Package 'sumFREGAT'

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Title Fast Region-Based Association Tests on Summary Statistics Version 1.0.0
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Description An adaptation of classical region/gene-based association analysis techniques that uses summary statistics (P values and effect sizes) and correlations between genetic variants as input. It is a tool to perform the most common and efficient gene-based tests on the results of genome-wide association (meta-)analyses without having the original genotypes and phenotypes at hand.
License GPL-3
LazyLoad yes
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BT

sumFREGAT-package sumFREGAT: Fast REGional Association Tests on summary statistics

Description

The sumFREGAT package computes the most common and efficient tests for the region-based association analysis on summary statistics data (beta and p values) and correlations between genetic variants. It does not require genotype or phenotype data. Methods implemented are SKAT and SKAT-O (sequence kernel association tests), BT (burden test), FLM (functional linear model), PCA (principal components analysis), and MLR (multiple linear regression).

Details

Package: sumFREGAT

Type: Package License: GPLv3

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ВТ

Family Burden Test

Description

Burden test on summary statistics

Usage

```
BT(scoreFile, geneFile, regions, cor.path = "", annoType = "", beta.par = c(1, 25), weights.function = ifelse(maf > 0, dbeta(maf, beta.par[1], beta.par[2]), 0), write.file = FALSE)
```

Arguments

scoreFile	name of data file generated by prep.score.files().
geneFile	name of a text file listing genes in refFlat format. If not set, hg19 file will be used (see Examples below).
regions	character vector of gene names to be analysed. If not set, function will attempt to analyse all genes listed in geneFile.

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cor.path path to a folder with correlation files (one file per each gene to be analysed). Names of correlation files should be constructed as "geneName.cor" (e.g. "ABCG1.cor", "ADAMTS1.cor", etc.) Each file should contain a square matrix with correlation coefficients (r) between genetic variants of a gene. An example of correlation file format: "snpname1" "snpname2" "snpname3" ... "snpname1" 1 0.018 -0.003 ... "snpname2" 0.018 1 0.081 ... "snpname3" -0.003 0.081 1 ... One way to generate such file from original genotypes is: write.table(cor(g), file = paste0(geneName, ".cor")) where q is a genotype matrix (nsample x nvariants) for a given gene with genotypes coded as 0, 1, 2 (exactly the same coding that was used to generate betas). for files annotated with the segminer package, a character (or character vecannoType tor) indicating annotation types to be used (e.g. "Nonsynonymous", "Start_Loss", "Stop_loss", "Essential_Splice_Site") beta.par two positive numeric shape parameters in the beta distribution to assign weights for each genetic variant as a function of MAF in the default weights function (see Details). Default = c(1, 25). weights.function a function of minor allele frequency (MAF) to assign weights for each genetic variant. By default, the weights will be calculated using the beta distribution (see Details).

Details

write.file

Burden test (collapsing technique) suggests that the effects of causal genetic variants within a region have the same direction. If this is not the case, other regional tests (SKAT and FLM) are shown to have higher power compared to burden test [Svishcheva, et al., 2015].

output file name. If specified, output (as it proceeds) will be written to the file.

By default, BT assigns weights calculated using the beta distribution. Given the shape parameters of the beta function, beta.par = c(a, b), the weights are defined using probability density function of the beta distribution:

$$W_i = (B(a,b))^{-1} MAF_i^{a-1} (1 - MAF_i)^{b-1},$$

where MAF_i is a minor allelic frequency for the i^{th} genetic variant in region, which is estimated from genotypes, and B(a,b) is the beta function.

beta.par = c(1, 1) corresponds to the unweighted burden test.

Value

A data frame containing P values, estimates of betas and their s.e., numbers of variants and filtered variants for each of analyzed regions.

References

Svishcheva G.R., Belonogova N.M. and Axenovich T.I. (2015) Region-based association test for familial data under functional linear models. PLoS ONE 10(6): e0128999.

