$\mathbf{secr}\ 4.6$ - spatially explicit capture—recapture in R

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This document provides an overview of **secr** 4.6, an R package for spatially explicit capture–recapture analysis (SECR). It includes some background on SECR, an outline of the package, and a more detailed description of how models are implemented. See secr-tutorial.pdf for an introductory tutorial. For details of how to use **secr** see the help pages and vignettes.

NOTE: **secr** was extensively re-written between versions 3.2 and 4.0, but the interface remained unchanged. For many datasets version 4 is significantly faster. Other changes are described in secr-version4.pdf.

Add-on packages extend the capability of **secr** and are documented separately. **secrlinear** enables the estimation of linear density (e.g., animals per km) for populations in linear habitats such as stream networks (secrlinear-vignette.pdf). **ipsecr** fits models by simulation and inverse prediction, rather than maximum likelihood; this is a rigorous way to analyse data from single-catch traps (ipsecr-vignette.pdf). **secrdesign** enables the assessment of alternative study designs by Monte Carlo simulation; scenarios may differ in detector (trap) layout, sampling intensity, and other characteristics (secrdesign-vignette.pdf).

Spatial open-population capture—recapture models are implemented in the R package **openCR** (Efford and Schofield 2020). Other open-population packages due to Ben Augustine and Richard Glennie are available on GitHub (https://github.com/benaug/OpenPopSCR; https://github.com/r-glennie/openpopscr).

Introduction to SECR

Spatially explicit capture—recapture (SECR) is a set of methods for modelling animal capture—recapture data collected with an array of 'detectors'. The methods are used primarily to estimate population density, but they also have advantages over non-spatial methods when the goal is to estimate population size (Efford and Fewster 2013). SECR methods overcome edge effects that are problematic in conventional capture—recapture estimation of animal populations (Otis et al. 1978). Detectors may be live-capture traps, with animals uniquely tagged, sticky traps or snags that passively sample hair, from which individuals are distinguished by their microsatellite DNA, or cameras that take photographs from which individuals are recognized by their natural marks. The concept of a detector extends to areas (polygons) or transects that are searched for animals or their sign.

The primary data for SECR are (i) the locations of the detectors, and (ii) detections of known individuals on one or more sampling occasions (i.e. their detection histories). The generic terms 'detector' and 'detections' cover several possibilities (see 'Detector types' below); we use them interchangeably with the more specific and familiar terms 'traps' and 'captures'. Table 1 gives a concrete example of trapping data (the structure differs for detectors that are not traps).

Table 1. Some spatially explicit detection data. Each entry (e.g., A9) records the detector at which a known animal (ID) was observed at each sample time (occasion). ': indicates no detection. Each detector has known x-y coordinates. Formats for data input are described in secr-datainput.pdf.

		Occa	sion		
ID	1	2	3	4	5
1	A9		•		
2	A12	A12	•		
3			C6	B5	
4			G3		F3
etc					

In SECR, a spatial model of the population and a spatial model of the detection process are fitted to the spatial detection histories. The resulting estimates of population density are unbiased by edge effects and incomplete detection (other sources of bias may remain). Inverse prediction (IP SECR) and maximum likelihood (ML SECR) are alternative methods for fitting the spatial detection model (Efford 2004, Borchers and Efford 2008). Of these, ML SECR is the more flexible, with a caveat for data from single-catch traps. Data augmentation and Markov chain Monte Carlo (MCMC) methods have also been used for SECR (Royle

and Young 2008, Royle et al. 2009, Singh et al. 2010, Royle and Gardner 2011, Royle et al. 2014), but this approach is much slower than ML SECR; it is not considered here.

State and observation models

Like other statistical methods for estimating animal abundance (Borchers et al. 2002), SECR combines a state model and an observation model. The state model describes the distribution of animal home ranges in the landscape, and the observation model (a spatial detection model) relates the probability of detecting an individual at a particular detector to the distance of the detector from a central point in each animal's home range. The distances are not observed directly (usually we don't know the range centres), so conventional distance sampling methods do not apply.

Distribution of home-range centres

The distribution of range centres in the population (Borchers and Efford 2008) will usually be treated as a homogeneous Poisson point process (Fig. 1a). Density (= intensity) is the sole parameter of a homogeneous Poisson process. An inhomogeneous Poisson distribution may also be fitted; this provides a means to evaluate the effects of habitat variables on density.

Detection functions

A detection model describes the decline in detection probability with distance (d) from the home-range centre (Fig. 1b). The probability g(d) is for the 'ideal' case of just one animal and one detector; the actual probability may differ (see discussion of 'traps' under Detector Types).

