secrdesign - sampling design for spatially explicit capture—recapture

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2 May, 2014

The R package **secrdesign** is a set of tools to assist the design of studies using spatially explicit capture–recapture (SECR). It provides convenient wrappers for simulation and model fitting functions in package **secr** to emulate many features of the 'Simulator' module of Density 5.0 (Efford 2012). Other tools may be added in future.

This document is a technical guide to using the package. It assumes an understanding of estimator properties such as bias, precision, and confidence interval coverage, and the use of Monte Carlo simulation to predict the frequentist performance of different sampling designs. Using **secrdesign** can be daunting because it allows for many different combinations of data generation, model fitting and summary statistics. Several examples are given to indicate the range of possibilities.

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1 Introduction

When designing a study we assume you have in mind –

- (i) a population parameter you want to measure (probably density or population size),
- (ii) one or more design variables over which you have some control (number and spacing of detectors, number of sampling occasions etc.),
 - (iii) some pilot data, or parameter estimates from published studies, and
- (iv) a criterion by which to evaluate different designs. This is most likely the precision of the estimates, as this in turn determines your ability (power)

to recognise changes. Cost or effort may be an explicit criterion, or the designs may be constructed to allocate constant effort in different ways.

Once you have sorted these out, you can proceed to use Monte Carlo simulation in **secrdesign** to evaluate how alternative sampling scenarios perform with respect to your chosen criterion.

1.1 Overview

Fig. 1 shows the sequence of steps taken in **secrdesign** to conduct simulations and summarise the results. Each step is described in detail in a later section. Simulations are specified by 'scenarios' stored in a dataframe. The scenario dataframe will usually be constructed with make.scenarios(). You may construct it manually, but there is a rigid list of required columns (Section 3).

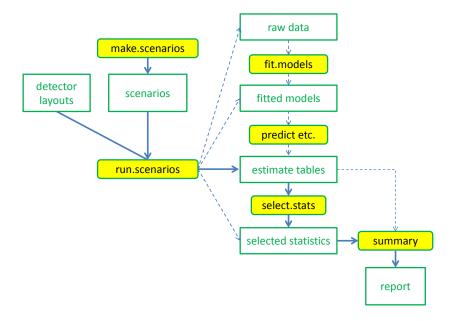


Figure 1: Core functions in **secrdesign** (yellow) and their main inputs and outputs. Output from the simulation function run.scenarios() may be saved as whole fitted models, predicted values (parameter estimates), or selected statistics. Each form of output requires different subsequent handling. The default path is shown by solid blue arrows.

Typically, you will (i) construct detector array(s), (ii) construct a dataframe of scenarios, (iii) use run.scenarios to generate data and fit SECR models,

(iv) select some statistics with select.stats, and (v) summarise and plot the results.

1.2 A simple example

As a simple introductory example, we construct a simple set of scenarios and perform some simulations. The trap layout is a default 6 x 6 grid of multi-catch traps at 20-m spacing. Density takes one of two levels (5/ha or 10/ha) and detection parameters sigma and g0 are fixed.

The output is an object of class c("estimatetables", "secrdesign", "list"). We use the summary method for estimatetables to view results, and here display only the summary output (omitting a header that describes the simulations).

> summary(sims1)\$OUTPUT

```
TD = 5
```

	n	mean	se
estimate	50	5.23767	0.24994
SE.estimate	50	1.84409	0.05958
lcl	50	2.70152	0.16476
ucl	50	10.28534	0.37589
RB	50	0.04753	0.04999
RSE	50	0.36890	0.00962
COV	50	0.92000	0.03876

 $^D = 10$

	n	mean	se
estimate	50	9.58795	0.36972
SE.estimate	50	2.45915	0.05721
lcl	50	5.86410	0.27453
ucl	50	15.75842	0.47775
RB	50	-0.04121	0.03697
RSE	50	0.26727	0.00668
COV	50	0.92000	0.03876

Later sections show how to customize the summary and plot results.

1.3 Terminology

We use 'relative standard error' (RSE) for the relative precision of an estimate. This is sometimes called the coefficient of variation (CV) of the estimate, but RSE is more appropriate. We use 'accuracy' in the sense of Williams et al. (2002 p.45) and other authors from the United States. Accuracy combines both systematic error (bias) and precision: one measure is the square root of the mean squared difference between the true value and the estimate (RMSE).

2 Detector layouts

Detector layouts are specified as **secr** 'traps' objects. These may be input from text files using **read.traps** or constructed according to a particular geometry and spacing with functions such as **make.grid**, **make.circle**, **make.systematic** or **trap.builder**. See the help files for these **secr** functions for further details. The detector type (multi-catch trap, proximity detector etc.) is stored as an attribute of each 'traps' object, which may also include detector-level covariates.

Multiple layouts are combined in a single list object; component names will be used to annotate later output.

This creates square grids with the default detector type 'multi' and default spacing 20 m. See ?secr::make.grid for other options.

3 The scenarios dataframe

The function make.scenarios() constructs a dataframe in which each row defines a simulation scenario. Its arguments are:

```
make.scenarios (trapsindex = 1, noccasions = 3, nrepeats = 1, D, g0,
    sigma, lambda0, detectfn = 0, recapfactor = 1, popindex = 1,
    detindex = 1, fitindex = 1, crosstraps = TRUE)
```

Each argument except for 'crosstraps' may be used to specify a range of values for a parameter. Four ('trapsindex', 'popindex', 'detindex', 'fitindex') are actually surrogate numerical indices; the index is used to select one component from a list of possibilities later provided as input to run.scenarios.

By default, a scenario is formed from each unique combination of the input values (trapsindex, noccasions, nrepeats, D, g0, sigma, lambda0, detectfn, recapfactor, popindex, and fitindex) using expand.grid. For example,

```
> make.scenarios(trapsindex = 1:3, noccasions = 4, D = 5, g0 = 0.2, sigma = c(20, 30))
```

	scenario	${\tt trapsindex}$	noccasions	${\tt nrepeats}$	D	g0	sigma	detectfn
1	1	1	4	1	5	0.2	20	0
2	2	2	4	1	5	0.2	20	0
3	3	3	4	1	5	0.2	20	0
4	4	1	4	1	5	0.2	30	0
5	5	2	4	1	5	0.2	30	0
6	6	3	4	1	5	0.2	30	0

recapfactor popindex detindex fitindex

1	1	1	1	1
2	1	1	1	1
3	1	1	1	1
4	1	1	1	1
5	1	1	1	1
6	1	1	1	1

In this case three different grids (possibly differing in number of traps) are trapped for the same number of occasions. A more interesting possibility is to vary the number of occasions inversely with the number of traps. However, if we naively set e.g., noccasions = c(8, 4, 2), this would generate all combinations of grid and number of occasions (18 different scenarios).

