Validation of 'sasLM' Package

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1 Tested Version and Books used for the Validation

1.1 Packages Used

• 'sasLM' version: 0.6.5

• 'SAS' version: 9.4 Licensed and University Edition

• 'car' version: 3.0.11

• R version: R version 4.1.2 (2021-11-01)

The 'car' package is not necessary for 'sasLM.' It is used for the comparison of the results.

If you see any difference betwwen 'car' and 'sasLM', 'SAS' results coincide with 'sasLM', not with 'car.'

Before 'sasLM' is available on CRAN, you can download using the following command in R.

```
install.packages("sasLM", repos="http://r.acr.kr")
```

1.2 Books and Articles used for the Test

- 1. Harvey WR. Least-Squares Analysis of Data with Unequal Subclass Frequencies. USDA, Agriculture Research Service, ARS 20-8. 1960. reprinted with corrections as ARS H-4, 1975, also reprinted 1979.
- 2. Snee RD. Computation and Use of Expected Mean Squares in Analysis of Variance. J Qual Tech. 1974:6(3);128-137.
- 3. Goodnight JH. The General Linear Models Procedure, Proceedings of the First International SAS User's Group, SAS Institute, Raleigh, N.C. 1976.
- 4. Littell RC, Stroup WW, Freund RJ. SAS for Linear Models 4e. John Wiley & Sons Inc. 2002.
- 5. Sahai H, Ojeda MM. Analysis of Variance for Random Models Volume 2 Unbalanced Data. 2005.
- Federer WT, King F. Variations on Split Plot and Split Block Experiment Designs. John Wiley & Sons Inc. 2007.
- 7. Hinkelmann K, Kempthorne O. Design and Analysis of Experiments Volume 1 Introduction to Experimental Design. 2e. John Wiley & Sons Inc. 2008.
- 8. Hinkelmann K, Kempthorne O. Design and Analysis of Experiments Volume 2 Advanced Experimental Design. John Wiley & Sons Inc. 2005.
- 9. Lawson J. Design and Analysis of Experiments with SAS. Taylor and Francis Group. 2010.
- 10. Searle SR, Gruber MHJ. Linear Models 2e, Kindle Edition. John Wiley & Sons Inc. 2016.

2 ARS20-8

Reference

• Harvey WR. Least-Squares Analysis of Data with Unequal Subclass Frequencies. USDA, Agriculture Research Service, ARS 20-8. 1960. reprinted with corrections as ARS H-4, 1975, also reprinted 1979.

2.1 p8

(1) MODEL

```
p8 = read.csv("C:/G/Rt/ANOVA/ARS20-8p8.csv")
p8 = af(p8, c("PigNo", "Ration"))
ANOVA(Barrow ~ Ration, p8)
$ANOVA
Response : Barrow
                Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                 2 11.111 5.5556 1.2626 0.3113
RESIDUALS
                15 66.000 4.4000
CORRECTED TOTAL 17 77.111
$`Type I`
       Df Sum Sq Mean Sq F value Pr(>F)
Ration 2 11.111 5.5556 1.2626 0.3113
$`Type II`
      Df Sum Sq Mean Sq F value Pr(>F)
Ration 2 11.111 5.5556 1.2626 0.3113
$`Type III`
       Df Sum Sq Mean Sq F value Pr(>F)
Ration 2 11.111 5.5556 1.2626 0.3113
```

2.2 p42

(2) MODEL

```
p42 = read.csv("C:/G/Rt/ANOVA/ARS20-8p42.csv")
p42 = af(p42, c("Ration", "Pig", "Sire"))
ANOVA(Y ~ Sire + Ration, p42)
```

```
$ANOVA
```

Response : Y

```
Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                3 20.819 6.9397 1.7259 0.2075
RESIDUALS
               14 56.292 4.0209
CORRECTED TOTAL 17 77.111
$`Type I`
      Df Sum Sq Mean Sq F value Pr(>F)
       2 11.1111 5.5556 1.3817 0.2834
Ration 1 9.7079 9.7079 2.4144 0.1425
$`Type II`
      Df Sum Sq Mean Sq F value Pr(>F)
       2 15.6829 7.8414 1.9502 0.1790
Ration 1 9.7079 9.7079 2.4144 0.1425
$`Type III`
      Df Sum Sq Mean Sq F value Pr(>F)
       2 15.6829 7.8414 1.9502 0.1790
Ration 1 9.7079 9.7079 2.4144 0.1425
 (3) MODEL
ANOVA(Y ~ Sire + Ration + Sire:Ration, p42)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
                5 51.044 10.2089 4.6997 0.01311 *
MODEL
RESIDUALS
               12 26.067 2.1722
CORRECTED TOTAL 17 77.111
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
           Df Sum Sq Mean Sq F value Pr(>F)
Sire
            2 11.1111 5.5556 2.5575 0.118799
            1 9.7079 9.7079 4.4691 0.056129 .
Ration
Sire:Ration 2 30.2255 15.1127 6.9573 0.009859 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
           Df Sum Sq Mean Sq F value Pr(>F)
            2 15.6829 7.8414 3.6099 0.059238 .
Sire
Ration
            1 9.7079 9.7079 4.4691 0.056129 .
Sire:Ration 2 30.2255 15.1127 6.9573 0.009859 **
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
           Df Sum Sq Mean Sq F value
            2 21.0007 10.5004 4.8339 0.028853 *
Sire
            1 3.5919 3.5919 1.6535 0.222736
Ration
Sire:Ration 2 30.2255 15.1127 6.9573 0.009859 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
2.3 p101
 (4) MODEL
p101 = read.csv("C:/G/Rt/ANOVA/ARS20-8p101.csv")
p101 = af(p101, c("Line", "Sire", "Dam", "Steer"))
ANOVA(Gain ~ Line + Sire + Dam + Line:Dam + Age + Weight, p101)
$ANOVA
Response : Gain
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               16 2.4972 0.156073 3.0675 0.001364 **
RESIDUALS
               48 2.4422 0.050879
CORRECTED TOTAL 64 4.9394
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value Pr(>F)
Line
         2 0.38009 0.190046 3.7352 0.03107 *
Sire
         6 0.92634 0.154391 3.0345 0.01347 *
Dam
         2 0.11894 0.059471 1.1689 0.31940
Line:Dam 4 0.64889 0.162222 3.1884 0.02113 *
         1 0.16462 0.164622 3.2356 0.07835 .
Age
         1 0.25828 0.258283 5.0764 0.02886 *
Weight
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
            Sum Sq Mean Sq F value Pr(>F)
        Df
Line
Sire
         6 0.95299 0.15883 3.1217 0.01155 *
         2 0.32039 0.16019 3.1485 0.05190 .
Line:Dam 4 0.46516 0.11629 2.2856 0.07373 .
         1 0.34830 0.34830 6.8456 0.01185 *
Age
         1 0.25828 0.25828 5.0764 0.02886 *
Weight
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
        Df Sum Sq Mean Sq F value Pr(>F)
Line
Sire
         6 0.95299 0.15883 3.1217 0.01155 *
         2 0.12469 0.06234 1.2253 0.30268
Dam
Line:Dam 4 0.46516 0.11629 2.2856 0.07373 .
         1 0.34830 0.34830 6.8456 0.01185 *
Age
         1 0.25828 0.25828 5.0764 0.02886 *
Weight
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
 (5) MODEL
ANOVA(Gain ~ Sire + Dam + Line:Dam, p101)
$ANOVA
Response : Gain
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
               14 2.0743 0.148162 2.5856 0.006996 **
MODEL
RESIDUALS
               50 2.8651 0.057302
CORRECTED TOTAL 64 4.9394
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value Pr(>F)
         8 1.30644 0.163305 2.8499 0.01089 *
Dam
         2 0.11894 0.059471 1.0379 0.36172
Dam:Line 4 0.64889 0.162222 2.8310 0.03412 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value Pr(>F)
         6 1.06000 0.176667 3.0831 0.01202 *
Sire
         2 0.11894 0.059471 1.0379 0.36172
Dam
Dam:Line 4 0.64889 0.162222 2.8310 0.03412 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
        Df Sum Sq Mean Sq F value Pr(>F)
```

```
Sire 6 1.06000 0.176667 3.0831 0.01202 *
Dam 2 0.02569 0.012844 0.2242 0.79999
Dam:Line 4 0.64889 0.162222 2.8310 0.03412 *
```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

3 Snee EMS ANOVA 1974

Reference

• Snee RD. Computation and Use of Expected Mean Squares in Analysis of Variance. J Qual Tech. 1974:6(3);128-137.

(6) MODEL

CORRECTED TOTAL 167 751.27

```
$`Type I`
```

MODEL RESIDUALS

Df Sum Sq Mean Sq F value Pr(>F)
Day 41 365.58 8.9166
Day:Machine 42 196.59 4.6807
Day:Machine:Analyst 42 118.80 2.8285
Day:Machine:Analyst:Test 42 70.30 1.6739

167 751.27 4.4986

0.00

0

\$`Type II`

Df Sum Sq Mean Sq F value Pr(>F)
Day 41 365.58 8.9166
Day:Machine 42 196.59 4.6807
Day:Machine:Analyst 42 118.80 2.8285
Day:Machine:Analyst:Test 42 70.30 1.6739

\$`Type III`

Df Sum Sq Mean Sq F value Pr(>F)
Day 41 359.44 8.7669

Day:Machine 42 199.40 4.7477
Day:Machine:Analyst 42 118.80 2.8285
Day:Machine:Analyst:Test 42 70.30 1.6739

```
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(Y ~ Day/Machine/Analyst/Test, Snee), type=3, singular.ok=TRUE)
# NOT WORKING
```

4 Goodnight

Reference

• Goodnight JH. The General Linear Models Procedure, Proceedings of the First International SAS User's Group, SAS Institute, Raleigh, N.C. 1976.

4.1 Type ISS

4.1.1 p7

(7) MODEL

```
p7 = read.csv("C:/G/Rt/ANOVA/Goodnight-p7.csv")
p7 = af(p7, c("A", "B"))
ANOVA(y \sim A + B + A:B, p7)
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                3 13.6027 4.5342
                                    2.807 0.1721
RESIDUALS
                4 6.4613 1.6153
CORRECTED TOTAL 7 20.0639
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 10.8113 10.8113 6.6929 0.06087 .
    1 1.3122 1.3122 0.8123 0.41839
A:B 1 1.4792 1.4792 0.9157 0.39279
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 10.8113 10.8113 6.6929 0.06087 .
    1 1.3122 1.3122 0.8123 0.41839
A:B 1 1.4792 1.4792 0.9157 0.39279
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 10.8113 10.8113 6.6929 0.06087 .
    1 1.3122 1.3122 0.8123 0.41839
A:B 1 1.4792 1.4792 0.9157 0.39279
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

(8) MODEL

$ANOVA(y \sim A + A:B + B, p7)$

```
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               3 13.6027 4.5342 2.807 0.1721
RESIDUALS
               4 6.4613 1.6153
CORRECTED TOTAL 7 20.0639
$`Type I`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 10.8113 10.8113 6.6929 0.06087 .
A:B 2 2.7914 1.3957 0.8640 0.48764
В
   0
___
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
A 1 10.8113 10.8113 6.6929 0.06087 .
A:B 1 1.4792 1.4792 0.9157 0.39279
B 1 1.3122 1.3122 0.8123 0.41839
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
   1 10.8113 10.8113 6.6929 0.06087 .
A:B 1 1.4792 1.4792 0.9157 0.39279
    1 1.3122 1.3122 0.8123 0.41839
В
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
 (9) MODEL
```

$ANOVA(y \sim B + A + A:B, p7)$

```
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                3 13.6027 4.5342 2.807 0.1721
RESIDUALS
               4 6.4613 1.6153
CORRECTED TOTAL 7 20.0639
```

```
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
   1 1.3122 1.3122 0.8123 0.41839
    1 10.8113 10.8113 6.6929 0.06087 .
B:A 1 1.4792 1.4792 0.9157 0.39279
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
  Df Sum Sq Mean Sq F value Pr(>F)
   1 1.3122 1.3122 0.8123 0.41839
   1 10.8113 10.8113 6.6929 0.06087 .
B:A 1 1.4792 1.4792 0.9157 0.39279
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
   1 1.3122 1.3122 0.8123 0.41839
   1 10.8113 10.8113 6.6929 0.06087 .
B:A 1 1.4792 1.4792 0.9157 0.39279
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(10) MODEL
ANOVA(y \sim B + A:B + A, p7)
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               3 13.6027 4.5342 2.807 0.1721
               4 6.4613 1.6153
RESIDUALS
CORRECTED TOTAL 7 20.0639
$`Type I`
  Df Sum Sq Mean Sq F value Pr(>F)
   1 1.3122 1.3122 0.8123 0.4184
B:A 2 12.2905 6.1452 3.8043 0.1187
    0
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 1.3122 1.3122 0.8123 0.41839
B:A 1 1.4792 1.4792 0.9157 0.39279
    1 10.8113 10.8113 6.6929 0.06087 .
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
   1 1.3122 1.3122 0.8123 0.41839
B:A 1 1.4792 1.4792 0.9157 0.39279
   1 10.8113 10.8113 6.6929 0.06087 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(11) MODEL
ANOVA(y \sim A:B + A + B, p7)
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
               3 13.6027 4.5342 2.807 0.1721
MODEL
RESIDUALS
               4 6.4613 1.6153
CORRECTED TOTAL 7 20.0639
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
A:B 3 13.603 4.5342 2.807 0.1721
    0
В
    0
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
A:B 1 1.4792 1.4792 0.9157 0.39279
A 1 10.8113 10.8113 6.6929 0.06087 .
    1 1.3122 1.3122 0.8123 0.41839
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
A:B 1 1.4792 1.4792 0.9157 0.39279
   1 10.8113 10.8113 6.6929 0.06087 .
В
   1 1.3122 1.3122 0.8123 0.41839
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(12) MODEL
```

```
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                3 13.6027 4.5342
                                 2.807 0.1721
RESIDUALS
                4 6.4613 1.6153
CORRECTED TOTAL 7 20.0639
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
A:B 3 13.603 4.5342 2.807 0.1721
    0
Α
В
    0
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
A:B 1 1.4792 1.4792 0.9157 0.39279
    1 10.8113 10.8113 6.6929 0.06087 .
    1 1.3122 1.3122 0.8123 0.41839
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
A:B 1 1.4792 1.4792 0.9157 0.39279
    1 10.8113 10.8113 6.6929 0.06087 .
    1 1.3122 1.3122 0.8123 0.41839
В
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
4.2 Type II SS
4.2.1 p14
(13) MODEL
ANOVA(y ~ A + B + A:B, p7[-8,]) # p16
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                3 12.7672 4.2557 2.0088 0.2906
MODEL
                3 6.3555 2.1185
RESIDUALS
```

 $ANOVA(y \sim A:B + A + B, p7)$

CORRECTED TOTAL 6 19.1227

```
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 9.9567 9.9567 4.6999 0.1187
    A:B 1 0.8880 0.8880 0.4192 0.5635
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 11.1715 11.1715 5.2733 0.1053
    1 1.9225 1.9225 0.9075 0.4111
A:B 1 0.8880 0.8880 0.4192 0.5635
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 9.5258  9.5258  4.4965  0.1241
    A:B 1 0.8880 0.8880 0.4192 0.5635
4.2.2 p24
(14) MODEL
p24 = read.csv("C:/G/Rt/ANOVA/Goodnight-p24.csv")
p24 = af(p24, c("A", "B", "C"))
ANOVA(Y ~ A + B + C, p24) # p27
$ANOVA
Response : Y
              Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               6 45.924 7.6540 9.1615 0.00499 **
RESIDUALS
               7 5.848 0.8354
CORRECTED TOTAL 13 51.772
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
 Df Sum Sq Mean Sq F value Pr(>F)
A 1 4.724 4.7235 5.6538 0.04904 *
B 3 37.998 12.6660 15.1606 0.00191 **
C 2 3.203 1.6013 1.9167 0.21686
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
 Df Sum Sq Mean Sq F value Pr(>F)
```

```
A 0
B 2 0.4424 0.2212 0.2648 0.7747
C 2 3.2025 1.6013 1.9167 0.2169
$`Type III`
CAUTION: Singularity Exists!
 Df Sum Sq Mean Sq F value Pr(>F)
B 2 0.4424 0.2212 0.2648 0.7747
C 2 3.2026 1.6013 1.9167 0.2169
4.3 Type III SS
4.3.1 p27
(15) MODEL
p27 = read.csv("C:/G/Rt/ANOVA/Goodnight-p27.csv")
p27 = af(p27, c("A", "B"))
ANOVA(y ~ A + B + A:B, p27) # p29
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                5 128.193 25.6386 53.469 6.77e-05 ***
MODEL
RESIDUALS
                    2.877 0.4795
CORRECTED TOTAL 11 131.070
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
                               Pr(>F)
    2 89.580 44.790 93.4102 3.013e-05 ***
    2 38.542 19.271 40.1901 0.0003351 ***
A:B 1 0.071 0.071 0.1471 0.7145464
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
    2 126.778 63.389 132.1977 1.093e-05 ***
    2 38.542 19.271 40.1901 0.0003351 ***
A:B 1 0.071
              0.071 0.1471 0.7145464
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
$`Type III`
   Df Sum Sq Mean Sq F value
    2 126.778 63.389 132.1977 1.093e-05 ***
    2 38.542 19.271 40.1901 0.0003351 ***
A:B 1 0.071 0.071
                        0.1471 0.7145464
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
4.3.2 p33
(16) MODEL
p33 = read.csv("C:/G/Rt/ANOVA/Goodnight-p33.csv")
p33 = af(p33, c("A", "B"))
ANOVA(y ~ A + B + A:B, p33) # p35
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                4 34.905 8.7261
MODEL
                0.000
RESIDUALS
CORRECTED TOTAL 4 34.905
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    2 11.3739 5.6870
    1 23.5225 23.5225
A:B 1 0.0081 0.0081
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 3.0276 3.0276
    1 23.5225 23.5225
A:B 1 0.0081 0.0081
$`Type III`
CAUTION: Singularity Exists!
   Df Sum Sq Mean Sq F value Pr(>F)
   1 3.0276 3.0276
Α
    1 23.5225 23.5225
A:B 1 0.0081 0.0081
options(contrasts = c("contr.sum", "contr.poly"))
Anova(lm(y ~ A + B + A:B, p33), type=3, singular.ok=TRUE) # NOT WORKING
```

5 SAS for Linear Models 4e

Reference

• Littell RC, Stroup WW, Freund RJ. SAS for Linear Models 4e. John Wiley & Sons Inc. 2002.

5.1 Chapter 2

5.1.1 p5

(17) MODEL

```
p5 = read.table("C:/G/Rt/SAS4lm/p5.txt", head=TRUE)
ANOVA(COST ~ CATTLE, p5) # p6 Output 2.2
```

```
$ANOVA
Response : COST
               Df Sum Sq Mean Sq F value
MODEL
                1 6582.1 6582.1
                                  59.34 6.083e-07 ***
RESIDUALS
               17 1885.7
                         110.9
CORRECTED TOTAL 18 8467.8
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
CATTLE 1 6582.1 6582.1 59.34 6.083e-07 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
      Df Sum Sq Mean Sq F value
CATTLE 1 6582.1 6582.1 59.34 6.083e-07 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
CATTLE 1 6582.1 6582.1 59.34 6.083e-07 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

5.1.2 p12

(18) MODEL

```
ANOVA(COST ~ CATTLE + CALVES + HOGS + SHEEP, p12)
$ANOVA
Response : COST
               Df Sum Sq Mean Sq F value
                                  52.31 2.885e-08 ***
MODEL
                4 7936.7 1984.18
RESIDUALS
               14 531.0
                          37.93
CORRECTED TOTAL 18 8467.8
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
CATTLE 1 6582.1 6582.1 173.5265 2.801e-09 ***
CALVES 1 186.7
                 186.7
                         4.9213 0.0435698 *
HOGS
       1 489.9
                 489.9 12.9145 0.0029351 **
SHEEP
       1 678.1
                 678.1 17.8773 0.0008431 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
CATTLE 1 2200.71 2200.71 58.0183 2.413e-06 ***
CALVES 1 136.08 136.08 3.5876 0.0790616 .
HOGS
       1 113.66 113.66 2.9964 0.1054198
       1 678.11 678.11 17.8773 0.0008431 ***
SHEEP
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
CATTLE 1 2200.71 2200.71 58.0183 2.413e-06 ***
CALVES 1 136.08 136.08 3.5876 0.0790616 .
       1 113.66 113.66 2.9964 0.1054198
HOGS
SHEEP
       1 678.11 678.11 17.8773 0.0008431 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(19) MODEL
ANOVA(COST ~ CATTLE + CALVES + SHEEP, p12)
```

p12 = read.table("C:/G/Rt/SAS4lm/p12.txt", head=TRUE)

Pr(>F)

Df Sum Sq Mean Sq F value

\$ANOVA

Response : COST

```
MODEL
                3 7823.1 2607.69 60.673 1.281e-08 ***
RESIDUALS
               15 644.7
                          42.98
CORRECTED TOTAL 18 8467.8
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value Pr(>F)
CATTLE 1 6582.1 6582.1 153.1443 2.835e-09 ***
CALVES 1 186.7
                 186.7
                         4.3432 0.0546701 .
SHEEP
      1 1054.3 1054.3 24.5306 0.0001735 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
      Df Sum Sq Mean Sq F value
                                 Pr(>F)
CATTLE 1 2519.8 2519.8 58.6265 1.471e-06 ***
CALVES 1 260.6
                 260.6 6.0634 0.0263909 *
SHEEP 1 1054.3 1054.3 24.5306 0.0001735 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value
                                 Pr(>F)
CATTLE 1 2519.8 2519.8 58.6265 1.471e-06 ***
CALVES 1 260.6
                 260.6 6.0634 0.0263909 *
SHEEP 1 1054.3 1054.3 24.5306 0.0001735 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(20) MODEL
ANOVA(COST ~ CATTLE + CALVES + offset(1*HOGS) + SHEEP, p12)
$ANOVA
Response : COST
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
                3 7823.1 2607.69 60.673 1.281e-08 ***
MODEL
RESIDUALS
               15 644.7
                          42.98
CORRECTED TOTAL 18 8467.8
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
CATTLE 1 6582.1 6582.1 153.1443 2.835e-09 ***
CALVES 1 186.7 186.7 4.3432 0.0546701 .
```

```
SHEEP
       1 1054.3 1054.3 24.5306 0.0001735 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
      Df Sum Sq Mean Sq F value
CATTLE 1 2519.8 2519.8 58.6265 1.471e-06 ***
                  260.6 6.0634 0.0263909 *
CALVES 1 260.6
SHEEP
      1 1054.3 1054.3 24.5306 0.0001735 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value
CATTLE 1 2519.8 2519.8 58.6265 1.471e-06 ***
CALVES 1 260.6
                260.6 6.0634 0.0263909 *
SHEEP
       1 1054.3 1054.3 24.5306 0.0001735 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(21) MODEL
ANOVA(COST ~ CATTLE + CALVES + I(HOGS + SHEEP), p12)
$ANOVA
Response : COST
               Df Sum Sq Mean Sq F value
                3 7936.7 2645.6 74.726 3.011e-09 ***
MODEL
RESIDUALS
               15 531.1
                            35.4
CORRECTED TOTAL 18 8467.8
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
CATTLE
                1 6582.1 6582.1 185.9151 7.406e-10 ***
CALVES
                1 186.7
                          186.7
                                  5.2726
                                           0.03649 *
I(HOGS + SHEEP) 1 1168.0 1168.0 32.9896 3.883e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
               Df Sum Sq Mean Sq F value
CATTLE
                1 2215.48 2215.48 62.5775 9.887e-07 ***
CALVES
                1 155.03 155.03 4.3788
                                            0.0538 .
I(HOGS + SHEEP) 1 1167.96 1167.96 32.9896 3.883e-05 ***
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
               Df Sum Sq Mean Sq F value
                                             Pr(>F)
                1 2215.48 2215.48 62.5775 9.887e-07 ***
CATTLE
CALVES
                1 155.03 155.03 4.3788
                                             0.0538 .
I(HOGS + SHEEP) 1 1167.96 1167.96 32.9896 3.883e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(22) MODEL
REG(COST ~ CATTLE + CALVES + I(HOGS + SHEEP) - 1, p12)
               Estimate Std. Error Df t value Pr(>|t|)
CATTLE
                 3.3000
                          0.38314 16 8.6131 2.100e-07 ***
CALVES
                 1.9672
                           0.59108 16 3.3281 0.004259 **
I(HOGS + SHEEP)
                 0.8068
                           0.13800 16 5.8466 2.479e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.2 Chapter 3
5.2.1 p63
(23) MODEL
p63w = read.table("C:/G/Rt/SAS4lm/p63.txt", header=TRUE)
p631 = reshape(p63w,
       direction = "long",
       varying = list(names(p63w)[2:9]),
       v.names = "fruitwt",
       idvar = c("irrig"),
       timevar = "bloc",
       times = 1:8)
p631 = af(p631, c("bloc"))
ANOVA(fruitwt ~ bloc + irrig, p631) # p64
$ANOVA
Response : fruitwt
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
               11 445334
                           40485
                                   12.04 6.643e-08 ***
                            3362
RESIDUALS
               28 94147
CORRECTED TOTAL 39 539481
```

```
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
$`Type I`
     Df Sum Sq Mean Sq F value
      7 401308 57330 17.0503 1.452e-08 ***
irrig 4 44026 11006 3.2734
                                0.02539 *
Signif. codes: 0 '*** 0.001 '** 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
bloc 7 401308 57330 17.0503 1.452e-08 ***
irrig 4 44026 11006 3.2734
                                0.02539 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
      7 401308 57330 17.0503 1.452e-08 ***
bloc
irrig 4 44026 11006 3.2734
                                0.02539 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.2.2 p72
(24) MODEL
p72 = read.table("C:/G/Rt/SAS4lm/p72.txt", header=TRUE)
p72 = af(p72, c("run", "pos", "mat"))
ANOVA(wtloss ~ run + pos + mat, p72) # p73
$ANOVA
Response : wtloss
               Df Sum Sq Mean Sq F value
MODEL
                9 7076.5 786.28 12.837 0.002828 **
RESIDUALS
                6 367.5
                          61.25
CORRECTED TOTAL 15 7444.0
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
run 3 986.5 328.83 5.3687 0.0390130 *
pos 3 1468.5 489.50 7.9918 0.0161685 *
mat 3 4621.5 1540.50 25.1510 0.0008498 ***
```

```
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
run 3 986.5 328.83 5.3687 0.0390130 *
pos 3 1468.5 489.50 7.9918 0.0161685 *
mat 3 4621.5 1540.50 25.1510 0.0008498 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
run 3 986.5 328.83 5.3687 0.0390130 *
pos 3 1468.5 489.50 7.9918 0.0161685 *
mat 3 4621.5 1540.50 25.1510 0.0008498 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
ANOVA(shrink ~ run + pos + mat, p72) # p73
$ANOVA
Response : shrink
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                9 265.75 29.528 9.8426 0.005775 **
RESIDUALS
                6 18.00
                          3.000
CORRECTED TOTAL 15 283.75
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
run 3 33.25 11.083 3.6944 0.081254 .
pos 3 60.25 20.083 6.6944 0.024212 *
mat 3 172.25 57.417 19.1389 0.001786 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                              Pr(>F)
run 3 33.25 11.083 3.6944 0.081254 .
pos 3 60.25 20.083 6.6944 0.024212 *
mat 3 172.25 57.417 19.1389 0.001786 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
```

```
run 3 33.25 11.083 3.6944 0.081254 .
pos 3 60.25 20.083 6.6944 0.024212 *
mat 3 172.25 57.417 19.1389 0.001786 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.2.3 p75
(25) MODEL
p75w = read.table("C:/G/Rt/SAS4lm/p75.txt", header=TRUE)
p751 = reshape(p75w,
       direction = "long",
       varying = list(names(p75w)[4:9]),
       v.names = "Y",
       idvar = c("method", "variety", "trt"),
       timevar = "yield",
       times = 1:6)
p751 = af(p751, c("variety", "yield"))
ANOVA(Y ~ method*variety, p751) # p78
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               14 1339.0 95.645 4.8674 2.723e-06 ***
               75 1473.8 19.650
RESIDUALS
CORRECTED TOTAL 89 2812.8
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
              Df Sum Sq Mean Sq F value
                                           Pr(>F)
               2 953.16 476.58 24.2531 7.525e-09 ***
method
variety
               4 11.38
                           2.85 0.1448
                                          0.96476
method:variety 8 374.49
                          46.81 2.3822
                                          0.02409 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
              Df Sum Sq Mean Sq F value
                                           Pr(>F)
               2 953.16 476.58 24.2531 7.525e-09 ***
method
               4 11.38
                           2.85 0.1448
variety
                                          0.96476
method:variety 8 374.49
                          46.81 2.3822
                                          0.02409 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$`Type III`
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
                2 953.16 476.58 24.2531 7.525e-09 ***
method
                4 11.38
                           2.85 0.1448
                                           0.96476
variety
                           46.81 2.3822
method:variety 8 374.49
                                           0.02409 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
5.3 Chapter 4
5.3.1 p94
(26) MODEL
p94w = read.table("C:/G/Rt/SAS4lm/p94.txt", head=TRUE)
p941 = reshape(p94w,
       direction = "long",
       varying = list(names(p94w)[3:8]),
       v.names = "ct",
       idvar = c("package"),
       timevar = "sample",
       times = 1:6)
p941\$sampleA = floor((p941\$sample + 1)/2)
p941\$sampleB = 2 - (p941\$sample) %% 2
p941\$logct = log10(p941\$ct)
p941 = af(p941, c("sample", "sampleA", "sampleB", "package"))
ANOVA(logct ~ package + sampleA %in% package, p941) # p97
$ANOVA
Response : logct
                 Df Sum Sq Mean Sq F value
                                              Pr(>F)
MODEL
                 59 50.463 0.85531 22.229 < 2.2e-16 ***
                 60 2.309 0.03848
RESIDUALS
CORRECTED TOTAL 119 52.772
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
                Df Sum Sq Mean Sq F value
                                             Pr(>F)
                19 30.529 1.60680 41.760 < 2.2e-16 ***
package
package:sampleA 40 19.934 0.49836 12.952 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
                Df Sum Sq Mean Sq F value
                                             Pr(>F)
```

```
19 30.529 1.60680 41.760 < 2.2e-16 ***
package
package:sampleA 40 19.934 0.49836 12.952 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
               Df Sum Sq Mean Sq F value
package
               19 30.529 1.60680 41.760 < 2.2e-16 ***
package:sampleA 40 19.934 0.49836 12.952 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.3.2 p116
(27) MODEL
ANOVA(Y ~ method + variety + method:variety, p751) # p116
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               14 1339.0 95.645 4.8674 2.723e-06 ***
RESIDUALS
               75 1473.8 19.650
CORRECTED TOTAL 89 2812.8
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
              Df Sum Sq Mean Sq F value
                                          Pr(>F)
               2 953.16 476.58 24.2531 7.525e-09 ***
method
               4 11.38
                           2.85 0.1448
                                         0.96476
variety
method:variety 8 374.49
                          46.81 2.3822
                                         0.02409 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
              Df Sum Sq Mean Sq F value
                                          Pr(>F)
               2 953.16 476.58 24.2531 7.525e-09 ***
method
               4 11.38
                           2.85 0.1448
                                         0.96476
variety
method:variety 8 374.49
                          46.81 2.3822
                                         0.02409 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
              Df Sum Sq Mean Sq F value
                                          Pr(>F)
               2 953.16 476.58 24.2531 7.525e-09 ***
method
```

```
4 11.38 2.85 0.1448 0.96476
variety
                         46.81 2.3822 0.02409 *
method:variety 8 374.49
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.3.3 p122
(28) MODEL
p122 = read.table("C:/G/Rt/SAS4lm/p122.txt", header=TRUE)
p122 = af(p122, c("et", "wafer", "pos"))
ANOVA(resista ~ et + wafer %in% et + pos + et:pos, p122)
$ANOVA
Response : resista
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               23 9.3250 0.40544 3.6477 0.001263 **
RESIDUALS
               24 2.6676 0.11115
CORRECTED TOTAL 47 11.9926
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value
                                    Pr(>F)
         3 3.1122 1.03739 9.3333 0.0002851 ***
et
et:wafer 8 4.2745 0.53431 4.8071 0.0012742 **
         3 1.1289 0.37630 3.3855 0.0345139 *
         9 0.8095 0.08994 0.8092 0.6125279
et:pos
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value
                                    Pr(>F)
         3 3.1122 1.03739 9.3333 0.0002851 ***
et:wafer 8 4.2745 0.53431 4.8071 0.0012742 **
pos
         3 1.1289 0.37630 3.3855 0.0345139 *
         9 0.8095 0.08994 0.8092 0.6125279
et:pos
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
        Df Sum Sq Mean Sq F value
                                    Pr(>F)
         3 3.1122 1.03739 9.3333 0.0002851 ***
et:wafer 8 4.2745 0.53431 4.8071 0.0012742 **
         3 1.1289 0.37630 3.3855 0.0345139 *
pos
```

9 0.8095 0.08994 0.8092 0.6125279

et:pos

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.3.4 p136
(29) MODEL
p136 = read.table("C:/G/Rt/SAS4lm/p136.txt", header=TRUE)
p136 = af(p136, "rep")
ANOVA(drywt ~ rep + cult + rep:cult + inoc + cult:inoc, p136)
$ANOVA
Response : drywt
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
                                   20.26 4.594e-06 ***
MODEL
               11 157.208 14.2917
RESIDUALS
               12
                    8.465 0.7054
CORRECTED TOTAL 23 165.673
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
                     8.440 11.9646 0.0006428 ***
          3 25.320
rep
          1 2.407
                     2.407 3.4117 0.0895283 .
cult
                    3.160 4.4796 0.0249095 *
rep:cult
          3 9.480
          2 118.176 59.088 83.7631 8.919e-08 ***
                     0.913 1.2942 0.3097837
cult:inoc 2
              1.826
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          3 25.320
                     8.440 11.9646 0.0006428 ***
rep
cult
              2.407
                      2.407 3.4117 0.0895283 .
rep:cult
          3 9.480
                     3.160 4.4796 0.0249095 *
inoc
          2 118.176 59.088 83.7631 8.919e-08 ***
cult:inoc 2 1.826
                     0.913 1.2942 0.3097837
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
rep
          3 25.320
                     8.440 11.9646 0.0006428 ***
              2.407
                      2.407 3.4117 0.0895283 .
cult
          1
rep:cult
          3
              9.480
                     3.160 4.4796 0.0249095 *
```

2 118.176 59.088 83.7631 8.919e-08 ***

inoc

```
cult:inoc 2 1.826 0.913 1.2942 0.3097837
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.4 Chapter 5
5.4.1 p142
(30) MODEL
p142 = read.table("C:/G/Rt/SAS4lm/p142.txt", header=TRUE, na.strings=".")
p142 = af(p142, c("STUDY", "PATIENT"))
ANOVA(FLUSH ~ STUDY + TRT, p142) # Incomplete data, 56 lines are truncated.
$ANOVA
Response : FLUSH
               Df Sum Sq Mean Sq F value Pr(>F)
                5 3619.9 723.98
                                  2.392 0.04607 *
MODEL
               71 21489.2 302.67
RESIDUALS
CORRECTED TOTAL 76 25109.1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value Pr(>F)
STUDY 4 3553.9 888.46 2.9355 0.02638 *
                66.04 0.2182 0.64185
      1 66.0
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value Pr(>F)
STUDY 4 3599.4 899.85 2.9731 0.02496 *
TRT
      1 66.0
                66.04 0.2182 0.64185
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value Pr(>F)
STUDY 4 3599.4 899.85 2.9731 0.02496 *
      1 66.0
               66.04 0.2182 0.64185
TRT
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

(31) MODEL

ANOVA(FLUSH ~ TRT + STUDY + TRT:STUDY, p142) # Different data

```
$ANOVA
Response : FLUSH
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                9 4093.7 454.86 1.4501 0.1851
               67 21015.4 313.66
RESIDUALS
CORRECTED TOTAL 76 25109.1
$`Type I`
         Df Sum Sq Mean Sq F value Pr(>F)
                    20.49 0.0653 0.79906
TRT
              20.5
STUDY
          4 3599.4 899.85 2.8688 0.02956 *
TRT:STUDY 4 473.8 118.45 0.3776 0.82383
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
         Df Sum Sq Mean Sq F value Pr(>F)
          1 66.0
                    66.04 0.2105 0.64783
          4 3599.4 899.85 2.8688 0.02956 *
STUDY
TRT:STUDY 4 473.8 118.45 0.3776 0.82383
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value Pr(>F)
TRT
               1.9
                      1.93 0.0062 0.9377
          4 3339.4 834.85 2.6616 0.0400 *
STUDY
TRT:STUDY 4 473.8 118.45 0.3776 0.8238
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.5 Chapter 6
5.5.1 p171
(32) MODEL
p171 = read.table("C:/G/Rt/SAS4lm/p171.txt", header=TRUE)
ANOVA(score2 ~ teach, p171) # p173 Output 6.2, p174 Output 6.5
```

Df Sum Sq Mean Sq F value Pr(>F)

\$ANOVA

Response : score2

```
MODEL
                2 49.74 24.868 0.5598 0.5776
RESIDUALS
               28 1243.94 44.426
CORRECTED TOTAL 30 1293.68
$`Type I`
     Df Sum Sq Mean Sq F value Pr(>F)
teach 2 49.736 24.868 0.5598 0.5776
$`Type II`
     Df Sum Sq Mean Sq F value Pr(>F)
teach 2 49.736 24.868 0.5598 0.5776
$`Type III`
     Df Sum Sq Mean Sq F value Pr(>F)
teach 2 49.736 24.868 0.5598 0.5776
5.5.2 p188
(33) MODEL
p188 = read.table("C:/G/Rt/SAS4lm/p188.txt", header=TRUE)
p188 = af(p188, c("a", "b"))
ANOVA(y ~ a + b + a:b, p188) # p189
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                5 63.711 12.7422 5.866 0.005724 **
MODEL
RESIDUALS
               12 26.067 2.1722
CORRECTED TOTAL 17 89.778
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 7.803 7.8028 3.5921 0.082395 .
    2 20.492 10.2459 4.7168 0.030798 *
a:b 2 35.416 17.7082 8.1521 0.005807 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                              Pr(>F)
   1 15.850 15.850 7.2968 0.019265 *
    2 20.492 10.246 4.7168 0.030798 *
a:b 2 35.416 17.708 8.1521 0.005807 **
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 9.641 9.6407 4.4382 0.056865 .
    2 30.866 15.4330 7.1047 0.009212 **
a:b 2 35.416 17.7082 8.1521 0.005807 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.5.3 p203
(34) MODEL
ANOVA(y \sim a + b + a:b, p188[-8,])
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               4 45.816 11.4539 5.2729 0.01097 *
RESIDUALS
               12 26.067 2.1722
CORRECTED TOTAL 16 71.882
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
   1 2.9252 2.9252 1.3466 0.268432
    2 13.3224 6.6612 3.0665 0.083997 .
a:b 1 29.5681 29.5681 13.6119 0.003095 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
   1 5.5652 5.5652 2.5620 0.135442
    2 13.3224 6.6612 3.0665 0.083997 .
a:b 1 29.5681 29.5681 13.6119 0.003095 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 0.3507 0.3507 0.1615 0.694881
a
    2 16.0733 8.0367 3.6997 0.056021 .
```

```
a:b 1 29.5681 29.5681 13.6119 0.003095 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.5.4 p215
(35) MODEL
p215 = read.table("C:/G/Rt/SAS4lm/p215.txt", header=TRUE)
p215 = af(p215, c("irrig", "reps"))
ANOVA(yield ~ irrig/reps + cult + irrig:cult, p215) # p216 Book is wrong.
$ANOVA
Response : yield
               Df Sum Sq Mean Sq F value Pr(>F)
               11 67.662 6.1511 0.6253 0.7636
MODEL
RESIDUALS
                6 59.023 9.8372
CORRECTED TOTAL 17 126.685
$`Type I`
          Df Sum Sq Mean Sq F value Pr(>F)
irrig
           2 7.320 3.6600 0.3721 0.7042
irrig:reps 6 59.870 9.9783 1.0143 0.4933
           1 0.467 0.4672 0.0475 0.8347
irrig:cult 2 0.004 0.0022 0.0002 0.9998
$`Type II`
          Df Sum Sq Mean Sq F value Pr(>F)
           2 7.320 3.6600 0.3721 0.7042
irrig
irrig:reps 6 59.870 9.9783 1.0143 0.4933
cult
           1 0.467 0.4672 0.0475 0.8347
irrig:cult 2 0.004 0.0022 0.0002 0.9998
$`Type III`
          Df Sum Sq Mean Sq F value Pr(>F)
irrig
           2 7.320 3.6600 0.3721 0.7042
irrig:reps 6 59.870 9.9783 1.0143 0.4933
           1 0.467 0.4672 0.0475 0.8347
irrig:cult 2 0.004 0.0022 0.0002 0.9998
# Compare with SAS output
```