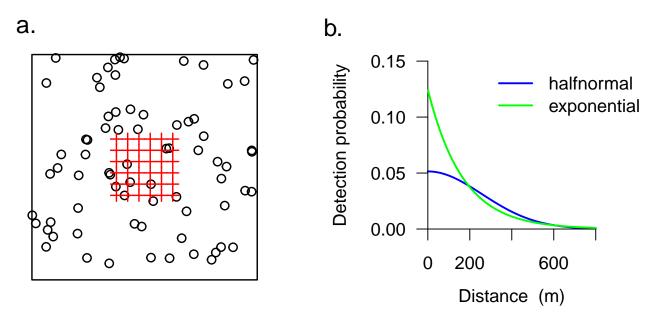


Fig. 1. (a) Hypothetical Poisson distribution of range centres near an array of detectors. Each dot represents one individual. SECR estimates the density of this distribution. (b) Alternative detection functions. The halfnormal is defined by $g(d) = g_0 \exp\left(\frac{-d^2}{2\sigma^2}\right)$ and the exponential by $g(d) = g_0 \exp\left(-\frac{d}{\sigma}\right)$. See ?detectfn for more (also the list in Appendix 1).

Detector types

The properties of detectors are an important part of the SECR observation model (Table 2). Inside **secr**, data are tagged with a detector type to ensure they are printed, plotted and analysed appropriately.

Some common detectors (camera 'traps' and hair snags for DNA) do not capture animals, but merely record that an animal has visited a site. These 'proximity' detectors can be considered to act independently of each other. With proximity detectors, each animal \times occasion 'cell' of a detection history potentially contains several positive records. In the simplest case each cell contains a binary vector coding presence or absence at each detector (for such binary proximity detectors each observation has a Bernoulli distribution). A 'count' detector is a generalised proximity detector in which the data are vectors of counts, one per detector. Models for 'count' data will specify a distribution for the counts via the 'binomN' argument of secr.fit (binomN = 0 indicates Poisson; binomN > 1 indicates binomial with size = binomN; binomN = 1 indicates binomial with size given by the 'usage' attribute for the detector and occasion).

Detectors that are true traps do not act independently because capture of an animal in one trap prevents it being caught in another trap until it is released. Traps expose animals to competing risks of capture. The per-trap probability of capture may be adjusted for the competing risk from other traps by using an additive hazard model (Borchers and Efford 2008). However, if the detectors are traps that catch only one animal at a time then there is a further level of competition – between animals for traps. Multi-catch and single-catch traps therefore represent distinct detector types. No general adjustment has been found for the per-trap probability of capture in the single-catch case (it's an open research question), and there is strictly no known maximum likelihood estimator. Estimates of average density using the multi-catch likelihood for single-catch data appear only slightly biased (Efford, Borchers and Byrom 2009), and this substitution is made automatically in **secr**, with a warning. However, the substitution is imperfect when density varies (Distiller and Borchers 2015). Simulation and inverse prediction in **ipsecr** is an alternative and more robust method for single-catch data.

Polygon and transect detectors are for binary or count detection data (e.g., number of detections per animal per polygon per occasion) supplemented with the x-y coordinates of each detection. When a study uses multiple search areas or multiple transects, detections may be either independent or dependent (e.g., maximum one per animal per polygon per occasion) as with traps. The dependent or 'exclusive' type is indicated by the suffix 'X'; in this case the counts are necessarily binary. Using the 'polygonX' or 'transectX' detector type ensures that a competing-risk model is fitted.

Acoustic 'signal strength' detectors produce a binary detection vector supplemented by measurements of signal strength, as from an array of microphones.

There is limited support in **secr** for the analysis of locational data from telemetry ('telemetry' detector type). Telemetry data are used to augment capture—recapture data (see addTelemetry and secr-telemetry.pdf).

Table 2. Detector types in secr

Detector	Description
single	traps that catch one animal at a time
multi	traps that may catch more than one animal at a time
proximity	records presence at a point without restricting movement
count	proximity detector allowing >1 detection per animal per time
capped	proximity detector with maximum one animal at a time
polygon	counts from searching one or more areas
transect	counts from searching one or more transects
polygonX	binary data from mutually exclusive areas
transectX	binary data from mutually exclusive transects
signal	detections and signal strengths at multiple microphones
telemetry	locations from radiotelemetry

Origins and outline of the package secr

The program DENSITY (Efford et al. 2004, Efford 2012) provides a graphical interface to SECR methods that has been accepted by many biologists. However, DENSITY has significant drawbacks: it requires the Windows operating system, its algorithms are not always transparent or well-documented, it fits only homogeneous Poisson models, and it omits recent advances in SECR.

The R package **secr** was written to address these weaknesses and allow for further development. It implements almost all the methods described by Borchers and Efford (2008), Efford et al. (2009), Efford (2011), Efford and Fewster (2013), Efford et al. (2013) and Efford and Mowat (2014). **secr** 4.6 uses external C++ code via package **Rcpp** for computationally intensive operations (Eddelbuettel and Francois 2011); Multi-threading on multiple CPUs with **RcppParallel** (Allaire et al. 2021) gives major speed gains. Appendix 1 compares the features of DENSITY and **secr**. The most important functions of **secr** are listed in Appendix 2.

How secr works

secr defines a set of R classes¹ and methods for data from detector arrays and models fitted to those data.

Table 3. Essential classes in secr.

Class	Data
traps capthist mask secr	locations of detectors; detector type ('proximity', 'multi', etc.) spatial detection histories, including a 'traps' object raster map of habitat near the detectors fitted SECR model

To perform an SECR analysis you explicitly or implicitly construct each of these objects in turn. Fig. 2 indicates the relationships among the classes.

