# strum package - examples

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This document contains the whole analysis process for the first three example models from the introduction document. Note that the input data used for these examples are not necessarily simulated to give a meaningful result for each analysis.

# > library(strum)

# 1 Genetic association analysis

This is an example of a typical genetic association analysis model with a latent trait (similar to MIMIC model). Suppose that there are three measurements (P1, P2 and P3), and it is hypothesized that there is a single latent trait (L1) underlying the three measurements. The latent variable L1 is influenced by a SNP and a set of variance components, polygenic(p) and random environmental(e). Each trait is also influenced by its own random environmental factor. This is the model diagram.

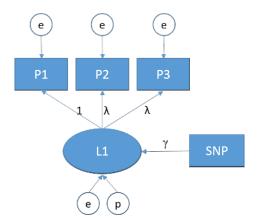


Figure 1: Genetic association analysis model

#### 1.1 Construct model

The first step is to construct a **strumModel** object specifying the above model using *createStrumModel()* function.

```
> assoForm1 =
    'L1 =~ P1 + P2 + P3 + <e>
    L1 \sim aSNP + \langle p, e \rangle
> myAssoModel = createStrumModel(formulas = assoForm1)
Creating strumModel ..... Done
> myAssoModel
Basic properties of the model:
        Model Class ..... strumModel
        Ascertainment ..... FALSE
List of all variables:
      Obs Covariate InEita
                            InY Exogen.
L1
    FALSE
              FALSE
                     TRUE FALSE
                                  FALSE
aSNP
     TRUE
               TRUE FALSE FALSE
                                     NA
P1
     TRUE
              FALSE FALSE TRUE
                                     NA
P2
              FALSE FALSE TRUE
     TRUE
                                     NA
Р3
     TRUE
              FALSE FALSE TRUE
                                     NA
Model formulas:
 L1 = P1 + P2 + P3 + <e>
 L1 ^{\sim} aSNP + <p,e>
```

# 1.2 Prepare data

The next step is to prepare data. In this example, the data must be a data.frame with 4 required fields - family, id, father, mother, since the model includes the polygenic variance component (p). To run a strum analysis, you need to construct a **strumData** object created by the *createStrumData()* function with a data.frame. The following code shows the step using the example input file "chr1Ped.csv".

Data type: Pedigree

Data size: 477 entries, 18 variables

First 5 rows of data values:

	family	id	fath	er moth	ner	sex	disease	proband		P1	P2	Р3
1	1	1		0	0	0	0	0	0.40	093955	0.44450079	-0.3867515
2	1	2		0	0	1	0	0	-1.50	037814	1.52582608	0.8832360
3	1	3		1	2	0	0	0	1.58	350090	0.08833692	0.9322619
4	1	4		1	2	1	0	0	1.62	246356	0.60065352	1.0895325
5	1	5		1	2	1	0	0	-0.4	111477	0.08588345	-0.6477336
	SBP		DBP	A1		A2	S1	S2	aSNP	rs6040	0343	
1	3.39	4.1	1800	1.300	1.	.630	1.9000	-0.0613	1		1	
2	-3.49	-2.7	7200	-0.784	-3	.550	-2.8900	-2.1300	0		0	
3	-3.40	0.0	0815	-1.820	-4	.390	-1.6700	-3.0900	1		0	
4	-7.04	-3.6	3500 ·	-0.183	-4	.740	-2.9800	-2.3500	0		0	
5	4.60	4.9	9900	2.440	-0.	.117	-0.0408	-0.4350	1		1	

phi object contains 75 matrices:

First matrix:

\$`1`

1 2 3 4 5 6 7
1 1.0 0.0 0.5 0.5 0.5 0.5 0.5
2 0.0 1.0 0.5 0.5 0.5 0.5 0.5
3 0.5 0.5 1.0 0.5 0.5 0.5 0.5
4 0.5 0.5 0.5 0.5 1.0 0.5 0.5 0.5
5 0.5 0.5 0.5 0.5 0.5 1.0 0.5 0.5
6 0.5 0.5 0.5 0.5 0.5 0.5 1.0 0.5
7 0.5 0.5 0.5 0.5 0.5 0.5 0.5 1.0

Empty IBD object.