(36) MODEL

```
ANOVA(yield ~ reps + irrig + reps:irrig + cult + cult:irrig, p215)
$ANOVA
Response : yield
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               11 67.662 6.1511 0.6253 0.7636
RESIDUALS
                6 59.023 9.8372
CORRECTED TOTAL 17 126.685
$`Type I`
          Df Sum Sq Mean Sq F value Pr(>F)
reps
           2 49.703 24.8517 2.5263 0.1600
           2 7.320 3.6600 0.3721 0.7042
irrig
reps:irrig 4 10.167 2.5417 0.2584 0.8944
cult
           1 0.467 0.4672 0.0475 0.8347
irrig:cult 2 0.004 0.0022 0.0002 0.9998
$`Type II`
          Df Sum Sq Mean Sq F value Pr(>F)
           2 49.703 24.8517 2.5263 0.1600
reps
           2 7.320 3.6600 0.3721 0.7042
irrig
reps:irrig 4 10.167 2.5417 0.2584 0.8944
cult
           1 0.467 0.4672 0.0475 0.8347
irrig:cult 2 0.004 0.0022 0.0002 0.9998
$`Type III`
          Df Sum Sq Mean Sq F value Pr(>F)
           2 49.703 24.8517 2.5263 0.1600
reps
           2 7.320 3.6600 0.3721 0.7042
irrig
reps:irrig 4 10.167 2.5417 0.2584 0.8944
           1 0.467 0.4672 0.0475 0.8347
cult
irrig:cult 2 0.004 0.0022 0.0002 0.9998
5.6 Chapter 7
5.6.1 p232
(37) MODEL
p232 = read.table("C:/G/Rt/SAS4lm/p232.txt", header=TRUE)
p232 = af(p232, c("trt", "rep"))
ANOVA(final ~ trt + initial, p232) # p233
```

\$ANOVA

Response : final

```
Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
                5 354.45 70.889 235.05 5.493e-13 ***
                          0.302
RESIDUALS
               14
                    4.22
CORRECTED TOTAL 19 358.67
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value
        4 198.41 49.602 164.47 1.340e-11 ***
trt
initial 1 156.04 156.040 517.38 1.867e-12 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
        4 12.089
                    3.022 10.021 0.0004819 ***
initial 1 156.040 156.040 517.384 1.867e-12 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value
        4 12.089 3.022 10.021 0.0004819 ***
initial 1 156.040 156.040 517.384 1.867e-12 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.6.2 p240
(38) MODEL
ANOVA(final ~ initial + trt + trt:initial, p232) # p240
$ANOVA
Response : final
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
                9 355.84 39.537 139.51 2.572e-09 ***
MODEL
RESIDUALS
               10
                    2.83
                          0.283
CORRECTED TOTAL 19 358.67
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
           Df Sum Sq Mean Sq F value
                                         Pr(>F)
```

1 342.36 342.36 1208.0336 9.211e-12 ***

initial

```
4 12.09
                       3.02
                             10.6645 0.001247 **
trt
initial:trt 4 1.39
                       0.35
                            1.2247 0.360175
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
           Df Sum Sq Mean Sq F value
initial
            1 156.040 156.040 550.5987 4.478e-10 ***
            4 12.089
                       3.022 10.6645 0.001247 **
               1.388
initial:trt 4
                       0.347
                               1.2247 0.360175
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
           Df Sum Sq Mean Sq F value
                                        Pr(>F)
            1 68.529 68.529 241.8091 2.472e-08 ***
initial
trt
            4 1.696
                      0.424
                              1.4963
                                        0.2752
initial:trt 4 1.388
                      0.347
                              1.2247
                                        0.3602
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.6.3 p241
(39) MODEL
p241 = read.table("C:/G/Rt/SAS4lm/p241.txt", header=TRUE)
p241 = af(p241, c("STORE", "DAY"))
ANOVA(Q1 ~ P1 + DAY + P1:DAY, p241) # p242
$ANOVA
Response: Q1
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               11 1111.52 101.048  4.6445  0.0008119 ***
RESIDUALS
               24 522.15 21.756
CORRECTED TOTAL 35 1633.68
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
       1 516.59 516.59 23.7444 5.739e-05 ***
Ρ1
DAY
       5 430.54 86.11 3.9578 0.009275 **
P1:DAY 5 164.39
                  32.88 1.5112 0.223566
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$`Type II`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
       1 696.73 696.73 32.0243 7.925e-06 ***
Ρ1
       5 430.54
                  86.11 3.9578 0.009275 **
DAY
P1:DAY 5 164.39
                  32.88 1.5112 0.223566
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
       1 554.79 554.79 25.4999 3.665e-05 ***
P1
       5 201.17
                 40.23 1.8493
                                  0.1412
DAY
P1:DAY 5 164.39
                  32.88 1.5112
                                  0.2236
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.6.4 p243
(40) MODEL
ANOVA(Q1 \sim DAY + DAY:P1, p241)
$ANOVA
Response : Q1
               Df Sum Sq Mean Sq F value Pr(>F)
               11 1111.52 101.048 4.6445 0.0008119 ***
MODEL
RESIDUALS
               24 522.15 21.756
CORRECTED TOTAL 35 1633.68
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
       5 250.40 50.079 2.3018 0.0764717 .
DAY:P1 6 861.13 143.521 6.5967 0.0003239 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
       5 250.40 50.079 2.3018 0.0764717 .
DAY:P1 6 861.13 143.521 6.5967 0.0003239 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
```

```
Df Sum Sq Mean Sq F value
                                  Pr(>F)
      5 201.17 40.234 1.8493 0.1411648
DAY
DAY:P1 6 861.13 143.521 6.5967 0.0003239 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
REG(Q1 ~ DAY + DAY:P1 - 1, p241) # Ouput 7.10
       Estimate Std. Error Df t value Pr(>|t|)
DAY1
         18.675
                   14.4110 24 1.2959 0.2073286
                   15.1094 24 2.5472 0.0176863 *
DAY2
         38.487
DAY3
         45.330
                 26.1576 24 1.7329 0.0959384 .
         49.149
DAY4
                  16.6092 24 2.9592 0.0068366 **
         77.899 27.5007 24 2.8326 0.0092034 **
DAY5
DAY6
         73.273 13.4837 24 5.4341 1.39e-05 ***
                  0.2915 24 -0.7562 0.4568599
DAY1:P1
         -0.220
                   0.2978 24 -2.0940 0.0470031 *
DAY2:P1
         -0.624
                  0.5049 24 -1.2102 0.2379998
DAY3:P1
         -0.611
                  0.3193 24 -2.4914 0.0200350 *
DAY4:P1
         -0.796
DAY5:P1
         -1.196
                    0.5049 24 -2.3683 0.0262648 *
DAY6:P1 -1.225
                    0.2652 24 -4.6199 0.0001092 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
(41) MODEL
ANOVA(Q1 \sim P1 + DAY + P1:DAY, p241)
$ANOVA
Response : Q1
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
               11 1111.52 101.048  4.6445  0.0008119 ***
               24 522.15 21.756
RESIDUALS
CORRECTED TOTAL 35 1633.68
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
Ρ1
       1 516.59 516.59 23.7444 5.739e-05 ***
       5 430.54
                  86.11 3.9578 0.009275 **
DAY
P1:DAY 5 164.39
                  32.88 1.5112 0.223566
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
```

```
Df Sum Sq Mean Sq F value
                                  Pr(>F)
      1 696.73 696.73 32.0243 7.925e-06 ***
Ρ1
       5 430.54
                 86.11 3.9578 0.009275 **
DAY
P1:DAY 5 164.39
                 32.88 1.5112 0.223566
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
       1 554.79 554.79 25.4999 3.665e-05 ***
Ρ1
       5 201.17
                 40.23 1.8493
DAY
                                  0.1412
P1:DAY 5 164.39
                 32.88 1.5112
                                  0.2236
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(42) MODEL
ANOVA(Q1 \sim STORE + DAY + P1 + P2, p241)
$ANOVA
Response: Q1
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
               12 1225.37 102.114 5.7521 0.0001688 ***
MODEL
RESIDUALS
               23 408.31 17.753
CORRECTED TOTAL 35 1633.68
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value
                                Pr(>F)
STORE 5 313.42 62.68 3.5310
                                0.01629 *
DAY
      5 250.40 50.08 2.8210
                                0.03957 *
Ρ1
      1 622.01 622.01 35.0377 4.924e-06 ***
P2
      1 39.54 39.54 2.2274
                                0.14917
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
STORE 5 223.83 44.77 2.5217 0.058346 .
DAY
      5 433.10 86.62 4.8793 0.003456 **
Ρ1
      1 538.17 538.17 30.3150 1.342e-05 ***
P2
      1 39.54
               39.54 2.2274 0.149171
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
```

```
Df Sum Sq Mean Sq F value
                                  Pr(>F)
STORE 5 223.83
                44.77 2.5217 0.058346 .
                 86.62 4.8793 0.003456 **
DAY
      5 433.10
P1
      1 538.17 538.17 30.3150 1.342e-05 ***
P2
      1 39.54
                 39.54 2.2274 0.149171
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
5.6.5 p250
(43) MODEL
p250 = read.table("C:/G/Rt/SAS4lm/p250.txt", header=TRUE)
p250 = af(p250, c("variety", "spacing", "plant"))
ANOVA(lint ~ bollwt + variety + spacing + variety:spacing + variety:spacing:plant,
    p250) # p252 Output 7.18, Parameter is different due to different order
$ANOVA
Response : lint
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
                8 31.160 3.8950 80.704 < 2.2e-16 ***
MODEL
RESIDUALS
               40 1.931 0.0483
CORRECTED TOTAL 48 33.091
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
                     Df Sum Sq Mean Sq F value
                      1 29.0693 29.0693 602.3107 < 2.2e-16 ***
bollwt
                      1 1.2635 1.2635 26.1802 8.158e-06 ***
variety
                      1 0.4666 0.4666
                                        9.6689 0.003447 **
spacing
                      1 0.0933 0.0933 1.9325 0.172169
variety:spacing
variety:spacing:plant 4 0.2673 0.0668 1.3847 0.256548
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
                     Df Sum Sq Mean Sq F value
                                                   Pr(>F)
                      1 11.1186 11.1186 230.3745 < 2.2e-16 ***
bollwt
                      1 1.1973 1.1973 24.8084 1.259e-05 ***
variety
                      1 0.4666 0.4666
                                        9.6689 0.003447 **
spacing
                      1 0.0933 0.0933 1.9325 0.172169
variety:spacing
variety:spacing:plant 4 0.2673 0.0668
                                        1.3847 0.256548
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$`Type III`
                    Df Sum Sq Mean Sq F value
                                                 Pr(>F)
                     1 11.1186 11.1186 230.3745 < 2.2e-16 ***
bollwt
                     1 0.9424 0.9424 19.5269 7.379e-05 ***
variety
                     1 0.3748 0.3748 7.7666 0.008101 **
spacing
                     1 0.0479 0.0479 0.9915 0.325350
variety:spacing
variety:spacing:plant 4 0.2673 0.0668 1.3847 0.256548
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.6.6 p254 Output 7.20
(44) MODEL
ANOVA(lint ~ bollwt + variety + spacing, p250)
$ANOVA
Response : lint
               Df Sum Sq Mean Sq F value
                3 30.799 10.2665 201.65 < 2.2e-16 ***
MODEL
RESIDUALS
               45 2.291 0.0509
CORRECTED TOTAL 48 33.091
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value
bollwt 1 29.0693 29.0693 570.9531 < 2.2e-16 ***
variety 1 1.2635 1.2635 24.8172 9.777e-06 ***
                         9.1655 0.004072 **
spacing 1 0.4666 0.4666
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
bollwt
      1 11.5717 11.5717 227.2815 < 2.2e-16 ***
variety 1 1.1973 1.1973 23.5168 1.516e-05 ***
spacing 1 0.4666 0.4666
                         9.1655 0.004072 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value
       1 11.5717 11.5717 227.2815 < 2.2e-16 ***
variety 1 1.1973 1.1973 23.5168 1.516e-05 ***
spacing 1 0.4666 0.4666
                         9.1655 0.004072 **
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.6.7 p256
(45) MODEL
p256 = read.table("C:/G/Rt/SAS4lm/p256.txt", header=TRUE)
p256b = af(p256, c("bloc", "type", "logdose"))
ANOVA(y ~ bloc + type + logdose + type:logdose, p256b) # p258 Output 7.22
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                8 816.50 102.063 6.0641 0.0014 **
MODEL
               15 252.46 16.831
RESIDUALS
CORRECTED TOTAL 23 1068.96
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
            Df Sum Sq Mean Sq F value
                                        Pr(>F)
             3 538.79 179.597 10.6709 0.0005223 ***
bloc
             1 12.04 12.042 0.7155 0.4109264
type
             2 121.58 60.792 3.6120 0.0524231 .
logdose
type:logdose 2 144.08 72.042 4.2804 0.0338265 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
            Df Sum Sq Mean Sq F value
                                        Pr(>F)
             3 538.79 179.597 10.6709 0.0005223 ***
bloc
             1 12.04 12.042 0.7155 0.4109264
type
             2 121.58 60.792 3.6120 0.0524231 .
logdose
type:logdose 2 144.08 72.042 4.2804 0.0338265 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
            Df Sum Sq Mean Sq F value
                                        Pr(>F)
             3 538.79 179.597 10.6709 0.0005223 ***
bloc
             1 12.04 12.042 0.7155 0.4109264
type
             2 121.58 60.792 3.6120 0.0524231 .
logdose
type:logdose 2 144.08 72.042 4.2804 0.0338265 *
```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

5.6.8 p261 Output 7.27

(46) MODEL

```
p256 = af(p256, c("bloc", "type"))
p256\$logd2 = (p256\$logdose)^2
ANOVA(y ~ bloc + type + logdose + logd2 + type:logdose + type:logd2, p256)
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                8 816.50 102.063 6.0641 0.0014 **
RESIDUALS
               15 252.46 16.831
CORRECTED TOTAL 23 1068.96
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
            Df Sum Sq Mean Sq F value
                                         Pr(>F)
             3 538.79 179.597 10.6709 0.0005223 ***
bloc
             1 12.04 12.042 0.7155 0.4109264
type
             1 115.56 115.562 6.8662 0.0193005 *
logdose
                        6.021 0.3577 0.5586917
logd2
                 6.02
type:logdose 1 138.06 138.062 8.2031 0.0118242 *
                        6.021 0.3577 0.5586917
                 6.02
type:logd2
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
            Df Sum Sq Mean Sq F value
                                         Pr(>F)
             3 538.79 179.597 10.6709 0.0005223 ***
bloc
             1 12.04 12.042 0.7155 0.4109264
type
             1 0.39 0.389 0.0231 0.8811262
logdose
logd2
             1
                 6.02
                        6.021 0.3577 0.5586917
                        0.812 0.0483 0.8290541
                 0.81
type:logdose
             1
                 6.02
                        6.021 0.3577 0.5586917
type:logd2
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
            Df Sum Sq Mean Sq F value
                                         Pr(>F)
bloc
             3 538.79 179.597 10.6709 0.0005223 ***
             1 28.12 28.125 1.6711 0.2156736
type
                 0.39
                        0.389 0.0231 0.8811262
logdose
             1
                 6.02
                        6.021 0.3577 0.5586917
logd2
             1
                        0.812 0.0483 0.8290541
type:logdose 1
                 0.81
type:logd2
                 6.02
                        6.021 0.3577 0.5586917
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.6.9 p262 Output 7.28
(47) MODEL
ANOVA(y ~ bloc + type + type:logdose, p256b)
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                8 816.50 102.063 6.0641 0.0014 **
MODEL
               15 252.46 16.831
RESIDUALS
CORRECTED TOTAL 23 1068.96
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
            Df Sum Sq Mean Sq F value
                                        Pr(>F)
             3 538.79 179.597 10.6709 0.0005223 ***
bloc
             1 12.04 12.042 0.7155 0.4109264
type
type:logdose 4 265.67 66.417 3.9462 0.0220552 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
            Df Sum Sq Mean Sq F value
                                        Pr(>F)
             3 538.79 179.597 10.6709 0.0005223 ***
bloc
             1 12.04 12.042 0.7155 0.4109264
type
type:logdose 4 265.67 66.417 3.9462 0.0220552 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
            Df Sum Sq Mean Sq F value
             3 538.79 179.597 10.6709 0.0005223 ***
bloc
             1 12.04 12.042 0.7155 0.4109264
type
type:logdose 4 265.67 66.417 3.9462 0.0220552 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

5.7 Chapter 8

5.7.1 p269

(48) MODEL

```
p269 = read.csv("C:/G/Rt/SAS4lm/fev1uni.csv")
p269 = af(p269, c("drug", "hour", "patient"))
ANOVA(fev1 ~ drug + patient %in% drug + hour + drug:hour, p269) # p271 Output 8.3
$ANOVA
Response : fev1
                Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
                92 296.65 3.2244 51.078 < 2.2e-16 ***
RESIDUALS
               483 30.49 0.0631
CORRECTED TOTAL 575 327.14
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
            Df Sum Sq Mean Sq F value
                                         Pr(>F)
             2 25.783 12.8913 204.212 < 2.2e-16 ***
drug:patient 69 247.412 3.5857 56.801 < 2.2e-16 ***
             7 17.170 2.4529 38.857 < 2.2e-16 ***
drug:hour
            14
                 6.280 0.4486
                                7.106 1.923e-13 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
            Df Sum Sq Mean Sq F value
                                         Pr(>F)
             2 25.783 12.8913 204.212 < 2.2e-16 ***
drug:patient 69 247.412 3.5857 56.801 < 2.2e-16 ***
             7 17.170 2.4529 38.857 < 2.2e-16 ***
hour
                6.280 0.4486
                                7.106 1.923e-13 ***
drug:hour
            14
___
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
            Df Sum Sq Mean Sq F value
                                         Pr(>F)
             2 25.783 12.8913 204.212 < 2.2e-16 ***
drug:patient 69 247.412 3.5857 56.801 < 2.2e-16 ***
             7 17.170 2.4529 38.857 < 2.2e-16 ***
hour
drug:hour
            14
                 6.280 0.4486
                               7.106 1.923e-13 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.8 Chapter 11
```

5.8.1 p390

(49) MODEL

```
p390 = read.table("C:/G/Rt/SAS4lm/p390.txt", header=TRUE)
p390$ca = ifelse(p390$a == 0, -1, 1)
p390$cb = ifelse(p390$b == 0, -1, 1)
p390cc = ifelse(p390cc == 0, -1, 1)
p390 = af(p390, c("rep", "blk", "a", "b", "c"))
ANOVA(y ~ rep/blk + ca*cb*cc, p390)
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
               12 81.75 6.8125 33.601 6.618e-07 ***
MODEL
                    2.23 0.2027
RESIDUALS
               11
CORRECTED TOTAL 23 83.98
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value
                                     Pr(>F)
         2 0.051
                    0.025
                           0.1256 0.8832237
rep
                    2.477 12.2194 0.0007966 ***
rep:blk
         3 7.432
         1 21.075 21.075 103.9487 6.090e-07 ***
ca
cb
         1 0.005
                  0.005
                            0.0224 0.8837872
                            8.4969 0.0140640 *
         1 1.723
                    1.723
ca:cb
         1 37.776 37.776 186.3209 3.063e-08 ***
СС
         1 2.318
                   2.318 11.4332 0.0061285 **
ca:cc
         1 11.340 11.340 55.9328 1.232e-05 ***
cb:cc
ca:cb:cc 1 0.031
                    0.031
                            0.1511 0.7049490
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value
                                      Pr(>F)
         2 0.051
                    0.025
                            0.1256 0.883224
rep
         3 1.668
                    0.556
                            2.7416 0.093789 .
rep:blk
ca
         1 21.075 21.075 103.9487 6.090e-07 ***
         1 0.005
                   0.005
                            0.0224 0.883787
cb
         1 1.723
                    1.723
                            8.4969 0.014064 *
ca:cb
         1 37.776 37.776 186.3209 3.063e-08 ***
СС
         1 2.318
                    2.318 11.4332 0.006129 **
ca:cc
         1 11.340 11.340 55.9328 1.232e-05 ***
cb:cc
ca:cb:cc 1 0.031
                            0.1511 0.704949
                    0.031
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
        Df Sum Sq Mean Sq F value
                                      Pr(>F)
         2 0.051
                  0.025
                          0.1256 0.883224
rep
```

```
3 1.668 0.556
                            2.7416 0.093789 .
rep:blk
         1 21.075 21.075 103.9487 6.090e-07 ***
ca
cb
         1 0.005
                   0.005
                            0.0224 0.883787
         1 1.723
                    1.723
                            8.4969 0.014064 *
ca:cb
         1 37.776 37.776 186.3209 3.063e-08 ***
СС
                   2.318 11.4332 0.006129 **
ca:cc
          1 2.318
cb:cc
         1 11.340 11.340 55.9328 1.232e-05 ***
ca:cb:cc 1 0.031
                    0.031
                            0.1511 0.704949
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.8.2 p394
(50) MODEL
p394 = read.table("C:/G/Rt/SAS4lm/p394.txt", header=TRUE)
p394 = af(p394, c("a", "b", "c", "d"))
ANOVA(y ~ ca*cb*cc*cd, p394)
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                7 6.3559 0.90798
MODEL
RESIDUALS
                0.0000
CORRECTED TOTAL 7 6.3559
$`Type I`
           Df Sum Sq Mean Sq F value Pr(>F)
            1 2.07061 2.07061
ca
            1 0.59951 0.59951
cb
ca:cb
            1 0.00031 0.00031
СС
            1 0.00551 0.00551
            1 0.80011 0.80011
ca:cc
cb:cc
            1 2.82031 2.82031
ca:cb:cc
            1 0.05951 0.05951
cd
            0
ca:cd
cb:cd
            0
ca:cb:cd
            0
cc:cd
            0
            0
ca:cc:cd
            0
cb:cc:cd
ca:cb:cc:cd 0
$`Type II`
           Df Sum Sq Mean Sq F value Pr(>F)
```

```
0
ca
cb
             0
             0
ca:cb
СС
             0
             0
ca:cc
cb:cc
             0
ca:cb:cc
cd
ca:cd
             0
cb:cd
             0
ca:cb:cd
             0
cc:cd
             0
             0
ca:cc:cd
cb:cc:cd
             0
ca:cb:cc:cd 0
$`Type III`
CAUTION: Singularity Exists!
            Df Sum Sq Mean Sq F value Pr(>F)
ca
             0
cb
             0
ca:cb
СС
ca:cc
             0
cb:cc
             0
ca:cb:cc
             0
             0
cd
             0
ca:cd
             0
cb:cd
ca:cb:cd
cc:cd
ca:cc:cd
             0
cb:cc:cd
ca:cb:cc:cd 0
(51) MODEL
ANOVA(y \sim a*b*c*d, p394)
$ANOVA
Response : y
                Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                 7 6.3559 0.90798
RESIDUALS
                 0 0.0000
CORRECTED TOTAL 7 6.3559
$`Type I`
```

```
Df Sum Sq Mean Sq F value Pr(>F)
         1 2.07061 2.07061
a
b
         1 0.59951 0.59951
a:b
         1 0.00031 0.00031
         1 0.00551 0.00551
         1 0.80011 0.80011
a:c
         1 2.82031 2.82031
         1 0.05951 0.05951
a:b:c
d
a:d
         0
b:d
         0
a:b:d
c:d
a:c:d
b:c:d
a:b:c:d 0
$`Type II`
        Df Sum Sq Mean Sq F value Pr(>F)
         0
a
         0
b
a:b
С
a:c
b:c
         0
a:b:c
         0
d
         0
a:d
b:d
a:b:d
c:d
a:c:d
         0
b:c:d
a:b:c:d 0
$`Type III`
CAUTION: Singularity Exists!
       Df Sum Sq Mean Sq F value Pr(>F)
         0
a
b
         0
         0
a:b
         0
С
a:c
         0
b:c
a:b:c
d
         0
a:d
         0
b:d
         0
```

```
a:b:d
        0
c:d
        0
a:c:d
        0
b:c:d
        0
a:b:c:d 0
5.8.3 p399
(52) MODEL
p399 = read.table("C:/G/Rt/SAS4lm/p399.txt", header=TRUE)
p399 = af(p399, c("blk", "trt"))
ANOVA(y ~ trt + blk, p399)
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                8 281.127 35.141 40.822 0.005606 **
MODEL
RESIDUALS
                3
                    2.583
                           0.861
CORRECTED TOTAL 11 283.710
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
                             Pr(>F)
trt 3 102.26 34.086 39.596 0.006515 **
blk 5 178.87 35.774 41.558 0.005691 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                               Pr(>F)
trt 3 59.018 19.673 22.853 0.014388 *
blk 5 178.871 35.774 41.558 0.005691 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
trt 3 59.017 19.672 22.853 0.014388 *
blk 5 178.871 35.774 41.558 0.005691 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.8.4 p403
```

(53) MODEL

```
p403 = read.table("C:/G/Rt/SAS4lm/p403.txt", header=TRUE)
p403 = af(p403, c("PATIENT", "VISIT"))
ANOVA(HR ~ SEQUENCE + PATIENT %in% SEQUENCE + VISIT + DRUG + RESIDS + RESIDT, p403)
$ANOVA
Response : HR
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               29 6408.7 220.99
                                  3.912 3.127e-05 ***
RESIDUALS
               42 2372.6
                           56.49
CORRECTED TOTAL 71 8781.3
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
                Df Sum Sq Mean Sq F value Pr(>F)
                 5 508.9 101.79 1.8019 0.133346
SEQUENCE
SEQUENCE: PATIENT 18 4692.3 260.69 4.6147 2.21e-05 ***
                 2 146.8
                          73.39 1.2991 0.283499
VISIT
DRUG
                 2 668.8 334.39 5.9194 0.005435 **
RESIDS
                 1 391.0 391.02 6.9219 0.011854 *
                      0.8
                             0.84 0.0149 0.903511
RESIDT
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
                Df Sum Sq Mean Sq F value
                                           Pr(>F)
SEQUENCE
                 5 701.2 140.237 2.4825 0.04665 *
SEQUENCE: PATIENT 18 4692.3 260.685 4.6147 2.21e-05 ***
VISIT
                 2 146.8 73.389 1.2991 0.28350
DRUG
                 2 344.0 171.975 3.0443 0.05826 .
RESIDS
                 1 309.2 309.174 5.4731 0.02414 *
RESIDT
                 1
                      0.8
                           0.840 0.0149 0.90351
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type III`
                Df Sum Sq Mean Sq F value
                                           Pr(>F)
                 5 701.2 140.237 2.4825 0.04665 *
SEQUENCE
SEQUENCE: PATIENT 18 4692.3 260.685 4.6147 2.21e-05 ***
VISIT
                 2 146.8 73.389 1.2991 0.28350
DRUG
                 2 343.9 171.975 3.0443 0.05826 .
RESIDS
                    309.2 309.174 5.4731 0.02414 *
RESIDT
                 1
                      0.8
                           0.840 0.0149 0.90351
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(HR ~ SEQUENCE + PATIENT %in% SEQUENCE + VISIT + DRUG + RESIDS + RESIDT,
        p403), type=3, singular.ok=TRUE) # NOT OK
Note: model has aliased coefficients
     sums of squares computed by model comparison
Anova Table (Type III tests)
Response: HR
                Sum Sq Df F values Pr(>F)
SEQUENCE
                   0.0 0
VISIT
                 146.8 2 1.2991 0.28350
DRUG
                 344.0 2
                            3.0443 0.05826 .
RESIDS
                 309.2 1
                            5.4731 0.02414 *
RESIDT
                   0.8 1
                            0.0149 0.90351
SEQUENCE: PATIENT 4692.3 18
                            4.6147 2.21e-05 ***
Residuals
                2372.6 42
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.8.5 p409 11.5
(54) MODEL
p409 = read.table("C:/G/Rt/SAS4lm/p409.txt", header=TRUE)
ANOVA(TS ~ SOURCE*AMT, p409) # p410 Output 11.21
$ANOVA
Response : TS
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
                5 258.727 51.745 263.71 1.785e-09 ***
RESIDUALS
                    1.766
                            0.196
                9
CORRECTED TOTAL 14 260.493
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
          Df Sum Sq Mean Sq F value
                                       Pr(>F)
SOURCE
           2 98.001 49.001 249.720 1.306e-08 ***
           1 138.245 138.245 704.534 7.392e-10 ***
TMA
SOURCE: AMT 2 22.481 11.240 57.284 7.595e-06 ***
```

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

```
$`Type II`
          Df Sum Sq Mean Sq F value
                                       Pr(>F)
           2 98.001 49.001 249.720 1.306e-08 ***
SOURCE
AMT
           1 138.245 138.245 704.534 7.392e-10 ***
SOURCE: AMT 2 22.481 11.240 57.284 7.595e-06 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
          Df Sum Sq Mean Sq F value
                                       Pr(>F)
               0.070
                       0.035
                              0.179
SOURCE
           2
                                        0.839
           1 138.245 138.245 704.534 7.392e-10 ***
AMT
SOURCE: AMT 2 22.481 11.240 57.284 7.595e-06 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.8.6 p412
(55) MODEL
p412 = read.table("C:/G/Rt/SAS4lm/p412.txt", header=TRUE)
ANOVA(ts ~ source:amt, p412) # p413 Output 11.24
$ANOVA
Response : ts
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
                3 393.01 131.002 903.34 < 2.2e-16 ***
                    2.32
                          0.145
RESIDUALS
               16
CORRECTED TOTAL 19 395.33
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
          Df Sum Sq Mean Sq F value
                                      Pr(>F)
source:amt 3 393.01
                       131 903.34 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
          Df Sum Sq Mean Sq F value
                                      Pr(>F)
                       131 903.34 < 2.2e-16 ***
source:amt 3 393.01
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
          Df Sum Sq Mean Sq F value
                                      Pr(>F)
```

```
source:amt 3 393.01 131 903.34 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.8.7 p414
(56) MODEL
p414 = read.table("C:/G/Rt/SAS4lm/p414.txt", header=TRUE)
p414 = af(p414, c("lackofit"))
ANOVA(loglivcu ~ level + lackofit, p414) # p415 Output 11.26
$ANOVA
Response : loglivcu
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
MODEL
                3 5.2310 1.74365 155.47 5.018e-14 ***
RESIDUALS
               20 0.2243 0.01122
CORRECTED TOTAL 23 5.4553
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value
                                    Pr(>F)
         1 4.9859 4.9859 444.555 3.997e-15 ***
level
lackofit 2 0.2450 0.1225 10.924 0.0006216 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value
                                     Pr(>F)
level
lackofit 2 0.24504 0.12252 10.924 0.0006216 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
        Df Sum Sq Mean Sq F value
                                     Pr(>F)
level
lackofit 2 0.24504 0.12252 10.924 0.0006216 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.8.8 p417
```

(57) MODEL

```
p417 = read.table("C:/G/Rt/SAS4lm/p417.txt", header=TRUE)
p417 = af(p417, c("TRT", "POT", "PLANT"))
ANOVA(Y ~ TRT + POT %in% TRT, p417) # p418 Output 11.28
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value
                7 267.226 38.175 12.433 7.522e-05 ***
MODEL
               13 39.917
                            3.071
RESIDUALS
CORRECTED TOTAL 20 307.143
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value
TRT
        2 236.921 118.460 38.580 3.412e-06 ***
TRT:POT 5 30.306 6.061
                          1.974
                                    0.1499
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
        2 236.921 118.460 38.580 3.412e-06 ***
TRT
TRT:POT 5 30.306
                    6.061
                          1.974
                                    0.1499
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value
                                    Pr(>F)
        2 200.111 100.055 32.586 8.626e-06 ***
TRT:POT 5 30.306
                  6.061
                          1.974
                                    0.1499
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(Y ~ TRT + POT %in% TRT, p417), type=3, singular.ok=TRUE) # NOT OK
Note: model has aliased coefficients
     sums of squares computed by model comparison
Anova Table (Type III tests)
Response: Y
         Sum Sq Df F values Pr(>F)
TRT
         22.310 1
                      7.266 0.01835 *
TRT:POT
         30.306 5
                      1.974 0.14991
```

```
Residuals 39.917 13
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
5.8.9 p431
(58) MODEL
p431 = read.table("C:/G/Rt/SAS4lm/p431.txt", header=TRUE)
p431 = af(p431, c("line", "sire", "agedam", "steerno"))
ANOVA(avdlygn ~ line + line:sire + agedam + line:agedam + age + intlwt, p431)
$ANOVA
Response : avdlygn
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               16 2.5275 0.157966 3.1437 0.001091 **
RESIDUALS
               48 2.4119 0.050248
CORRECTED TOTAL 64 4.9394
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
           Df Sum Sq Mean Sq F value Pr(>F)
            2 0.38009 0.190046 3.7821 0.02983 *
line
            6 0.92634 0.154391 3.0726 0.01260 *
line:sire
            2 0.11894 0.059471 1.1835 0.31497
agedam
line:agedam 4 0.64889 0.162222 3.2284 0.02000 *
            1 0.18349 0.183487 3.6516 0.06200 .
age
            1 0.26970 0.269704 5.3674 0.02483 *
intlwt
___
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
           Df Sum Sq Mean Sq F value
                                       Pr(>F)
line
            2 0.05526 0.02763 0.5498 0.580636
            6 0.97389 0.16231 3.2303 0.009543 **
line:sire
            2 0.33106 0.16553 3.2943 0.045640 *
agedam
line:agedam 4 0.45343 0.11336 2.2560 0.076821 .
            1 0.38128 0.38128 7.5878 0.008277 **
age
            1 0.26970 0.26970 5.3674 0.024830 *
intlwt
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
           Df Sum Sq Mean Sq F value
                                       Pr(>F)
            2 0.13620 0.06810 1.3553 0.267560
line
```

```
line:sire
            6 0.97389 0.16231 3.2303 0.009543 **
            2 0.13011 0.06505 1.2946 0.283392
agedam
line:agedam 4 0.45343 0.11336 2.2560 0.076821 .
            1 0.38128 0.38128 7.5878 0.008277 **
age
            1 0.26970 0.26970 5.3674 0.024830 *
intlwt
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
# p433 Output 11.40
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(avdlygn ~ line + line:sire + agedam + line:agedam + age + intlwt, p431),
     type=3, singular.ok=TRUE) # NOT OK for line
Note: model has aliased coefficients
     sums of squares computed by model comparison
Anova Table (Type III tests)
Response: avdlygn
            Sum Sq Df F values
line
           0.00000 0
           0.13011 2 1.2946 0.283392
agedam
           0.38128 1 7.5878 0.008277 **
age
           0.26970 1 5.3674 0.024830 *
intlwt
line:sire 0.97389 6 3.2303 0.009543 **
line:agedam 0.45343 4
                        2.2560 0.076821 .
Residuals 2.41192 48
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(59) MODEL
ANOVA(avdlygn ~ sire + agedam, p431) # # p434 Output 11.41
$ANOVA
Response : avdlygn
               Df Sum Sq Mean Sq F value Pr(>F)
               10 1.4254 0.142538 2.1904 0.03237 *
MODEL
RESIDUALS
               54 3.5140 0.065074
CORRECTED TOTAL 64 4.9394
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
```

```
Df Sum Sq Mean Sq F value Pr(>F)
       8 1.30644 0.163305 2.5095 0.02138 *
sire
agedam 2 0.11894 0.059471 0.9139 0.40707
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
      Df Sum Sq Mean Sq F value Pr(>F)
       8 1.33017 0.166271 2.5551 0.01937 *
agedam 2 0.11894 0.059471 0.9139 0.40707
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value Pr(>F)
       8 1.33017 0.166271 2.5551 0.01937 *
agedam 2 0.11894 0.059471 0.9139 0.40707
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
5.8.10 p437 ABSORB option in SAS
(60) MODEL
ANOVA(avdlygn ~ line + sire + agedam + line:agedam + age + intlwt, p431)
$ANOVA
Response : avdlygn
               Df Sum Sq Mean Sq F value Pr(>F)
               16 2.5275 0.157966 3.1437 0.001091 **
MODEL
               48 2.4119 0.050248
RESIDUALS
CORRECTED TOTAL 64 4.9394
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
           Df Sum Sq Mean Sq F value Pr(>F)
line
            2 0.38009 0.190046 3.7821 0.02983 *
            6 0.92634 0.154391 3.0726 0.01260 *
sire
agedam
            2 0.11894 0.059471 1.1835 0.31497
line:agedam 4 0.64889 0.162222 3.2284 0.02000 *
            1 0.18349 0.183487 3.6516 0.06200 .
age
intlwt
            1 0.26970 0.269704 5.3674 0.02483 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$`Type II`
           Df Sum Sq Mean Sq F value
                                       Pr(>F)
line
sire
            6 0.97389 0.16231 3.2303 0.009543 **
agedam
            2 0.33106 0.16553 3.2943 0.045640 *
line:agedam 4 0.45343 0.11336 2.2560 0.076821 .
age
            1 0.38128 0.38128 7.5878 0.008277 **
            1 0.26970 0.26970 5.3674 0.024830 *
intlwt
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
           Df Sum Sq Mean Sq F value Pr(>F)
line
sire
            6 0.97389 0.16231 3.2303 0.009543 **
agedam
            2 0.13011 0.06505 1.2946 0.283392
line:agedam 4 0.45343 0.11336 2.2560 0.076821 .
            1 0.38128 0.38128 7.5878 0.008277 **
            1 0.26970 0.26970 5.3674 0.024830 *
intlwt
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

6 Sahai - Unbalanced

Reference

• Sahai H, Ojeda MM. Analysis of Variance for Random Models Volume 2 Unbalanced Data. 2005.