¹Technically, these are S3 classes. A 'class' in R specifies a particular type of data object and the functions (methods) by which it is manipulated (computed, printed, plotted etc). See the R documentation for further explanation.

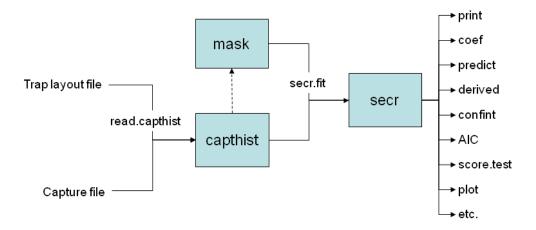


Fig. 2. Essentials of the secr package.

- Each object class (shaded box) comes with methods to display and manipulate the data it contains (e.g. print, summary, plot, rbind, subset)².
- The function read.capthist forms a 'traps' object from the detector layout data and saves it as an attribute, along with capture data read from another file, in a 'capthist' object.
- By default, a habitat mask is generated automatically by secr.fit using a specified buffer around the detectors (traps). The function make.mask gives greater control over this step.
- Any of the objects input to secr.fit (traps, capthist, mask) may include a dataframe of covariates saved as an attribute. Covariate names may be used in model formulae; the covariates method is used to extract or replace covariates. Use addCovariates for covariates from spatial data sources (e.g., shapefile or 'sf' object)
- Fitted secr models may be manipulated with the methods shown on the right and others listed in Appendix 3.

Input

Data input is covered in the separate document secr-datainput.pdf. One option is to use text files in the formats used by DENSITY; these accommodate most types of data. Two files are required, one of detector (trap) locations and one of the detections (captures) themselves; the function read.capthist reads both files and constructs a capthist object. It is also possible to construct the capthist object in two stages, first making a traps object (with read.traps) and a captures dataframe, and then combining these with make.capthist. This more general route may be needed for unusual datasets.

Output

The output from the function secr.fit is an object of class secr. This is an R list with many components. Assigning the output to a named object saves both the fit and the data for further manipulation. Typing the name at the R prompt invokes print.secr which formats the key results. These include the dataframe of estimates from the predict method for secr objects. Functions are provided for further computations on secr objects (e.g., AIC model selection, model averaging, profile-likelihood confidence intervals, and likelihood-ratio tests). Many of these are listed in Appendix 3.

One system of units is used throughout **secr**. Distances are in metres and areas are in hectares (ha). The unit of density for 2-dimensional habitat is animals per hectare. 1 ha = $10000 \text{ m}^2 = 0.01 \text{ km}^2$. To convert density to animals per km², multiply by 100. Density in linear habitats (see package **secrlinear**) is expressed in animals per km.

²Text in this font refers to R objects that are documented in online help for the **secr** package, or in base R.

Documentation

The primary documentation for **secr** is in the help pages that accompany the package. Help for a function is obtained in the usual way by typing a question mark at the R prompt, followed by the function name. Note the 'Index' link at the bottom of each help page – you will probably need to scroll down to find it. The index may also be accessed with help(package = secr).

The consolidated help pages are in the file secr-manual.pdf. Searching this text is a powerful way to locate a function for a particular task.

Other documentation, in the form of pdf vignettes built with **knitr**, will be added from time to time. The 'User guides...' link in the package help index lists available files. The vignettes in Table 4 may be found on the Density website.

Table 4. Vignettes for secr 4.6.

Vignette	Topic
secr-overview.pdf	introduction (this document)
secr-datainput.pdf	data formats and input functions
secr-version4.pdf	what's new in secr 4.x
secr-tutorial.pdf	tutorial using Burnham and Cushwa snowshoe hare data
secr-habitatmasks.pdf	habitat masks, buffer width and related topics
secr-models.pdf	general description of models in secr
${\it secr-trouble shooting.pdf}$	problems with secr.fit, including speed issues
secr-densitysurfaces.pdf	modelling density surfaces
secr-finitemixtures.pdf	mixture models for individual heterogeneity
secr-markresight.pdf	mark-resight models
secr-multisession.pdf	data from multiple independent sessions
secr-noneuclidean.pdf	non-Euclidean distance models
secr-parameterisations.pdf	alternative parameterisations of detection
secr-polygondetectors.pdf	using polygon and transect detector types
secr-sound.pdf	analysing data from microphone arrays
secr-spatialdata.pdf	tips on external spatial data and functions
secr-telemetry.pdf	analysing combined telemetry and capture–recapture data
secr-varyingeffort.pdf	variable effort (usage) in SECR models

The web page https://www.otago.ac.nz/density/ should be checked for news of bug fixes and new releases. New versions will be posted on CRAN, but there may be a delay of a few days. Help may be sought at phidot; see also the FAQ there for DENSITY and **secr**. Another forum intended for both software issues and wider discussion is secrgroup. For information on changes in each version, type at the R prompt:

```
news (package = "secr")
```

Defining models with the 'model' argument of secr.fit

By default, the parameters of SECR models are assumed to be constant. We specify more interesting, and often better-fitting, models with the 'model' argument of secr.fit. Here 'models' relates to variation in the parameters that may be explained by known factors and covariates. The explanation in secr-models.pdf may help. If you just want to know how to use models, read on.