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Examples

```
## Run BT with example files:
VCFfileName <- system.file("testfiles/CFH.scores.anno.vcf.gz",
package = "sumFREGAT")
cor.path <- system.file("testfiles/", package = "sumFREGAT")
out <- BT(VCFfileName, region = 'CFH', cor.path = cor.path)</pre>
```

FLM

Functional Linear Model

Description

A region-based association test on summary statistics under functional linear models (functional data analysis approach)

Usage

```
FLM(scoreFile, geneFile, regions, cor.path = "", annoType = "",
n, beta.par = c(1, 1), weights.function = ifelse(maf > 0,
dbeta(maf, beta.par[1], beta.par[2]), 0), GVF = FALSE,
BSF = "fourier", kg = 30, kb = 25, order = 4, flip.genotypes = FALSE,
Fan = TRUE, write.file = FALSE)
```

Arguments

scoreFile	name of data file generated by prep.score.files().
geneFile	name of a text file listing genes in refFlat format. If not set, hg19 file will be used (see Examples below).
regions	character vector of gene names to be analysed. If not set, function will attempt to analyse all genes listed in geneFile.
cor.path	path to a folder with correlation files (one file per each gene to be analysed). Names of correlation files should be constructed as "geneName.cor" (e.g. "ABCG1.cor", "ADAMTS1.cor", etc.) Each file should contain a square matrix with correlation coefficients (r) between genetic variants of a gene. An example of correlation file format: "snpname1" "snpname2" "snpname3" "snpname1" 1 0.018 -0.003 "snpname2" 0.018 1 0.081 "snpname3" -0.003 0.081 1
	One way to generate such file from original genotypes is: write.table(cor(g), file = paste0(geneName, ".cor")) where g is a genotype matrix (nsample x nvariants) for a given gene with genotypes coded as 0, 1, 2 (exactly the same coding that was used to generate betas).
annoType	for files annotated with the seqminer package, a character (or character vector) indicating annotation types to be used (e.g. "Nonsynonymous", "Start_Loss", "Stop_loss", "Essential_Splice_Site")
n	size of the sample on which summary statitics were obtained.

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beta.par two positive numeric shape parameters in the beta distribution to assign weights for each genetic variant as a function of MAF in the default weights function (see Details). Default = c(1, 1) corresponds to standard unweighted FLM.

weights.function

GVF

a function of minor allele frequency (MAF) to assign weights for each genetic variant. By default, the weights will be calculated using the beta distribution (see Details).

a basis function type for Genetic Variant Functions. Can be set to "bspline" (B-

spline basis) or "fourier" (Fourier basis). The default GVF = FALSE assumes

beta-smooth only. If GVF = TRUE the B-spline basis will be used.

a basis function type for beta-smooth. Can be set to "bspline" (B-spline basis) BSF

or "fourier" (Fourier basis, default).

the number of basis functions to be used for GVF (default = 30, has no effect kg

under GVF = FALSE).

the number of basis functions to be used for BSF (default = 25). kb

a polynomial order to be used in "bspline". Default = 4 corresponds to the cubic order

B-splines. as no effect if only Fourier bases are used.

flip.genotypes

a logical value indicating whether the genotypes of some genetic variants should be flipped (relabeled) for their better functional representation [Vsevolozhskaya,

et al., 2014]. Default = FALSE.

if TRUE (default) then linearly dependent genetic variants will be omitted, as it Fan

was done in the original realization of FLM test by Fan et al. (2013).

write.file output file name. If specified, output (as it proceeds) will be written to the file.

Details

The test assumes that the effects of multiple genetic variants (and also their genotypes if GVFs are used) can be described as a continuous function, which can be modelled through B-spline or Fourier basis functions. When the number of basis functions (set by Kq and Kb) is less than the number of variants within the region, the famFLM test may have an advantage of using less degrees of freedom [Svishcheva, et al., 2015].

Several restrictions exist in combining B-spline or Fourier bases for construction of GVFs and BSF [Svishcheva, et al., 2015], and the famFLM function takes them into account. Namely:

- 1) $m \ge Kg \ge Kb$, where m is the number of polymorphic genetic variants within a region.
- 2) Under Kg = Kb, B-B and B-F models are equivalent to 0-B model, and F-F and F-B models are equivalent to 0-F model. 0-B and 0-F models will be used for these cases, respectively.
- 3) Under m = Kb, 0-B and 0-F models are equivalent to a standard multiple linear regression, and it will be used for these cases.
- 4) When Fourier basis is used, the number of basis functions should be an odd integer. Even values will be changed accordingly.