6.1 Table 11.2

(61) MODEL

```
T11.2 = read.table("C:/G/Rt/ANOVA/T11.2.txt")
colnames(T11.2) = c("Group", "Y")
T11.2 = af(T11.2, "Group")
ANOVA(Y ~ Group, T11.2) # p115
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value
                4 80.401 20.1003 5.9884 0.0004103 ***
MODEL
RESIDUALS
               59 198.036 3.3565
CORRECTED TOTAL 63 278.438
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value Pr(>F)
Group 4 80.401 20.1 5.9884 0.0004103 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
Group 4 80.401 20.1 5.9884 0.0004103 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
Group 4 80.401
                  20.1 5.9884 0.0004103 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

6.2 Table 12.6

(62) MODEL

```
T12.6 = read.table("C:/G/Rt/ANOVA/T12.6.txt")
colnames(T12.6) = c("Location", "Family", "Y")
T12.6 = af(T12.6, c("Location", "Family"))
ANOVA(Y ~ Location + Family, T12.6) # p184
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
                7 1.6144 0.230636 8.9562 7.223e-07 ***
RESIDUALS
               45 1.1588 0.025752
CORRECTED TOTAL 52 2.7733
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value
                                     Pr(>F)
Location 3 0.74036 0.24679 9.5833 5.219e-05 ***
        4 0.87410 0.21852 8.4859 3.436e-05 ***
Family
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value
                                     Pr(>F)
Location 3 0.83765 0.27921 10.8426 1.753e-05 ***
Family
         4 0.87410 0.21852 8.4859 3.436e-05 ***
___
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
        Df Sum Sq Mean Sq F value
                                     Pr(>F)
Location 3 0.83765 0.27921 10.8426 1.753e-05 ***
       4 0.87410 0.21852 8.4859 3.436e-05 ***
Family
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
6.3 Table 13.6
(63) MODEL
T13.6 = read.table("C:/G/Rt/ANOVA/T13.6.txt")
colnames(T13.6) = c("Site", "Worker", "Y")
T13.6 = af(T13.6, c("Site", "Worker"))
ANOVA(Y ~ Site + Worker + Site:Worker, T13.6)
```

\$ANOVA

```
Response : Y
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
               11 2643.11 240.283 60.323 < 2.2e-16 ***
MODEL
RESIDUALS
               35 139.42
                           3.983
CORRECTED TOTAL 46 2782.52
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
           Df Sum Sq Mean Sq F value
                                        Pr(>F)
            2 1281.55 640.77 160.866 < 2.2e-16 ***
Site
            3 399.27 133.09 33.412 2.234e-10 ***
Worker
Site:Worker 6 962.29 160.38 40.264 2.720e-14 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
           Df Sum Sq Mean Sq F value
Site
            2 1322.24 661.12 165.973 < 2.2e-16 ***
Worker
            3 399.27 133.09 33.412 2.234e-10 ***
Site:Worker 6 962.29 160.38 40.264 2.720e-14 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
           Df Sum Sq Mean Sq F value
                                       Pr(>F)
            2 804.83 402.42 101.026 2.887e-15 ***
Site
            3 430.88 143.63 36.058 8.310e-11 ***
Site:Worker 6 962.29 160.38 40.264 2.720e-14 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
6.4 Table 14.2
(64) MODEL
T14.2 = read.csv("C:/G/Rt/ANOVA/T14.2.csv")
T14.2 = T14.2[!is.na(T14.2$Y),]
T14.2 = af(T14.2, c("Day", "Machine", "Operator"))
ANOVA(Y ~ Day + Machine + Operator, T14.2)
$ANOVA
Response: Y
                Df Sum Sq Mean Sq F value
                                             Pr(>F)
MODEL
                 7 6345.4 906.48 8.1297 5.931e-08 ***
RESIDUALS
               110 12265.3 111.50
```

```
CORRECTED TOTAL 117 18610.6
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value
         2 3737.8 1868.90 16.7611 4.426e-07 ***
         2 2440.7 1220.33 10.9445 4.625e-05 ***
Operator 3 166.9
                  55.63 0.4989
                                    0.6838
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value
Day
         2 3795.1 1897.56 17.0181 3.636e-07 ***
         2 2464.8 1232.39 11.0526 4.227e-05 ***
Machine
Operator 3 166.9
                  55.63 0.4989
                                    0.6838
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
        Df Sum Sq Mean Sq F value
                                    Pr(>F)
         2 3795.1 1897.56 17.0181 3.636e-07 ***
Machine 2 2464.8 1232.39 11.0526 4.227e-05 ***
Operator 3 166.9 55.63 0.4989
                                    0.6838
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
6.5 Table 15.3
(65) MODEL
T15.3 = read.table("C:/G/Rt/ANOVA/T15.3.txt")
colnames(T15.3) = c("Dam", "Sire", "pH")
T15.3 = af(T15.3, c("Dam", "Sire"))
ANOVA(pH ~ Dam/Sire, T15.3) # p301
$ANOVA
Response : pH
                Df Sum Sq Mean Sq F value Pr(>F)
                36 0.25804 0.0071678 2.8977 7.2e-06 ***
MODEL
               123 0.30425 0.0024736
RESIDUALS
CORRECTED TOTAL 159 0.56229
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$`Type I`
                     Mean Sq F value
        Df
             Sum Sq
                                        Pr(>F)
        14 0.178017 0.0127155 5.1405 1.563e-07 ***
Dam:Sire 22 0.080024 0.0036374 1.4705
                                       0.09662 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
             Sum Sq Mean Sq F value
                                        Pr(>F)
        14 0.178017 0.0127155 5.1405 1.563e-07 ***
Dam
Dam:Sire 22 0.080024 0.0036374 1.4705
                                       0.09662 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
                     Mean Sq F value
                                        Pr(>F)
        Df
             Sum Sq
        14 0.179405 0.0128146 5.1805 1.347e-07 ***
Dam:Sire 22 0.080024 0.0036374 1.4705
                                       0.09662 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
options(contrasts = c("contr.sum", "contr.poly"))
Anova(lm(pH ~ Dam/Sire, T15.3), type=3, singular.ok=TRUE) # NOT OK
Note: model has aliased coefficients
     sums of squares computed by model comparison
Anova Table (Type III tests)
Response: pH
           Sum Sq Df F values
                                 Pr(>F)
         0.081011
Dam
                   6
                      5.4584 4.898e-05 ***
Dam:Sire 0.080024 22
                       1.4705
                                0.09662 .
Residuals 0.304253 123
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
6.6 Table 16.3
(66) MODEL
T16.3 = read.csv("C:/G/Rt/ANOVA/T16.3.csv")
colnames(T16.3) = c("Plot", "Sample", "Subsample", "Residue")
T16.3 = af(T16.3, c("Plot", "Sample", "Subsample"))
ANOVA(Residue ~ Plot/Sample/Subsample, T16.3) # p344
```

```
$ANOVA
Response : Residue
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
               54 3.1897 0.059069 5.8842 1.476e-05 ***
               22 0.2208 0.010039
RESIDUALS
CORRECTED TOTAL 76 3.4106
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
                     Df Sum Sq Mean Sq F value
                                                   Pr(>F)
Plot
                     10 1.84041 0.184041 18.3332 1.929e-08 ***
                     22 0.99175 0.045079 4.4906 0.0004209 ***
Plot:Sample
Plot:Sample:Subsample 22 0.35757 0.016253 1.6191 0.1330632
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
                     Df Sum Sq Mean Sq F value
                                                   Pr(>F)
                     10 1.84041 0.184041 18.3332 1.929e-08 ***
Plot
                     22 0.99175 0.045079 4.4906 0.0004209 ***
Plot:Sample
Plot:Sample:Subsample 22 0.35757 0.016253 1.6191 0.1330632
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
                     Df Sum Sq Mean Sq F value
                                                   Pr(>F)
                     10 1.78686 0.178686 17.7998 2.547e-08 ***
Plot
                     22 0.99175 0.045079 4.4906 0.0004209 ***
Plot:Sample
Plot:Sample:Subsample 22 0.35757 0.016253 1.6191 0.1330632
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
options(contrasts = c("contr.sum", "contr.poly"))
Anova(lm(Residue ~ Plot/Sample/Subsample, T16.3), type=3, singular.ok=TRUE)
Note: model has aliased coefficients
     sums of squares computed by model comparison
Anova Table (Type III tests)
Response: Residue
                      Sum Sq Df F values Pr(>F)
Plot
                     0.00000 0
Plot:Sample
                     0.36613 11
                                  3.3156 0.00805 **
Plot:Sample:Subsample 0.35758 22
                                  1.6191 0.13306
Residuals
                     0.22085 22
```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

NOT OK

7 Federer - Variations

Reference

 Federer WT, King F. Variations on Split Plot and Split Block Experiment Designs. John Wiley & Sons Inc. 2007.

7.1 Example 1.1

(67) MODEL

```
ex1.1 = read.table("C:/G/Rt/Split/Ex1.1-spex1.txt", header=TRUE)
ex1.1 = af(ex1.1, c("R", "A", "B"))
ANOVA(Y \sim R + A + R:A + B + A:B, ex1.1)
$ANOVA
Response: Y
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
MODEL
               27 4905.7 181.694
                                10.75 1.994e-10 ***
RESIDUALS
               36 608.5 16.902
CORRECTED TOTAL 63 5514.2
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    3 223.8 74.60 4.4138
                              0.00963 **
R
    3 194.6
              64.85 3.8370 0.01756 *
R:A 9 158.2 17.58 1.0402 0.42842
    3 4107.4 1369.13 81.0030 4.441e-16 ***
A:B 9 221.7 24.64 1.4577
                            0.20117
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                             Pr(>F)
    3 223.8 74.60 4.4138 0.00963 **
R
    3 194.6
              64.85 3.8370
                              0.01756 *
Α
R:A 9 158.2 17.58 1.0402
                              0.42842
    3 4107.4 1369.13 81.0030 4.441e-16 ***
A:B 9 221.7 24.64 1.4577
                            0.20117
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
                              Pr(>F)
```

```
R.
    3 223.8
              74.60 4.4138 0.00963 **
    3 194.6 64.85 3.8370 0.01756 *
Α
R:A 9 158.2
              17.58 1.0402
                              0.42842
    3 4107.4 1369.13 81.0030 4.441e-16 ***
A:B 9 221.7
               24.64 1.4577
                              0.20117
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
7.2 Example 1.2
(68) MODEL
ex1.2 = read.table("C:/G/Rt/Split/Ex1.2-spex2.txt", header=TRUE)
ex1.2 = af(ex1.2, c("R", "A", "B"))
ANOVA(Y \sim R + A + R:A + B + A:B, ex1.2)
$ANOVA
Response : Y
              Df Sum Sq Mean Sq F value
                                          Pr(>F)
               47 35573 756.88 31.243 < 2.2e-16 ***
MODEL
                          24.23
RESIDUALS
               48
                   1163
CORRECTED TOTAL 95 36736
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
                                Pr(>F)
         38.6
               19.3 0.7963 0.4568480
R
    7
        763.2
               109.0 4.5003 0.0006418 ***
R:A 14 1377.2
                98.4 4.0608 0.0001343 ***
    3 30774.3 10258.1 423.4386 < 2.2e-16 ***
A:B 21 2620.1
              124.8 5.1502 1.327e-06 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
         38.6
                19.3
                      0.7963 0.4568480
R.
      763.2
              109.0
                       4.5003 0.0006418 ***
Α
    7
R:A 14 1377.2
                98.4
                       4.0608 0.0001343 ***
    3 30774.3 10258.1 423.4386 < 2.2e-16 ***
A:B 21 2620.1 124.8 5.1502 1.327e-06 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
```

```
Df Sum Sq Mean Sq F value
                                 Pr(>F)
                19.3 0.7963 0.4568480
R
    2
         38.6
Α
    7
        763.2
               109.0 4.5003 0.0006418 ***
R:A 14 1377.2
                 98.4 4.0608 0.0001343 ***
    3 30774.3 10258.1 423.4386 < 2.2e-16 ***
A:B 21 2620.1
               124.8 5.1502 1.327e-06 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
7.3 Example 2.1
(69) MODEL
ex2.1 = read.table("C:/G/Rt/Split/sbex.txt", header=TRUE)
colnames(ex2.1) = c("Y", "R", "A", "B")
ex2.1 = af(ex2.1, c("R", "A", "B"))
ANOVA(Y \sim R + A + R:A + B + R:B + A:B, ex2.1)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               41 274.750 6.7012 5.1475 0.0002305 ***
RESIDUALS
               18 23.433 1.3019
CORRECTED TOTAL 59 298.183
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
    1 2.817 2.8167 2.1636 0.1585807
    9 77.683 8.6315 6.6302 0.0003456 ***
R:A 9 81.017 9.0019 6.9147 0.0002658 ***
    2 35.433 17.7167 13.6088 0.0002510 ***
R:B 2 16.233 8.1167 6.2347 0.0087635 **
A:B 18 61.567 3.4204 2.6273 0.0236253 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                               Pr(>F)
    1 2.817 2.8167 2.1636 0.1585807
    9 77.683 8.6315 6.6302 0.0003456 ***
R:A 9 81.017 9.0019 6.9147 0.0002658 ***
    2 35.433 17.7167 13.6088 0.0002510 ***
R:B 2 16.233 8.1167 6.2347 0.0087635 **
A:B 18 61.567 3.4204 2.6273 0.0236253 *
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
    1 2.817 2.8167 2.1636 0.1585807
    9 77.683 8.6315 6.6302 0.0003456 ***
R:A 9 81.017 9.0019 6.9147 0.0002658 ***
    2 35.433 17.7167 13.6088 0.0002510 ***
R:B 2 16.233 8.1167 6.2347 0.0087635 **
A:B 18 61.567 3.4204 2.6273 0.0236253 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
7.4 Example 2.2
(70) MODEL
ex2.2 = read.table("C:/G/Rt/Split/sbex2_2.txt", header=TRUE)
ex2.2 = af(ex2.2, c("Row", "Column", "R", "S"))
ANOVA(Y ~ Column + R + R:Column + S + S:Column + R:S, ex2.2)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
               51 10328 202.51 0.8112 0.7688
MODEL
RESIDUALS
               48 11982 249.63
CORRECTED TOTAL 99 22310
$`Type I`
        Df Sum Sq Mean Sq F value Pr(>F)
Column
         4 1318.6 329.66 1.3206 0.2758
         4 1159.8 289.94 1.1615 0.3396
Column: R 16 2808.6 175.54 0.7032 0.7766
         3 351.9 117.29 0.4699 0.7047
Column:S 12 3863.3 321.94 1.2897 0.2555
R:S
        12 826.0
                    68.83 0.2757 0.9906
$`Type II`
        Df Sum Sq Mean Sq F value Pr(>F)
         4 1318.6 329.66 1.3206 0.2758
Column
         4 1159.8 289.94 1.1615 0.3396
Column: R 16 2808.6 175.54 0.7032 0.7766
         3 351.9 117.29 0.4699 0.7047
Column:S 12 3863.3 321.94 1.2897 0.2555
        12 826.0
                  68.83 0.2757 0.9906
R:S
```

```
$`Type III`
        Df Sum Sq Mean Sq F value Pr(>F)
         4 1318.6 329.66 1.3206 0.2758
         4 1159.8 289.94 1.1615 0.3396
Column: R 16 2808.6 175.54 0.7032 0.7766
         3 351.9 117.29 0.4699 0.7047
Column:S 12 3863.3 321.94 1.2897 0.2555
        12 826.0 68.83 0.2757 0.9906
(71) MODEL
ANOVA(Y \sim Row + R + Row:R + S + Column:S + R:S + Column:R:S, ex2.2)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               99 22310 225.36
RESIDUALS
                0
                       0
CORRECTED TOTAL 99 22310
$`Type I`
          Df Sum Sq Mean Sq F value Pr(>F)
           4
              147.4
                       36.86
Row
           4 1159.8 289.94
R
          16 3979.8 248.74
Row:R
S
               351.9 117.29
           3
          12 3863.3 321.94
S:Column
          12
               826.0
                      68.83
R:S:Column 48 11982.3 249.63
$`Type II`
          Df Sum Sq Mean Sq F value Pr(>F)
Row
           0
           4 1159.8 289.94
R
Row:R
           0
           3
               351.9 117.29
S:Column
          12 3863.3 321.94
R:S
          12
               826.0
                      68.83
R:S:Column 48 11982.3 249.63
$`Type III`
CAUTION: Singularity Exists!
          Df Sum Sq Mean Sq F value Pr(>F)
Row
           0
R
           4 1159.8 289.94
Row:R
```

```
3
                351.9 117.29
S:Column
           12 3863.3 321.94
                       68.83
                826.0
R:S
           12
R:S:Column 48 11982.3 249.63
(72) MODEL
ANOVA(Y \sim Row + R + S + R:S + Row:R + Column:S + Column:R:S, ex2.2)
$ANOVA
Response : Y
                Df Sum Sq Mean Sq F value Pr(>F)
                  22310 225.36
MODEL
RESIDUALS
                0
CORRECTED TOTAL 99 22310
$`Type I`
              Sum Sq Mean Sq F value Pr(>F)
           Df
               147.4
Row
           4
                       36.86
           4 1159.8 289.94
R
S
           3
               351.9 117.29
R:S
                826.0
           12
                      68.83
Row:R
           16 3979.8 248.74
S:Column
           12 3863.3 321.94
R:S:Column 48 11982.3 249.63
$`Type II`
           Df Sum Sq Mean Sq F value Pr(>F)
Row
           0
R
            4 1159.8 289.94
S
           3
               351.9 117.29
R:S
           12
                826.0
                      68.83
Row:R
           0
           12 3863.3 321.94
S:Column
R:S:Column 48 11982.3 249.63
$`Type III`
CAUTION: Singularity Exists!
           Df Sum Sq Mean Sq F value Pr(>F)
Row
           0
R
            4 1159.8 289.94
S
           3
                351.9 117.29
R:S
           12
                826.0
                       68.83
Row:R
           0
           12 3863.3 321.94
S:Column
```

R:S:Column 48 11982.3 249.63

7.5 Example 3.1

```
(73) MODEL
ex3.1 = read.table("C:/G/Rt/Split/spedsite.txt", header=TRUE)
ex3.1 = af(ex3.1, c("Site", "A", "B", "C", "Block"))
ANOVA(Yield ~ Site + Site:Block + A + B + A:B + A:Site + B:Site + A:B:Site +
    A:B:Site:Block + C + A:C + B:C + A:B:C + C:Site + A:C:Site + B:C:Site +
   A:B:C:Site, ex3.1)
$ANOVA
Response : Yield
                       Sum Sq Mean Sq F value
                                                  Pr(>F)
                Df
               239 2724374186 11399055 23.682 < 2.2e-16 ***
MODEL
RESIDUALS
               240 115521933
                                481341
CORRECTED TOTAL 479 2839896119
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
                              Mean Sq F value Pr(>F)
              Df
                     Sum Sq
               3 621230991 207076997 430.2082 < 2e-16 ***
Site
               8 1305369943 163171243 338.9928 < 2e-16 ***
Site:Block
                    1333205
                              1333205 2.7698 0.09737 .
               1
                   47928577 11982144 24.8932 < 2e-16 ***
В
               4
A:B
                      14849
                                 3712 0.0077 0.99988
               4
Site:A
               3
                      33010
                                11003
                                        0.0229 0.99531
Site:B
              12
                      37932
                                 3161
                                        0.0066 1.00000
Site:A:B
                                  958
                                        0.0020 1.00000
              12
                      11494
                               114440
Site:Block:A:B 72
                    8239680
                                        0.2378 1.00000
С
                  739890389 246630130 512.3809 < 2e-16 ***
               3
A:C
                                 1078
                                        0.0022 0.99985
               3
                       3233
                                        0.0061 1.00000
B:C
              12
                      34961
                                 2913
A:B:C
              12
                      11077
                                  923
                                        0.0019 1.00000
Site:C
               9
                                        0.0060 1.00000
                      25983
                                 2887
Site:A:C
               9
                      22227
                                 2470
                                        0.0051 1.00000
Site:B:C
              36
                      88610
                                 2461
                                        0.0051 1.00000
                                 2723
                                        0.0057 1.00000
Site:A:B:C
              36
                      98025
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

\$`Type II`

```
Df
                                Mean Sq F value Pr(>F)
                      Sum Sq
                   621230991 207076997 430.2082 < 2e-16 ***
Site
                3
Site:Block
                8 1305369943 163171243 338.9928 < 2e-16 ***
Α
                1
                                1333205
                                          2.7698 0.09737 .
                      1333205
                               11982144 24.8932 < 2e-16 ***
В
                4
                    47928577
                                          0.0077 0.99988
A:B
                4
                        14849
                                   3712
Site:A
                3
                        33010
                                  11003
                                          0.0229 0.99531
Site:B
               12
                       37932
                                   3161
                                          0.0066 1.00000
                                    958
                                          0.0020 1.00000
Site:A:B
               12
                        11494
Site:Block:A:B 72
                     8239680
                                 114440
                                          0.2378 1.00000
С
                   739890389 246630130 512.3809 < 2e-16 ***
                3
A:C
                3
                                   1078
                                          0.0022 0.99985
                        3233
                                          0.0061 1.00000
B:C
               12
                       34961
                                   2913
                                    923
A:B:C
               12
                       11077
                                          0.0019 1.00000
Site:C
                9
                       25983
                                   2887
                                          0.0060 1.00000
Site:A:C
                9
                       22227
                                   2470
                                          0.0051 1.00000
Site:B:C
               36
                       88610
                                   2461
                                          0.0051 1.00000
Site:A:B:C
               36
                       98025
                                   2723
                                          0.0057 1.00000
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
               Df
                      Sum Sq
                                Mean Sq F value Pr(>F)
                   621230991 207076997 430.2082 < 2e-16 ***
Site
                3
Site:Block
                8 1305369943 163171243 338.9928 < 2e-16 ***
Α
                1
                     1333205
                                1333205
                                          2.7698 0.09737 .
В
                4
                    47928577
                               11982144 24.8932 < 2e-16 ***
A:B
                4
                        14849
                                   3712
                                          0.0077 0.99988
                3
                                          0.0229 0.99531
Site:A
                        33010
                                  11003
Site:B
               12
                       37932
                                   3161
                                          0.0066 1.00000
Site:A:B
               12
                        11494
                                    958
                                          0.0020 1.00000
                                 114440
                                          0.2378 1.00000
Site:Block:A:B 72
                     8239680
С
                3
                   739890389 246630130 512.3809 < 2e-16 ***
A:C
                3
                        3233
                                   1078
                                          0.0022 0.99985
               12
                                   2913
                                          0.0061 1.00000
B:C
                       34961
A:B:C
               12
                       11077
                                    923
                                          0.0019 1.00000
Site:C
                9
                       25983
                                   2887
                                          0.0060 1.00000
Site:A:C
                9
                       22227
                                   2470
                                          0.0051 1.00000
               36
                                          0.0051 1.00000
Site:B:C
                       88610
                                   2461
Site:A:B:C
               36
                       98025
                                   2723
                                          0.0057 1.00000
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(74) MODEL
ex3.1a = read.table("C:/G/Rt/Split/Ex3.1-example.txt", header=TRUE)
ex3.1a = af(ex3.1a, c("row", "P", "column", "R", "S"))
```

```
ANOVA(height ~ P + column + column:P + R + P:R + column:R + column:R:P + S +
  P:S + column:S + column:S:P + R:S + R:S:column + R:S:P + R:S:P:column, ex3.1a)
$ANOVA
Response : height
                Df Sum Sq Mean Sq F value Pr(>F)
               199 7534.8 37.863
MODEL
RESIDUALS
                0
                     0.0
CORRECTED TOTAL 199 7534.8
$`Type I`
            Df Sum Sq Mean Sq F value Pr(>F)
Ρ
             1 253.1 253.125
             4 109.4 27.357
column
P:column
             4 207.9 51.987
R.
             4
               90.6 22.657
P:R
            4 505.0 126.238
column:R
            16 3357.8 209.864
            16 1442.6 90.163
P:column:R
S
            3 16.4 5.458
P:S
            3
               14.3 4.765
column:S
            12 265.4 22.121
P:column:S 12 96.5 8.044
R.: S
            12 195.1 16.254
column:R:S
            48 365.5 7.615
P:R:S
            12 100.3 8.361
P:column:R:S 48 514.7 10.723
$`Type II`
            Df Sum Sq Mean Sq F value Pr(>F)
             1 253.1 253.125
             4 109.4 27.358
column
P:column
             4 208.0 51.988
R
             4 90.6 22.657
P:R
            4 504.9 126.237
            16 3357.8 209.864
column:R
P:column:R
            16 1442.6 90.162
S
            3 16.4 5.458
P:S
               14.3 4.765
            3
column:S
            12 265.5 22.121
P:column:S 12 96.5 8.044
R:S
            12 195.0 16.254
column:R:S
            48 365.5 7.615
P:R:S
            12 100.3 8.361
P:column:R:S 48 514.7 10.723
```

\$`Type III`

```
Df Sum Sq Mean Sq F value Pr(>F)
Р
                                          1 253.1 253.125
                                          4 109.4 27.358
column
P:column
                                          4 208.0 51.988
R
                                                  90.6 22.657
                                          4
P:R
                                          4 505.0 126.238
column:R
                                       16 3357.8 209.864
                                       16 1442.6 90.163
P:column:R
                                         3
                                                      16.4 5.458
P:S
                                                      14.3
                                                                          4.765
                                          3
column:S
                                       12 265.4 22.121
P:column:S
                                                  96.5
                                                                        8.044
                                       12
R:S
                                       12 195.0 16.254
column:R:S
                                       48 365.5
                                                                        7.615
P:R:S
                                       12 100.3
                                                                         8.361
P:column:R:S 48 514.7 10.723
 (75) MODEL
ANOVA(height \sim row + R + P + S + S:R + row:P + R:P + row:R:P + S:P + S:P:row + R:P + R:P
            S:R:P + R:S:P:row, ex3.1a)
$ANOVA
Response : height
                                                   Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                                                199 7534.8 37.863
                                                                      0.0
RESIDUALS
                                                      0
CORRECTED TOTAL 199 7534.8
$`Type I`
                              Df Sum Sq Mean Sq F value Pr(>F)
                                 4 2017.03 504.26
row
                                        90.63
                                                                     22.66
R
Ρ
                                 1 253.12 253.12
S
                                             16.38
                                                                     5.46
                                 3
R:S
                              12 195.05
                                                                     16.25
                                 4 167.25
                                                                   41.81
row:P
                                4 504.95 126.24
R:P
row:R:P
                              32 2933.52
                                                                  91.67
P:S
                               3
                                         14.29
                                                                    4.76
row:P:S
                              24 234.68
                                                                        9.78
R:P:S
                              12 100.33
                                                                      8.36
row:R:P:S 96 1007.52
                                                                     10.49
$`Type II`
                              Df Sum Sq Mean Sq F value Pr(>F)
```

4 2017.03 504.26

row

```
R
          4 90.63
                     22.66
Р
          1 253.12 253.12
                      5.46
S
          3
             16.38
R:S
         12 195.05
                     16.25
         4 167.25
                     41.81
row:P
R:P
          4 504.95 126.24
row:R:P
         32 2933.52
                    91.67
P:S
         3
            14.29
                      4.76
row:P:S
         24 234.68
                      9.78
R:P:S
         12 100.33
                      8.36
row:R:P:S 96 1007.52
                     10.49
$`Type III`
         Df Sum Sq Mean Sq F value Pr(>F)
row
          4 2017.03 504.26
R
            90.63
                     22.66
Р
          1 253.12 253.12
S
          3
            16.38
                    5.46
R:S
         12 195.05
                    16.25
row:P
         4 167.25
                    41.81
R:P
          4 504.95 126.24
         32 2933.52
                    91.67
row:R:P
P:S
         3
            14.30
                    4.77
row:P:S
         24 234.68
                      9.78
R:P:S
         12 100.33
                    8.36
row:R:P:S 96 1007.52
                     10.50
options(contrasts=c("contr.sum", "contr.poly"))
S:P:row + S:R:P + R:S:P:row, ex3.1a), type=3, singular.ok=TRUE)
        # NOT WORKING
alias(height \sim row + R + P + S + S:R + row:P + R:P + row:R:P + S:P + S:P:row +
   S:R:P + R:S:P:row, ex3.1a) # NO ALIAS
Model :
height \sim row + R + P + S + S:R + row:P + R:P + row:R:P + S:P +
   S:P:row + S:R:P + R:S:P:row
(76) MODEL
  • p94 Appendix 3.1
ex3.1b = read.table("C:/G/Rt/Split/spexvar3.txt", header=TRUE)
ex3.1b = af(ex3.1b, c("rep", "var", "nit", "row", "col"))
ANOVA(yield ~ rep + var + rep:var + nit + var:nit, ex3.1b)
```

```
$ANOVA
Response : yield
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
MODEL
               26 44017 1692.97 9.5603 4.779e-11 ***
               45
                  7969 177.08
RESIDUALS
CORRECTED TOTAL 71 51986
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value
                                  Pr(>F)
       5 15875.3 3175.1 17.9297 9.525e-10 ***
rep
        2 1786.4 893.2 5.0438 0.010557 *
var
rep:var 10 6013.3 601.3 3.3957 0.002251 **
        3 20020.5 6673.5 37.6856 2.458e-12 ***
           321.7
                    53.6 0.3028 0.932199
var:nit 6
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
        5 15875.3 3175.1 17.9297 9.525e-10 ***
rep
        2 1786.4 893.2 5.0438 0.010557 *
                  601.3 3.3957 0.002251 **
rep:var 10 6013.3
        3 20020.5 6673.5 37.6856 2.458e-12 ***
           321.7 53.6 0.3028 0.932199
var:nit 6
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value
                                   Pr(>F)
        5 15875.3 3175.1 17.9297 9.525e-10 ***
rep
        2 1786.4 893.2 5.0438 0.010557 *
var
rep:var 10 6013.3 601.3 3.3957 0.002251 **
        3 20020.5 6673.5 37.6856 2.458e-12 ***
                    53.6 0.3028 0.932199
var:nit 6
           321.7
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(77) MODEL
ANOVA(yield ~ rep + var + rep:var + nit + var:nit + row + col, ex3.1b)
```

37 48090 1299.7 11.341 6.734e-11 ***

Df Sum Sq Mean Sq F value

\$ANOVA

MODEL

Response : yield

Pr(>F)

```
RESIDUALS
               34
                    3896
                          114.6
CORRECTED TOTAL 71 51986
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value
        5 15875.3 3175.1 27.7056 4.391e-11 ***
rep
        2 1786.4
                  893.2 7.7939 0.0016359 **
var
                   601.3 5.2472 0.0001207 ***
rep:var 10 6013.3
        3 20020.5 6673.5 58.2331 1.754e-13 ***
nit
            321.7
                    53.6 0.4679 0.8271333
var:nit 6
                  100.1 0.8734 0.5575581
        9
            900.9
row
        2 3171.5 1585.7 13.8373 4.012e-05 ***
col
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
                                   Pr(>F)
        2 5942.5 2971.3 25.9273 1.449e-07 ***
rep
        2 2799.8 1399.9 12.2155 0.0001005 ***
                  249.4 2.1767 0.0926008 .
rep:var 4
            997.8
        3 12559.3 4186.4 36.5308 9.683e-11 ***
            477.8
                    79.6 0.6949 0.6553307
var:nit 6
        9
            945.0 105.0 0.9162 0.5230151
row
        2 3171.5 1585.7 13.8373 4.012e-05 ***
col
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
       Df Sum Sq Mean Sq F value
                                  Pr(>F)
        2 5942.5 2971.3 25.9273 1.449e-07 ***
rep
        2 2799.8 1399.9 12.2155 0.0001005 ***
var
            997.8
                  249.4 2.1767 0.0926008 .
rep:var 4
        3 11977.9 3992.6 34.8397 1.775e-10 ***
nit
                    79.6 0.6949 0.6553307
var:nit 6
            477.8
            945.0
                   105.0 0.9162 0.5230151
row
        2 3171.5 1585.7 13.8373 4.012e-05 ***
col
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(yield ~ rep + var + rep:var + nit + var:nit + row + col, ex3.1b),
     type=3, singular.ok=TRUE) # NOT OK for var
```

Note: model has aliased coefficients

```
Anova Table (Type III tests)
Response: yield
          Sum Sq Df F values
                                Pr(>F)
          5942.5 2 25.9273 1.449e-07 ***
var
             0.0 0
          11977.9 3 34.8397 1.775e-10 ***
nit
row
           945.0 9
                     0.9162
                                0.5230
          3171.5 2 13.8373 4.012e-05 ***
col
                      2.1767
                                0.0926 .
rep:var
           997.8 4
           477.8 6
                     0.6949
                                0.6553
var:nit
Residuals 3896.4 34
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
7.6 Example 4.1
(78) MODEL
ex4.1 = read.table("C:/G/Rt/Split/Ex4.1-example.txt", header=TRUE)
ex4.1 = af(ex4.1, c("row", "P", "column", "R", "S"))
ANOVA(height ~ P + column + column:P + R + P:R + column:R + column:R:P + S +
  P:S + column:S + column:S:P + R:S + R:S:column + R:S:P + R:S:P:column, ex4.1)
$ANOVA
Response : height
                Df Sum Sq Mean Sq F value Pr(>F)
               199 1710.2 8.5937
MODEL
RESIDUALS
                 0
                      0.0
CORRECTED TOTAL 199 1710.2
$`Type I`
            Df Sum Sq Mean Sq F value Pr(>F)
Ρ
             1 28.12 28.1250
column
             4 34.33 8.5825
             4 91.45 22.8625
P:column
R
             4 31.03 7.7575
P:R
             4 48.95 12.2375
column:R
            16 467.92 29.2450
            16 350.10 21.8813
P:column:R
S
             3
                 3.77 1.2583
P:S
             3
                 3.29 1.0983
            12 74.55 6.2125
column:S
```

P:column:S

12 47.03 3.9192

```
R:S
            12 36.65 3.0542
            48 197.40 4.1125
column:R:S
P:R:S
            12 26.33 2.1942
P:column:R:S 48 269.22 5.6087
$`Type II`
            Df Sum Sq Mean Sq F value Pr(>F)
Ρ
             1 28.13 28.1250
             4 34.33 8.5825
column
P:column
             4 91.45 22.8625
R
             4 31.03 7.7575
P:R
             4 48.95 12.2375
            16 467.92 29.2450
column:R
P:column:R
            16 350.10 21.8812
             3 3.77 1.2583
P:S
            3
               3.30 1.0983
            12 74.55 6.2125
column:S
P:column:S 12 47.03 3.9192
R:S
            12 36.65 3.0542
column:R:S
            48 197.40 4.1125
P:R:S
            12 26.33 2.1942
P:column:R:S 48 269.22 5.6087
$`Type III`
            Df Sum Sq Mean Sq F value Pr(>F)
             1 28.12 28.1250
             4 34.33 8.5825
column
             4 91.45 22.8625
P:column
             4 31.03 7.7575
R
P:R
            4 48.95 12.2375
column:R
            16 467.92 29.2450
P:column:R
            16 350.10 21.8813
S
            3 3.77 1.2583
P:S
            3 3.29 1.0983
column:S
            12 74.55 6.2125
P:column:S
           12 47.03 3.9192
R:S
            12 36.65 3.0542
column:R:S
            48 197.40 4.1125
P:R:S
            12 26.33 2.1942
P:column:R:S 48 269.22 5.6088
(79) MODEL
ANOVA (height ~ row + R + P + S + S:R + row:P + R:P + row:R:P + S:P + S:P:row +
   S:R:P + R:S:P:row, ex4.1)
```

\$ANOVA

```
Response : height
                Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               199 1710.2 8.5937
RESIDUALS
                 0
                      0.0
CORRECTED TOTAL 199 1710.2
$`Type I`
         Df Sum Sq Mean Sq F value Pr(>F)
          4 309.43 77.357
row
          4 31.03
                     7.758
R
Р
          1 28.12 28.125
S
          3
              3.77
                    1.258
R:S
         12 36.65
                     3.054
          4 130.25 32.563
row:P
          4 48.95 12.237
R:P
row:R:P
         32 504.12 15.754
P:S
          3 3.29
                    1.098
         24 171.28
row:P:S
                    7.137
R:P:S
         12 26.33
                     2.194
row:R:P:S 96 416.92
                     4.343
$`Type II`
         Df Sum Sq Mean Sq F value Pr(>F)
          4 309.43 77.357
row
R
          4 31.03
                    7.757
Ρ
          1 28.12 28.125
S
          3
              3.78
                    1.258
         12 36.65
R:S
                     3.054
          4 130.25 32.563
row:P
R:P
          4 48.95 12.238
row:R:P
         32 504.12 15.754
P:S
          3
              3.30
                    1.098
         24 171.28
row:P:S
                     7.137
R:P:S
         12 26.33
                     2.194
row:R:P:S 96 416.92
                     4.343
$`Type III`
         Df Sum Sq Mean Sq F value Pr(>F)
          4 309.43 77.358
row
          4 31.03
R
                     7.757
Ρ
          1 28.13 28.125
              3.78
S
          3
                    1.258
R:S
          12 36.65
                     3.054
          4 130.25 32.563
row:P
          4 48.95 12.237
R:P
row:R:P
         32 504.12 15.754
P:S
          3
              3.30
                    1.098
row:P:S
         24 171.28
                    7.137
```

```
R:P:S
         12 26.33
                    2.194
row:R:P:S 96 416.92
                    4.343
```

7.7 Example 5.1

(80) MODEL

```
ex5.1 = read.table("C:/G/Rt/Split/sbsp.txt", header=TRUE)
ex5.1 = af(ex5.1, c("R", "A", "C", "B", "Tx"))
ANOVA(Y \sim R + A + R:A + C + B + C:B + Tx + B:Tx, ex5.1)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value
MODEL
               20 193.583 9.6792 9.4176 2.969e-05 ***
RESIDUALS
               15 15.417 1.0278
CORRECTED TOTAL 35 209.000
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
    Df Sum Sq Mean Sq F value
                                 Pr(>F)
     2 33.500 16.7500 16.2973 0.0001734 ***
Α
     1 16.000 16.0000 15.5676 0.0012951 **
R:A
     2 32.167 16.0833 15.6486 0.0002133 ***
С
     2 0.500 0.2500 0.2432 0.7871141
         1.778 1.7778 1.7297 0.2081966
В
     1
         0.389 0.1944 0.1892 0.8295745
C:B
Tx
     5 103.333 20.6667 20.1081 3.63e-06 ***
B:Tx 5
         5.917 1.1833 1.1514 0.3770453
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
    Df Sum Sq Mean Sq F value
                                 Pr(>F)
     2 23.047 11.5236 11.2122 0.0010520 **
R
     1 12.375 12.3751 12.0406 0.0034285 **
R:A
     2 27.164 13.5819 13.2148 0.0004907 ***
         0.500 0.2500 0.2432 0.7871141
C
     2
В
     1
         1.778 1.7778 1.7297 0.2081966
C:B
         0.389 0.1944 0.1892 0.8295745
Tx
     5 103.333 20.6667 20.1081 3.63e-06 ***
B:Tx 5 5.917 1.1833 1.1514 0.3770453
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
$`Type III`
    Df Sum Sq Mean Sq F value
     2 22.451 11.2254 10.9220 0.0011828 **
R
     1 15.001 15.0013 14.5958 0.0016719 **
Α
R:A
     2 27.164 13.5819 13.2148 0.0004907 ***
С
         0.500 0.2500 0.2432 0.7871141
В
         1.778 1.7778 1.7297 0.2081966
C:B
         0.389 0.1944 0.1892 0.8295745
     5 103.333 20.6667 20.1081 3.63e-06 ***
B:Tx 5
         5.917 1.1833 1.1514 0.3770453
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(81) MODEL
ANOVA(Y \sim R + A + A:R + C + B + C:B + Tx + A:Tx, ex5.1)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value
MODEL
               20 194.188 9.7094 9.8323 2.254e-05 ***
               15 14.813 0.9875
RESIDUALS
CORRECTED TOTAL 35 209.000
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
    Df Sum Sq Mean Sq F value
     2 33.500 16.7500 16.9620 0.0001410 ***
R
     1 16.000 16.0000 16.2025 0.0011013 **
R:A
     2 32.167 16.0833 16.2869 0.0001739 ***
С
     2
         0.500 0.2500 0.2532 0.7795913
В
         1.778 1.7778 1.8003 0.1996385
C:B
         0.389 0.1944 0.1969 0.8233570
     5 103.333 20.6667 20.9283 2.813e-06 ***
A:Tx 5
         6.521 1.3042 1.3207 0.3078554
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
    Df Sum Sq Mean Sq F value
                                  Pr(>F)
     2 33.500 16.7500 16.9620 0.0001410 ***
     1 16.000 16.0000 16.2025 0.0011013 **
R:A
     2 32.167 16.0833 16.2869 0.0001739 ***
C
     2
         0.807 0.4037 0.4088 0.6716130
В
         1.757 1.7574 1.7797 0.2020905
     1
```