Models are defined symbolically in **secr** using R formula notation. A separate linear predictor is used for each core parameter. Core parameters are 'real' parameters in the terminology of MARK, and **secr** uses that

term because it will be familiar to biologists.

Three real parameters are commonly modelled in **secr** 4.6; these are denoted 'D' (for density), 'g0' (or 'lambda0') and 'sigma'. Only the last two real parameters, which jointly define the model for detection probability as a function of location, can be estimated directly when the model is fitted by maximizing the conditional likelihood (CL = TRUE in **secr.fit**). D is then a derived parameter that is computed from an **secr** object with the function **derived** or one of its siblings (**derivedCluster** etc.).

Here is a simple example of the model argument in use:

```
secr.fit(captdata, model = g0~t)
```

The real parameter g0 is no longer constant, but takes a unique value on each sampling occasion (t).

Other 'real' parameters appear in particular contexts. 'z' is a shape parameter that is used only when the detection function has three parameters (annular halfnormal, cumulative gamma, hazard-rate etc. – see ?detectfn). Some detection functions primarily model 'exposure' or the cumulative hazard of detection, rather than the probability of detection; these use the real parameter 'lambda0' in place of 'g0' (see ?detectfn). 'lambda0' is also used with count detectors. A further 'real' parameter is the mixing proportion 'pmix', used in finite mixture models and hybrid mixture models (see ?hcov).

Sometimes it is illuminating and efficient to parameterise the detection function using a function of the primary 'real' parameters described above. This gives rise to the surrogate 'real' parameters a0 and sigmak; see the vignette secr-parameterisations.pdf for details and references.

Detection parameters and density parameters are modelled separately, as we now describe.

Detection parameters

Effects on parameters of detection probability are specified via R formulae. The variable names used in formulae are either names for standard effects (Table 5) or the names of user-supplied covariates. Effects 'b', 'B', 'bk', and 'Bk' refer to individuals whereas 'k' and 'K' refer only to sites. Groups ('g') are used only in models fitted by maximizing the full likelihood; for conditional likelihood models use a factor covariate to achieve the same effect. See also the later section on modelling sex differences.

Variable	Description	Notes
g	group	individual covariates listed in secr.fit argument 'groups'
t	time factor	one level for each occasion
T	time trend	linear trend over occasions on link scale
b	learned response	step change after first detection
В	transient response	depends on detection at preceding occasion (Markovian response)
bk	animal x site response	site-specific step change
Bk	animal x site response	site-specific transient response
k	site learned response	site effectiveness changes once any animal caught
K	site transient response	site effectiveness depends on preceding occasion
session	session factor	one level for each session
Session	session trend	linear trend on link scale
h2	2-class mixture	finite mixture model with 2 latent classes
ts	marking vs sighting	two levels (marking and sighting occasions)

Any name in a formula that is not a variable in Table 5 is assumed to refer to a user-supplied covariate. secr.fit looks for user-supplied covariates in data frames embedded in the 'capthist' argument, or supplied in the 'timecov' and 'sessioncov' arguments, or named with the 'timevaryingcov' attribute of a traps object, using the first match (Table 6).

Table 6. Types of user-provided covariate for in detection models. The names of columns in the respective dataframes, and names of components in the 'timevaryingcov' attribute, may be used in model formulae

Covariate type	Data source	Notes
Individual	covariates(capthist)	conditional likelihood only
Time Detector	timecov argument covariates(traps(capthist))	
Detector x Time	covariates(traps(capthist))	see ?timevaryingcov
Session	sessioncov argument	

The formula for any detection parameter (e.g., g0, lambda0 or sigma) may be constant (~ 1 , the default) or some combination of terms in standard R formula notation (see ?formula). For example, g0 \sim b + T specifies a model with a learned response and a linear time trend in g0; the effects are additive on the link scale. See Table 7 for other examples.

Table 7. Some examples of the 'model' argument in secr.fit

Formula	Effect
$g0 \sim 1$	g0 is constant across animals, occasions and detectors
$g0 \sim b$	learned response affects g0
$list(g0 \sim b, sigma \sim b)$	learned response affects both g0 and sigma
$g0 \sim h2$	2-class finite mixture for heterogeneity in g0
$g0 \sim b + T$	learned response in g0 combined with trend over occasions
$sigma \sim g$	detection scale sigma differs between groups
$sigma \sim g^*T$	group-specific trend in sigma
$D \sim cover$	density varies with 'cover', a variable in covariates(mask)
$list(D \sim g, g0 \sim g)$	both density and g0 differ between groups
$D \sim session$	session-specific density

For other effects, the design matrix for detection parameters may also be provided manually in the argument dframe of secr.fit. This feature is untested.

Inhomogeneous density models

The SECR log likelihood is evaluated by summing values at points on a 'habitat mask' (the 'mask' argument of secr.fit). Each point in a habitat mask represents a grid cell of potentially occupied habitat (their combined area may be almost any shape). The full design matrix for density (D) has one row for each point in the mask. As for the detection submodels, the design matrix has one column for the intercept (constant) term and one for each predictor.

