

Homework # 6

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Parameters

```
clear;  
cp_0 = 0.5;  
crho = 0.5;  
sigma_u = 0.1;  
cdelta = 0.95;
```

Question 2

Take a look at `tauchen.m` in the repository, use it to generate a grid that approximates the process for p_t with 21 grid points

```
% Number of grid points for the price  
npgrid = 21;  
[prob, pgrid] = tauchen(npgrid, cp_0, crho, sigma_u);  
  
% Number of grid points for the stock of timber  
nxgrid = 201;  
  
% Grid for timber stock  
xgrid = linspace(0,100, nxgrid)';
```

Question 3

Solve the firm's problem using value function iteration. Plot the value of the firm depending on its initial stock (x-axis) and the current price of timber for $p \in \{0.9, 1, 1.1\}$.

```
% Value function iteration  
% Initial Value function matrix  
Vold = zeros(nxgrid, npgrid);  
  
% Store updated values here  
Vnew = zeros(nxgrid, npgrid);  
  
% Store policy indices here  
pol_index = zeros(nxgrid, npgrid);
```

```

% Amount Harvested
h = xgrid - xgrid';

% Value function iteration

for j = 1:npgrid
    values = period_profit(h, pgrid(j)) + ...
        cdelta*prob(j,:) * Vold';
    Vnew(:,j) = max(values, [], 2);
end

diff = norm(Vnew - Vold) / norm(Vnew);

tol = 0.00001;

iters = 0;
while diff > tol
    Vold = Vnew;
    for j = 1:npgrid
        values = period_profit(h, pgrid(j)) + ...
            cdelta*prob(j,:) * Vold';
        [Vnew(:,j), pol_index(:,j)] = max(values, [], 2);
    end

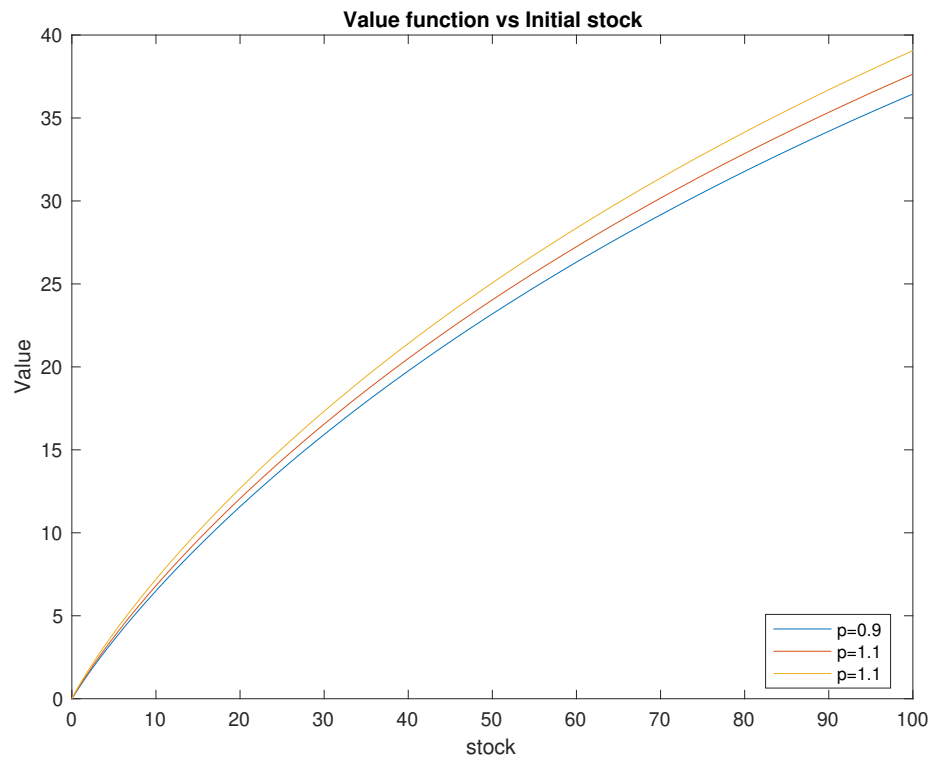
    diff = norm(Vnew - Vold) / norm(Vnew);
    iters = iters + 1;
end

policy = xgrid(pol_index);

% Plot the value of the firm
v0_9 = Vnew(:,8);
v1 = Vnew(:,11);
v1_1 = Vnew(:,14);

figure
plot(xgrid, v0_9, xgrid, v1, xgrid, v1_1)
title('Value function vs Initial stock')
xlabel('stock')
ylabel('Value')
legend({'p = 0.9', 'p = 1.1', 'p = 1.1'}, 'Location', ...
    'best')