# 1.3 Run analysis

Now, run the association analysis by the function call strum() with two previously constructed objects as the arguments.

> myAssoResult = strum(myAssoModel, myAssoData)

Analysis completed!

## 1.4 Result

The result object contains the model description and two result tables. The first table contains the fitted parameter values with standard errors, confidence intervals, and p-values. The second table contains the information on the model fit from four different measures. For association analysis, you would test  $H_0$ :  $\gamma = 0$  versus  $H_1$ :  $\gamma \neq 0$ . In this model,  $\gamma$  is the parameter L1  $\sim$  aSNP, which equals to 0.9445929 with the pvalue = 7.955090e-22.

#### > myAssoResult

```
Model
```

```
Basic properties of the model:
```

```
Model Class ...... strumFittedModel Ascertainment ..... FALSE
```

#### List of all variables:

```
Obs Covariate InEita
                                InY Exogen.
                         TRUE FALSE
                                       FALSE
L1
     FALSE
                FALSE
aSNP
      TRUE
                 TRUE
                       FALSE FALSE
                                          NA
P1
      TRUE
                FALSE
                       FALSE
                               TRUE
                                          NA
P2
      TRUE
                FALSE
                       FALSE
                               TRUE
                                          NA
РЗ
      TRUE
                FALSE
                       FALSE
                               TRUE
                                          NΑ
```

#### Model formulas:

```
L1 = ^{\sim} P1 + P2 + P3 + ^{\sim} L1 ^{\sim} aSNP + ^{\sim}P, e>
```

# =======

Result

#### Parameter estimates:

```
estimate
                           stdError
                                         lowerCI
                                                   upperCI
                                                                 pValue
L1=~P2
               0.9885029 0.05314867
                                     0.88433341 1.0926724 1.642115e-77
L1=~P3
               1.0105280 0.05822325
                                      0.89641252 1.1246435 8.869942e-68
L1~aSNP
               0.9445929 0.09913024
                                      0.75030117 1.1388846 7.955090e-22
P1~[intercept] 0.2880181 0.13404076
                                      0.02530298 0.5507331 1.582771e-02
P2~[intercept] 0.1829933 0.13133455
                                     -0.07441771 0.4404043 8.175896e-02
P3~[intercept] 0.3505190 0.12747443
                                     0.10067375 0.6003643 2.982307e-03
P1~~P1<e>
               1.1318519 0.18199793
                                     0.77514251 1.4885613 2.501075e-10
P2~~P2<e>
               1.2400615 0.14775629
                                     0.95046454 1.5296585 2.377245e-17
P3~~P3<e>
               0.6908993 0.19387808 0.31090526 1.0708934 1.829182e-04
```

L1~~L1 0.9445110 0.26947683 0.41634613 1.4726759 2.283205e-04 L1~~L1<e> 1.1478948 0.20752417 0.74115493 1.5546347 1.588615e-08

# Chi-square statistics of fit:

-		kappa	chiStat	df	pValue
Un-adjusted					0.99357480
Mean adjusted		0.2057025	13.397307	7	0.06299978
Mean-Variance	adjusted	0.1599908	17.225108	9	0.04530531
Theoretically	corrected	1.0000000	11.687927	7	0.11130000

# 2 Genetic linkage analysis

In this section, we show an example of a typical genetic linkage analysis model with a latent trait using IBD information. Suppose again that there are three measurements as above (P1, P2 and p3) and a single latent trait (L1) underlying the three measurements. The latent variable L1 is influenced by a set of genetic and random variance components. Each trait is also influenced by its own random environmental factor. The model diagram looks like following.