Predictors may be based on Cartesian coordinates (e.g. 'x' for an east-west trend), a continuous habitat variable (e.g. vegetation cover) or a categorical (factor) habitat variable. Predictors must be known for all points in the mask (non-habitat excluded). The variables 'x' and 'y' are the coordinates of the habitat mask and are automatic, as are 'x2', 'y2', and 'xy'. Other spatial covariates should be named columns in the 'covariates' attribute of the habitat mask.

Regression splines are particularly effective for modelling spatial trend. For these and general guidance on fitting and displaying density surfaces, see the vignette secr-density surfaces.pdf.

Model fitting and estimation

Models are fitted in secr.fit by numerically maximizing the likelihood. The likelihood involves integration over the unknown locations of the animals' range centres. This is achieved in practice by summation over points in the habitat mask, which has some implications for the user. Computation may be slow, especially if there are many points in the mask, and estimates may be sensitive to the particular choice of mask (either explicitly in make.mask or implicitly via the 'buffer' argument).

The default maximization algorithm is Newton-Raphson in the function stats::nlm. By default, all reported variances, covariances, standard errors and confidence limits are asymptotic and based on a numerical estimate of the information matrix. The Newton-Raphson algorithm is fast, but it sometimes fails to compute the information matrix correctly, causing some standard errors to be set to NA; see the 'method' argument of secr.fit for alternatives. Use confint.secr for profile likelihood intervals and sim.secr for parametric bootstrap intervals (both are slow).

Habitat masks

We have already introduced the idea of a habitat mask. The SECR likelihood is evaluated by summing values at points on a mask; each point represents a grid cell of potentially occupied habitat. Masks may be constructed by placing a buffer of arbitrary width around the detectors, possibly excluding known non-habitat. How wide should the buffer be? The general answer is 'Wide enough not to cause bias in estimated densities'. This depends on the scale of movement of the animal, and on the chosen detection function. For specifics, see the separate vignette on habitat masks secr-habitatmasks.pdf and the help for 'mask' and the various mask-related functions (make.mask, mask.check, suggest.buffer, and esa.plot). Heavy-tailed detection functions such as the hazard-rate and lognormal can be problematic because they require an unreasonably large buffer for stable density estimates.

Miscellaneous topics

Modelling sex differences

There are many ways to model sex differences in **secr**. Here we sketch some possibilities, in order of usefulness (your mileage may vary).

- 1. Fit a hybrid mixture model as described in the online help (?hcov). This accommodates occasional missing values and estimates the sex ratio (pmix).
- 2. Use conditional likelihood (CL = TRUE) and include a categorical (factor) covariate in model formulae (e.g., $g0 \sim sex$). To get sex-specific densities then specify groups = "sex" in derived.
- 3. Use full likelihood (CL = FALSE) and separate data for the two sexes as different sessions (most easily, by coding 'female' or 'male' in the first column of the capture file read with read.capthist). Then include a group term 'session' in relevant model formulae (e.g., g0 ~ session).
- 4. Use full likelihood (CL = FALSE), define groups = "sex" or similar, and include a group term 'g' in relevant formulae (e.g., $g0 \sim g$).

'CL' and 'groups' are arguments of secr.fit. Possibilities 1–4 should not be mixed for comparing AIC. Sex differences in home-range size (and hence sigma) may be mitigated by compensatory variation in g0 or lambda0 (Efford and Mowat 2014).

Varying effort

The probability of observing an individual at a particular detector may depend directly on a known quantity such as how long the detector was exposed on a particular occasion. In the extreme, a detector may not have been operated. The terms 'effort' and 'usage' are used here interchangeably for variation in the duration

of exposure and similar known effects. Usage is an attribute of the detectors in a traps object (a traps x occasions matrix); it may be entered with the detector coordinates in a trap layout file or added later (see ?usage). Models fitted to data including a usage attribute will adjust automatically for varying usage across detectors and occasions. Usage may take any non-negative value. This simplifies the modelling of data aggregated over varying numbers of occasions or nearby sites.

See the separate document secr-varyingeffort.pdf and Efford et al. (2013) for more.

Mark-resight

Mark—resight data include sampling occasions on which previously marked animals were recorded, but new animals were not distinguished from each other. secr 4.6 provides a suite of spatial models for these data, as documented in secr-markresight.pdf. Two general classes of spatial mark—resight model are included: those in which the marking process is modelled (we call these spatial capture—mark—resight models), and those in which the process is not modelled and pre-marked animals are assumed to follow some distribution (e.g., uniform across a known area) (sighting-only or mark—resight models). Mark—resight models in secr 4.6 discard some spatial information in the unmarked sightings—information that is used in the models of Chandler and Royle (2013) and Sollmann et al. (2013). This results in some (probably small) loss of precision, and requires an adjustment for overdispersion to ensure confidence intervals have good coverage properties. The vignette secr-markresight.pdf should be consulted.