The alternative is to set crosstraps = FALSE. Then the vectors 'trapsindex', 'noccasions', and 'nrepeats' are locked together (if fewer values are provided in one of the vectors then it is re-used as required), and only the combination is crossed with the remaining parameter scenarios:

```
> make.scenarios(trapsindex = 1:3, noccasions = c(8, 4, 2), D = 5, g0 = 0.2, sigma = c(20, 30), crosstraps = FALSE)
```

	scenario	trapsindex	noccasions	nrepeats	D	g0	sigma	detectfn
1	1	1	8	1	5	0.2	20	0
2	2	2	4	1	5	0.2	20	0
3	3	3	2	1	5	0.2	20	0
4	4	1	8	1	5	0.2	30	0
5	5	2	4	1	5	0.2	30	0

2

1 5 0.2

30

3

6

	recapfactor	popindex	detindex	fitindex
1	1	1	1	1
2	1	1	1	1
3	1	1	1	1
4	1	1	1	1
5	1	1	1	1
6	1	1	1	1

All arguments except 'fitindex' control the generation of data. Note that 'g0' and 'lambda0' are alternatives: use the one appropriate to the detection function specified with 'detectfn' (see ?detectfn for codes). 'D' is omitted if an inhomogeneous Poisson distribution is specified using a mask covariate (see 6.3). D is in animals / hectare (1 ha = $0.01 \mathrm{km}^2$) and sigma is in metres, as in secr.

The nrepeats column refers to the number of notional independent replicates of the particular detector layout. Notional replicates are simulated by (invisibly) multiplying density (D) by this factor, and ultimately dividing it into the estimate. Think of 5 grids of automatic cameras so widely separated that no animal moves between the grids. As detections of different animals are ordinarily modelled as independent, the entire design is equivalent to 5 times the density of animals interacting with one grid. This breaks down, of course, if animals compete for traps (as with single-catch traps), and should not be used in that case except as a rough approximation.

Just as trapsindex serves as a placeholder for entire detector arrays, popindex, detindex and fitindex tell run.scenarios which set of arguments to select from pop.args and fit.args for sim.popn, sim.capthist and secr.fit respectively. These are for more advanced use: you may not need them.

4 Running simulations

The function run.scenarios generates multiple datasets and, if requested, fits an SECR model to each one. In this section we describe its main arguments, with additional detail on habitat masks and customizing the output.

4.1 Arguments of run.scenarios

```
run.scenarios (nrepl, scenarios, trapset, maskset, xsigma = 4,
    nx = 32, pop.args, det.args, fit = FALSE, fit.args, extractfn =
    NULL, ncores = 1, seed = 123)
```

nrepl determines the number of replicate simulations. Make this large enough that the summary statistics have enough precision to answer your question. This is usually a matter for experimentation, remembering that precision (SE) is proportional to the square root of nrepl.

scenarios is the dataframe constructed with make.scenarios() as described in the last section.

trapset is a single 'traps' object or a list of traps objects. as described in 'Detector layouts' above.

maskset is an optional set of habitat masks, usually one per detector layout. If not specified, then masks will be constructed 'on the fly' using secr::make.mask with a 'buffer' of width xsigma $\times \sigma$ and 'nx' cells in the x dimension.

pop.args provides additional control over sim.popn (see ?sim.popn for more). You may wish, for example, to set pop.args = list(Ndist = "fixed") to override the default of Poisson variation in the total number of simulated animals.

det.args provides additional control over sim.capthist (see ?sim.capthist for more). One use is to retain the simulated population as an attribute of the capthist object by setting det.args = list(savepopn = TRUE); another is to set the binomN argument for count detectors. The sim.capthist arguments traps, popn, detectpar, detectfn and noccasions are defined in the scenario or pop.args and cannot be overridden by setting det.args.

Use fit = FALSE to generate and summarise detection data without fitting SECR models. This lets you check that your scenarios result in reasonable numbers of detected individuals (n), detections (ndet), and movements (nmov), before launching a full-blown simulation.

fit.args lets you specify how SECR models will be fitted to the simulated data. Most default arguments of secr.fit may be overridden by including them in fit.args. For example, to specify a negative exponential detection function use fit.args = list(detectfn = "EX"). If you wish to compare nspec different model specifications then fit.args should be a list of lists, one per specification, with fitindex taking values in the range 1:nspec.

4.2 Customising run.scenarios()

The output from run.scenarios() is controlled by its argument extractfn. This is a short function that is applied either (i) to each simulated raw dataset (capthist object) (fit = FALSE), or (ii) to each fitted model (fit = TRUE).

The default (builtin) extractfn behaves appropriately for either data type:

```
extractfn <- function(x) {
   if (inherits(x, "capthist")) {</pre>
```

```
## assume single-session CH
   nmoves <- sum(unlist(sapply(moves(x), function(y) y>0)))
   ## detectors per animal
   dpa <- if (length(dim(x)) == 2)
        mean(apply(abs(x), 1, function(y) length(unique(y[y>0]))))
   else
        mean(apply(apply(abs(x), c(1,3), sum)>0, 1, sum))
        c(n=nrow(x), ndet=sum(abs(x)>0), nmov = nmoves, dpa = dpa)
}
else if (inherits(x, "secr"))
        predict(x)
else
   data.frame() ## 0 rows, 0 columns
}
```

When fit = FALSE, the default output from each replicate is a vector of 4 summary statistics:

- n number of different individuals
- ndet total number of detections ('captures' and 'recaptures')
- nmov total number of detections at a detector other than the one where an animal was last detected
- dpa detectors per animal (average number of detectors at which each animal was recorded)

When fit = TRUE, the default output from each replicate is the result of applying 'predict' to the fitted model, i.e. a dataframe of 'real' parameter estimates and their standard errors etc. (an empty dataframe is returned if model fitting fails). Nearly the same is achieved by setting extractfn = predict; for the 'beta' coefficients set extractfn = coef. For a conditional likelihood fit it may be appropriate to set extractfn = derived. To focus on population size in the masked region, set extractfn = region.N.