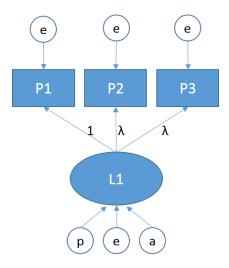


Figure 2: Genetic linkage analysis model

# 2.1 Construct model

The above linkage model can be construited as a strumModel object using createStrumModel() function.

```
Ascertainment ..... FALSE
List of all variables:
    Obs Covariate InEita
                          InY Exogen.
L1 FALSE
            FALSE
                    TRUE FALSE
                                FALSE
Ρ1
  TRUE
            FALSE FALSE
                                   NA
                        TRUE
   TRUE
P2
            FALSE FALSE
                         TRUE
                                   NA
   TRUE
Р3
            FALSE FALSE
                         TRUE
                                   NA
Model formulas:
 L1 = P1 + P2 + P3 + < e >
 L1 ~ <a,p,e>
```

# 2.2 Prepare data

From the above linkage analysis model, a represents the major gene variance components, which requires the ibd information to be imported. The ibd information for the family data can be imported by specifying the name of ibd file into ibdFileName argument for createStrumData(). The use of the example ibd file "GENIBD.chr1Ped.ibd", which contains the ibd information of family data in "chr1Ped.csv", is shown in the following code. We use the data.frame, dF, created for the previous association analysis model.

#### 2.3 Run analysis

Now, run the linkage analysis by the function call strum(). If you want to perform the linkage analysis on all markers exist in the IBD file, you don't need to specify the marker name as an argument for strum() function. In this case, each marker will be analysed one by one, and the result object will contain a list of the linkage analysis results for all markers.

```
> myLinkResultAll = strum(myLinkModel, myLinkData)
```

To analyze a subset of IBD markers, then you can specify the names of them as follows;

```
> mNames = c("chrimarker1", "chrimarker2")
> myLinkResult = strum(myLinkModel, myLinkData, ibdMarkers=mNames)
Start STRUM analysis ...
```

# chr1marker1: Fitting model step 1 ... Done Fitting model step 2 ... Done Testing model fit ... Done chr1marker2: Fitting model step 1 ... Done Fitting model step 2 ... Done Testing model fit ... Done

Analysis completed!

# 2.4 Result

The result object again contains the model description and result tables. The first table contains the fitted parameter values with standard errors, confidence intervals, and p-values. The second table contains the information on the model fit from four different measures. For linkage analysis, you would test  $H_0$ :  $\alpha = 0$  versus  $H_1$ :  $\alpha \neq 0$ . In this model,  $\alpha$  is the parameter L1  $\sim L1$ , which equals to 1.3114935 with the pvalue = 5.973887e-03.

```
> myLinkResult[[1]]
=======
 Model
=======
Basic properties of the model:
        Model Class ..... strumFittedModel
        Ascertainment ..... FALSE
List of all variables:
    Obs Covariate InEita
                          InY Exogen.
L1 FALSE
            FALSE
                   TRUE FALSE
                                FALSE
P1 TRUE
            FALSE FALSE TRUE
                                  NA
P2
   TRUE
            FALSE FALSE
                        TRUE
                                  NA
РЗ
  TRUE
            FALSE FALSE TRUE
                                  NA
Model formulas:
 L1 = P1 + P2 + P3 + <e>
 L1 ^{\sim} <a,p,e>
=======
 Result
=======
```

#### Parameter estimates:

```
lowerCI upperCI
               estimate stdError
                                                            pValue
L1=~P2
              0.8678695 0.07590839 0.7190918 1.016647 1.428314e-30
L1=~P3
              0.8910605 0.09321847 0.7083556 1.073765 5.954188e-22
P1~[intercept] 1.1238196 0.11825192 0.8920501 1.355589 1.013733e-21
P2~[intercept] 1.0432875 0.11808091 0.8118532 1.274722 4.988756e-19
P3~[intercept] 1.1673092 0.12331581 0.9256146 1.409004 1.453634e-21
P1~~P1<e>
              0.8799191 0.30659124 0.2790113 1.480827 2.052312e-03
P2~~P2<e>
              1.3934769 0.19780518 1.0057859 1.781168 9.293497e-13
P3~~P3<e>
              0.6745702 0.21172640 0.2595941 1.089546 7.211563e-04
L1~~L1
              1.3114935 0.52174178 0.2888984 2.334089 5.973887e-03
L1~~L1<e>
              1.4101136 0.35762894 0.7091738 2.111053 4.024244e-05
L1~~L1<a>
              0.2787365 0.43203390 -0.5680344 1.125507 2.594076e-01
```