```

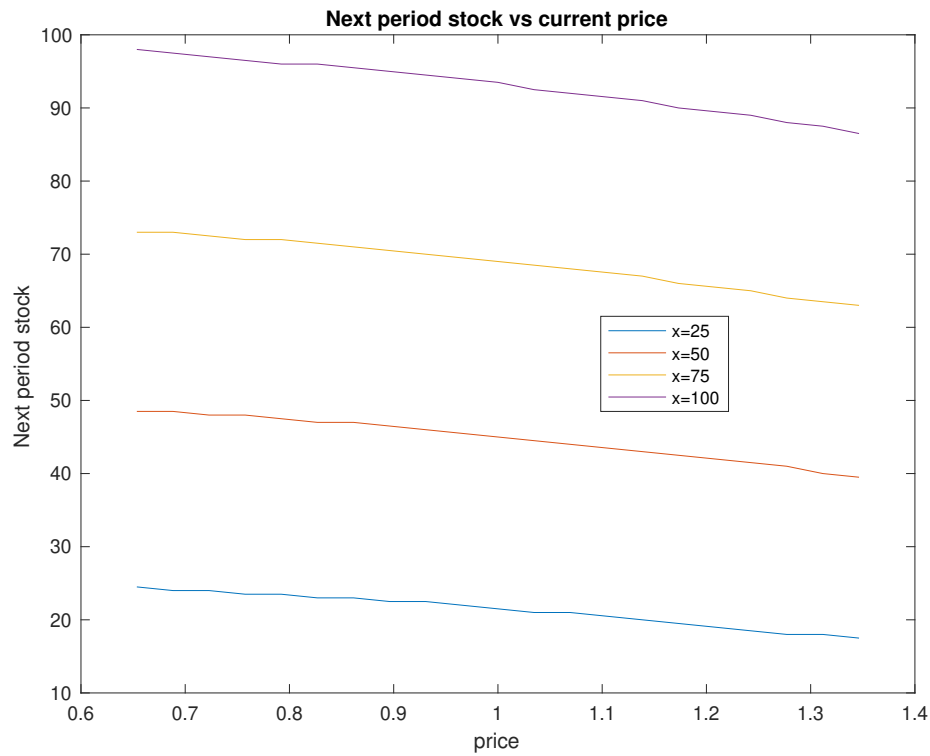


Question 4

Plot next period optimal stock (or harvest amount if you prefer) as a function of today's price for different amounts of lumber left in stock.

```
x25 = policy (51 ,:);
x50 = policy (101 ,:);
x75 = policy (151 ,:);
x100 = policy (201 ,:);

figure
plot(pgrid, x25, pgrid, x50, pgrid, x75, pgrid, x100);
title('Next period stock vs current price')
xlabel('price')
ylabel('Next period stock')
legend({'x = 25 ', 'x = 50 ', 'x = 75 ', 'x = 100 '}, ...
       'Location ', 'best')
```