Because of these restrictions, the model in effect may not always be the same as it has been set. The ultimate model name is returned in results in the "model" column (see below).

6 MLR

beta.par = c(a, b) can be used to set weights for genetic variants. Given the shape parameters of the beta function, beta.par = c(a, b), the weights are defined using probability density function of the beta distribution:

$$W_i = (B(a,b))^{-1} MAF_i^{a-1} (1 - MAF_i)^{b-1},$$

where MAF_i is a minor allelic frequency for the i^{th} genetic variant in the region, which is estimated from genotypes, and B(a,b) is the beta function. This way of defining weights is the same as in original SKAT (see [Wu, et al., 2011] for details).

Value

A data frame containing P values, numbers of variants and filtered variants for each of analyzed regions. It also contains the names of the functional models used for each region (it may not always coincide with what was set, because of restrictions described in Details section). The first part of the name relates to the functional basis of GVFs and the second one to that of BSF, e.g. "F30-B25" means that 30 Fourier basis functions were used for construction of GVFs and 25 B-spline basis functions were used for construction of BSF. "0-F25" means that genotypes were not smoothed and 25 Fourier basis functions were used for beta-smooth. "MLR" means that standard multiple linear regression was applied.

References

Svishcheva G.R., Belonogova N.M. and Axenovich T.I. (2015) Region-based association test for familial data under functional linear models. PLoS ONE 10(6): e0128999.

Vsevolozhskaya O.A., et al. (2014) Functional Analysis of Variance for Association Studies. PLoS ONE 9(9): e105074.

Wu M.C., et al. (2011) Rare-variant association testing for sequencing data with the sequence kernel association test. Am. J. Hum. Genet., Vol. 89, P. 82-93.

Fan R, Wang Y, Mills JL, Wilson AF, Bailey-Wilson JE, et al. (2013) Functional linear models for association analysis of quantitative traits. Genet Epidemiol 37: 726-42.

Examples

```
## Run FLM with example files:
VCFfileName <- system.file("testfiles/CFH.scores.anno.vcf.gz",
package = "sumFREGAT")
cor.path <- system.file("testfiles/", package = "sumFREGAT")
n <- 85 # your sample size
out <- FLM(VCFfileName, region = 'CFH', cor.path = cor.path, n = n)</pre>
```

MLR

Multiple Linear Regression

Description

Multiple linear regression approach on summary statistics

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Usage

```
MLR(scoreFile, geneFile, regions, cor.path = "", annoType = "",
n, write.file = FALSE)
```

Arguments

scoreFile	name of data file generated by prep.score.files().
geneFile	name of a text file listing genes in refFlat format. If not set, hg19 file will be used (see Examples below).
regions	character vector of gene names to be analysed. If not set, function will attempt to analyse all genes listed in geneFile.
cor.path	path to a folder with correlation files (one file per each gene to be analysed). Names of correlation files should be constructed as "geneName.cor" (e.g. "ABCG1.cor", "ADAMTS1.cor", etc.) Each file should contain a square matrix with correlation coefficients (r) between genetic variants of a gene. An example of correlation file format: "snpname1" "snpname2" "snpname3" "snpname1" 1 0.018 -0.003 "snpname2" 0.018 1 0.081 "snpname3" -0.003 0.081 1
	One way to generate such file from original genotypes is: write.table(cor(g), file = paste0(geneName, ".cor")) where g is a genotype matrix (nsample x nvariants) for a given gene with genotypes coded as 0, 1, 2 (exactly the same coding that was used to generate betas).
annoType	for files annotated with the seqminer package, a character (or character vector) indicating annotation types to be used (e.g. "Nonsynonymous", "Start_Loss", "Stop_loss", "Essential_Splice_Site")
n	size of the sample on which summary statitics were obtained.
write.file	output file name to write results as they come (sequential mode only).
• • •	<pre>other arguments that could be passed to null(), read.plink() and readVCFToMatrixByGene().</pre>

Value

A data frame containing P values, numbers of variants and filtered variants for each of analyzed regions.

