Author(s)

Robin K. S. Hankin

References

- G. E. Andrews. "The theory of partitions", Cambridge University Press, 1998
- R. K. S. Hankin 2006. "Additive integer partitions in R". *Journal of Statistical Software*, Volume 16, code snippet 1

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• R. K. S. Hankin 2007. "Urn sampling without replacement: enumerative combinatorics in R". *Journal of Statistical Software*, Volume 17, code snippet 1

- R. K. S. Hankin 2007. "Set partitions in R". *Journal of Statistical Software*, Volume 23, code snippet 2
- N. J. A. Sloane, 2008, The On-Line Encyclopedia of Integer Sequences. Sequence A001700
- D. Knuth, 2004. The art of computer programming, pre-fascicle 2B "Generating all permutations"

See Also

```
nextpart
```

Examples

```
parts(5)
diffparts(10)
matplot(t(diffparts(27)),type='1',lty=1)
restrictedparts(9,4)
restrictedparts(9,4,FALSE)
restrictedparts(9,4,decreasing=TRUE)
blockparts(1:4)
blockparts(1:4,3)
blockparts(1:4,3,include.fewer=TRUE)
blockparts(c(4,3,3,2),5) # Knuth's example, pre-fascicle 3a, p16
compositions(4)
                          # not the same as parts(4)
compositions(4,4)
# With 10 blocks, enumerate all partitions with maxima of 1:5 and minima
# of c(0,1,1,2,1):
a \leftarrow c(0,1,1,2,1)
sweep(blockparts(1:5-a,10-sum(a)),1,a,"+")
#Knuth's example:
multiset(c(1,2,2,3))
multiset(rep(4+1:3,1:3),3)
```

perms

Enumerate the permutations of a vector

Description

Given an integer n, return a matrix whose columns enumerate various permutations of 1:n.

Function perms() returns all permutations in lexicographic order; function plainperms() returns all permutations by repeatedly exchanging adjacent pairs.

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Usage

```
perms(n)
plainperms(n)
```

Arguments

n

Integer argument; permutations of 1:n returned

Note

Comments in the C code; algorithm lifted from 'fasc2b.pdf'.

Author(s)

D. E. Knuth; C and R transliteration by Robin K. S. Hankin

References

• D. E. Knuth 2004. "The art of computer programming, pre-fascicle 2B. A draft of section 7.2.1.2: Generating all permutations". https://www-cs-faculty.stanford.edu/~knuth/taocp.html

See Also

```
parts
```

Examples

print.partition

Print methods for partition objects and equivalence objects

Description

A print method for partition objects, summary partition objects, and equivalence classes. Includes various configurable options

Usage

```
## S3 method for class 'partition'
print(x, mat = getOption("matrixlike"), h = getOption("horiz"), ...)
## S3 method for class 'summary.partition'
print(x, ...)
## S3 method for class 'equivalence'
print(x, sep = getOption("separator"), ...)
```

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Arguments

Х	Object to be printed: an object of class either partition or summary.partition
mat	Boolean, with TRUE meaning to print like a matrix, and any other value meaning to print without column names (which usually results in more compact appearance)
h	Boolean governing the orientation of the printed matrix, with TRUE meaning to print with the rows being the partitions and any other value (the default) meaning to print the transpose
sep	Character vector, with special value of NULL interpreted as a comma; see examples section
	Further arguments provided for compatibility

Author(s)

Robin K. S. Hankin

Examples

```
print(parts(5))
summary(parts(7))
listParts(3)
options(separator="")
listParts(5)
```

setparts

Set partitions

Description

Enumeration of set partitions

Usage

```
setparts(x)
listParts(x,do.set=FALSE)
vec_to_set(vec)
vec_to_eq(vec)
```

Arguments

X	If a vector of length 1, the size of the set to be partitioned. If a vector of length greater than 1, return all equivalence relations with equivalence classes with sizes of the elements of x . If a matrix, return all equivalence classes with sizes of the columns of x
do.set	Boolean, with TRUE meaning to return the set partitions in terms of sets (as per sets package) and default FALSE meaning to present the result in terms of equivalence classes
vec	An integer vector representing a set partition

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Details

A partition of a set $S = \{1, ..., n\}$ is a family of sets $T_1, ..., T_k$ satisfying

```
• i \neq j \longrightarrow T_i \cap T_j = \emptyset
```

- $\bigcup_{i=1}^k T_k = S$
- $T_i \neq \emptyset$ for $i = 1, \dots, k$

The induced equivalence relation has $i \sim j$ if and only if i and j belong to the same partition. Equivalence classes may be listed using listParts()

There are exactly fifteen ways to partition a set of four elements:

```
\begin{array}{l} (1234) \\ (123)(4), (124)(3), (134)(2), (234)(1) \\ (12)(34), (13)(24), (14)(23) \\ (12)(3)(4), (13)(2)(4), (23)(1)(4), (24)(1)(3), (34)(1)(2) \\ (1)(2)(3)(4) \end{array}
```

Note that (12)(3)(4) is the same partition as, for example, (3)(4)(21) as the equivalence relation is the same.