The user may also choose to save the entire dataset (fit = FALSE) or the entire fitted model (secrobject; fit = TRUE) for each replicate by setting extractfn = identity. For a large analysis there is a risk of exceeding memory limits in R, and saving everything is generally not a good idea. For most purposes it is sufficient to save a trimmed version of the fitted model extractfn = trim (note secr defines the function 'trim'). However, the full model is needed for derived.SL or regionN.SL.

run.scenarios sets the class¹ of its output to distinguish among fitted models ("fittedmodels"), estimate tables from predict, coef etc. ("estimatetables"), and numeric values ready for summarisation ("selectdstatistics") class. Simulated data saved with fit = FALSE, extractfn = identity have class c("rawdata", "secrdesign", "list"). An attribute 'outputtype' is used to make finer distinctions among these types of output ('secrfit', 'predicted', coef', 'capthist', or 'numeric'). Output from extractfn = derived is treated as 'predicted'.

When fit = TRUE, analyses are performed with secr.fit. Other analyses may be specified by setting fit = FALSE and providing the analysis function as the value for extractfn. The function should accept a 'capthist' object as input. For example, conventional closed-population estimates may be obtained with

This applies various *nonspatial* estimators to simulated *spatial* samples. Named arguments of extractfn may be included (here, 'estimator'); these are used for all scenarios, unlike fit.args which may vary among scenarios. Summarisation of alternative analyses will usually require careful selection of 'parameter' and 'statistics' in select.stats (5.2).

4.3 More on masks

A habitat mask in **secr** is a raster representation of the region near the detectors in which the centres of detected animals may lie. This excludes both nearby non-habitat, and habitat that is so distant that it is implausible any animal centred there would reach a detector. It is often convenient to define a mask to include all cells whose centre is within a certain distance of a detector - the buffer radius.

Within **secrdesign**, a mask is used both when generating populations of animals with sim.popn and when fitting SECR models with secr.fit. The extent of the mask used to generate populations is important if you are concerned with population size (for example, if you set extractfn = region.N). Then the size of the region determines the 'true' value of the parameter of interest (N), and influences its sampling variance. The extent of the mask is less critical when density is the parameter of interest.

The default behaviour of run.scenarios is to use a concave buffer of width xsigma × sigma around the particular detector layout. The 'coarseness' of the

¹the full class is actually c(x, "secrdesign", "list") where x is as described

mask is determined by nx; note that the default for run.scenarios (32) is coarser than the default for secr::make.mask (64). This makes for speed, and is fairly safe when the buffer width is well matched to the scale of movement (of course we know sigma, so the default buffer width is well-matched). The same mask is used both for generating populations and fitting models.

Users may specify their own masks in the 'maskset' list argument. If the number of masks in 'maskset' is one or a number equal to the number of detector layouts, then a column 'maskindex' is added automatically to the 'scenarios' dataframe (all 1, or equal to trapsindex, in the two cases). Otherwise, the user must have manually added a maskindex column to 'scenarios' to clarify which mask should be used with which scenario.

5 Summarising simulation output

run.scenarios usually takes a long time to run, but having saved its output you can quickly extract and summarise the results in many different ways.

We saw in the previous section and Fig. 1 that the output from run.scenarios for each replicate may be a fitted model, a table of parameter estimates, or a numeric vector. Summarisation across replicates (the summary method) requires output in 'selected statistics' form, so each of the other forms must be processed first².

Look again at Fig. 1: you will see that the primary input to the summary function is in the form of selected statistics. A secondary route is to automatically extract statistics from estimates tables, as shown by the dashed line in Fig. 1 – we used this in the simple example of 1.2. We now address how other forms of output from run.scenarios can be processed into 'selected statistics' form.

5.1 Extracting estimate tables from fitted models

The methods predict and coef for the 'fittedmodels' class and the function derived.SL are provided to extract estimates of 'real' parameters from each fitted model. These are direct analogues of predict, coef and derived in secr. Here, they apply across all replicates of all scenarios and return an object of class 'estimatetables'. regionN.SL is another possibility.

In each case, the result is a dataframe or list of dataframes for each replicate. Rows correspond to estimated parameters (or 'R.N' and 'E.N' for regionN.SL)

²Processing happens silently using default settings of select.stats when summary is applied directly to 'estimate tables' output

and columns to the respective estimates, standard errors, and confidence limits (with some variations).

The ... argument lets you pass arguments such as 'alpha' to the **secr** functions predict.secr and derived.

We can skip this step for the output from our simple example as it is already in 'estimatetables' form.

5.2 Choosing the statistics to summarise

Given tabular output from predict() or derived.SL(), we must select replicatespecific numerical quantities for further summarisation.³ This is the role of select.stats(), which has arguments –

```
select.stats(object, parameter = "D", statistics)
```

The parameter of interest defaults to density ("D"); others such as "g0" or "sigma" may be substituted, so long as they appear in the input object. To check which parameters are available use

```
find.param(object)
```

The task of select.stats is to reduce each replicate to a vector of numeric values - we can think of the result as a replicate × value matrix for each scenario (Fig. 2). A later step (summary) computes statistics ('fields') such as mean and SE for each column in the matrix, as described in the next section.

Here we describe the replicate-specific statistics that form the numeric vector. These may be simply 'estimate', 'SE.estimate', 'lcl' and 'ucl' as output from predict.secr.

Additionally, when fit = TRUE, we can include statistics derived from the estimates of a parameter (Table 1). To describe these we use 'true' to stand for the known value of a real parameter, and 'estimate' for the estimate from a particular replicate.

We use ('lcl', 'ucl') to represent a confidence interval for 'estimate'. Usually these are 95% intervals, but the level may be varied by setting the argument 'alpha' in predict (e.g., alpha = 0.1 for a 90% interval). Intervals from

³If run.scenarios has been used with fit = FALSE, then the output from each replicate is probably already in the form of selected statistics (the default raw data summaries 'n', 'ndet', 'nmov' and 'dpa') and select.stats is not relevant. The same may also apply with a user-provided extractfn when fit = TRUE.