0.030 0.0150 0.0152 0.9849064

C:B

```
5 103.333 20.6667 20.9283 2.813e-06 ***
Tx
A:Tx 5 6.521 1.3042 1.3207 0.3078554
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
    Df Sum Sq Mean Sq F value
R
     2 33.500 16.7500 16.9620 0.0001410 ***
     1 16.000 16.0000 16.2025 0.0011013 **
Α
     2 32.167 16.0833 16.2869 0.0001739 ***
R:A
С
         0.780 0.3902 0.3952 0.6803789
         1.776 1.7756 1.7980 0.1999029
В
C:B
         0.030 0.0150 0.0152 0.9849064
     5 103.333 20.6667 20.9283 2.813e-06 ***
Tx
A:Tx 5
         6.521 1.3042 1.3207 0.3078554
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(82) MODEL
ANOVA(Y \sim R + A + A:R + C + B + B:C + Tx + A:Tx + B:Tx, ex5.1)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
               24 196.238 8.1766 7.0476 0.0008758 ***
MODEL
RESIDUALS
               11 12.762 1.1602
CORRECTED TOTAL 35 209.000
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
    Df Sum Sq Mean Sq F value
                                 Pr(>F)
     2 33.500 16.7500 14.4373 0.0008391 ***
     1 16.000 16.0000 13.7908 0.0034197 **
R:A
     2 32.167 16.0833 13.8626 0.0009856 ***
         0.500 0.2500 0.2155 0.8094766
C
         1.778 1.7778 1.5323 0.2415358
В
     1
C:B
         0.389 0.1944 0.1676 0.8478141
     5 103.333 20.6667 17.8131 6.055e-05 ***
Tx
A:Tx 5
         6.521 1.3042 1.1241 0.4027183
B:Tx 4
         2.050 0.5126 0.4418 0.7761730
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
    Df Sum Sq Mean Sq F value
                                 Pr(>F)
```

```
2 23.116 11.5581 9.9622 0.003396 **
     1 12.375 12.3751 10.6664 0.007519 **
Α
R:A
     2 27.426 13.7132 11.8197
                               0.001820 **
С
         0.970 0.4850 0.4180
                               0.668392
         1.757 1.7574 1.5148 0.244080
В
C:B
         0.085 0.0424 0.0366 0.964202
Tx
     5 103.333 20.6667 17.8131 6.055e-05 ***
         2.655 0.6636 0.5720 0.688652
         2.050 0.5126 0.4418 0.776173
B:Tx 4
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
    Df Sum Sq Mean Sq F value
                                 Pr(>F)
     2 22.186 11.0928 9.5611 0.003924 **
R
Α
     1 15.185 15.1853 13.0886 0.004042 **
R:A
     2 27.426 13.7132 11.8197
                               0.001820 **
С
     2 1.010 0.5049 0.4352 0.657839
В
         1.792 1.7922 1.5448 0.239751
         0.085 0.0424 0.0366 0.964202
C:B
     5 103.333 20.6667 17.8131 6.055e-05 ***
Tx
A:Tx 4
         2.655 0.6636 0.5720 0.688652
B:Tx 4
         2.050 0.5126 0.4418 0.776173
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
alias(Y \sim R + A + A:R + C + B + B:C + Tx + A:Tx + B:Tx, ex5.1)
Model:
Y \sim R + A + A:R + C + B + B:C + Tx + A:Tx + B:Tx
Complete:
      (Intercept) R1
                      R2
                           A1
                                C1
                                     C2
                                          B1
                                               Tx1 Tx2 Tx3 Tx4 Tx5 R1:A1
                          0 - 1/5
                                        0 - 1/5
                                                  0
                                                       0
                                                           0
                                                                0
B1:Tx5
                                   0
      R2:A1 C1:B1 C2:B1 A1:Tx1 A1:Tx2 A1:Tx3 A1:Tx4 A1:Tx5 B1:Tx1 B1:Tx2 B1:Tx3
         0
                     0
                         1/5
                                      1/5
B1:Tx5
               0
                               1/5
                                             1/5
                                                     -1
                                                           1/5
                                                                 1/5
                                                                        1/5
      B1:Tx4
B1:Tx5 1/5
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(Y \sim R + A + A:R + C + B + B:C + Tx + A:Tx + B:Tx, ex5.1),
     type=3, singular.ok=TRUE) # NOT OK
```

Note: model has aliased coefficients sums of squares computed by model comparison

Anova Table (Type III tests) Response: Y Sum Sq Df F values Pr(>F) 22.186 2 9.5611 0.003924 ** R 0.000 0 Α С 1.010 2 0.4352 0.657839 В 0.000 0 103.333 5 17.8131 6.055e-05 *** Tx R:A 27.426 2 11.8197 0.001820 ** C:B 0.085 2 0.0366 0.964202 2.655 4 0.5720 0.688652 A:TxB:Tx2.050 4 0.4418 0.776173 Residuals 12.762 11 Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1 (83) MODEL $ANOVA(Y \sim R + A + A:R + C + B + C:B + Tx + A:Tx + B:Tx + A:B:Tx, ex5.1)$ \$ANOVA Response : Y Df Sum Sq Mean Sq F value Pr(>F) 28 204.2 7.2929 10.635 0.001719 ** MODEL 7 RESIDUALS 4.8 0.6857 CORRECTED TOTAL 35 209.0 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 \$`Type I` Df Sum Sq Mean Sq F value Pr(>F) 2 33.500 16.7500 24.4271 0.0006969 *** R 1 16.000 16.0000 23.3333 0.0018985 ** Α R:A 2 32.167 16.0833 23.4549 0.0007889 *** С 2 0.500 0.2500 0.3646 0.7069339 1.778 1.7778 2.5926 0.1513998 В 1 2 0.389 0.1944 0.2836 0.7613494 C:B 5 103.333 20.6667 30.1389 0.0001357 *** Tx 6.521 1.3042 1.9019 0.2123307 A:Tx5 B:Tx 4 2.050 0.5126 0.7475 0.5896365 A:B:Tx 4 7.962 1.9905 2.9029 0.1038803

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

\$`Type II`

Df Sum Sq Mean Sq F value Pr(>F)

```
R
       2 31.838 15.9191 23.2153 0.0008139 ***
       1 12.375 12.3751 18.0470 0.0038017 **
Α
R:A
           2.017 2.0174 2.9420 0.1300172
       1
С
           0.500 0.2500 0.3645 0.7069558
           1.757 1.7574 2.5629 0.1534298
В
C:B
           0.644 0.6445 0.9399 0.3646045
Tx
        5 103.333 20.6667 30.1389 0.0001357 ***
A:Tx
           2.655 0.6636 0.9678 0.4812226
           2.050 0.5126 0.7475 0.5896365
B:Tx
           7.962 1.9905 2.9029 0.1038803
A:B:Tx 4
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
       Df Sum Sq Mean Sq F value
                                    Pr(>F)
R
       2 28.112 14.0562 20.4986 0.0011846 **
       1 14.655 14.6551 21.3720 0.0024176 **
Α
R:A
       1
          2.017 2.0174 2.9420 0.1300172
С
           0.471 0.2356 0.3436 0.7205632
В
           1.769 1.7694 2.5804 0.1522328
C:B
           0.644 0.6445 0.9399 0.3646045
       5 103.815 20.7630 30.2793 0.0001336 ***
           2.951 0.7378 1.0760 0.4358837
A:Tx
B:Tx
       4
           3.553 0.8882 1.2954 0.3579988
           7.962 1.9905 2.9029 0.1038803
A:B:Tx 4
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
alias(Y \sim R + A + A:R + C + B + C:B + Tx + A:Tx + B:Tx + A:B:Tx, ex5.1)
Model :
Y \sim R + A + A:R + C + B + C:B + Tx + A:Tx + B:Tx + A:B:Tx
Complete :
          (Intercept) R1
                          R2
                               A1
                                    C1
                                         C2
                                            B1
                                                   Tx1 Tx2 Tx3 Tx4 Tx5
B1:Tx5
                        0
                             0 -1/5
                                       0
                                            0 -1/5
                                                      0
                                                           0
                                                                0
                                                                     0
A1:B1:Tx5 -1/6
                        0
                             0
                                  0
                                            0
                                                 0 1/6 1/6 1/6 1/6 -5/6
                                       0
                             0 4/45 2/3 -2/3 4/45 -1/3 1/3 -1/3
                      2/3
A1:B1:Tx6
         R1:A1 R2:A1 C1:B1 C2:B1 A1:Tx1 A1:Tx2 A1:Tx3 A1:Tx4 A1:Tx5 B1:Tx1
B1:Tx5
            0
                  0
                        0
                              0
                                  1/5
                                         1/5
                                                1/5
                                                       1/5
                                                               -1
                                                                     1/5
A1:B1:Tx5
            0
                  0
                        0
                              0
                                    0
                                           0
                                                  0
                                                         0
                                                                0
                                                                       0
A1:B1:Tx6 -2/9
                4/9 -2/9 -2/9 -1/5
                                        -1/5
                                               -1/5
                                                       4/5
                                                                    -1/5
         B1:Tx2 B1:Tx3 B1:Tx4 A1:B1:Tx1 A1:B1:Tx2 A1:B1:Tx3 A1:B1:Tx4
          1/5
                                 0
                                           0
                                                     0
B1:Tx5
                 1/5
                        1/5
                                                               0
A1:B1:Tx5
                          0
                                 0
                                           0
                                                     0
                                                               0
            0
                   0
A1:B1:Tx6 -1/5
                -1/5
                        4/5
                                 1
                                          -1
                                                     1
                                                               0
```

```
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(Y \sim R + A + A:R + C + B + C:B + Tx + A:Tx + B:Tx + A:B:Tx, ex5.1),
      type=3, singular.ok=TRUE) # NOT OK
Note: model has aliased coefficients
      sums of squares computed by model comparison
Anova Table (Type III tests)
Response: Y
         Sum Sq Df F values
                              Pr(>F)
R
         11.643 1 16.9793 0.004456 **
          0.000 0
Α
С
          0.002 1
                     0.0025 0.961483
          0.000 0
Tx
         89.178 3 43.3503 6.87e-05 ***
R:A
          2.017 1 2.9420 0.130017
C:B
          0.644 1 0.9399 0.364604
A:Tx
          0.543 3 0.2640 0.849381
B:Tx
          3.384 3 1.6451 0.264128
          7.962 4
                     2.9029 0.103880
A:B:Tx
Residuals 4.800 7
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
7.8 Example 7.1
(84) MODEL
ex7.1 = read.table("C:/G/Rt/Split/asped.txt", header=TRUE)
ex7.1 = af(ex7.1, c("R", "G", "F"))
ANOVA(Y \sim R + G + R:G + F + F:G, ex7.1)
$ANOVA
Response : Y
                Df Sum Sq Mean Sq F value
MODEL
                95 577.83 6.0824 5.3082 1.068e-05 ***
RESIDUALS
                24 27.50 1.1458
CORRECTED TOTAL 119 605.33
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
                                Pr(>F)
    3 84.76 28.2528 24.6570 1.655e-07 ***
```

```
27 343.48 12.7216 11.1025 4.286e-08 ***
R:G 9 11.75 1.3056 1.1394
                                0.3749
    2 59.85 29.9250 26.1164 9.481e-07 ***
G:F 54 77.98 1.4441 1.2603
                                0.2718
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                               Pr(>F)
    3 5.75 1.9167 1.6727
                                0.1994
R
   27 343.48 12.7216 11.1025 4.286e-08 ***
R:G 9 11.75 1.3056 1.1394
                                0.3749
    2 59.85 29.9250 26.1164 9.481e-07 ***
G:F 54 77.98 1.4441 1.2603
                                0.2718
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
                               Pr(>F)
       5.75 1.9167 1.6727
R
                                0.1994
   27 343.48 12.7216 11.1025 4.286e-08 ***
G
R:G 9 11.75 1.3056 1.1394
                                0.3749
    2 50.51 25.2525 22.0385 3.686e-06 ***
G:F 54 77.98 1.4441 1.2603
                                0.2718
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(Y ~ R + G + R:G + F + F:G, ex7.1), type=3, singular.ok=TRUE) # NOT OK
Note: model has aliased coefficients
     sums of squares computed by model comparison
Anova Table (Type III tests)
Response: Y
          Sum Sq Df F values
                               Pr(>F)
           0.000 0
R
G
         202.417 3 58.8848 3.258e-11 ***
F
          50.505 2 22.0385 3.686e-06 ***
R:G
          11.750 9
                     1.1394
                                0.3749
          77.983 54
                     1.2603
                                0.2718
Residuals 27.500 24
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

7.9 Example 7.2

(85) MODEL

```
ex7.2 = read.table("C:/G/Rt/Split/aspedt.txt", header=TRUE)
ex7.2 = af(ex7.2, c("R", "T", "G"))
ANOVA(Y \sim R + T + R:T + G + G:T, ex7.2)
$ANOVA
Response : Y
                Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                99 538.70 5.4415 5.1892 1.286e-05 ***
                24 25.17 1.0486
RESIDUALS
CORRECTED TOTAL 123 563.87
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
    3 73.255 24.4183 23.2863 2.752e-07 ***
    3 32.000 10.6667 10.1722 0.0001645 ***
R:T 9 28.402 3.1558 3.0095 0.0149568 *
   21 309.908 14.7575 14.0734 7.158e-09 ***
T:G 63 95.140 1.5102 1.4401 0.1617931
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                                Pr(>F)
       4.229 1.4097 1.3444 0.2834998
R
Τ
    3 32.000 10.6667 10.1722 0.0001645 ***
R:T 9 10.854 1.2060 1.1501 0.3684706
  21 309.908 14.7575 14.0734 7.158e-09 ***
T:G 63 95.140 1.5102 1.4401 0.1617931
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
                                Pr(>F)
       4.229 1.4097 1.3444 0.283500
    3 22.668 7.5559 7.2056 0.001299 **
R:T 9 10.854 1.2060 1.1501 0.368471
   21 309.908 14.7575 14.0734 7.158e-09 ***
T:G 63 95.140 1.5102 1.4401 0.161793
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

7.10 Example 7.3

(86) MODEL

```
ex7.3 = read.table("C:/G/Rt/Split/assped.txt", header=TRUE)
ex7.3 = af(ex7.3, c("R", "T", "G", "F"))
ANOVA(Y ~ R + T + R:T + G + G:T + R:T:G + F + F:T + F:G + F:G:T, ex7.3)
$ANOVA
Response : Y
                Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               155 656.12 4.2330 13.446 3.997e-14 ***
                36 11.33 0.3148
RESIDUALS
CORRECTED TOTAL 191 667.45
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value
      3 27.06
                9.019 28.6489 1.203e-09 ***
R
Т
      1 10.55 10.547 33.5018 1.334e-06 ***
R:T
      3
          2.97
               0.991
                       3.1489 0.036705 *
G
     22 389.01 17.682 56.1668 < 2.2e-16 ***
T:G
     22 18.42 0.837
                       2.6601 0.004445 **
R:T:G 12
         8.78
                0.731
                       2.3235 0.025315 *
      2 164.28 82.141 260.9173 < 2.2e-16 ***
T:F
          0.84
               0.422
                       1.3401 0.274574
G:F
     44 23.47
                0.533
                       1.6943 0.053191 .
T:G:F 44 10.74 0.244
                       0.7753 0.790640
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
      3 12.49
                4.162 13.2206 5.655e-06 ***
R.
Τ
      1 10.55 10.547 33.5018 1.334e-06 ***
R:T
          1.15
               0.384
                       1.2206 0.316281
      3
G
     22 389.01 17.682 56.1668 < 2.2e-16 ***
T:G
     22 18.42
                       2.6601 0.004445 **
                0.837
R:T:G 12
          8.78
               0.731
                        2.3235 0.025315 *
      2 164.28 82.141 260.9173 < 2.2e-16 ***
          0.84
               0.422
                       1.3401 0.274574
     44 23.47
                 0.533
                        1.6943 0.053191 .
G:F
T:G:F 44 10.74 0.244
                       0.7753 0.790640
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
$`Type III`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
                4.162 13.2206 5.655e-06 ***
R
      3 12.49
      1 11.16 11.158 35.4430 8.021e-07 ***
      3
R:T
          1.15 0.384 1.2206 0.316281
G
     22 389.01 17.682 56.1668 < 2.2e-16 ***
T:G
     22 18.42 0.837
                       2.6601 0.004445 **
                0.731
R:T:G 12
          8.78
                       2.3235 0.025315 *
      2 120.56 60.282 191.4828 < 2.2e-16 ***
          0.82 0.411 1.3060 0.283432
T:F
G:F
     44 23.47 0.533 1.6943 0.053191 .
T:G:F 44 10.74 0.244 0.7753 0.790640
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(Y \sim R + T + R:T + G + G:T + R:T:G + F + F:T + F:G + F:G:T, ex7.3),
     type=3, singular.ok=TRUE) # NOT OK
Note: model has aliased coefficients
     sums of squares computed by model comparison
Anova Table (Type III tests)
Response: Y
          Sum Sq Df F values
                               Pr(>F)
R
           0.000 0
Т
           0.000 0
G
          73.444 2 116.6471 < 2.2e-16 ***
F
         120.563 2 191.4828 < 2.2e-16 ***
R:T
           0.000 0
T:G
           5.778 2
                    9.1765 0.0006018 ***
T:F
           0.822 2 1.3060 0.2834316
G:F
          23.469 44 1.6943 0.0531910 .
          8.778 12 2.3235 0.0253153 *
R:T:G
T:G:F
          10.740 44
                    0.7753 0.7906401
```

7.11 Example 8.1

Residuals 11.333 36

(87) MODEL

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

```
ex8.1 = read.table("C:/G/Rt/Split/asbed.txt", header=TRUE)
ex8.1 = af(ex8.1, c("R", "A", "B"))
ANOVA(Y \sim R + A + R:A + B + B:R + A:B + A:B:R, ex8.1)
$ANOVA
Response : Y
                Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               104 3951.8 37.999
RESIDUALS
                 0
                      0.0
CORRECTED TOTAL 104 3951.8
$`Type I`
     Df Sum Sq Mean Sq F value Pr(>F)
      2 1787.68 893.84
R
Α
     12 601.24
                  50.10
R:A
      6
         24.93
                  4.16
      8 156.87 19.61
В
R:B
      4 319.87
                  79.97
A:B
     60 1012.26 16.87
R:A:B 12 49.00
                4.08
$`Type II`
     Df Sum Sq Mean Sq F value Pr(>F)
R
      2 372.22 186.111
     12 601.24 50.103
Α
R:A
      6
         50.00 8.333
      8 156.87 19.609
В
         87.44 21.861
R:B
      4
     60 1012.26 16.871
R:A:B 12 49.00 4.083
$`Type III`
     Df Sum Sq Mean Sq F value Pr(>F)
R
      2 372.22 186.111
     12 572.31 47.692
Α
         50.00 8.333
R:A
      6
      8 185.85 23.231
R:B
      4
         87.44 21.861
     60 1012.26 16.871
A:B
R:A:B 12
          49.00 4.083
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(Y \sim R + A + R:A + B + B:R + A:B + A:B:R, ex8.1), type="III",
     singular.ok=TRUE) # NOT WORKING
```

7.12 Example 9.1

(88) MODEL

```
ex9.1 = read.table("C:/G/Rt/Split/Ex9.1-spex1.txt", header=TRUE)
ex9.1 = af(ex9.1, c("R", "A", "B"))
ANOVA(Y \sim R + A + R:A + B + A:B, ex9.1)
$ANOVA
Response : Y
              Df Sum Sq Mean Sq F value
                                         Pr(>F)
MODEL
              27 4920.8 182.251 10.594 5.927e-10 ***
              34 584.9 17.203
RESIDUALS
CORRECTED TOTAL 61 5505.6
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
                             Pr(>F)
    3 218.7 72.89 4.2369
                             0.01199 *
R
Α
    3 194.9
              64.96 3.7760
                             0.01930 *
R:A 9 186.9
              20.76 1.2070
                             0.32287
    3 4087.4 1362.47 79.2018 1.998e-15 ***
A:B 9 233.0
              25.88 1.5047 0.18602
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    3 157.8 52.61 3.0583 0.04134 *
R
Α
    3 227.2
              75.73 4.4020
                             0.01014 *
R:A 9 94.5
              10.50 0.6106
                             0.77932
    3 4087.4 1362.47 79.2018 1.998e-15 ***
A:B 9 233.0
              25.88 1.5047
                             0.18602
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
                             Pr(>F)
R
    3 171.0 57.01 3.3138
                             0.03143 *
    3 209.7
              69.92 4.0643
                             0.01431 *
R:A 9 94.5
              10.50 0.6106
                             0.77932
    3 4089.9 1363.29 79.2493 1.998e-15 ***
A:B 9 233.0 25.88 1.5047
                            0.18602
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

7.13 Example 9.2

(89) MODEL

```
ex9.2 = read.table("C:/G/Rt/Split/Ex9.2-sbex.txt", header=TRUE)
ex9.2 = af(ex9.2, c("rep", "hyb", "gen"))
ANOVA(yield ~ rep + hyb + rep:hyb + gen + gen:rep + gen:hyb, ex9.2)
$ANOVA
Response : yield
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               40 247.813 6.1953 4.4606 0.001119 **
               16 22.222 1.3889
RESIDUALS
CORRECTED TOTAL 56 270.035
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value
                                   Pr(>F)
        1 0.239 0.2388 0.1719 0.6839085
        9 66.796 7.4218 5.3437 0.0018370 **
hyb
rep:hyb 8 67.000 8.3750 6.0300 0.0011569 **
        2 36.351 18.1754 13.0863 0.0004293 ***
rep:gen 2 16.923 8.4616 6.0924 0.0107858 *
hyb:gen 18 60.504 3.3613 2.4201 0.0408545 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
                                   Pr(>F)
        1 0.167 0.1667 0.1200 0.7335481
rep
        9 66.796 7.4218 5.3437 0.0018370 **
hyb
rep:hyb 8 67.000 8.3750 6.0300 0.0011569 **
        2 36.351 18.1754 13.0863 0.0004293 ***
rep:gen 2 12.111 6.0556 4.3600 0.0308015 *
hyb:gen 18 60.504 3.3613 2.4201 0.0408545 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value
                                   Pr(>F)
        1 0.167 0.1667 0.1200 0.7335481
rep
        9 66.796 7.4218 5.3437 0.0018370 **
hyb
rep:hyb 8 67.000 8.3750 6.0300 0.0011569 **
        2 30.671 15.3356 11.0416 0.0009707 ***
rep:gen 2 12.111 6.0556 4.3600 0.0308015 *
hyb:gen 18 60.504 3.3613 2.4201 0.0408545 *
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(yield ~ rep + hyb + rep:hyb + gen + gen:rep + gen:hyb, ex9.2), type=3,
     singular.ok=TRUE) # NOT OK
Note: model has aliased coefficients
     sums of squares computed by model comparison
Anova Table (Type III tests)
Response: yield
         Sum Sq Df F values
                              Pr(>F)
          0.000 0
rep
         66.704 8 6.0033 0.0011847 **
hyb
         30.671 2 11.0416 0.0009707 ***
gen
         67.000 8 6.0300 0.0011569 **
rep:hyb
rep:gen
         12.111 2 4.3600 0.0308015 *
                     2.4201 0.0408545 *
hyb:gen
         60.504 18
Residuals 22.222 16
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
7.14 Example 10.1
(90) MODEL
ex10.1 = read.table("C:/G/Rt/Split/Ex10.1-new.txt", header=TRUE)
ex10.1 = af(ex10.1, c("Site", "Block", "A", "B", "C"))
f10.1 = Yield ~ Site/Block + A/Site + B/Site + A:B + A:B:Site + A:B:Site:Block +
       C + A:C + B:C + A:B:C + C:Site + A:C:Site + B:C:Site + A:B:C:Site
ANOVA(f10.1, ex10.1)
$ANOVA
Response : Yield
                       Sum Sq Mean Sq F value
                Df
                                               Pr(>F)
MODEL
               239 1639561484 6860090
                                        2162 < 2.2e-16 ***
RESIDUALS
               240
                       761522
                                 3173
CORRECTED TOTAL 479 1640323006
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
              Df
                     Sum Sq
                              Mean Sq
                                      F value Pr(>F)
```

```
Site
                      552717
                                 184239 5.8064e+01 < 2e-16 ***
                3
                                 882790 2.7822e+02 < 2e-16 ***
Site:Block
                8
                     7062320
                4 1387680917 346920229 1.0933e+05 < 2e-16 ***
Α
Site:A
                                   2839 8.9470e-01 0.55301
               12
                       34068
В
                1
                   100939695 100939695 3.1812e+04 < 2e-16 ***
                3
                                    539 1.6990e-01 0.91662
Site:B
                         1618
A:B
                4
                    31444008
                                7861002 2.4775e+03 < 2e-16 ***
Site:A:B
               12
                       33737
                                   2811 8.8600e-01 0.56185
                                   2596 8.1810e-01 0.84155
Site:Block:A:B 72
                      186911
                3
                    19356264
                                6452088 2.0334e+03 < 2e-16 ***
                                2172983 6.8483e+02 < 2e-16 ***
A:C
               12
                    26075792
                                7967129 2.5109e+03 < 2e-16 ***
B:C
                3
                    23901388
               12
                    41996729
                                3499727 1.1030e+03 < 2e-16 ***
A:B:C
Site:C
                9
                       47625
                                   5292 1.6677e+00 0.09747 .
Site:A:C
               36
                      104110
                                   2892 9.1140e-01 0.61768
                9
                                   6790 2.1400e+00 0.02701 *
Site:B:C
                       61111
Site:A:B:C
               36
                       82475
                                   2291 7.2200e-01 0.87941
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
                      Sum Sa
               Df
                                Mean Sq
                                           F value Pr(>F)
Site
                3
                      552717
                                 184239 5.8064e+01 < 2e-16 ***
                     7062320
                                 882790 2.7822e+02 < 2e-16 ***
Site:Block
                8
                4 1387680917 346920229 1.0933e+05 < 2e-16 ***
Δ
                                   2839 8.9470e-01 0.55301
               12
                        34068
Site:A
                   100939695 100939695 3.1812e+04 < 2e-16 ***
В
                1
Site:B
                3
                         1618
                                    539 1.6990e-01 0.91662
                                7861002 2.4775e+03 < 2e-16 ***
A:B
                4
                    31444008
Site:A:B
               12
                       33737
                                   2811 8.8600e-01 0.56185
Site:Block:A:B 72
                      186911
                                   2596 8.1810e-01 0.84155
                                6452088 2.0334e+03 < 2e-16 ***
C
                3
                    19356264
A:C
               12
                    26075792
                                2172983 6.8483e+02 < 2e-16 ***
B:C
                                7967129 2.5109e+03 < 2e-16 ***
                3
                    23901388
                                3499727 1.1030e+03 < 2e-16 ***
A:B:C
               12
                    41996729
Site:C
                9
                       47625
                                   5292 1.6677e+00 0.09747 .
Site:A:C
               36
                      104110
                                   2892 9.1140e-01 0.61768
Site:B:C
                9
                       61111
                                   6790 2.1400e+00 0.02701 *
                                   2291 7.2200e-01 0.87941
Site:A:B:C
               36
                       82475
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
               Df
                      Sum Sq
                                Mean Sq
                                           F value Pr(>F)
Site
                3
                      552717
                                 184239 5.8064e+01 < 2e-16 ***
Site:Block
                8
                     7062320
                                 882790 2.7822e+02 < 2e-16 ***
Α
                4 1387680917 346920229 1.0933e+05 < 2e-16 ***
Site:A
               12
                       34068
                                   2839 8.9470e-01 0.55301
```

```
100939695 100939695 3.1812e+04 < 2e-16 ***
                1
                                   539 1.6990e-01 0.91662
Site:B
                3
                        1618
A:B
                4
                    31444008
                               7861002 2.4775e+03 < 2e-16 ***
Site:A:B
               12
                                  2811 8.8600e-01 0.56185
                       33737
                                  2596 8.1810e-01 0.84155
Site:Block:A:B 72
                      186911
                               6452088 2.0334e+03 < 2e-16 ***
               3
                    19356264
A:C
               12
                    26075792
                               2172983 6.8483e+02 < 2e-16 ***
B:C
               3
                    23901388
                              7967129 2.5109e+03 < 2e-16 ***
A:B:C
                    41996729
                               3499727 1.1030e+03 < 2e-16 ***
               12
                                  5292 1.6677e+00 0.09747 .
Site:C
               9
                       47625
Site:A:C
                                 2892 9.1140e-01 0.61768
               36
                     104110
               9
                                 6790 2.1400e+00 0.02701 *
Site:B:C
                      61111
                                 2291 7.2200e-01 0.87941
Site:A:B:C
                       82475
               36
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(f10.1, ex10.1), type=3, singular.ok=TRUE) # NOT OK for Site:Block
```

Note: model has aliased coefficients sums of squares computed by model comparison

Anova Table (Type III tests)

```
Response: Yield
```

```
Sum Sq Df
                                F values Pr(>F)
Site
                   552717
                            3 5.8064e+01 < 2e-16 ***
               1387680917
                            4 1.0933e+05 < 2e-16 ***
Α
В
                100939695
                            1 3.1812e+04 < 2e-16 ***
C
                            3 2.0334e+03 < 2e-16 ***
                 19356264
                            0
Site:Block
                        0
Site:A
                    34068 12 8.9470e-01 0.55301
                            3 1.6990e-01 0.91662
Site:B
                     1618
A:B
                 31444008
                            4 2.4775e+03 < 2e-16 ***
                 26075792 12 6.8483e+02 < 2e-16 ***
A:C
B:C
                 23901388
                            3 2.5109e+03 < 2e-16 ***
Site:C
                    47625
                            9 1.6677e+00 0.09747 .
Site:A:B
                    33737 12 8.8600e-01 0.56185
A:B:C
                 41996729 12 1.1030e+03 < 2e-16 ***
Site:A:C
                   104110 36 9.1140e-01 0.61768
                            9 2.1400e+00 0.02701 *
Site:B:C
                    61111
Site:Block:A:B
                  186911 72 8.1810e-01 0.84155
                   82475 36 7.2200e-01 0.87941
Site:A:B:C
Residuals
                   761522 240
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

7.15 Example 10.2

(91) MODEL

```
ex10.2 = read.table("C:/G/Rt/Split/Ex10.2-spbsite.txt", header=TRUE)
ex10.2 = af(ex10.2, c("Site", "Block", "A", "B"))
ANOVA(Yield ~ Site + Site:Block + A + A:Site + A:Site:Block + B + B:Site +
           B:Site:Block + A:B + A:B:Site, ex10.2)
$ANOVA
Response : Yield
                 Df
                        Sum Sq Mean Sq F value
                                                   Pr(>F)
MODEL
                227 6370995084 28066058
                                          10814 < 2.2e-16 ***
RESIDUALS
                252
                        654049
                                   2595
CORRECTED TOTAL 479 6371649132
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
                                        F value
                                                   Pr(>F)
             Df
                    Sum Sq
                             Mean Sq
             2 523573968 261786984 1.0086e+05 < 2.2e-16 ***
Site
             9 3756646710 417405190 1.6082e+05 < 2.2e-16 ***
Site:Block
                  29288163
                             7322041 2.8211e+03 < 2.2e-16 ***
                               30987 1.1939e+01 1.998e-14 ***
Site:A
             8
                    247899
Site:Block:A 36
                   1783391
                               49539 1.9087e+01 < 2.2e-16 ***
             7 1937592291 276798899 1.0665e+05 < 2.2e-16 ***
Site:B
             14
                  15903698
                             1135978 4.3768e+02 < 2.2e-16 ***
Site:Block:B 63 105727288
                             1678211 6.4660e+02 < 2.2e-16 ***
             28
                                3255 1.2541e+00
                                                   0.1838
A:B
                     91141
             56
                    140534
                                2510 9.6690e-01
                                                   0.5461
Site:A:B
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
                             Mean Sq
                                        F value
            Df
                    Sum Sq
                                                   Pr(>F)
Site
              2 523573968 261786984 1.0086e+05 < 2.2e-16 ***
             9 3756646710 417405190 1.6082e+05 < 2.2e-16 ***
Site:Block
              4
                             7322041 2.8211e+03 < 2.2e-16 ***
Α
                  29288163
                               30987 1.1939e+01 1.998e-14 ***
Site:A
             8
                    247899
Site:Block:A 36
                   1783391
                               49539 1.9087e+01 < 2.2e-16 ***
             7 1937592291 276798899 1.0665e+05 < 2.2e-16 ***
                           1135978 4.3768e+02 < 2.2e-16 ***
             14
                 15903698
                             1678211 6.4660e+02 < 2.2e-16 ***
Site:Block:B 63
               105727288
A:B
             28
                    91141
                                3255 1.2541e+00
                                                   0.1838
Site:A:B
             56
                    140534
                                2510 9.6690e-01
                                                   0.5461
```

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

```
$`Type III`
            Df
                            Mean Sq
                                       F value
                                                  Pr(>F)
                   Sum Sq
Site
             2 523573968 261786984 1.0086e+05 < 2.2e-16 ***
             9 3756646710 417405190 1.6082e+05 < 2.2e-16 ***
Site:Block
                 29288163
                            7322041 2.8211e+03 < 2.2e-16 ***
Site:A
             8
                   247899
                               30987 1.1939e+01 1.998e-14 ***
Site:Block:A 36
                   1783391
                              49539 1.9087e+01 < 2.2e-16 ***
             7 1937592291 276798899 1.0665e+05 < 2.2e-16 ***
Site:B
                            1135978 4.3768e+02 < 2.2e-16 ***
             14
                 15903698
                            1678211 6.4660e+02 < 2.2e-16 ***
Site:Block:B 63 105727288
            28
                               3255 1.2541e+00
                                                  0.1838
A:B
                    91141
                               2510 9.6690e-01
Site:A:B
            56
                    140534
                                                  0.5461
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
7.16 Example 11.1
(92) MODEL
ex11.1 = read.table("C:/G/Rt/Split/Ex11.1-cov.txt", header=TRUE)
ex11.1 = af(ex11.1, c("R", "T", "S"))
ANOVA(Y \sim R + T + R:T + S + S:T, ex11.1)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               11
                      328 29.8182 3.1948 0.02875 *
                      112 9.3333
RESIDUALS
               12
CORRECTED TOTAL 23
                      440
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
                  24 2.5714 0.11765
    2
           48
R
Τ
    1
           24
                   24 2.5714 0.13479
R:T 2
                   8 0.8571 0.44880
           16
                  52 5.5714 0.01251 *
S
    3
         156
T:S 3
           84
                   28 3.0000 0.07277 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
          48
                  24 2.5714 0.11765
R
```

```
1
          24
                  24 2.5714 0.13479
R:T 2
                   8 0.8571 0.44880
          16
                  52 5.5714 0.01251 *
S
     3
         156
T:S 3
          84
                  28 3.0000 0.07277 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
                  24 2.5714 0.11765
R
          48
Т
     1
          24
                  24 2.5714 0.13479
R:T 2
                  8 0.8571 0.44880
          16
                  52 5.5714 0.01251 *
S
     3
         156
T:S 3
          84
                  28 3.0000 0.07277 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(93) MODEL
ANOVA(Z \sim R + T + R:T + S + S:T, ex11.1)
$ANOVA
Response : Z
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                      46 4.1818 2.5091 0.06452 .
               11
RESIDUALS
               12
                      20
                         1.6667
CORRECTED TOTAL 23
                      66
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    2
           9
                 4.5
                         2.7 0.1076
R
Т
    1
                 6.0
                         3.6 0.0821 .
           6
R:T 2
                 0.5
           1
                         0.3 0.7462
S
    3
           9
                 3.0
                         1.8 0.2008
T:S 3
          21
                 7.0
                         4.2 0.0301 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    2
                 4.5
                         2.7 0.1076
R
                         3.6 0.0821 .
    1
           6
                 6.0
R:T 2
           1
                 0.5
                         0.3 0.7462
S
     3
           9
                 3.0
                        1.8 0.2008
T:S 3
          21
                 7.0
                        4.2 0.0301 *
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
                 4.5
                        2.7 0.1076
Т
    1
           6
                 6.0
                        3.6 0.0821 .
R:T 2
           1
                0.5
                        0.3 0.7462
           9
                 3.0
                       1.8 0.2008
S
    3
T:S 3
          21
                7.0
                        4.2 0.0301 *
___
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(94) MODEL
ANOVA(Y \sim R + T + R:T + S + S:T + Z, ex11.1)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               12 342.45 28.5375
                                  3.218 0.03116 *
RESIDUALS
               11 97.55 8.8682
CORRECTED TOTAL 23 440.00
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    2 48.00 24.00 2.7063 0.11071
    1 24.00 24.00 2.7063 0.12820
R:T 2 16.00 8.00 0.9021 0.43373
    3 156.00 52.00 5.8637 0.01211 *
T:S 3 84.00
               28.00 3.1574 0.06828 .
               14.45 1.6294 0.22807
Z
    1 14.45
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    2 18.300 9.1500 1.0318 0.38844
    1 2.679 2.6786 0.3020 0.59359
R:T 2 9.450 4.7250 0.5328 0.60137
    3 79.196 26.3985 2.9768 0.07822 .
T:S 3 37.474 12.4915 1.4086 0.29234
    1 14.450 14.4500 1.6294 0.22807
```

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

```
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    2 20.209 10.1043 1.1394 0.35505
    1 6.104 6.1038 0.6883 0.42439
R:T 2 9.450 4.7250 0.5328 0.60137
    3 84.243 28.0810 3.1665 0.06782 .
T:S 3 37.474 12.4915 1.4086 0.29234
    1 14.450 14.4500 1.6294 0.22807
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
7.17 Example 11.2
(95) MODEL
ex11.2a = read.table("C:/G/Rt/Split/Ex11.2-sp3.txt", header=TRUE)
ex11.2a = af(ex11.2a, "A")
ex11.2a$MY = (ex11.2a$Y1 + ex11.2a$Y2)/sqrt(2)
ex11.2a$Z = 2*ex11.2a$Z/sqrt(2)
ANOVA(MY ~ Z + A, ex11.2a)
$ANOVA
Response : MY
               Df Sum Sq Mean Sq F value Pr(>F)
                2 234.639 117.32 9.5696 0.01953 *
MODEL
                           12.26
               5 61.298
RESIDUALS
CORRECTED TOTAL 7 295.937
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
Df Sum Sq Mean Sq F value Pr(>F)
Z 1 190.148 190.148 15.5101 0.01098 *
A 1 44.492 44.492 3.6291 0.11512
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
Df Sum Sq Mean Sq F value Pr(>F)
Z 1 166.577 166.577 13.5874 0.0142 *
A 1 44.492 44.492 3.6291 0.1151
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
```

```
Df Sum Sq Mean Sq F value Pr(>F)
Z 1 166.577 166.577 13.5874 0.0142 *
A 1 44.492 44.492 3.6291 0.1151
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
(96) MODEL
ex11.2b = read.table("C:/G/Rt/Split/Ex11.2-two.txt", header=TRUE)
ex11.2b = af(ex11.2b, c("sub", "A", "B"))
ANOVA(Y \sim A + A:sub + B + A:B, ex11.2b)
$ANOVA
Response: Y
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
MODEL
                9 382.06 42.451 39.954 0.0001135 ***
RESIDUALS
                6 6.38
                          1.062
CORRECTED TOTAL 15 388.44
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
      1 68.062 68.062 64.0588 0.0002029 ***
A:sub 6 227.875 37.979 35.7451 0.0001934 ***
      1 85.562 85.562 80.5294 0.0001070 ***
      1 0.562 0.562 0.5294 0.4942562
A:B
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
      1 68.062 68.062 64.0588 0.0002029 ***
A:sub 6 227.875 37.979 35.7451 0.0001934 ***
      1 85.562 85.562 80.5294 0.0001070 ***
A:B
      1 0.562 0.562 0.5294 0.4942562
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
      1 68.062 68.062 64.0588 0.0002029 ***
A:sub 6 227.875 37.979 35.7451 0.0001934 ***
      1 85.562 85.562 80.5294 0.0001070 ***
A:B
      1 0.562 0.562 0.5294 0.4942562
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

(97) MODEL

```
ex11.2c = read.table("C:/G/Rt/Split/Ex11.2-spcov2.txt", header=TRUE)
ex11.2c = af(ex11.2c, c("block", "whole", "split"))
ANOVA(Y ~ block + whole + block:whole + split + split:whole, ex11.2c)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                     328 29.8182 3.1948 0.02875 *
               11
RESIDUALS
               12
                     112 9.3333
CORRECTED TOTAL 23
                     440
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
           Df Sum Sq Mean Sq F value Pr(>F)
block
            2
                  48
                          24 2.5714 0.11765
whole
            1
                  24
                          24 2.5714 0.13479
block:whole 2
                  16
                           8 0.8571 0.44880
split
            3
                 156
                          52 5.5714 0.01251 *
whole:split 3
                          28 3.0000 0.07277 .
                  84
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
           Df Sum Sq Mean Sq F value Pr(>F)
                  48
                          24 2.5714 0.11765
block
whole
            1
                  24
                          24 2.5714 0.13479
                  16
                           8 0.8571 0.44880
block:whole
split
                          52 5.5714 0.01251 *
                 156
whole:split 3
                  84
                          28 3.0000 0.07277 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
           Df Sum Sq Mean Sq F value Pr(>F)
            2
                  48
                          24 2.5714 0.11765
block
whole
                  24
                          24 2.5714 0.13479
block:whole 2
                  16
                          8 0.8571 0.44880
            3
                 156
                          52 5.5714 0.01251 *
split
whole:split 3
                  84
                          28 3.0000 0.07277 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(98) MODEL
```