#### Chi-square statistics of fit:

	kappa	chiStat	df	pValue
Un-adjusted	1.0000000	3.295630	10	0.9862138
Mean adjusted	0.4177845	7.888349	10	0.6397420
Mean-Variance adjusted	0.3481538	9.466019	12	0.6626947
Theoretically corrected	1.0000000	9.054915	10	0.5269000

# 3 Structural Equation Model

This is an example of a SEM model with latent variables and polygeneic effect. Suppose that there are six measurements and three underline latent variables, anger is a latent variable which underlies the two measurements (A1, A2), bp is a latent variable which underlies the two measurements (SBP, DBP) and stress is a latent variable which underlies the two measurements (S1, S2). bp is caused by anger and stress, and stress is caused by anger and a SNP (rs6040343). All traits and latent variables are also influenced by their own polygenic and random variance components except stress, which the variance is fixed at 0.1 for both polygenic and random componants. The model diagram looks like following.

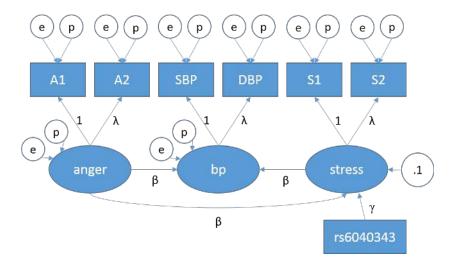


Figure 3: Structural equation model

# 3.1 Construct model

The above SEM model can be construited as a **strumModel** object using createStrumModel() function.

```
> semForm1 =
+ 'bp = SBP + DBP
+ anger = A1 + A2
+ stress = S1 + S2
+ bp anger + stress
+ stress anger + rs6040343
+ var(stress) = .1
+ '
> mySemModel = createStrumModel(formulas = semForm1)
```

```
Creating strumModel ..... Done
> mySemModel
Basic properties of the model:
        Model Class ..... strumModel
        Ascertainment ..... FALSE
List of all variables:
           Obs Covariate InEita
                                 InY Exogen.
         FALSE
                  FALSE
bp
                          TRUE FALSE
                                       FALSE
         FALSE
                  FALSE
                          TRUE FALSE
                                        TRUE
anger
         FALSE
                  FALSE
                          TRUE FALSE
                                       FALSE
stress
rs6040343 TRUE
                   TRUE FALSE FALSE
                                         NA
SBP
          TRUE
                  FALSE FALSE
                                TRUE
                                         NA
DBP
          TRUE
                  FALSE FALSE
                                TRUE
                                         NA
A1
          TRUE
                  FALSE FALSE
                                TRUE
                                         NA
A2
          TRUE
                  FALSE FALSE
                                TRUE
                                         NA
S1
          TRUE
                  FALSE FALSE
                                TRUE
                                         NA
S2
          TRUE.
                  FALSE FALSE TRUE
                                         NΑ
Model formulas:
 bp =~ SBP + DBP
 anger = ^{\sim} A1 + A2
 stress = S1 + S2
 bp ~ anger + stress
 stress ~ anger + rs6040343
 var(stress) = .1
```