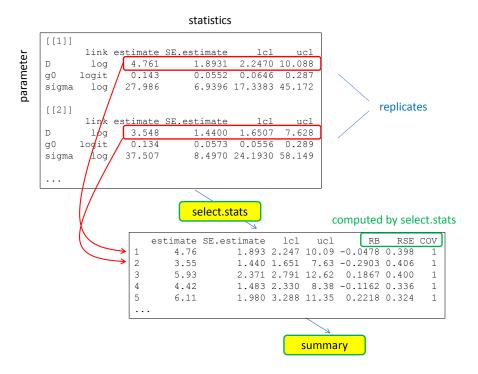


Figure 2: Operation of select.stats()

predict.secr are symmetrical on the link scale, and hence asymmetrical on
the natural scale. Note also the argument loginterval in derived; the default
loginterval = TRUE gives an asymmetrical interval on the natural scale.

The coverage indicator COV is a binary value; this becomes interesting later when averaged over a large number of replicates to give a coverage proportion. The absolute deviation also comes into its own later as the basis for RMSE. In a sense the same is true of replicate-specific RB: RB should be reported only as an average over a large number of replicates.

Returning to our simple example, we apply select.stats to focus on the density parameter "D".

Table 1: Computed statistics available in select.stats

Statistic	Short name	Value
Relative bias ¹	RB	(estimate – true) / true
Relative SE^2	RSE	SE.estimate / estimate
Absolute deviation	ERR	abs(estimate - true)
Coverage indicator	COV	(estimate $>$ lcl) & (estimate $<$ ucl)

- 1. Also called 'normalised bias'
- 2. Also called 'coefficient of variation'

```
3 3.860603 1.838079 8.108603 -0.22787945 0.3926149
                                                      1
4 4.455237 2.395654 8.285477 -0.10895269 0.3246465
                                                      1
$`2`
   estimate
                  lcl
                           ucl
                                        RB
                                                  RSE COV
1 16.329709 11.210633 23.78629 0.63297089 0.1936836
            5.694946 16.18535 -0.03992348 0.2712667
2 9.600765
                                                        1
3 10.305960
             6.417433 16.55067 0.03059603 0.2452631
                                                        1
4 12.628829
            8.370561 19.05336 0.26288289 0.2121620
                                                        1
```

The two scenarios yield two replicates \times statistic matrices, from which we display the first 4 rows.

5.3 Disposing of rogue values

Simulation output may contain rogue values due to idiosyncracies of model fitting. For example, nonidentifiability due to inadequate data can result in spurious extreme 'estimates' of the sampling variance. The median (chosen as a 'field' value in summary) is recommended as a robust alternative to the mean when there are some extreme estimates.

```
validate (x, test, validrange = c(0, Inf), targets = test)
```

Another way to deal with the problem is to set statistics to NA when a simulation fails. The function validate sets selected 'target' statistics to NA for replicates in which another 'test' statistic is out-of-range or NA. The permissable bounds are usually arbitrary, and the method should be used with care. The keyword "all" may be used for targets to indicate all columns.

validate accepts a 'selected statistics' object (x) as input and returns a modified 'selected statistics' object. See 8.2 for an application.

5.4 Summary method

The summary method for 'selected statistics' objects reports both header information on the simulation scenarios and user-selected summaries of the pre-selected statistics.

```
summary (object, dec = 5, fields = c("n", "mean", "se"), alpha = 0.05,
type = c("list", "dataframe", "array"), ...)
```

Here the summary statistics are called 'fields' to distinguish them from the 'statistics' in each column of the numeric replicate \times value matrix for each scenario (see 5.2). The task of the summary method is to compute the 'field' value for each 'statistic', summarising across replicates to give a 'statistic' \times 'field' matrix for each scenario. The choice of 'fields' is shown in Table 2.

Table 2: Statistic 'fields' available in the summary method for 'selectedstatistics' objects

Field	Description
n	number of non-missing values
mean	mean
se	standard error
sd	sample standard deviation
\min	minimum
max	maximum
lcl	lower $100(1-\alpha)$ % confidence limit
ucl	upper $100(1-\alpha)$ % confidence limit
${ m rms}$	root mean square
median	median
qxxx	xxx/1000 quantile
qyyy	yyy/1000 quantile

The summary fields 'lcl' and 'ucl' are for a simple Wald interval $(\bar{x}+z_{\alpha/2}SE(x), \bar{x}+z_{1-\alpha/2}SE(x))$ where z_{α} is the 100α -percentile of a standard normal distribution (e.g., $z_{0.975}=1.96$). [Do not confuse these with the confidence limit statistics of the same name that are symmetrical only on the link scale].

Quantiles are specified as 'qxxx' and 'qyyy' where xxx and yyy are integers between 1 and 999 corresponding to quantiles 0.001 to 0.999. For example, 'q025' refers to the 2.5% quantile.

Applying the 'rms' field to the absolute deviation of an estimate ('ERR') provides the root-mean-square-error 'RMSE'.

To recap – a summary value is reported for each combination of a selected statistic, computed for each replicate, and a 'field' that summarises the statistic across replicates, potentially resulting in a table with this structure:

I	7i	elds										
Statistics	n	mean	se	sd	min	max	lcl	ucl	rms	median	q025	q975
estimate	•	•	•	•	•	•	•	•		•	•	•
SE.estimate	•	•	•	•	•	•	•	•		•	•	•
lcl	•	•	•	•	•	•				•	•	•
ucl	•	•	•	•	•	•				•	•	•
RB	•	•	•	•	•	•				•	•	•
RSE	•	•	•	•	•	•	•	•		•	•	•
ERR	•	•	•	•	•	•	•	•	•	•	•	•
COV	•	•	•	•	•	•						

Cells are left blank for combinations that are unlikely to be meaningful. 'rms' is useful with 'ERR' (i.e. RMSE), but not when applied to other statistics. 'n', 'mean' and 'se' summarise the 'COV' indicator, but other potential summaries are (almost) meaningless.