Detector clusters

For surveying large areas it is efficient to use groups of detectors: within a group the detectors are close enough that animals may be re-detected at multiple points, while groups of detectors may be distributed across a region according to a probability design to sample possible spatial variation in density. **secr** allows for detector groups with the 'cluster' data structure. This is an attribute of a traps object that records which detectors belong to which cluster³.

Functions are provided to generate detector arrays with a clustered structure (trap.builder, make.systematic), to extract or replace the cluster attribute (clusterID), to compute the geometric centres and numbers of detections per cluster (cluster.centres, cluster.counts), etc.

A lacework design (Efford in prep.) is an alternative to a clustered design that is suitable when the region is intermediate size. Lacework designs may be constructed with make.lacework.

Data from a large, clustered design may often be analysed more quickly if the 'capthist' object is first collapsed into one using the geometry of a single cluster (the object retains a memory of the number of individuals from each original cluster in the attribute 'n.mash'). Use the function mash for this. Functions derived, derivedMash and the method predict.secr use 'n.mash' to adjust their output density, SE, and confidence limits.

Parallel processing

On processors with multiple cores it is possible to speed up computation by using cores in parallel. In **secr** 4.6 this happens automatically in **secr.fit** and a few other functions using the multi-threading paradigm of **RcppParallel** (Allaire et al. 2021). The number of threads may be set directly with the function **setNumThreads**, or via the 'ncores' argument of several functions.

Earlier versions of **secr** relied on parallel processing with the **parallel** package (invoked when the argument ncores was set greater than 1). The benefits of that form of parallel processing were variable (considerable with simulations in **sim.secr**, but otherwise unimpressive).

The functions par.secr.fit, par.region.N and par.derived allowed models to be fitted or analysed in parallel, one per core. The greater speed of secr.fit in secr 4.6 makes par.secr.fit redundant. All three

³Clusters are assumed to share the same geometry (number of detectors, within-cluster spacing etc.).

functions now appear to run faster with ncores=1 than with ncores>1. They are retained because it is sometimes useful to process several models at once.

Regression splines

The standard models for 'real' parameters in **secr** are linear on the link scale, much like a generalised linear model. Semi-parametric 'regression spline' smooths provide more flexibility. These are implemented in **secr** using a method suggested by Borchers and Kidney (2014): Simon Wood's R package **mgcv** is used to parse s() and te() terms in model formulae and construct basis functions that are used like linear covariates within **secr**. Any 'real' parameter may be modelled with regression splines (D, lambda0, sigma, noneuc etc.). For details see the help page (?smooths) and the documentation for **mgcv**.

Non-Euclidean distances

'Distance' in SECR models usually, and by default, means the Euclidean distance $d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$. The observation model can be customised by replacing the Euclidean distance with one that 'warps' space in some ecologically meaningful way. There are innumerable ways to do this. Royle et al. (2013) envisioned an 'ecological distance' that is a function of landscape covariates. Redefining distance is a way to model spatial variation in the size of home ranges, and hence the spatial scale of movement σ ; Efford et al. (2016) use this to model inverse covariation between density and home range size. Distances measured along a linear habitat network such as a river system are also non-Euclidean (see package **secrlinear**).

secr provides general tools for specifying and modelling non-Euclidean distance, via the secr.fit details component 'userdist'. This may be a user-specified function or a pre-computed matrix. See secr-noneuclidean.pdf for a full explanation and examples.

References

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Appendix 1. Software feature comparisons

- full implementation
- $\circ\,$ incomplete or inferior implementation.

Feature	DENSITY 5.0	secr 4.6
General		
Graphical interface	•	0
Inverse prediction (IP SECR)	•	•
Maximum likelihood estimation (ML SECR)	•	•
Non-spatial closed-population estimators	•	•
Simulation of spatial sampling	•	•
Build detector arrays	•	•
Control of random number generator	0	•
Closure tests	0	•
Import or export DENSITY text files	•	•
Convert BUGS data		0
GIS polygons as habitat mask	•	•
Clustered detector layouts		•
Mash data from clustered layouts		•
Upload coordinates to GPS (uses GPSBabel)		•
Multi-threaded C++ for fast model fitting		•
ML secr		
Density models (inhomogeneous 2-D Poisson)		•
Regional population size (region.N)		•
Varying effort (detector usage)	0	•
Fixed parameters	0	•
Parametric bootstrap	0	•
Between-session models	•	•
Profile likelihood confidence intervals	•	•
Mixture models for individual heterogeneity	•	•
Confidence ellipses	•	•
Formula-based model notation		•
Plot density models		•
Groups (e.g. males & females)		•
Score tests for model selection		•
Model averaging		•
Plot likelihood surface		•
Empirical variance from replicate units		•
Mask diagnostics	0	•
Suggested buffer width Contours of detection probability	_	•
Compute pdf for individual's range centre	•	•
Time-varying detector covariates	•	•
Hybrid mixture models (hcov)		•
Compensation (a0 parameterization)		•
Density-dependent sigma (sigmak parameterization)		•
Variance-only mode (method = 'none')		•
Combined telemetry-detection models		•
Regression splines		•
Non-Euclidean distance		•
Mark-resight		•
Detector types		
V I ***		