# 3.2 Prepare data

The next step is to prepare data. Note again that the data must be a data.frame with 4 required fields - family, id, father, mother, since the model includes the polygenic variance component (p) by default. A **strumData** object is created by *createStrumData()* function with a data.frame. Again, we use the data.frame, dF, created above using the example input file "chr1Ped.csv".

```
family id father mother sex disease proband
                                                         P1
                                                                     P2
                                                                                 РЗ
                                                  0.4093955 0.44450079 -0.3867515
          1
                  0
                         0
                             0
                                      0
1
       1
2
       1
          2
                         0
                             1
                                      0
                                               0 -1.5037814 1.52582608
                                                                         0.8832360
3
                         2
       1
          3
                             0
                                      0
                                              0
                                                  1.5850090 0.08833692
                                                                         0.9322619
                  1
4
       1
          4
                  1
                         2
                             1
                                      0
                                                  1.6246356 0.60065352
                                                                         1.0895325
5
          5
                         2
                                      0
       1
                  1
                             1
                                               0 -0.4111477 0.08588345 -0.6477336
    SBP
            DBP
                     A1
                            A2
                                     S1
                                              S2 aSNP rs6040343
                  1.300
                         1.630
                                 1.9000 -0.0613
   3.39
        4.1800
                                                    1
                                                               1
2 -3.49 -2.7200 -0.784 -3.550 -2.8900 -2.1300
                                                    0
3 -3.40 0.0815 -1.820 -4.390 -1.6700 -3.0900
                                                    1
                                                              0
4 -7.04 -3.6500 -0.183 -4.740 -2.9800 -2.3500
                                                    0
                                                              0
   4.60 4.9900 2.440 -0.117 -0.0408 -0.4350
                                                    1
                                                               1
```

phi object contains 75 matrices:

First matrix:

```
$`1`
```

```
1 2 3 4 5 6 7
1 1.0 0.0 0.5 0.5 0.5 0.5 0.5
2 0.0 1.0 0.5 0.5 0.5 0.5 0.5
3 0.5 0.5 1.0 0.5 0.5 0.5 0.5
4 0.5 0.5 0.5 1.0 0.5 0.5 0.5
5 0.5 0.5 0.5 0.5 0.5 1.0 0.5 0.5
6 0.5 0.5 0.5 0.5 0.5 0.5 1.0 0.5
7 0.5 0.5 0.5 0.5 0.5 0.5 0.5 1.0
```

Empty IBD object.

## 3.3 Run analysis

Now, run the analysis by the function call strum() with two previously constructed objects as the arguments.

> mySemResult = strum(mySemModel, mySemData)

Analysis completed!

## 3.4 Result

The result object again contains the model description and result tables. To test the SNP effect to stress, you would test  $H_0$ :  $\gamma = 0$  versus  $H_1$ :  $\gamma \neq 0$ . In this model,  $\gamma$  is the parameter stress  $\sim$  rs6040343, which equals to 1.013427436 with the pvalue = 2.000891e-12.

# > mySemResult

=======

Model

=======

# Basic properties of the model:

Model Class ..... strumFittedModel Ascertainment ..... FALSE

# List of all variables:

Obs Covariate InEita InY Exogen. bp FALSE FALSE TRUE FALSE FALSE anger FALSE FALSE TRUE FALSE TRUE FALSE FALSE TRUE FALSE FALSE stress rs6040343 TRUE TRUE FALSE FALSE TRUE FALSE FALSE TRUE SBP NADBP TRUE FALSE FALSE TRUE NAA1 TRUE FALSE FALSE TRUE NAA2 TRUE FALSE FALSE TRUE NAS1 TRUE FALSE FALSE TRUE NAS2 TRUE FALSE FALSE TRUE NA

# Model formulas:

bp = SBP + DBP
anger = A1 + A2
stress = S1 + S2
bp anger + stress
stress anger + rs6040343
var(stress) = .1