```
$ANOVA
Response : Z
               Df Sum Sq Mean Sq
                                   F value
                                              Pr(>F)
MODEL
               11
                      38 3.4545 3.5903e+15 < 2.2e-16 ***
                       0.0000
               12
RESIDUALS
CORRECTED TOTAL 23
                      38
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
           Df Sum Sq Mean Sq
                               F value Pr(>F)
            2 36.000 18.0000 1.8707e+16 <2e-16 ***
block
whole
            1 0.667 0.6667 6.9286e+14 <2e-16 ***
block:whole 2 1.333 0.6667 6.9286e+14 <2e-16 ***
            3 0.000 0.0000 0.0000e+00
split
whole:split 3 0.000 0.0000 0.0000e+00
                                            1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
           Df Sum Sq Mean Sq
                               F value Pr(>F)
block
            2 36.000 18.0000 1.8707e+16 <2e-16 ***
whole
            1 0.667 0.6667 6.9286e+14 <2e-16 ***
block:whole 2 1.333 0.6667 6.9286e+14 <2e-16 ***
            3 0.000 0.0000 0.0000e+00
split
whole:split 3 0.000 0.0000 0.0000e+00
                                            1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
           Df Sum Sq Mean Sq
                              F value Pr(>F)
            2 36.000 18.0000 1.8707e+16 <2e-16 ***
block
            1 0.667 0.6667 6.9286e+14 <2e-16 ***
whole
block:whole 2 1.333 0.6667 6.9286e+14 <2e-16 ***
split
            3 0.000 0.0000 0.0000e+00
whole:split 3 0.000 0.0000 0.0000e+00
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(99) MODEL
ANOVA(Y ~ block + whole + block: whole + split + split: whole + Z, ex11.2c)
```

ANOVA(Z ~ block + whole + block: whole + split + split: whole, ex11.2c)

```
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
                     328 29.8182 3.1948 0.02875 *
MODEL
               11
RESIDUALS
               12
                     112 9.3333
CORRECTED TOTAL 23
                     440
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
           Df Sum Sq Mean Sq F value Pr(>F)
            2
                  48
                         24 2.5714 0.11765
block
whole
                  24
                         24 2.5714 0.13479
            1
block:whole 2
                          8 0.8571 0.44880
                  16
            3
                 156
                         52 5.5714 0.01251 *
split
whole:split
                  84
                         28 3.0000 0.07277 .
Z
            0
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
           Df Sum Sq Mean Sq F value Pr(>F)
            2 13.286
                       6.643 0.7117 0.51039
block
whole
            1 16.000 16.000 1.7143 0.21495
block:whole 1 16.000 16.000 1.7143 0.21495
split
            3 156.000 52.000 5.5714 0.01251 *
whole:split 3
              84.000 28.000 3.0000 0.07277 .
            0
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
           Df Sum Sq Mean Sq F value Pr(>F)
block
            2 13.286
                       6.643 0.7117 0.51039
whole
            1 16.000 16.000 1.7143 0.21495
block:whole 1 16.000 16.000 1.7143 0.21495
            3 156.000 52.000 5.5714 0.01251 *
whole:split 3
              84.000 28.000 3.0000 0.07277 .
Z
            0
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

7.18 Example 11.3

(100) MODEL

```
ex11.3 = read.table("C:/G/Rt/Split/Ex11.3-sbcov.txt", header=TRUE)
ex11.3 = af(ex11.3, c("block", "A", "B"))
ANOVA(Y \sim block + A + block:A + B + block:B + A:B, ex11.3)
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               17 16.833 0.9902 1.9804 0.2038
                6 3.000 0.5000
RESIDUALS
CORRECTED TOTAL 23 19.833
$`Type I`
       Df Sum Sq Mean Sq F value Pr(>F)
        3 4.5000 1.5000 3.0000 0.11696
block
        1 1.5000 1.5000 3.0000 0.13397
block: A 3 0.5000 0.1667 0.3333 0.80220
        2 8.3333 4.1667 8.3333 0.01855 *
block:B 6 1.0000 0.1667 0.3333 0.89648
A:B
       2 1.0000 0.5000 1.0000 0.42188
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value Pr(>F)
        3 4.5000 1.5000 3.0000 0.11696
block
        1 1.5000 1.5000 3.0000 0.13397
block: A 3 0.5000 0.1667 0.3333 0.80220
        2 8.3333 4.1667 8.3333 0.01855 *
block:B 6 1.0000 0.1667 0.3333 0.89648
A:B
        2 1.0000 0.5000 1.0000 0.42188
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value Pr(>F)
        3 4.5000 1.5000 3.0000 0.11696
        1 1.5000 1.5000 3.0000 0.13397
block: A 3 0.5000 0.1667 0.3333 0.80220
        2 8.3333 4.1667 8.3333 0.01855 *
block:B 6 1.0000 0.1667 0.3333 0.89648
        2 1.0000 0.5000 1.0000 0.42188
A:B
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

(101) MODEL

```
ANOVA(Z \sim block + A + block:A + B + block:B + A:B, ex11.3)
$ANOVA
Response : Z
              Df Sum Sq Mean Sq F value Pr(>F)
MODEL
              17 31.167 1.83333
                                  3.3 0.07324 .
RESIDUALS
               6 3.333 0.55556
CORRECTED TOTAL 23 34.500
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value Pr(>F)
block
       3 6.8333 2.2778
                           4.1 0.06689 .
        1 6.0000 6.0000
                          10.8 0.01669 *
block:A 3 1.6667 0.5556
                          1.0 0.45472
        2 13.0000 6.5000 11.7 0.00850 **
block:B 6 3.6667 0.6111
                        1.1 0.45542
      2 0.0000 0.0000
A:B
                           0.0 1.00000
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value Pr(>F)
      3 6.8333 2.2778 4.1 0.06689 .
block
        1 6.0000 6.0000
                          10.8 0.01669 *
block: A 3 1.6667 0.5556
                          1.0 0.45472
        2 13.0000 6.5000 11.7 0.00850 **
block:B 6 3.6667 0.6111
                          1.1 0.45542
        2 0.0000 0.0000
A:B
                           0.0 1.00000
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value Pr(>F)
        3 6.8333 2.2778
                          4.1 0.06689 .
block
        1 6.0000 6.0000
                          10.8 0.01669 *
block:A 3 1.6667 0.5556
                          1.0 0.45472
        2 13.0000 6.5000
                         11.7 0.00850 **
block:B 6 3.6667 0.6111
                          1.1 0.45542
        2 0.0000 0.0000
                           0.0 1.00000
A:B
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

(102) MODEL

$ANOVA(Y \sim block + A + block:A + B + block:B + A:B + Z, ex11.3)$ \$ANOVA Response : Y Df Sum Sq Mean Sq F value Pr(>F) MODEL 18 17.8417 0.99120 2.4884 0.1589 RESIDUALS 5 1.9917 0.39833 CORRECTED TOTAL 23 19.8333 \$`Type I` Df Sum Sq Mean Sq F value Pr(>F) 3 4.5000 1.5000 3.7657 0.09378 . block 1 1.5000 1.5000 3.7657 0.10999 block: A 3 0.5000 0.1667 0.4184 0.74788 2 8.3333 4.1667 10.4603 0.01634 * block:B 6 1.0000 0.1667 0.4184 0.84059 2 1.0000 0.5000 1.2552 0.36163 A:B Z 1 1.0083 1.0083 2.5314 0.17248 Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1 \$`Type II` Df Sum Sq Mean Sq F value Pr(>F) 3 3.6203 1.20678 3.0296 0.1319 1 0.0000 0.00000 0.0000 1.0000 block: A 3 0.2583 0.08611 0.2162 0.8813 2 1.0317 0.51587 1.2951 0.3522 block:B 6 0.4210 0.07017 0.1762 0.9717 2 1.0000 0.50000 1.2552 0.3616 1 1.0083 1.00833 2.5314 0.1725 \$`Type III` Df Sum Sq Mean Sq F value Pr(>F) 3 3.6613 1.22045 3.0639 0.1297 block 1 0.0054 0.00536 0.0134 0.9122 block: A 3 0.2583 0.08611 0.2162 0.8813

2 0.7685 0.38427 0.9647 0.4423

2 1.0000 0.50000 1.2552 0.3616

1 1.0083 1.00833 2.5314 0.1725

block:B 6 0.4210 0.07017 0.1762 0.9717

A:B

7.

8 Hinkelmann & Kempthorne - Volume 1

Reference

• Hinkelmann K, Kempthorne O. Design and Analysis of Experiments Volume 1 Introduction to Experimental Design. 2e. John Wiley & Sons Inc. 2008.

8.1 Chapter 6

8.1.1 p202

(103) MODEL

```
v1p202 = read.table("C:/G/Rt/Kemp/v1p202.txt", head=TRUE)
v1p202 = af(v1p202,c("brand"))
ANOVA(miles ~ brand, v1p202) # OK
$ANOVA
Response : miles
              Df Sum Sq Mean Sq F value
               4 47.234 11.809 15.661 0.004924 **
MODEL
RESIDUALS
               5 3.770
                         0.754
CORRECTED TOTAL 9 51.004
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value Pr(>F)
brand 4 47.234 11.809 15.661 0.004924 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value Pr(>F)
brand 4 47.234 11.809 15.661 0.004924 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value Pr(>F)
brand 4 47.234 11.809 15.661 0.004924 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

8.1.2 p205

(104) MODEL

```
v1p205 = read.table("C:/G/Rt/Kemp/v1p205.txt", head=TRUE)
v1p205 = af(v1p205,c("brand", "car"))
ANOVA(miles ~ brand + car %in% brand, v1p205) # OK
$ANOVA
Response : miles
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
MODEL
               9 140.05 15.561
                                 80.21 1.017e-13 ***
RESIDUALS
               20
                    3.88
                          0.194
CORRECTED TOTAL 29 143.93
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          4 133.243 33.311 171.7053 3.553e-15 ***
brand
                            7.0137 0.0006214 ***
brand:car 5 6.803
                    1.361
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          4 133.243 33.311 171.7053 3.553e-15 ***
brand
brand:car 5 6.803
                            7.0137 0.0006214 ***
                    1.361
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          4 133.243 33.311 171.7053 3.553e-15 ***
brand
brand:car 5 6.803
                    1.361
                            7.0137 0.0006214 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.2 Chapter 7
```

8.2.1 p232

(105) MODEL

```
v1p232 = read.table("C:/G/Rt/Kemp/v1p232.txt", head=TRUE)
v1p232 = af(v1p232,c("trt"))
ANOVA(yield ~ trt, v1p232) # OK
$ANOVA
Response : yield
               Df Sum Sq Mean Sq F value Pr(>F)
                4 59.174 14.793 28.781 0.0012 **
MODEL
RESIDUALS
                5 2.570
                          0.514
CORRECTED TOTAL 9 61.744
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
trt 4 59.174 14.793 28.781 0.0012 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
trt 4 59.174 14.793 28.781 0.0012 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
trt 4 59.174 14.793 28.781 0.0012 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.2.2 p235
(106) MODEL
v1p235 = read.table("C:/G/Rt/Kemp/v1p235.txt", head=TRUE)
v1p235 = af(v1p235,c("density"))
ANOVA(yield ~ density, v1p235) # OK
$ANOVA
Response : yield
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
                4 88.007 22.0017 32.198 1.095e-05 ***
               10 6.833 0.6833
RESIDUALS
CORRECTED TOTAL 14 94.840
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value Pr(>F)
density 4 88.007 22.002 32.198 1.095e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
                                   Pr(>F)
density 4 88.007 22.002 32.198 1.095e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value
                                    Pr(>F)
density 4 88.007 22.002 32.198 1.095e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
8.3 Chapter 8
8.3.1 p265
(107) MODEL
v1p265 = read.table("C:/G/Rt/Kemp/v1p265.txt", head=TRUE)
v1p265 = af(v1p265, c("trt"))
ANOVA(y ~ trt + x, v1p265) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
                3 84.678 28.2260 36.866 4.941e-06 ***
               11 8.422 0.7656
RESIDUALS
CORRECTED TOTAL 14 93.100
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
trt 2 66.868 33.434 43.668 5.858e-06 ***
    1 17.810 17.810 23.262 0.0005333 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$`Type II`
   Df Sum Sq Mean Sq F value
                               Pr(>F)
trt 2 83.147 41.573 54.299 1.996e-06 ***
    1 17.810 17.810 23.262 0.0005333 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
                               Pr(>F)
trt 2 83.147 41.573 54.299 1.996e-06 ***
    1 17.810 17.810 23.262 0.0005333 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.3.2 p272
(108) MODEL
ANOVA(y ~ trt + x %in% trt, v1p265) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
                5 85.711 17.142 20.881 0.0001046 ***
RESIDUALS
                9 7.389
                           0.821
CORRECTED TOTAL 14 93.100
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
      2 66.868 33.434 40.7254 3.092e-05 ***
trt
trt:x 3 18.843 6.281 7.6509 0.007578 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                               Pr(>F)
      2 66.868 33.434 40.7254 3.092e-05 ***
trt
               6.281 7.6509 0.007578 **
trt:x 3 18.843
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value Pr(>F)
```

```
2 6.1392 3.0696 3.7390 0.065769 .
trt
trt:x 3 18.8433 6.2811 7.6509 0.007578 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
8.3.3 p273
(109) MODEL
ANOVA(y ~ trt + x + x %in% trt, v1p265) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
                5 85.711 17.142 20.881 0.0001046 ***
MODEL
                9 7.389
RESIDUALS
                          0.821
CORRECTED TOTAL 14 93.100
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value Pr(>F)
      2 66.868 33.434 40.7254 3.092e-05 ***
      1 17.810 17.810 21.6940 0.001189 **
trt:x 2 1.033 0.517 0.6294 0.554843
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
      2 83.147 41.573 50.6397 1.267e-05 ***
trt
      1 17.810 17.810 21.6940 0.001189 **
trt:x 2 1.033 0.517 0.6294 0.554843
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value Pr(>F)
      2 6.1392 3.0696 3.7390 0.065769 .
trt
      1 17.2071 17.2071 20.9597 0.001331 **
trt:x 2 1.0334 0.5167 0.6294 0.554843
___
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

8.4 Chapter 9

8.4.1 p344

(110) MODEL

(111) MODEL

```
v1p344 = read.table("C:/G/Rt/Kemp/v1p344.txt", head=TRUE)
v1p344 = af(v1p344,c("diet", "litter"))
ANOVA(gain ~ litter + diet, v1p344)
$ANOVA
Response : gain
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
                9 4915.6 546.18 15.544 3.363e-07 ***
MODEL
               20 702.8
                          35.14
RESIDUALS
CORRECTED TOTAL 29 5618.4
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
litter 5 4438.0 887.6 25.2608 5.298e-08 ***
       4 477.6
                  119.4 3.3981
                                 0.02824 *
diet
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
litter 5 4438.0 887.6 25.2608 5.298e-08 ***
                 119.4 3.3981
       4 477.6
diet
                                 0.02824 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value
                                 Pr(>F)
litter 5 4438.0 887.6 25.2608 5.298e-08 ***
                 119.4 3.3981
       4 477.6
                                 0.02824 *
diet
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.4.2 p349
```

```
v1p349 = read.table("C:/G/Rt/Kemp/v1p349.txt", head=TRUE)
v1p349 = af(v1p349,c("subject", "exercise"))
ANOVA(diast ~ subject + exercise + subject:exercise, v1p349) # OK
$ANOVA
Response : diast
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               14 1541.5 110.105 28.475 2.953e-08 ***
RESIDUALS
               15
                    58.0
                           3.867
CORRECTED TOTAL 29 1599.5
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
                Df Sum Sq Mean Sq F value
                                            Pr(>F)
                 4 905.13 226.283 58.5216 5.672e-09 ***
subject
                 2 591.27 295.633 76.4569 1.357e-08 ***
exercise
subject:exercise 8 45.07 5.633 1.4569
                                             0.2522
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
                Df Sum Sq Mean Sq F value
                                            Pr(>F)
                 4 905.13 226.283 58.5216 5.672e-09 ***
subject
exercise
                 2 591.27 295.633 76.4569 1.357e-08 ***
subject:exercise 8 45.07
                            5.633 1.4569
                                             0.2522
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
                Df Sum Sq Mean Sq F value
                                            Pr(>F)
                 4 905.13 226.283 58.5216 5.672e-09 ***
subject
                 2 591.27 295.633 76.4569 1.357e-08 ***
exercise
subject:exercise 8 45.07
                            5.633 1.4569
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.4.3 p354
(112) MODEL
v1p354 = read.table("C:/G/Rt/Kemp/v1p354.txt", head=TRUE)
v1p354 = af(v1p354,c("loc", "block", "HSF"))
ANOVA(height ~ loc + block %in% loc + HSF + loc:HSF + block:loc:HSF, v1p354) # OK
```

```
Response : height
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
               23 40782 1773.12 80.444 < 2.2e-16 ***
RESIDUALS
               24
                     529
                           22.04
CORRECTED TOTAL 47 41311
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
             Df Sum Sq Mean Sq F value
                                            Pr(>F)
              1 20336.3 20336.3 922.6314 < 2.2e-16 ***
loc
              6 1462.3
                          243.7 11.0573 6.408e-06 ***
loc:block
              2 12170.7 6085.3 276.0832 < 2.2e-16 ***
HSF
              2 6511.2 3255.6 147.7013 3.242e-14 ***
loc:HSF
                  301.2
loc:block:HSF 12
                           25.1
                                  1.1386
                                            0.3769
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
             Df Sum Sq Mean Sq F value
                                            Pr(>F)
              1 20336.3 20336.3 922.6314 < 2.2e-16 ***
loc
              6 1462.3
                          243.7 11.0573 6.408e-06 ***
loc:block
HSF
              2 12170.7 6085.3 276.0832 < 2.2e-16 ***
loc:HSF
              2 6511.2 3255.6 147.7013 3.242e-14 ***
loc:block:HSF 12
                  301.2
                           25.1
                                  1.1386
                                            0.3769
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
             Df Sum Sq Mean Sq F value
                                            Pr(>F)
              1 20336.3 20336.3 922.6314 < 2.2e-16 ***
loc
loc:block
              6 1462.3
                          243.7 11.0573 6.408e-06 ***
HSF
              2 12170.7 6085.3 276.0832 < 2.2e-16 ***
loc:HSF
              2 6511.2 3255.6 147.7013 3.242e-14 ***
                  301.2
loc:block:HSF 12
                           25.1
                                  1.1386
                                            0.3769
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.4.4 p357
(113) MODEL
v1p357 = read.table("C:/G/Rt/Kemp/v1p357.txt", head=TRUE)
v1p357 = af(v1p357, c("var", "N"))
ANOVA(y ~ var + N + var:N, v1p357) # OK
```

```
Response : y
               Df Sum Sq Mean Sq F value
MODEL
                9 4465.5 496.16 14.116 0.000142 ***
RESIDUALS
               10 351.5
                           35.15
CORRECTED TOTAL 19 4817.0
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
       1 140.5 140.45 3.9957 0.073519 .
var
      4 3393.7 848.42 24.1373 4.027e-05 ***
var:N 4 931.3 232.82 6.6238 0.007152 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
       1 140.5 140.45 3.9957 0.073519 .
var
      4 3393.7 848.43 24.1373 4.027e-05 ***
var:N 4 931.3 232.82 6.6238 0.007152 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
      1 140.5 140.45 3.9957 0.073519 .
var
      4 3393.7 848.42 24.1373 4.027e-05 ***
var:N 4 931.3 232.83 6.6238 0.007152 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.4.5 p361
(114) MODEL
v1p361 = read.table("C:/G/Rt/Kemp/v1p361.txt", head=TRUE)
v1p361 = af(v1p361,c("block", "trt"))
ANOVA(y ~ block + trt, v1p361) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                4 241.33 60.333 40.222 0.1176
RESIDUALS
                    1.50
                           1.500
                1
CORRECTED TOTAL 5 242.83
```

```
$`Type I`
     Df Sum Sq Mean Sq F value Pr(>F)
block 2 24.333 12.167 8.1111 0.24097
      2 217.000 108.500 72.3333 0.08286 .
trt
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value Pr(>F)
                54.0 36.000 0.11704
block 2
           108
      2
           217 108.5 72.333 0.08286 .
trt
___
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value Pr(>F)
block 2
           108
                  54.0 36.000 0.11704
      2
           217
                 108.5 72.333 0.08286 .
trt
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
y = model.frame(y ~ block + trt, v1p361)[,1]
x = ModelMatrix(y ~ block + trt, v1p361)
rx = lfit(x, y)
K = cbind(rep(1, 3), matrix(1/3, nrow=3, ncol=3), diag(3)); K
    [,1]
              [,2]
                        [,3]
                                  [,4] [,5] [,6] [,7]
[1,]
       1 0.3333333 0.3333333 0.3333333
                                              0
                                         1
       1 0.3333333 0.3333333 0.3333333
[2,]
                                              1
                                                   0
[3,]
       1 0.3333333 0.3333333 0.3333333
                                                   1
est(K, x$X, rx)
    Estimate Lower CL Upper CL Std. Error t value Df
                                                        Pr(>|t|)
[1,]
        29.5 17.334735 41.66526 0.9574271 30.81175 1 0.02065434
[2.]
        16.5 4.334735 28.66526 0.9574271 17.23369 1 0.03689905
[3,]
        13.5 1.334735 25.66526 0.9574271 14.10029 1 0.04507394
attr(,"Estimability")
[1] TRUE TRUE TRUE
8.5 Chapter 10
```

8.5.1 p405

(115) MODEL

```
v1p405 = read.table("C:/G/Rt/Kemp/v1p405.txt", head=TRUE)
v1p405 = af(v1p405,c("trt", "Row", "Col"))
ANOVA(y ~ Row + Col + trt, v1p405) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               12 4094.7 341.23 2.3416 0.07739 .
RESIDUALS
               12 1748.7 145.73
CORRECTED TOTAL 24 5843.4
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
Row 4 514.24 128.56 0.8822 0.50328
Col 4 1711.44 427.86 2.9360 0.06611 .
trt 4 1869.04 467.26 3.2064 0.05229 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
Row 4 514.24 128.56 0.8822 0.50328
Col 4 1711.44 427.86 2.9360 0.06611 .
trt 4 1869.04 467.26 3.2064 0.05229 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
Row 4 514.24 128.56 0.8822 0.50328
Col 4 1711.44 427.86 2.9360 0.06611 .
trt 4 1869.04 467.26 3.2064 0.05229 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.5.2 p408
(116) MODEL
v1p408 = read.table("C:/G/Rt/Kemp/v1p408.txt", head=TRUE)
v1p408 = af(v1p408,c("breed", "farm", "wclass", "dosage"))
ANOVA(response ~ breed + breed:farm + wclass + dosage + breed:dosage, v1p408) # OK
```

```
Response : response
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               16 4470.2 279.391 140.87 2.039e-13 ***
RESIDUALS
               15
                    29.7
                           1.983
CORRECTED TOTAL 31 4500.0
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
                                          Pr(>F)
            Df Sum Sq Mean Sq
                                F value
             1 3280.5 3280.5 1654.0336 < 2.2e-16 ***
breed
                  9.0
                          1.5
                                 0.7563
                                          0.6146
breed:farm
             6
             3 466.8
                        155.6
wclass
                                78.4454 2.142e-09 ***
             3 580.2 193.4
                                97.5210 4.596e-10 ***
dosage
                                22.4790 8.366e-06 ***
breed:dosage 3 133.8
                        44.6
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
            Df Sum Sq Mean Sq
                                F value
                                          Pr(>F)
             1 3280.5 3280.5 1654.0336 < 2.2e-16 ***
breed
                  9.0
                          1.5
                                 0.7563
breed:farm
             6
                                          0.6146
wclass
             3 466.7
                        155.6
                                78.4454 2.142e-09 ***
             3 580.2
                       193.4
                                97.5210 4.596e-10 ***
dosage
breed:dosage 3 133.8
                        44.6
                                22.4790 8.366e-06 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
            Df Sum Sq Mean Sq
                                F value
                                          Pr(>F)
breed
             1 3280.5 3280.5 1654.0336 < 2.2e-16 ***
breed:farm
             6
                  9.0
                          1.5
                                0.7563
                                           0.6146
wclass
             3 466.8
                        155.6
                                78.4454 2.142e-09 ***
             3 580.3 193.4
                                97.5210 4.596e-10 ***
dosage
                                22.4790 8.366e-06 ***
breed:dosage 3 133.7
                        44.6
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.5.3 p410
(117) MODEL
v1p410 = read.table("C:/G/Rt/Kemp/v1p410.txt", head=TRUE)
v1p410$carry = ifelse(v1p410$carry == 0, 3, v1p410$carry)
v1p410 = af(v1p410,c("period", "sequence", "steer", "trt", "carry"))
ANOVA(y ~ period + sequence + steer: sequence + trt + carry, v1p410) # OK
```

```
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                             Pr(>F)
MODEL
               17 1302.51 76.618 8.7402 1.572e-05 ***
                            8.766
RESIDUALS
               18 157.79
CORRECTED TOTAL 35 1460.31
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
              Df Sum Sq Mean Sq F value
                                           Pr(>F)
               2 292.06 146.028 16.6580 8.038e-05 ***
period
               5 326.47 65.294 7.4484 0.0006072 ***
sequence
sequence:steer 6 118.50 19.750 2.2530 0.0849122 .
trt
               2 549.06 274.528 31.3166 1.377e-06 ***
               2 16.43
                          8.215 0.9372 0.4100385
carry
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
              Df Sum Sq Mean Sq F value
               2 172.31 86.154 9.8279 0.0013030 **
period
sequence
               5 318.69 63.738 7.2709 0.0006954 ***
sequence:steer 6 118.50 19.750 2.2530 0.0849122 .
               2 440.61 220.304 25.1311 6.164e-06 ***
trt
                          8.215 0.9372 0.4100385
               2 16.43
carry
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
              Df Sum Sq Mean Sq F value
                                           Pr(>F)
               2 172.31 86.154 9.8279 0.0013030 **
period
sequence
               5 318.69 63.738 7.2709 0.0006954 ***
sequence:steer 6 118.50 19.750 2.2530 0.0849122 .
               2 440.61 220.304 25.1311 6.164e-06 ***
trt
carry
               2 16.43
                          8.215 0.9372 0.4100385
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(y ~ period + sequence + steer:sequence + trt + carry, v1p410), type=3,
     singular.ok=TRUE) # NOT OK for sequence
```

Note: model has aliased coefficients sums of squares computed by model comparison

Anova Table (Type III tests)

```
Response: y
              Sum Sq Df F values
                                    Pr(>F)
              172.31 2
                          9.8279 0.001303 **
period
sequence
                0.00 0
              440.61 2 25.1311 6.164e-06 ***
trt
               16.43 2
                          0.9372 0.410038
carry
sequence:steer 118.50 6
                          2.2530 0.084912 .
Residuals
              157.79 18
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.6 Chapter 11
8.6.1 p432
(118) MODEL
v1p432 = read.table("C:/G/Rt/Kemp/v1p432.txt", head=TRUE)
v1p432 = af(v1p432,c("V", "Block", "A", "B", "C"))
ANOVA(Y \sim V + Block:V + A + B + A:B + V:A + V:B + V:A:B + Block:A:V + Block:B:V,
   v1p432) # OK
$ANOVA
Response: Y
                Df Sum Sq Mean Sq F value
                94 261663 2783.65 30.584 2.065e-14 ***
MODEL
RESIDUALS
                25
                     2275
                            91.02
CORRECTED TOTAL 119 263939
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
                                       Pr(>F)
          4 102743
                     25686 282.2094 < 2.2e-16 ***
V:Block
         25 50019
                      2001 21.9825 1.588e-11 ***
Α
          1 18451
                     18451 202.7233 1.692e-13 ***
В
          1 78541
                     78541 862.9280 < 2.2e-16 ***
A:B
          1
               108
                       108
                             1.1899
                                      0.28575
          4 3751
                       938 10.3023 4.532e-05 ***
V:A
V:B
          4
               307
                        77
                             0.8421
                                     0.51168
V:A:B
          4 1495
                       374
                             4.1058
                                      0.01081 *
V:Block:A 25
              3416
                       137
                             1.5011
                                      0.15818
V:Block:B 25 2833
                       113
                             1.2451
                                      0.29390
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

```
$`Type II`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          4 102743
                     25686 282.2094 < 2.2e-16 ***
         25 50019
                     2001 21.9825 1.588e-11 ***
V:Block
          1 18451
                     18451 202.7233 1.692e-13 ***
В
          1 78541
                     78541 862.9280 < 2.2e-16 ***
A:B
               108
                       108
                             1.1899
                                     0.28575
V:A
          4
              3751
                       938 10.3023 4.532e-05 ***
               307
V:B
          4
                        77
                             0.8421
                                     0.51168
V:A:B
          4 1495
                       374
                             4.1058
                                     0.01081 *
              3416
                             1.5011
                                     0.15818
V:Block:A 25
                       137
V:Block:B 25
              2833
                       113
                             1.2451
                                     0.29390
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
V
          4 102743
                     25686 282.2094 < 2.2e-16 ***
V:Block
         25 50019
                      2001 21.9825 1.588e-11 ***
                     18451 202.7233 1.692e-13 ***
          1 18451
В
          1 78541
                     78541 862.9280 < 2.2e-16 ***
A:B
          1
               108
                       108
                             1.1899
                                     0.28575
V:A
          4
              3751
                       938 10.3023 4.532e-05 ***
V:B
          4
              307
                       77
                             0.8421
                                     0.51168
V:A:B
          4 1495
                       374
                             4.1058
                                     0.01081 *
V:Block:A 25 3416
                             1.5011
                                     0.15818
                       137
V:Block:B 25 2833
                       113
                             1.2451
                                     0.29390
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.6.2 p434
(119) MODEL
ANOVA(Y ~ V + Block:V + A + B + A:B + V:A + V:B + V:A:B, v1p432) # OK
$ANOVA
Response : Y
                Df Sum Sq Mean Sq F value
                                            Pr(>F)
                44 255415 5804.9 51.075 < 2.2e-16 ***
MODEL
                     8524
                            113.7
RESIDUALS
                75
CORRECTED TOTAL 119 263939
```

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

```
$`Type I`
       Df Sum Sq Mean Sq F value Pr(>F)
                   25686 225.9988 < 2.2e-16 ***
        4 102743
V:Block 25 50019
                  2001 17.6040 < 2.2e-16 ***
        1 18451
                 18451 162.3447 < 2.2e-16 ***
        1 78541
                 78541 691.0494 < 2.2e-16 ***
A:B
             108
                     108
                          0.9529
                                   0.33212
V:A
            3751
                     938
                           8.2503 1.435e-05 ***
V:B
             307
                      77
                           0.6744
                                   0.61182
            1495
                     374
                           3.2880
                                   0.01541 *
V:A:B
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
        4 102743
                   25686 225.9988 < 2.2e-16 ***
V:Block 25 50019
                   2001 17.6040 < 2.2e-16 ***
        1 18451
                 18451 162.3447 < 2.2e-16 ***
В
        1 78541
                  78541 691.0494 < 2.2e-16 ***
A:B
        1
             108
                     108
                          0.9529
                                  0.33212
                     938
V:A
        4
            3751
                          8.2503 1.435e-05 ***
V:B
             307
                      77
                          0.6744
                                   0.61182
        4
V:A:B
            1495
                     374
                           3.2880
                                   0.01541 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value
                                    Pr(>F)
                  25686 225.9988 < 2.2e-16 ***
        4 102743
V:Block 25 50019
                  2001 17.6040 < 2.2e-16 ***
        1 18451
                  18451 162.3447 < 2.2e-16 ***
Α
В
        1 78541
                  78541 691.0494 < 2.2e-16 ***
                          0.9529
A:B
        1
             108
                     108
                                   0.33212
V:A
            3751
                     938
                          8.2503 1.435e-05 ***
V:B
             307
                      77
                          0.6744
        4
                                   0.61182
V:A:B
            1495
                     374
                           3.2880
                                   0.01541 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.6.3 p438
(120) MODEL
```

ANOVA(Y ~ V + Block:V + C + V:C, v1p432) # OK

```
Response : Y
                Df Sum Sq Mean Sq F value Pr(>F)
                44 255415 5804.9 51.075 < 2.2e-16 ***
MODEL
RESIDUALS
                75
                     8524
                           113.7
CORRECTED TOTAL 119 263939
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value
                                    Pr(>F)
        4 102743
                  25686 225.9988 < 2.2e-16 ***
V:Block 25 50019 2001 17.6040 < 2.2e-16 ***
        3 97100
                   32367 284.7823 < 2.2e-16 ***
V:C
       12
            5552
                     463
                          4.0709 7.23e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
                                    Pr(>F)
        4 102743 25686 225.9988 < 2.2e-16 ***
V:Block 25 50019 2001 17.6040 < 2.2e-16 ***
        3 97100
                   32367 284.7823 < 2.2e-16 ***
V:C
       12
            5552
                     463
                          4.0709 7.23e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value
                                    Pr(>F)
        4 102743
                  25686 225.9988 < 2.2e-16 ***
V:Block 25 50019
                   2001 17.6040 < 2.2e-16 ***
        3 97100
                   32367 284.7823 < 2.2e-16 ***
C
V:C
       12
            5552
                     463
                          4.0709 7.23e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.6.4 p444
(121) MODEL
v1p444 = v1p432[v1p432$Block==5,]
ANOVA(Y ~ V + A + B + A:B + V:A, v1p444) # OK
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
```

11 39278 3570.8 59.787 1.897e-06 ***

MODEL

```
RESIDUALS
                8
                     478
                           59.7
CORRECTED TOTAL 19 39756
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
    4 19287.7 4821.9 80.7355 1.674e-06 ***
    1 3380.0 3380.0 56.5927 6.780e-05 ***
    1 14045.0 14045.0 235.1612 3.247e-07 ***
В
A:B 1 115.2
              115.2 1.9288 0.202326
V:A 4 2450.5 612.6 10.2574 0.003081 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                                 Pr(>F)
    4 19287.7 4821.9 80.7355 1.674e-06 ***
Α
    1 3380.0 3380.0 56.5927 6.780e-05 ***
    1 14045.0 14045.0 235.1612 3.247e-07 ***
A:B 1
       115.2
               115.2 1.9288 0.202326
V:A 4 2450.5
              612.6 10.2574 0.003081 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
                                 Pr(>F)
    4 19287.7 4821.9 80.7355 1.674e-06 ***
    1 3380.0 3380.0 56.5927 6.780e-05 ***
    1 14045.0 14045.0 235.1612 3.247e-07 ***
        115.2
               115.2
                       1.9288 0.202326
A:B 1
V:A 4 2450.5
              612.6 10.2574 0.003081 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.6.5 p482
(122) MODEL
v1p482 = read.table("C:/G/Rt/Kemp/v1p482.txt", head=TRUE)
v1p482 = af(v1p482,c("block", "A", "B"))
ANOVA(y ~ block + A + B + A:B, v1p482) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
```

```
MODEL
                8 156.88 19.6094 9.8871 9.377e-05 ***
RESIDUALS
               15 29.75 1.9833
CORRECTED TOTAL 23 186.62
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
                                 Pr(>F)
block 5 108.38 21.675 10.9286 0.0001415 ***
          4.00 4.000 2.0168 0.1760166
       1 42.25 42.250 21.3025 0.0003365 ***
В
          2.25 2.250 1.1345 0.3036727
A:B
       1
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
block 5 31.417 6.283 3.1681 0.0377804 *
       1 4.000 4.000 2.0168 0.1760166
       1 42.250 42.250 21.3025 0.0003365 ***
A:B
      1 2.250 2.250 1.1345 0.3036727
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
block 5 31.417 6.283 3.1681 0.0377804 *
      1 4.000 4.000 2.0168 0.1760166
       1 42.250 42.250 21.3025 0.0003365 ***
A:B
      1 2.250 2.250 1.1345 0.3036727
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.7 Chapter 12
8.7.1 p525
(123) MODEL
v1p525 = read.table("C:/G/Rt/Kemp/v1p525.txt", head=TRUE)
REG(y \sim x1 + x2 + x3, v1p525)
           Estimate Std. Error Df t value Pr(>|t|)
(Intercept) 14.2125 0.10383 12 136.8787 < 2.2e-16 ***
             0.7875
                       0.10383 12
                                   7.5843 6.465e-06 ***
x1
x2
             1.3875
                       0.10383 12 13.3628 1.446e-08 ***
```

```
1.6625
                       0.10383 12 16.0113 1.839e-09 ***
x3
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
ANOVA(y ~ x1 + x2 + x3, v1p525) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                3 84.948 28.3158 164.15 5.26e-10 ***
RESIDUALS
               12 2.070 0.1725
CORRECTED TOTAL 15 87.018
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
  Df Sum Sq Mean Sq F value
x1 1 9.923 9.923 57.522 6.465e-06 ***
x2 1 30.803 30.803 178.565 1.446e-08 ***
x3 1 44.223 44.223 256.362 1.839e-09 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                              Pr(>F)
x1 1 9.923 9.923 57.522 6.465e-06 ***
x2 1 30.803 30.803 178.565 1.446e-08 ***
x3 1 44.223 44.223 256.362 1.839e-09 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
  Df Sum Sq Mean Sq F value
                              Pr(>F)
x1 1 9.923 9.923 57.522 6.465e-06 ***
x2 1 30.803 30.803 178.565 1.446e-08 ***
x3 1 44.223 44.223 256.362 1.839e-09 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
8.7.2 p527
(124) MODEL
v1p527 = read.table("C:/G/Rt/Kemp/v1p527.txt", head=TRUE)
ANOVA(y ~ A + B, v1p527) # OK
```

```
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                2 22.99 11.4952 4.8917 0.04686 *
                7 16.45 2.3499
RESIDUALS
CORRECTED TOTAL 9 39.44
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 10.364 10.364 4.4103 0.07386 .
B 1 12.626 12.626 5.3730 0.05355 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
 Df Sum Sq Mean Sq F value Pr(>F)
A 1 10.364 10.364 4.4103 0.07386 .
B 1 12.626 12.626 5.3730 0.05355 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
 Df Sum Sq Mean Sq F value Pr(>F)
A 1 10.364 10.364 4.4103 0.07386 .
B 1 12.626 12.626 5.3730 0.05355 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
8.7.3 p529
(125) MODEL
v1p529 = read.table("C:/G/Rt/Kemp/v1p529.txt", head=TRUE)
ANOVA(y ~ A + B + I(A*A) + I(B*B) + I(A*B), v1p529) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                5 35.713 7.1427 6.7928 0.01857 *
MODEL
                6 6.309 1.0515
RESIDUALS
CORRECTED TOTAL 11 42.023
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
$`Type I`
        Df Sum Sq Mean Sq F value Pr(>F)
         1 11.6012 11.6012 11.0329 0.01597 *
Α
         1 12.6263 12.6263 12.0077 0.01338 *
I(A * A) 1 1.7167 1.7167 1.6326 0.24855
I(B * B) 1 5.3593 5.3593 5.0967 0.06476 .
I(A * B) 1 4.4100 4.4100 4.1940 0.08649 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value Pr(>F)
         1 11.6012 11.6012 11.0329 0.01597 *
         1 12.6263 12.6263 12.0077 0.01338 *
I(A * A) 1 5.5468 5.5468 5.2750 0.06137 .
I(B * B) 1 5.3593 5.3593 5.0967 0.06476 .
I(A * B) 1 4.4100 4.4100 4.1940 0.08649 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
        Df Sum Sq Mean Sq F value Pr(>F)
         1 11.6012 11.6012 11.0329 0.01597 *
         1 12.6263 12.6263 12.0077 0.01338 *
I(A * A) 1 5.5468 5.5468 5.2750 0.06137.
I(B * B) 1 5.3593 5.3593 5.0967 0.06476 .
I(A * B) 1 4.4100 4.4100 4.1940 0.08649 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.8 Chapter 13
8.8.1 p563
(126) MODEL
v1p563 = read.table("C:/G/Rt/Kemp/v1p563.txt", head=TRUE)
v1p563 = af(v1p563, c("rep", "A", "B"))
ANOVA(y ~ rep + A + rep:A + B + A:B, v1p563) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
               14 2097.08 149.792 17.228 8.385e-05 ***
MODEL
RESIDUALS
                9
                    78.25
                           8.694
CORRECTED TOTAL 23 2175.33
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
      3 1241.00 413.67 47.5783 7.606e-06 ***
rep
      2 353.08 176.54 20.3051 0.0004613 ***
rep:A 6 192.25
                 32.04 3.6853 0.0393557 *
      1 216.00 216.00 24.8435 0.0007550 ***
                  47.38 5.4489 0.0281496 *
A:B
          94.75
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
      3 1241.00 413.67 47.5783 7.606e-06 ***
rep
      2 353.08 176.54 20.3051 0.0004613 ***
Α
rep:A 6 192.25
                32.04 3.6853 0.0393557 *
      1 216.00 216.00 24.8435 0.0007550 ***
В
A:B
      2 94.75
                47.38 5.4489 0.0281496 *
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
      3 1241.00 413.67 47.5783 7.606e-06 ***
rep
      2 353.08 176.54 20.3051 0.0004613 ***
rep:A 6 192.25
                32.04 3.6853 0.0393557 *
      1 216.00 216.00 24.8435 0.0007550 ***
A:B
         94.75
                47.38 5.4489 0.0281496 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.8.2 p566
(127) MODEL
v1p566 = read.table("C:/G/Rt/Kemp/v1p566.txt", head=TRUE)
v1p566 = af(v1p566, c("subject", "A", "B"))
ANOVA(y ~ A + B + A:B, v1p566) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
                5 1469.58 293.92
                                    86.2 5.592e-09 ***
RESIDUALS
               12
                    40.92
                            3.41
```