Apply this to the selected statistics from our simple example:

```
> summary(stats1)
run.scenarios(nrepl = 50, scenarios = scen1, trapset = traps1,
    fit = TRUE, seed = 345)
```

Replicates 50

Started 11:07:01 02 May 2014

Run time 1.693 minutes
Output class selectedstatistics

\$constant

	value
trapsindex	1
noccasions	3
nrepeats	1
g0	0.2
sigma	25
detectfn	0
recapfactor	1
popindex	1
detindex	1

```
fitindex
                1
maskindex
                1
$varying
 scenario
           D
        1 5
        2 10
$detectors
 trapsindex trapsname
          1
               traps1
OUTPUT
D = 5
                mean
estimate 50
             5.23767 0.24994
             2.70152 0.16476
lcl
         50 10.28534 0.37589
ucl
RB
             0.04753 0.04999
RSE
             0.36890 0.00962
COV
         50
             0.92000 0.03876
D = 10
                mean
estimate 50
             9.58795 0.36972
lcl
             5.86410 0.27453
ucl
         50 15.75842 0.47775
RB
         50 -0.04121 0.03697
RSE
             0.26727 0.00668
         50
COV
             0.92000 0.03876
         50
```

5.5 Plot method

Use the plot method to visualise the distributions of 'selected statistics' that you have simulated. You may plot either (i) histograms of the selected statistics (type = 'hist') or (ii) the estimate and confidence interval for each replicate (type = 'CI'). One histogram is plotted for each combination of scenario and statistic – you may want to select a subset of scenarios and statistics, and use the graphics options mfcol or mfrow to control the layout. For type = 'CI' the statistics must include 'estimate', 'lcl' and 'ucl' (or 'beta', 'lcl' and 'ucl' if outputtype = 'coef').

```
> par(mfrow = c(2, 2))
> plot(stats1, type = "hist", statistic = "estimate")
> plot(stats1, type = "CI")
```

See Fig. 3 for the result.

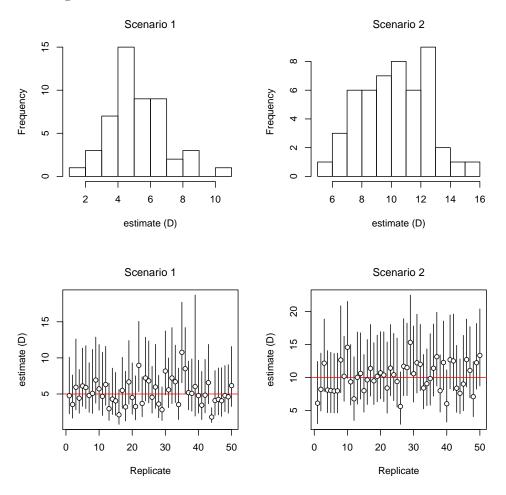


Figure 3: Plot method applied to a 2-scenario 'selected statistics' object with type = 'hist' (top) and type = 'CI' (bottom)

6 Additional topics

6.1 Parallel processing

Setting ncores > 1 causes run.scenarios to run separate scenarios on separate cores. This uses the R package parallel. Technically, it relies on Rscript, and

communication between the master and worker processes is via sockets. As stated in the R **parallel** documentation "Users of Windows and Mac OS X may expect pop-up dialog boxes from the firewall asking if an R process should accept incoming connections". It appears to be safe to accept these.

Use parallel::detectCores() to get an idea of how many cores are available on your machine; this may (in Windows) include virtual cores over and above the number of physical cores. If you use the maximum available cores for run.scenarios then expect any other processes on the machine to slow down!

Running one scenario per core is suboptimal if scenarios differ widely in how long they take to run: the system waits for the slowest. There is no way around this limitation in **secrdesign**.

Random number generation for multiple cores uses the "L'Ecuyer-CMRG" random number generator as described in ?RNG.

6.2 Shortcut evaluation of precision

The asymptotic variance (and hence RSE) of a maximum likelihood estimate is typically obtained from the curvature of the likelihood computed numerically at the fitted value of the parameter(s) (i.e., at the MLE). Fitting SECR models is slow. An alternative estimate of the RSE that is sufficient for most purposes may be got from the curvature of the likelihood computed at the known 'true' value(s) of the parameter(s). This is much faster as it does not require the model to be fitted.

secr.fit may be 'tricked' into providing this variance estimate by setting
method = "none" and providing the true values as the start vector. run.scenarios
makes this easy by assuming that if you specify method = "none" you wish to
use start = "true". However, this works only when there is a 1:1 relationship
between 'beta' and 'real' parameters; it does not work when 'recapfactor' is
specified.

Replicates 50

Started 13:56:27 02 May 2014

Run time 0.364 minutes
Output class selectedstatistics

\$constant

value trapsindex noccasions 3 nrepeats 1 g0 0.2 25 sigma ${\tt detectfn}$ 0 recapfactor 1 popindex detindex 1 fitindex 1 maskindex 1

\$varying

scenario D

1 5

2 10

\$detectors

trapsindex trapsname

1 traps1

\$fit.args

fitindex method

1 none

OUTPUT

\$`D = 5`

 n
 mean
 se

 estimate
 50
 5.00000
 0.00000

 SE.estimate
 49
 1.88876
 0.04280

 lcl
 49
 2.46033
 0.03457

 ucl
 49
 10.27008
 0.16263

 RB
 0
 NA
 NA

```
RSE
                 0.37775 0.00856
             49
COV
              0
                       NΑ
                                NΑ
$`D = 10`
              n
                     mean
                                se
estimate
             50 10.00000 0.00000
SE.estimate 50
                 2.66698 0.05948
                 6.00324 0.06291
lcl
             50
ucl
             50
                16.75599 0.19230
RΒ
              0
                       NΑ
                                NΑ
RSE
                 0.26670 0.00595
             50
COV
              0
                                ΝA
                       NA
```

Each estimate of RSE is essentially the same as before, but the run time is reduced by nearly 80%. Note the true value of density appears as a constant "estimate" in the summary. Care is need with this method as its performance in extreme cases has not been investigated fully.

6.3 Non-uniform populations

The simulated population by default has a uniform (homogeneous) Poisson distribution. To generate and sample from a spatially inhomogeneous population we use the 'IHP' option for argument 'model2D' in secr::sim.popn. This involves three steps:

- 1. Create a habitat mask object with the desired extent.
- 2. Add to the mask a covariates dataframe with one or more columns defining pixel-specific densities.
- 3. In run.scenarios specify a list of pop.args including model2D = "IHP" and D = "XX" where XX is the name of the particular mask covariate you wish to use for density, and name your mask in the 'maskset' argument.

A full demonstration is given in the Appendix (8.3).

To visualise simulated populations you should set savepopn = TRUE in det.args and later extract the populations the capthist object (for example, with a custom extractfn).

To compare several inhomogeneous distributions, specify several pop.args lists and use the popindex argument in make.scenarios. The distribution may be varied simply by using the sim.popn argument 'D' to select different covariates of one mask.