Question 5

Assume firm starts with stock of 100 and today's price is 1. Plot expected stock over time for 20 periods ahead. Include the 90 percent confidence interval

```
P = zeros(nxgrid*npgrid, nxgrid*npgrid);

% Transition matrix for the states
for i = 1:npgrid
    for j = 1:npgrid
        P((i-1)*nxgrid + 1:i*nxgrid, ...
          (j-1)*nxgrid + 1:j*nxgrid) = prob(i,j)*(kron(ones(1,nxgrid), ...
            policy(:,i)) = kron(ones(nxgrid,1),xgrid')));
    end
end

% For the following periods ahead
nperiods = 20;

% Store distribution over states here
q = zeros(nperiods + 1, nxgrid*npgrid);
```

```

% Start at p=1, x=100
q(1,11*nxgrid) = 1;

for t = 1:nperiods
    q(t+1,:) = q(t,:)*P;
end

% Expected Values

% Store the marginal probability distributions of x
x__margdist = zeros(nperiods+1, nxgrid);

for t = 1:nperiods+1
    mat__q = reshape(q(t,:), [nxgrid, npgrid]);
    x__margdist(t,:) = sum(mat__q,2)';
end

% Expected values
mu__x = x__margdist*xgrid;

% Confidence interval
index = 1:nxgrid;

% Cumulative distributions
x__cumsum = cumsum(x__margdist,2);

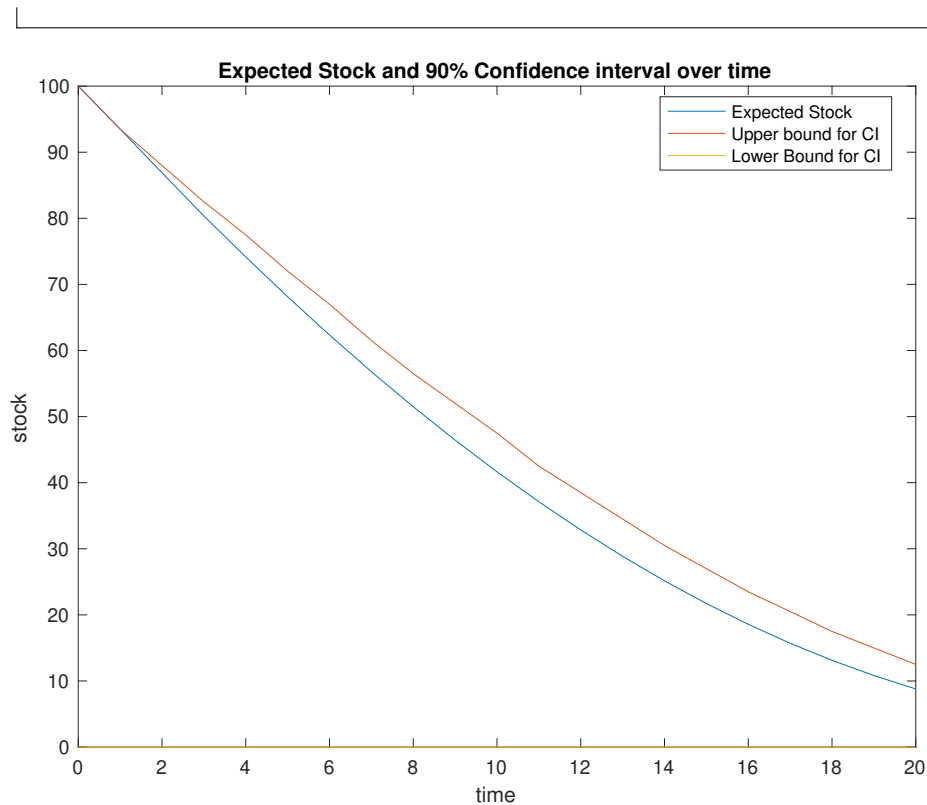
% Obtain 90th quantiles
indices90 = zeros(nperiods+1,1);
for t = 1:nperiods+1
    indices90(t,1) = min(index(x__cumsum(t,:) >= 0.8));
end
x90 = xgrid(indices90);

lb = zeros(nperiods+1,1);
time = 0:20;

plot(time, mu__x, time, x90, time, lb)

title('Expected Stock and 90% Confidence interval ...
      over time')
xlabel('time')
ylabel('stock')
legend({'Expected Stock', 'Upper bound for CI', ...
      'Lower Bound for CI'}, 'Location', 'best')

```



Question 6.

Redo 2-4 for the coarse grid of 5 points in Tauchen's representation

Question 6.2. Take a look at tauchen.m in the repository, use it to generate a grid that approximates the process for p_t with 5 grid points

```
% Number of grid points for the price
npgrid = 5;
[prob, pgrid, invdist] = tauchen(npgrid, cp_0, crho, ...
    sigma_u);

% Number of grid points for the stock of timber
nxgrid = 201;

% Grid for timber stock
xgrid = linspace(0,100, nxgrid)';
```