```
CORRECTED TOTAL 17 1510.50
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
                                 Pr(>F)
    2 1390.04 695.02 203.8350 5.466e-10 ***
       76.06
                76.06 22.3055 0.0004945 ***
A:B 2
         3.49
                1.74 0.5112 0.6122667
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
     2 1390.04 695.02 203.8350 5.466e-10 ***
       76.06
               76.06 22.3055 0.0004945 ***
A:B 2
         3.49
                1.74 0.5112 0.6122667
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value
    2 1390.04 695.02 203.8350 5.466e-10 ***
       79.00
               79.00 23.1700 0.0004237 ***
A:B 2
         3.49
               1.74 0.5112 0.6122667
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
8.9 Chapter 14
8.9.1 p581
(128) MODEL
v1p581 = read.table("C:/G/Rt/Kemp/v1p581.txt", head=TRUE)
v1p581 = af(v1p581, c("drug", "person", "time"))
ANOVA(rate ~ drug + person:drug + time + drug:time, v1p581) # OK
$ANOVA
Response : rate
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               23 2449.5 106.500 12.733 3.469e-11 ***
RESIDUALS
               36 301.1
                           8.364
CORRECTED TOTAL 59 2750.6
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

```
$`Type I`
           Df Sum Sq Mean Sq F value
                                         Pr(>F)
            2 337.60 168.800 20.1820 1.323e-06 ***
drug
drug:person 12 1498.50 124.875 14.9303 1.501e-10 ***
time
            3 256.33 85.444 10.2159 5.230e-05 ***
drug:time
            6 357.07 59.511 7.1152 4.707e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
                                         Pr(>F)
           Df Sum Sq Mean Sq F value
            2 337.60 168.800 20.1820 1.323e-06 ***
drug
drug:person 12 1498.50 124.875 14.9303 1.501e-10 ***
            3 256.33 85.444 10.2159 5.230e-05 ***
time
drug:time
            6 357.07 59.511 7.1152 4.707e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
           Df Sum Sq Mean Sq F value
            2 337.60 168.800 20.1820 1.323e-06 ***
drug
drug:person 12 1498.50 124.875 14.9303 1.501e-10 ***
            3 256.33 85.444 10.2159 5.230e-05 ***
time
drug:time
            6 357.07 59.511 7.1152 4.707e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

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Reference - Hinkelmann K, Kempthorne O. Design and Analysis of Experiments Volume 2 Advanced Experimental Design. 2e. John Wiley & Sons Inc. 2008.

9.1 Chapter 1

9.1.1 p53

```
(129) MODEL
v2p53 = read.table("C:/G/Rt/Kemp/v2p53.txt", head=TRUE)
v2p53 = af(v2p53, c("TRT", "BLOCK"))
ANOVA(Y ~ BLOCK + TRT, v2p53) # OK
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
                7 518.21 74.030 8.1408 0.1137
MODEL
RESIDUALS
                2 18.19
                          9.094
CORRECTED TOTAL 9 536.40
$`Type I`
     Df Sum Sq Mean Sq F value Pr(>F)
BLOCK 4 261.40 65.350 7.1863 0.12587
TRT
      3 256.81 85.604 9.4135 0.09755 .
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
$`Type II`
     Df Sum Sq Mean Sq F value Pr(>F)
BLOCK 4 79.146 19.786 2.1758 0.33880
TRT
      3 256.812 85.604 9.4135 0.09755 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value Pr(>F)
BLOCK 4 79.146 19.786 2.1758 0.33880
      3 256.813 85.604 9.4135 0.09755 .
TRT
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
9.1.2 p62
```

(130) MODEL

```
ANOVA(Y ~ TRT + BLOCK, v2p53) # OK
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
                7 518.21 74.030 8.1408 0.1137
MODEL
RESIDUALS
                2 18.19
                          9.094
CORRECTED TOTAL 9 536.40
$`Type I`
     Df Sum Sq Mean Sq F value Pr(>F)
      3 439.07 146.356 16.0941 0.05907 .
BLOCK 4 79.15 19.786 2.1758 0.33880
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value Pr(>F)
      3 256.812 85.604 9.4135 0.09755 .
BLOCK 4 79.146 19.786 2.1758 0.33880
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value Pr(>F)
      3 256.813 85.604 9.4135 0.09755 .
BLOCK 4 79.146 19.786 2.1758 0.33880
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
9.2 Chapter 2
9.2.1 p82
(131) MODEL
v2p82 = read.table("C:/G/Rt/Kemp/v2p82.txt", head=TRUE)
v2p82 = af(v2p82, c("B", "Tx"))
ANOVA(Y ~ B + Tx, v2p82) # OK
```

```
$ANOVA
Response : Y

Df Sum Sq Mean Sq F value Pr(>F)

MODEL 14 889.11 63.508 6.3183 0.000518 ***
RESIDUALS 15 150.77 10.052
```

```
CORRECTED TOTAL 29 1039.89
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
                              Pr(>F)
  9 730.39 81.154 8.0738 0.0002454 ***
Tx 5 158.73 31.745 3.1583 0.0381655 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
  Df Sum Sq Mean Sq F value
                              Pr(>F)
B 9 595.74 66.193 6.5854 0.0007602 ***
Tx 5 158.73 31.745 3.1583 0.0381655 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
  Df Sum Sq Mean Sq F value
                              Pr(>F)
  9 595.74 66.193 6.5854 0.0007602 ***
Tx 5 158.73 31.745 3.1583 0.0381655 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
9.2.2 p87
(132) MODEL
v2p87 = read.table("C:/G/Rt/Kemp/v2p87.txt", head=TRUE)
ANOVA(y \sim x1 + x2 + x3 + x4 + x5 + x6, v2p87) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                5 1613.25 322.65 2.2332 0.2282
RESIDUALS
                4 577.91 144.48
CORRECTED TOTAL 9 2191.16
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
x1 1 1044.48 1044.48 7.2293 0.05473 .
       89.79 89.79 0.6215 0.47459
x2 1
x3 1 10.45 10.45 0.0724 0.80124
x4 1 407.08 407.08 2.8176 0.16854
x5 1 61.44 61.44 0.4253 0.54990
```

```
x6 0
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
   0
x2
x3 0
x4 0
x5 0
x6 0
$`Type III`
CAUTION: Singularity Exists!
   Df Sum Sq Mean Sq F value Pr(>F)
x1
x2 0
x3 0
x4 0
x5 0
x6 0
9.3 Chapter 6
9.3.1 p217
(133) MODEL
v2p217 = read.table("C:/G/Rt/Kemp/v2p217.txt", head=TRUE)
v2p217 = af(v2p217, c("R", "C", "Tx"))
ANOVA(Y ~ R + C + Tx, v2p217) # OK
$ANOVA
Response : Y
                Df Sum Sq Mean Sq F value
                                            Pr(>F)
                22 4305.1 195.687 7.5094 0.0002682 ***
MODEL
RESIDUALS
                13 338.8 26.059
CORRECTED TOTAL 35 4643.9
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value
                               Pr(>F)
  3 3951.4 1317.15 50.5446 1.998e-07 ***
   8 168.9 21.11 0.8101
                               0.6062
```

```
Tx 11 184.8 16.80 0.6446
                            0.7638
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
  Df Sum Sq Mean Sq F value
                             Pr(>F)
  3 3403.5 1134.51 43.5360 4.83e-07 ***
  8 112.4 14.05 0.5390
                             0.8077
Tx 11 184.8 16.80 0.6446
                             0.7638
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
  Df Sum Sq Mean Sq F value
                             Pr(>F)
   3 3403.5 1134.51 43.5360 4.83e-07 ***
C 8 112.4 14.05 0.5390
                             0.8077
Tx 11 184.8 16.80 0.6446
                             0.7638
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
9.3.2 p234
(134) MODEL
v2p234 = read.table("C:/G/Rt/Kemp/v2p234.txt", head=TRUE)
v2p234 = af(v2p234, c("R", "C", "Tx"))
ANOVA(Y ~ C + R + Tx, v2p234) # OK
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               13 426.50 32.808 7.0936 0.1302
                          4.625
RESIDUALS
                2
                    9.25
CORRECTED TOTAL 15 435.75
$`Type I`
  Df Sum Sq Mean Sq F value Pr(>F)
  3 16.25 5.417 1.1712 0.49129
R 3 357.25 119.083 25.7477 0.03762 *
Tx 7 53.00 7.571 1.6371 0.43052
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type II`
  Df Sum Sq Mean Sq F value Pr(>F)
C 3 10.25 3.417 0.7387 0.6189
```

```
3 285.50 95.167 20.5766 0.0467 *
Tx 7 53.00 7.571 1.6371 0.4305
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
  Df Sum Sq Mean Sq F value Pr(>F)
  3 10.25
             3.417 0.7387 0.6189
R 3 285.50 95.167 20.5766 0.0467 *
Tx 7 53.00 7.571 1.6371 0.4305
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
9.4 Chapter 7
9.4.1 p268
(135) MODEL
v2p268 = read.table("C:/G/Rt/Kemp/v2p268.txt", head=TRUE)
v2p268 = af(v2p268, c("A", "B", "C"))
ANOVA(y ~ block + A*B*C, v2p268) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                8 1026.00 128.250 24.981 0.0001765 ***
MODEL
RESIDUALS
                7
                    35.94
                           5.134
CORRECTED TOTAL 15 1061.94
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
block 1 715.56 715.56 139.3791 7.093e-06 ***
Α
       1 68.06
                 68.06 13.2574 0.0082753 **
                  0.06 0.0122 0.9152401
В
       1
          0.06
A:B
       1
          0.56
                  0.56
                       0.1096 0.7503276
С
       1 232.56 232.56 45.2991 0.0002698 ***
A:C
          0.06
                  0.06 0.0122 0.9152401
          7.56
                  7.56
                       1.4730 0.2642229
B:C
A:B:C 1
         1.56
                  1.56 0.3043 0.5983312
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
```

```
Df Sum Sq Mean Sq F value
block 1 715.56 715.56 139.3791 7.093e-06 ***
Α
       1 68.06
                 68.06 13.2574 0.0082753 **
В
          0.06
                  0.06
                        0.0122 0.9152401
          0.56
                  0.56
                        0.1096 0.7503276
A:B
       1 232.56 232.56 45.2991 0.0002698 ***
A:C
          0.06
                  0.06
                        0.0122 0.9152401
B:C
          7.56
                  7.56
                        1.4730 0.2642229
          1.56
                  1.56
                        0.3043 0.5983312
A:B:C 1
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value
block 1 715.56 715.56 139.3791 7.093e-06 ***
       1 68.06
                68.06 13.2574 0.0082753 **
В
          0.06
                  0.06
                        0.0122 0.9152401
A:B
          0.56
                  0.56
                       0.1096 0.7503276
       1
С
       1 232.56 232.56 45.2991 0.0002698 ***
A:C
          0.06
                  0.06
                       0.0122 0.9152401
B:C
          7.56
                  7.56 1.4730 0.2642229
A:B:C 1
          1.56
                  1.56 0.3043 0.5983312
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
9.4.2 p273
(136) MODEL
v2p273 = read.table("C:/G/Rt/Kemp/v2p273.txt", head=TRUE)
v2p273 = af(v2p273, c("block", "A", "B", "C"))
ANOVA(y ~ block + A*B*C + block:A:B:C, v2p273) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               15 2245.0 149.665 129.44 8.427e-14 ***
RESIDUALS
               16
                    18.5
                           1.156
CORRECTED TOTAL 31 2263.5
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
           Df Sum Sq Mean Sq F value
block
            1 1498.78 1498.78 1296.2432 < 2.2e-16 ***
            1 132.03 132.03 114.1892 1.083e-08 ***
Α
```

```
В
                 0.03
                         0.03
                                 0.0270
                                           0.87148
            1
                  1.53
                          1.53
                                  1.3243
                                           0.26673
A:B
            1
C
            1 504.03 504.03 435.9189 4.926e-13 ***
A:C
             1
                 0.78
                         0.78
                                 0.6757
                                           0.42316
B:C
                 3.78
                          3.78
             1
                                 3.2703
                                           0.08938 .
A:B:C
                  2.53
                          2.53
                                  2.1892
                                           0.15840
block:A:B:C 7
               101.47
                         14.50
                                 12.5367 1.965e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
                                           Pr(>F)
            Df Sum Sq Mean Sq
                                F value
            1 1498.78 1498.78 1296.2432 < 2.2e-16 ***
block
               132.03 132.03 114.1892 1.083e-08 ***
В
             1
                 0.03
                         0.03
                                  0.0270
                                           0.87148
                 1.53
                          1.53
                                  1.3243
                                           0.26673
A:B
            1
С
             1
               504.03 504.03 435.9189 4.926e-13 ***
A:C
             1
                 0.78
                         0.78
                                 0.6757
                                          0.42316
B:C
                 3.78
                          3.78
                                 3.2703
                                           0.08938 .
            1
A:B:C
                 2.53
                         2.53
                                 2.1892
                                           0.15840
block:A:B:C 7 101.47
                        14.50
                                 12.5367 1.965e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
            Df Sum Sq Mean Sq
                                 F value
                                           Pr(>F)
             1 1498.78 1498.78 1296.2432 < 2.2e-16 ***
block
               132.03 132.03 114.1892 1.083e-08 ***
Α
В
                 0.03
                         0.03
                                 0.0270
                                           0.87148
             1
A:B
             1
                 1.53
                          1.53
                                  1.3243
                                           0.26673
               504.03 504.03 435.9189 4.926e-13 ***
            1
A:C
            1
                 0.78
                         0.78
                                 0.6757
                                          0.42316
B:C
            1
                 3.78
                          3.78
                                 3.2703
                                           0.08938 .
A:B:C
             1
                 2.53
                         2.53
                                 2.1892
                                           0.15840
block:A:B:C 7 101.47
                                 12.5367 1.965e-05 ***
                        14.50
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

9.5 Chapter 8

9.5.1 p304

(137) MODEL

```
v2p304 = read.table("C:/G/Rt/Kemp/v2p304.txt", head=TRUE)
v2p304 = af(v2p304, c("rep", "block", "A", "B", "C"))
ANOVA(y ~ rep + block %in% rep + A*B*C - A:B:C, v2p304) # OK
```

```
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
                9 699.06 77.674 248.56 5.096e-07 ***
                    1.88
                           0.312
RESIDUALS
                6
CORRECTED TOTAL 15 700.94
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          1 390.06 390.06 1248.2 3.428e-08 ***
                              13.0 0.0065918 **
rep:block 2
              8.12
                      4.06
          1 18.06
                     18.06
                             57.8 0.0002696 ***
          1 175.56 175.56
                             561.8 3.702e-07 ***
В
              0.06
                     0.06
                             0.2 0.6704121
A:B
          1
С
          1 68.06
                     68.06
                             217.8 6.083e-06 ***
A:C
          1
              0.06
                     0.06
                               0.2 0.6704121
B:C
          1 39.06
                     39.06
                             125.0 3.056e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
         Df Sum Sq Mean Sq F value
                                     Pr(>F)
          1 390.06 390.06 1248.2 3.428e-08 ***
rep
              8.12
                      4.06
                              13.0 0.0065918 **
rep:block 2
          1 18.06
                     18.06
                             57.8 0.0002696 ***
          1 175.56 175.56
В
                             561.8 3.702e-07 ***
                               0.2 0.6704121
              0.06
                     0.06
A:B
C
          1 68.06
                     68.06
                             217.8 6.083e-06 ***
A:C
          1
              0.06
                      0.06
                               0.2 0.6704121
B:C
          1 39.06
                     39.06
                             125.0 3.056e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value
          1 390.06 390.06 1248.2 3.428e-08 ***
rep
rep:block 2
              8.12
                      4.06
                              13.0 0.0065918 **
          1 18.06
                     18.06
                             57.8 0.0002696 ***
Α
В
          1 175.56 175.56
                             561.8 3.702e-07 ***
A:B
              0.06
                     0.06
                               0.2 0.6704121
          1
С
          1 68.06
                     68.06
                             217.8 6.083e-06 ***
              0.06
                     0.06
                               0.2 0.6704121
A:C
          1
          1 39.06
                             125.0 3.056e-05 ***
B:C
                     39.06
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

9.5.2 p309

(138) MODEL

```
ANOVA(y ~ rep*A*B*C, v2p304) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               15 700.94 46.729
RESIDUALS
                0
                    0.00
CORRECTED TOTAL 15 700.94
$`Type I`
         Df Sum Sq Mean Sq F value Pr(>F)
rep
          1 390.06 390.06
          1 18.06
                     18.06
Α
              0.06
                      0.06
rep:A
          1
          1 175.56 175.56
В
              1.56
                      1.56
rep:B
              0.06
A:B
                      0.06
              0.06
                     0.06
rep:A:B
          1 68.06
                     68.06
          1 0.06
rep:C
                     0.06
A:C
              0.06
                     0.06
          1
rep:A:C
          1
              0.06
                     0.06
B:C
          1 39.06
                     39.06
              0.06
rep:B:C
          1
                     0.06
A:B:C
             7.56
                      7.56
              0.56
rep:A:B:C 1
                      0.56
$`Type II`
         Df Sum Sq Mean Sq F value Pr(>F)
          1 390.06 390.06
rep
          1 18.06
                     18.06
Α
              0.06
                      0.06
rep:A
          1 175.56 175.56
          1 1.56
                     1.56
rep:B
A:B
          1
              0.06
                      0.06
              0.06
                     0.06
rep:A:B
          1
          1 68.06
                     68.06
С
rep:C
          1
              0.06
                     0.06
              0.06
                     0.06
A:C
          1
rep:A:C
          1
              0.06
                     0.06
          1 39.06
B:C
                     39.06
              0.06
                      0.06
rep:B:C
A:B:C
              7.56
                      7.56
```

```
rep:A:B:C 1 0.56
                      0.56
$`Type III`
         Df Sum Sq Mean Sq F value Pr(>F)
          1 390.06 390.06
rep
          1 18.06
                     18.06
rep:A
              0.06
                      0.06
В
          1 175.56 175.56
              1.56
                     1.56
rep:B
          1
              0.06
                      0.06
A:B
          1
              0.06
                      0.06
rep:A:B
          1
          1 68.06
                     68.06
С
              0.06
                     0.06
          1
rep:C
              0.06
                     0.06
A:C
          1 0.06
rep:A:C
                     0.06
B:C
          1 39.06
                     39.06
rep:B:C
          1 0.06
                     0.06
A:B:C
              7.56
                     7.56
          1
              0.56
                      0.56
rep:A:B:C 1
9.6 Chapter 9
9.6.1 p343
(139) MODEL
v2p343 = read.table("C:/G/Rt/Kemp/v2p343.txt", head=TRUE)
v2p343 = af(v2p343, c("rep", "block", "A", "B", "C"))
ANOVA(y ~ rep + block %in% rep + A*B*C - A:B:C, v2p343) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
MODEL
               17 1889.8 111.167 14.659 0.001608 **
RESIDUALS
                    45.5
                           7.583
CORRECTED TOTAL 23 1935.3
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
                                       Pr(>F)
          2 1537.33 768.67 101.3626 2.375e-05 ***
rep:block 9 127.00
                     14.11
                              1.8608
                                      0.23163
              36.00
                      36.00
                              4.7473
Α
          1
                                      0.07218 .
В
          1
              36.00
                      36.00
                              4.7473
                                      0.07218 .
A:B
              12.25
                     12.25
                              1.6154
                                      0.25079
          1
```

```
C
          1 56.25
                     56.25
                             7.4176
                                     0.03448 *
              81.00
                     81.00 10.6813
                                     0.01707 *
A:C
          1
B:C
          1
               4.00
                      4.00
                             0.5275
                                     0.49502
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type II`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          2 1537.33 768.67 101.3626 2.375e-05 ***
rep
                     13.31
                             1.7558
rep:block 9 119.83
                                     0.25388
              36.00
                     36.00
                            4.7473
                                     0.07218 .
Α
          1
              36.00
                     36.00
                             4.7473
                                     0.07218 .
В
          1
              12.25
                     12.25
                                     0.25079
A:B
                             1.6154
          1
C
          1 56.25
                     56.25
                            7.4176
                                     0.03448 *
                     81.00 10.6813
A:C
          1
              81.00
                                     0.01707 *
B:C
          1
              4.00
                    4.00
                             0.5275
                                     0.49502
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          2 1537.33 768.67 101.3626 2.375e-05 ***
rep
rep:block 9 119.83
                     13.31
                            1.7558
                                     0.25388
              36.00
                     36.00
                             4.7473
                                     0.07218 .
Α
          1
В
          1
              36.00
                     36.00 4.7473
                                     0.07218 .
          1 12.25
                     12.25
                             1.6154
                                     0.25079
A:B
          1
C
              56.25
                     56.25
                           7.4176
                                     0.03448 *
A:C
              81.00
                     81.00 10.6813
          1
                                     0.01707 *
B:C
              4.00
                      4.00
                             0.5275
                                     0.49502
          1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
9.6.2 p348
(140) MODEL
ANOVA(y ~ rep + A*B*C + block %in% rep, v2p343) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                         Pr(>F)
MODEL
               17 1889.8 111.167 14.659 0.001608 **
                          7.583
RESIDUALS
                   45.5
CORRECTED TOTAL 23 1935.3
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
$`Type I`
          Df Sum Sq Mean Sq F value
                                         Pr(>F)
           2 1537.33 768.67 101.3626 2.375e-05 ***
rep
                       88.17
                              11.6264
                                        0.01432 *
Α
           1
               88.17
В
               37.50
                       37.50
                               4.9451
                                        0.06785 .
A:B
           1
               2.67
                       2.67
                               0.3516
                                        0.57484
C
           1
               66.67
                       66.67
                               8.7912
                                        0.02512 *
A:C
           1
               37.50
                      37.50
                               4.9451
                                        0.06785 .
B:C
           1
               0.17
                       0.17
                               0.0220
                                        0.88700
               24.00
                       24.00
A:B:C
           1
                               3.1648
                                        0.12555
               95.83
                       11.98
                               1.5797
                                        0.29730
rep:block 8
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
          Df Sum Sq Mean Sq F value
                                         Pr(>F)
           2 1537.33 768.67 101.3626 2.375e-05 ***
rep
           1
               36.00
                       36.00
                               4.7473
                                        0.07218 .
Α
В
           1
               36.00
                       36.00
                               4.7473
                                        0.07218 .
A:B
               12.25
                       12.25
                               1.6154
                                        0.25079
С
               56.25
                       56.25
           1
                               7.4176
                                        0.03448 *
A:C
           1
               81.00
                      81.00
                              10.6813
                                        0.01707 *
B:C
           1
               4.00
                        4.00
                               0.5275
                                        0.49502
A:B:C
           0
                                        0.29730
rep:block 8
               95.83
                       11.98
                               1.5797
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
          Df Sum Sq Mean Sq F value
                                         Pr(>F)
           2 1537.33 768.67 101.3626 2.375e-05 ***
rep
               36.00
                      36.00
                               4.7473
                                        0.07218 .
Α
           1
               36.00
                      36.00
                               4.7473
                                        0.07218 .
В
           1
A:B
               12.25
                       12.25
                               1.6154
                                        0.25079
С
                       56.25
                                        0.03448 *
           1
               56.25
                               7.4176
A:C
           1
               81.00
                      81.00
                              10.6813
                                        0.01707 *
B:C
               4.00
                        4.00
                               0.5275
                                        0.49502
           1
A:B:C
           0
rep:block 8
               95.83
                       11.98
                               1.5797
                                        0.29730
___
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

9.6.3 p353

(141) MODEL

```
v2p353 = read.table("C:/G/Rt/Kemp/v2p353.txt", head=TRUE)
v2p353 = af(v2p353, c("rep", "block", "A", "B", "C", "D"))
ANOVA(y ~ rep + rep:block + A*B*C*D - A:B:C:D, v2p353) # OK
$ANOVA
Response : y
                Df Sum Sq Mean Sq F value
                                             Pr(>F)
                21 7132.2 339.63 56.022 9.795e-08 ***
MODEL
RESIDUALS
                10
                     60.6
                             6.06
CORRECTED TOTAL 31 7192.9
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
                                        Pr(>F)
           1 5940.5 5940.5 979.8763 2.600e-11 ***
rep
rep:block 6 777.4
                      129.6 21.3711 3.675e-05 ***
             171.1
                      171.1 28.2268 0.0003412 ***
Α
В
           1
              18.0
                      18.0
                             2.9691 0.1155937
                             0.2577 0.6226914
A:B
                1.6
                        1.6
С
             120.1
                      120.1 19.8144 0.0012326 **
A:C
           1
                0.6
                        0.6 0.0928 0.7669127
B:C
           1
                2.0
                        2.0
                             0.3299 0.5784103
A:B:C
                4.5
                        4.5
                             0.7423 0.4091189
           1
D
                6.1
                        6.1
                             1.0103 0.3385304
           1
                1.1
                        1.1
                             0.1856 0.6757693
A:D
           1
                5.1
B:D
           1
                        5.1
                             0.8351 0.3823203
                       0.5
                             0.0825 0.7798349
A:B:D
                0.5
C:D
           1
                1.6
                       1.6
                             0.2577 0.6226914
                              1.6701 0.2253083
A:C:D
           1
              10.1
                       10.1
B:C:D
           1
              72.0
                       72.0 11.8763 0.0062660 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
         Df Sum Sq Mean Sq F value
                                       Pr(>F)
           1 5940.5 5940.5 979.8763
                                       2.6e-11 ***
rep
rep:block 6 406.9
                      67.8 11.1856 0.0006129 ***
             171.1
                      171.1 28.2268 0.0003412 ***
Α
           1
                      18.0
                             2.9691 0.1155937
В
           1
              18.0
                1.6
                        1.6
                             0.2577 0.6226914
A:B
           1
С
           1 120.1
                      120.1 19.8144 0.0012326 **
                0.6
                        0.6
                             0.0928 0.7669127
A:C
           1
B:C
           1
                2.0
                        2.0
                             0.3299 0.5784103
A:B:C
           1
                4.5
                       4.5
                             0.7423 0.4091189
D
           1
                6.1
                        6.1
                              1.0103 0.3385304
A:D
           1
                1.1
                        1.1
                             0.1856 0.6757693
```

```
B:D
               5.1
                       5.1
                             0.8351 0.3823203
A:B:D
               0.5
                       0.5
                            0.0825 0.7798349
          1
C:D
          1
               1.6
                       1.6
                            0.2577 0.6226914
A:C:D
          1
              10.1
                      10.1
                             1.6701 0.2253083
              72.0
B:C:D
                      72.0 11.8763 0.0062660 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          1 5940.5 5940.5 979.8763
                                     2.6e-11 ***
rep
rep:block 6 406.9
                     67.8 11.1856 0.0006129 ***
                   171.1 28.2268 0.0003412 ***
          1 171.1
              18.0
                     18.0 2.9691 0.1155937
В
               1.6
                      1.6 0.2577 0.6226914
A:B
          1 120.1
                    120.1 19.8144 0.0012326 **
A:C
          1
               0.6
                       0.6 0.0928 0.7669127
                       2.0 0.3299 0.5784103
B:C
          1
               2.0
A:B:C
          1
               4.5
                       4.5
                            0.7423 0.4091189
          1
               6.1
                       6.1
                             1.0103 0.3385304
A:D
          1
               1.1
                       1.1
                             0.1856 0.6757693
               5.1
                       5.1
                            0.8351 0.3823203
B:D
          1
A:B:D
          1
               0.5
                       0.5
                             0.0825 0.7798349
C:D
          1
               1.6
                       1.6 0.2577 0.6226914
                      10.1 1.6701 0.2253083
A:C:D
          1 10.1
B:C:D
          1
            72.0
                      72.0 11.8763 0.0062660 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
9.7 Chapter 10
9.7.1 p388
(142) MODEL
v2p388 = read.table("C:/G/Rt/Kemp/v2p388.txt", head=TRUE)
v2p388 = af(v2p388, c("rep", "block", "A", "B"))
ANOVA(y ~ rep + A*B + rep:block, v2p388) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
MODEL
               11 1136.8 103.343 124.01 3.698e-06 ***
                           0.833
RESIDUALS
                6
                     5.0
```

CORRECTED TOTAL 17 1141.8

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
                                       Pr(>F)
          1 410.89 410.89 493.0667 5.455e-07 ***
rep
          2 228.11 114.06 136.8667 9.868e-06 ***
Α
В
              3.44
                      1.72
                             2.0667 0.207585
A:B
          4 464.22 116.06 139.2667 4.801e-06 ***
rep:block 2 30.11 15.06 18.0667 0.002888 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
         Df Sum Sq Mean Sq F value
                                       Pr(>F)
rep
          1 410.89 410.89 493.0667 5.455e-07 ***
          2 228.11 114.06 136.8667 9.868e-06 ***
Α
В
              3.44
                      1.72
                             2.0667 0.207585
          2 18.78
                      9.39 11.2667 0.009298 **
A:B
rep:block 2 30.11
                     15.06 18.0667 0.002888 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
         Df Sum Sq Mean Sq F value
                                       Pr(>F)
          1 410.89 410.89 493.0667 5.455e-07 ***
rep
          2 228.11 114.06 136.8667 9.868e-06 ***
Α
В
              3.44
                     1.72
                             2.0667 0.207585
          2 18.78
                      9.39 11.2667 0.009298 **
A:B
rep:block 2 30.11
                     15.06 18.0667 0.002888 **
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
9.8 Chapter 14
9.8.1 p570
(143) MODEL
v2p570 = read.table("C:/G/Rt/Kemp/v2p570.txt", head=TRUE)
v2p570 = af(v2p570, c("A", "B", "C", "D"))
ANOVA(Y \sim A + B + C + D + A:B + A:C + A:D + B:C + B:D + C:D, v2p570) # OK
$ANOVA
Response : Y
```

Df Sum Sq Mean Sq F value Pr(>F)

```
MODEL
                8 22.222 2.7778
              0 0.000
RESIDUALS
CORRECTED TOTAL 8 22.222
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    2 2.8889 1.4444
В
    2 2.8889 1.4444
С
    2 1.5556 0.7778
D
    2 14.8889 7.4444
A:B O
A:C O
A:D 0
B:C 0
B:D 0
C:D 0
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
Α
    0
В
    0
С
    0
D
    0
A:B 0
A:C O
A:D O
B:C 0
B:D O
C:D 0
$`Type III`
CAUTION: Singularity Exists!
   Df Sum Sq Mean Sq F value Pr(>F)
Α
    0
В
    0
С
    0
D
    0
A:B 0
A:C O
A:D O
B:C O
B:D 0
C:D 0
9.8.2 p578
```

(144) MODEL

144) WODEL

```
v2p578 = read.table("C:/G/Rt/Kemp/v2p578.txt", head=TRUE)
v2p578 = af(v2p578, 1:11)
ANOVA(Y ~ A + B + C + D + E + F + G + H + J + K + L, v2p578) # OK
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                     575 52.273
               11
                       0
RESIDUALS
                0
CORRECTED TOTAL 11
                     575
$`Type I`
 Df Sum Sq Mean Sq F value Pr(>F)
      3.000
              3.000
В
  1 27.000 27.000
С
  1 12.000 12.000
D 1 16.333 16.333
Ε
 1 176.333 176.333
F
  1 133.333 133.333
G 1
      1.333
              1.333
  1 21.333 21.333
Н
J
  1 108.000 108.000
K
 1
      1.333
             1.333
L
 1 75.000 75.000
$`Type II`
 Df Sum Sq Mean Sq F value Pr(>F)
      3.000
              3.000
В
  1 27.000 27.000
С
 1 12.000 12.000
D 1 16.333 16.333
Ε
 1 176.333 176.333
F
  1 133.333 133.333
G 1
      1.333
             1.333
H 1 21.333 21.333
J
  1 108.000 108.000
      1.333
              1.333
K
  1
  1 75.000 75.000
$`Type III`
 Df Sum Sq Mean Sq F value Pr(>F)
      3.000
             3.000
A 1
 1 27.000 27.000
В
С
 1 12.000 12.000
D 1 16.333 16.333
E 1 176.333 176.333
```

F 1 133.333 133.333

```
G 1
     1.333
             1.333
H 1 21.333 21.333
J 1 108.000 108.000
K 1
      1.333
              1.333
  1 75.000 75.000
(145) MODEL
ANOVA(Y ~ E*F + E*J + F*J + E*L + F*L + J*L, v2p578) # OK
$ANOVA
Response : Y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               10 574.5
                          57.45
                                  114.9 0.07249 .
                           0.50
RESIDUALS
               1
                    0.5
CORRECTED TOTAL 11 575.0
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 176.333 176.333 352.6667 0.03387 *
    1 133.333 133.333 266.6667 0.03894 *
F
E:F 1 65.333 65.333 130.6667 0.05555 .
J
    1 66.667 66.667 133.3333 0.05500 .
E:J 1
       2.667
                2.667
                       5.3333 0.26015
    1 112.667 112.667 225.3333 0.04235 *
    1 10.800 10.800 21.6000 0.13492
E:L 1 5.486
              5.486 10.9714 0.18666
F:L 1 0.176
              0.176 0.3516 0.65925
J:L 1 1.038
               1.038
                       2.0769 0.38618
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 61.633 61.633 123.2667 0.05719 .
    1 75.208 75.208 150.4167 0.05179 .
E:F 1 9.346 9.346 18.6923 0.14470
    1 54.675 54.675 109.3500 0.06069 .
E:J 1 0.115
             0.115
                      0.2308 0.71490
F:J 1 72.115 72.115 144.2308 0.05289 .
    1 10.800 10.800 21.6000 0.13492
E:L 1 5.654
              5.654 11.3077 0.18402
F:L 1 0.115
             0.115
                     0.2308 0.71490
J:L 1 1.038
               1.038
                      2.0769 0.38618
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 61.038 61.038 122.0769 0.05746 .
    1 61.038 61.038 122.0769 0.05746 .
E:F 1 9.346 9.346 18.6923 0.14470
    1 61.038 61.038 122.0769 0.05746 .
E:J 1 0.115 0.115
                      0.2308 0.71490
F:J 1 72.115 72.115 144.2308 0.05289 .
    1 9.346 9.346 18.6923 0.14470
L
E:L 1 5.654 5.654 11.3077 0.18402
F:L 1 0.115 0.115 0.2308 0.71490
J:L 1 1.038 1.038 2.0769 0.38618
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
9.9 Chapter 16
9.9.1 p619
(146) MODEL
v2p619 = read.table("C:/G/Rt/Kemp/v2p619.txt", head=TRUE)
v2p619 = af(v2p619, c("A", "B", "C"))
ANOVA(y \sim A + B + C + A:B, v2p619) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                4 31.429 7.8571
RESIDUALS
                2 0.000 0.0000
CORRECTED TOTAL 6 31.429
$`Type I`
   Df Sum Sq Mean Sq F value
                                Pr(>F)
    1 13.7619 13.7619
                         Inf < 2.2e-16 ***
Α
В
    1 1.6667 1.6667
                         Inf < 2.2e-16 ***
С
    1 10.0000 10.0000
                         Inf < 2.2e-16 ***
A:B 1 6.0000 6.0000
                         Inf < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value
                               Pr(>F)
   1 19.6 19.6
                        Inf < 2.2e-16 ***
```

```
1
        3.6
                3.6
                         Inf < 2.2e-16 ***
        13.5
                13.5
                         Inf < 2.2e-16 ***
     1
                 6.0
A:B 1
         6.0
                         Inf < 2.2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type III`
    Df Sum Sq Mean Sq F value
                               Pr(>F)
        24.0
                24.0
                         Inf < 2.2e-16 ***
Α
         6.0
                 6.0
                         Inf < 2.2e-16 ***
В
С
     1
        13.5
                13.5
                        Inf < 2.2e-16 ***
         6.0
                6.0
                        Inf < 2.2e-16 ***
A:B 1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(147) MODEL
ANOVA(y ~ A + B + C + A:C, v2p619) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                4 26.0952 6.5238 2.4464 0.3106
RESIDUALS
                2 5.3333 2.6667
CORRECTED TOTAL 6 31.4286
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 13.7619 13.7619 5.1607 0.1511
     1 1.6667 1.6667 0.6250 0.5120
     1 10.0000 10.0000 3.7500 0.1924
A:C 1 0.6667 0.6667 0.2500 0.6667
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 19.6000 19.6000
                         7.35 0.1134
Α
     1 2.6667 2.6667
                         1.00 0.4226
     1 10.0000 10.0000
                       3.75 0.1924
A:C 1 0.6667 0.6667
                      0.25 0.6667
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 16.6667 16.6667 6.2500 0.1296
Α
     1 2.6667 2.6667 1.0000 0.4226
     1 8.1667 8.1667 3.0625 0.2222
A:C 1 0.6667 0.6667 0.2500 0.6667
```

(148) MODEL

ANOVA(y ~ A + B + C + B:C, v2p619) # OK \$ANOVA Response : y Df Sum Sq Mean Sq F value Pr(>F) MODEL 4 26.0952 6.5238 2.4464 0.3106 RESIDUALS 2 5.3333 2.6667 CORRECTED TOTAL 6 31.4286 \$`Type I` Df Sum Sq Mean Sq F value Pr(>F) 1 13.7619 13.7619 5.1607 0.1511 1 1.6667 1.6667 0.6250 0.5120 1 10.0000 10.0000 3.7500 0.1924 B:C 1 0.6667 0.6667 0.2500 0.6667 \$`Type II` Df Sum Sq Mean Sq F value Pr(>F) 1 16.6667 16.6667 Α 6.25 0.1296 1 3.6000 3.6000 1.35 0.3652 С 1 10.0000 10.0000 3.75 0.1924 B:C 1 0.6667 0.6667 0.25 0.6667 \$`Type III` Df Sum Sq Mean Sq F value Pr(>F) 1 16.6667 16.6667 6.2500 0.1296 В 1 2.6667 2.6667 1.0000 0.4226 С 1 8.1667 8.1667 3.0625 0.2222 B:C 1 0.6667 0.6667 0.2500 0.6667 9.9.2 p626 (149) MODEL v2p626 = read.table("C:/G/Rt/Kemp/v2p626.txt", head=TRUE) v2p626 = af(v2p626, c("A", "B", "C"))ANOVA(y ~ A + B + C + A:B, v2p626) # OK \$ANOVA Response : y Df Sum Sq Mean Sq F value Pr(>F) 4 42.092 10.5231 22.002 0.04395 * MODEL 2 0.957 0.4783 RESIDUALS

```
CORRECTED TOTAL 6 43.049
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 16.2088 16.2088 33.890 0.02826 *
     1 4.8150 4.8150 10.068 0.08662 .
    1 15.7339 15.7339 32.898 0.02908 *
A:B 1 5.3346 5.3346 11.154 0.07916 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 25.4131 25.4131 53.136 0.01830 *
    1 8.6630 8.6630 18.113 0.05102 .
C
    1 19.5193 19.5193 40.812 0.02364 *
A:B 1 5.3346 5.3346 11.154 0.07916 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 29.7950 29.7950 62.297 0.01568 *
    1 11.7460 11.7460 24.559 0.03839 *
     1 19.5193 19.5193 40.812 0.02364 *
A:B 1 5.3346 5.3346 11.154 0.07916 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(150) MODEL
ANOVA(y ~ A + B + C + A:C, v2p626) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                4 39.229 9.8072 5.1346 0.1696
MODEL
RESIDUALS
                2 3.820
                         1.9100
CORRECTED TOTAL 6 43.049
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 16.2088 16.2088 8.4862 0.1004
Α
В
     1 4.8150 4.8150 2.5209 0.2533
```

C

1 15.7339 15.7339 8.2376 0.1030

```
A:C 1 2.4711 2.4711 1.2937 0.3733
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 25.4131 25.4131 13.3052 0.06762 .
    1 6.0361 6.0361 3.1602 0.21743
    1 15.7339 15.7339 8.2376 0.10298
A:C 1 2.4711 2.4711 1.2937 0.37327
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 20.1428 20.1428 10.5459 0.08317 .
    1 6.0361 6.0361 3.1602 0.21743
    1 11.8863 11.8863 6.2232 0.13007
A:C 1 2.4711 2.4711 1.2937 0.37327
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(151) MODEL
ANOVA(y ~ A + B + C + B:C, v2p626) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                4 37.340 9.3349 3.2701 0.2477
RESIDUALS
                2 5.709 2.8546
CORRECTED TOTAL 6 43.049
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 16.2088 16.2088 5.6781 0.1400
     1 4.8150 4.8150 1.6867 0.3236
     1 15.7339 15.7339 5.5118 0.1434
B:C 1 0.5819 0.5819 0.2038 0.6959
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 21.9995 21.9995 7.7067 0.1090
     1 8.6630 8.6630 3.0347 0.2236
     1 15.7339 15.7339 5.5118 0.1434
B:C 1 0.5819 0.5819 0.2038 0.6959
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
```