The columns 'nrepeats' and 'D' in the scenarios object as input are ignored when model2D = "IHP". 'D' is replaced by the average density over the mask, which is used as the 'true' value of density in computing RB, RSE etc. in summaries. For stratified analyses you will have to define your own extractfn.

6.4 Splitting data generation and model fitting

Each new detector layout or new model specification (in a fit.args list) defines a new scenario. The default procedure is to generate new data (both animal locations and simulated detection histories) for each scenario. To compare different models applied to the same dataset, save raw data from an initial call to run.scenarios with fit = FALSE, extractfn = identity, and separately fit a list of models with fit.models. You can also peek at the raw data with the summary method.

Here, scen3 describes two scenarios, and in the call to fit.models each of these is split into two new scenarios, one for each component of fit.args.

It is not possible within **secrdesign** precisely to evaluate the application to the same animal distribution (population) of differing detector layouts or specifications for the fitted model (cf Fewster and Buckland 2004). Comparisons inevitably include variance from the varying number and placement of animals, and the sampling process; this variance may be reduced by fixing the number of individuals (pop.args = list(Ndist = "fixed")).

6.5 Limitations, tips and troubleshooting

secrdesign has some limitations (Surprise!).

 A progress message is output only on the completion of each scenario, which can be annoying, and when using multiple cores even this message is lost. It is strongly recommended that you start by generating summaries of raw data only (run.scenarios with fit = FALSE), and confirm that your scenarios are realistic by reviewing the simulated number of detected individuals, total number of detections, etc. If these are inadequate or unrealistically large then there's no point going on. Then, try fitting with just a few replicates to be sure you have specified the model you intended and to assess the likely run time. Only then submit a run with a large number of replicates.

- Only 2-parameter detection functions are allowed for data generation.
 This excludes the hazard-rate function, the cumulative gamma, and some others.
- 3. The default extractfn does does not handle models that produce more than one estimates table per replicate (e.g., finite mixture models). A custom extractfn is needed; it should either produce a numeric vector of 'selected statistics' or mimic single-dataframe output from predict().
- 4. The function secr::sim.capthist that generates detection histories for secrdesign has limited capacity for simulating temporal, behavioural or other heterogeneity in detection probability. The capacity of run.scenarios is even more limited: only a general learned response is allowed (recapfactor).
- 5. As noted before, the same mask is used for generating populations and fitting models. It would be possible to replace the maskset component of a 'rawdata' object before running fit.models, but this is not recommended.
- 6. It is easy to forget the random number seed. Consider replacing the default value.
- 7. The method for fitting a fixed-N model (distribution = binomial) is somewhat fragile: it can fail when given a start value for D that is less than the minimum density observed (i.e., the number of distinct individuals divided by the mask area). This can easily happen when a population is simulated with pop.args = list(Ndist = "poisson") (the default) and sampled with high detection probability, but secr.fit is called with (distribution = "binomial"). The solution is to use pop.args = list(Ndist = "fixed").
- 8. If your summaries do not include enough significant digits, increase the 'dec' argument!

7 References

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8 Appendix. Examples

Here we give some annotated examples of simulation code and selected output. Running this code with reduced nrepl, and viewing the output, will give you an idea of how secrdesign works.

8.1 Multiple grids, varying number of occasions

This is the other example from the main text, slightly extended

8.2 Learned trap response

Here we assess the bias in \hat{D} caused by ignoring a learned trap response.

```
## set up and run simulations
traps5 <- list(grid6x6 = make.grid(6,6),</pre>
                grid10x10 = make.grid(10,10)
scen5 <- make.scenarios (trapsindex = 1:2, noccasions = 5, D = 5,</pre>
    g0 = 0.2, sigma = 25, recapfactor = c(0.5, 1, 2), fitindex = 1:2)
sims5 <- run.scenarios(nrepl = 500, trapset = traps5, scenarios =</pre>
    scen5, fit = TRUE, fit.args = list(list(model = g0 ~ 1),
    list(model = g0 ~ b)), ncores = 6)
## select statistics and throw out any replicates with SE > 100
## (there is one -- see reduced n in output for scenario 11)
stats5 <- select.stats(sims5)</pre>
stats5 <- validate(stats5, "SE.estimate", c(0,100), "all")</pre>
## plot
sum5 <- summary(stats5, fields = c("n","mean","se","lcl","ucl", "median"))</pre>
plot(c(0.5,6.5), c(-0.2,0.4), type="n", xlab = "Scenario", ylab = "RB(D-hat)")
for (i in 1:12) {
    xv \leftarrow if (i \le 6) i else (i-6) + 0.05
    segments (xv, sum5$0UTPUT[[i]]["RB","lc1"], xv, sum5$0UTPUT[[i]]["RB","uc1"])
    ptcol <- if (i<=6) "white" else "black"</pre>
    points(xv, sum5$OUTPUT[[i]]["RB", "mean"], pch = 21, bg = ptcol)
abline(h = 0, col="red")
text(c(1.5,3.5,5.5), rep(0.38,3), paste("recapfactor", c(0.5,1,2), sep = " = "))
```

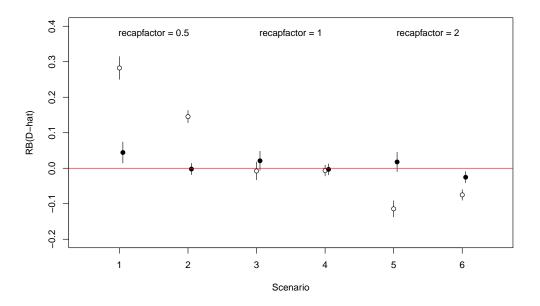


Figure 4: Relative bias of SECR density estimate from null model (filled circles) and $g0 \sim b$ model (open circles) when data were generated with negative, zero, or positive learned response.

```
## look at extended output
sum5
```

```
run.scenarios(nrepl = 500, scenarios = scen5, trapset = traps5,
   fit = TRUE, fit.args = list(list(model = g0 ~ 1), list(model = g0 ~
   b)), ncores = 6)
```