Examples

```
## Run MLR with example files:
VCFfileName <- system.file("testfiles/CFH.scores.anno.vcf.gz",
package = "sumFREGAT")
cor.path <- system.file("testfiles/", package = "sumFREGAT")
n <- 85 # your sample size
out <- MLR(VCFfileName, region = 'CFH', cor.path = cor.path, n = n)</pre>
```

PCA

PCA

Principal Components Analysis

Description

Test for association between a trait and principal components of genotypes within a region, on summary statistics

Usage

```
PCA(scoreFile, geneFile, regions, cor.path = "", annoType = "",
n, beta.par = c(1, 1), weights.function = ifelse(maf > 0,
dbeta(maf, beta.par[1], beta.par[2]), 0), var.fraction = .85,
write.file = FALSE)
```

Arguments

	scoreFile	name of data file generated by prep.score.files().
	geneFile	name of a text file listing genes in refFlat format. If not set, hg19 file will be used (see Examples below).
	regions	character vector of gene names to be analysed. If not set, function will attempt to analyse all genes listed in geneFile.
	cor.path	path to a folder with correlation files (one file per each gene to be analysed). Names of correlation files should be constructed as "geneName.cor" (e.g. "ABCG1.cor", "ADAMTS1.cor", etc.) Each file should contain a square matrix with correlation coefficients (r) between genetic variants of a gene. An example of correlation file format: "snpname1" "snpname2" "snpname3" "snpname1" 1 0.018 -0.003 "snpname2" 0.018 1 0.081 "snpname3" -0.003 0.081 1 One way to generate such file from original genotypes is: write.table(cor(g), file = paste0(geneName, ".cor"))
		where g is a genotype matrix (nsample x nvariants) for a given gene with genotypes coded as 0, 1, 2 (exactly the same coding that was used to generate betas).
	annoType	for files annotated with the seqminer package, a character (or character vector) indicating annotation types to be used (e.g. "Nonsynonymous", "Start_Loss", "Stop_loss", "Essential_Splice_Site")
	n	size of the sample on which summary statitics were obtained.
	beta.par	two positive numeric shape parameters in the beta distribution to assign weights for each genetic variant as a function of MAF in the default weights function (see Details). Default = $c(1, 1)$.
weights.function		
		a function of minor allele frequency (MAF) to assign weights for each genetic variant. By default, the weights will be calculated using the beta distribution (see Details).
	var.fraction	minimal proportion of genetic variance within region that should be explained by principal components used (see Details for more info).
	write.file	output file name. If specified, output (as it proceeds) will be written to the file.

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Details

PCA test is a useful tool to detect association between genetic variants of a region and a trait when genetic variants are strongly correlated. PCA test is based on the spectral decomposition of correlation matrix among genetic variants. The number of top principal components will be chosen in such a way that >= var.fraction of region variance can be explained by these PCs. By default, var.fraction = 0.85, i.e. >= 85% of region variance will be explained by PCs. If var.fraction = 1 then the results of PCA test and MLR-based test are identical.

beta.par = c(a, b) can be used to set weights for genetic variants. Given the shape parameters of the beta function, beta.par = c(a, b), the weights are defined using probability density function of the beta distribution:

$$W_i = (B(a,b))^{-1} MAF_i^{a-1} (1 - MAF_i)^{b-1},$$

where MAF_i is a minor allelic frequency for the i^{th} genetic variant in the region, which is estimated from genotypes, and B(a,b) is the beta function. This way of defining weights is the same as in original SKAT (see [Wu, et al., 2011] for details).

Precision of input values (betas and P) can be important for perfect correspondence between PCA on summary statistics and PCA performed on genotypes. We suggest to keep as much decimal points as possible for input values.

Value

a data frame containing P values, numbers of variants and filtered variants for each of analyzed regions. It also contains the number of the principal components used for each region and the proportion of genetic variance they make up.