Feature	DENSITY 5.0	secr 4.6
Single-catch trap ^a	0	0
Multi-catch trap	•	•
Proximity	•	•
Signal strength (acoustic)		•
Count		•
Capped		0
Polygon		•
Transect		•
Polygon (exclusive)		•
Transect (exclusive)		•
Telemetry		•
Detection functions		
Halfnormal	•	•
Hazard rate ^b	•	•
Exponential	•	•
Compound halfnormal		•
Uniform ^a	0	0
w-exponential		•
Annular halfnormal		•
Binary signal strength		•
Signal strength		•
Signal strength spherical		•
Cumulative lognormal ^b		•
Cumulative gamma		•
Hazard halfnormal		•
Hazard hazard rate ^b		•
Hazard exponential		•
Hazard annular halfnormal		•
Hazard cumulative gamma		•
Hazard variable power		•

a. Not fitted by ML secr

b. Not recommended because of heavy tail

Appendix 2. Core functions of secr

These are the core functions of $\sec 4.6$ – the ones that you are most likely to use. S3 methods are marked with an asterisk.

Function	Purpose
addCovariates	add spatial covariates to traps or mask
AIC*	model selection, model weights
covariates	extract or replace covariates of traps, capthist or mask
$\mathtt{derived}^*$	compute density from conditional likelihood models
make.mask	construct habitat mask (= mesh)
plot*	plot capthist, traps or mask
read.capthist	input captures and trap layout from Density format, one call
predict*	compute 'real' parameters for arbitrary levels of predictor variables
predictDsurface	evaluate density surface at each point of a mask
region.N*	compute expected and realised population size in specified region
secr.fit	maximum likelihood fit; result is a fitted 'secr' object
$\mathtt{summary}^*$	summarise capthist, traps or mask
traps	extract or replace traps object in capthist

Appendix 3. Classified index to secr functions

Here is an index of **secr** functions classified by use (some minor functions are omitted). S3 methods are marked with an asterisk.

- $\bullet \;$ Manipulate core objects
- Attributes of traps object
- Attributes of capthist object
- Data for each detection
- Operate on fitted model(s)
- Mask diagnostics
- Specialised graphics
- Convert or export data
- Miscellaneous

Function	Purpose
Manipulate data objects	
addCovariates	add spatial covariates to 'traps' or 'mask'
as.mask	coerce 'traps' object to 'mask' for specialised plotting
deleteMaskPoints	edit 'mask'
discretize	rasterize area-search capthist data
head*	first rows of 'capthist', 'traps' or 'mask'
join	combine sessions of multi-session 'capthist' object
make.grid	construct detector array
make.capthist	form 'capthist' from 'traps' and detection data
make.mask	construct habitat mask (mesh)
make.systematic	construct clustered random systematic design
make.lacework	construct lacework random systematic design
MS.capthist	combine 'capthist' objects into one multi-session 'capthist'
plot*	plot 'capthist', 'traps' or 'mask'
plotMaskEdge	draw line around mask cells
randomHabitat	generates habitat mask with random landscape
rbind*	append 'capthist', 'traps', 'popn' or 'mask' objects
read.capthist	input captures and trap layout from Density format, one call
read.traps	input detector locations from text file
reduce*	aggregate detectors or occasions; change detector type
sim.capthist	simulate capture histories
sightingPlot	bubble plot of sightings in capthist object
snip	split transect(s) into equal sections
split*	split a single-session capthist or mask by various criteria
subset*	filter 'capthist', 'traps' or 'mask'
summary*	summarise 'capthist', 'traps' or 'mask'
tail*	last rows of 'capthist', 'traps' or 'mask'
trap.builder	construct various complex designs
verify*	check 'capthist', 'traps' or 'mask' for internal consistency
Attributes of traps object	
clusterID	cluster identifier
clustertrap	detector number within cluster
covariates*	detector-level covariates
detector*	detector type ('multi', 'proximity' etc.)
markocc	vector distinguishing marking and sighting occasions
polyID*	polygon or transect identifier
timevaryingcov	name time-varying covariate(s)
usage*	occasion- and detector-specific effort

Function Purpose

Attributes of capthist object

addSightings add sighting data to a 'proximity', 'count' or 'polygon' object

addTelemetry add telemetry data to a 'proximity' or 'count' object covariates* individual-level covariates, including grouping factors

session*session identifier(s)signalmatrixsound x microphone tabletelemetryxycoordinates of telemetry fixes

Tm counts of marked animals that were not identified

traps* embedded traps object(s)
Tu counts of unmarked animals

Data for each detection

alive TRUE/FALSE animalID individual ID clusterID cluster identifier

clustertrap detector number within cluster

noise (signal detectors)

occasion occasion

signal strength (signal detectors)

signalframe whole signal | noise dataframe (rows = detections)

trap detector

xy detection coordinates (polygon and transect detectors)

Fit SECR model(s)

par.secr.fit parallel secr.fit() (several models, using multiple cores)
secr.fit maximum likelihood fit; result is a fitted secr object

Operate on fitted model(s)

adjustVarD apply c-hat to density SE and confidence intervals

AIC* model selection, model weights chat.nk overdispersion of activity centres

coef* 'beta' parameters

collate tabulate estimates from several models confint* profile likelihood confidence intervals