Replicates 500

Started 12:05:03 02 May 2014

Run time 99.6 minutes
Output class selectedstatistics

\$constant

	value
noccasions	5
nrepeats	1
D	5
g0	0.2
sigma	25
detectfn	0

popindex 1 detindex 1

\$varying

scenario	trapsindex	recapfactor	fitindex	maskindex
1	1	0.5	1	1
2	2	0.5	1	2
3	1	1.0	1	1
4	2	1.0	1	2
5	1	2.0	1	1
6	2	2.0	1	2
7	1	0.5	2	1
8	2	0.5	2	2
9	1	1.0	2	1
10	2	1.0	2	2
11	1	2.0	2	1
12	2	2.0	2	2

\$detectors

trapsindex trapsname

1 grid6x6

2 grid10x10

\$fit.args

fitindex model

1 g0 ~ 1

2 g0 ~ b

OUTPUT

```
$`trapsindex = 1, recapfactor = 0.5, fitindex = 1, maskindex = 1`
                  mean
                            se
                                   lcl
                                           ucl median
            n
           500 6.41255 0.08204 6.25175 6.57334 6.25433
estimate
SE.estimate 500 1.99650 0.02054 1.95623 2.03676 1.93299
lcl
           500 3.55072 0.05517 3.44258 3.65885 3.36304
           500 11.67837 0.12692 11.42960 11.92714 11.32535
ucl
RB
           500 0.28251 0.01641 0.25035 0.31467 0.25087
RSE
           500 0.32141 0.00251 0.31649 0.32633 0.31316
COV
           500 0.86000 0.01553 0.82956 0.89044 1.00000
```

```
SE.estimate 500 1.02213 0.00456 1.01319 1.03107 1.01752
1cl
            500 4.05010 0.03642 3.97872 4.12148 4.00269
ucl
            500 8.10669 0.05348 8.00187 8.21152 8.03134
RB
            500 0.14553 0.00892 0.12805 0.16301 0.13330
            500 0.18094 0.00069 0.17958 0.18229 0.17943
RSE
            500 0.88000 0.01455 0.85149 0.90851 1.00000
COV
$`trapsindex = 1, recapfactor = 1, fitindex = 1, maskindex = 1`
                                      lcl
                                              ucl
                                                    median
             n
                   mean
                              se
            500
                                 4.83654 5.08669 4.98843
estimate
               4.96161 0.06381
SE.estimate 500 1.47525 0.01175 1.45223 1.49828 1.47518
            500 2.81512 0.04459 2.72772 2.90251 2.78540
lcl
            500 8.79952 0.08750 8.62803 8.97102 8.84495
ucl
RB
            500 -0.00768 0.01276 -0.03269 0.01734 -0.00231
RSE
            500 0.30992 0.00240 0.30521 0.31463 0.29930
COV
               0.95000 0.00976 0.93088 0.96912 1.00000
$`trapsindex = 2, recapfactor = 1, fitindex = 1, maskindex = 2`
                                      lcl
                                              ucl
                                                    median
             n
                   mean
                              se
estimate
            500 4.96749 0.03917 4.89071 5.04426 4.92346
SE.estimate 500  0.88098  0.00375  0.87364  0.88832  0.88014
            500 3.52016 0.03224 3.45698 3.58334 3.47659
lcl
            500 7.01611 0.04641 6.92515 7.10708 6.97002
ucl
RB
            500 -0.00650 0.00783 -0.02186 0.00885 -0.01531
RSE
            500
               0.18008 0.00073 0.17866 0.18151 0.17812
COV
            500
                0.96000 0.00877 0.94281 0.97719
$`trapsindex = 1, recapfactor = 2, fitindex = 1, maskindex = 1`
                                      lcl
                                              ucl
                   mean
                                                     median
             n
                              se
            500 4.42837 0.05842 4.31386 4.54287
estimate
                                                   4.41579
SE.estimate 500 1.29956 0.00981 1.28034
                                          1.31878
                                                    1.30119
lcl
            500 2.53232 0.04180 2.45039
                                          2.61425
                                                    2.49668
ucl
            500 7.80193 0.07721
                                 7.65061
                                          7.95325
                                                    7.80782
RB
            500 -0.11433 0.01168 -0.13723 -0.09143 -0.11684
            500 0.30702 0.00243 0.30225
RSE
                                          0.31178
                                                   0.29720
COV
            500 0.94400 0.01029 0.92383
                                          0.96417
                                                   1.00000
$`trapsindex = 2, recapfactor = 2, fitindex = 1, maskindex = 2`
              n
                    mean
                              se
                                      lcl
                                              ucl
                                                     median
```

500 5.72766 0.04459 5.64026 5.81506 5.66648

estimate

estimate

4.59226

500 4.62434 0.03824 4.54939 4.69929

```
lcl
           500 3.28267 0.03149 3.22094 3.34440
                                                   3.23926
           500 6.52046 0.04528 6.43172 6.60920
ucl
                                                   6.49095
RB
           500 -0.07513 0.00765 -0.09012 -0.06014 -0.08155
RSE
           500 0.17943 0.00076 0.17795 0.18092
                                                   0.17822
COV
           500 0.93200 0.01127 0.90991 0.95409
$`trapsindex = 1, recapfactor = 0.5, fitindex = 2, maskindex = 1`
                  mean
                            se
                                   lcl
                                            ucl median
estimate
           500 5.22167 0.07578 5.07315 5.37019 5.18323
SE.estimate 500 1.74583 0.02123 1.70423 1.78744 1.71095
           500 2.78488 0.05062 2.68566 2.88410 2.70792
lcl
           500 9.94459 0.12380 9.70195 10.18723 9.75850
ucl
           500 0.04433 0.01516 0.01463 0.07404 0.03665
RB
RSE
           500 0.34976 0.00350 0.34290 0.35661 0.33759
           500 0.94200 0.01046 0.92149 0.96251 1.00000
COV
$`trapsindex = 2, recapfactor = 0.5, fitindex = 2, maskindex = 2`
                                     lcl
             n
                   mean
                                             ucl
                                                   median
                             se
           500 4.98864 0.04090 4.90848 5.06880 4.97724
estimate
SE.estimate 500 0.92341 0.00434 0.91490 0.93192 0.92743
           500 3.48357 0.03322 3.41845 3.54868 3.47396
lcl
           500 7.15203 0.04916 7.05567 7.24838 7.15163
ucl
           500 -0.00227 0.00818 -0.01830 0.01376 -0.00455
RB
RSE
           500 0.18824 0.00084 0.18659 0.18989 0.18550
COV
           500 0.94600 0.01012 0.92617 0.96583 1.00000
$`trapsindex = 1, recapfactor = 1, fitindex = 2, maskindex = 1`
                                     lcl
                                              ucl
             n
                   mean
                             se
                                                    median
           500 5.10488 0.06876 4.97011 5.23966 4.95098
estimate
SE.estimate 500 1.72420 0.08918 1.54942 1.89899
                                                   1.58177
           500 2.78061 0.04719 2.68812
                                          2.87311
lcl
                                                   2.67837
ucl
           500 10.08840 0.61405 8.88488 11.29193
RB
           500 0.02098 0.01375 -0.00598
                                          0.04793 -0.00980
RSE
           500 0.34471 0.01301 0.31922
                                          0.37021
           500 0.95800 0.00898 0.94040 0.97560
COV
                                                   1.00000
$`trapsindex = 2, recapfactor = 1, fitindex = 2, maskindex = 2`
                                     lcl
                                             ucl
             n
                   mean
                             se
                                                   median
estimate
           500 4.98399 0.03952 4.90652 5.06145 4.95613
SE.estimate 500  0.90665  0.00427  0.89827  0.91502  0.90778
```