References

Jolliffe, I.T. A note on the use of principal components in regression. J R Stat Soc Ser C 31, 300-303 (1982).

Examples

```
## Run PCA with example files:
VCFfileName <- system.file("testfiles/CFH.scores.anno.vcf.gz",
package = "sumFREGAT")
cor.path <- system.file("testfiles/", package = "sumFREGAT")
n <- 85 # your sample size
out <- PCA(VCFfileName, region = 'CFH', cor.path = cor.path, n = n)</pre>
```

```
prep.score.files Prepare score files
```

Description

Calculates Z scores from P values and beta input

Usage

```
prep.score.files(input.file, output.file.prefix)
```

Arguments

input.file a file with the following columns:

"CHROM": chromosome

"POS": positions

"ID": names of genetic variants, same as in files with genetic correlations

"REF": reference allele
"ALT": alternative allele

"P": p value

"BETA": effect size (betas and genetic correlations should be calculated for the

same genotype coding)

"EAF": effect allele freequency

For example:

```
CHROM POS ID REF ALT pvalue beta EAF
```

1 196632134 1:196632134 C T 0.80675 0.22946 0.00588 1 196632386 1:196632386 G A 0.48694 0.65208 0.00588 1 196632470 1:196632470 A G 0.25594 -0.19280 0.19412

Avoid rounding of betas and pvalues as this can affect the precision of regional tests

output.file.prefix

if not set, the input file name will be used as output prefix.

Value

does not return any value, writes output files with Z scores to be used in any type of gene-based analysis: SKAT(), BT(), MLR(), FLM(), PCA().

Examples

```
input.file <- system.file("testfiles/CFH.pvalues.dat",
package = "sumFREGAT")
prep.score.files(input.file, "CFH.scores")</pre>
```

SKAT

Sequence kernel association test

Description

Sequence kernel association tests (SKAT and SKAT-O) on summary statistics

Usage

```
SKAT(scoreFile, geneFile, regions, cor.path = "", annoType = "", beta.par = c(1, 25), weights.function = ifelse(maf > 0, dbeta(maf, beta.par[1], beta.par[2]), 0), method = "kuonen", acc = 1e-8, lim = 1e+6, rho = FALSE, write.file = FALSE)
```

Arguments

	scoreFile	name of data file generated by prep.score.files().
	geneFile	name of a text file listing genes in refFlat format. If not set, hg19 file will be used (see Examples below).
	regions	character vector of gene names to be analysed. If not set, function will attempt to analyse all genes listed in geneFile.
	cor.path	path to a folder with correlation files (one file per each gene to be analysed). Names of correlation files should be constructed as "geneName.cor" (e.g. "ABCG1.cor", "ADAMTS1.cor", etc.) Each file should contain a square matrix with correlation coefficients (r) between genetic variants of a gene. An example of correlation file format: "snpname1" "snpname2" "snpname3" "snpname1" 1 0.018 -0.003 "snpname2" 0.018 1 0.081 "snpname3" -0.003 0.081 1
		One way to generate such file from original genotypes is: write.table(cor(g), file = paste0(geneName, ".cor")) where g is a genotype matrix (nsample x nvariants) for a given gene with genotypes coded as 0, 1, 2 (exactly the same coding that was used to generate betas).
	annoType	for files annotated with the seqminer package, a character (or character vector) indicating annotation types to be used (e.g. "Nonsynonymous", "Start_Loss", "Stop_loss", "Essential_Splice_Site")
	beta.par	two positive numeric shape parameters in the beta distribution to assign weights for each genetic variant as a function of MAF in the default weights function (see Details). Default = $c(1, 25)$.
weights.function		
		a function of minor allele frequency (MAF) to assign weights for each genetic variant. By default, the weights will be calculated using the beta distribution (see Details).
	method	the method for computing P value. Available methods are "kuonen", "davies" and "hybrid" (see Details). Default = "kuonen".
	acc	accuracy parameter for "davies" method.
	lim	limit parameter for "davies" method.
	rho	If TRUE the optimal test (SKAT-O) is performed [Lee, et al., 2012]. rho can be a vector of grid values from 0 to 1. The default grid is $c(0, 0.1^2, 0.2^2, 0.3^2, 0.4^2, 0.5^2, 0.5, 1)$.
	write.file	output file name. If specified, output (as it proceeds) will be written to the file.