Question 6.3

Solve the firm's problem using value function iteration. Plot the value of the firm depending on its initial stock (x-axis) and the current price of timber for $p \in \{0.9, 1, 1.1\}$.

```
% Value function iteration
% Initial Value function matrix
Vold = zeros(nxgrid, npgrid);

% Store updated values here
Vnew = zeros(nxgrid, npgrid);

% Store policy indices here
pol_index = zeros(nxgrid, npgrid);

% Amount Harvested
h = xgrid - xgrid';

% Value function iteration
for j = 1:npgrid
    values = period_profit(h, pgrid(j)) + ...
        cdelta*prob(j,:) * Vold';
    Vnew(:, j) = max(values, [], 2);
end

diff = norm(Vnew - Vold) / norm(Vnew);

tol = 0.00001;

iters = 0;
while diff > tol
    Vold = Vnew;
    for j = 1:npgrid
        values = period_profit(h, pgrid(j)) + ...
            cdelta*prob(j,:) * Vold';
        [Vnew(:, j), pol_index(:, j)] = max(values, [], 2);
    end

    diff = norm(Vnew - Vold) / norm(Vnew);
    iters = iters + 1;
end

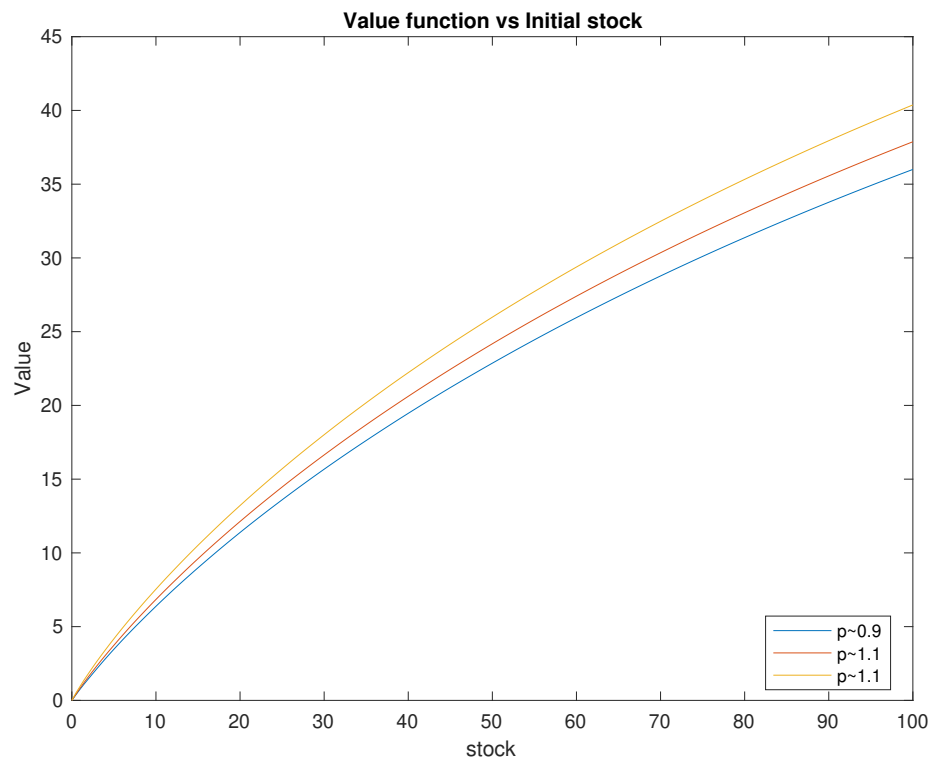
policy = xgrid(pol_index);
```

```

% Plot the value of the firm
v0_9 = Vnew(:,2);
v1 = Vnew(:,3);
v1_1 = Vnew(:,4);

figure
plot(xgrid, v0_9, xgrid, v1, xgrid, v1_1)
title('Value function vs Initial stock')
xlabel('stock')
ylabel('Value')
legend({'p~0.9', 'p~1.1', 'p~1.1'}, 'Location', 'best')

```



Question 6.4

Plot next period optimal stock (or harvest amount if you prefer) as a function of today's price for different amounts of lumber left in stock.

```

x25 = policy(51,:);
x50 = policy(101,:);
x75 = policy(151,:);

```



```

x100 = policy (201,:);

figure
plot(pgrid, x25, pgrid, x50, pgrid, x75, pgrid, x100);
title('Next period stock vs current price')
xlabel('price')
ylabel('Next period stock')
legend({'x = 25 ', 'x = 50 ', 'x = 75 ', 'x = 100 '}, ...
       'Location ', 'best ')

```

