an \Re^{m_X} dimensional unit cube. This makes it easier to construct prior distributions for the width parameters to the correlation function $K(\cdot,\cdot)$. Proposals for all parameters which require MH sampling are taken from a uniform "sliding window" centered around the location of the last accepted setting. For example, a proposed a new nugget parameter g_{ν} to the correlation function $K(\cdot,\cdot)$ in region r_{ν} would go as

 $g_{\nu}^* \sim \text{Unif}\left(\frac{3}{4}g_{\nu}, \frac{4}{3}g_{\nu}\right).$

Calculating the corresponding forward and backwards proposal probabilities for the MH acceptance ratio is straightforward.

B Interfaces and features

The following subsections describe some of the ancillary features of the tgp package such as the gathering and summarizing of MCMC parameter traces, the progress meter, and an example of how to use the predict.tgp function in a collaborative setting.

B.1 Parameter traces

Traces of (almost) all parameters to the tgp model can be collected by supplying trace=TRUE to the b* functions. In the current version traces for the linear prior correlation matrix (**W**) are not provided. I shall illustrate the gathering and analyzing of traces through example. But first, a few notes and cautions.

Models which involve treed partitioning may have more than one base model (GP or LM). The process governing a particular input **x** depends on the coordinates of **x**. As such, tgp records region—specific traces of parameters to GP (and linear) models at the locations enumerated in the XX argument. Even traces of single—parameter Markov chains can require hefty amounts of storage, so recording traces at each of the XX locations can be an enormous memory hog. A related warning will be given if the product of |XX|, (BTE[2]-BTE[1])/BTE[3] and R is beyond a threshold. The easiest way to keep the storage requirements for traces down is to control the size of XX and the thinning level BTE[3]. Finally, traces for most of the parameters are stored in output files. The contents of the trace files are read into R and stored as data.frame objects, and the files are removed. The existence of partially written trace files in the current working directory (CWD)—while the C code is executing—means that not more than one tgp run (with trace = TRUE) should be active in the CWD at one time.

Consider again the exponential data. For illustrative purposes I chose XX locations (where traces are gathered) to be (1) in the interior of the interesting region, (2) on/near the plausible intersection of partition boundaries, and (3) in the interior of the flat region. The hierarchical prior bprior = "b0" is used to leverage a (prior) belief the most of the input domain is uninteresting.

```
> exp2d.data <- exp2d.rand(n2 = 150, lh = 0, dopt = 10)
> X <- exp2d.data$X</pre>
```

```
> Z <- exp2d.data$Z
> XX <- rbind(c(0, 0), c(2, 2), c(4, 4))
```

We now fit a treed GP LLM and gather traces, and also gather EI and ALC statistics for the purposes of illustration. Prediction at the input locations ${\tt X}$ is turned off to be thrifty.

Figure 18 shows a dump of out\$trace which is a "tgptraces"-class object. It depicts the full set of parameter traces broken down into the elements of a list: \$XX with GP/LLM parameter traces for each XX location (the parameters are listed); \$hier with traces for (non-input-dependent) hierarchical parameters (listed); \$linarea recording proportions of the input space under the LLM; \$parts with the boundaries of all partitions visited; \$post containing (log) posterior probabilities; preds containing traces of samples from the posterior predictive distribution and adaptive sampling statistics.

Plots of traces are useful for assessing the mixing of the Markov chain. For example, Figure 19 plots traces of the range parameter (d) for each of the 3 predictive locations XX. It is easy to see which of the locations is in the same partition with others, and which have smaller range parameters than others.

The mean area under the LLM can be calculated as

```
> linarea <- mean(out$trace$linarea$la)
> linarea
[1] 0.530641
```

This means that the expected proportion of the input domain under the full LLM is 0.531. Figure 20 shows a histogram of areas under the LLM. The clumps near 0, 0.25, 0.5, and 0.75 can be thought of as representing quadrants (none, one, two, and tree) under the LLM. Similarly, we can calculate the probability that each of the XX locations is governed by the LLM.

> out\$trace

This 'tgptraces'-class object contains traces of the parameters to a tgp model. Access is as a list:

 \$XX contains the traces of GP parameters for 3 predictive locations

Each of XX[[1]] ... XX[[3]] is a data frame with the columns representing GP parameters:

- [1] index lambda s2 tau2 beta0 beta1 beta2 nug
- [9] d b ldetK
- 2.) \$hier has a trace of the hierarchical params:
- [1] s2.a0 s2.g0 tau2.a0 tau2.g0 beta0 beta1 beta2
- [15] nug.g1
- 3.) \$linarea has a trace of areas under the LLM. It is a data frame with columns:

count: number of booleans b=0, indicating LLM

la: area of domain under LLM

ba: area of domain under LLM weighed by dim

- 4.) \$parts contains all of the partitions visited. Use the tgp.plot.parts.[1d,2d] functions for visuals
- 5.) \$post is a data frame with columns showing the following: log posterior (\$lpost), tree height (\$height), IS weights (\$w), tempered log posterior (\$tlpost), inv-temp (\$itemp), and weights adjusted for ESS (\$wess)
- 6.) \$preds is a list containing data.frames for samples from the posterior predictive distributions data (X) locations (if pred.n=TRUE: \$Zp, \$Zp.km, \$Zp.ks2) and (XX) locations (if XX != NULL: \$ZZ, \$ZZ.km, \$ZZ.ks2), with \$Ds2x when input argument ds2x=TRUE, and \$improv when improv=TRUE