CVa, CVa0 CV of individual detection from fitted mixture model

derived* density from conditional likelihood models

deviance* model deviance

df.residual* degrees of freedom for deviance

derivednj variance from replicated sampling units
derivedCluster variance from replicated sampling units
derivedExternal variance from replicated sampling units
ellipse.secr confidence ellipses for estimated parameters
fxi.secr probability density of home-range centre
LLsurface* compute likelihood surface and plot contours

logLik* log-likelihood of fitted model
LR.test likelihood-ratio test of two models

modelAverage* combine estimates using AIC or AICc weights

par.derived parallel derived()
par.region.N parallel region.N()

plot* plot detection functions with confidence bands

predict* 'real' parameters for arbitrary levels of predictor variables

region.N* expected and realised population size in specified region

RSE extract precision (relative SE) of 'real' parameter estimates

score.test model selection with score statistic using observed information

Function	Purpose
-	
secr.test	Monte Carlo goodness-of-fit tests
simulate*	generate realisations of fitted model
sim.secr	parametric bootstrap
vcov*	variance-covariance matrix of 'beta' or 'real' parameters
Mask diagnostics	
esa.plot	cumulative plot esa or \hat{D} vs buffer width
mask.check	likelihood or estimates vs. buffer width and spacing
suggest.buffer	find buffer width to keep bias within bounds
Specialised graphics	concerns and conver houndary string
buffer.contour	concave and convex boundary strips
fx.total	summed pdfs of home-range centre pdfs (use with plot.Dsurface)
fxi.contour	contour plot of detection probability
pdot.contour	contour plot of detection probability
Strip.legend	add colour legend to existing plot
Convert or export data	convert 'capthist' to dataframe for RMark
RMarkInput write.capthist	export 'capthist' as text files for DENSITY
write.DA	convert 'capthist' for analysis in WinBUGS
writeGPS	upload coordinates to GPS using GPSBabel
Miscellaneous	upload coordinates to G1 5 using G1 5Daber
ARL	asymptotic range length
autoini	generate starting values of D, g0 and sigma for secr.fit
centroids	centroid of each animal's detections
clone	replicate points to emulate overdispersion
closure.test	closure tests of Otis et al. (1978) and Stanley Burnham (1999)
closedN	closed population size by various conventional estimators
counts	summary data from 'capthist' object
CV	coefficient of variation
dbar	mean distance between capture locations
distancetotrap	from an arbitrary set of points
edist	Euclidean distance
Enk	expected individuals per detector
gridCells	grid cells around points (e.g. traps object)
kfn	overlap index for halfnormal home range
MMDM	mean maximum distance moved
moves	distances between capture locations
nearesttrap	from an arbitrary set of points
nedist	Non-Euclidean distance
ORL	observed range length
pdot	location-specific net probability of detection
PG	proportion of telemetry fixes in given polygons
pmixProfileLL	profile likelihood as function of mixing proportion
RPSV	'root pooled spatial variance', a simple measure of home-range size
setNumThreads	sets environment variable RCPP_PARALLEL_NUM_THREADS
trapsPerAnimal	frequency distribution of detectors per animal

Appendix 4. Datasets

See each help page for details e.g., ?deermouse. Code for model fitting is in Appendix 2 of secr-version4.pdf.

deermouse

Peromyscus maniculatus Live-trapping data of V. H. Reid published as a CAPTURE example by Otis et al. (1978) Wildlife Monographs 62

hornedlizard

Repeated searches of a quadrat in Arizona for flat-tailed horned lizards *Phrynosoma mcallii* (Royle & Young *Ecology* **89**, 2281–2289)

housemouse

 $Mus\ musculus$ live-trapping data of H. N. Coulombe published as a CAPTURE example by Otis et al. (1978) Wildlife Monographs ${\bf 62}$

ovenbird

Multi-year mist-netting study of ovenbirds Seiurus aurocapilla at a site in Maryland, USA.

ovensong

Acoustic detections of ovenbirds (Dawson & Efford Journal of Applied Ecology 46, 1201–1209)

OVpossum

Brushtail possum *Trichosurus vulpecula* live trapping in the Orongorongo Valley, Wellington, New Zealand 1996–1997 (Efford and Cowan In: *The Biology of Australian Possums and Gliders* Goldingay and Jackson eds. Pp. 471–483).

possum

Brushtail possum *Trichosurus vulpecula* live trapping at Waitarere, North Island, New Zealand April 2002 (Efford et al. 2005 Wildlife Society Bulletin **33**, 731–738)

secrdemo

Simulated data 'captdata', and some fitted models

skink

Multi-session lizard (*Oligosoma infrapunctatum* and *O. lineoocellatum*) pitfall trapping data from Lake Station, Upper Buller Valley, South Island, New Zealand (M. G. Efford, B. W. Thomas and N. J. Spencer unpublished).

stoatDNA

Stoat *Mustela erminea* hair tube DNA data from Matakitaki Valley, South Island, New Zealand (Efford, Borchers and Byrom 2009).