```
1 21.9995 21.9995 7.7067 0.1090
     1 7.0709 7.0709 2.4770 0.2562
     1 13.3221 13.3221 4.6669 0.1633
C
B:C 1 0.5819 0.5819 0.2038 0.6959
9.10 Chapter 17
9.10.1 p642
(152) MODEL
v2p642 = read.table("C:/G/Rt/Kemp/v2p642.txt", head=TRUE)
v2p642 = af(v2p642, 2:11)
ANOVA(Y ~ A + B + C + D + E + F + G, v2p642) # OK
$ANOVA
Response: Y
               Df Sum Sq Mean Sq F value Pr(>F)
                    11.0 1.57143 1.6688 0.1646
MODEL
RESIDUALS
               24
                    22.6 0.94167
CORRECTED TOTAL 31
                    33.6
$`Type I`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 5.7800 5.7800 6.1381 0.02066 *
B 1 0.1800 0.1800 0.1912 0.66587
C 1 0.1250 0.1250 0.1327 0.71879
D 1 2.5312 2.5312 2.6881 0.11415
E 1 0.6613 0.6613 0.7022 0.41031
F 1 0.0112 0.0112 0.0119 0.91387
G 1 1.7113 1.7113 1.8173 0.19023
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type II`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 5.7800 5.7800 6.1381 0.02066 *
B 1 0.1800 0.1800 0.1912 0.66587
C 1 0.1250 0.1250 0.1327 0.71879
D 1 2.5312 2.5312 2.6881 0.11415
E 1 0.6613 0.6613 0.7022 0.41031
F 1 0.0112 0.0112 0.0119 0.91387
G 1 1.7113 1.7113 1.8173 0.19023
```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```
$`Type III`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 5.7800 5.7800 6.1381 0.02066 *
B 1 0.1800 0.1800 0.1912 0.66587
C 1 0.1250 0.1250 0.1327 0.71879
D 1 2.5312 2.5312 2.6881 0.11415
E 1 0.6613 0.6613 0.7022 0.41031
F 1 0.0112 0.0112 0.0119 0.91387
G 1 1.7113 1.7113 1.8173 0.19023
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(153) MODEL
ANOVA(log(S) \sim A + B + C + D + E + F + G, v2p642) # OK
$ANOVA
Response : log(S)
                Df Sum Sq Mean Sq F value Pr(>F)
                 7 266.43 38.062
MODEL
                            0.000
RESIDUALS
                24
                     0.00
CORRECTED TOTAL 31 266.43
$`Type I`
  Df Sum Sq Mean Sq F value
                                Pr(>F)
               1.511
                         Inf < 2.2e-16 ***
A 1
       1.511
B 1
       0.600
               0.600
                         Inf < 2.2e-16 ***
                         Inf < 2.2e-16 ***
C
  1
       0.284
               0.284
D
       0.384
               0.384
                         Inf < 2.2e-16 ***
  1
F. 1
                         Inf < 2.2e-16 ***
       0.741
               0.741
F 1 261.783 261.783
                         Inf < 2.2e-16 ***
G 1
       1.127
               1.127
                         Inf < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
                               Pr(>F)
  Df Sum Sq Mean Sq F value
A 1
       1.511
               1.511
                         Inf < 2.2e-16 ***
B 1
       0.600
               0.600
                         Inf < 2.2e-16 ***
С
       0.284
               0.284
                         Inf < 2.2e-16 ***
 1
D 1
       0.384
               0.384
                         Inf < 2.2e-16 ***
E 1
       0.741
               0.741
                         Inf < 2.2e-16 ***
F 1 261.783 261.783
                         Inf < 2.2e-16 ***
G 1
       1.127
               1.127
                         Inf < 2.2e-16 ***
```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```
$`Type III`
 Df Sum Sq Mean Sq F value Pr(>F)
      1.511 1.511
                       Inf < 2.2e-16 ***
A 1
B 1
      0.600 0.600
                       Inf < 2.2e-16 ***
C 1
      0.284 0.284
                       Inf < 2.2e-16 ***
D 1
      0.384 0.384
                       Inf < 2.2e-16 ***
E 1
      0.741 0.741
                       Inf < 2.2e-16 ***
F 1 261.783 261.783
                      Inf < 2.2e-16 ***
G 1 1.127 1.127
                       Inf < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
9.11 Chapter 19
9.11.1 p700
(154) MODEL
v2p700 = read.table("C:/G/Rt/Kemp/v2p700.txt", head=TRUE)
v2p700 = af(v2p700, 2:5)
ANOVA(Y ~ P + S + T + C, v2p700) # OK
$ANOVA
Response: Y
               Df Sum Sq Mean Sq F value Pr(>F)
               12 378.80 31.5670 57.256 0.003319 **
MODEL
RESIDUALS
                    1.65 0.5513
CORRECTED TOTAL 15 380.46
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
 Df Sum Sq Mean Sq F value Pr(>F)
P 3 53.888 17.963 32.580 0.008646 **
S 3 154.508 51.503 93.414 0.001845 **
T 3 149.848 49.949 90.597 0.001930 **
C 3 20.561 6.854 12.431 0.033708 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
 Df Sum Sq Mean Sq F value Pr(>F)
             1.110 2.0133 0.278974
     2.220
S 3 111.966 37.322 67.6941 0.002969 **
T 3 161.828 53.943 97.8403 0.001722 **
C 3 20.561 6.854 12.4311 0.033708 *
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
  Df Sum Sq Mean Sq F value
                             Pr(>F)
P 2 2.220 1.110 2.0133 0.278974
S 3 111.966 37.322 67.6941 0.002969 **
T 3 161.828 53.943 97.8403 0.001722 **
C 3 20.561 6.854 12.4311 0.033708 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
9.11.2 p703
(155) MODEL
v2p703 = read.table("C:/G/Rt/Kemp/v2p703.txt", head=TRUE)
v2p703C = ifelse(v2p703C == 0, 4, v2p703C)
v2p703 = af(v2p703, 2:5)
ANOVA(Y ~ P + S + T + C, v2p703) # OK
$ANOVA
Response: Y
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
               13 385.18 29.6293 21.766 0.0005673 ***
MODEL
RESIDUALS
                6
                    8.17 1.3613
CORRECTED TOTAL 19 393.35
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
  Df Sum Sq Mean Sq F value
                              Pr(>F)
P 4 56.408 14.102 10.3596 0.0073255 **
S 3 119.260 39.753 29.2036 0.0005620 ***
T 3 190.430 63.477 46.6312 0.0001498 ***
C 3 19.083 6.361 4.6728 0.0518237 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
 Df Sum Sq Mean Sq F value
P 4 52.288 13.072 9.6028 0.0088641 **
S 3 167.414 55.805 40.9952 0.0002163 ***
T 3 190.430 63.477 46.6312 0.0001498 ***
C 3 19.083 6.361 4.6728 0.0518237 .
```

```
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

$`Type III`
Df Sum Sq Mean Sq F value Pr(>F)
P 4 52.287 13.072 9.6028 0.0088641 **
S 3 167.414 55.805 40.9952 0.0002163 ***
T 3 190.430 63.477 46.6312 0.0001498 ***
C 3 19.083 6.361 4.6728 0.0518237 .
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

10 Lawson - DAE with SAS

Reference

• Lawson J. Design and Analysis of Experiments with SAS. Taylor and Francis Group. 2010.

```
Loading required package: daewr

Registered S3 method overwritten by 'DoE.base':
  method from
  factorize.factor conf.design

require(daewr)
```

10.1 Chapter 2

ANOVA(height ~ time, bread) # OK

10.1.1 p22

(156) MODEL

```
$ANOVA
Response : height
               Df Sum Sq Mean Sq F value Pr(>F)
               2 21.573 10.7865 4.6022 0.042 *
MODEL
RESIDUALS
               9 21.094 2.3438
CORRECTED TOTAL 11 42.667
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
    Df Sum Sq Mean Sq F value Pr(>F)
time 2 21.573 10.787 4.6022 0.042 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
    Df Sum Sq Mean Sq F value Pr(>F)
time 2 21.573 10.787 4.6022 0.042 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
    Df Sum Sq Mean Sq F value Pr(>F)
```

```
time 2 21.573 10.787 4.6022 0.042 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.1.2 p32
(157) MODEL
ANOVA(height(1 - 1.294869) ~ time, bread) # OK
$ANOVA
Response : height^(1 - 1.294869)
               Df
                    Sum Sq
                            Mean Sq F value Pr(>F)
MODEL
                2 0.0130560 0.0065280 5.9356 0.02271 *
RESIDUALS
                9 0.0098983 0.0010998
CORRECTED TOTAL 11 0.0229544
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
    Df
         Sum Sq Mean Sq F value Pr(>F)
time 2 0.013056 0.006528 5.9356 0.02271 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
    Df
         Sum Sq Mean Sq F value Pr(>F)
time 2 0.013056 0.006528 5.9356 0.02271 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Sum Sq Mean Sq F value Pr(>F)
time 2 0.013056 0.006528 5.9356 0.02271 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
10.1.3 p42
(158) MODEL
ANOVA(yield ~ treat, sugarbeet) # OK
```

\$ANOVA

Response : yield

```
Df Sum Sq Mean Sq F value
                                         Pr(>F)
MODEL
                3 291.00 97.002 45.9 1.718e-07 ***
               14 29.59
RESIDUALS
                          2.113
CORRECTED TOTAL 17 320.59
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
treat 3 291 97.002 45.9 1.718e-07 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                                 Pr(>F)
treat 3
           291 97.002 45.9 1.718e-07 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value
           291 97.002
                       45.9 1.718e-07 ***
treat 3
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
10.2 Chapter 3
10.2.1 p63
(159) MODEL
ANOVA(CO ~ Eth + Ratio + Eth:Ratio, COdata) # OK
$ANOVA
Response : CO
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
MODEL
                8 1654.0 206.750 40.016 3.861e-06 ***
RESIDUALS
                    46.5
                          5.167
CORRECTED TOTAL 17 1700.5
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
Eth
          2
               324
                    162.0 31.355 8.790e-05 ***
Ratio
          2
               652
                    326.0 63.097 5.067e-06 ***
```

```
Eth:Ratio 4
               678 169.5 32.806 2.240e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
          Df Sum Sq Mean Sq F value
                                      Pr(>F)
                324
                      162.0 31.355 8.790e-05 ***
                      326.0 63.097 5.067e-06 ***
Ratio
                652
                678
                      169.5 32.806 2.240e-05 ***
Eth:Ratio 4
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
          Df Sum Sq Mean Sq F value
                      162.0 31.355 8.790e-05 ***
Eth
           2
                324
Ratio
           2
                652
                      326.0 63.097 5.067e-06 ***
Eth:Ratio 4
                678
                      169.5 32.806 2.240e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(160) MODEL
ANOVA(CO ~ Ratio + Eth + Ratio:Eth, COdata) # OK
$ANOVA
Response : CO
                Df Sum Sq Mean Sq F value
                 8 1654.0 206.750 40.016 3.861e-06 ***
MODEL
RESIDUALS
                    46.5
                           5.167
CORRECTED TOTAL 17 1700.5
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
$`Type I`
          Df Sum Sq Mean Sq F value
                                      Pr(>F)
           2
                652
                      326.0 63.097 5.067e-06 ***
Ratio
           2
                324
                      162.0 31.355 8.790e-05 ***
Eth
                      169.5 32.806 2.240e-05 ***
Ratio:Eth 4
                678
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
          Df Sum Sq Mean Sq F value
Ratio
           2
                652
                      326.0 63.097 5.067e-06 ***
Eth
           2
                324
                      162.0 31.355 8.790e-05 ***
                678
                      169.5 32.806 2.240e-05 ***
Ratio:Eth 4
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value
          2
Ratio
               652
                     326.0 63.097 5.067e-06 ***
               324
                     162.0 31.355 8.790e-05 ***
Eth
Ratio:Eth 4
               678
                     169.5 32.806 2.240e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
10.2.2 p74
(161) MODEL
ANOVA(CO ~ Eth + Ratio + Eth:Ratio, COdata[-18,]) # OK
$ANOVA
Response : CO
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
                8 1423.0 177.879 31.978 2.749e-05 ***
MODEL
RESIDUALS
                    44.5
                           5.563
CORRECTED TOTAL 16 1467.5
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
                                     Pr(>F)
          2 472.66 236.33 42.486 5.482e-05 ***
Eth
          2 395.33 197.66 35.535 0.0001048 ***
Ratio
Eth:Ratio 4 555.04 138.76 24.945 0.0001427 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
         Df Sum Sq Mean Sq F value
                                      Pr(>F)
          2 398.26 199.13 35.799 0.0001020 ***
Eth
          2 395.33 197.66 35.535 0.0001048 ***
Eth:Ratio 4 555.04 138.76 24.945 0.0001427 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value
                                     Pr(>F)
          2 319.45 159.73 28.715 0.0002235 ***
Eth
          2 511.45 255.73 45.973 4.105e-05 ***
Ratio
Eth:Ratio 4 555.04 138.76 24.945 0.0001427 ***
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.2.3 p91
(162) MODEL
volt$XA = (as.numeric(as.character(volt$A)) - 27)/5
volt$XB = (as.numeric(as.character(volt$B)) - 2.75)/2.25
volt$XC = (as.numeric(as.character(volt$C)) - 2.75)/2.25
ANOVA(y ~ XA + XB + XC + XA:XB + XA:XC + XB:XC + XA:XB:XC, volt) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
                7 8843.4 1263.35 3.8686 0.0385 *
MODEL
RESIDUALS
                8 2612.5 326.56
CORRECTED TOTAL 15 11455.9
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value
                                   Pr(>F)
XA
         1 4522.6 4522.6 13.8490 0.005859 **
ΧB
             14.1
                    14.1 0.0431 0.840793
XC
                    473.1 1.4486 0.263154
         1 473.1
XA:XB
         1 715.6
                  715.6 2.1912 0.177071
XA:XC
         1 2525.1 2525.1 7.7322 0.023899 *
XB:XC
             52.6
                     52.6 0.1610 0.698780
XA:XB:XC 1 540.6
                  540.6 1.6553 0.234218
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value
XΑ
         1 4522.6 4522.6 13.8490 0.005859 **
XВ
             14.1
                    14.1 0.0431 0.840793
         1 473.1
                   473.1 1.4486 0.263154
XC
XA:XB
         1 715.6 715.6 2.1912 0.177071
XA:XC
         1 2525.1 2525.1 7.7322 0.023899 *
                     52.6 0.1610 0.698780
XB:XC
             52.6
XA:XB:XC 1 540.6
                  540.6 1.6553 0.234218
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
```

```
Df Sum Sq Mean Sq F value Pr(>F)
XA
          1 4522.6 4522.6 13.8490 0.005859 **
XВ
             14.1
                     14.1 0.0431 0.840793
XC
          1 473.1
                    473.1 1.4486 0.263154
XA:XB
          1 715.6 715.6 2.1912 0.177071
XA:XC
          1 2525.1 2525.1 7.7322 0.023899 *
                     52.6 0.1610 0.698780
XB:XC
             52.6
XA:XB:XC 1 540.6
                    540.6 1.6553 0.234218
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.2.4 p97
(163) MODEL
chem2 = af(chem, c("A", "B", "C", "D"))
ANOVA(y ~ A*B*C*D, chem2) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                15 6369.4 424.63
RESIDUALS
                0
                     0.0
CORRECTED TOTAL 15 6369.4
$`Type I`
       Df Sum Sq Mean Sq F value Pr(>F)
        1 637.6
                   637.6
Α
         1 5076.6 5076.6
A:B
        1 451.6
                   451.6
             0.6
С
         1
                     0.6
A:C
         1
             10.6
                    10.6
B:C
             1.6
                     1.6
         1
A:B:C
             0.6
                     0.6
         1
D
         1
             7.6
                     7.6
             68.1
                    68.1
A:D
         1
B:D
        1
             0.1
                     0.1
A:B:D
             7.6
                     7.6
         1
             7.6
                     7.6
C:D
         1
A:C:D
        1
            95.1
                    95.1
B:C:D
             3.1
                     3.1
         1
             1.6
                     1.6
A:B:C:D 1
$`Type II`
        Df Sum Sq Mean Sq F value Pr(>F)
        1 637.6
                   637.6
Α
```

```
1 5076.6 5076.6
В
A:B
         1 451.6
                    451.6
С
              0.6
                      0.6
         1
A:C
         1
             10.6
                     10.6
              1.6
B:C
                      1.6
         1
A:B:C
         1
              0.6
                      0.6
D
         1
              7.6
                      7.6
A:D
             68.1
                     68.1
         1
B:D
         1
              0.1
                      0.1
A:B:D
              7.6
                      7.6
         1
C:D
              7.6
                      7.6
         1
A:C:D
         1
             95.1
                     95.1
                      3.1
B:C:D
              3.1
         1
A:B:C:D 1
              1.6
                      1.6
$`Type III`
        Df Sum Sq Mean Sq F value Pr(>F)
         1 637.6
                    637.6
Α
         1 5076.6 5076.6
В
         1 451.6
                    451.6
A:B
С
              0.6
                      0.6
         1
A:C
         1
             10.6
                     10.6
B:C
              1.6
                      1.6
         1
A:B:C
         1
              0.6
                      0.6
D
         1
              7.6
                      7.6
A:D
         1
             68.1
                     68.1
B:D
              0.1
                      0.1
         1
A:B:D
              7.6
                      7.6
         1
                      7.6
C:D
              7.6
A:C:D
         1
             95.1
                     95.1
              3.1
                      3.1
B:C:D
         1
A:B:C:D 1
              1.6
                      1.6
```

10.2.5 p104

(164) MODEL

ANOVA(y ~ A*B*C*D, BoxM) # OK

```
$ANOVA
Response : y

Df Sum Sq Mean Sq F value Pr(>F)
MODEL 15 207.1 13.807
RESIDUALS 0 0.0
CORRECTED TOTAL 15 207.1
```

```
$`Type I`
       Df Sum Sq Mean Sq F value Pr(>F)
        1 2.560
                   2.560
Α
В
        1 71.234 71.234
        1 3.312
A:B
                   3.312
С
        1 55.056 55.056
A:C
        1 24.800
                  24.800
B:C
        1 2.560
                   2.560
A:B:C
        1 5.760
                   5.760
D
        1 4.080
                  4.080
A:D
        1 1.346
                   1.346
B:D
        1 5.570
                   5.570
A:B:D
        1 2.074
                   2.074
C:D
        1 8.880
                   8.880
A:C:D
        1 0.640
                   0.640
B:C:D
        1 9.986
                   9.986
A:B:C:D 1 9.242
                   9.242
$`Type II`
       Df Sum Sq Mean Sq F value Pr(>F)
        1 2.560
                   2.560
В
        1 71.234 71.234
        1 3.312
                  3.312
A:B
С
        1 55.056 55.056
A:C
        1 24.800 24.800
B:C
        1 2.560
                   2.560
A:B:C
        1 5.760
                  5.760
D
        1 4.080
                  4.080
A:D
        1 1.346
                   1.346
B:D
        1 5.570
                   5.570
        1 2.074
A:B:D
                   2.074
        1 8.880
C:D
                   8.880
A:C:D
        1 0.640
                   0.640
B:C:D
        1 9.986
                   9.986
A:B:C:D 1 9.242
                   9.242
$`Type III`
       Df Sum Sq Mean Sq F value Pr(>F)
Α
        1 2.560
                   2.560
В
        1 71.234 71.234
        1 3.312
A:B
                  3.312
        1 55.056
С
                 55.056
A:C
        1 24.800
                  24.800
        1 2.560
B:C
                  2.560
A:B:C
        1 5.760
                  5.760
        1 4.080
D
                   4.080
A:D
        1 1.346
                   1.346
B:D
        1 5.570
                   5.570
```

```
A:B:D 1 2.074 2.074
C:D 1 8.880 8.880
A:C:D 1 0.640 0.640
B:C:D 1 9.986 9.986
A:B:C:D 1 9.242 9.242
```

10.3 Chapter 4

10.3.1 p122

(165) MODEL

```
ANOVA(rate ~ rat + dose, drug) # OK
$ANOVA
Response : rate
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               13 2.12867 0.163744 19.613 1.59e-12 ***
RESIDUALS
               36 0.30055 0.008349
CORRECTED TOTAL 49 2.42922
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
    Df Sum Sq Mean Sq F value
                                Pr(>F)
rat 9 1.66846 0.18538 22.205 3.749e-12 ***
dose 4 0.46021 0.11505 13.781 6.535e-07 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
    Df Sum Sq Mean Sq F value
                                Pr(>F)
rat 9 1.66846 0.18538 22.205 3.749e-12 ***
dose 4 0.46021 0.11505 13.781 6.535e-07 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
    Df Sum Sq Mean Sq F value
rat 9 1.66846 0.18538 22.205 3.749e-12 ***
dose 4 0.46021 0.11505 13.781 6.535e-07 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

10.3.2 p127

(166) MODEL

```
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                          Pr(>F)
                8 543.22 67.902 26.203 0.0001507 ***
MODEL
RESIDUALS
                7 18.14
                          2.591
CORRECTED TOTAL 15 561.36
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
            Df Sum Sq Mean Sq F value
                                        Pr(>F)
             1 47.61
                       47.61 18.3721 0.003627 **
block
             1 422.30 422.30 162.9613 4.194e-06 ***
treat
             3 32.96 10.99 4.2399 0.052741 .
strain
treat:strain 3 40.34
                       13.45 5.1892 0.033685 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
            Df Sum Sq Mean Sq F value
                                        Pr(>F)
             1 47.61
                       47.61 18.3721 0.003627 **
block
             1 422.30 422.30 162.9613 4.194e-06 ***
treat
strain
             3 32.96 10.99 4.2399 0.052741 .
                       13.45
treat:strain 3 40.34
                               5.1892 0.033685 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
            Df Sum Sq Mean Sq F value
                                        Pr(>F)
             1 47.61
                       47.61 18.3721 0.003627 **
block
             1 422.30 422.30 162.9613 4.194e-06 ***
treat
             3 32.96 10.99
                               4.2399 0.052741 .
strain
treat:strain 3 40.34
                       13.45
                               5.1892 0.033685 *
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.3.3 p129
(167) MODEL
ANOVA(cdistance ~ id + teehgt, rcb) # OK
```

ANOVA(y ~ block + treat + strain + treat:strain, bha) # OK

\$ANOVA

```
Response : cdistance
                Df Sum Sq Mean Sq F value Pr(>F)
                10 126465 12646.5 161.72 < 2.2e-16 ***
MODEL
RESIDUALS
               124
                     9697
                             78.2
CORRECTED TOTAL 134 136162
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
       8 124741 15593 199.394 < 2.2e-16 ***
id
teehgt 2 1724
                  862 11.023 3.926e-05 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
                                   Pr(>F)
       8 124741 15593 199.394 < 2.2e-16 ***
id
teehgt 2 1724
                    862 11.023 3.926e-05 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
      Df Sum Sq Mean Sq F value
                                  Pr(>F)
       8 124741 15593 199.394 < 2.2e-16 ***
id
          1724
                   862 11.023 3.926e-05 ***
teehgt 2
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
10.3.4 p136
(168) MODEL
ANOVA(AUC ~ Subject + Period + Treat, bioeqv) # OK
$ANOVA
Response : AUC
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                6 174461
                           29077 0.1315 0.9774
RESIDUALS
                2 442158 221079
CORRECTED TOTAL 8 616618
$`Type I`
       Df Sum Sq Mean Sq F value Pr(>F)
Subject 2 114264 57132 0.2584 0.7946
Period 2 45196 22598 0.1022 0.9073
```

```
Treat 2 15000 7500 0.0339 0.9672
$`Type II`
       Df Sum Sq Mean Sq F value Pr(>F)
Subject 2 114264 57132 0.2584 0.7946
Period 2 45196 22598 0.1022 0.9073
Treat 2 15000 7500 0.0339 0.9672
$`Type III`
       Df Sum Sq Mean Sq F value Pr(>F)
Subject 2 114264 57132 0.2584 0.7946
Period 2 45196 22598 0.1022 0.9073
        2 15000 7500 0.0339 0.9672
Treat
10.4 Chapter 5
10.4.1 p152
(169) MODEL
ANOVA(conc ~ lab, Apo) # OK
$ANOVA
Response : conc
               Df Sum Sq Mean Sq F value Pr(>F)
               3 0.092233 0.0307444 42.107 4.009e-10 ***
MODEL
               26 0.018984 0.0007302
RESIDUALS
CORRECTED TOTAL 29 0.111217
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Sum Sq Mean Sq F value
                                 Pr(>F)
lab 3 0.092233 0.030744 42.107 4.009e-10 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Sum Sq Mean Sq F value Pr(>F)
lab 3 0.092233 0.030744 42.107 4.009e-10 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
        Sum Sq Mean Sq F value Pr(>F)
```

lab 3 0.092233 0.030744 42.107 4.009e-10 ***

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.4.2 p181
(170) MODEL
ANOVA(residue ~ form + tech + form:tech + plot:form:tech, pesticide) # OK
$ANOVA
Response : residue
                    Sum Sq Mean Sq F value Pr(>F)
                7 0.036857 0.0052653 11.804 0.001187 **
MODEL
RESIDUALS
                8 0.003569 0.0004461
CORRECTED TOTAL 15 0.040426
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
                   Sum Sq Mean Sq F value
                                             Pr(>F)
form
               1 0.000018 0.000018 0.0405
                                             0.84554
tech
               1 0.032310 0.032310 72.4339 2.789e-05 ***
               1 0.002186 0.002186 4.8997
                                             0.05776 .
form:tech
form:tech:plot 4 0.002344 0.000586 1.3136
                                             0.34317
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
                   Sum Sq Mean Sq F value
              Df
                                             Pr(>F)
               1 0.000018 0.000018 0.0405
form
                                             0.84554
tech
               1 0.032310 0.032310 72.4339 2.789e-05 ***
               1 0.002186 0.002186 4.8997
                                             0.05776 .
form:tech
form:tech:plot 4 0.002344 0.000586 1.3136
                                             0.34317
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
              Df
                   Sum Sq Mean Sq F value
                                             Pr(>F)
               1 0.000018 0.000018 0.0405
form
                                             0.84554
tech
               1 0.032310 0.032310 72.4339 2.789e-05 ***
               1 0.002186 0.002186 4.8997
form:tech
                                             0.05776 .
form:tech:plot 4 0.002344 0.000586 1.3136
                                             0.34317
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

10.5 Chapter 7

10.5.1 p260

(171) MODEL

```
ANOVA(score ~ recipe + panelist, taste) # OK
$ANOVA
Response : score
               Df Sum Sq Mean Sq F value Pr(>F)
               14 28.458 2.03274
MODEL
                                  2.661 0.0719 .
RESIDUALS
               9 6.875 0.76389
CORRECTED TOTAL 23 35.333
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value Pr(>F)
         3 21.0000 7.000 9.1636 0.004246 **
recipe
panelist 11 7.4583 0.678 0.8876 0.581099
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value Pr(>F)
         3 9.1250 3.04167 3.9818 0.04649 *
recipe
panelist 11 7.4583 0.67803 0.8876 0.58110
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
        Df Sum Sq Mean Sq F value Pr(>F)
         3 9.1250 3.04167 3.9818 0.04649 *
panelist 11 7.4583 0.67803 0.8876 0.58110
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.5.2 p262
(172) MODEL
ANOVA(pressure ~ Block + Treatment, BPmonitor) # OK
```

Response : pressure

\$ANOVA

```
Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                8 321.00 40.125 4.4174 0.1245
                3 27.25
                           9.083
RESIDUALS
CORRECTED TOTAL 11 348.25
$`Type I`
         Df Sum Sq Mean Sq F value Pr(>F)
          5 73.75 14.750 1.6239 0.36606
Treatment 3 247.25 82.417 9.0734 0.05149 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
         Df Sum Sq Mean Sq F value Pr(>F)
          5 83.25 16.650 1.8330 0.32772
Treatment 3 247.25 82.417 9.0734 0.05149 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df Sum Sq Mean Sq F value Pr(>F)
          5 83.25 16.650 1.8330 0.32772
Treatment 3 247.25 82.417 9.0734 0.05149 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.5.3 p276
(173) MODEL
ANOVA(weight ~ Blocks + A + B + C + D + E + F + G + H, Bff) # OK
$ANOVA
Response : weight
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
               15 158.37 10.558
RESIDUALS
                0
                    0.00
CORRECTED TOTAL 15 158.37
$`Type I`
      Df Sum Sq Mean Sq F value Pr(>F)
Blocks 7 30.567
                  4.367
       1 21.879 21.879
       1 8.338
                 8.338
С
       1 6.213
                  6.213
```

1 12.870 12.870

```
Ε
       1 0.098
                  0.098
F
       1 1.260
                1.260
G
       1 71.868 71.868
Η
       1 5.279 5.279
$`Type II`
      Df Sum Sq Mean Sq F value Pr(>F)
Blocks 7 30.567
                 4.367
       1 21.879 21.879
Α
В
       1 8.338
                8.338
С
       1 6.213
                6.213
D
       1 12.870 12.870
Е
       1 0.098
                0.098
F
       1 1.260
                1.260
G
       1 71.868 71.868
       1 5.279
Н
                5.279
$`Type III`
      Df Sum Sq Mean Sq F value Pr(>F)
Blocks 7 30.567
                4.367
       1 21.879 21.879
В
       1 8.338
                8.338
С
       1 6.213
                6.213
D
       1 12.870 12.870
       1 0.098 0.098
F.
F
       1 1.260 1.260
G
       1 71.868 71.868
Η
       1 5.279 5.279
10.6 Chapter 8
10.6.1 p315
(174) MODEL
ANOVA(ys ~ Block + A*B + Block:A:B + C*D + A:C + A:D + B:C + B:D + A:B:C + A:B:D +
        A:C:D + B:C:D + A:B:C:D, sausage) # OK
$ANOVA
Response : ys
                    Sum Sq Mean Sq F value Pr(>F)
```

19 0.064059 0.0033715 14.134 1.74e-05 ***

12 0.002862 0.0002385

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

MODEL RESIDUALS

CORRECTED TOTAL 31 0.066922

```
$`Type I`
                                           Pr(>F)
         Df
              Sum Sq Mean Sq F value
           1 0.000903 0.000903
                                 3.7860 0.075482 .
Block
           1 0.045753 0.045753 191.8035 9.647e-09 ***
Α
В
           1 0.002628 0.002628 11.0175 0.006119 **
A:B
           1 0.001128 0.001128
                                 4.7293 0.050371 .
Block:A:B 3 0.005484 0.001828
                                 7.6638 0.004007 **
           1 0.003828 0.003828
                               16.0480 0.001743 **
C
D
           1 0.000528 0.000528
                                 2.2140 0.162566
C:D
           1 0.000253 0.000253
                                 1.0611 0.323272
           1 0.000153 0.000153
                                 0.6419 0.438593
A:C
A:D
           1 0.000903 0.000903
                                 3.7860 0.075482 .
                                 0.3275 0.577693
B:C
           1 0.000078 0.000078
B:D
           1 0.000253 0.000253
                                 1.0611 0.323272
           1 0.001378 0.001378
                                 5.7773 0.033299 *
A:B:C
A:B:D
           1 0.000703 0.000703
                                 2.9476 0.111680
A:C:D
           1 0.000028 0.000028
                                 0.1179 0.737260
B:C:D
           1 0.000028 0.000028
                                 0.1179
                                        0.737260
A:B:C:D
           1 0.000028 0.000028
                                 0.1179 0.737260
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
              Sum Sq Mean Sq F value
                                           Pr(>F)
         Df
           1 0.000903 0.000903
                                 3.7860 0.075482 .
Block
           1 0.045753 0.045753 191.8035 9.647e-09 ***
Α
В
           1 0.002628 0.002628
                                11.0175 0.006119 **
                                 4.7293 0.050371 .
A:B
           1 0.001128 0.001128
Block: A:B 3 0.005484 0.001828
                                 7.6638 0.004007 **
С
           1 0.003828 0.003828
                                16.0480 0.001743 **
D
           1 0.000528 0.000528
                                 2.2140 0.162566
C:D
           1 0.000253 0.000253
                                 1.0611 0.323272
A:C
           1 0.000153 0.000153
                                 0.6419 0.438593
           1 0.000903 0.000903
                                 3.7860 0.075482 .
A:D
B:C
           1 0.000078 0.000078
                                 0.3275 0.577693
           1 0.000253 0.000253
                                 1.0611 0.323272
B:D
A:B:C
           1 0.001378 0.001378
                                 5.7773 0.033299 *
           1 0.000703 0.000703
                                 2.9476 0.111680
A:B:D
           1 0.000028 0.000028
A:C:D
                                 0.1179 0.737260
B:C:D
           1 0.000028 0.000028
                                 0.1179 0.737260
A:B:C:D
           1 0.000028 0.000028
                                 0.1179 0.737260
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df
              Sum Sq Mean Sq F value
                                           Pr(>F)
           1 0.000903 0.000903
                                3.7860 0.075482 .
Block
```

```
Α
           1 0.045753 0.045753 191.8035 9.647e-09 ***
В
           1 0.002628 0.002628 11.0175 0.006119 **
                                4.7293 0.050371 .
A:B
           1 0.001128 0.001128
Block:A:B 3 0.005484 0.001828
                                7.6638 0.004007 **
С
           1 0.003828 0.003828 16.0480 0.001743 **
D
           1 0.000528 0.000528
                                 2.2140 0.162566
C:D
           1 0.000253 0.000253
                                 1.0611 0.323272
           1 0.000153 0.000153
A:C
                                 0.6419 0.438593
A:D
           1 0.000903 0.000903
                                 3.7860 0.075482 .
B:C
           1 0.000078 0.000078
                                0.3275 0.577693
B:D
           1 0.000253 0.000253
                                 1.0611 0.323272
A:B:C
           1 0.001378 0.001378
                                 5.7773 0.033299 *
           1 0.000703 0.000703
                                 2.9476 0.111680
A:B:D
A:C:D
           1 0.000028 0.000028
                                 0.1179 0.737260
           1 0.000028 0.000028
B:C:D
                                 0.1179 0.737260
A:B:C:D
           1 0.000028 0.000028
                                 0.1179 0.737260
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.6.2 p320
(175) MODEL
ANOVA(y ~ A*B*C*D*E, plasma) # OK
$ANOVA
Response : y
                Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                31 6672.9 215.26
RESIDUALS
                 0
                      0.0
CORRECTED TOTAL 31 6672.9
$`Type I`
          Df Sum Sq Mean Sq F value Pr(>F)
           1 1118.65 1118.65
В
           1 142.81 142.81
           1 141.96 141.96
A:B
              91.80
C
           1
                      91.80
A:C
           1
               70.81
                      70.81
B:C
           1
               5.78
                       5.78
A:B:C
               65.55
                       65.55
           1 1824.08 1824.08
D
A:D
           1 2194.53 2194.53
```

B:D

C:D

A:B:D

87.78

87.12

22.45

1

1

1

87.78

87.12

22.45

```
A:C:D
                42.78
                        42.78
            1
B:C:D
                12.25
                        12.25
            1
A:B:C:D
               375.38
                       375.38
            1
Ε
                78.75
                        78.75
               278.48
A:E
                       278.48
B:E
            1
                 0.72
                          0.72
                 0.10
                          0.10
A:B:E
            1
C:E
                 0.15
                          0.15
            1
A:C:E
            1
                 0.24
                          0.24
B:C:E
                 6.48
                          6.48
            1
A:B:C:E
            1
                 1.53
                          1.53
D:E
            1
                 8.40
                          8.40
A:D:E
                 5.28
                          5.28
            1
                          0.28
B:D:E
            1
                 0.28
A:B:D:E
                 0.60
                          0.60
            1
                 0.85
C:D:E
            1
                          0.85
A:C:D:E
            1
                 0.55
                          0.55
B:C:D:E
                 6.30
                          6.30
            1
A:B:C:D:E 1
                 0.50
                          0.50
$`Type II`
          Df Sum Sq Mean Sq F value Pr(>F)
            1 1118.65 1118.65
Α
            1 142.81 142.81
В
A:B
            1 141.96
                       141.96
С
            1
                91.80
                        91.80
A:C
                70.81
                        70.81
            1
B:C
                 5.78
                         5.78
            1
                65.55
                         65.55
A:B:C
D
            1 1824.08 1824.08
            1 2194.53 2194.53
A:D
B:D
            1
                87.78
                        87.78
A:B:D
                87.12
                        87.12
            1
C:D
            1
                22.45
                        22.45
A:C:D
                42.78
                        42.78
B:C:D
                12.25
                         12.25
            1
A:B:C:D
              375.38
                       375.38
                78.75
                        78.75
A:E
               278.48
            1
                       278.48
B:E
            1
                 0.72
                          0.72
A:B:E
                 0.10
                         0.10
            1
C:E
            1
                 0.15
                         0.15
A:C:E
            1
                 0.24
                          0.24
                 6.48
                          6.48
B:C:E
            1
A:B:C:E
                 1.53
                          1.53
            1
                 8.40
                          8.40
D:E
            1
A:D:E
            1
                 5.28
                          5.28
B:D:E
            1
                 0.28
                          0.28
```

```
0.60
A:B:D:E
           1
                 0.60
C:D:E
                 0.85
                         0.85
           1
A:C:D:E
                 0.55
                         0.55
           1
B:C:D:E
           1
                 6.30
                         6.30
A:B:C:D:E 1
                 0.50
                         0.50
$`Type III`
          Df Sum Sq Mean Sq F value Pr(>F)
Α
           1 1118.64 1118.64
В
              142.80
                      142.80
A:B
           1 141.96
                      141.96
С
                91.80
                        91.80
A:C
                70.81
                        70.81
           1
                         5.78
B:C
           1
                 5.78
A:B:C
                65.55
                        65.55
           1 1824.08 1824.08
A:D
           1 2194.53 2194.53
B:D
                87.78
                        87.78
A:B:D
                87.12
                        87.12
C:D
                22.45
                        22.45
A:C:D
                42.78
                        42.78
B:C:D
                12.25
                        12.25
A:B:C:D
              375.38
                       375.38
                78.75
                        78.75
A:E
           1
              278.48
                       278.48
B:E
                 0.72
                         0.72
           1
                 0.10
A:B:E
           1
                         0.10
C:E
                 0.15
                         0.15
           1
                 0.24
                         0.24
A:C:E
B:C:E
                 6.48
                         6.48
A:B:C:E
           1
                 1.53
                         1.53
D:E
           1
                 8.40
                         8.40
A:D:E
                 5.28
                         5.28
           1
B:D:E
           1
                 0.28
                         0.28
A:B:D:E
           1
                 0.60
                         0.60
C:D:E
                         0.85
           1
                 0.85
A:C:D:E
           1
                 0.55
                         0.55
B:C:D:E
                 6.30
                         6.30
A:B:C:D:E 1
                 0.50
                         0.50
```

10.6.3 p335

(176) MODEL

```
gear$A = as.numeric(as.character(gear$A))
gear$B = as.numeric(as.character(gear$B))
gear$C = as.numeric(as.character(gear$C))
```

```
gear$P = as.numeric(as.character(gear$P))
gear$Q = as.numeric(as.character(gear$Q))
REG(y \sim A*B*C + P + Q + A:P + A:Q + B:P + B:Q + C:P + C:Q, gear) # OK
            Estimate Std. Error Df t value Pr(>|t|)
(Intercept)
             15.4062
Α
             -4.9062
                                  0
             -0.1562
                                  0
В
A:B
              0.5312
                                  0
С
                                  0
              3.9688
A:C
              2.9062
                                  0
B:C
              0.4062
                                  0
A:B:C
              0.5938
                                  0
Ρ
             -2.3438
                                  0
             -3.4062
                                  0
Q
A:P
             -0.9062
                                  0
A:Q
             -0.3438
                                  0
B:P
                                  0
              1.0938
                                  0
B:Q
              0.1562
C:P
             -0.2812
                                  0
C:Q
              0.7812
10.7 Chapter 9
10.7.1 p349
(177) MODEL
ANOVA(pl ~ Subject + Period + Treat, antifungal) # OK
$ANOVA
Response : pl
                Df Sum Sq Mean Sq F value Pr(>F)
                18 118.558 6.5866 1.4435 0.2388
MODEL
RESIDUALS
                15 68.444 4.5630
CORRECTED TOTAL 33 187.002
$`Type I`
        Df Sum Sq Mean Sq F value Pr(>F)
Subject 16 114.642 7.1651 1.5703 0.1942
Period
             0.922 0.9224 0.2021 0.6594
Treat
             2.993 2.9932 0.6560 0.4306
$`Type II`
```

Df Sum Sq Mean Sq F value Pr(>F)