Details

SKAT uses the linear weighted kernel function to set the inter-individual similarity matrix $K=GWWG^T$ for SKAT and $K=GW(I\rho+(1-\rho)ee^T)WG^T$ for SKAT-O, where G is the $n\times p$

genotype matrix for n individuals and p genetic variants in the region, W is the $p \times p$ diagonal weight matrix, I is the $p \times p$ identity matrix, ρ is pairwise correlation coefficient between genetic effects (which will be adaptively selected from given rho), and e is the $p \times 1$ vector of ones. Given the shape parameters of the beta function, beta.par = c(a, b), the weights are defined using probability density function of the beta distribution:

$$W_i = (B(a,b))^{-1} MAF_i^{a-1} (1 - MAF_i)^{b-1},$$

where MAF_i is a minor allelic frequency for the i^{th} genetic variant in the region, which is estimated from genotypes, and B(a,b) is the beta function. This way of defining weights is the same as in original SKAT (see [Wu, et al., 2011] for details). beta.par = c(1, 1) corresponds to the unweighted SKAT. Depending on the method option chosen, either Kuonen or Davies method is used to calculate P values from the score statistics. Both an Applied Statistics algorithm that inverts the characteristic function of the mixture chisq [Davies, 1980] and a saddlepoint approximation [Kuonen, 1999] are nearly exact, with the latter usually being a bit faster. A hybrid approach was recently proposed by Wu et al. [2016]. It uses the Davies' method with high accuracy, and then switches to the saddlepoint approximation method when the Davies' method fails to converge. This approach yields more accurate results in terms of type I errors, especially for small significance levels. However, 'hybrid' method runs several times slower than the saddlepoint approximation method itself (i.e. 'kuonen' method). We therefore recommend using the hybrid approach only for those regions that show significant (or nearly significant) P values to ensure their accuracy.

Value

A list with values:

results	a data frame containing P values, numbers of variants and polymorphic variants
	for each of analyzed regions.

If return.variance.explained = TRUE it contains also the column with marginal amounts of variance explained by each region. If reml = FALSE the new estimates of heritability (h2) and total variance with corresponding total

log-likelihood are also returned.

nullmod an object containing the estimates of the null model parameters: heritability

(h2), total variance (total.var), estimates of fixed effects of covariates (alpha),

the gradient (df), and the total log-likelihood (logLH).

sample.size the sample size after omitting NAs.

time If return.time = TRUE a list with running times for null model, regional

analysis and total analysis is returned. See ${\tt proc.time}$ () for output format.

References

Davies R.B. (1980) Algorithm AS 155: The Distribution of a Linear Combination of chi-2 Random Variables, Journal of the Royal Statistical Society. Series C (Applied Statistics), Vol. 29, N 3, P. 323-333.

Kuonen D. (1999) Saddlepoint Approximations for Distributions of Quadratic Forms in Normal Variables. Biometrika, Vol. 86, No. 4, P. 929-935.

Wu M.C., et al. (2011) Rare-variant association testing for sequencing data with the sequence kernel association test. Am. J. Hum. Genet., Vol. 89, P. 82-93.

Lee S., et al. (2012) Optimal unified approach for rare variant association testing with application to small sample case-control whole-exome sequencing studies. American Journal of Human Genetics, 91, 224-237.

Wu B., et al. (2016) On efficient and accurate calculation of significance p-values for sequence kernel association testing of variant set. Ann Hum Genet, 80(2): 123-135.

Examples

```
## Run SKAT with example files:
VCFfileName <- system.file("testfiles/CFH.scores.anno.vcf.gz",
package = "sumFREGAT")
cor.path <- system.file("testfiles/", package = "sumFREGAT")
out <- SKAT(VCFfileName, region = 'CFH', cor.path = cor.path)</pre>
```

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