=======

Result

========

## Parameter estimates:

	estimate	${ t stdError}$	lowerCI	upperCI	pValue
bp=~DBP	1.035032181	0.04257460	0.95158750	1.1184769	7.494250e-131
anger=~A2	1.003172952	0.08028815	0.84581106	1.1605348	3.991982e-36
stress=~S2	1.055164010	0.08278765	0.89290320	1.2174248	1.652860e-37
bp~anger	0.823477032	0.19646223	0.43841813	1.2085359	1.385408e-05
stress~anger	0.942564976	0.07702239	0.79160386	1.0935261	9.793374e-35
bp~stress	1.052862536	0.16355422	0.73230215	1.3734229	6.077212e-11
${\tt stress\~rs}6040343$	1.013427436	0.14608766	0.72710087	1.2997540	2.000891e-12
<pre>SBP~[intercept]</pre>	-0.117910325	0.30223817	-0.71028625	0.4744656	3.482225e-01

```
DBP<sup>*</sup>[intercept] -0.302734413 0.30931966 -0.90898981 0.3035210 1.638615e-01
A1~[intercept]
                 0.018375752 0.22433007 -0.42130310 0.4580546 4.673576e-01
A2~[intercept] -0.030596742 0.21819352 -0.45824819 0.3970547 4.442401e-01
S1~[intercept]
                 0.118914923 0.21176180 -0.29613058 0.5339604 2.872112e-01
S2~[intercept]
                 0.009989653 0.19519661 -0.37258867 0.3925680 4.795921e-01
SBP~~SBP
                 0.477083708 0.51395234 -0.53024436 1.4844118 1.766352e-01
DBP~~DBP
                 1.345743296 0.60224112 0.16537238 2.5261142 1.272316e-02
                 1.133010959 0.32774658 0.49063946 1.7753825 2.731402e-04
A1~~A1
                 0.807655100 0.38678524 0.04956996 1.5657402 1.839338e-02
A2~~A2
S1~~S1
                 1.097210966 0.39553172 0.32198304 1.8724389 2.768455e-03
S2~~S2
                 0.680742260 0.35435561 -0.01378198 1.3752665 2.736138e-02
SBP~~SBP<e>
                 1.259787424 0.30649356 0.65907108 1.8605038 1.975534e-05
DBP~~DBP<e>
                 0.624278077 \ 0.36314414 \ -0.08747135 \ 1.3360275 \ \ 4.279884e-02
                 0.702376222 0.20543107 0.29973873 1.1050137 3.142170e-04
A1~~A1<e>
A2~~A2<e>
                1.225357642 0.27516889 0.68603653 1.7646788 4.231747e-06
S1~~S1<e>
                1.273773004 0.25233960 0.77919648 1.7683495 2.234023e-07
S2~~S2<e>
                1.234330774 0.25197404 0.74047073 1.7281908 4.825049e-07
bp~~bp
                 0.586876864 0.60011805 -0.58933290 1.7630866 1.640531e-01
                 1.154779475 0.25292433 0.65905691 1.6505020 2.489016e-06
anger~~anger
                 1.078347705 0.40995946 0.27484193 1.8818535 4.264518e-03
bp~~bp<e>
anger~~anger<e>
                 0.886146282 0.19375800 0.50638758 1.2659050 2.398569e-06
```

# Chi-square statistics of fit:

kappa chiStat df pValue Un-adjusted 1.0000000 7.407714 25 0.9999831 Mean adjusted 0.5440739 13.615273 25 0.9680314 Mean-Variance adjusted 0.4857802 15.249105 28 0.9756850 Theoretically corrected 1.0000000 18.067778 25 0.8395000

# 4 SessionInfo

```
> sessionInfo();
R version 3.0.2 (2013-09-25)
Platform: x86_64-w64-mingw32/x64 (64-bit)
locale:
[1] LC_COLLATE=English_United States.1252
[2] LC_CTYPE=English_United States.1252
[3] LC_MONETARY=English_United States.1252
[4] LC_NUMERIC=C
[5] LC_TIME=English_United States.1252
attached base packages:
[1] grid
              stats
                       graphics grDevices utils
                                                     datasets methods
[8] base
other attached packages:
[1] strum_0.4
                   Rgraphviz_2.6.0 graph_1.40.0
                                                   pedigree_1.4
[5] reshape_0.8.4
                   plyr_1.8
                                   HaploSim_1.8.4 Matrix_1.1-0
loaded via a namespace (and not attached):
[1] BiocGenerics_0.8.0 lattice_0.20-24 MASS_7.3-29
                                                            parallel_3.0.2
[5] Rcpp_0.11.2
                     stats4_3.0.2
                                         tools_3.0.2
```

# References

Morris, N.J., Elston, R.C., & Stein, C.M. (2010). A framework for structural equation models in general pedigrees. *Human heredity*, 70, 278–286.