```
Subject 16 114.642 7.1651 1.5703 0.1942
             0.734 0.7344 0.1609 0.6939
Period
         1
             2.993 2.9932 0.6560 0.4306
Treat
         1
$`Type III`
        Df Sum Sq Mean Sq F value Pr(>F)
Subject 16 114.642 7.1651 1.5703 0.1942
Period
             0.734 0.7344 0.1609 0.6939
Treat
             2.993 2.9932 0.6560 0.4306
         1
10.7.2 p355
(178) MODEL
ANOVA(y ~ Group + Subject:Group + Period + Treat + Carry, bioequiv) # OK
$ANOVA
Response : y
                 Df Sum Sq Mean Sq F value
                 39 417852 10714.1 20.367 < 2.2e-16 ***
MODEL
RESIDUALS
                 68 35772
                             526.1
CORRECTED TOTAL 107 453624
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
              Df Sum Sq Mean Sq F value
                                           Pr(>F)
Group
               1 43335
                         43335 82.3763 2.46e-13 ***
Group:Subject 34 370970
                          10911 20.7406 < 2.2e-16 ***
Period
               2
                    287
                            143 0.2723
                                          0.7624
Treat
               1
                   2209
                           2209 4.1993
                                           0.0443 *
Carry
               1
                   1051
                           1051 1.9970
                                          0.1622
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
              Df Sum Sq Mean Sq F value
                                          Pr(>F)
                         32616 61.9998 3.712e-11 ***
Group
               1 32616
Group:Subject 34 370970
                          10911 20.7406 < 2.2e-16 ***
Period
               1
                     38
                             38 0.0724
                                          0.7888
                   2209
                           2209 4.1993
Treat
               1
                                           0.0443 *
                           1051 1.9970
                                          0.1622
Carry
               1
                   1051
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
```

```
CAUTION: Singularity Exists!
             Df Sum Sq Mean Sq F value
                                         Pr(>F)
              1 32616
                        32616 61.9998 3.712e-11 ***
Group
Group:Subject 34 370970
                         10911 20.7406 < 2.2e-16 ***
Period
              1
                    38
                            38 0.0724
                                          0.7888
Treat
              1
                  2209
                          2209 4.1993
                                          0.0443 *
Carry
              1
                  1051
                          1051 1.9970
                                         0.1622
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(179) MODEL
ANOVA(y ~ Subject + Period + Treat + Carry, bioequiv) # OK
$ANOVA
Response : y
                Df Sum Sq Mean Sq F value Pr(>F)
                39 417852 10714.1 20.367 < 2.2e-16 ***
MODEL
RESIDUALS
                68 35772
                            526.1
CORRECTED TOTAL 107 453624
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value Pr(>F)
Subject 35 414306 11837.3 22.5016 <2e-16 ***
Period
             287
                   143.3 0.2723 0.7624
            2209 2209.1 4.1993 0.0443 *
Treat
        1
            1051 1050.6 1.9970 0.1622
Carry
        1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value Pr(>F)
Subject 35 403586 11531.0 21.9194 <2e-16 ***
Period
              38
                    38.1 0.0724 0.7888
        1
Treat
            2209 2209.1 4.1993 0.0443 *
        1
            1051 1050.6 1.9970 0.1622
Carry
        1
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
       Df Sum Sq Mean Sq F value Pr(>F)
Subject 35 403586 11531.0 21.9194 <2e-16 ***
Period
        1
              38
                    38.1 0.0724 0.7888
Treat
            2209 2209.1 4.1993 0.0443 *
```

1

```
1 1051 1050.6 1.9970 0.1622
Carry
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.7.3 p361
(180) MODEL
ANOVA(Time ~ Subject + Period + Treat + Carry, chipman) # OK
$ANOVA
Response : Time
               Df Sum Sq Mean Sq F value
                                           Pr(>F)
MODEL
               17 28.0757 1.65151 64.421 1.139e-12 ***
RESIDUALS
               18 0.4615 0.02564
CORRECTED TOTAL 35 28.5372
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
       Df Sum Sq Mean Sq F value
Subject 11 24.2084 2.20076 85.8462 3.157e-13 ***
Period 2 3.2065 1.60325 62.5388 7.894e-09 ***
Treat
        2 0.4276 0.21382 8.3406 0.002733 **
        2 0.2332 0.11660 4.5484 0.025188 *
Carry
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
Subject 11 24.2547 2.20497 86.0105 3.104e-13 ***
Period
       1 0.0018 0.00184 0.0717 0.7919554
        2 0.6392 0.31958 12.4661 0.0004003 ***
Treat
Carry
        2 0.2332 0.11660 4.5484 0.0251881 *
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
       Df Sum Sq Mean Sq F value
Subject 11 24.2547 2.20497 86.0105 3.104e-13 ***
Period 1 0.0018 0.00184 0.0717 0.7919554
        2 0.6392 0.31958 12.4661 0.0004003 ***
Treat
        2 0.2332 0.11660 4.5484 0.0251881 *
Carry
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

10.7.4 p372

(181) MODEL

```
residue$lc1 = log(residue$X1)
residue$1c2 = log(residue$X2)
residue$1c3 = log(residue$X3)
residue$lc4 = log(residue$X4)
residue$1c5 = log(residue$X5)
residue$sp = 7*residue$lc2+ 14*residue$lc3 + 30*residue$lc4 + 60*residue$lc5
residue$sm = residue$lc1 + residue$lc2+ residue$lc3 + residue$lc4 + residue$lc5
residue$num = 5*residue$sp - 111*residue$sm
residue$den = 5*4745 - 111^2
residue$k = residue$num/residue$den
residue HL = -log(2)/residuek
residue$logHL = log(residue$HL)
ANOVA(logHL ~ temp*moisture*soil, residue) # OK
$ANOVA
Response : logHL
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
                7 7.5133 1.07332 13.543 0.0007329 ***
RESIDUALS
                8 0.6340 0.07925
CORRECTED TOTAL 15 8.1473
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
                  Df Sum Sq Mean Sq F value
                                               Pr(>F)
                   1 6.0503 6.0503 76.3427 2.303e-05 ***
temp
moisture
                   1 0.9521 0.9521 12.0134 0.008492 **
                   1 0.0013 0.0013 0.0162 0.901779
temp:moisture
soil
                   1 0.4098 0.4098 5.1712 0.052559 .
temp:soil
                   1 0.0086 0.0086 0.1081 0.750753
                   1 0.0860 0.0860 1.0855 0.327921
moisture:soil
temp:moisture:soil 1 0.0051 0.0051 0.0648 0.805427
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
                  Df Sum Sq Mean Sq F value
                                               Pr(>F)
                   1 6.0503 6.0503 76.3427 2.303e-05 ***
temp
                   1 0.9521 0.9521 12.0134 0.008492 **
moisture
                   1 0.0013 0.0013 0.0162 0.901779
temp:moisture
soil
                   1 0.4098 0.4098 5.1712 0.052559 .
temp:soil
                   1 0.0086 0.0086 0.1081 0.750753
moisture:soil
                   1 0.0860 0.0860 1.0855 0.327921
```

```
temp:moisture:soil 1 0.0051 0.0051 0.0648 0.805427
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
                  Df Sum Sq Mean Sq F value
                                              Pr(>F)
                   1 6.0503 6.0503 76.3427 2.303e-05 ***
temp
moisture
                   1 0.9521 0.9521 12.0134 0.008492 **
                   1 0.0013 0.0013 0.0162 0.901779
temp:moisture
soil
                   1 0.4098 0.4098 5.1712 0.052559 .
                   1 0.0086 0.0086 0.1081 0.750753
temp:soil
                   1 0.0860 0.0860 1.0855 0.327921
moisture:soil
temp:moisture:soil 1 0.0051 0.0051 0.0648 0.805427
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.8 Chapter 11
10.8.1 p461
(182) MODEL
ANOVA(y ~ x1 + x2 + x1:x2 + x1:x3 + x2:x3, pest) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                                            Pr(>F)
MODEL
                5 275.642 55.128 160.38 4.631e-07 ***
                           0.344
RESIDUALS
                7
                    2.406
CORRECTED TOTAL 12 278.048
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
         Sum Sq Mean Sq F value
       1 83.402 83.402 242.6351 1.086e-06 ***
x1
x2
       1 161.734 161.734 470.5191 1.116e-07 ***
x1:x2 1
         0.246
                  0.246
                          0.7169 0.4251627
x1:x3 1 15.663 15.663 45.5660 0.0002649 ***
x2:x3 1 14.596 14.596 42.4614 0.0003291 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
     Df Sum Sq Mean Sq F value
                                  Pr(>F)
      1 215.951 215.951 628.246 4.105e-08 ***
x1
```

```
1 175.256 175.256 509.855 8.458e-08 ***
x2
x1:x2 1 0.025 0.025 0.072 0.7961658
x1:x3 1 14.539 14.539 42.298 0.0003330 ***
x2:x3 1 14.596 14.596 42.461 0.0003291 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
     Df Sum Sq Mean Sq F value
x1
      1 178.372 178.372 518.922 7.958e-08 ***
      1 145.518 145.518 423.341 1.608e-07 ***
x2
x1:x2 1 0.025
                0.025 0.072 0.7961658
x1:x3 1 14.539 14.539 42.298 0.0003330 ***
x2:x3 1 14.596 14.596 42.461 0.0003291 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.8.2 p469
(183) MODEL
ANOVA(y ~ x1 + x2 + x1:x2 + x1:x3 + x2:x3 + x1:x2:x3, polvdat) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value
                6 12.5313 2.08854 37.056 0.0005473 ***
MODEL
                5 0.2818 0.05636
RESIDUALS
CORRECTED TOTAL 11 12.8131
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
        Df Sum Sq Mean Sq F value
                                    Pr(>F)
         1 5.4668 5.4668 96.9942 0.0001839 ***
         1 0.3660 0.3660 6.4944 0.0513654 .
         1 4.6897 4.6897 83.2068 0.0002652 ***
x1:x2
         1 1.2450 1.2450 22.0887 0.0053378 **
x1:x3
         1 0.4707 0.4707 8.3509 0.0341949 *
x2:x3
x1:x2:x3 1 0.2931 0.2931 5.2004 0.0714991 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
        Df Sum Sq Mean Sq F value
                                    Pr(>F)
         1 0.0184 0.0184 0.3265 0.5924707
x1
```

```
1 0.2419 0.2419 4.2911 0.0930613 .
x2
        1 3.8824 3.8824 68.8834 0.0004147 ***
x1:x2
x1:x3
        1 1.4383 1.4383 25.5196 0.0039276 **
x2:x3
        1 0.4707 0.4707 8.3509 0.0341949 *
x1:x2:x3 1 0.2931 0.2931 5.2004 0.0714991 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
       Df Sum Sq Mean Sq F value Pr(>F)
        1 0.25744 0.25744 4.5677 0.08562 .
x1
        1 0.12956 0.12956 2.2987 0.18992
x2
x1:x2
        1 0.65909 0.65909 11.6939 0.01885 *
        1 0.26323 0.26323 4.6704 0.08307 .
x1:x3
        1 0.12999 0.12999 2.3063 0.18931
x2:x3
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

10.8.3 p482

(184) MODEL

```
REG(y ~ x1 + x2 + x3 + x1:x2 + x1:x3 + x2:x3 + x1:z1 + x2:z1 + x3:z1 + x1:x2:z1 + x1:x3:z1 + x2:x3:z1 + x1:z2 + x2:z2 + x3:z2 + x1:x2:z2 + x1:x3:z2 + x2:x3:z2 + x1:z1:z2 + x2:z1:z2 + x3:z1:z2 + x1:x2:z1:z2 + x1:x3:z1:z2 + x2:x3:z1:z2 - 1, MPV) # OK
```

```
Estimate Std. Error Df t value Pr(>|t|)
x1
              346948
                         294197 11 1.1793 0.2631550
                8223
                            490 11 16.7869 3.467e-09 ***
x2
x3
                1656
                            459 11 3.6104 0.0040950 **
                         312262 11 -1.3273 0.2113017
x1:x2
             -414463
             -334747
                         311426 11 -1.0749 0.3054382
x1:x3
                           1199 11 -5.4032 0.0002156 ***
               -6476
x2:x3
                         328922 11 0.3133 0.7599297
x1:z1
              103044
x2:z1
               -2241
                            548 11 -4.0924 0.0017824 **
x3:z1
                 823
                            513 11 1.6056 0.1366709
                         349120 11 -0.1834 0.8578546
x1:x2:z1
              -64013
                         348184 11 -0.3554 0.7290412
x1:x3:z1
             -123730
x2:x3:z1
                4659
                           1340 11 3.4765 0.0051806 **
x1:z2
              244320
                         328922 11 0.7428 0.4731733
x2:z2
                 886
                            548 11 1.6187 0.1338108
                            513 11 0.1670 0.8704301
x3:z2
                  86
x1:x2:z2
             -266052
                         349120 11 -0.7621 0.4620497
x1:x3:z2
             -253151
                         348184 11 -0.7271 0.4823761
```

```
x2:x3:z2
             -1822
                          1340 11 -1.3593 0.2012686
             259038
                        328922 11 0.7875 0.4476062
x1:z1:z2
                           548 11 -0.2500 0.8071853
x2:z1:z2
               -137
x3:z1:z2
                100
                           513 11 0.1955 0.8485983
                        349120 11 -0.7720 0.4563702
x1:x2:z1:z2 -269527
x1:x3:z1:z2 -269249
                       348184 11 -0.7733 0.4556454
x2:x3:z1:z2
               -328
                          1340 11 -0.2448 0.8111141
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.9 Chapter 12
10.9.1 p513
(185) MODEL
ANOVA(ybar ~ A + B + C + D + E + F + G, tile) # OK
$ANOVA
Response : ybar
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                7 0.68737 0.098196
RESIDUALS
                0 0.00000
CORRECTED TOTAL 7 0.68737
$`Type I`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 0.04984 0.04984
B 1 0.01992 0.01992
C 1 0.51534 0.51534
D 1 0.01532 0.01532
E 1 0.05965 0.05965
F 1 0.00879 0.00879
G 1 0.01851 0.01851
$`Type II`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 0.04984 0.04984
B 1 0.01992 0.01992
C 1 0.51534 0.51534
D 1 0.01532 0.01532
E 1 0.05965 0.05965
F 1 0.00879 0.00879
```

\$`Type III`

G 1 0.01851 0.01851

```
Df Sum Sq Mean Sq F value Pr(>F)
A 1 0.04984 0.04984
B 1 0.01992 0.01992
C 1 0.51534 0.51534
D 1 0.01532 0.01532
E 1 0.05965 0.05965
F 1 0.00879 0.00879
G 1 0.01851 0.01851
(186) MODEL
ANOVA(lns2 ~ A + B + C + D + E + F + G, tile) # OK
$ANOVA
Response : lns2
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                7 12.305 1.7578
RESIDUALS
                0.000
CORRECTED TOTAL 7 12.305
$`Type I`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 1.6436 1.6436
B 1 0.3109 0.3109
C 1 7.1858 7.1858
D 1 2.3199 2.3199
E 1 0.0248 0.0248
F 1 0.7379 0.7379
G 1 0.0820 0.0820
$`Type II`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 1.6436 1.6436
B 1 0.3109 0.3109
C 1 7.1858 7.1858
D 1 2.3199 2.3199
E 1 0.0248 0.0248
F 1 0.7379 0.7379
G 1 0.0820 0.0820
$`Type III`
  Df Sum Sq Mean Sq F value Pr(>F)
A 1 1.6436 1.6436
B 1 0.3109 0.3109
C 1 7.1858 7.1858
D 1 2.3199 2.3199
```

E 1 0.0248 0.0248

```
F 1 0.7379 0.7379
G 1 0.0820 0.0820
```

10.9.2 p521

(187) MODEL

```
strng = reshape(tile,
       direction = "long",
       varying = list(c("y1", "y2")),
       v.names = "y",
        idvar = c("A", "B", "C", "D", "E", "F", "G"),
       timevar = "H",
        times = c(-1, 1)
ANOVA(y ~ A/H + B/H + C/H + D/H + E/H + F/H + G/H, strng) # OK
$ANOVA
Response : y
               Df Sum Sq Mean Sq F value Pr(>F)
               14 1.65427 0.11816 0.1433 0.9807
MODEL
RESIDUALS
                1 0.82473 0.82473
CORRECTED TOTAL 15 2.47901
$`Type I`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 0.09968 0.09968 0.1209 0.7870
A:H 1 0.04015 0.04015 0.0487 0.8618
    1 0.03984 0.03984 0.0483 0.8623
H:B 1 0.00043 0.00043 0.0005 0.9854
     1 1.03069 1.03069 1.2497 0.4646
H:C 1 0.15307 0.15307 0.1856 0.7410
     1 0.03064 0.03064 0.0372 0.8788
H:D 1 0.04690 0.04690 0.0569 0.8510
     1 0.11929 0.11929 0.1446 0.7686
H:E 1 0.01883 0.01883 0.0228 0.9045
     1 0.01758 0.01758 0.0213 0.9077
H:F 1 0.01384 0.01384 0.0168 0.9180
     1 0.03702 0.03702 0.0449 0.8671
H:G 1 0.00632 0.00632 0.0077 0.9444
$`Type II`
   Df Sum Sq Mean Sq F value Pr(>F)
     1 0.09968 0.09968 0.1209 0.7870
A:H 1 0.04015 0.04015 0.0487 0.8618
     1 0.03984 0.03984 0.0483 0.8623
H:B 1 0.00043 0.00043 0.0005 0.9854
```

```
1 1.03069 1.03069 1.2497 0.4646
H:C 1 0.15307 0.15307 0.1856 0.7410
             1 0.03064 0.03064 0.0372 0.8788
H:D 1 0.04690 0.04690 0.0569 0.8510
             1 0.11929 0.11929 0.1446 0.7686
H:E 1 0.01883 0.01883 0.0228 0.9045
             1 0.01758 0.01758 0.0213 0.9077
H:F 1 0.01384 0.01384 0.0168 0.9180
             1 0.03702 0.03702 0.0449 0.8671
H:G 1 0.00632 0.00632 0.0077 0.9444
$`Type III`
          Df Sum Sq Mean Sq F value Pr(>F)
            1 0.09968 0.09968 0.1209 0.7870
A:H 1 0.04015 0.04015 0.0487 0.8618
             1 0.03984 0.03984 0.0483 0.8623
H:B 1 0.00043 0.00043 0.0005 0.9854
             1 1.03069 1.03069 1.2497 0.4646
H:C 1 0.15307 0.15307 0.1856 0.7410
             1 0.03064 0.03064 0.0372 0.8788
H:D 1 0.04690 0.04690 0.0569 0.8510
             1 0.11929 0.11929 0.1446 0.7686
H:E 1 0.01883 0.01883 0.0228 0.9045
             1 0.01758 0.01758 0.0213 0.9077
H:F 1 0.01384 0.01384 0.0168 0.9180
             1 0.03702 0.03702 0.0449 0.8671
H:G 1 0.00632 0.00632 0.0077 0.9444
10.9.3 p525
(188) MODEL
prod2 = af(prodstd, 1:7)
ANOVA(Pof \sim A + B + C + D + E + F + G + A:G + A:E:F + B:E:G + C:E:G + C:E:G:F + ANOVA(Pof \sim A + B + C + D + E + F + G + A:G + A:E:F + B:E:G + C:E:G + C:E:G:F + ANOVA(Pof \sim A + B + C + D + E + F + G + A:G + A:E:F + B:E:G + C:E:G + C:E:G:F + ANOVA(Pof \sim A + B + C + D + E + F + G + A:G + A:G + A:E:F + B:E:G + C:E:G + C:E:G:F + ANOVA(Pof \sim A + B + C + D + E + F + G + A:G + A:G + A:E:F + B:E:G + C:E:G + C:E:G:F + ANOVA(Pof \sim A + B + C + D + E + F + G + A:G + A:E:F + B:E:G + C:E:G + C:E:G:F + ANOVA(Pof \sim A + B + C + D + E + F + G + A:G + A:E:F + B:E:G + C:E:G + C:
                          D:E + D:F, prod2) # OK
$ANOVA
Response : Pof
                                         Df Sum Sq Mean Sq F value
                                                                                                                   Pr(>F)
MODEL
                                         47 769.49 16.3721 5.1667 2.737e-05 ***
RESIDUALS
                                         24 76.05 3.1688
CORRECTED TOTAL 71 845.54
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
```

```
Df Sum Sq Mean Sq F value
                                    Pr(>F)
                  25.288 7.9806 0.0022023 **
Α
        2 50.577
В
        2 13.384
                    6.692 2.1118 0.1429491
С
        2 68.594 34.297 10.8234 0.0004463 ***
D
        2 23.674 11.837 3.7355 0.0386914 *
Ε
        1 275.733 275.733 87.0165 1.878e-09 ***
F
        1 161.700 161.700 51.0296 2.204e-07 ***
G
            1.051
                    1.051 0.3318 0.5699896
        2 26.567 13.284 4.1921 0.0274494 *
A:G
A:E:F
        7 28.404
                    4.058 1.2806 0.3013844
        7 22.453
                    3.208 1.0123 0.4475160
B:E:G
C:E:G
        6 35.546
                    5.924 1.8696 0.1277692
C:E:F:G 10 24.607
                    2.461 0.7766 0.6500534
        2 21.745 10.873 3.4312 0.0489076 *
D:E
D:F
        2 15.450
                    7.725 2.4379 0.1086730
___
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
       Df Sum Sq Mean Sq F value
                                    Pr(>F)
        2 50.577 25.288 7.9806 0.0022023 **
В
        2 13.384
                    6.692 2.1118 0.1429491
С
        2 68.594 34.297 10.8234 0.0004463 ***
D
        2 23.674 11.837 3.7355 0.0386914 *
F.
        1 275.733 275.733 87.0165 1.878e-09 ***
F
        1 161.700 161.700 51.0296 2.204e-07 ***
G
            1.051
                    1.051 0.3318 0.5699896
        2 26.567 13.284 4.1921 0.0274494 *
A:G
        6 24.623
                    4.104 1.2951 0.2970196
A:E:F
B:E:G
        6 19.770
                    3.295 1.0398 0.4246194
                    5.924 1.8696 0.1277692
C:E:G
        6 35.546
C:E:F:G 10 24.607
                    2.461 0.7766 0.6500534
D:E
        2 21.745 10.873 3.4312 0.0489076 *
D:F
        2 15.450
                    7.725 2.4379 0.1086730
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
CAUTION: Singularity Exists!
       Df Sum Sq Mean Sq F value
                                    Pr(>F)
        2 50.577 25.288 7.9806 0.0022023 **
Α
В
        2 13.384
                    6.692 2.1118 0.1429491
С
        2 68.594 34.297 10.8234 0.0004463 ***
D
        2 23.674 11.837 3.7355 0.0386914 *
Ε
        1 275.733 275.733 87.0165 1.878e-09 ***
F
        1 161.700 161.700 51.0296 2.204e-07 ***
G
        1
            1.051
                    1.051 0.3318 0.5699896
        2 26.567 13.284 4.1921 0.0274494 *
A:G
```

```
A:E:F 6 24.623 4.104 1.2951 0.2970196
        6 19.770 3.295 1.0398 0.4246194
B:E:G
C:E:G 6 35.546 5.924 1.8696 0.1277692
C:E:F:G 10 24.607 2.461 0.7766 0.6500534
D:E
     2 21.745 10.873 3.4312 0.0489076 *
        2 15.450 7.725 2.4379 0.1086730
D:F
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.9.4 p532
(189) MODEL
ANOVA(torque ~ A + B + C + D + E + A:B + A:C + A:D + A:E, Smotor) # OK
$ANOVA
Response : torque
                              Mean Sq F value Pr(>F)
                     Sum Sq
MODEL
               15 0.0112217 0.00074811
                                       102.2 0.009731 **
                2 0.0000146 0.00000732
RESIDUALS
CORRECTED TOTAL 17 0.0112363
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type I`
   Df
         Sum Sq Mean Sq F value
    1 0.0039545 0.0039545 540.2187 0.001846 **
В
    2 0.0003817 0.0001909 26.0732 0.036937 *
C
    2 0.0057241 0.0028620 390.9837 0.002551 **
    2 0.0000265 0.0000133 1.8104 0.355820
    1 0.0000984 0.0000984 13.4406 0.067009 .
A:B 2 0.0010068 0.0005034 68.7668 0.014333 *
A:C 2 0.0000031 0.0000016 0.2134 0.824110
A:D 2 0.0000009 0.0000004 0.0599 0.943521
A:E 1 0.0000258 0.0000258 3.5198 0.201458
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df
                 Mean Sq F value
         Sum Sq
                                   Pr(>F)
    1 0.0039545 0.0039545 540.2187 0.001846 **
Α
В
    2 0.0003817 0.0001909 26.0732 0.036937 *
С
    2 0.0032014 0.0016007 218.6753 0.004552 **
    2 0.0000268 0.0000134 1.8319 0.353123
Ε
    1 0.0000423 0.0000423
                           5.7744 0.138172
A:B 2 0.0010068 0.0005034 68.7668 0.014333 *
```

```
A:C 2 0.0000031 0.0000016 0.2134 0.824110
A:D 2 0.0000052 0.0000026 0.3536 0.738760
A:E 1 0.0000258 0.0000258 3.5198 0.201458
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
         Df
                        Sum Sq Mean Sq F value
                                                                                           Pr(>F)
            1 0.0034241 0.0034241 467.7636 0.002131 **
            2 0.0003817 0.0001909 26.0732 0.036937 *
В
С
            2 0.0032014 0.0016007 218.6753 0.004552 **
            2 0.0000268 0.0000134 1.8319 0.353123
Ε
            1 0.0000423 0.0000423 5.7744 0.138172
A:B 2 0.0010068 0.0005034 68.7668 0.014333 *
A:C 2 0.0000031 0.0000016 0.2134 0.824110
A:D 2 0.0000052 0.0000026 0.3536 0.738760
A:E 1 0.0000258 0.0000258 3.5198 0.201458
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
10.9.5 p535
(190) MODEL
ANOVA(shrinkage \sim A + B + C + D + E + F + G + A:B + A:C + A:D + A:E + A:F + A:G + A:B + A:C + 
                                      B:D, inject) # OK
$ANOVA
Response : shrinkage
                                      Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                                      14 6659.4 475.67 129.08 1.97e-05 ***
RESIDUALS
                                        5
                                                  18.4
                                                                     3.68
CORRECTED TOTAL 19 6677.8
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type I`
         Df Sum Sq Mean Sq F value
                                                                                    Pr(>F)
            1 770.1
                                    770.1 208.9722 2.858e-05 ***
Α
В
            1 5076.6 5076.6 1377.6289 2.674e-07 ***
С
                                                           0.8311 0.403773
            1
                        3.1
                                           3.1
D
                                           7.6
                                                            2.0522 0.211416
            1
                        7.6
Ε
            1
                        0.6
                                        0.6
                                                       0.1526 0.712112
F
                        0.6
                                        0.6
                                                      0.1526 0.712112
            1
G
                     95.1
                                        95.1
                                                         25.7972 0.003837 **
            1
A:B 1 564.1 564.1 153.0699 6.112e-05 ***
```

```
A:C 1
        10.6
                10.6
                        2.8664
                                0.151230
    1 115.6
                       31.3602
                                0.002508 **
A:D
               115.6
A:E
        14.1
                14.1
                        3.8161
                                0.108185
A:F
          1.6
                 1.6
                        0.4240
    1
                                 0.543677
A:G 1
         0.1
                 0.1
                        0.0170
                                0.901459
         0.1
                        0.0170 0.901459
B:D
                 0.1
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type II`
   Df Sum Sq Mean Sq
                       F value
                                   Pr(>F)
     1 770.1
               770.1 208.9722 2.858e-05 ***
     1 5076.6 5076.6 1377.6289 2.674e-07 ***
В
С
                  3.1
                        0.8311 0.403773
    1
         3.1
D
         7.6
                 7.6
    1
                        2.0522
                                0.211416
Ε
         0.6
                 0.6
                        0.1526
                                0.712112
    1
F
    1
         0.6
                 0.6
                        0.1526
                                0.712112
G
                       25.7972 0.003837 **
     1
        95.1
                95.1
A:B
    1 564.1
               564.1 153.0699 6.112e-05 ***
A:C
        10.6
                10.6
                        2.8664 0.151230
                       31.3602 0.002508 **
A:D
    1 115.6
               115.6
        14.1
                 14.1
                        3.8161
A:E
    1
                                0.108185
A:F
    1
         1.6
                 1.6
                        0.4240
                                0.543677
A:G 1
         0.1
                 0.1
                        0.0170
                                0.901459
                        0.0170 0.901459
B:D
    1
         0.1
                 0.1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type III`
   Df Sum Sq Mean Sq
                       F value
                                   Pr(>F)
    1 770.1
               770.1 208.9722 2.858e-05 ***
Α
В
    1 5076.6 5076.6 1377.6289 2.674e-07 ***
С
    1
         3.1
                 3.1
                        0.8311 0.403773
D
         7.6
                 7.6
                        2.0522 0.211416
     1
Ε
         0.6
                 0.6
                        0.1526
                                0.712112
     1
F
         0.6
     1
                 0.6
                        0.1526
                                0.712112
G
        95.1
                        25.7972 0.003837 **
                95.1
A:B
       564.1
               564.1 153.0699 6.112e-05 ***
A:C
        10.6
                10.6
                        2.8664 0.151230
    1
A:D 1 115.6
                       31.3602 0.002508 **
               115.6
A:E 1
        14.1
                14.1
                        3.8161 0.108185
A:F
         1.6
                 1.6
                        0.4240
                                0.543677
    1
A:G
         0.1
                 0.1
                        0.0170
                                0.901459
    1
B:D
                        0.0170
                                0.901459
    1
         0.1
                 0.1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

10.9.6 p539

(191) MODEL

A:C 1 0.03218 0.03218

```
eptax = cbind(eptaxr[1:16,], y2=eptaxr[17:32,9], y3=eptaxr[33:48,9],
                                           y5=eptaxr[49:64,9])
eptax$ybar = (eptax$y + eptax$y2 + eptax$y3 + eptax$y5)/4
ANOVA(ybar \sim A + B + C + D + E + F + G + H + A:B + A:C + A:D + A:E + A:F + A:G + A:B + A:C + A:B + A:C + A:B + A:C + A:B + A:C + A
                                  A:H, eptax) # OK
$ANOVA
Response : ybar
                                                  Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                                                  15 2.8452 0.18968
RESIDUALS
                                                     0 0.0000
CORRECTED TOTAL 15 2.8452
$`Type I`
           Df Sum Sq Mean Sq F value Pr(>F)
               1 0.02686 0.02686
В
               1 0.00042 0.00042
С
               1 0.06306 0.06306
D
               1 2.49443 2.49443
F.
             1 0.00304 0.00304
F
               1 0.03209 0.03209
               1 0.02954 0.02954
Н
               1 0.12879 0.12879
A:B 1 0.00047 0.00047
A:C 1 0.03218 0.03218
A:D 1 0.01185 0.01185
A:E 1 0.00380 0.00380
A:F 1 0.01674 0.01674
A:G 1 0.00186 0.00186
A:H 1 0.00012 0.00012
$`Type II`
           Df Sum Sq Mean Sq F value Pr(>F)
               1 0.02686 0.02686
               1 0.00042 0.00042
С
               1 0.06306 0.06306
D
               1 2.49443 2.49443
Ε
               1 0.00304 0.00304
F
               1 0.03209 0.03209
G
               1 0.02954 0.02954
Η
               1 0.12879 0.12879
A:B 1 0.00047 0.00047
```

```
A:D 1 0.01185 0.01185
A:E 1 0.00380 0.00380
A:F 1 0.01674 0.01674
A:G 1 0.00186 0.00186
A:H 1 0.00012 0.00012
$`Type III`
   Df Sum Sq Mean Sq F value Pr(>F)
    1 0.02686 0.02686
В
    1 0.00042 0.00042
С
    1 0.06306 0.06306
D
    1 2.49443 2.49443
Е
    1 0.00304 0.00304
F
    1 0.03209 0.03209
    1 0.02954 0.02954
G
    1 0.12879 0.12879
A:B 1 0.00047 0.00047
A:C 1 0.03218 0.03218
A:D 1 0.01185 0.01185
A:E 1 0.00380 0.00380
A:F 1 0.01674 0.01674
A:G 1 0.00186 0.00186
A:H 1 0.00012 0.00012
```

11 Searle - Linear Models 2e

Reference

• Searle SR, Gruber MHJ. Linear Models 2e, Kindle Edition. John Wiley & Sons Inc. 2016.

weight = c(8,13,9,12,7,11,6,12,12,14,9,7,14,16,10,14,11,13)

"tc", "tc", "tc", "tc")

11.1 7.2 (p390, 59%)

(192) MODEL

```
variety = c("va","va","va","vd","vd","vd","va","vb","vb","vb","vb","vc",
           "vc", "vd", "vd", "vd")
d1 = data.frame(weight, treatment, variety)
ANOVA(weight ~ treatment*variety, d1)
$ANOVA
Response : weight
               Df Sum Sq Mean Sq F value Pr(>F)
MODEL
                7
                      82 11.714 2.0918
                                          0.14
RESIDUALS
               10
                      56
                           5.600
CORRECTED TOTAL 17
                     138
$`Type I`
                 Df Sum Sq Mean Sq F value Pr(>F)
                  2 10.500 5.250 0.9375 0.42348
treatment
                  3 36.786 12.262 2.1896 0.15232
variety
treatment:variety 2 34.714 17.357 3.0995 0.08965 .
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
$`Type II`
                 Df Sum Sq Mean Sq F value Pr(>F)
                  2 9.486 4.7429 0.8469 0.45731
treatment
                  3 36.786 12.2619 2.1896 0.15232
variety
treatment: variety 2 34.714 17.3571 3.0995 0.08965 .
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
$`Type III`
                 Df Sum Sq Mean Sq F value Pr(>F)
treatment
                  2 12.471 6.2353 1.1134 0.36595
                  3 34.872 11.6240 2.0757 0.16719
variety
treatment:variety 2 34.714 17.3571 3.0995 0.08965 .
```

```
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
options(contrasts = c("contr.sum", "contr.poly"))
Anova(lm(weight ~ treatment*variety, d1), type=3, singular.ok=TRUE) # NOT OK
Note: model has aliased coefficients
      sums of squares computed by model comparison
Anova Table (Type III tests)
Response: weight
                  Sum Sq Df F values Pr(>F)
treatment
                  0.000 0
                  0.000 0
variety
treatment:variety 34.714 2
                             3.0995 0.08965 .
Residuals
                 56.000 10
___
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
11.2 7.2 (p393, 60%)
(193) MODEL
percent = c(31,33,44,36,38,26,37,59,42,42,34,42,28,39,36,32,38,42,36,22,42,46,
            26,37,43)
refinery = c(rep("g",9),rep("n",8),rep("s",8))
process = as.factor(c(1,1,1,1,1,1,2,2,2,1,1,1,1,2,2,2,2,1,1,1,2,2,2,2,2))
source0 = c("t","t","t","t","o","m","t","o","m","i","i","i","i","t","o","m","m",
            "t", "o", "i", "o", "o", "m", "i", "i")
d2 = data.frame(percent, refinery, process, source=source0)
ANOVA(percent ~ refinery*source, d2)
$ANOVA
Response : percent
                Df Sum Sq Mean Sq F value Pr(>F)
                10 442.56 44.256 0.6361 0.7616
MODEL
RESIDUALS
                14 974.00 69.571
CORRECTED TOTAL 24 1416.56
$`Type I`
               Df Sum Sq Mean Sq F value Pr(>F)
                2 20.963 10.481 0.1507 0.8615
refinery
                 3 266.124 88.708 1.2751 0.3212
source
refinery:source 5 155.474 31.095 0.4469 0.8086
```

```
$`Type II`
```

Df Sum Sq Mean Sq F value Pr(>F)
refinery 2 25.535 12.767 0.1835 0.8343
source 3 266.124 88.708 1.2751 0.3212
refinery:source 5 155.474 31.095 0.4469 0.8086

\$`Type III`

Df Sum Sq Mean Sq F value Pr(>F)
refinery 2 10.766 5.383 0.0774 0.9259
source 3 282.633 94.211 1.3542 0.2972
refinery:source 5 155.474 31.095 0.4469 0.8086

```
options(contrasts=c("contr.sum", "contr.poly"))
Anova(lm(percent ~ refinery*source, d2), type=3, singular.ok=TRUE) # NOT OK
```

Note: model has aliased coefficients sums of squares computed by model comparison

Anova Table (Type III tests)

Response: percent

 Sum Sq Df
 F values
 Pr(>F)

 refinery
 2.52
 1
 0.0362
 0.8518

 source
 268.19
 2
 1.9275
 0.1822

 refinery:source
 155.47
 5
 0.4469
 0.8086

Residuals 974.00 14

12 Test Summary

Package	Version	Total Count	Identical to SAS	Different from SAS
sasLM	0.6.5	193	193 (100%)	0 (0%)
car	3.0.11	193	< 174 (90%)	>= 20 (10%)

All of the results in sasLM 0.6.5 were identical, while type III SSs of Model (83) and (84) were different from those of SAS in sasLM 0.1.2 package.

Slight differences in the last digits between type II and type III SS (when they should be same) are resulted from the round-to-even number way of R rounding function.

If you are uncertain about the equivalence of the 'sasLM' to 'SAS,' you can use 'SAS University Edition' for free.

If you find any discrepancies, please mail to the author, Kyun-Seop Bae k@acr.kr.

13 Sesssion Information

```
R version 4.1.2 (2021-11-01)
Platform: x86_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 17763)
Matrix products: default
locale:
[1] LC_COLLATE=Korean_Korea.949 LC_CTYPE=Korean_Korea.949
[3] LC_MONETARY=Korean_Korea.949 LC_NUMERIC=C
[5] LC_TIME=Korean_Korea.949
attached base packages:
[1] stats
              graphics grDevices utils
                                             datasets methods
                                                                 base
other attached packages:
[1] daewr_1.2-7
                   car_3.0-11
                                  carData_3.0-4 sasLM_0.6.5
                                                                 mvtnorm_1.1-3
[6] rmarkdown_2.11
loaded via a namespace (and not attached):
 [1] tinytex_0.34
                          zoo_1.8-9
                                                xfun_0.27
[4] partitions_1.10-4
                          haven_2.4.3
                                                lattice_0.20-45
 [7] colorspace_2.0-2
                          vctrs_0.3.8
                                                htmltools_0.5.2
[10] yaml_2.2.1
                          gmp_0.6-2
                                                utf8_1.2.2
[13] rlang_0.4.12
                          pillar_1.6.4
                                                foreign_0.8-81
[16] readxl_1.3.1
                          lifecycle_1.0.1
                                                stringr_1.4.0
[19] combinat 0.0-8
                          cellranger_1.1.0
                                                DoE.base 1.2
[22] zip_2.2.0
                          evaluate_0.14
                                                knitr_1.36
[25] rio_0.5.27
                          forcats_0.5.1
                                                fastmap_1.1.0
[28] lmtest_0.9-38
                                                curl_4.3.2
                          numbers_0.8-2
[31] fansi_0.5.0
                          vcd_1.4-9
                                                conf.design_2.0.0
[34] Rcpp_1.0.7
                          polynom_1.4-0
                                                scatterplot3d_0.3-41
[37] abind 1.4-5
                          FrF2 2.2-2
                                                hms 1.1.1
[40] digest_0.6.28
                          stringi_1.7.6
                                                openxlsx_4.2.4
[43] grid_4.1.2
                          mathjaxr_1.4-0
                                                tools_4.1.2
[46] magrittr 2.0.1
                          tibble 3.1.5
                                                crayon_1.4.2
[49] pkgconfig_2.0.3
                          ellipsis_0.3.2
                                                MASS_7.3-54
[52] data.table_1.14.2
                          sfsmisc_1.1-12
                                                igraph_1.2.7
[55] compiler_4.1.2
```