Figure 18: Listing the contents of "tgptraces"-class objects.

```
> trXX <- out$trace$XX
> ltrXX <- length(trXX)
> y <- trXX[[1]]$d
> for (i in 2:ltrXX) y <- c(y, trXX[[i]]$d)
> plot(log(trXX[[1]]$d), type = "l", ylim = range(log(y)),
+     ylab = "log(d)", main = "range (d) parameter traces")
> names <- "XX[1,]"
> for (i in 2:ltrXX) {
+     lines(log(trXX[[i]]$d), col = i, lty = i)
+     names <- c(names, paste("XX[", i, ",]", sep = ""))
+ }
> legend("bottomleft", names, col = 1:ltrXX, lty = 1:ltrXX)
```

range (d) parameter traces

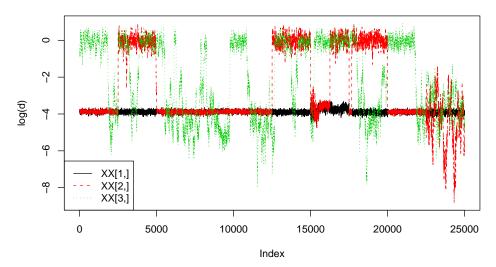


Figure 19: Traces of the (log of the) first range parameter for each of the three XX locations

The final column above represents the probability that the corresponding XX location is under the LLM (which is equal to 1-b).

Traces of posterior predictive and adaptive sampling statistics are contained in the \$preds field. For example, Figure 21 shows samples of the ALC statistic $\Delta\sigma^2(\tilde{\mathbf{x}})$. We can see from the trace that statistic is generally lowest for XX[3,] which is in the uninteresting region, and that there is some competition between XX[2,] which lies on the boundary between the regions, and XX[1,] which is in the interior of the interesting region. Similar plots can be made for the other adaptive sampling statistics (i.e., ALM & EI).

> hist(out\$trace\$linarea\$la)

Histogram of out\$trace\$linarea\$la

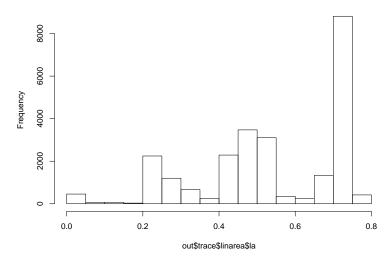


Figure 20: Histogram of proportions of the area of the input domain under the LLM

B.2 Explaining the progress meter

The progress meter shows the progress of the MCMC as it iterates through the desired number of rounds of burn-in (BTE[1]), and sampling (BTE[2]-BTE[1]), for the requested number of repeats (R). The verbosity of progress meter print statements is controlled by the verb arguments to the b* functions. Providing verb=0 silences all non-warning (or error) statements. To suppress warnings, try enclosing commands within suppressWarnings(...), or globally set options(warn=0). See the help file (?options) for more global warning settings.

The default verbosity setting (verb=1) shows all grows and prunes, and a summary of d–(range) parameters for each partition every 1000 rounds. Higher verbosity arguments will show more tree operations, e.g., change and swap, etc. Setting verb=2 will cause an echo of the tgp model parameters and their starting values; but is otherwise the same as verb=1. The max is verb=4 shows all successful tree operations. Here is an example grow statement.

The *GROW* statements indicate the depth of the split leaf node; the splitting dimension u and location v is shown between square brackets [u,v], followed by the size of the two new children n=(n1,n2). *PRUNE* is about the same, without printing n=(n1,n2).

Every 1000-rounds a progress indicator is printed. Its format depends on a number of things: (1) whether parallelization is turned on or not, (2) the

ALC: samples from Ds2x

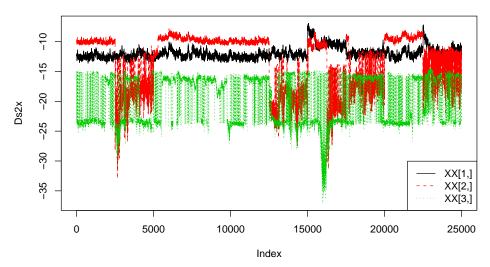


Figure 21: Traces of the (log of the) samples for the ALC statistic $\Delta \sigma^2(\tilde{\mathbf{x}})$ at for each of the three XX locations

correlation model [isotropic or separable], (3) whether jumps to the LLM are allowed. Here is an example with the 2-d exp data with parallel prediction under the separable correlation function:

```
(r,1)=(5000,104) d=[0.0144 0.0236] [1.047 0/0.626]; mh=2 n=(59,21)
```

The first part (r,1)=(5000,104) is indicating the MCMC round number r=5000 and the number of leaves waiting to be "consumed" for prediction by the parallel prediction thread. When parallelization is turned off (default), the print will simply be "r=5000".

The second part is a printing of the d–(range) parameter to a separable correlation function. For 2 partitions there are two sets of square brackets. Inside the square brackets is the m_X (2 in this case) range parameters for the separable correlation function. Whenever the LLM governs one of the input