SE.estimate 500 0.81600 0.00362 0.80891 0.82309

0.81839

```
lcl
            500 3.50121 0.03202 3.43845 3.56397 3.48533
            500 7.10126 0.04781 7.00755 7.19497 7.08731
ucl
            500 -0.00320 0.00790 -0.01870 0.01229 -0.00877
RB
RSE
            500 0.18461 0.00076 0.18313 0.18609
                                                  0.18262
COV
            500 0.95000 0.00976 0.93088 0.96912 1.00000
$`trapsindex = 1, recapfactor = 2, fitindex = 2, maskindex = 1`
             n
                  mean
                             se
                                     lcl
                                            ucl median
estimate
            499 5.08846 0.06975 4.95175 5.22517 5.08003
SE.estimate 499 1.58825 0.01682 1.55528 1.62122 1.57657
            499 2.81611 0.04749 2.72302 2.90920 2.80196
lcl
            499 9.28585 0.10583 9.07842 9.49327 9.22943
ucl
RB
            499 0.01769 0.01395 -0.00965 0.04503 0.01601
            499 0.32504 0.00269 0.31976 0.33031 0.31165
RSE
COV
            499 0.93587 0.01098 0.91436 0.95739 1.00000
$`trapsindex = 2, recapfactor = 2, fitindex = 2, maskindex = 2`
                                      lcl
                                               ucl
             n
                   mean
                              se
                                                     median
estimate
            500
               4.87325 0.04075
                                 4.79337
                                           4.95313
                                                    4.82339
SE.estimate 500 0.89038 0.00427
                                 0.88201
                                          0.89876
                                                    0.88879
lcl
            500 3.41845 0.03312 3.35353
                                          3.48337
                                                    3.39162
ucl
            500 6.95444 0.04902 6.85836
                                          7.05052
                                                   6.91494
            500 -0.02535 0.00815 -0.04133 -0.00937 -0.03532
R.B
            500 0.18580 0.00080 0.18422
RSE
                                          0.18737
COV
            500 0.94800 0.00994
                                 0.92852
                                          0.96748 1.00000
```

8.3 Non-uniform possums

Code to illustrate the use of homogeneous and inhomogeneous density models.

```
## add covariates to builtin secr object possummask
## D1 is homogeneous density
## D2 is artificial SW - NE gradient in density

xy <- apply(possummask,1,sum) / 500
covariates(possummask)[, "D1"] <- 2
covariates(possummask)[, "D2"] <- xy - mean(xy) + 2.5

## Note that this object already had a covariates dataframe
## -- if it didn't we would use
## covariates(possummask) <- data.frame ( D1 = ..., D2 = ...)</pre>
```

```
## specify scenarios
## anticipate two different sets of arguments for sim.popn
## with popindex = 1:2
scen5 <- make.scenarios (g0 = 0.2, sigma = 45, noccasions = 5,</pre>
    popindex = 1:2)
## specify alternate models for distribution of animals
poplist <- list(list(model2D = "IHP", D = "D1"),</pre>
                list(model2D = "IHP", D = "D2"))
## run scenarios and summarise
## we use the trap layout from the builtin secr object possumCH
sims5 <- run.scenarios (50, scen5, traps(possumCH), possummask,</pre>
   pop.args = poplist)
summary(sims5)
## output follows
run.scenarios(nrepl = 50, scenarios = scen5, trapset = traps(possumCH),
   maskset = possummask, pop.args = poplist)
Replicates
Started
              09:53:30 29 Apr 2014
             0.092 minutes
Run time
Output class selectedstatistics
$constant
            value
trapsindex
               1
noccasions
                5
nrepeats
              1
              0.2
g0
sigma
             45
detectfn
                0
recapfactor
               1
detindex
                1
fitindex
                1
```

```
maskindex 1
```

\$varying

scenario D popindex 1 2.0 1 2 2.5 2

\$detectors

\$pop.args

 $\begin{array}{ccc} \text{popindex} & \text{model2D} & \text{D} \\ & 1 & \text{IHP} & \text{D1} \\ & 2 & \text{IHP} & \text{D2} \end{array}$

OUTPUT

\$`D = 2.5, popindex = 2`
n mean se
n 50 136.46000 1.50026
ndet 50 328.76000 3.92497
nmov 50 170.46000 2.39101
dpa 50 2.16096 0.01142

To visualise individual realisations of the distribution of animals, use fit = FALSE (the default), det.args = list(savepopn = TRUE), and save the entire capthist object (extractfn = identity). Here we create a single replicate.

```
tmp <- run.scenarios (1, scen5, traps(possumCH), possummask,
    pop.args = poplist, det.args = list(savepopn = TRUE),
    extractfn = identity)</pre>
```

tmp\$output is now a list (one component per scenario) of lists
(one component per replicate) of simulated capthist objects, each

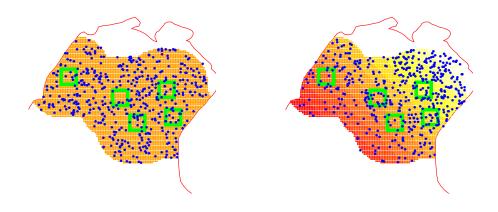


Figure 5: Simulated homogeneous (left) and inhomogeneous (right) distributions of brushtail possums at Waitarere, New Zealand. Traps in green (each hollow grid 180 m square).