Consider partitions of a set S of five elements (named 1, 2, 3, 4, 5) with sizes 2,2,1. These may be enumerated as follows:

```
> u <- c(2,2,1)
> setparts(u)

[1,] 1 1 1 1 1 1 1 1 1 1 1 1 1 3 3 3
[2,] 2 2 3 1 1 1 2 2 3 2 2 3 1 1 1
[3,] 3 2 2 3 2 2 1 1 1 3 2 2 2 1 2
[4,] 2 3 2 2 3 2 3 2 2 1 1 1 2 2 1
[5,] 1 1 1 2 2 3 2 3 2 3 2 2 3 2 1 2 2
```

See how each column has two 1s, two 2s and one 3. This is because the first and second classes have size two, and the third has size one.

The first partition, x=c(1,2,3,2,1), is read "class 1 contains elements 1 and 5 (because the first and fifth element of x is 1); class 2 contains elements 2 and 4 (because the second and fourth element of x is 2); and class 3 contains element 3 (because the third element of x is 3)". Formally, class i has elements which (x==u[i]).

You can change the print method by setting, eg, option(separator="").

Functions vec_to_set() and vec_to_eq() are low-level helper functions. These take an integer vector, typically a column of a matrix produced by setparts() and return their set representation.

Value

Returns a matrix each of whose columns show a set partition; an object of class "partition". Type ?print.partition to see how to change the options for printing.

Note

The **clue** package by Kurt Hornik contains functionality for partitions (specifically cl_meet() and cl_join()) which might be useful. Option do.set invokes functionality from the **sets** package by Meyer et al.

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Author(s)

Luke G. West (C++) and Robin K. S. Hankin (R); listParts() provided by Diana Tichy

References

- R. K. S. Hankin 2006. *Additive integer partitions in R. Journal of Statistical Software*, Code Snippets 16(1)
- R. K. S. Hankin 2007. "Set partitions in R". *Journal of Statistical Software*, Volume 23, code snippet 2
- Kurt Hornik (2017). *clue: Cluster ensembles*. R package version 0.3-53. https://CRAN. R-project.org/package=clue
- Kurt Hornik (2005). *A CLUE for CLUster Ensembles*. Journal of Statistical Software 14/12. https://www.jstatsoft.org/v14/i12/

See Also

```
parts, print.partition
```

Examples

```
# all partitions of a set of 4 elements
setparts(4)
setparts(c(3,3,2))
                           # all partitions of a set of 8 elements
                           # into sets of sizes 3,3,2.
jj <- restrictedparts(5,3)</pre>
                           # partitions of a set of 5 elements into
setparts(jj)
                           # at most 3 sets
listParts(jj)
                           # induced equivalence classes
setparts(conjugate(jj))
                           # partitions of a set of 5 elements into
                           # sets not exceeding 3 elements
                           # partitions of a set of 5 elements into
setparts(diffparts(5))
                           # sets of different sizes
```

summary.partition

Provides a summary of a partition

Description

Provides a summary of an object of class partition: usually the first and last few partitions (columns)

Usage

```
## S3 method for class 'partition'
summary(object, ...)
```

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Arguments

object Partition

... Further arguments; see details section below

Details

The ellipsis arguments are used to pass how many columns at the start and the end of the matrix are selected; this defaults to 10.

The function is designed to behave as expected: if there is an argument named "n", then this is used. If there is no such argument, the first one is used.

Value

A summary object is a list, comprising three elements:

shortened Boolean, with TRUE meaning that the middle section of the matrix is ommitted,

and FALSE meaning that the entire matrix is returned because n is too big

n Number of columns to return at the start and the end of the matrix

out Matrix returned: just the first and last n columns (if shortened is TRUE), or the

whole matrix if not

Author(s)

Robin K. S. Hankin

```
summary(parts(7))
summary(parts(11),3)
```

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